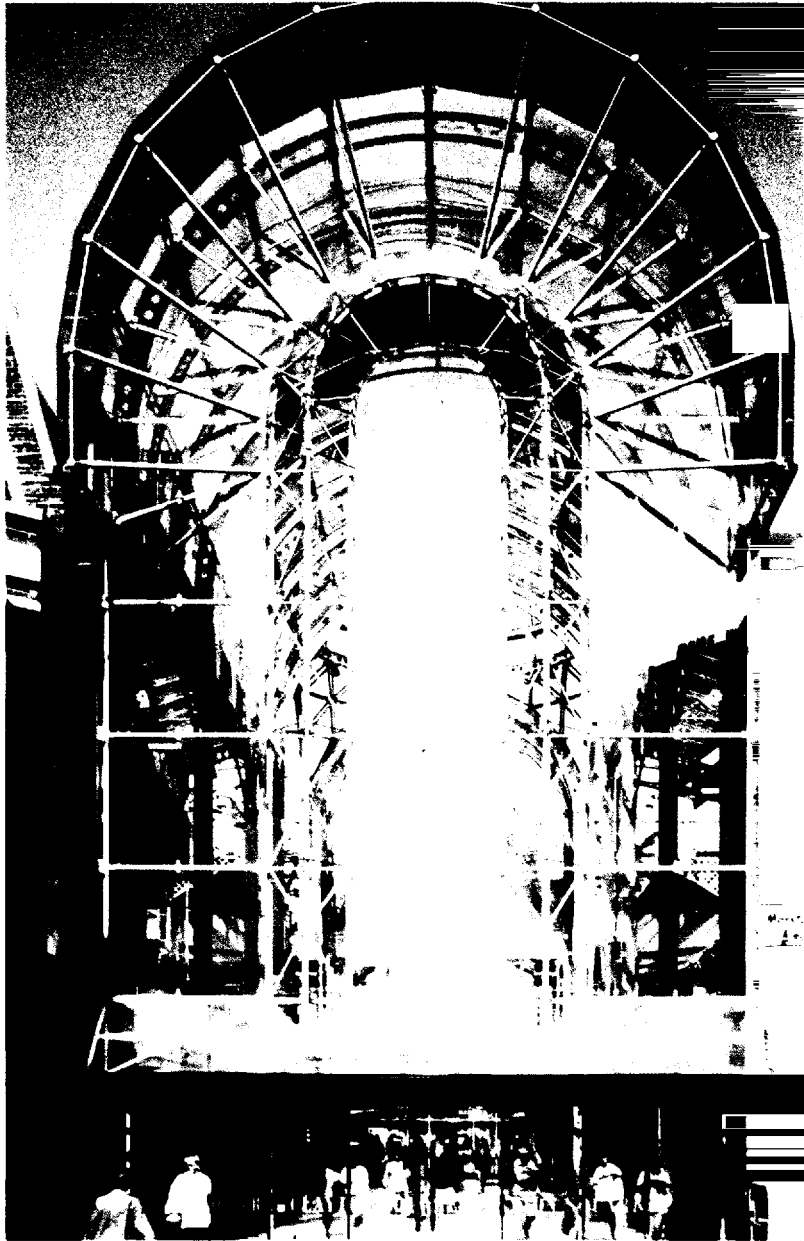


# Steel Designers' Manual



The Steel  
Construction  
Institute

Editors: Graham W. Owens  
and Peter R. Knowles



*b*

Blackwell  
Science

Fifth edition

# Steel Designers' Manual

# STEEL DESIGNERS' MANUAL

FIFTH EDITION

**The Steel Construction Institute**

Edited by

**Graham W. Owens**

*Director, The Steel Construction Institute*

and the late

**Peter R. Knowles**

*Consultant Engineer, Peter Knowles & Associates*

with the assistance of an Advisory Committee, chaired by

**Patrick J. Dowling**

*British Steel Professor of Steel Structures and Head of Civil Engineering  
Department, Imperial College, London*

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**Blackwell  
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# Foreword to fifth edition

At the instigation of the Iron and Steel Federation, the late Bernard Godfrey began work in 1952 on the first edition of the *Steel Designers' Manual*. As principal author he worked on the manuscript almost continually for a period of two years. On many Friday evenings he would meet with his co-authors, Charles Gray, Lewis Kent and W.E. Mitchell to review progress and resolve outstanding technical problems. A remarkable book emerged. Within approximately 900 pages it was possible for the steel designer to find everything necessary to carry out the detailed design of most conventional steelwork. Although not intended as an analytical treatise, the book contained the best summary of methods of analysis then available. The standard solutions, influence lines and formulae for frames could be used by the ingenious designer to disentangle the analysis of the most complex structure. Information on element design was intermingled with guidance on the design of both overall structures and connections. It was a book to dip into rather than read from cover to cover. However well one thought one knew its contents, it was amazing how often a further reading would give some useful insight into current problems. Readers forgave its idiosyncrasies, especially in the order of presentation. How could anyone justify slipping a detailed treatment of angle struts between a very general discussion of space frames and an overall presentation on engineering workshop design?

The book was very popular. It ran to four editions with numerous reprints in both hard and soft covers. Special versions were also produced for overseas markets. Each edition was updated by the introduction of new material from a variety of sources. However, the book gradually lost the coherence of its original authorship and it became clear in the 1980s that a more radical revision was required.

After thirty-six very successful years it was decided to rewrite and re-order the book, while retaining its special character. This decision coincided with the formation of the Steel Construction Institute and it was given the task of co-ordinating this activity. An Advisory Committee was established comprising:

|                    |  |
|--------------------|--|
| Patrick J. Dowling | Imperial College of Science, Technology & Medicine<br>(Chairman) |
| David Dibb-Fuller  | Gifford & Partners, previously Conder Southern                   |
| Alan Hart          | Ove Arup & Partners  |
| Alan Hayward       | Cass Hayward & Partners  |

|               |  |
|---------------|--|
| Peter Knowles | (Editor)                               |
| Jim Mathys    | H.L. Watermans                         |
| Roger Pope    | Blight & White Ltd                     |
| Graham Owens  | Steel Construction Institute (Editor). |

The committee endorsed a complete restructuring of the book, with more material on overall design and a new section on construction. The analytical material was condensed because it is now widely available elsewhere, but all the design data were retained in order to maintain the practical usefulness of the book as a day-to-day design manual. Earlier editions had been based on allowable stress design concepts (in accordance with the relevant codes BS 449 and BS 153). This edition is the first to be entirely based on limit state design concepts. It gives relevant background to BS 5950 for buildings and BS 5400 for bridges. Design examples are to the more appropriate of these two codes for each particular application. Thirty authors were commissioned to produce individual chapters and Peter Knowles was commissioned to carry out detailed editorial work.

As principal editor, I would like to pay tribute to all those who have made this fifth edition possible; the Advisory Committee for the direction that they provided at the outset, the authors who gave so freely of their time and were patient with the editorial process as the book was welded into a coherent whole, and the staff at the Institute, particularly Ip-Luew Lee, Derek Mullett and David Waters, who have worked so hard on the design data and the worked examples. Finally, I would like to pay tribute to the invaluable contribution from Peter Knowles. Sadly, Peter died in late 1991, having completed a meticulous piece of editing, but without seeing the final results of his and our labours.

By kind permission of the British Standards Institution, references are made to British Standards throughout the manual. The tables of fabrication and erection tolerances in Chapter 31 are taken from the *National Structural Steelwork Specification*, second edition. Much of the text and illustrations for Chapter 33 are taken from *Steelwork Erection* by Harry Arch. Both these sources are used by kind permission of the British Constructional Steelwork Association, the publishers. These permissions are gratefully acknowledged.

Graham Owens

Further information on the SCI is given in a prospectus available free on request from: The Membership Secretary, The Steel Construction Institute, Silwood Park, Ascot, Berkshire SL5 7QN.  
Telephone: 01344 623345, Fax: 01344 622944.

# Introduction to fifth edition

It is just over one hundred years since steel was first used in the construction of a major bridge, Britain's Forth Railway Bridge, and the first all steel building, the Second Rand McNally Building in Chicago. Since then it has demonstrated its versatility in almost the full range of structural applications.

The recent renaissance in steel construction which has been centred on the United Kingdom has benefited greatly from the many improvements made in the various aspects of steel technology, the advances in steel fabrication techniques, the improved understanding of structural behaviour, and the upgrading in the standard of structural steel design, as well as the wide dissemination of excellent material on which the training of the users of structural steel can be based.

The manufacture of the raw material has improved in a number of significant ways:

- Basic oxygen steel-making and continuous casting produce a fine-grained weldable material with consistent strength and toughness.
- Modern rolling mills manufacture a wide range of shapes of close tolerance, good surface finish and consistent, homogeneous composition.
- Heat treatments during production permit greater control and enhancement of mechanical properties.

The range of commercially available structural steels has been widened. The higher yield strength steels are attractive because they can show economies in design. In appropriate atmospheric conditions it is possible to leave weather-resistant steels unpainted throughout the life of a structure. Stainless steels are produced in a wide range of compositions. In the thinner gauge products, coatings can be applied to produce attractive, corrosion-resistant cladding and roofing sheeting. And thin gauge strip material produced by cold rolling can be shaped into a variety of cold-formed sections.

The fabrication of structural steelwork has also shown significant increases in quality in recent years. The production of fabricated steelwork is now very much a manufacturing operation with the emphasis on accurate cutting, shaping, drilling and welding of components on a production line which makes considerable use of numerically-controlled machine tools. Substantial use has been made of automation in a range of pre-engineered building systems now available. Protective anti-

corrosion treatment has been much improved by the introduction of automatic shot blasting and painting plants.

Design, aided by research, has become more refined with the result that designers are able, with confidence, to propose structures which make more economical use of steel. Many design improvements have been incorporated in Codes of Practice, such as the new Eurocodes which draw together the best information available not only throughout the European Community, but also worldwide.

Steel structures have always had the advantages of lightness, stiffness and strength and lend themselves to rapid construction compared to other construction materials. Developments which have made steel even more competitive in the building field include the use of metal deck as permanent shuttering to concrete slabs, composite steel and concrete construction and lightweight fire protection. Many of these design improvements have had the effect of further facilitating speedy construction. Steel also comes into its own in refurbishment of existing buildings because of its flexibility. The application of steel to long-span bridges is, of course, well established, but its advantages for short- to medium-span bridges are becoming more and more obvious to bridge engineers as is the application of steel to motorway bridge widening and upgrading schemes.

Developments in structural steel are still possible, a century after the first use of the material. Some of the possible areas of improvement include:

- Developments in steel production technology which will lead to higher strength steels becoming available at a competitive price.
- An increasingly large range of both hot- and cold-rolled products to permit greater flexibility in design.
- Greater use of the tensile strength of steel in cable structures.
- Improvements in fire engineering and corrosion-resistant steel, giving the material greater opportunity for expansion.
- An increasing use of computers leading to greater refinement of design to reduce fabrication and construction costs.
- Greater emphasis on prefabrication to reduce the amount of site work.
- Greater use of standard connections.
- A more sophisticated use of composite construction over a wide range of applications.

The authors of each chapter have been chosen on the basis of their known expertise in the area and present the best relevant information likely to be useful to the modern structural steelwork designer. By putting this knowledge at the disposal of the reader they hope to share with them some of the excitement and satisfaction they have had in designing much of Britain's new evolving infrastructure using that most versatile of building materials, steel.

## Scope

The *Steel Designers' Manual* is aimed at designers of structural steelwork of all kinds. It is divided into seven main sections:

- Design synthesis
- Steel technology
- Design theory
- Element design
- Connection design
- Other elements
- Construction.

### **Design synthesis: Chapters 1–5**

A description of the nature of the process by which design solutions are arrived at for a wide range of steel structures including:

- Single- and multi-storey buildings (Chapters 1 and 2)
- Heavy industrial frames (Chapter 3)
- Bridges (Chapter 4)
- Other diverse structures such as space frames, cable structures, towers and masts, atria and steel in housing (Chapter 5).

### **Steel technology: Chapters 6–8**

Background material sufficient to inform designers of the important problems inherent in the production and use of steel and methods of overcoming them in practical design.

- Applied metallurgy (Chapter 6)
- Fatigue (Chapter 7)
- Brittle fracture (Chapter 8).

### **Design theory: Chapters 9–12**

A résumé of analytical methods for determining the forces and moments in structures subject to static or dynamic loads, both manual and computer-based. Comprehensive tables for a wide variety of beams and frames are given in the Appendix.

- Manual and computer analysis (Chapter 9)
- Beam analysis (Chapter 10)
- Frame analysis (Chapter 11)
- Applicable dynamics (Chapter 12).

### **Element design: Chapters 13–22**

A comprehensive treatment of the design of steel elements, singly, in combination or acting compositely with concrete.

- Local buckling and cross-section classification (Chapter 13)

- Tension members (Chapter 14)
- Columns and struts (Chapter 15)
- Beams (Chapter 16)
- Plate girders (Chapter 17)
- Members with compression and moments (Chapter 18)
- Trusses (Chapter 19)
- Composite floors (Chapter 20)
- Composite beams (Chapter 21)
- Composite columns (Chapter 22).

### **Connection design: Chapters 23–27**

The general basis of design of connections is surveyed and amplified by consideration of specific connection methods.

- Bolts (Chapter 23)
- Welds (Chapter 24)
- Plate and stiffener elements (Chapter 25)
- Design of connections (Chapter 26)
- Foundations and holding-down systems (Chapter 27).

### **Other elements: Chapters 28–30**

- Bearings and joints (Chapter 28)
- Piles (Chapter 29)
- Floors and orthotropic decks (Chapter 30).

### **Construction: Chapters 31–35**

Important aspects of steel construction about which a designer must be informed if he is to produce structures which can be economically fabricated and erected and which will have a long and safe life.

- Tolerances (Chapter 31)
- Fabrication (Chapter 32)
- Erection (Chapter 33)
- Fire protection and fire engineering (Chapter 34)
- Corrosion resistance (Chapter 35).

### **Appendix**

A comprehensive collection of data of direct use to the practising designer.

Patrick Dowling



---

# Contributors

## **Harry Arch**

Harry Arch graduated from Manchester Faculty of Technology. For many years he worked for Sir William Arrol, where he became a director, responsible for all outside construction activities including major bridges, power stations and steel-works construction. In 1970 he joined Redpath Dorman Long International, working on offshore developments. Now retired, he is still widely in demand as a lecturer on fabrication and erection.

## **Hubert Barber**

Hubert Barber joined Redpath Brown in 1948 and for five years gained a wide experience in steel construction. The remainder of his working life was spent in local government, first at Manchester and then in Yorkshire where he became Chief Structural Engineer of West Yorkshire. He also lectured part-time for fourteen years at the University of Bradford.

## **Michael Burdekin**

Michael Burdekin graduated from Cambridge University in 1959. After fifteen years of industrial research and design experience he went to UMIST, where he is now Professor of Civil and Structural Engineering. His specific expertise is the field of welded steel structures, particularly in the application of fracture mechanics to fracture and fatigue failure.

## **Brian Cheal**

Brian Cheal graduated from Brighton Technical College in 1951 with an External Degree of the University of London. He was employed with W.S. Atkins and

Partners from 1951 to 1986, becoming a Technical Director in 1979, and specialized in the analysis and design of steel-framed structures, including heavy structural framing for power stations and steelworks. He has written design guides and given lectures on various aspects of connection design and is co-author of *Structural Steelwork Connections*.

### **David Dibb-Fuller**

David Dibb-Fuller started his career with the Cleveland Bridge and Engineering Company in London. His early bridge related work gave a strong emphasis to heavy fabrication; in later years he moved on to building structures. As Technical Director for Conder Southern in Winchester his strategy was to develop close links between design for strength and design for production. Currently he is a partner with Gifford and Partners in Southampton where he continues to exercise his skills in the design of steel structures.

### **Patrick Dowling**

Patrick Dowling graduated from University College Dublin in 1960. After post-graduate training and four years at BCSA, he joined the Civil Engineering Department of Imperial College in 1968 where he is now British Steel Professor of Steel Structures and Head of Department. The author of 175 papers and editor of three books, his numerous outside activities include the chairmanship of the Eurocode Committee on Design of Steel Structures.

### **Ian Duncan**

Ian Duncan joined the London office of Ove Arup and Partners in 1966 after graduating from Surrey University. From 1975 he taught for four years at University College Cardiff before joining Buro Happold. He now runs his own practice in Bristol.

### **Michael Green**

Michael Green graduated from Liverpool University in 1971. After an early career in general civil engineering, he joined Buro Happold, where he is now an executive partner. He has worked on a wide variety of building projects, developing a specialist expertise in atria and large-span structures.

**Alan Hart**

Alan Hart graduated from the University of Newcastle-upon-Tyne in 1968 and joined Ove Arup and Partners. During his career he has been involved in the design of a number of major award-winning buildings, including Carlsberg Brewery, Northampton; Cummins Engine Plant, Shotts, Lanarkshire; the Hongkong and Shanghai Bank, Hong Kong. He is a project director of Ove Arup and Partners.

**Alan Hayward**

Alan Hayward is a partner of Cass Hayward and Partners, specialist structural steel consultants, who design and devise the erection methodology for all kinds of steel bridges, many built on a design:construct basis. Projects include London Docklands Light Railway viaducts, the M25/M4 and M25/A1(M) interchanges, the Festival Way Flyover (Stoke-on-Trent) and a number of roll-on/roll-off berthing structures. He is a former Chief Examiner for the Institution of Structural Engineers and chairman of the Wales branch. He became a visiting professor at the Polytechnic of Central London in 1991.

**Eric Hindhaugh**

Eric Hindhaugh trained as a structural engineer in design and constructional steel work, timber and lightweight roll-formed sections. He then branched into promotional and marketing activities. Most recently he has been a Market Development Manager in Construction for British Steel Strip Products, where he has been involved in Colorcoat and the widening use of lightweight steel sections for structural steel products.

**Ken Johnson**

Ken Johnson is head of corrosion and coatings at British Steel's Swinden Laboratories. His early experience was in the paint industry but he has since worked in steel for over twenty-five years, dealing with the corrosion and protection aspects of the whole range of British Steel's products, including plates, section, piling, strip products, tubes, stainless steels, etc. He represents the steel industry on several BSI and European Committees and is a Council member of the Paint Research Association.

**Mark Lawson**

A graduate of Imperial College, and the University of Salford, where he worked in the field of cold-formed steel, Mark Lawson spent his early career at Ove Arup and Partners and the Construction Industry Research and Information Association. In 1987 he joined the newly formed Steel Construction Institute as Research Manager for steel in buildings, with particular reference to composite construction, fire engineering and cold-formed steel. He is a member of the Eurocode 4 project team on fire-resistant design.

**Ian Liddell**

After leaving Cambridge, Ian Liddell joined Ove Arup and Partners to work on the roof of the Sydney Opera House and on the South Bank Art Centre. His early career encompassed a wide range of projects, with particular emphasis on shell structures and lightweight tension and fabric structures. Since 1976 he has been a partner of Buro Happold and has been responsible for a wide range of projects, many with special structural engineering features, including mosques, auditoriums, mobile and temporary structures, stadiums and retail atria.

**Stephen Matthews**

Stephen Matthews graduated from the University of Nottingham in 1974 and completed postgraduate studies at Imperial College in 1976–7. His early professional experience was gained with Rendel Palmer and Tritton in their structural steelwork design office, and on the Thames Barrier site. During subsequent employment with Fairfield Mabey and Cass Hayward and Partners, he worked on the design of several large composite bridges including the Tweed Bridge, Berwick; Simon De Montfort Bridge, Evesham; and viaducts on the Island Gardens Branch of the Docklands Light Railway. He is currently associate director of the Structures Division of Frank Graham Consulting Engineers.

**Rangachari Narayanan**

Rangachari Narayanan graduated in civil engineering from Annamalai University (India) in 1951. In a varied professional career spanning over forty years, he has held senior academic positions at the Universities of Delhi, Manchester and Cardiff. He is the recipient of several awards including the Benjamin Baker Gold Medal and George Stephenson Gold Medal, both from the Institution of Civil

Engineers. Currently he heads the Education and Publication Divisions at the Steel Construction Institute.

### **David Nethercot**

Since graduating from the University of Wales, Cardiff, David Nethercot has completed twenty-five years of teaching, research and specialist advisory work in the area of structural steelwork. The author of over 100 technical papers, he has lectured frequently on post-experience courses, he is vice-chairman of the BSI Committee responsible for BS 5950 and is a frequent contributor to technical initiatives associated with the structural steelwork industry. Since 1989 he has been professor of civil engineering at the University of Nottingham.

### **Gerard Parke**

Gerry Parke is a lecturer in structural engineering at the University of Surrey specializing in the analysis and design of steel structures. His particular interests lie in assessing the collapse behaviour of both steel industrial buildings and large-span steel space structures.

### **Alan Pottage**

Alan Pottage graduated from the University of Newcastle-upon-Tyne in 1976 and gained a Masters degree in structural steel design from Imperial College in 1984. He has gained experience in all forms of steel construction, particularly portal frame and multi-rise structures, and has contributed to various code committees, and SCI guides on composite design and connections. He is presently employed as Technical Director at J.N. Rowen Ltd.

### **Graham Raven**

Graham Raven graduated from King's College, London in 1963 and joined Ove Arup and Partners. After thirteen years with consulting engineers he joined a software house pioneering work in structural steelwork design and detailing systems. This experience took him to Ward Building Systems Ltd where, in addition to design responsibilities, he was closely associated with the development of cold-formed cladding and rail systems and the increased use of welded sections for

portals and composite beams in commercial buildings. He has recently joined the Steel Construction Institute's staff as Manager of Construction.

### **John Righiniotis**

John Righiniotis graduated from the University of Thessalonika in 1987 and obtained an MSc in structural steel design from Imperial College in 1988. He worked at the Steel Construction Institute on a wide range of projects until June 1990 when he was required to return to Greece to carry out his military service.

### **John Roberts**

John Roberts graduated from the University of Sheffield in 1969 and was awarded a PhD there in 1972 for research on the impact loading of steel structures. His professional career has included working on site for Alfred McAlpine. In 1981 he joined Allott and Lomax, consulting engineers, becoming director in charge of structural engineering in 1985. He has been involved with many major industrial projects, including power stations. He serves as a member of council of the Institution of Structural Engineers and represents the Association of Consulting Engineers on the Constructional Steelwork QA scheme.

### **Jef Robinson**

Jef Robinson graduated in metallurgy from Durham University in 1962 where he undertook a research project into high temperature material behaviour for the NASA space programme. His early career in the steel industry included designing high-strength notch-tough steels for super-tankers, North Sea drilling platforms and large bridges. Currently the Market Development Manager for the structural sections division of British Steel he chaired the BSI Committee which formulated BS 5950: Part 8 *Fire-resistant design* for structural steelwork.

### **Robert Simpson**

Robert Simpson graduated from the University of Surrey in 1974. In 1977 he obtained an MSc in offshore engineering from Cranfield Institute of Technology and undertook research into weldability of offshore steels. He spent four years with the Steel Construction Institute and more recently moved to the Health and Safety Executive as research manager.

**Dick Stainsby**

Dick Stainsby was for many years chief designer with Redpath Dorman Long, Middlesbrough, and previously Dorman Long and Co, dealing with 'design & build' contracts for which that company was famous. He is now Managing Director of Cleveland Technical Services, engaged in the design and detailing of steel structures particularly using computer techniques. He is author of the *National Steelwork Specification for Building Structures*, and is currently compiling *Joints in Simple Structures – Practical Applications*.

**Paul Tasou**

Paul Tasou graduated from Queen Mary College, London in 1978 and subsequently obtained an MSc in structural steel design from Imperial College, London. He spent eleven years at Rendel Palmer and Tritton working on a wide range of bridge, building and civil engineering projects. He is now principal partner in Tasou Associates.

**Colin Taylor**

Colin Taylor graduated from Cambridge in 1959. He started his professional career in steel fabrication, initially in the West Midlands and subsequently in South India. After eleven years he moved into consultancy where, besides practical design, he became involved with graduate training, the use of computers for design and drafting, company technical standards and drafting work for British Standards and for Eurocodes as editorial secretary for Eurocode 3. Moving to the Steel Construction Institute on its formation as manager of the Codes and Advisory Division, he also became involved with the European standard for steel fabrication and erection *Execution of Steel Structures*.

**John Tyrrell**

John Tyrrell graduated from Aston University in 1965 and immediately joined Ove Arup and Partners. He has worked for them on a variety of projects in the UK, Australia and West Africa; he is now a Project Director. He has been responsible for the design of a wide range of towers and guyed masts. He currently leads the Industrial Structures Group covering diverse fields of engineering from telecommunications and broadcasting to the power industry.

### **Dennis Waite**

Dennis Waite has spent thirty-nine years in the steel industry, involved initially in the design of structural steelwork and later in the design of steel piled structures. In 1985, he became an independent consulting engineer specializing in foundations and earth retaining structures. He is a member of BSI code drafting committee CSB/2, *Code of Practice for Earth Retaining Structures* and CSB/17, *Code of Practice for Maritime Structures*. He is chairman of the Institution of Civil Engineers' Piling Panel.

### **Peter Wickens**

Having graduated from Nottingham University in 1971, Peter Wickens spent much of his early career in civil engineering, designing bridges and Metro stations. In 1980, he changed to the building structures field and was Project Engineer for the Billingsgate Development, one of the first of the new generation of steel composite buildings. He is currently manager of the Structural Division and Head of Discipline for Building Structures at Mott MacDonald.

### **Michael Willford**

Michael Willford graduated from Cambridge in 1975. He has worked with Ove Arup and Partners since graduation, becoming a Technical Director in 1986. Between 1980 and 1983 he played a major role in the design of the Hongkong and Shanghai Bank Building, Hong Kong. Recently he has been associated with many major building and industrial structures, specializing in design for dynamic and environmental loads.



# Notation

Several different notations are adopted in steel design; different specializations frequently give different meanings to the same symbol. These differences have been maintained in this book. To do otherwise would be to separate this text both from other literature on a particular subject and from common practice. The principal definitions for symbols are given below. For conciseness, only the most commonly adopted subscripts are given; others are defined adjacent to their usage.

|              |  |
|--------------|--|
| $A$          | Area   |
|              | or End area of pile  |
|              | or Constant in fatigue equations   |
| $A_e$        | Effective area   |
| $A_g$        | Gross area   |
| $A_s$        | Shear area of a bolt   |
| $A_t$        | Tensile stress area of a bolt  |
| $A_v$        | Shear area of a section  |
| $a$          | Spacing of transverse stiffeners   |
|              | or Effective throat size of weld   |
|              | or Crack depth   |
|              | or Distance from central line of bolt to edge of plate   |
|              | or Shaft area of pile  |
| $B$          | Breadth  |
| $\mathbf{B}$ | Transformation matrix  |
| $b$          | Outstand   |
|              | or Width of panel  |
|              | or Distance from centreline of bolt to toe of fillet weld or to half of root radius as appropriate |
| $b_e$        | Effective breadth or effective width   |
| $b_1$        | Stiff bearing length   |
| $C$          | Crack growth constant  |
| $\mathbf{C}$ | Transformation matrix  |
| $C_v$        | Charpy impact value  |
| $C_y$        | Damping coefficient  |
| $c$          | Bolt cross-centres   |
|              | or Cohesion of clay soils  |

|              |   |
|--------------|---|
| $D$          | Depth of section<br>Diameter of section or hole                               |
| $\mathbf{D}$ | Elasticity matrix   |
| $D_r$        | Profile height for metal deck   |
| $D_s$        | Slab depth  |
| $d$          | Depth of web<br>or Nominal diameter of fastener<br>or Depth                   |
| $d_c$        | Effective depth of slab   |
| $E$          | Modulus of elasticity of steel (Young's modulus)                              |
| $e$          | End distance  |
| $e_y$        | Material yield strain   |
| $F_c$        | Compressive force due to axial load   |
| $F_s$        | Shear force (bolts)   |
| $F_t$        | Tensile force   |
| $F_v$        | Shear force (sections)  |
| $f$          | Flexibility coefficient   |
| $f_a$        | Longitudinal stress in flange   |
| $f_c$        | Compressive stress due to axial load  |
| $f_{cu}$     | Cube strength of concrete   |
| $f_m$        | Force per unit length on weld group from moment                               |
| $f_r$        | Resultant force per unit length on weld group from applied<br>concentric load |
| $f_v$        | Force per unit length on weld group from shear<br>or Shear stress             |
| $G$          | Shear modulus of steel  |
| $g$          | Gravitational acceleration  |
| $H$          | Warping constant of section<br>or Horizontal reaction                         |
| $h$          | Height<br>or Stud height<br>or Depth of overburden                            |
| $I_o$        | Polar second moment of area of bolt group                                     |
| $I_{oo}$     | Polar second moment of area of weld group of unit throat about<br>polar axis  |
| $I_x$        | Second moment of area about major axis  |
| $I_{xx}$     | Polar second moment of area of weld group of unit throat about $xx$<br>axis   |
| $I_y$        | Second moment of area about minor axis  |
| $I_{yy}$     | Polar second moment of area of weld group of unit throat about $yy$<br>axis   |
| $K$          | Degree of shear connection<br>or Stiffness                                    |
| $\mathbf{K}$ | Stiffness matrix  |

|                                  |  |
|----------------------------------|--|
| $K_s$                            | Curvature of composite section from shrinkage  |
| or                               | Constant in determining slip resistance of HSFG bolts                                      |
| $K_1, K_2, K_3$                  | Empirical constants defining the strength of composite columns                             |
| $k_a$                            | Coefficient of active pressure   |
| $k_d$                            | Empirical constant in composite slab design  |
| $k_p$                            | Coefficient of passive resistance  |
| $L$                              | Length of span or cable  |
| $L_y$                            | Shear span length of composite slab  |
| $M$                              | Moment   |
| or                               | Larger end moment  |
| $M_{ax}, M_{ay}$                 | Maximum buckling moment about major or minor axis in presence of axial load                |
| $M_b$                            | Buckling resistance moment (lateral-torsional)   |
| $M_E$                            | Elastic critical moment  |
| $M_o$                            | Mid-length moment on a simply-supported span equal to unrestrained length                  |
| $M_{pc}$                         | Plastic moment capacity of composite section   |
| $M_{rx}, M_{ry}$                 | Reduced moment capacity of section about major or minor axis in the presence of axial load |
| $M_x, M_y$                       | Applied moment about major or minor axis   |
| $\overline{M}_x, \overline{M}_y$ | Equivalent uniform moment about major or minor axis  |
| $M_1, M_2$                       | End moments for a span of a continuous composite beam                                      |
| $m$                              | Equivalent uniform moment factor   |
| or                               | Empirical constant in fatigue equation   |
| or                               | Number of vertical rows of bolts   |
| $m_d$                            | Empirical constant in composite slab design  |
| $N$                              | Number of cycles to failure  |
| $N_c, N_q, N_\gamma$             | Constants in Terzaghi's equation for the bearing resistance of clay soils                  |
| $n$                              | Slenderness correction factor  |
| or                               | Crack growth constant  |
| or                               | Number of shear studs per trough in metal deck   |
| or                               | Number of horizontal rows of bolts   |
| or                               | Distance from bolt centreline to plate edge  |
| $P$                              | Force in structural analysis   |
| or                               | Load per unit surface area on cable net  |
| or                               | Crushing resistance of web   |
| $P_{bb}$                         | Bearing capacity of a bolt   |
| $P_{bg}$                         | Bearing capacity of parts connected by friction-grip fasteners                             |
| $P_{bs}$                         | Bearing capacity of parts connected by ordinary bolts                                      |
| $P_c$                            | Compression resistance   |
| $P_{cx}, P_{cy}$                 | Compression resistance considering buckling about major or minor axis only                 |
| $P_o$                            | Minimum shank tension for preloaded bolt   |
| $P_s$                            | Shear capacity of a bolt   |

|            |  |
|------------|--|
| $P_{sL}$   | Slip resistance provided by a friction-grip fastener   |
| $P_t$      | Tension capacity of a member or fastener   |
| $P_u$      | Compressive strength of stocky composite column  |
| $P_v$      | Shear capacity of a section  |
| $p$        | Ratio of cross-sectional area of profile to that of concrete in a composite slab   |
| $p_b$      | Bending strength   |
| $p_{bb}$   | Bearing strength of a bolt   |
| $p_{bg}$   | Bearing strength of parts connected by friction-grip fasteners   |
| $p_{bs}$   | Bearing strength of parts connected by ordinary bolts  |
| $p_c$      | Compressive strength   |
| $p_E$      | Euler strength   |
| $p_o$      | Minimum proof stress of a bolt   |
| $p_s$      | Shear strength of a bolt   |
| $p_t$      | Tension strength of a bolt   |
| $p_w$      | Design strength of a fillet weld   |
| $p_y$      | Design strength of steel   |
| $Q$        | Prying force   |
| $q$        | Ultimate bearing capacity  |
| $q_b$      | Basic shear strength of a web panel  |
| $q_{cr}$   | Critical shear strength of a web panel   |
| $q_e$      | Elastic critical shear strength of a web panel   |
| $q_f$      | Flange-dependent shear strength factor   |
| $R$        | Reaction   |
|            | or Load applied to bolt group  |
|            | or Radius of curvature   |
| $R_c$      | Compressive capacity of concrete section in composite construction   |
| $R_q$      | Capacity of shear connectors between point of contraflexure and point of maximum negative moment in composite construction |
| $R_r$      | Tensile capacity in reinforcement in composite construction  |
| $R_s$      | Tensile capacity in steel section in composite construction  |
| $R_w$      | Compression in web section in composite construction   |
| $r$        | Root radius in rolled section  |
| $r_r$      | Reduction factor in composite construction   |
| $r_x, r_y$ | Radius of gyration of a member about its major or minor axis   |
| $S$        | Span of cable  |
| $S_R$      | Applied stress range   |
| $S_x, S_y$ | Plastic modulus about major or minor axis  |
| $s$        | Spacing  |
|            | or Leg length of a fillet weld   |
| $T$        | Thickness of a flange or leg   |
|            | or Tension in cable  |
| $t$        | Thickness of web   |
| $U$        | Elastic energy   |
| $U_s$      | Specified minimum ultimate tensile strength of steel   |
| $u$        | Buckling parameter of the section  |

|               |  |
|---------------|--|
| $V$           | Shear force  |
| or            | Shear resistance per unit length of beam in composite construction   |
| $V_b$         | Shear buckling resistance of stiffened web utilizing tension field action  |
| $V_{cr}$      | Shear buckling resistance of stiffened or unstiffened web without utilizing tension field action                           |
| $\nu$         | Slenderness factor for beam  |
| $W$           | Point load   |
| or            | Foundation mass  |
| or            | Load per unit length on a cable  |
| or            | Energy required for crack growth   |
| $w$           | Lateral displacement   |
| or            | Effective width of flange per bolt   |
| or            | Uniformly distributed load on plate  |
| $X_c$         | Elastic neutral axis depth in composite section  |
| $x$           | Torsion index of section   |
| $x_p$         | Plastic neutral axis depth in composite section  |
| $Y$           | Correction factor in fracture mechanics  |
| $Y_s$         | Specified minimum yield stress of steel  |
| $Z_c$         | Elastic section modulus for compression  |
| $Z_{oo}$      | Elastic modulus for weld group of unit throat subject to torsional load  |
| $Z_x, Z_y$    | Elastic modulus about major or minor axis  |
| $z$           | Depth of foundation  |
| $\alpha$      | Coefficient of linear thermal expansion  |
| $\alpha_c$    | Modular ratio  |
| $\beta$       | Ratio of smaller to larger end moment  |
| or            | Coefficient in determination of prying force   |
| $\gamma$      | Ratio $M/M_o$ , i.e. ratio of larger end moment to mid-length moment on simply-supported span equal to unrestrained length |
| or            | Bulk density of soil   |
| or            | Coefficient in determination of prying force   |
| $\gamma_f$    | Overall load factor  |
| $\gamma_m$    | Material strength factor   |
| $\Delta$      | Displacements in vector  |
| $\delta$      | Deflection   |
| or            | Elongation   |
| $\delta_c$    | Deflection of composite beam at serviceability limit state   |
| $\delta_{ic}$ | Deflection of composite beam at serviceability limit state in presence of partial shear connection                         |
| $\delta_o$    | Deflection of steel beam at serviceability limit state   |
| $\delta_{oo}$ | Deflection in continuous composite beam at serviceability limit state  |
| $\epsilon$    | Constant $(275/p_y)^{1/2}$   |
| or            | Strain   |

xxx     *Notation*

|                |  |
|----------------|--|
| $\eta$         | Load ratio for composite columns                                 |
| $\lambda$      | Slenderness, i.e. effective length divided by radius of gyration |
| $\lambda_{cr}$ | Elastic critical load factor                                     |
| $\lambda_{LO}$ | Limiting equivalent slenderness                                  |
| $\lambda_{LT}$ | Equivalent slenderness   |
| $\lambda_o$    | Limiting slenderness   |
| $\mu$          | Slip factor  |
| $\mu_x, \mu_y$ | Reduction factors on moment resistance considering axial load    |
| $\sigma$       | Stress   |
| $\sigma_e$     | Tensile stress   |
| $\phi$         | Diameter of composite column                                     |
| or             | Angle of friction in granular soil                               |

# Chapter 1

## Single-storey buildings

by GRAHAM RAVEN and ALAN POTTAGE

### 1.1 Range of building types

It is estimated that around 50% of the hot-rolled constructional steel used in the UK is fabricated into single-storey buildings being some 40% of the total steel used in them. The remainder is light-gauge steel cold-formed into purlins, rails, cladding and accessories. Over 90% of single-storey non-domestic buildings have steel frames demonstrating the dominance of steel construction for this class of building. These relatively light, long-span, durable structures are simply and quickly erected and developments in steel cladding have enabled architects to design economical buildings of attractive appearance to suit a wide range of applications and budgets.

The traditional image was a dingy industrial shed with a few exceptions such as aircraft hangars and exhibition halls. Changes in retailing and the replacement of traditional heavy industry with electronics-based products have led to a demand for increased architectural interest and enhancement.

Clients expect their buildings to have the potential for easy change of layout several times during the building's life. This is true for both institutional investors and owner users. The primary feature is therefore flexibility of planning which, in general terms, means as few columns as possible consistent with economy. The ability to provide spans up to 60 m, but most commonly around 30 m, gives an extremely popular structural form for the supermarkets, do-it-yourself stores and the like, which are now surrounding towns in the UK. The development of steel cladding in a wide variety of colours and shapes has enabled distinctive and attractive forms and house styles to be created.

Improved reliability of steel-intensive roofing systems has contributed to their acceptability in buildings used by the public and perhaps more importantly in 'high-tech' buildings requiring controlled environments. The structural form will vary according to span, aesthetics, integration with services, cost and suitability for the proposed activity. A cement manufacturing building will clearly have different requirements from a warehouse, food processing plant or computer factory.

The growth of the leisure industry has provided a challenge to designers, and buildings vary from the straightforward requirement of cover for bowls, tennis, etc., to an exciting environment which encourages people to spend days of their holidays indoors at water centres and similar controlled environments suitable for year round recreation.

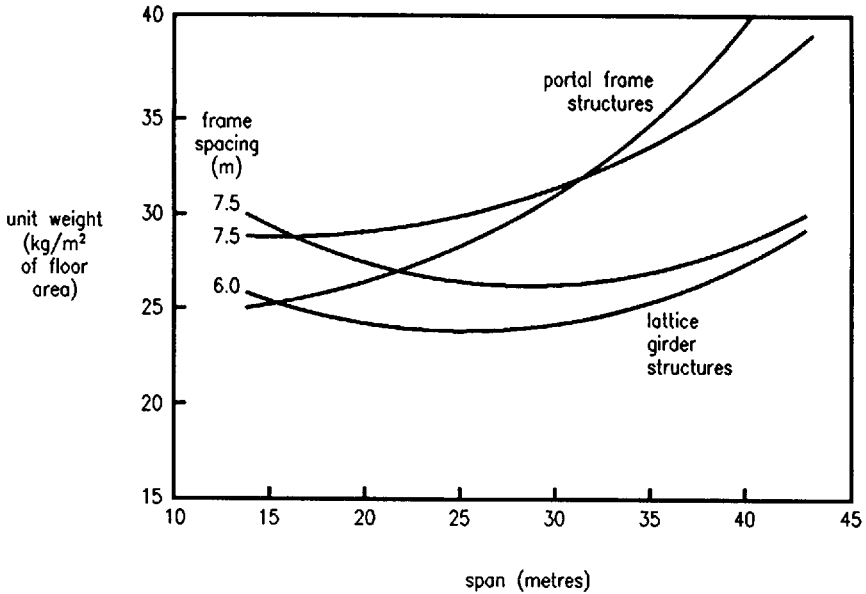


Fig. 1.1 Comparison of bare frame weights for portal and lattice structures

In all instances the requirement is to provide a covering to allow a particular activity to take place; the column spacing is selected to give as much freedom of use of the space consistent with economy. The normal span range will be from 12 m to 50 m, but larger spans are feasible for hangars and enclosed sports stadia.

Figure 1.1 shows how steel weight varies with structural form and span.<sup>1</sup>

## 1.2 Anatomy of structure

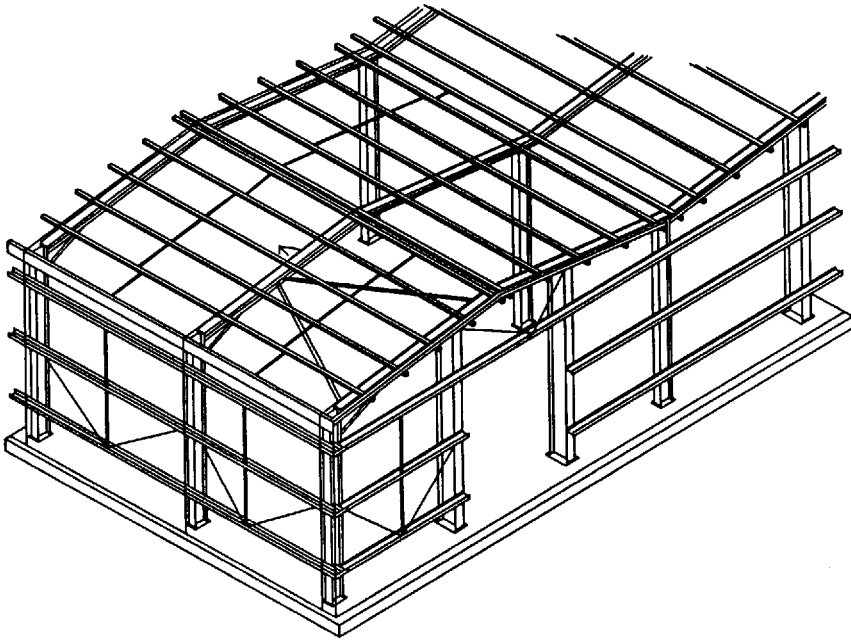
A typical single-storey building consisting of cladding, secondary steel and a frame structure is shown in Fig. 1.2.

### 1.2.1 Cladding

Cladding is required to be weathertight, to provide insulation, to have penetrations for daylight and access, to be aesthetically pleasing and to last the maximum time with a minimum of maintenance consistent with the budget.

The requirements for the cladding to roofs and walls are somewhat different. The weathertightness of the roof is clearly paramount, particularly as the demand





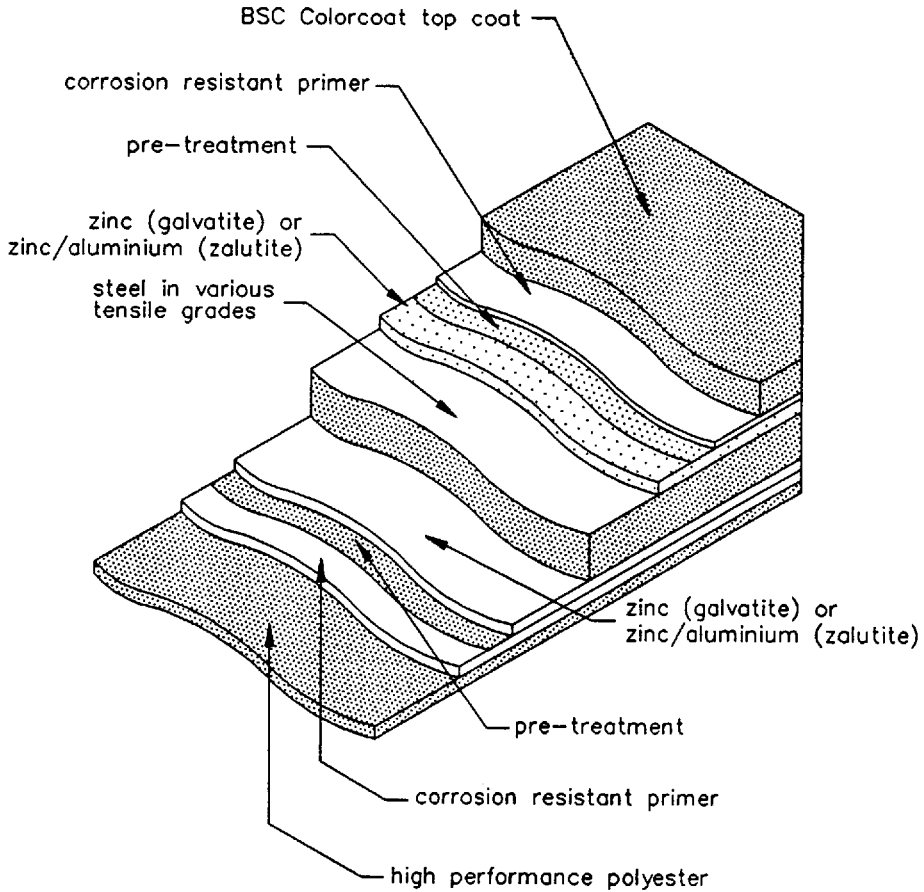
*Fig. 1.2* Structural form for portal-frame building (some rafter bracing omitted for clarity)

for lower pitches increases, whereas aesthetics dominate in the choice of walling. Over the last 20 years metal cladding has emerged as the most popular choice for both areas. The two major substrates are steel and aluminium. Steel is more economical and, with a much lower coefficient of expansion, has practical advantages but it does depend on the integrity of the coatings to maintain corrosion-resistance and this has led to the selection of aluminium in some sensitive cases. However current British Steel formulations (HP200 plastisol, and PVF2) have Agrément Certificates with life expectancy to first maintenance of 10–25 years depending on environment.

The sheeting (Fig. 1.3) from which the cladding is formed consists of a steel substrate with layers of galvanizing, primer and colour coating. The inner surface is normally finished in white polyester with the outer coating in PVF2, PVC (plastisol) or polyester. Plastisol is the most popular, providing a robust 200 micron thick coating but with restrictions on use in marine environments or in latitudes less than 49°. Light colours are recommended for roofs to minimize heat absorption.

The construction of the cladding skin can take several forms. Those most commonly seen in the UK are:

- (1) single-skin trapezoidal
- (2) double trapezoidal shell



*Fig. 1.3* Cladding sheet strata

- (3) standing seam and concealed fix
- (4) composite.

Further information on cladding is given in section 1.4.7.

### 1.2.2 Secondary elements

In the normal single-storey building the cladding is supported on secondary members which transmit the loads back to main structural steel frames. The spacing of the frames, determined by the overall economy of the building, is normally in the range 5 m–8 m, with 6 m and 7.5 m as the most common spacings.

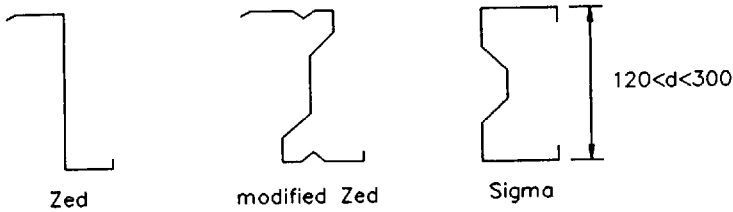


Fig. 1.4 Popular purlin and frame sections

A combination of cladding performance, erectability and the restraint requirements for economically-designed main frames dictates that the purlin and rail spacing should be 1.5–2 m.

For this range the most economic solution has proved to be cold-formed light-gauge sections of proprietary shape and volume produced to order on computer numerically controlled (CNC) rolling machines. These have proved to be extremely efficient since the components are delivered to site pre-engineered to the exact requirements, which minimizes fabrication and erection times and eliminates material wastage. Because of the high volumes, manufacturers have been encouraged to develop and test all material-efficient sections. These fall into three main categories: Zed, modified Zed and Sigma sections. Figure 1.4 illustrates the range.

The Zed section was the first shape to be introduced. It is material-efficient but the major disadvantage is that the principal axes are inclined to the web. If subject to unrestrained bending in the plane of the web, out-of-plane displacements occur; if these are restrained, out-of-plane forces are generated.

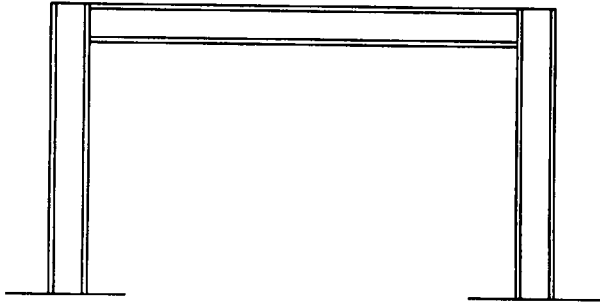
More complicated shapes have to be rolled rather than press braked. This is a feature of the UK where the market is supplied by relatively few manufacturers and the volumes produced by each allow the advanced manufacturing techniques to be employed giving competitive products and service.

As roof pitches become lower, modified Zed sections have been developed with the inclination of the principal axis considerably reduced, so enhancing overall performance. Stiffening has been introduced, improving material efficiency.

The Sigma shape in which the shear centre is approximately coincident with the load application line has advantages. One manufacturer now produces, using rolling, a second-generation product of this configuration, which is economical.

### 1.2.3 Primary frames

The frame supports the cladding but, with increasing architectural and service demands, other factors are important. The basic structural form has developed against the background of achieving the lowest cost envelope by enclosing the minimum volume. Plastic design of portal frames brings limitations on the spacing



*Fig. 1.5* Simplest single-storey structure

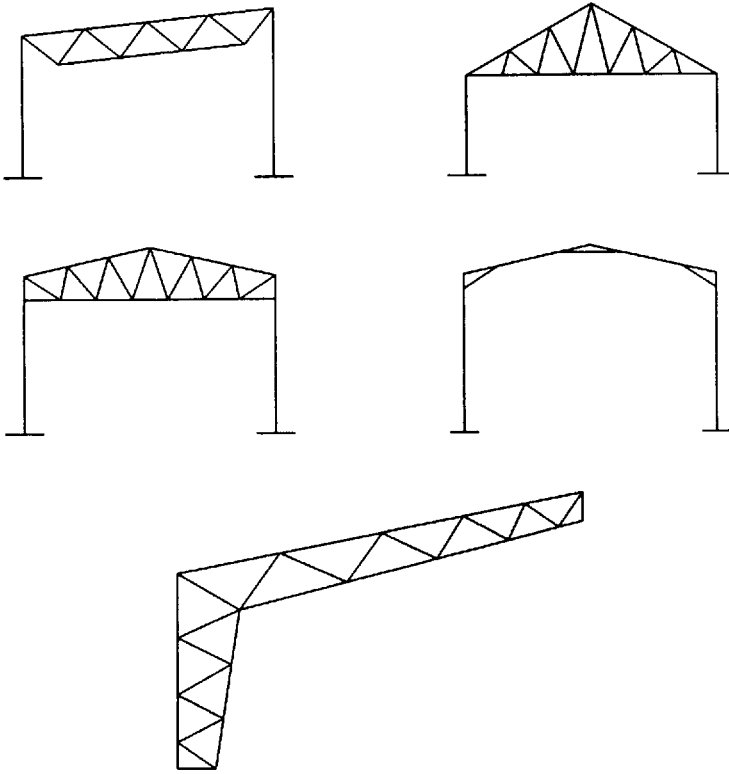
of restraints of around 1.8–2 m. The cladding profiles are economic in this range; they can support local loads and satisfy drainage requirements. The regime is therefore for the loads to be transferred from the sheeting on to the purlins and rails which in turn must be supported on a primary structure. Figure 1.5 shows the simplest possible type of structure with vertical columns and a horizontal spanning beam. There is a need for a fall in the roof finish to provide drainage, but for small spans the beam can be effectively horizontal with the fall being created in the finishes or by a nominal slope in the beam. The minimum slope is also a function of weatherproofing requirements of the roof material.

The simple form shown would be a mechanism unless restraint to horizontal forces is provided. This is achieved either by the addition of bracing in both plan and vertical planes or by the provision of redundancies in the form of moment-resisting joints. The important point is that all loads must be transmitted to the foundations in a coherent fashion even in the simplest of buildings, whatever their size.

The range of frame forms is discussed in more detail in later sections but Fig. 1.6 shows the structural solutions commonly used. The most common is the portal shape with pinned bases, although this gives a slightly heavier frame than the fixed-base option. The overall economy, including foundations, is favourable. The portal form is both functional and economic with overall stability being derived from the provision of moment-resisting connections at eaves and apex.

The falls required to the roof are provided naturally with the cladding being carried on purlins which in turn are supported by the main frame members. Architectural pressures have led to the use of flatter slopes compatible with weathertightness; the most common is around  $6^\circ$ , but slopes as low as  $1^\circ$  are used, which means deflection control is increasingly important.

Traditionally, portal frames have been fabricated from compact rolled sections and designed plastically. More recently the adoption of automated welding techniques has led to the introduction of welded tapered frames which have been



*Fig. 1.6* A range of structural forms

extensively used for many years in the USA. For economy these frames have deep slender sections and are designed elastically. In addition to material economies, the benefit is in the additional stiffness and reduced deflections.

Although the portal form is inherently pleasing to the eye, given a well-proportioned and detailed design, the industrial connotation, together with increased service requirements, has encouraged the use of lattice trusses for the roof structure. They are used both in the simple forms with fixed column bases and as portal frames with moment-resisting connections between the tops of the columns for long-span structures such as aircraft hangars, exhibition halls and enclosed sports facilities.

#### 1.2.4 Resistance to sway forces

Most of the common forms provide resistance to sideways forces in the plane of the frame. It is essential also to provide resistance to out-of-plane forces; these

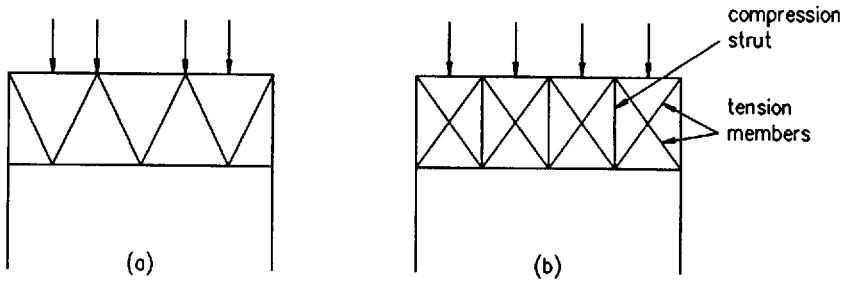


Fig. 1.7 Roof bracing

are usually transmitted to the foundations with a combination of horizontal and vertical girders. The horizontal girder in the plane of the roof can be of two forms as shown in Fig. 1.7. Type (a) is formed from members, often tubes, capable of carrying tension or compression. One of the benefits is in the erection stage as the braced bay can be erected first and lined and levelled to provide a square and safe springboard for the erection of the remainder.

Type (b) uses less material but more members are required. The diagonals are tension-only members (wire rope has been used) and the compression is taken in the orthogonal strut which has the shortest possible effective length. It may be possible to use the purlins, strengthened where necessary, for this purpose.

Similar arrangements must be used in the wall to carry the forces down to foundation level. If the horizontal and vertical girders are not in the same bay, care must be taken to provide suitable connecting members.

## 1.3 Loading

### 1.3.1 External gravity loads

The dominant gravity load is from snow. The general case is the application of a basic uniform load of  $0.6 \text{ kN/m}^2$ , but with sloping roofs having multiple spans and parapets, the action of drifting snow has to be considered. Design information is given in BS 6399<sup>2</sup> and Building Research Establishment (BRE) Digest 332.<sup>3</sup> The basic loading is variable according to location and is derived from the snow map which has been incorporated into BS 5502.<sup>4</sup> The main frame design for portals can be carried out using the uniform load case but the variable loads caused by drifting are to be applied to cladding and purlins. The effects of drifting are idealized into triangular loadings with formulae given for the various effects of valleys, parapets, upstands, etc. Early tests carried out at the BRE established that equivalent uniformly distributed loads can be used for the purlin design. In

the areas of high local load, consideration has to be given as to whether to reduce purlin spacing or to increase the gauge. Where practicable the reduction of spacing is preferable as it prevents the dangers and disruption involved with identification and production of different thicknesses of purlin supplied to one job.

The load factor for snow loading is 1.6 for both secondary and main frame elements unless in combination with crane or similar loading. The factors to be used for various combinations are given in BS 5950: Part 1.<sup>5</sup>

For portal frames the frame strength will usually be determined by the snow load case, unless the eaves height is large in relation to span.

### 1.3.2 Wind loads

With lightweight cladding and purlins and rails, wind loads are important. Cladding and its fasteners are designed for the local pressure coefficient as given in BS 6399: Part 3.<sup>2</sup> Purlins and main frames are designed using the relevant statistical factors, but not additional local coefficients. Care must be taken to include the total effect of both internal and external pressure coefficients.

When designing to BS 5950 the load factor for the wind force is 1.4 acting against dead loads having a factor 1.0.

### 1.3.3 Internal gravity loads

Service loads for lighting, etc., are reasonably included in the global  $0.6 \text{ kN/m}^2$ . As service requirements have increased, it has become necessary to consider carefully the provision to be made.

Most purlin manufacturers can provide proprietary clips for hanging limited point loads to give flexibility of layout. Where services and sprinklers are required, it is normal to design the purlins for a global service load of  $0.1\text{--}0.2 \text{ kN/m}^2$  with a reduced value for the main frames to take account of likely spread. Particular items of plant must be treated individually. The specifying engineer should make a realistic assessment of the need as the elements are sensitive and while the loads may seem low, they represent a significant percentage of the total and affect design economy accordingly.

### 1.3.4 Cranes

The most common form of craneage is the overhead type running on beams supported by the columns. The beams are carried on cantilever brackets or in heavier cases by providing dual columns.

In addition to the weight of the cranes and their load, the effects of acceleration and deceleration have to be catered for. This is simplified by a quasi-static approach with enhanced load factors being used. The allowances to be made are given in BS 6399: Part 1. For simple forms of crane gantry these are:

- (1) for loads acting vertically, the maximum static wheel loads increased by 25% for an electric overhead crane or 10% for a hand-operated crane;
- (2) for the horizontal force acting transverse to the rails, the following percentage of the combined weight of the crab and the load lifted:
  - (a) 10% for an electric overhead crane, or
  - (b) 5% for a hand-operated crane;
- (3) for the horizontal forces acting along the rails, 5% of the static wheel loads which can occur on the rails for overhead cranes which are either electric or hand-operated.

For heavy, high-speed or multiple cranes the allowances should be specially calculated with reference to the manufacturers.

The combination load factors for design are given in BS 5950: Part 1. The constant movement of a crane gives rise to a fatigue condition. This is, however, restricted to the local areas of support, i.e. the crane beam itself, the support bracket and its connection to the main column. It is not normal to design the whole frame for fatigue as the stress levels due to the crane travel are relatively low.

## **1.4 Design of common structural forms**

### **1.4.1 Beam and column**

The cross section shown in Fig. 1.5 is undoubtedly the simplest framing solution which can be used to provide structural integrity to single-storey buildings. Used predominantly in spans of up to 10 m, where flat roof construction is acceptable, the frame comprises standard hot-rolled sections having simple or moment-resisting joints.

Flat roofs are notoriously difficult to weatherproof, since deflections of the horizontal cross-beam induce ponding of rainwater on the roof which tends to penetrate the laps of traditional cladding profiles and, indeed, any weakness of the exterior roofing fabric. To counteract this, either the cross-member is cambered to provide the required fall across the roof, or the cladding itself is laid to a predetermined fall, again facilitating drainage of surface water off the roof.

Due to the need to control excessive deflections, the sections tend to be somewhat heavier than those required for strength purposes alone, particularly if the cross-beam is designed as simply-supported. In its simplest form, the cross-beam is designed as spanning between columns, which, for gravity loadings, are in



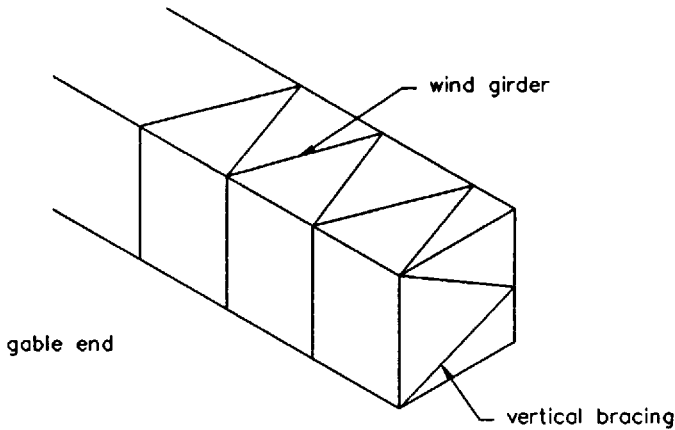


Fig. 1.8 Simple wind bracing system

direct compression apart from a small bending moment at the top of the column due to the eccentricity of the beam connection. The cross-beam acts in bending due to the applied gravity loads, the compression flange being restrained either by purlins, which support the roof sheet, or by a proprietary roof deck which may span between the main frames and which must be adequately fastened. The columns are treated as vertical cantilevers for in-plane wind loads.

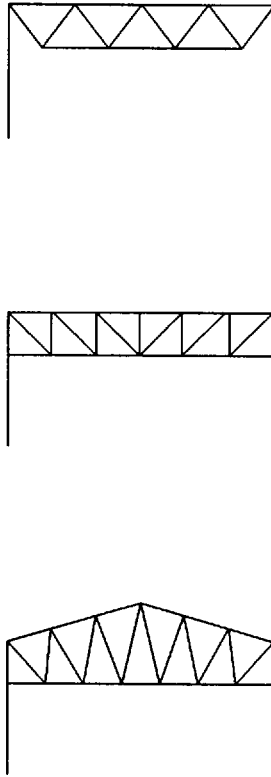
Resistance to lateral loads is achieved by the use of a longitudinal wind girder, usually situated within the depth of the cross-beam. This transmits load from the top of the columns to bracing in the vertical plane, and thence to the foundation. The bracing is generally designed as a pin-jointed frame, in keeping with the simple joints used in the main frame. Details are shown in Fig. 1.8.

Buildings which employ the use of beam-and-column construction often have brickwork cladding in the vertical plane. With careful detailing, the brickwork can be designed to provide the vertical sway bracing, acting in a similar manner to the shear walls of a multi-storey building.

Resistance to lateral loading can also be achieved either by the use of rigid connections at the column/beam joint or by designing the columns as fixed-base cantilevers. The latter point is covered in more detail in the following sub-section relating to the truss and stanchion framing system.

#### 1.4.2 Truss and stanchion

The truss and stanchion system is essentially an extension of the beam-and-column solution, providing an economic means of increasing the useful span.



*Fig. 1.9* Truss configurations

Typical truss shapes are shown in Fig. 1.9.

Members of lightly-loaded trusses are generally hot-rolled angles as the web elements, and either angles or structural tees as the boom and rafter members, the latter facilitating ease of connection without the use of gusset plates. More heavily loaded trusses comprise universal beam and column sections and hot-rolled channels, with connections invariably employing the use of heavy gusset plates.

In some instances there may be a requirement for alternate columns to be omitted for planning requirements. In this instance load transmission to the foundations is effected by the use of long-span eaves beams carrying the gravity loads of the intermediate truss to the columns; lateral loading from the intermediate truss is transmitted to points of vertical bracing, or indeed vertical cantilevers by means of longitudinal bracing as detailed in Fig. 1.10. The adjacent frames must be designed for the additional loads.

Considering the truss and stanchion frame shown in Fig. 1.11, the initial assumption is that all joints are pinned, i.e. they have no capacity to resist

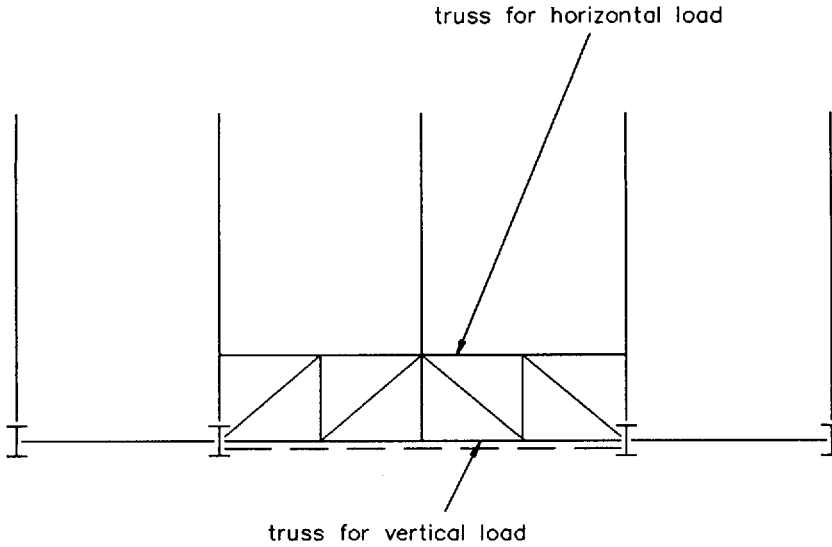


Fig. 1.10 Additional framing where edge column is omitted

bending moment. The frame is modelled in a structural analysis package or by hand calculation, and for the load cases considered, applied loads are assumed to act at the node points. It is clear from Fig. 1.11 that the purlin positions and nodes are not coincident; consequently, due account must be taken of the bending moment induced in the rafter section. The rafter section is analyzed as a continuous member from eaves to apex, the node points being assumed as the supports, and the purlin positions as the points of load application (Fig. 1.12).

The rafter is sized by accounting for bending moment and axial loads, the web members and bottom chord of the truss being initially sized on the basis of axial load alone.

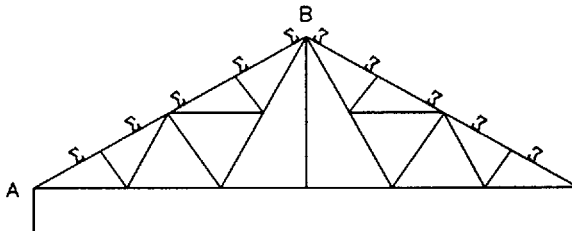


Fig. 1.11 Truss with purlins offset from nodes

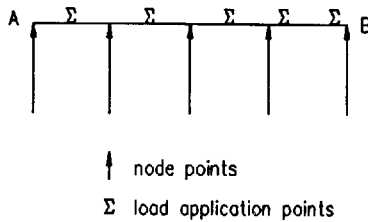


Fig. 1.12 Rafter analyzed for secondary bending

Use of structural analysis packages allows the engineer to rapidly analyze any number of load combinations. Typically, dead load, live load and wind load cases are analyzed separately, and their factored combinations are then investigated to determine the worst loading case for each individual member. Most software packages provide an envelope of forces on the truss for all load combinations, giving maximum tensile and compressive forces in each individual member, thus facilitating rapid member design.

Under gravity loading the bottom chord of the truss will be in tension and the rafter chords in compression. In order to reduce the slenderness of the compression members, lateral restraint must be provided along their length, which in the present case is provided by the purlins which support the roof cladding. In the case of load reversal, the bottom chord is subject to compression and must be restrained. A typical example of restraint to the bottom chord is the use of ties, which run the length of the building at a spacing governed by the slenderness limits of the compression member; they are restrained by a suitable end bracing system. Another solution is to provide a compression strut from the chord member to the roof purlin, in a similar manner to that used to restrain compression flanges of rolled sections used in portal frames. The sizing of all restraints is directly related to the compressive force in the primary member, usually expressed as a percentage of the compressive force in the chord. Care must be taken in this instance to ensure that, should the strut be attached to a thin-gauge purlin, bearing problems in thin-gauge material are accounted for. Examples of restraints are shown in Fig. 1.13.

Connections are initially assumed as pins, thereby inferring that the centroidal axes of all members intersecting at a node point are coincident. Practical considerations invariably dictate otherwise, and it is quite common for member axes to be eccentric to the assumed node for reasons of fit-up and the physical constraints that are inherent in the truss structure. Such eccentricities induce secondary bending stresses of the node points which must be accounted for not only by local bending and axial load checks at the ends of all constituent members, but also in connection design. Typical truss joints are detailed in Fig. 1.14.

It is customary to calculate the net bending moment at each node point due to any eccentricities, and proportion this moment to each member connected to the node in relation to member stiffness.

In heavily-loaded members secondary effects may be of such magnitude as to

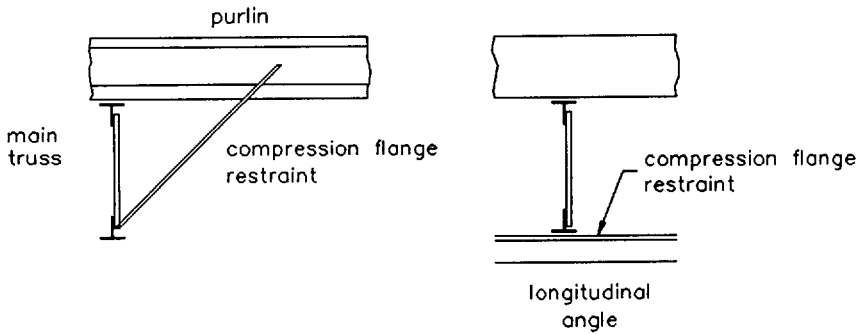


Fig. 1.13 Restraints to bottom chord members

require member sizes to be increased quite markedly above those required when considering axial load effects alone. In such instances, consideration should be given to the use of gusset plates, which can be used to ensure that member centroids are coincident at node points, as shown in Fig. 1.15. Types of truss connections are very much dependent on member size and loadings. For lightly-loaded members, welding is most commonly used with bolted connections in the chords if the truss is to be transported to site in pieces and then erected. In heavily-loaded members, using gusset plates, either bolting, welding or a combination of the two may be used. However, the type of connection is generally based on the fabricator's own reference.

Where the roof truss has a small depth at the eaves, lateral loading is resisted either by longitudinal wind girders in the plane of the bottom boom and/or rafter, or by designing the columns as vertical fixed-base cantilevers, as shown in Fig. 1.16. Where the truss has a finite depth at the eaves, benefit can be obtained by developing a moment connection at this position with the booms designed for appropriate additional axial loads. This latter detail may allow the column base to be designed as a pin, rather than fixed, depending on the magnitude of the applied loading, and the serviceability requirements for deflection.

Longitudinal stability is provided by a wind girder in the plane of the truss boom and/or rafter at the gable wall; the load from the gable being transmitted to the foundations by vertical bracing as shown in Fig. 1.17.

### 1.4.3 Portal frames

By far the most common form of structure for single-storey structures is the portal frame, the principal types being shown in Fig. 1.18.

Spans of up to 60 m can be achieved by this form of construction, the frame generally comprising hot-rolled universal beam sections. However, with the

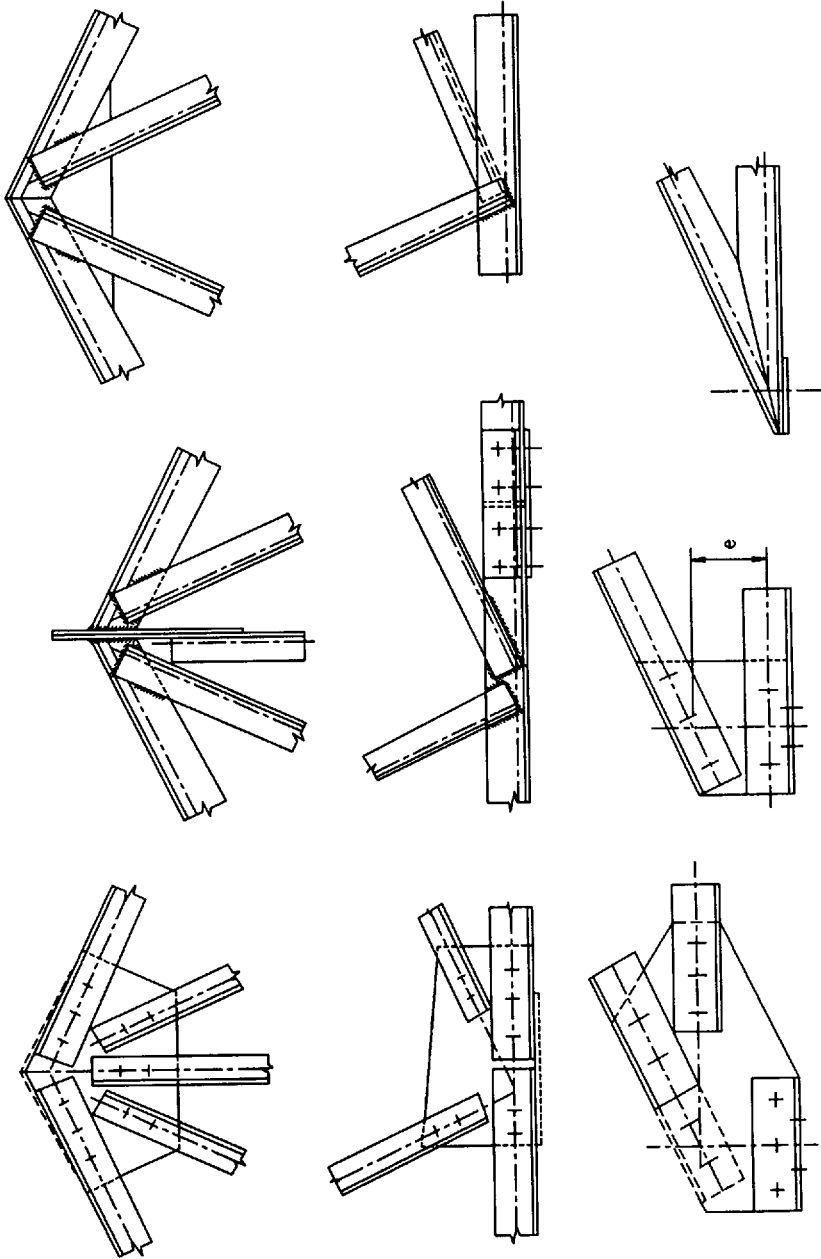


Fig. 1.14 Typical joints in trusses

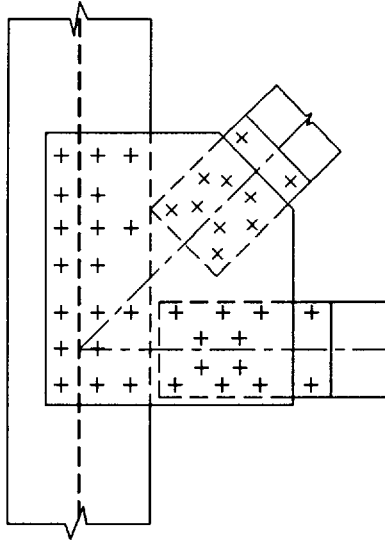


Fig. 1.15 Ideal joint with all member centroids coincident

increase in understanding of how slender plate elements react under combined bending moment, axial load and shear force, several fabricators now offer a structural frame fabricated from plate elements. These frames use tapered stanchions and rafters to provide an economic structural solution for single-storey buildings, the frame being 'custom designed' for each particular loading criterion.

Roof slopes for portal frames are generally of the order of  $6^\circ$  but slopes as low as  $1^\circ$  are becoming increasingly popular with the advent of new cladding systems such as standing seam roofs. It should be noted, however, that frame deflections at low slopes must be carefully controlled, and due recognition must be taken of the large horizontal thrusts that arise at the base.

Frame centres are commonly of the order of 6–7.5 m, with eaves heights ranging from 6–15 m in the case of aircraft hangars or similar structures.

Resistance to lateral loading is provided by moment-resisting connections at the eaves, stanchion bases being either pinned or fixed. Frames which are designed on the basis of having pinned bases are heavier than those having fixity at the bases,

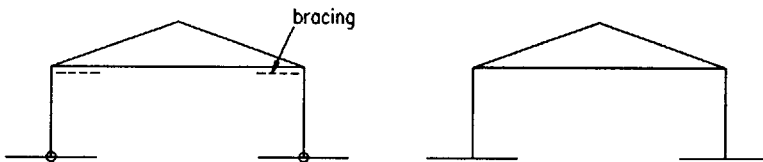


Fig. 1.16 Sway resistance for truss roofs

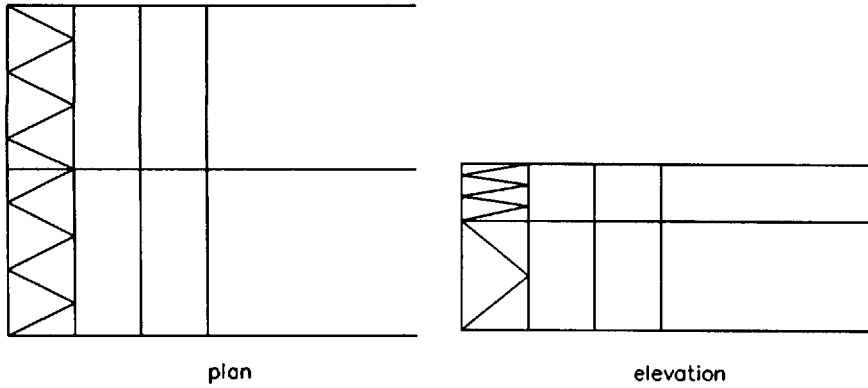


Fig. 1.17 Gable-end bracing systems

although the increase in frame cost is offset by the reduced foundation size for the pinned-base frames.

Parallel-flange universal sections, subject to meeting certain physical constraints regarding breadth-to-thickness ratios of both flanges and webs, lend themselves to rapid investigation by the plastic methods of structural analysis. The basis of the plastic method is the need to determine the load applied to the frame which will induce a number of 'plastic hinges' within the frame, thereby causing failure of the frame as a mechanism.

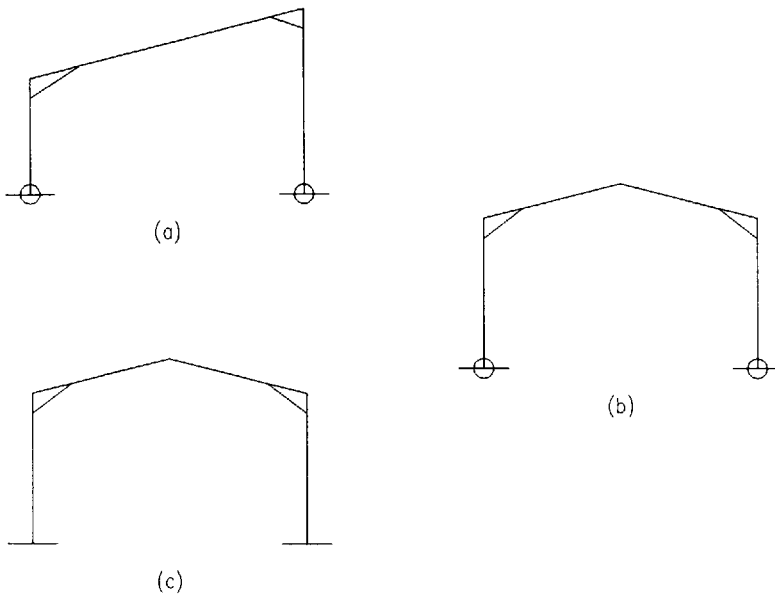


Fig. 1.18 Portal-frame structures



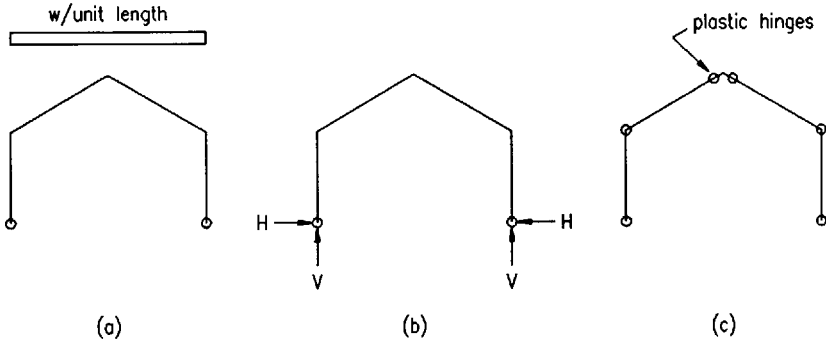


Fig. 1.19 Structural behaviour of pinned-base portal

This requirement is best illustrated by the following simple example.

Considering the pinned-base frame shown in Fig. 1.19(a), subject to a uniform vertical load,  $w$ , per unit length, the reactions at the foundations are shown in Fig. 1.19(b). The frame has one degree of indeterminacy. In order that the frame fails as a mechanism, at least two plastic hinges must form (i.e. the (degree of indeterminacy + 1)) as shown in Fig. 1.19(c). (It should be noted that although four hinges are shown in Fig. 1.19(c), due to ‘theoretical’ symmetry only one pair either side of the apex will in fact form, due to the obvious imperfections in both loading and erection conditions.)

In many structures, other than the most simple, it is not clear where the plastic hinges will form. There are several methods available to the design engineer which greatly assist the location of these hinge positions, not least the abundance of proprietary software packages specifically relating to this form of analysis. Prior to the use of these packages, however, it is imperative that the engineer fully understands the fundamentals of plastic analysis by taking time to calculate, by hand, several design examples. The example which follows uses a graphical construction as a means of illustrating the applications of the method to a simple portal frame. Further information on plastic analysis is given in Chapter 11.

The frame shown in Fig. 1.20(a) has one degree of indeterminacy. It is made statically determinate by assuming a roller at the right-hand base as shown in Fig. 1.20(b), and the free-bending moment diagram drawn as shown in Fig. 1.20(c). The reactant line for the horizontal force ‘removed’ to achieve a statically determinate structure must now be drawn as follows:

- (1) Considering member DC, the bending moment due to the reaction  $R$  at point D,  $M_D = Rh_1$ . Similarly, at point C,  $M_C = R(h_1 + h_2)$ .
- (2) The gradient of the reactant line along member DC,

$$m = \frac{R(h_1 + h_2) - R(h_1)}{L_1} = \frac{Rh_2}{L_1}$$

(3) The reactant line must pass through a point O as shown in Fig. 1.20(c). By similar triangles,

$$\frac{Rh_1}{x} = \frac{Rh_2}{L_1} \quad \text{giving} \quad x = \frac{L_1 h_1}{h_2}$$

Therefore, by rotating the reactant line through point O, the positions of the bending moment of equal magnitude in the positive and negative regions can be found and the member sized accordingly based on this value of bending moment.

Having found the positions of the reactant line which gives the number of hinges required for a mechanism to form, in this case two, the reactant line for the stanchions can be drawn through point O, a distance  $h_1$  from the end of the free-bending moment diagram. The unknown reaction,  $H$ , is then calculated as  $H = M_D/h_1$ .

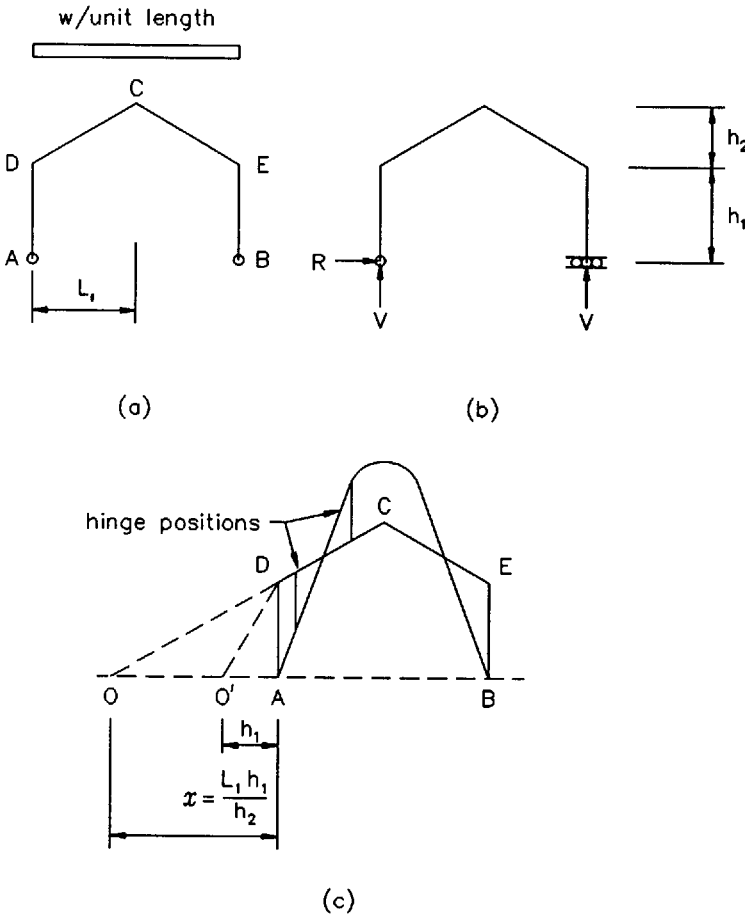


Fig. 1.20 Application of graphical method

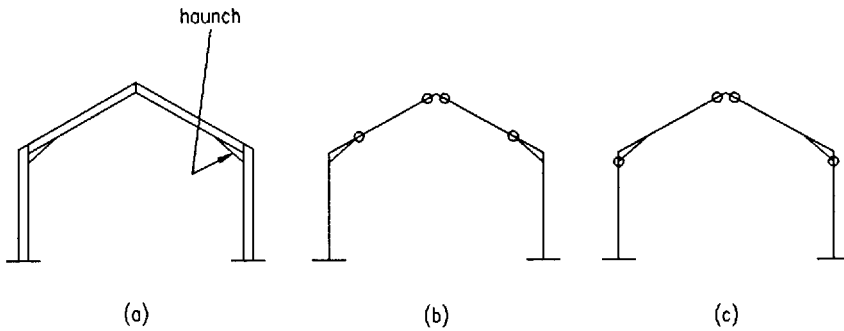


Fig. 1.21 Alternative hinge locations for haunched portal frames

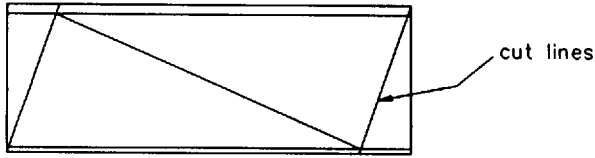
In a majority of instances, portal frames are constructed with a haunch at the eaves, as shown in Fig. 1.21(a).

Depending on the length/depth of the haunch, the plastic hinges required for a mechanism to form are shown in Figs 1.21(b) and (c). The dimensional details for the haunch can be readily investigated by the graphical method by superimposing the dimensions of the haunch on the free-bending moment diagram. The reactant line can then be rotated accordingly until the required mechanism is achieved and members sized accordingly.

Haunches are generally fabricated from parallel beam sections (Fig. 1.22). In all cases, the haunch must remain in the elastic region. A detailed check is required along its length, from a stability point of view, in accordance with the requirements laid down in the relevant code of practice. In some instances, bracing of the bottom flange must be provided from a purlin position within its length, as shown in Fig. 1.23.

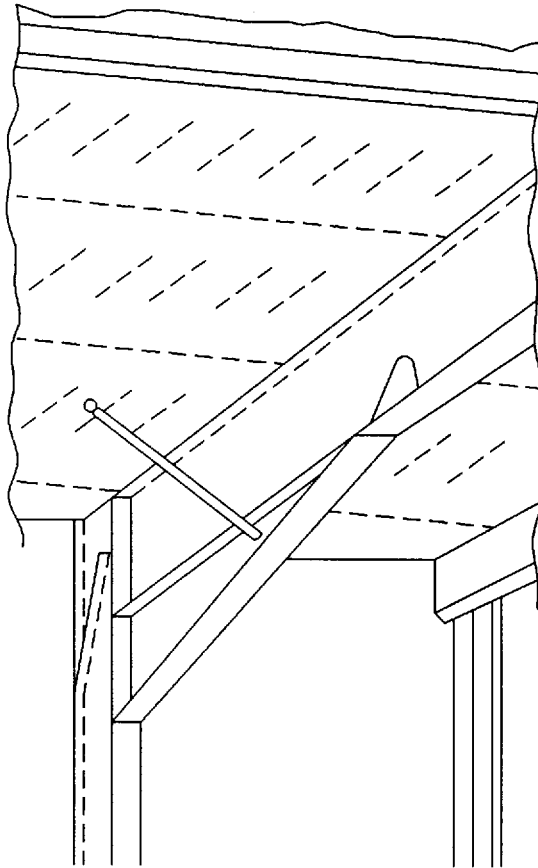
Portal frames analyzed by the plastic methods of structural analysis tend to be more economical in weight than their elastically designed counterparts. However, engineers should be aware that minimum weight sections, and by inference minimum depth sections, have to be connected together to withstand the moments and forces induced by the applied loading. Particular attention should be made at an *early stage* in the design process as to the economics of the connection. Cost penalties may be induced by having to provide, for example, gusset plates between pairs of bolts should the section be so shallow as to necessitate a small number of highly-stressed bolts. In addition, end plates should not be much thicker than the flanges of the sections to which they are attached.

Providing the engineer is prepared to consider the implications of his calculated member sizes on the connections inherent in the structure at an early stage, an economic solution will undoubtedly result. Leaving connection design solely to the fabricator, without any consideration as to the physical constraints of providing a number of bolts in an extremely shallow depth, will undoubtedly result in a connection which is both difficult to design and fabricate, and is costly.



*Fig. 1.22* Haunch fabrication

Having sized the members based on the previous procedure, it is imperative that an analysis at Serviceability Limit State is carried out (i.e. unfactored loads) to check deflections at both eaves and apex. This check is required, not only to ascertain whether deflections are excessive, but also as a check to ensure that the deflections and accompanying frame movement can be accommodated by the



*Fig. 1.23* Bottom flange restraint

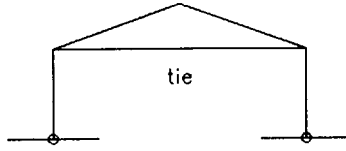


Fig. 1.24 Tied portal frame

building envelope without undue cracking of any brickwork or tearing of metal cladding sheets at fixing positions. Excessive lateral deflections can be reduced by increasing the rafter size and/or by fixing the frame bases. It should be noted that the haunch has a significant effect on frame stiffness due to its large section properties in regions of high bending moment.

#### 1.4.4 Tied portal

The tied portal, a variation of the portal frame, is illustrated in Fig. 1.24.

Economy of material can be achieved, albeit at the expense of reducing the allowable headroom of the building, by provision of a tie at eaves level. Under vertical loading, the eaves spread is reduced due to the induced tensile force in the tie. However, although the rafter size is reduced, because under vertical loading the only possible mode of failure of the rafter is that of a fixed-end beam, deflections are more critical. Lateral loading due to wind further complicates the problem since in some cases the tie may not act in tension and becomes redundant. It is common, therefore, for tied portals to have fixed bases, which provide greater stability and resistance to horizontal loading.

#### 1.4.5 Stressed-skin design

In addition to providing the weathertight membrane, the steel sheeting can also be utilized as a structural element itself. Correct detailing of connections between individual cladding sheets (and their connections to the support steelwork) will induce a stressed-skin effect which can offer both resistance to transverse wind loads, and restraint to the compression flanges of the main frame elements.

It is clear that when vertical load is applied to a pitched roof portal frame, the apex tends to deflect downwards, and the eaves spread horizontally. This displacement cannot occur without some deformation of the cladding. Since the cladding is fixed to the purlins, the behaviour of the cladding and purlins together is analogous to that of a deep plate girder, i.e. the purlins resist the bending moment, in the form of axial forces, and the steel sheeting resists the applied shear, as shown in Fig. 1.25.

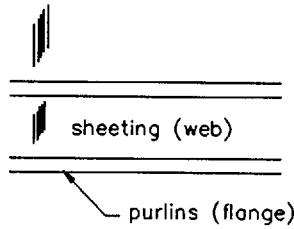


Fig. 1.25 Stressed-skin action

As a consequence of this action, the load applied over the 'length' of the 'plate girder' has to be resisted at the ends of the span. In the case of stressed-skin action being used to resist transverse wind loads on the gable end of the structure, adequate connection must be present over the end bay to transmit the load from the assumed 'plate girder' into the braced bay, and into the foundations, as shown in Fig. 1.26.

Some degree of stressed-skin action is present in all portal frame structures where cladding is fixed to the supporting members by mechanical fasteners. Claddings which are either brittle (i.e. fibre cement) or are attached to the supporting structure by clips (i.e. standing seam systems) are not suitable for stressed-skin applications.

Correct detailing and correct fixing is essential to the integrity of stressed-skin applications:

- (1) suitable bracing members must be used to allow the applied loads from diaphragm action to be transmitted to the foundations.
- (2) at the position of laps in the sheeting, suitable mechanical fasteners must be present to allow continuity of load between sheets. These fasteners can be

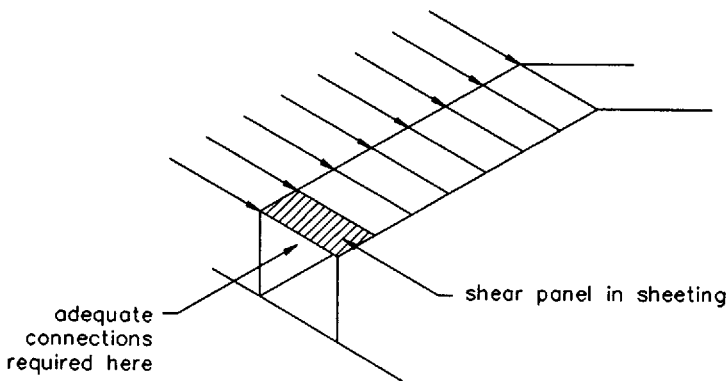


Fig. 1.26 Stressed-skin action for gable-end bracing

screws or rivets, which must be capable of withstanding both shear and pull out due to the stressed-skin effect and applied loads respectively.

- (3) the ends of the sheet must similarly be connected to the supporting members (i.e. purlins).
- (4) all stressed-skin panels must be connected to adequately designed edge members, which must be capable of transmitting the axial forces induced by bending, in addition to the forces induced by imposed and wind load effects.

### 1.4.6 Purlins and siderails

Due to the increasing awareness of the load-carrying capabilities of sections formed from thin-gauge material, proprietary systems for both purlins and siderails have been developed by several manufacturers in the United Kingdom. Consequently, unless a purlin or siderail is to be used in a long-span or high-load application (when a hot-rolled angle or channel may be used) a cold-formed section is the most frequently used cladding support member for single-storey structures.

Cold-formed sections manufactured from thin-gauge material are particularly prone to twisting and buckling due to several factors which are directly related to the section's shape. The torsional constant of all thin-gauge sections is low (it is a function of the cube of the thickness); in the case of lipped channels the shear centre is eccentric to the point of application of load thus inducing a twist on the section; in the case of Zeds the principal axes are inclined to the plane of the web thus inducing bi-axial bending effects. These effects affect the load-carrying capacity of the section.

When used in service the support system is subject to downward loading, due to dead and live loads such as cladding weight, snow, services, etc., and uplift if the design wind pressure is greater than the dead load of the system. Therefore, for a typical double-span system as shown in Fig. 1.27, the compression flange is restrained against rotation by the cladding for downward loading, but it is not so restrained in the case of load reversal.

In supporting the external fabric of the building, the purlins and siderails gain some degree of restraint against twisting and rotation from the type of cladding used and the method of its fastening to the supporting member. In addition, the

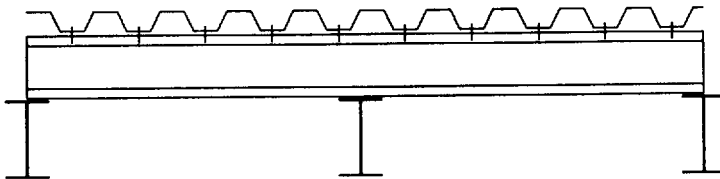


Fig. 1.27 Typical double-span purlin with cladding restraint

connection of the support member to the main frame also has a significant effect on the load-carrying capacity of the section. Economical design, therefore, must take account of the above effects.

There are four possible approaches to the design of a purlin system.

- (1) Design by calculation based on an elastic analysis as detailed in the relevant code of practice BS 5950: Part 5.<sup>6</sup> This approach neglects any beneficial effect of cladding restraint for the wind uplift case.
- (2) Empirical design based on approximate procedures for Zeds as given in the codes of practice. This approach leads to somewhat uneconomic design.
- (3) Design by calculation based on a rational analysis which accounts for the stabilizing influence of the cladding, plasticity in the purlin as the ultimate load is approached and the behaviour of the cleat at the internal support. The effects, however, are difficult to quantify.
- (4) Design on the basis of full-scale testing.

Manufacturers differ in the methods; the example used here is from one manufacturer who has published the method used.<sup>7</sup>

For volume production, design by testing is the approach which is used. Although this approach is expensive, maximum economy of material can be achieved and the cost of the testing can be spread over several years of production.

Design by testing involves the 'fine-tuning' of theoretical expressions for the collapse load of the system. The method is based on the mechanism shown in Fig. 1.28 for a two-span system.

From the above mechanism it can be shown that:

$$\begin{aligned} \text{the collapse load, } W_c &= f(M_1, M_2, x, L) \\ x &= f(M_1, M_2, L) \\ \theta_1 &= f(W_c, M_1, L) \end{aligned}$$

The performance of, for example, a two-span system is considerably enhanced if some redistribution of bending moment from the internal support is taken into account. The moment-rotation characteristic at the support is very much dependent on the cleat detail and the section shape. The characteristics of the central support can be found by testing a simply-supported beam subject to a central

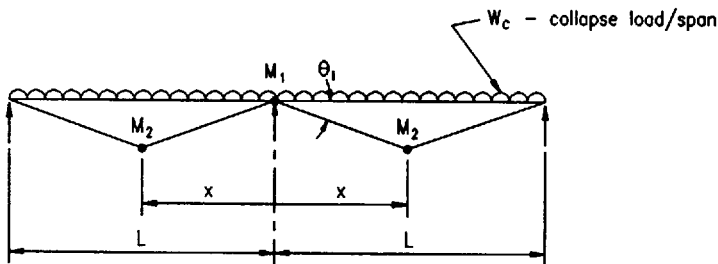


Fig. 1.28 Collapse mechanism for a two-span purlin system



point load, so as to simulate the behaviour of the central support of a double-span system.

From this test, the load–deflection characteristics can be plotted well beyond the deflection at which first yield occurs. A lower bound empirical expression can then be found for the support moment,  $M_1$ , based on an upper limit rotational capacity. A similar expression can be found for  $M_2$ , the internal span moment, again on the basis of a test on a simply-supported beam subject to a uniformly distributed load, applied by the use of a vacuum rig, or perhaps sand bags.

The design expressions can then be confirmed by the execution of numerous full-scale tests on double-span systems employing pairs of purlins supporting proprietary cladding.

As described earlier, load reversal under wind loading invariably occurs thereby inducing compressive forces to the flange in the internal span which is not restrained by the cladding, as is the case in the downward load case. Anti-sag rods or the like are placed within the internal span, thereby reducing the overall buckling length of the member. The system is again tested in load reversal conditions and, as before, the design expressions can be further refined.

In some instances, sheeting other than conventional trapezoidal cladding (which is invariably through fixed to the purlin by self-drilling fastenings in alternate troughs) will not afford the full restraint to the compression flange; examples are: standing seam roofs, brittle cladding, etc. The amount of restraint afforded by these latter types of cladding cannot easily be quantified. For the reasons outlined above, further full-scale testing is carried out and similar procedures of verification of design expressions are carried out.

The results of the full-scale tests are then condensed into easy to use load–span tables which are given in the purlin manufacturers’ design and detail literature. The use of these tables is outlined in Table 1.1.

The tabular format is typical of that contained in all purlin manufacturers’ technical literature. The table is generally prefaced by explanatory notes regarding fixing condition and lateral restraint requirements, the latter being particularly

**Table 1.1** Typical load table

| Span (m) | Section  | UDL (kN) <sup>a</sup> | Purlin centres (mm) |      |      |      |      |
|----------|----------|-----------------------|---------------------|------|------|------|------|
|          |          |                       | 1000                | 1200 | 1400 | 1600 | 1800 |
| 6.0      | CF170160 | 9.50                  | 1.58                | 1.32 | 1.13 | 0.99 | 0.88 |
|          | CF170170 | 10.75                 | 1.79                | 1.49 | 1.28 | 1.12 | 1.00 |
|          | CF170180 | 11.75                 | 1.96                | 1.63 | 1.40 | 1.22 | 1.09 |
|          | CF200160 | 12.25                 | 2.04                | 1.70 | 1.46 | 1.28 | 1.13 |
|          | CF200180 | 13.50                 | 2.25                | 1.88 | 1.61 | 1.41 | 1.25 |

<sup>a</sup> UDL is the *total* uniformly distributed load on a single purlin of a 6 m double-span system which would produce a failure of the section.

Loads given beneath the columns under purlin centres give the allowable uniformly distributed load on the purlin at a given spacing. The figure is arrived at by dividing the UDL by the product of span and purlin centres, i.e. for CF170180, 6 m span, 1800 mm centre,

$$\text{allowable load} = 11.75 / (6 \times 1.8) = 1.09 \text{ kN/m}^2$$

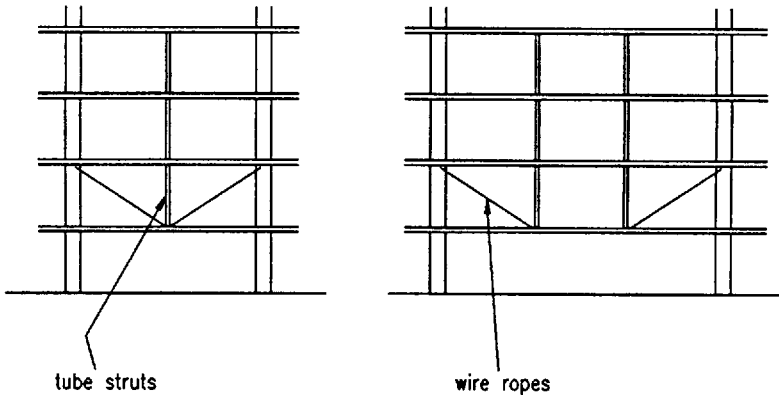


Fig. 1.29 Anti-sag systems for side wall rails

relevant to the load-reversal case. Conditions which arise in practice, and which are not covered in the technical literature, are best dealt with by the manufacturers' Technical Services Department which should be consulted for all non-standard cases.

Siderail design is essentially identical to that for purlins; load capacities are again arrived at after test procedures.

Self-weight deflections of siderails due to bending about the weak axis of the section are overcome by a tensioned wire system incorporating tube struts, typically at mid-span for spans of 6–7 m, and third-points of the span for spans of 7–8 m and above (Fig. 1.29).

### 1.4.7 Cladding

In addition to the visual requirements the cladding system has to provide the weatherproofing and insulation requirements suited to the building. It has to be strong enough to withstand the applied loads, normally snow, wind and traffic, during erection and maintenance. It must also provide the necessary lateral stability to the supporting purlins and rails and occasionally will form part of the structure itself in a stressed-skin design.

Cladding profiles are roll-formed and produced in volume so giving excellent economy and this means that, apart from an extremely rare occasion, the chosen profile will be from a manufacturer's published range. The loads that the profile can withstand are determined by the manufacturer and published in his brochure. Until recently they would have been determined by test, but calculation methods have been developed which are satisfactory for trapezoidal shapes. These give slightly conservative answers but in general, profiles that are walkable will have capacities in excess of those required. Sheeting can be erected satisfactorily without the need to walk indiscriminately over the whole area. The crowns at

mid-span are the most susceptible to foot traffic but these positions can easily be avoided, even if crawl boards are not used.

In double-skin construction it is normal to assume all loads are taken on the outer sheet and the inner liner merely has to be erectable and stiff enough to prevent noticeable sag once installed.

The specifier, therefore, has to select the profile appropriate to the design requirement and check the strength and deflection criteria against the manufacturer's published load tables. Care must also be taken to ensure the fasteners are adequate.

A variety of systems is available to suit environmental and financial constraints. The most common are listed below.

### *Single skin trapezoidal roofing*

This was widely used in the past with plasterboard or similar material as the lining material, and fibreglass insulation in the sandwich. The construction is susceptible to the plasterboard becoming damp due to condensation. An alternative is the use of rigid insulation boards, which are impervious to damp, supported on tee bars between the purlins. Unless the joints are sealed, which is difficult to achieve, condensation is likely to form. Although inexpensive, this type is therefore limited in its applicability.

The minimum slope is governed by the need to provide watertight joints and fasteners. If manufacturers' instructions on the use of sealants and stitching to laps are rigorously followed, this type can be used down to slopes of approximately 4°.

### *Double shell roof construction*

In this form of construction the plasterboard has been replaced by a steel liner sheet of 0.4 mm thickness with some stiffening corrugations. The lining is first installed and fastened to the purlins, followed by the spacing Zeds, insulation and outer sheet. The liner tray is not designed to take full wind and erection loads and, therefore, large areas should not be erected in advance of the outer skin. The liner tray is normally supplied in white polyester finish providing a pleasing internal finish. The weatherproofing criteria are the same as for single-skin systems and generally the minimum slope is 4°. Differing thicknesses of insulation are accommodated by varying spacer depths. The norm is 80 mm of fibreglass giving a nominal  $U$  value of  $0.44 \text{ W/m}^2 \text{ }^\circ\text{C}$ .

### *Standing seam systems*

The traditional forms of construction described above suffer from the inherent disadvantage of having to be fixed by screw-type fasteners penetrating the sheet.

Traditional fixing methods also limit the length of sheet that can be handled even if, in theory, long lengths can be rolled; thus laps are required.

The need for weathertightness at the lap constrains the minimum slope. A 5000 m<sup>2</sup> traditional roof has 20000 through fasteners and has to resist around 1 million gallons of water a year. The difficulty in ensuring that this large number of fasteners is watertight demonstrates the desirability of minimizing the number of penetrations. This has led to the development of systems having concealed fastenings and the ability to roll and fix long lengths. In order to cater for the thermal expansion in sheets, which may be 30 m long, the fastenings are in the form of clips which, while holding down the sheeting, allow it to move longitudinally. As discussed elsewhere, this may reduce the restraint available to the purlins and affect their design. When used in double-skin configuration the liner panel is normally conventionally fastened and provides sufficient restraint. The available permutations are too numerous to give general rules but purlin manufacturers will give advice.

It is necessary to fasten the sheets to the structure at one point to resist downslope forces and progressive movement during expansion and contraction. With the through fasteners reduced to the minimum and laps eliminated or specially detailed roof slopes as low as 1°, (after deflection) can be utilized. The roofs must be properly maintained since accumulation of debris is more likely and ponding leads to a reduced coating life.

Standing seam systems are used to replace the traditional trapezoidal outer sheets in single- and double-skin arrangements as described earlier.

### *Composite panels*

This most recent development in cladding systems provides solutions for many of the potential problems with metal roofing. The insulating foam is integral with the sheets and so totally fills the cavity, and with good detailing at the joints condensation can be eliminated in most environments.

The strength of the panel is dependent on the composite action of the two metal skins in conjunction with the foam. Theoretical calculations are possible although there are no codified design procedures. Since both steel and foam properties can vary and these are predetermined by the manufacturer, it is a question of selecting the panels from load tables provided rather than individual design. In addition to having to resist external loads, the effects of temperature differential must be taken into account. The critical combinations are wind suction with summer temperatures and snow acting with winter temperatures. The range of temperature considered is dependent on the colour and hence heat absorption of the outer skin; darker colours for roofs should only be considered in conjunction with the manufacturer, if at all.

Both standing seam and traditional trapezoidal forms are available with the same slope restrictions as non-composite forms.

A particular advantage is the erectability of the panels, which is a one-pass

operation and, therefore, a rapid process. This is combined with inherent robustness and walkability.

Since the integrity of the panel is important, and it is difficult to inspect the foam and its adhesion once manufactured, quality control of the materials and manufacturing environment in terms of temperature and dust control is vital. Reputable manufacturers should, therefore, be specified and their manufacturing methods ascertained.


### *External firewall*

Where buildings are close to the site boundary the Building Regulations require that the construction is such that reasonable steps are taken to prevent fire spreading to adjacent property. It has been demonstrated by tests that walls of double-skin steel construction with fibreglass or mineral wool insulation can achieve a four hour fire rating. The siderails and fixings require special details which were included in the test arrangements of the particular manufacturer and it is important that these are followed closely. They include such things as providing slotted holes to allow expansion of the rails rather than induce buckling, which may allow gaps to open in the sheeting at joints.

## **References to Chapter 1**

1. Horridge J.F. (1985) *Design of Industrial Buildings*. Civil Engineering Steel Supplement, November.
2. British Standards Institution (1988) Part 3: *Code of practice for imposed roof loads*. BS 6399, BSI, London.
3. Building Research Establishment (1988) *Loads on roofs from snow drifting against vertical obstructions and in valleys*. BRE Digest 332, May. BRE, Watford.
4. British Standards Institution (1987) Part 22: *Code of practice for design, construction and loading of buildings and structures for agriculture*. BS 5502, BSI, London.
5. British Standards Institution (1990) Part 1: *Code of practice for design in simple and continuous construction: hot rolled sections*. BS 5950, BSI, London.
6. British Standards Institution (1987) Part 5: *Code of practice for design of cold formed sections*. BS 5950, BSI, London.
7. Davies J.M. & Raven G.K. (1986) Design of cold formed purlins. *IABSE Colloquium, Thin Walled Metal Structures in Buildings*, Stockholm.

A worked example follows which is relevant to Chapter 1.

|  |   |  |                                     |
|--|---|--|-------------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL 5 7QN</p> | <p>Subject</p> <p><b>SINGLE STOREY DESIGN</b></p> |  | <p>Chapter ref.</p> <p><b>1</b></p> |
|  | <p>Design code</p> <p><b>BSS950: Part 1</b></p>   | <p>Made by <b>AVP</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no.</p> <p><b>1</b></p>    |

**Problem**

**Design the column and rafter of a portal frame using the graphical method to determine the position of the plastic hinges.**

**30 m span portal frame, 6° pitch**  
**6 m frame centres**  
**6 m to underside of haunch**  
**Foundations 450 mm below finished floor level, pinned bases**

**Loading**

**Dead (including self weight)      0.20 kN/m<sup>2</sup>**  
**Services                                    0.10 kN/m<sup>2</sup>**  
**Imposed                                    0.60 kN/m<sup>2</sup>**

**For (Dead & Imposed) case at ultimate limit state,**

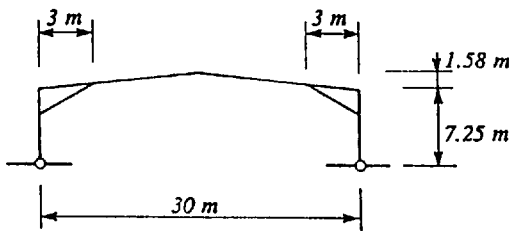
$$w_u = 1.40 (0.20 + 0.10) + 1.60 \times 0.60 \text{ kN/m}^2$$

$$= 1.38 \text{ kN/m}^2$$

**Load to frame,      W      =      6 × 1.38      =      8.28 kN/m**


**Free bending moment      =       $\frac{8.28 \times 30^2}{8}$       =      931.5 kNm**

**Draw free bending moment diagram and reactant lines**

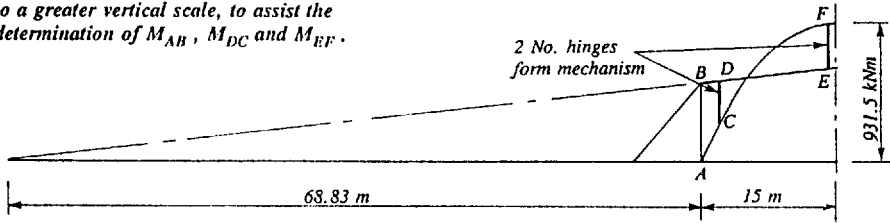


**i.e.       $L_1 = 15.00 \text{ m}$        $h_1 = 7.25 \text{ m}$        $h_2 = 1.58 \text{ m}$**

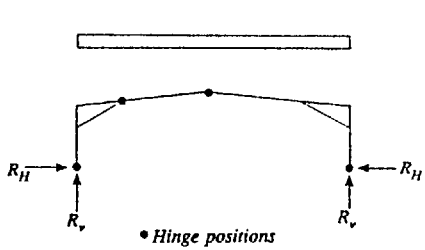
**∴       $L_1 h_1 / h_2 = 68.83 \text{ m}$**

|   |   |  |                                     |
|---|---|--|-------------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>SINGLE STOREY DESIGN</b></p> |  | <p>Chapter ref.</p> <p><b>1</b></p> |
|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p>   | <p>Made by <b>AVP</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no.</p> <p><b>2</b></p>    |

Note that in practice this diagram would be drawn to a greater vertical scale, to assist the determination of  $M_{AB}$ ,  $M_{DC}$  and  $M_{EF}$ .



**Reactions**



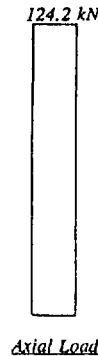
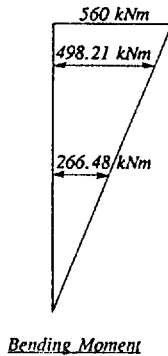
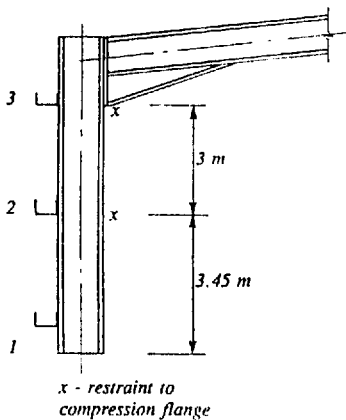
$$R_v = \frac{30 \times 8.28}{2} = 124.20 \text{ kN}$$

$$M_{AB} = 560 \text{ kNm (scaled from diagram)}$$

$$R_H = \frac{M_{AB}}{7.25} = 77.24 \text{ kN}$$


$$M_{DC} = M_{EF} = 250 \text{ kNm (scaled from diagram)}$$

**Stanchion design**




Try 533 × 210 × 82 UB (Grade 43) stanchion

BS 5950:  
Part 1:  
1990

|   |  |   |                          |
|---|--|---|--------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>SINGLE STOREY DESIGN</b> |   | Chapter ref.<br><b>1</b> |
|   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>AVP</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>       |
| <b>Section capacity check</b>   |  |   |                          |
| $F_v = 77.24 \text{ kN}$  |  |   |                          |
| $P_v = 0.6 p_y A_y = 0.6 \times 275 \times 528.3 \times 9.6 \times 10^{-3} = 836.83 \text{ kN}$   |  |   |                          |
| $F_v < 0.6 P_y$ , no reduction in bending capacity due to shear   |  |   |                          |
| $M_{cx} = S_x p_y = 2060 \times 275/10^3 = 566.50 \text{ kN}$   |  |   |                          |
| $P = A_g p_y = 104 \times 275/10 = 2860 \text{ kN}$   |  |   |                          |
| $\frac{F}{P} + \frac{M_x}{M_{cx}} = \frac{124.20}{2860} + \frac{498.21}{566.50} = 0.923 < 1.0$ <u>satisfactory</u>  |  |   |                          |
| <b>Overall buckling check - simplified approach</b>   |  |   |                          |
| $\frac{F}{A_g p_c} + \frac{m M_x}{M_b} \leq 1$  |  |   |                          |
| <b>Length 1 - 2</b>   |  |   |                          |
| $m = 0.57$ , $m M_x = 0.57 \times 266.48 = 151.90 \text{ kNm}$  |  |   |                          |
| For $L_e = 3.45 \text{ m}$ , $M_b = 364 \text{ kNm}$  |  |   |                          |
| $\frac{m M_x}{M_b} = 0.417$   |  |   |                          |
| For $L_e = 3.45 \text{ m}$ , $A_g p_c = 1320 \text{ kN}$  |  |   |                          |
| $\frac{F}{A_g p_c} = 0.094$   |  |   |                          |
| Steelwork Design Guide Vol. 1   |  |   |                          |



|   |   |   |                                 |
|---|---|---|---------------------------------|
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|   | Design code<br><p><b>BS5950: Part 1</b></p>   | Made by <b>AVP</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>              |

$$\therefore \frac{F}{A_g p_c} + \frac{m M_x}{M_b} = 0.511 < 1.00 \text{ satisfactory}$$

A similar exercise for length 2 - 3 gives

$$\frac{F}{A_g p_c} + \frac{m M_x}{M_b} = \frac{124.20}{1420} + \frac{386.17}{453.29} = 0.939 < 1.00 \text{ satisfactory}$$

**Rafter design**

$$M_p = 250 \text{ kNm}$$

$$\text{Minimum, } S_x = \frac{250 \times 10^3}{275} = 909.09 \text{ cm}^3$$

$$\text{Use } 406 \times 178 \times 54 \text{ UB, } S_x = 1050 \text{ cm}^3$$

Clearly,  $S_x$  provided exceeds that required, and economy would be achieved by reducing the haunch length.

Local capacity checks, and overall buckling checks are carried out as shown above, with due cognizance being paid to hinge positions, which should be restrained.

Checks for members containing plastic hinges are covered in BS 5950 Clause 5.3.5 and/or Appendix G.

It is common practice to use proprietary computer programs in the design of portal frames. The above example was analysed with the following results:

$$\begin{aligned} \text{Stanchion moment ( 6.45 m from base )} &= 485 \text{ kNm} \\ \text{Rafter moment ( 3.0 m position )} &= 256 \text{ kNm} \end{aligned}$$

Most programs have the great benefit of performing all the required stability, buckling and deflection checks automatically, together with providing the foundation loads.

# Chapter 2

## Multi-storey buildings

by ALAN HART

### 2.1 Introduction

The term multi-storey building encompasses a wide range of building forms. This chapter reviews some of the factors that should be considered when designing the type of multi-storey buildings commonly found in Europe, namely those less than 15 storeys in height. Advice on designing taller buildings may be found in the references to this chapter.<sup>1-5</sup>

#### 2.1.1 The advantages of steel

In recent years the development of steel-framed buildings with composite metal deck floors has transformed the construction of multi-storey buildings in the UK. During this time, with the growth of increasingly sophisticated requirements for building services, the very efficiency of the design has led to the steady decline of the cost of the structure as a proportion of the overall cost of the building, yet the choice of the structural system remains a key factor in the design of successful buildings.

The principal reasons for the appeal of steel for multi-storey buildings are noted below.

- Steel frames are fast to erect.
- The construction is lightweight, particularly in comparison with traditional concrete construction.
- The elements of the framework are prefabricated and manufactured under controlled, factory conditions to established quality procedures.
- The accuracy implicit in the manufacturing process by which the elements are produced enables the designer to take a confident view of the geometric properties of the erected framework.
- The dryness of the form of construction results in less on-site activities, plant, materials and labour.
- The framework is not susceptible to drying-out movement or delays due to slow strength gain.
- Steel frames have potential for adaptability inherent in their construction.

Later modification to a building can be achieved relatively easily by unbolting a connection: with traditional concrete construction such modifications would be expensive, and more extensive and disruptive.

- The use of steel makes possible the creation of large, column-free internal spaces which can be divided by partitions and, by eliminating the external wall as a load-bearing element, allows the development of large window areas incorporated in prefabricated cladding systems.

### 2.1.2 Design aims

For the full potential of the advantages of steel-frame construction to be realized, the design of multi-storey buildings requires a considered and disciplined approach by the architects, engineers and contractors involved in the project. They must be aware of the constraints imposed on the design programme by the lead time between placing a contract for the supply of the steel frame and the erection of the first pieces on site. The programme should include such critical dates on information release as are necessary to ensure that material order and fabrication can progress smoothly.

The designer must recognize that the framework is the skeleton around which every other element of the building will be constructed. The design encompasses not only the structure but also the building envelope, services and internal finishes. All these elements must be co-ordinated by a firm dimensional discipline, which recognizes the modular nature of the components, to ensure maximum repetition and standardization. Consequently it is impossible to consider the design of the framework in isolation. It is vital to see the frame as part of an integrated building design from the outset: the most efficient solution for the structure may not be effective in achieving a satisfactory solution for the total building.

In principle, the design aims can be considered under three headings:

- Technical
- Architectural
- Financial.

#### *Technical aims*

The designer must ensure that the framework, its elements and connections are strong enough to withstand the applied loads to which the framework will be subjected throughout its design life. The system chosen on this basis must be sufficiently robust to prevent the progressive collapse of the building or a significant part of it under accidental loading. This is the primary technical aim. However, as issues related to strength have become better understood and techniques for the

strength design of frameworks have been formalized, designers have progressively used lighter and stronger materials. This has generated a greater need to consider serviceability, including dynamic floor response, as part of the development of the structural concept.

Other important considerations are to ensure adequate resistance to fire and corrosion. The design should aim to minimize the cost, requirements and intrusion of the protection systems on the efficiency of the overall building.

### *Architectural aims*

For the vast majority of buildings the most effective structural steel frame is the one which is least obtrusive. In this way it imposes least constraint on internal planning, and produces maximum usable floor area, particularly for open-plan offices. It also provides minimal obstruction to the routing of building services. This is an important consideration, particularly since building services are becoming more extensive and demanding on space and hence on the building framework.

Occasionally the structure is an essential feature of the architectural expression of the building. Under these circumstances the frame must achieve, among other aims, a balance between internal planning efficiency and an expressed structural form. However, these buildings are special, not appropriate to this manual, and will not be considered in more detail, except to give a number of references.

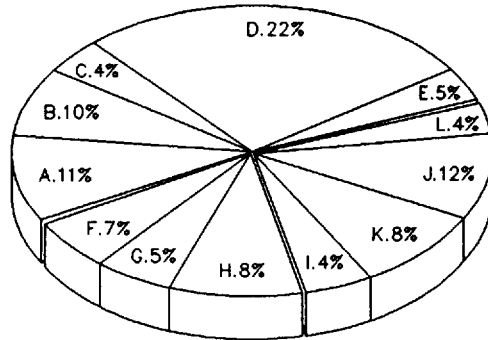
### *Financial aims*

The design of a steel frame should aim to achieve minimum overall cost. This is a balance between the capital cost of the frame and the improved revenue from early occupation of the building through fast erection of the steel frame: a more expensive framework may be quicker to build and for certain uses would be more economic to a client in overall terms. Commercial office developments are a good example of this balance. Figure 2.1 shows a breakdown of construction costs for a typical development.

## **2.1.3 Influences on overall design concept**

### *Client brief*

Clients specify their requirements through a brief. It is essential for effective design to understand exactly the intentions of the client: the brief is the way in which the client expresses and communicates these intentions. As far as the frame designer is concerned, the factors which are most important are intended use, budget cost limits, time to completion and quality. Once these are understood a



|   |            |
|---|------------|
| <b>Fabric</b>   |            |
| A Demolition, Piling foundations and concrete work..... | 11%        |
| B Steel Frame, Deck and Fire Protection.....            | 10%        |
| C Brickwork and Drywalling.....                         | 4%         |
| D External and Internal Cladding and Sunscreens.....    | 22%        |
| E Roofing and Rooflights.....                           | 5%         |
|   | <u>52%</u> |
| <b>Finishes</b>   |            |
| F Ceilings and Floors..                                 | 7%         |
| G Stone .....   | 5%         |
| H Others .....  | 8%         |
|   | <u>20%</u> |
| <b>Services</b>   |            |
| I Plumbing and Sprinklers..                             | 4%         |
| J H.V.A.C.....  | 12%        |
| K Electrics .....                                       | 8%         |
| L Lifts .....   | 4%         |
|   | <u>28%</u> |

Fig. 2.1 Typical cost breakdown

realistic basis for producing the design will be established. The designer should recognize however that in practice the brief is likely to evolve as the design develops.

*Statutory constraints*

The design of all buildings is subject to some form of statutory constraint. Multi-storey buildings, particularly those in an urban environment, are subject to a high level of constraint which will generally be included in the conditions attached to the granting of Outline Planning Permission. The form and degree that this may take could have significant impact on the frame design. For example, street patterns and lighting restrictions may result in a non-rectilinear plan with a 'stepped-back' structure. If an appropriate layout is to be provided it is vital to understand these constraints from the outset.

### *Physical factors*

The building must be designed to suit the parameters determined by its intended use and its local environment.

Its intended use will dictate the intensity of imposed loadings, the fire protection and corrosion resistance requirements and the scope of building services.

The local environment will dictate the lateral load requirements but more importantly it will determine the nature of the existing ground conditions. To achieve overall structural efficiency it is essential that the structural layout of the frame is responsive to the constraints imposed by these ground conditions.

These factors are considered in more detail in the next section.

## **2.2 Factors influencing choice of form**

### *Environmental*

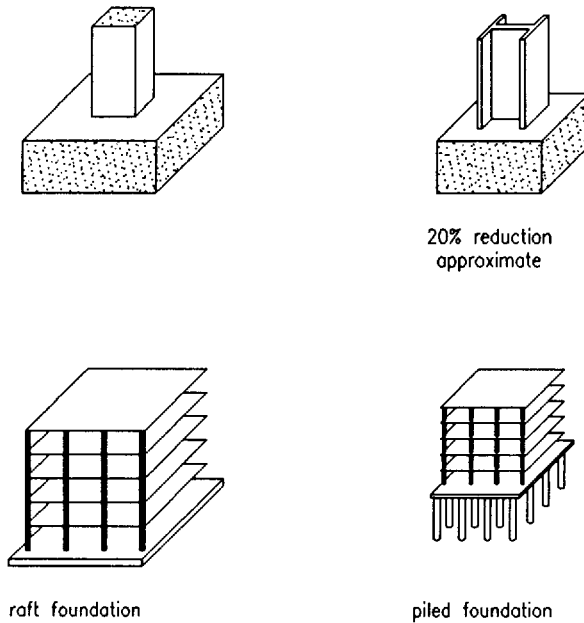
There are a number of factors which influence the choice of structural form that are particular to the site location. These can have a dominant effect on the framing arrangement for the structure.

The most obvious site-dependent factors are related to the ground conditions. A steel-framed building is likely to be about 60% of the weight of a comparable reinforced concrete building. This difference will result in smaller foundations with a consequent reduction on costs. In some cases this difference in weight enables simple pad foundations to be used for the steel frame where the equivalent reinforced concrete building would require a more complex and expensive solution. For non-uniformly loaded structures it will also reduce the magnitude of differential settlements and for heavily loaded structures may make possible the use of a simple raft foundation in preference to a large capacity piled solution (Fig. 2.2).

Difficult ground conditions may dictate the column grid. Long spans may be required to bridge obstructions in the ground. Such obstructions could include, for example, buried services, underground railways or archaeological remains. Generally, a widely spaced column grid is desirable since it reduces the number of foundations and increases the simplicity of construction in the ground.

Other site-dependent constraints are more subtle. In urban areas they relate to the physical constraints offered by the surrounding street plan, and the rights of light of adjoining owners. They also relate to the planning and architectural objectives for specific sites. The rights of light issues or planning considerations may dictate that upper floors are set back from the perimeter resulting in stepped construction of the upper levels. Invariably the resulting framing plan is not rectilinear and may have skew grids, cantilevers and re-entrant corners.

These constraints need to be identified early in the design in order that they are accommodated efficiently into the framing. For example, wherever possible,



*Fig. 2.2* Foundation savings

stepped-back façades should be arranged so that steps take place on the column grid and hence avoid the need for heavy bridging structures. In other situations the designer should always investigate ways in which the impact of lack of uniformity in building form can be contained within a simple structural framing system which generates a minimum of element variations and produces simple detailing.

*Building use*

The building use will dictate the planning module of the building which will in turn determine the span and column grids. Typical grids may be based on a planning module of 600/1200 mm or 500/1500 mm. However, the use has much wider impact, particularly on floor loadings and building services. The structural arrangement, and depth selected, must satisfy and accommodate these requirements.

For example, financial-dealing floors require clear open spaces located on the lower floors which would dictate a different structural solution to the rest of the building. This may necessitate the use of a transfer structure to carry the upper floors on an economical column grid (Fig. 2.3).

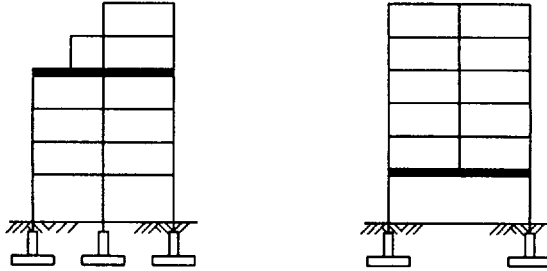


Fig. 2.3 Typical load transfer systems

### *Floor loadings*

Because steel-framed buildings are relatively light in weight, excessive imposed loadings will have a greater effect on the sizing of structural components, particularly floor beams, than with reinforced concrete structures.

The floor loadings to be supported by the structure have two components:

- The permanent or dead loading comprising the self-weight of the flooring and the supporting structure together with the weight of finishes, raised flooring, ceiling, air-conditioning ducts and equipment.
- The imposed loading which is the load that the floor is likely to sustain during its life and will depend on the building use. Imposed floor loads for various types of building are governed by BS 6399 but the standard loading for office buildings is usually  $4 \text{ kN/m}^2$  with an additional allowance of  $1 \text{ kN/m}^2$  for movable partitioning.

For normal office loadings, dead and imposed loadings are roughly equal in proportion but higher imposed load allowances will be necessary in plantrooms or to accommodate special requirements such as storage or heavy equipment.

Floor beams will be designed to limit deflection under the imposed loadings. British Standard BS 5950 governing the design of structural steelwork sets a limit for deflection under imposed loading of (span/200) generally and (span/360) where there are brittle finishes. Edge beams supporting cladding will be subject to restriction on deflection of 10–15 mm. Deflections may be noticeable in the ceiling layout and should be taken into account when determining the available clearance for service routes. The designer should therefore check the cumulative effect of deflections in the individual members of a floor system although the actual maximum displacement is in practice almost always less than that predicted. In some instances, vibrations of floor components may cause discomfort or affect sensitive equipment and the designer should check the fundamental frequency of the floor system. The threshold of perceptible vibrations in building is difficult to define and present limits are rather arbitrary. There is some evidence that modern



long span, lightweight floors can be sensitive to dynamic loads which may have an effect on delicate equipment.

*Building services and finishes*

In buildings requiring anything other than minimal electrical services distribution, the inter-relationship of the structure, the mechanical and electrical services and the building finishes will need to be considered together from the outset.

It is essential to co-ordinate the details of the building services, cladding and structure at an early stage of the project in order to produce a building which is simple to fabricate and quick to erect. Apparently minor variations to the steelwork, brought about by services and finishes requirements, defined after a steel fabrication contract has been let, can have a disproportionate effect on the progress of fabrication and erection. Steel buildings impose a strict discipline on the designer in terms of the early production of final design information. If the designer fails to recognize this, the advantages of steel-framed building cannot be realized.

The integration of the building services with the structure is an important factor in the choice of an economic structural floor system. The overall depth of the floor construction will depend on the type and distribution of services in the ceiling void. The designer may choose to separate the structural and services zones or accommodate the services by integrating them with the structure allowing for the structural system to occupy the full depth of the floor construction. (See Fig. 2.4).

Separation of zones usually requires confining the ducts, pipes and cables to a horizontal plane below the structure resulting in either a relatively deep overall floor construction or close column spacings. Integration of services with structure requires either deep perforated structural components or vertical zoning of the services and structure.

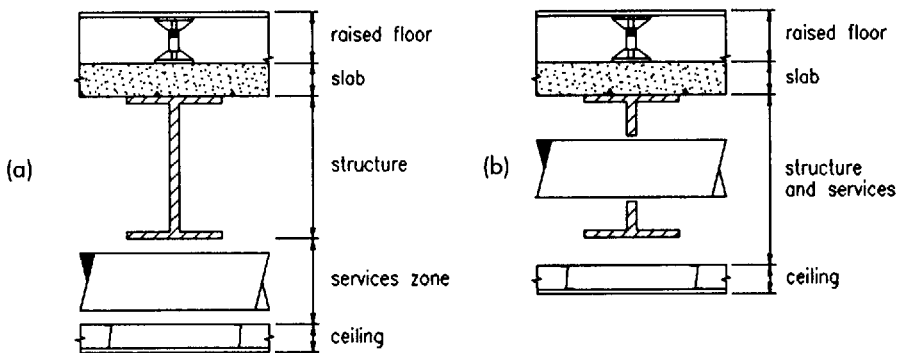


Fig. 2.4 Building services and floor structure: (a) separation of services and structure; (b) integration of services and structure

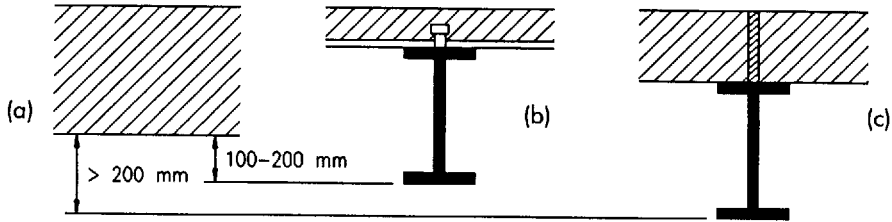


Fig. 2.5 Overall floor depths: (a) R.C. flat slab; (b) composite; (c) non-composite

For the range of structural grids used in conventional building, traditional steel floor construction is generally deeper than the equivalent reinforced concrete flat slab: the difference is generally 100–200 mm for floor structures which utilize composite action and greater for non-composite floors (Fig. 2.5). The increased depth is only at the beam position: elsewhere, between beams, the depth is much less and the space between them may accommodate services, particularly if the beams may be penetrated (Fig. 2.6). The greater depth of steel construction does not therefore necessarily result in an increase in building height if the services are integrated within the zone occupied by the structure. A number of possible solutions exist for integrated systems, particularly in long-span structures utilizing castellated or stub-girder beams. (See Fig. 2.7.)

Recently a number of solutions have been developed which allow long spans to co-exist with separation of the building services by profiling the steel beam to provide space for services, either at the support or in the span. The concept of this approach is not new; the innovation has come from the use of automated plate cutting and welding techniques to produce economical profiled plate girders. (See Fig. 2.8.)

Overall depth may be reduced by utilizing rigid or semi-rigid rather than simple connections at the ends of the beams. This reduces the maximum bending moment and deflection. However, such solutions are not as efficient as would first appear since the non-composite section at the support is much less efficient than the

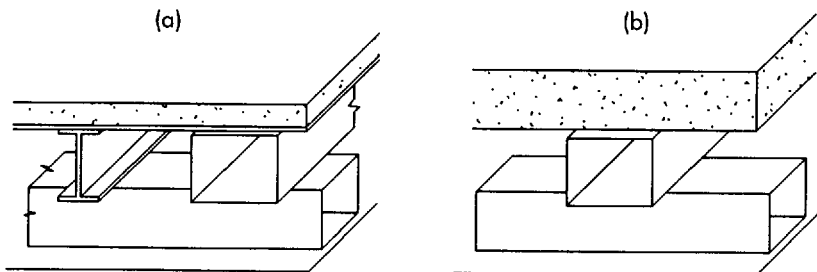


Fig. 2.6 Ceiling voids: (a) steel frame: variable void height; (b) concrete slab: constant void height

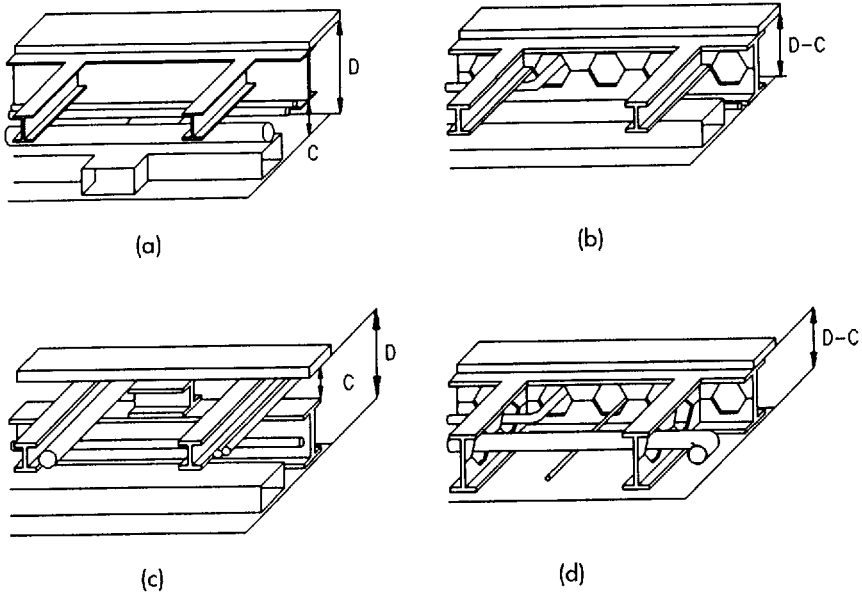


Fig. 2.7 Integration of services: (a) separated (traditional); (b) integrated (short-medium span 'secondary' beams); (c) integrated (long span 'primary' beam – stub girder); (d) integrated (long span 'secondary' beams)

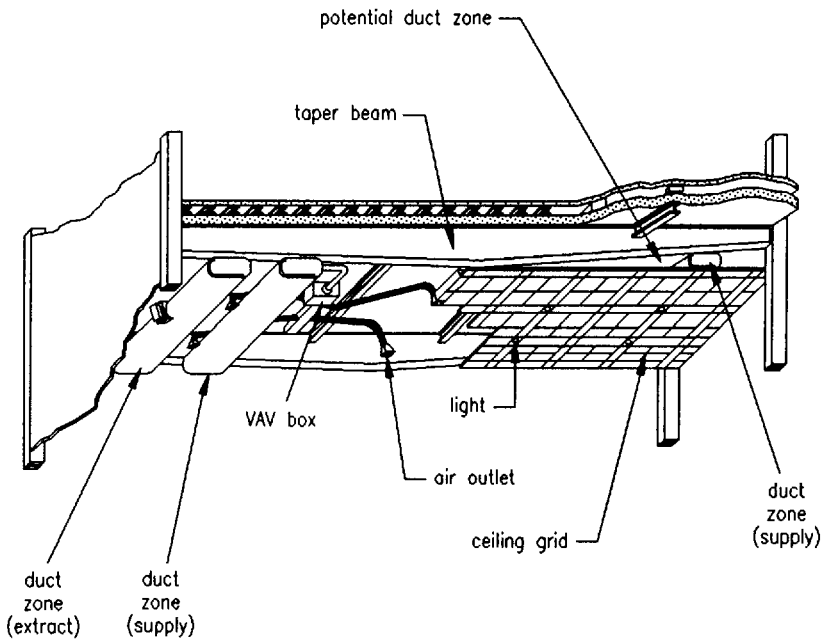


Fig. 2.8 Tapered beams and services

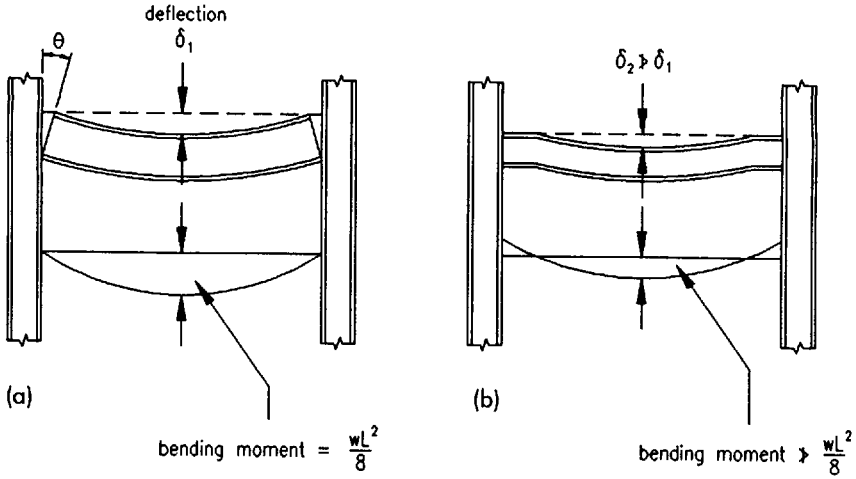


Fig. 2.9 Floor depth, (a) simple and (b) rigid

composite section at mid-span. Indeed, if the support bending moments are large in comparison to the span bending moments the depth may be greater than the simply-supported composite beam. This is an expensive fabrication in comparison to straight rolled beam sections. (See Fig. 2.9.) In addition, the use of rigid joints can increase column sizes considerably.

The overall depth may also be reduced by using higher-strength steel, but this is only of advantage where the element design is controlled by strength. The stiffness characteristics of both steels are the same; hence, where deflection or vibration govern, no advantage is gained by using the stronger steel.

### *External wall construction*

The external skin of a multi-storey building is supported off the structural frame. In most high quality commercial buildings the cost of external cladding systems greatly exceeds the cost of the structure. This influences the design and construction of the structural system in a number of ways:

- The perimeter structure must provide a satisfactory platform to support the cladding system and be sufficiently rigid to limit deflections of the external wall.
- A reduction to the floor zone may be more cost-effective than an overall increase in the area of cladding.
- Fixings to the structure should facilitate rapid erection of cladding panels.
- A reduction in the weight of cladding at the expense of cladding cost will not necessarily lead to a lower overall construction cost.

### *Lateral stiffness*

Steel buildings must have sufficient lateral stiffness and strength to resist wind and other lateral loads. In tall buildings the means of providing sufficient lateral stiffness forms the dominant design consideration. This is not the case for low- to medium-rise buildings.

Most multi-storey buildings are designed on the basis that wind forces acting on the external cladding are transmitted to the floors which form horizontal diaphragms transferring the lateral load to rigid elements and then to the ground. These rigid elements are usually either braced-bay frames, rigid-jointed frames or reinforced concrete shear walls.

British Standard BS 5950 sets a limit on lateral deflection of columns as height/300 but height/600 may be a more reasonable figure for buildings where the external envelope consists of sensitive or brittle materials such as stone facings.

### *Accidental loading*

A series of incidents in the 1960s culminating in the partial collapse of a system-built tower block at Ronan Point in 1968 led to a fundamental reappraisal of the approach to structural stability in building.

Traditional load-bearing masonry buildings have many in-built elements providing inherent stability which are lacking in modern steel-framed buildings. Modern structures can be refined to a degree where they can resist the horizontal and vertical design loadings with the required factor of safety but may lack the ability to cope with the unexpected.

It is this concern with the safety of the occupants and the need to limit the extent of any damage in the event of unforeseen or accidental loadings that has led to the concept of robustness in building design. Any element in the structure that supports a major part of the building either must be designed for blast loading or must be capable of being supported by an alternative load path. In addition, suitable ties should be incorporated in the horizontal direction in the floors and in the vertical direction through the columns. The designer should be aware of the consequences of the sudden removal of key elements of the structure and ensure that such an event does not lead to the progressive collapse of the building or a substantial part of it. In practice, most modern steel structures can be shown to be adequate without any modification.

### *Cost considerations*

The time taken to realize a steel building from concept to completion is generally less than that for a reinforced concrete alternative. This reduces time-related building costs, enables the building to be used earlier and produces an earlier return on the capital invested.

To gain full benefit from the 'factory' process and particularly the advantages of

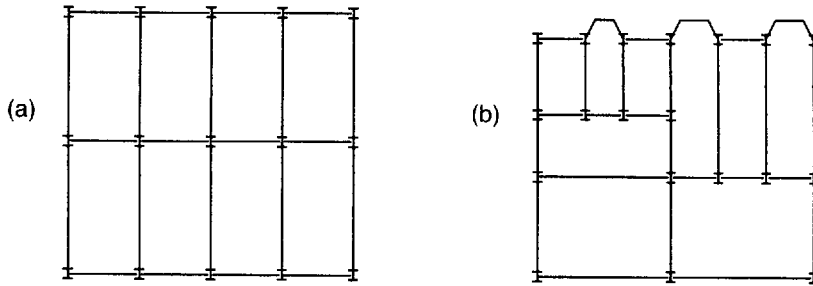


Fig. 2.10 Structural costs: (a) economic and (b) uneconomic layouts

speed of construction, prefabrication, accuracy and lightness, the cladding and finishes of the building must have similar attributes. The use of heavy, slow and in situ finishing materials is not compatible with the lightweight, prefabricated and fast construction of a steel framework.

The cost of steel frameworks is governed to a great extent by the degree of simplicity and repetition embodied in the frame components and connections. This also applies to the other elements which complete the building.

The criterion for the choice of an economic structural system will not necessarily be to use the minimum weight of structural steel. Material costs represent only 30–40% of the total cost of structural steelwork. The remaining 60–70% is accounted for in the design, detailing, fabrication, erection and protection. Hence a choice which needs a larger steel section to avoid, say, plate stiffeners around holes or allows greater standardization will reduce fabrication costs and may result in the most economic overall system.

Because a steel framework is made up of prefabricated components produced in a factory, repetition of dimensions, shapes and details will streamline the manufacturing process and are major factors in economic design (Fig. 2.10).

### *Fabrication*

The choice of structural form and method of connection detailing have a significant impact on the cost and speed of fabrication and erection. Simple braced frameworks with bolted connections are considered the most economic and the fastest to build for low- to medium-rise buildings.

Economy is generally linked to the use of standard rolled sections but, with the advent of automated cutting and welding equipment, special fabricated sections are becoming economic if there is sufficient repetition.

The development of efficient, automated, cold-sawing techniques and punching and drilling machines has led to the fabrication of building frameworks with bolted assemblies. Welded connections involve a greater amount of handling in the fabrication shop, with consequent increases in labour and cost.

Site-welded connections require special access, weather protection, inspection

and temporary erection supports. By comparison, on-site bolted connections enable the components to be erected rapidly and simply into the frame and require no further handling.

The total weight of steel used in rigid frames is less than in simple frames, but the connections for rigid frames are more complex and costly to fabricate and erect. On balance, the cost of a rigid frame structure is greater, but there may be other considerations which offset this cost differential. For example, in general the overall structural depth of rigid frames is less. This may reduce the height of the building or improve the distribution of building services, both of which could reduce the overall cost of the building.

Corrosion protection to internal building elements is an expensive and time-consuming activity. Experience has shown that it is unnecessary for most internal locations and consequently only steelwork in risk areas should require any protection.

### *Construction*

A period of around 10–14 weeks is usual between placing a steel order and the arrival of the first steel components on site. Site preparation and foundation construction generally take a similar or longer period (see Fig. 2.11). Hence, by progressing fabrication in parallel with site preparation, significant on-site construction time may be saved, as commencement of shop fabrication is equivalent to start-on-site for an in situ concrete-framed building. By manufacturing the frame in a factory, the risks of delay caused by bad weather or insufficient or inadequate construction resources in the locality of the site are significantly reduced.

Structural steel frameworks should generally be capable of being erected without temporary propping or scaffolding, although temporary bracing will be required, especially for welded frames. This applies particularly to the construction of the concrete slab which should be self-supporting at all stages of erection. Permanent metal or precast concrete shutters should be used to support the in situ concrete.

In order to allow a rapid start to construction, the structural steelwork frame should commence at foundation level and preference should be given to single foundations for each column rather than raft or shared foundations (Fig. 2.12).

Speed of erection is directly linked to the number of crane hours available. To reduce the number of lifts required on site, the number of elements forming the framework should be minimized within the lifting capacity of the craneage provided on site for other building components. For similar sized buildings, the one with the longer spans and fewer elements will be the fastest to erect. However, as has been mentioned earlier, longer spans require deeper, heavier elements which will increase the cost of raw materials and pose a greater obstruction to the distribution of building services thereby requiring the element to be perforated or shaped and hence increasing the cost of fabrication.

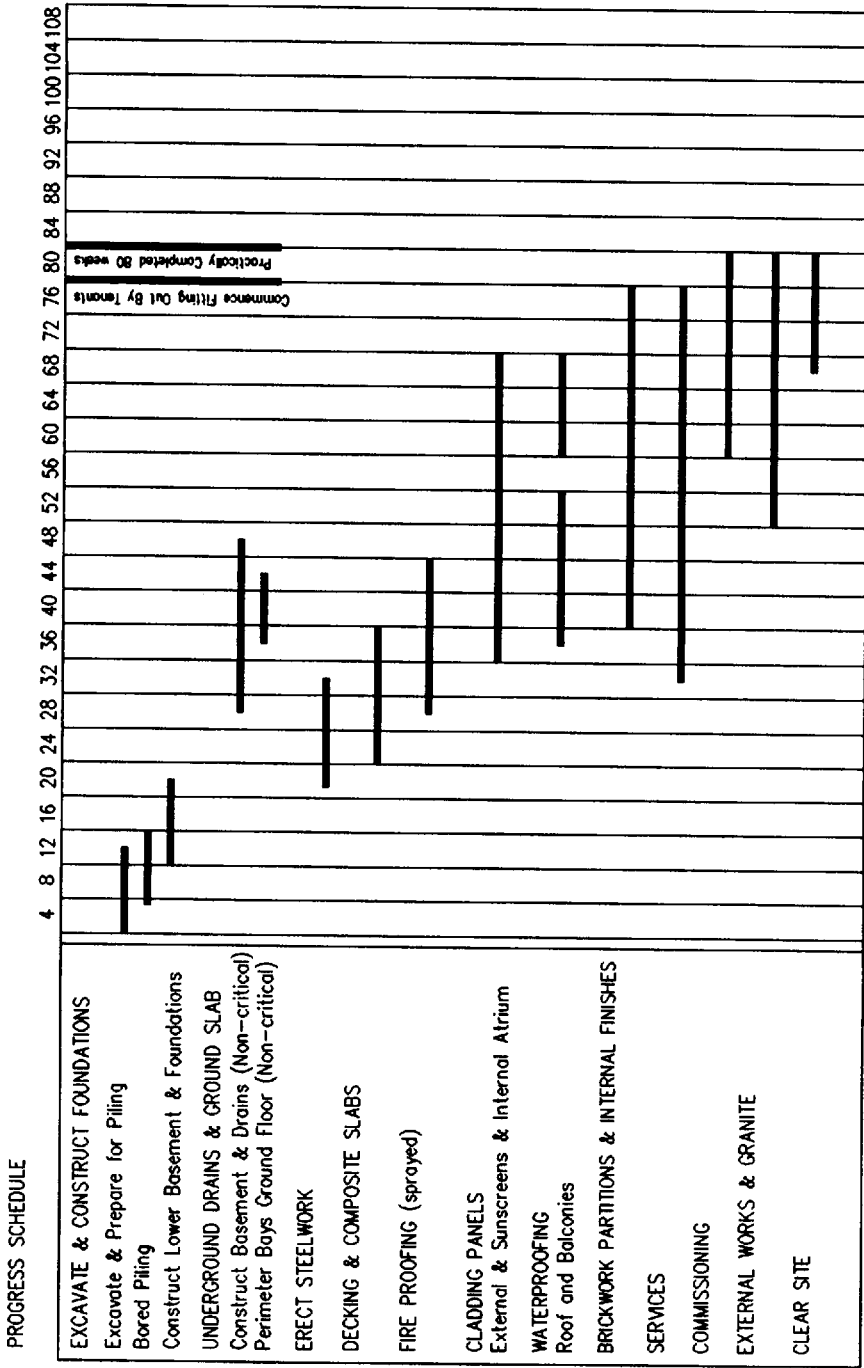


Fig. 2.11 Typical progress schedule (in weeks)



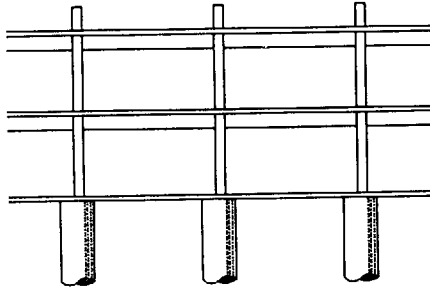


Fig. 2.12 Columns on large diameter bored piles

Columns are generally erected in multi-storey lengths; two is common and three is not unusual. The limitation on longer lengths is related more to erection than restrictions on transportation, although for some urban locations, length is a major consideration for accessibility.

To provide rapid access to the framework the staircases should follow the erection of the frame. This is generally achieved by using prefabricated stairs which are detailed as part of the steel frame.

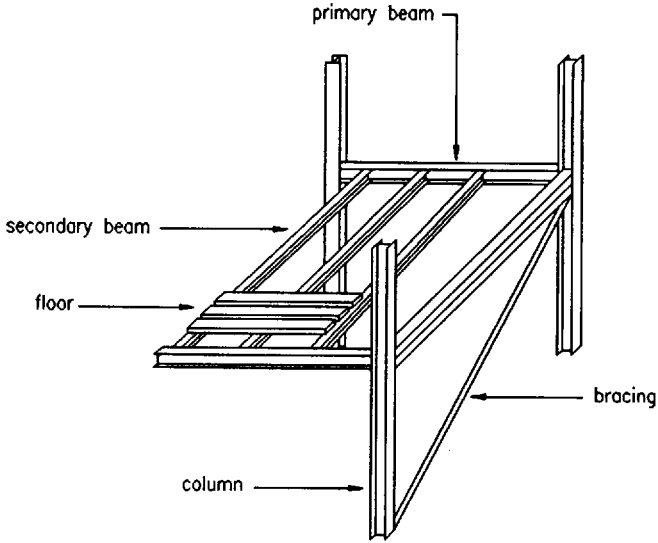
The speed of installation of the following building elements is hastened if their connection and fixing details are considered at the same time as the structural steel frame design. In this way the details can either be incorporated in the framework or separated from it, whichever is the most effective overall: it is generally more efficient to separate the fixings and utilize the high inherent accuracy of the frame to use simple post-fixed details, provided these do not require staging or scaffolding to give access.

Finally, on-site painting extends the construction period and provides potential compatibility problems with following applied fire protection systems. Painting should therefore only be specified when absolutely necessary.

### 2.3 Anatomy of structure

In simple terms, the vertical load-carrying structure of a multi-storey building comprises a system of vertical column elements interconnected by horizontal beam elements which support floor-element assemblies. The resistance to lateral loads is provided by diagonal bracing elements, or wall elements, introduced into the vertical rectangular panels bounded by the columns and beams to form vertical trusses, or walls, called 'no-sway' frames. Alternatively, lateral resistance may be provided by developing a rigid-frame action between the beams and columns, called 'sway' frames. The floor-element assemblies provide the resistance to lateral loads in the horizontal plane.

In summary, the components of a building structure are columns, beams, floors and bracing systems (Fig. 2.13).



*Fig. 2.13* Steel frame components

### 2.3.1 Columns

These are generally standard, universal column, hot-rolled sections. They provide a compact, efficient section for normal building storey heights. Also, because of the section shape, they give unobstructed access for beam connections to either the flange or web. For a given overall width and depth of section, there is a range of weights which enable the overall dimensions of structural components to be maintained for a range of loading intensities.

Where the loading requirements exceed the capacity of standard sections, additional plates may be welded to the section to form plated columns, or fabricated columns may be formed by welding plates together to form a plate-column (Fig. 2.14).

The use of circular or rectangular tubular elements marginally improves the load-carrying efficiency of components as a result of their higher stiffness-to-weight ratio. However, connections to beams become more complicated.

### 2.3.2 Beams

Structural steel floor systems consist of prefabricated standard components, and columns should be laid out on a repetitive grid which establishes a standard structural bay. For most multi-storey buildings, functional requirements will deter-

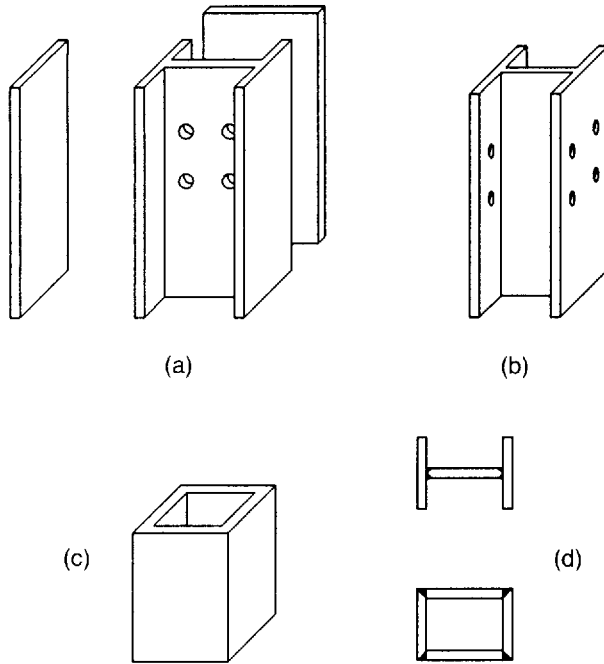


Fig. 2.14 Types of column: (a) plated (by addition of plates to U.C. section); (b) universal; (c) tubular; (d) fabricated plate

mine the column grid which will dictate spans where the limiting criterion will be stiffness rather than strength (Fig. 2.15).

Steel components are uni-directional and consequently orthogonal structural column and beam grids have been found to be the most efficient. The most efficient floor plan is rectangular, not square, in which main, or 'primary', beams span the shorter distance between columns and closely-spaced 'secondary' floor beams span the longer distance between main beams. The spacing of the floor beams is controlled by the spanning capability of the concrete floor construction (Fig. 2.16).

Having decided on the structural grid, the designer must choose an economic structural system to satisfy all the design constraints. The choice of system and its depth depends on the span of the floor (Fig. 2.17). The minimum depth is fixed by practical considerations such as fitting practical connections. As the span increases, the depth will be determined by the bending strength of the member and, for longer spans, by the stiffness necessary to prevent excessive deflection under imposed load or excessive sensitivity to induced vibrations (Fig. 2.18). For spans up to 10–12 m, simple universal beams with precast floors or composite metal deck floors are likely to be most economic. A range of section capacities for each depth enables a constant depth of construction to be maintained for a range

Steelwork Plan Level 3

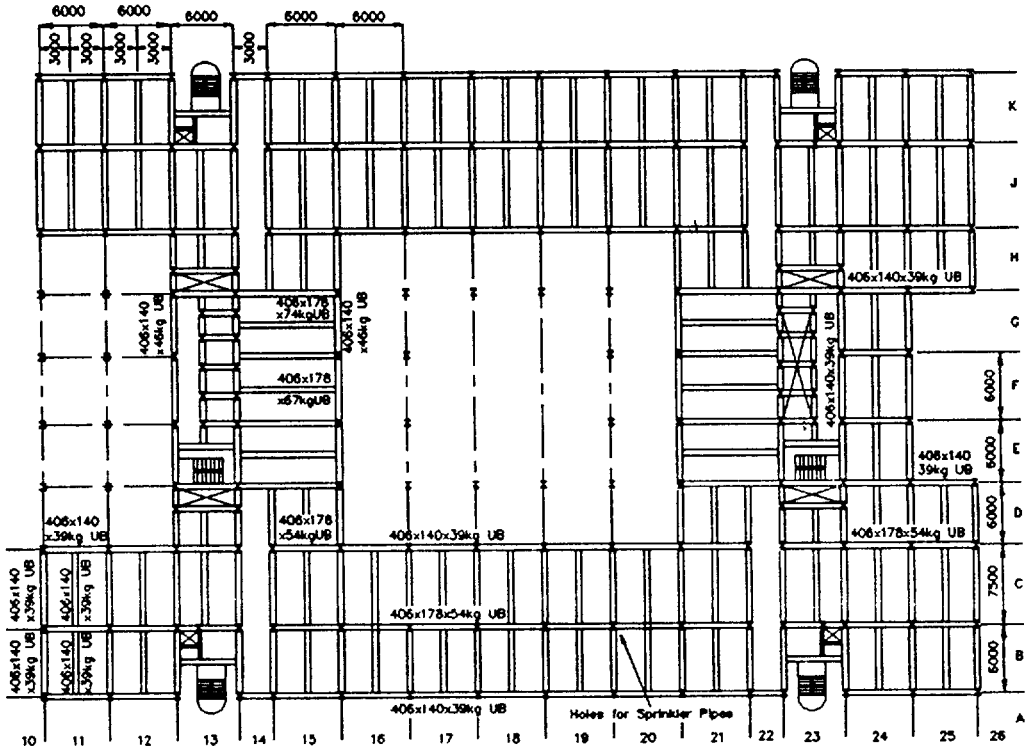


Fig. 2.15 Typical floor layout

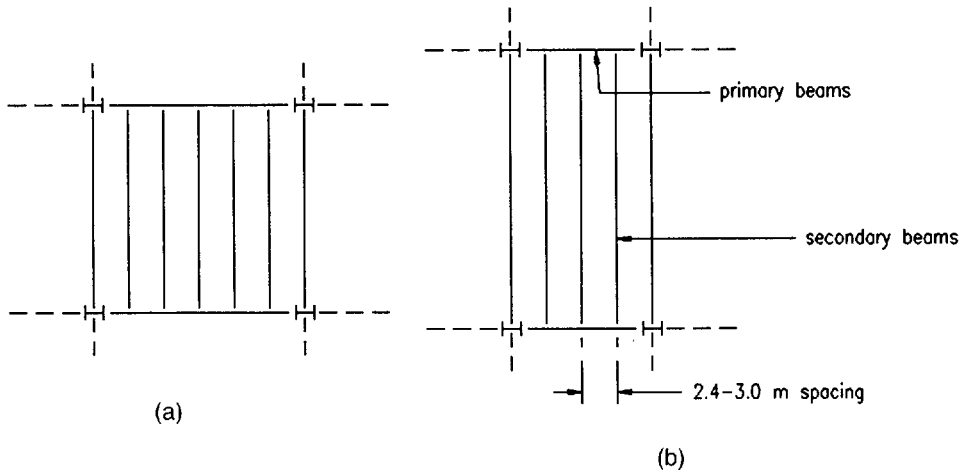


Fig. 2.16 Beam layout: (a) inefficient; (b) efficient

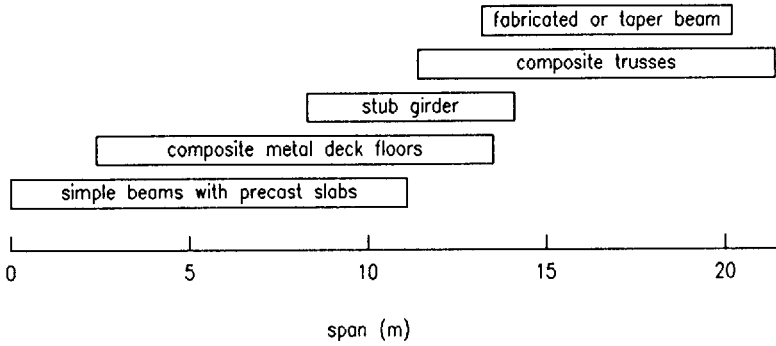


Fig. 2.17 Choice of floor system

of spans and loading. As with column components, plated-beams and fabricated girders may be used for spans above 10–12 m. They are particularly appropriate where heavier loading is required and overall depth is limited. For medium- to lightly-loaded floors and long spans, beams may also take the form of castellated beams fabricated from standard sections. Above 15 m, composite steel trusses may be economic. As the span increases the depth and weight of the structural floor increase and above 15 m spans, depth predominates because of the need to achieve adequate stiffness.

*Castellated beam sections*

Castellated beams (Fig. 2.19) have been used for many years to increase the bending capacity of the beam section and to provide limited openings for services. These openings are rarely of sufficient size for ducts to penetrate without significant

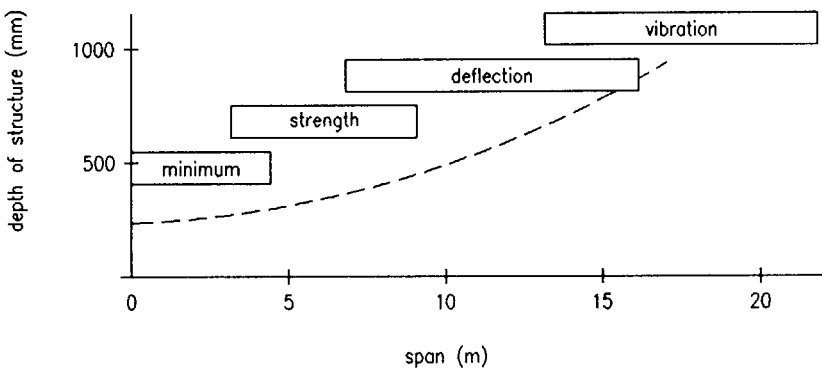
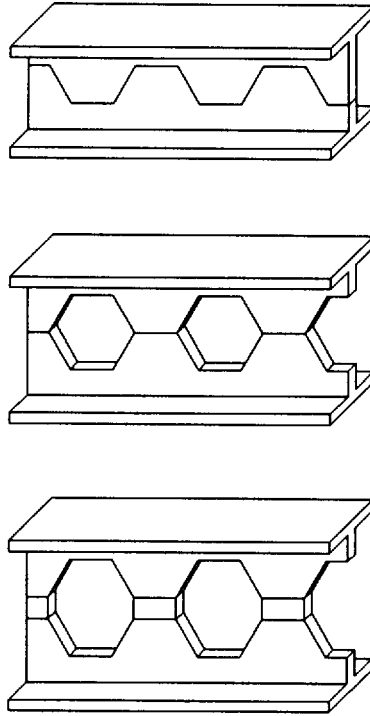


Fig. 2.18 Structural criteria governing choice



*Fig. 2.19* Castellated beams

modification and fabrication costs are high. The cellform concept is a development of castellated beams that provides circular spans and greater shear capacity.

### *Fabricated plate girders*

Conventional universal beams span a maximum of about 15 m. Recent advances in automatic and semi-automatic fabrication techniques have allowed the economic production of plate girders for longer span floors. Particularly if a non-symmetric plate girder is used, it is possible to achieve economic construction well in excess of 15 m. (Fig. 2.20.)

### *Taper beams*

Taper beams (Fig. 2.20) are similar to fabricated plate girders except that their depth varies from a maximum in mid-span to a minimum at supports thus achieving a highly efficient structural configuration. For simply-supported composite taper beams in buildings the integration of the services can be accommodated by

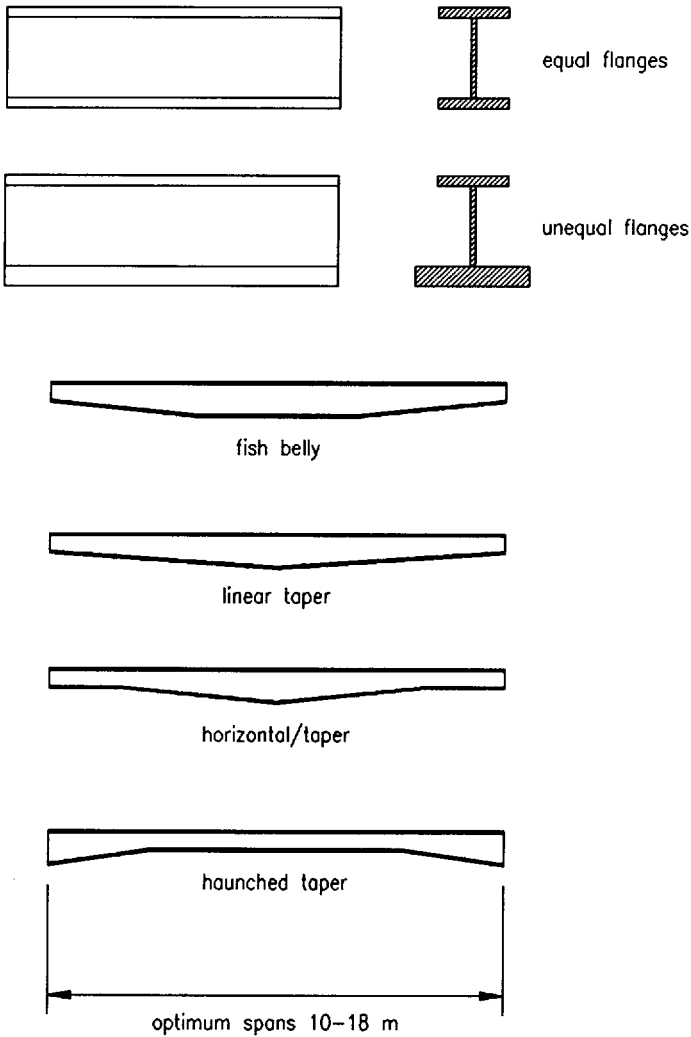


Fig. 2.20 Fabricated plate girders and taper beams

locating the main ducts close to the columns. Alternative taper beam configurations can be used to optimize the integration of the building services.

*Composite steel floor trusses*

Use of composite steel floor trusses as primary beams in the structural floor system permits much longer spans than would be possible with conventional universal beams. The use of steel trusses for flooring systems is common for multi-

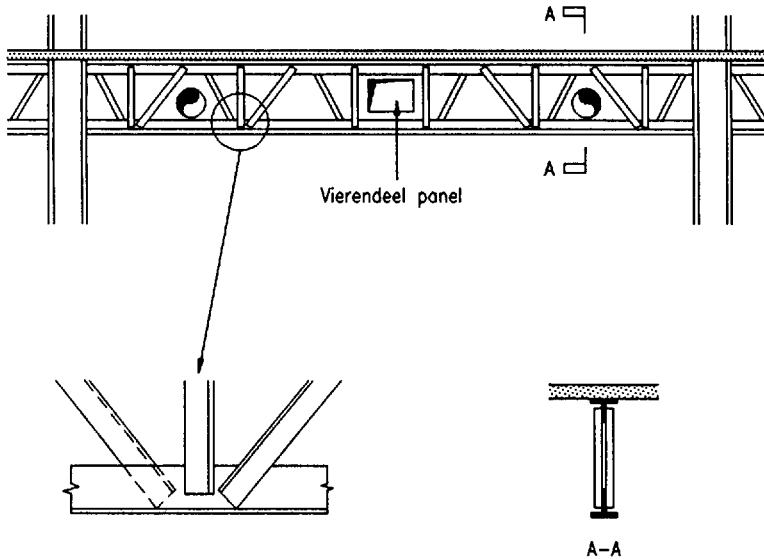


Fig. 2.21 Composite truss

storey buildings in North America but seldom is used in Britain. Although they are considerably lighter than the equivalent universal beam section the cost of fabrication is very much greater as is the cost of fireproofing the truss members. For maximum economy, trusses should be fabricated from T-sections and angles using simple welded lap joints. The openings between the diagonal members should be designed to accept service ducts and if a larger opening is required a Vierendeel panel can be incorporated at the centre of the span. Because a greater depth is required for floor trusses, the integration of the services is always within the structural zone. (Fig. 2.21.)

### *Stub girder construction*

Stub girders were developed in North America in the 1970s as an alternative form of construction for intermediate range spans of between 10–14 m. They have not been used significantly in the UK. Figure 2.22 shows a typical stub girder with a bottom chord consisting of a compact universal column section which supports the secondary beams at approximately 3-metre centres. Between the secondary beams a steel stub is welded on to the bottom chord to provide additional continuity and to support the floor slab. The whole system acts as a composite Vierendeel truss. A disadvantage of stub girders is that the construction needs to be propped while the concrete is poured and develops strength. Arguably, a deep universal beam with large openings provides a more cost-effective alternative to the stub girder because of the latter's high fabrication content.



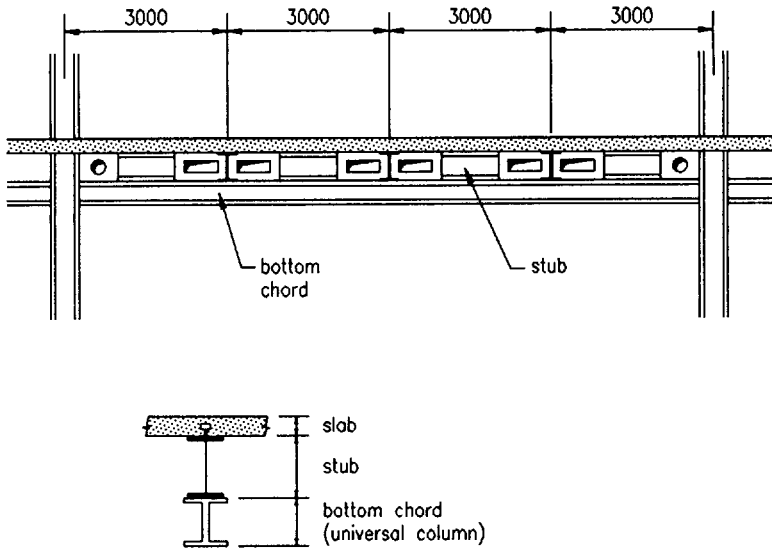


Fig. 2.22 Stub girder

### 2.3.3 Floors

These take the form of concrete slabs of various forms of construction spanning between steel floor beams (Fig. 2.23). The types generally found are:

- in situ concrete slab cast on to permanent profiled metal decking, acting compositely with the steel floor beams;
- precast concrete slabs acting non-compositely with the floor beams;
- in situ concrete slab, with conventional removable shuttering, acting compositely with the floor beams;
- in situ concrete slab cast on thin precast concrete slabs to form a composite slab, which in turn acts compositely with the floor beams.

The most widely used construction internationally is profiled metal decking. Composite action with the steel beam is provided by shear connectors welded through the metal decking on to the beam flange. Precast concrete systems are, however, still used extensively in the UK.

#### *Metal deck floor construction*

Composite action enables the floor slab to work with the beam enhancing its strength and reducing deflection (Fig. 2.24). Because composite action works by

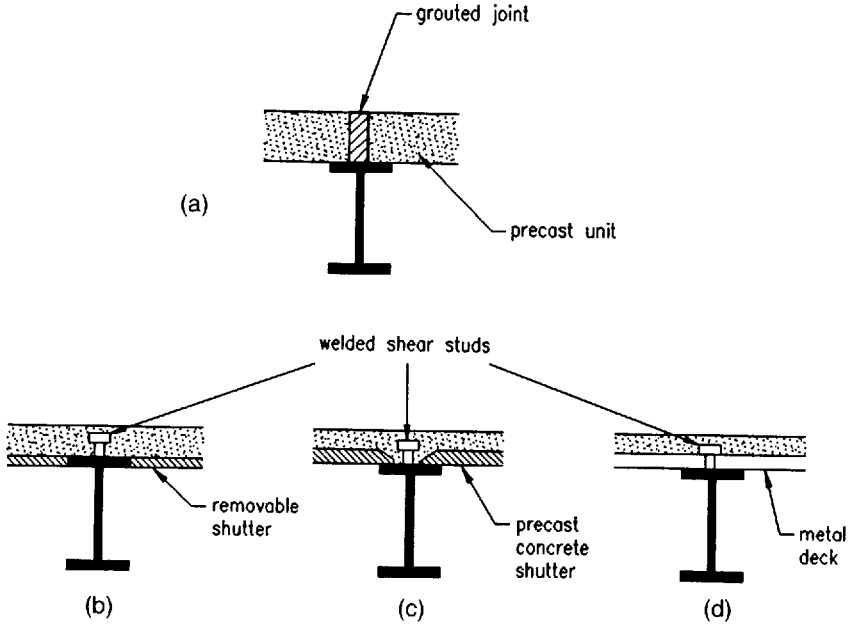


Fig. 2.23 Floor construction: (a) precast (non-composite); (b) in situ (composite); (c) in situ/precast (composite); (d) in situ/metal decking (composite)

allowing the slab to act as the compression flange of the combined steel and concrete system, the advantage is greatest when the beam is sagging. Consequently composite floor systems are usually designed as simply supported.

Experience has shown that the most efficient floor arrangements are those using metal decking spanning about 3 m between floor beams. For these spans the metal decking does not normally require propping during concreting and the concrete thicknesses are near the practical minimum for consideration of strength and fire separation.

Steel studs are welded through the decking on the flange of the beams below to form a connection between steel beam and concrete slab. Concrete, which may be either lightweight or normal weight, is then poured on to the decking usually by pumping to make up the composite system. Metal decking acts both as permanent formwork for the concrete and as tensile reinforcement for the slab. There are

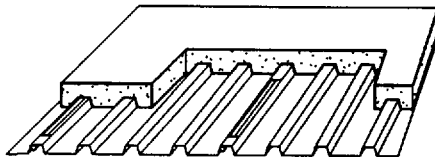


Fig. 2.24 Metal deck floor slabs

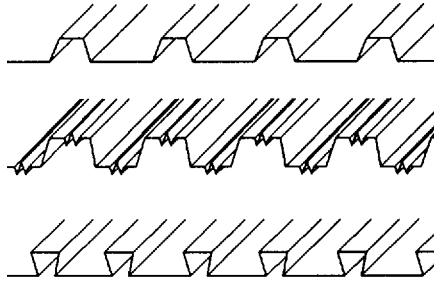


Fig. 2.25 Metal deck profiles

many types of steel decking available (Fig. 2.25) but perhaps the most commonly used is the re-entrant profile type which provides a flat soffit and facilitates fixings for building services and ceilings.

Some of the advantages of composite metal deck floor construction are:

- Steel decking acts as permanent shuttering which can eliminate the need for slab reinforcement and, due to its high stiffness and strength, propping of the construction while the wet concrete develops strength.
- Composite action reduces the overall depth of structure.
- It provides up to 2 hours fire resistance without additional fire protection and 4 hours with added thickness or extra surface protection.
- It is a light, adaptable system that can be easily manhandled on site, cut to awkward shapes and drilled or cut out for additional service requirements.
- Lightweight construction reduces frame loadings and foundation costs.
- It allows simple, rapid construction techniques.

Figure 2.26 illustrates alternative arrangements of primary and secondary beams for an optimum deck span of 3 m.

### *Precast floor systems*

Universal beams supporting precast prestressed floor units have some advantages over other forms of construction. Although of heavier construction than comparable composite metal deck floors, this system offers the following advantages.

- Fewer floor beams since precast floor units can span up to 6–8 m without difficulty.
- No propping is required.
- Shallow floor construction can be obtained by supporting precast floor units on shelf angles or on wide plates attached to the bottom flanges of universal columns acting as beams (Slim floor).

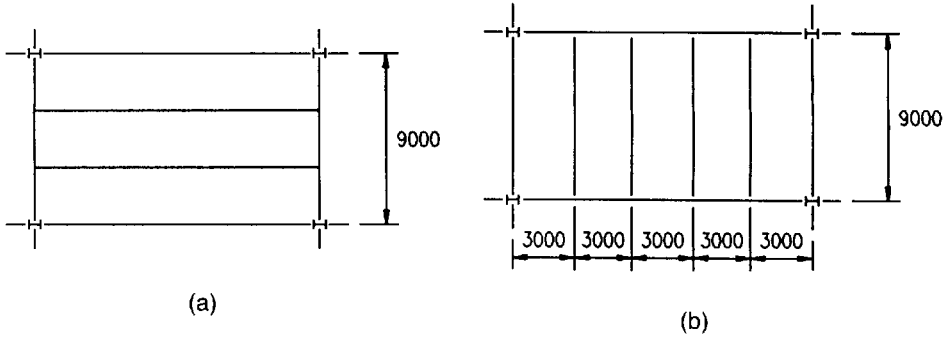


Fig. 2.26 Alternative framing systems for floors: (a) long span secondary beams; (b) long span primary beams

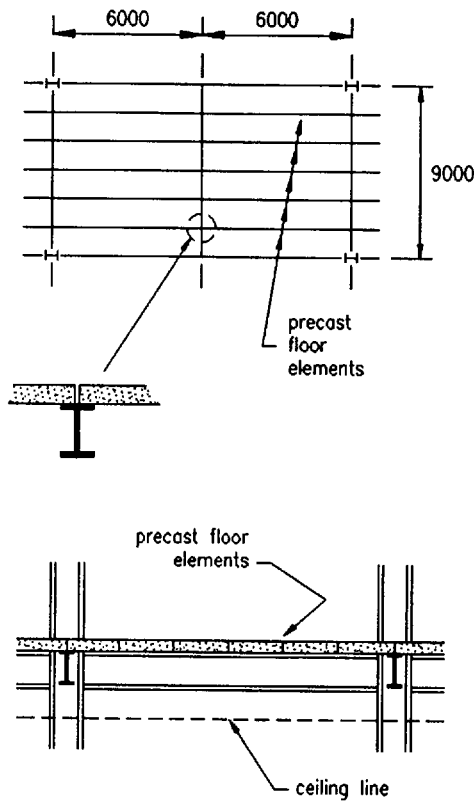


Fig. 2.27 Precast concrete floors

- Fast construction because no time is needed for curing and the development of concrete strength.

On the other hand the disadvantages are:

- Composite action is not readily achieved without a structural floor screed.
- Heavy floor units are difficult to erect in many locations and require the use of a tower crane which may have implications for the construction programme.

### 2.3.4 Bracings

Three structural systems are used to resist lateral loads: rigidly-jointed frames, reinforced concrete walls and braced-bay frames (Fig. 2.28). Combinations of these systems may also be used.

#### *Rigid frames*

Rigidly-jointed frames, or 'sway' frames, are those with full moment resisting connections between beam and columns. It is not necessary that all connections in a building are detailed in this way; only sufficient frames to satisfy the performance requirements of the building.

The advantage of the rigid frame is:

- Provides total internal adaptability with no bracings between columns or walls to obstruct circulation.

However, the disadvantages are:

- Increased fabrication for complex framing connections
- Increased site connection work, particularly if connections are welded
- Columns are larger to resist bending moments
- Generally, less stiff than other bracing systems.

#### *Shear walls*

Reinforced concrete walls constructed to enclose lift, stair and service cores generally possess sufficient strength and stiffness to resist the lateral loading.

Cores should be located to avoid eccentricity between the line of action of the lateral load and the centre of stiffness of the core arrangement. However, the core locations are not always ideal because they may be irregularly shaped, located at one end of the building or are too small. In these circumstances,

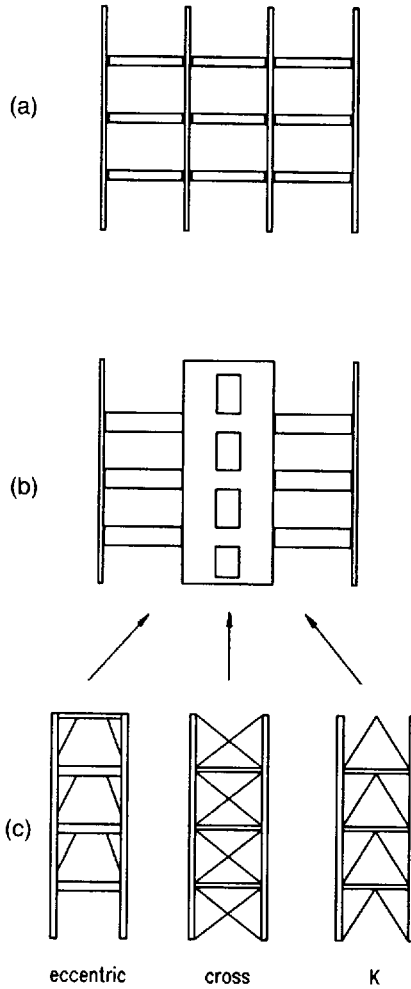


Fig. 2.28 Bracing structures: (a) rigid frame; (b) reinforced concrete wall; (c) braced bay frames

additional braced bays or rigidly-jointed frames should be provided at other locations. (Fig. 2.29.)

Although shear walls are normally constructed in in situ reinforced concrete they may also be constructed of either precast concrete or brickwork.

The advantages of shear walls are:

- The beam-to-column connections throughout the frame are simple, easily fabricated and rapidly erected.
- Concrete walls tend to be thinner than other bracing systems and hence save space in congested areas such as service and lift cores.

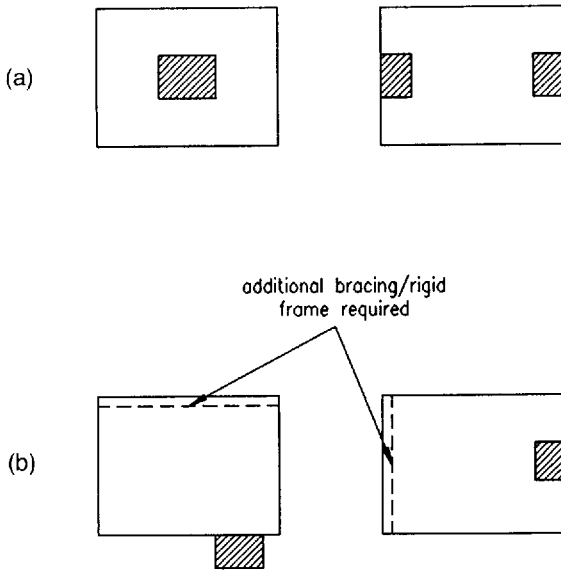


Fig. 2.29 Core locations: (a) efficient; (b) inefficient

- They are very rigid and highly effective.
- They act as fire compartment walls.

The disadvantages are:

- The construction of walls, particularly in low- and medium-rise buildings, is slow and less accurate than steelwork.
- The walls are difficult to modify if alterations to the building are required in the future.
- They are a separate form of construction which is likely to delay the contract programme.
- It is difficult to provide connections between steel and concrete to transfer the large forces generated.

### Braced-bay frames

Braced-bays are positioned in similar locations to reinforced concrete walls, so they have minimal impact upon the planning of the building. They act as vertical trusses which resist the wind loads by cantilever action.

The bracing members can be arranged in a variety of forms designed to carry solely tension or alternatively tension and compression. When designed to take tension only, the bracing is made up of crossed diagonals. Depending on the wind direction, one diagonal will take all the tension while the other remains inactive.

Tensile bracing is smaller than the equivalent strut and is usually made up of flat-plate, channel or angle sections. When designed to resist compression, the bracings become struts and the most common arrangement is the 'K' brace.

The advantages of braced-bay frames are:

- All beam-to-column connections are simple
- The braced bays are concentrated in location on plan
- The bracing configurations may be adjusted to suit planning requirements (eccentric bracing)
- The system is adjustable if building modifications are required in the future
- Bracing can be arranged to accommodate doors and openings for services
- Bracing members can be concealed in partition walls
- They provide an efficient bracing system.

A disadvantage is:

- Diagonal members with fire proofing can take up considerable space.

### 2.3.5 Connections

The most important aspect of structural steelwork for buildings is the design of the connections between individual frame components.

The selection of a component should be governed not only by its capability to support the applied load, but also by its ease of connection to other components.

Basically there are three types of connection, each defined by its structural behaviour; simple, rigid and semi-rigid (Fig. 2.30):

- (1) Simple connections transmit negligible bending moment across the joint; the connection is detailed to allow the beam end to rotate. The beam behaves as a simply supported beam.
- (2) Rigid connections are designed to transmit shear force and bending moment across the joint. The connection is detailed to ensure a monolithic joint. Beam end moments are transmitted into the column itself and any beam framing into the column on the opposite side.
- (3) Semi-rigid connections are designed to transmit the shear force and a proportion of the bending moment across the joint. The principle of these connections is to provide a partial restraint to beam end-rotation without introducing complicated fabrication to the joint. However, the design of such joints is complex and their wider application will be dependent to a large extent on the development of simple design procedures based upon experimental evidence. In the absence of these procedures, many details which may exhibit semi-rigid behaviour are used as simple connections.



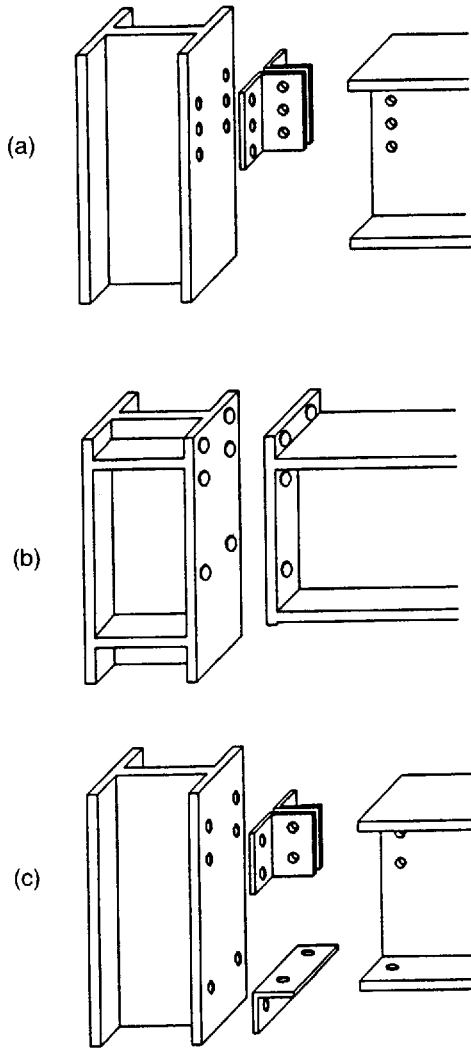


Fig. 2.30 Connections: (a) simple; (b) rigid; (c) semi-rigid

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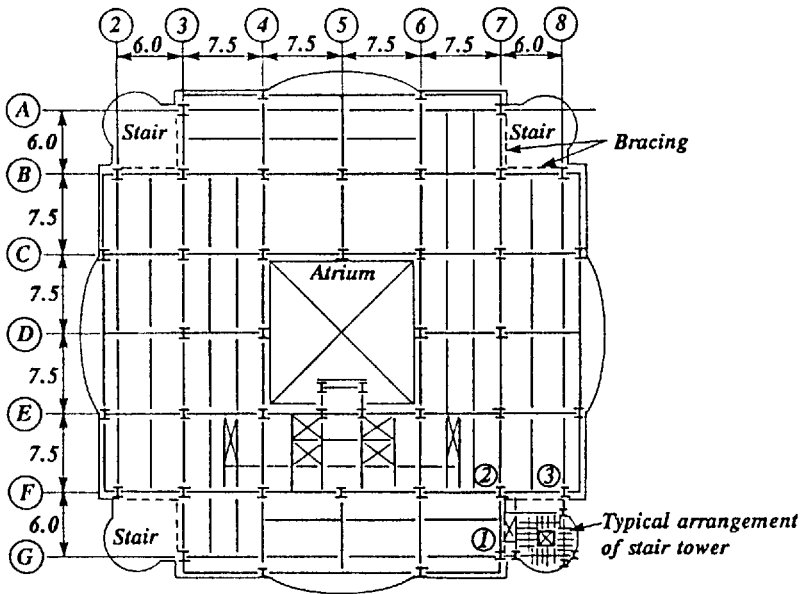
### **Further reading for Chapter 2**

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A worked example follows which is relevant to Chapter 2.


|  |   |   |
|--|---|---|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><br><b>MULTI-STOREY<br/>DESIGN EXAMPLE</b> | Chapter ref.<br><br><b>2</b>                |
|  | Design code<br><b>BS5950: Part 1</b>                  | Made by <b>AJK</b><br>Checked by <b>GWO</b> |


### Building geometry



*Typical floor plan*

**Building use:** Office building with basement car parking and high level plant room. Imposed loading for office floors exceeds minimum statutory loading at client's request. Design example illustrates design of elements in braced towers provided in four corners of building to achieve lateral stability. Floor plate is generally 130 mm lightweight aggregate concrete on metal decking which acts compositely with decking and floor beams. Fire protection is achieved with sprayed vermiculite cement.

|   |   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
|---|---|---|--------------------------|-------------------------------|-------------|-----------------------------|------------|-----------------|------------|-----------------------|-------------------|--|-------------|-----------------------------|------------|-------------------------------|-------------|--------------------------------|-------------|--------------------------|---------------------|-----------------|----------------------------|--|-----------------------|---------------------|----------------------|-------------------------------|-------------|--------------------------------|-------------|--------------------------|-------------------------|---------------------|------------|-----------------|--------------------------------|--|---------------------------|---------------------|------------|-------------------|------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN  | Subject<br><b>MULTI-STOREY DESIGN EXAMPLE</b> |   | Chapter ref.<br><b>2</b> |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
|   | Design code<br><b>BS5950: Part 1</b>          | Made by <b>AJK</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>       |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <p><b><u>Loading</u></b></p> <p style="text-align: right;"><b><i>kN/m<sup>2</sup></i></b></p> <p><b>Roof:</b></p> <table style="width: 100%;"> <tr> <td style="width: 80%;"><b>Steelwork + metal deck</b></td> <td style="text-align: right;"><b>0.27</b></td> </tr> <tr> <td><b>Concrete (130 mm lw)</b></td> <td style="text-align: right;"><b>1.8</b></td> </tr> <tr> <td><b>Finishes</b></td> <td style="text-align: right;"><b>2.0</b></td> </tr> <tr> <td><b>Services below</b></td> <td style="text-align: right;"><u><b>0.3</b></u></td> </tr> <tr> <td></td> <td style="text-align: right;"><b>4.37</b></td> </tr> <tr> <td><b>BS 6399 Imposed load</b></td> <td style="text-align: right;"><b>1.5</b></td> </tr> </table> <p><b>Plant room/BI:</b></p> <table style="width: 100%;"> <tr> <td style="width: 80%;"><b>Steelwork + metal deck</b></td> <td style="text-align: right;"><b>0.49</b></td> </tr> <tr> <td><b>150 mm lw concrete slab</b></td> <td style="text-align: right;"><b>2.15</b></td> </tr> <tr> <td><b>Suspended ceiling</b></td> <td style="text-align: right;"><b>0.2 (not BI)</b></td> </tr> <tr> <td><b>Services</b></td> <td style="text-align: right;"><u><b>0.3 (not BI)</b></u></td> </tr> <tr> <td></td> <td style="text-align: right;"><b>3.14 2.64 (BI)</b></td> </tr> <tr> <td><b>Imposed load</b></td> <td style="text-align: right;"><b>7.5 2.50 (BI)</b></td> </tr> </table> <p><b>Office floors:</b></p> <table style="width: 100%;"> <tr> <td style="width: 80%;"><b>Steelwork + metal deck</b></td> <td style="text-align: right;"><b>0.27</b></td> </tr> <tr> <td><b>130 mm lw concrete slab</b></td> <td style="text-align: right;"><b>1.80</b></td> </tr> <tr> <td><b>Suspended ceiling</b></td> <td style="text-align: right;"><b>0.2 (not ground)</b></td> </tr> <tr> <td><b>Raised floor</b></td> <td style="text-align: right;"><b>0.3</b></td> </tr> <tr> <td><b>Services</b></td> <td style="text-align: right;"><u><b>0.3 (not ground)</b></u></td> </tr> <tr> <td></td> <td style="text-align: right;"><b>2.87 2.37 (ground)</b></td> </tr> <tr> <td><b>Imposed load</b></td> <td style="text-align: right;"><b>5.0</b></td> </tr> <tr> <td><b>Partitions</b></td> <td style="text-align: right;"><b>1.0</b></td> </tr> </table> |   |   |                          | <b>Steelwork + metal deck</b> | <b>0.27</b> | <b>Concrete (130 mm lw)</b> | <b>1.8</b> | <b>Finishes</b> | <b>2.0</b> | <b>Services below</b> | <u><b>0.3</b></u> |  | <b>4.37</b> | <b>BS 6399 Imposed load</b> | <b>1.5</b> | <b>Steelwork + metal deck</b> | <b>0.49</b> | <b>150 mm lw concrete slab</b> | <b>2.15</b> | <b>Suspended ceiling</b> | <b>0.2 (not BI)</b> | <b>Services</b> | <u><b>0.3 (not BI)</b></u> |  | <b>3.14 2.64 (BI)</b> | <b>Imposed load</b> | <b>7.5 2.50 (BI)</b> | <b>Steelwork + metal deck</b> | <b>0.27</b> | <b>130 mm lw concrete slab</b> | <b>1.80</b> | <b>Suspended ceiling</b> | <b>0.2 (not ground)</b> | <b>Raised floor</b> | <b>0.3</b> | <b>Services</b> | <u><b>0.3 (not ground)</b></u> |  | <b>2.87 2.37 (ground)</b> | <b>Imposed load</b> | <b>5.0</b> | <b>Partitions</b> | <b>1.0</b> |
| <b>Steelwork + metal deck</b>   | <b>0.27</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Concrete (130 mm lw)</b>   | <b>1.8</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Finishes</b>   | <b>2.0</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Services below</b>   | <u><b>0.3</b></u>                             |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
|   | <b>4.37</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>BS 6399 Imposed load</b>   | <b>1.5</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Steelwork + metal deck</b>   | <b>0.49</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>150 mm lw concrete slab</b>  | <b>2.15</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Suspended ceiling</b>  | <b>0.2 (not BI)</b>                           |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Services</b>   | <u><b>0.3 (not BI)</b></u>                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
|   | <b>3.14 2.64 (BI)</b>                         |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Imposed load</b>   | <b>7.5 2.50 (BI)</b>                          |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Steelwork + metal deck</b>   | <b>0.27</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>130 mm lw concrete slab</b>  | <b>1.80</b>                                   |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Suspended ceiling</b>  | <b>0.2 (not ground)</b>                       |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Raised floor</b>   | <b>0.3</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Services</b>   | <u><b>0.3 (not ground)</b></u>                |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
|   | <b>2.87 2.37 (ground)</b>                     |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Imposed load</b>   | <b>5.0</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |
| <b>Partitions</b>   | <b>1.0</b>                                    |   |                          |                               |             |                             |            |                 |            |                       |                   |  |             |                             |            |                               |             |                                |             |                          |                     |                 |                            |  |                       |                     |                      |                               |             |                                |             |                          |                         |                     |            |                 |                                |  |                           |                     |            |                   |            |

|   |   |   |                          |
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|   | Design code<br><b>BS5950: Part 1</b>          | Made by <b>AJK</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>       |

**Perimeter loads**

*kN/m*

**Roof**                    **1.5**  
**Plant room**         **18.8**  
**General**               **9.6**


**Length supported by column 1** = **1.65 m (G7)**  
**2** = **0 (F7)**  
**3** = **1.65 m (F8)**

**Imposed stair loading** = **4.0 kN/m<sup>2</sup>**  
**Total stair area** = **158.0 m<sup>2</sup>**

| <b>* Area supported (m<sup>2</sup>)</b> |              |              |              |
|---|--------------|--------------|--------------|
|   | <b>Col.1</b> | <b>Col.2</b> | <b>Col.3</b> |
| <b>Floor</b>                            | <b>24.8</b>  | <b>43.8</b>  | <b>20.9</b>  |
| <b>Stairs</b>                           | <b>0.8</b>   | <b>1.6</b>   | <b>0</b>     |

**\* The above areas apply to all levels.**

**Total floor area = 1688 m<sup>2</sup>**

|  |   |   |                          |
|--|---|---|--------------------------|
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|  | Design code<br><b>BSS950: Part 1</b>          | Made by <b>AJK</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>       |

**Column Imposed loads**


| Level | Imposed load kN/m <sup>2</sup> | % Imposed load reduction | Column load (kN) |              |       | * Cumulative loads in columns (kN) |              |       |
|-------|--------------------------------|--------------------------|------------------|--------------|-------|------------------------------------|--------------|-------|
|       |                                |                          | Col.1            | Col.2        | Col.3 | Col.1                              | Col.2        | Col.3 |
| R     | 1.5                            | 0                        | 40.4             | 72.1         | 31.4  | 40.4                               | 72.1         | 31.4  |
| P     | 7.5                            | 10.0                     | 189.2<br>(1)     | 334.9<br>(2) | 156.8 | 206.6                              | 366.3        | 169.4 |
| 9.0   | 6.0                            | 20.0                     | 152              | 269.2        | 125.4 | 305.3                              | 541.0<br>(3) | 250.9 |
| 8.0   | 6.0                            | 30.0                     | 152              | 269.2        | 125.4 | 373.5                              | 661.8        | 307.3 |
| 7.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 411.4                              | 728.8        | 338.6 |
| 6.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 502.6                              | 890.3        | 413.9 |
| 5.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 593.8                              | 1051.8       | 489.1 |
| 4.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 685.0                              | 1213.3       | 564.4 |
| 3.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 776.2                              | 1374.8       | 639.6 |
| 2.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 867.4                              | 1536.4       | 714.8 |
| 1.0   | 6.0                            | 40.0                     | 152              | 269.2        | 125.4 | 958.6                              | 1697.9       | 790.1 |
| G     | 6.0                            | 50.0                     | 152              | 269.2        | 125.4 | 874.8                              | 1549.5       | 721.1 |
| B1    | 6.0                            | 50.0                     | 152              | 269.2        | 125.4 | 950.8                              | 1684.1       | 783.8 |
| B2    | 2.5                            | 50.0                     | 65.2             | 115.9        | 52.3  | 983.4                              | 1742.1       | 810.0 |

**Note:** The above loads are based on the areas for floors and stairs shown in the Table on Sheet no.3.

\* values include % Imposed load reduction.

**Examples:**

- (1)  $(7.5 \times 24.8) + (4.0 \times 0.8) = 189.2 \text{ kN}$   
 (2)  $(7.5 \times 43.8) + (4.0 \times 1.6) = 334.9 \text{ kN}$   
 (3)  $(72.1 + 334.9 + 269.2) 0.8 = 541.0 \text{ kN}$


|   |   |   |                          |
|---|---|---|--------------------------|
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|   | Design code<br><b>BSS950: Part 1</b>          | Made by <b>AJK</b><br>Checked by <b>GWO</b> | Sheet no. <b>5</b>       |

Column Dead loads

|    | Unit loads                 |                 | Col. Dead loads |              |         | Cumulative Dead loads |         |         |
|----|----------------------------|-----------------|-----------------|--------------|---------|-----------------------|---------|---------|
|    | Floor<br>kN/m <sup>2</sup> | Perim.R<br>kN/m | 1<br>kN         | 2<br>kN      | 3<br>kN | 1<br>kN               | 2<br>kN | 3<br>kN |
| R  | 4.37                       | 1.5             | 114.4           | 198.4<br>(2) | 93.8    | 114.4                 | 198.4   | 93.8    |
| P  | 3.14                       | 18.8            | (1)             | 142.6        | 96.6    | 225.8                 | 341.0   | 190.4   |
| 10 | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 315.1                 | 471.3   | 266.2   |
| 9  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 404.4                 | 601.6   | 342.0   |
| 8  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 493.7                 | 731.9   | 417.8   |
| 7  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 583.0                 | 862.2   | 493.6   |
| 6  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 672.3                 | 992.5   | 569.4   |
| 5  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 761.6                 | 1122.8  | 645.2   |
| 4  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 850.9                 | 1253.1  | 721.0   |
| 3  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 940.2                 | 1383.4  | 796.8   |
| 2  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 1029.5                | 1513.7  | 872.6   |
| 1  | 2.87                       | 9.6             | 89.3            | 130.3        | 75.8    | 1118.8                | 1644.0  | 948.4   |
| G  | 2.37                       | -               | 60.7            | 107.6        | 49.5    | 1179.5                | 1751.6  | 997.9   |
| B1 | 2.64                       | -               | 67.6            | 119.9        | 55.2    | 1247.1                | 1871.5  | 1053.1  |
| B2 |                            |                 |                 |              |         |                       |         |         |

**Examples:**

- (1)  $(3.14 \times 24.8) + (18.8 \times 1.65) + (3.14 \times 0.8) = 111.4 \text{ kN}$
- (2)  $(4.37 \times 43.8) + (4.37 \times 1.6) = 198.4 \text{ kN}$
- (3)  $198.4 + 142.6 = 341.0 \text{ kN}$

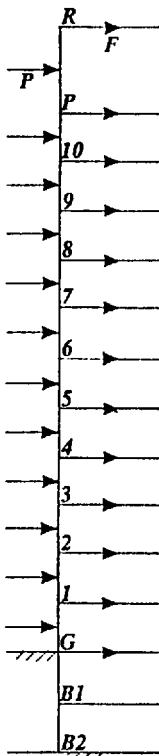
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**Wind load**

CP3 Ch. V: Part 2: 1972

Basic wind speed  $V_B = 38$  m/s (London) $S_1 = S_3 = 1.0$  (no topography/statistical considerations) $C_f = 0.95$ 

Building width = 48.0 m


 $V_s = S_1 S_2 S_3 V_B$  $q = 0.613 V_s^2$  (N/m<sup>2</sup>)


|    | $h$ | $S_2$ | $q$ (kN/m <sup>2</sup> ) | $A$ (m <sup>2</sup> ) | Force $P$ (kN) | Force $F$ (kN) |
|----|-----|-------|--------------------------|-----------------------|----------------|----------------|
| R  | 54  | 1.04  | 0.957                    | 384                   | 349            | 175            |
| P  | 46  | 1.02  | 0.921                    | 192                   | 168            | 258            |
| 10 | 42  | 1.01  | 0.903                    | 192                   | 165            | 167            |
| 9  | 38  | 1.00  | 0.885                    | 192                   | 161            | 163            |
| 8  | 34  | 0.98  | 0.850                    | 192                   | 155            | 158            |
| 7  | 30  | 0.97  | 0.833                    | 192                   | 152            | 154            |
| 6  | 26  | 0.94  | 0.782                    | 192                   | 143            | 148            |
| 5  | 22  | 0.91  | 0.733                    | 192                   | 134            | 139            |
| 4  | 18  | 0.88  | 0.685                    | 192                   | 125            | 130            |
| 3  | 14  | 0.81  | 0.581                    | 192                   | 106            | 116            |
| 2  | 10  | 0.74  | 0.485                    | 192                   | 83.5           | 94.8           |
| J  | 6   | 0.67  | 0.397                    | 288                   | 109            | 96.3           |
| G  |     |       |                          |                       |                | 54.5           |
| B1 |     |       |                          |                       |                |                |
| B2 |     |       |                          |                       |                |                |

 $F$  is the total force applied at that level.

Loads are divided by 4 in the analysis to represent the force applied to one braced tower.



|   |   |   |                          |
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**Notional Horizontal Forces (NHF):**

To account for practical imperfections such as lack of verticality, notional horizontal forces are considered.

At each level,

$$F_{NHF} = 0.5\% \text{ factored dead and imposed load at that level}$$

(the imposed loads are reduced by the overall reduction factor of 0.5)

e.g. for level 9:

$$\text{stair area} = 158 \text{ m}^2$$

| Level | NHF (kN) |
|-------|----------|
| R     | 17.74    |
| P     | 28.84    |
| 10    | 23.10    |
| 9     | 23.10    |
| 8     | 23.10    |
| 7     | 23.10    |
| 6     | 23.10    |
| 5     | 23.10    |
| 4     | 23.10    |
| 3     | 23.10    |
| 2     | 23.10    |
| 1     | 23.10    |
| G     | 18.42    |
| B1    | 13.38    |
| B2    | -        |

$$D.L. = 2.87 \text{ (1688 + 158) } + (9.6 \times 164.6) = 6878 \text{ kN}$$

floor
perimeter

reduced imposed load


$$= [(1688 \times 6.0) + (158 \times 6.0)] 0.5 = 5538 \text{ kN}$$

Note: For this case, it is convenient to keep the floor and stair imposed loads equal to 6.0 kN/m<sup>2</sup>.

$$\therefore \text{NHF per tower} = \frac{0.5}{100 \times 4} [(1.4 \times 6878) + (1.6 \times 5538)]$$

$$= 23.1 \text{ kN}$$

The NHF load case is considered as acting simultaneously with dead and applied loads when no wind forces are acting.

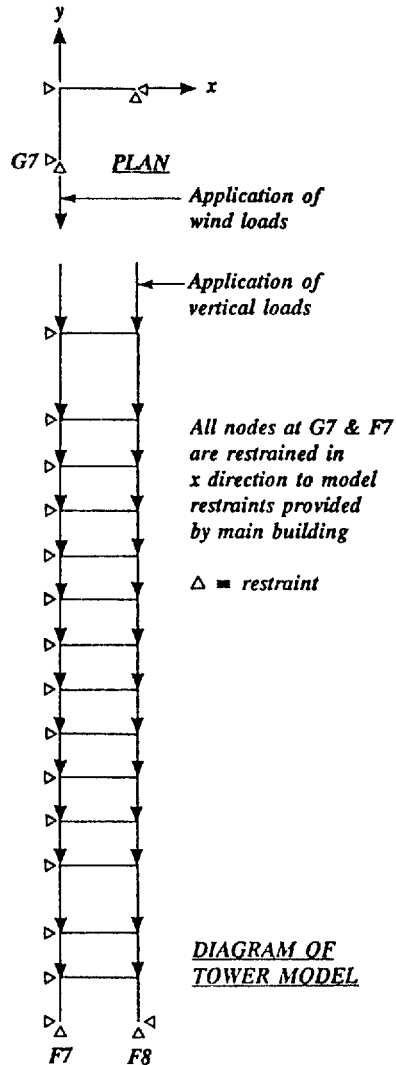
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Because of symmetry one of the four braced towers only was modelled as a space frame and analysed using beam finite elements on a personal computer, subject to a quarter of total horizontal loading.

**Basic load cases**

1. Wind loading (y direction)
2. Notional Horizontal Forces (NHF)
3. Dead loads
4. Reduced Imposed loads

| Results from NHF load case |                    |                            |   |
|----------------------------|--------------------|----------------------------|---|
|                            | Lateral disp. (mm) | Storey drift $\Delta$ (mm) | $\phi_s = \frac{\Delta}{h}$ ( $\times 10^3$ ) |
| R                          | 8                  | 75.56                      |   |
|                            |                    |                            | 9.74  |
| P                          | 4                  | 65.82                      |   |
| 10                         | 4                  | 60.94                      | 4.88  |
| 9                          | 4                  | 56.07                      | 4.87  |
| 8                          | 4                  | 51.19                      | 4.88  |
| 7                          | 4                  | 46.31                      | 4.88  |
| 6                          | 4                  | 41.43                      | 4.88  |
| 5                          | 4                  | 36.55                      | 4.88  |
| 4                          | 4                  | 31.67                      | 4.88  |
| 3                          | 4                  | 26.79                      | 4.88  |
| 2                          | 4                  | 21.91                      | 4.88  |
| 1                          | 4                  | 17.03                      | 4.88  |
| G                          | 6                  |                            | 7.30  |
| B1                         | 4                  | 9.73                       | 4.87  |
| B2                         | 4                  | 4.86                       | 4.86  |



|  |   |                                      |   |
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***P - Δ effects***

*The amplified sway method was used to account for P - Δ (secondary) effects.* **F.2.3**  
**5.6.3 (b)**

*Elastic critical factor is estimated from the max. sway index under notional horizontal forces.*

$$\lambda_{cr} = \frac{I}{200 \phi_{s \max}} = \frac{I}{200 \times 1.22 \times 10^{-3}} = 4.1$$


*Amplified sway factor*

$$m = \frac{\lambda_{cr}}{\lambda_{cr} - 1} = 1.32$$

*P - Δ effects occur when real horizontal loads are applied (i.e. wind loads but not NHF).*

***Load case combinations***

- 1.4 Dead + 1.6 Imposed**
- 1.2 (Dead + Imposed ± m × wind)**
- 1.4 Dead ± 1.4 m × wind**
- 1.0 Dead ± 1.4 m × wind**
- 1.4 Dead + 1.6 Imposed ± 1.0 NHF** **2.4.2.3**

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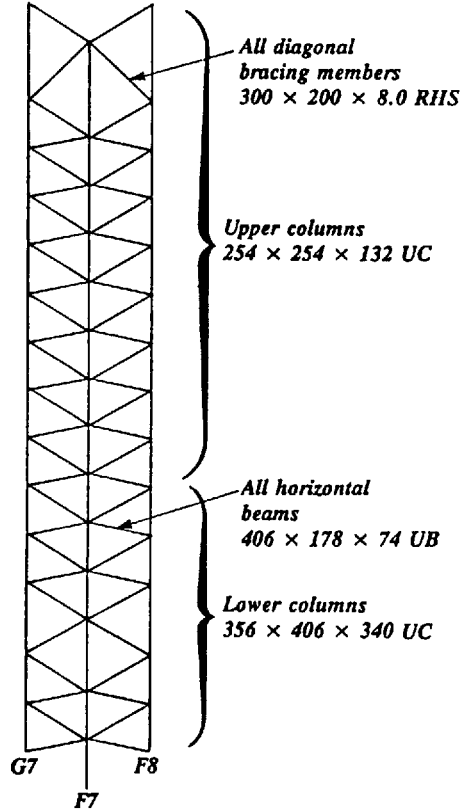
Proposed section sizes

Steel Grade 50

Lateral deflection

Under wind load case:

| Level | Deflection (mm) | h/Δ  |
|-------|-----------------|------|
| R     | 156             | 364  |
| P     | 134             | 364  |
| 10    | 123             | 333  |
| 9     | 111             | 333  |
| 8     | 99              | 333  |
| 7     | 87              | 462  |
| 6     | 74              | 364  |
| 5     | 63              | 333  |
| 4     | 51              | 400  |
| 3     | 41              | 444  |
| 2     | 32              | 444  |
| 1     | 23              | 500  |
| G     | 11              | 571  |
| B1    | 4               | 1000 |
| B2    | 0               | -    |




Maximum differential storey

Table 5

$$\text{deflection} = \frac{h}{333} < \frac{h}{300}$$

∴ deflection is acceptable.

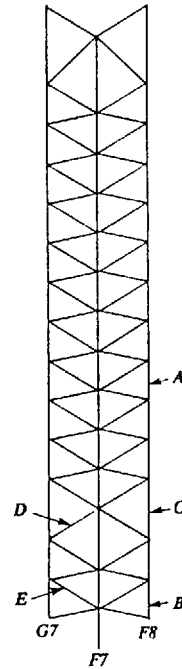
*N.B. The magnification factor may be re-evaluated for each combination considered, based on the factored gravity load acting in that combination.*

|  |   |   |                          |
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### Confirmation of element sizes

Critical member forces determined from an examination of all load cases are:

|                                 | Compression load case |       | Tension load case |       | Stress ratio max. |
|---------------------------------|-----------------------|-------|-------------------|-------|-------------------|
|                                 | $F_c$                 | $M_x$ | $F_T$             | $M_x$ |                   |
| A. Upper column                 | 3426                  | 4     | 1222              | 10    | 0.86              |
| B. Lower column                 | 6666                  | 40    | 3682              | 40    | 0.58              |
| C. Lower column ( $L_e = 6.0$ ) | 5112                  | 31    | 2424              | 31    | 0.70              |
| D. Diagonal                     | 906                   | -     | 897               | -     | 0.73              |
| E. Horizontal                   | 633                   | -     | 631               | -     | 0.85              |



By inspection compression is critical in each case. All sections are adequate.

Local capacity check:

$$\frac{F_c}{A_g p_y} + \frac{M_x}{M_{cx}} \leq 1$$

4.8.3.2


overall buckling check:

$$\frac{F_c}{A_g p_c} + \frac{m M_x}{M_b} \leq 1$$

4.8.3.3

### Section summary

|                    |                       |
|--------------------|-----------------------|
| UPPER COLUMNS      | : 254 × 254 × 132 UC  |
| LOWER COLUMNS      | : 356 × 406 × 340 UC  |
| (LEVEL B2 - 3)     |                       |
| DIAGONAL BRACING   | : 300 × 200 × 8.0 RHS |
| HORIZONTAL BRACING | : 406 × 178 × 74 UB   |

|  |   |   |   |
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|  |   | Design code<br><b>BS5950: Part 1</b>              | Made by <b>AJK</b><br>Checked by <b>GWO</b> |

**Robustness of frame**

To allow for practical imperfections such as lack of verticality in columns, column ties should be capable of transmitting:

2.4.5.3

- (1) The general tying force given by  $0.5 w_f s_t L_a$  for internal ties or  $0.25 w_f s_t L_a$  for edge ties but not less than 75 kN, where:

- $w_f$  = factored dead and imposed load per unit area
- $s_t$  = mean transverse spacing of ties
- $L_a$  = maximum span within the overall length of the tie

$$\begin{aligned} \text{tying force} &= 0.5 \times [(2.87 \times 1.4) + (6.0 \times 1.6)] \times 7.5 \times 7.5 \\ &= 383 \text{ kN} > 75 \text{ kN} \end{aligned}$$

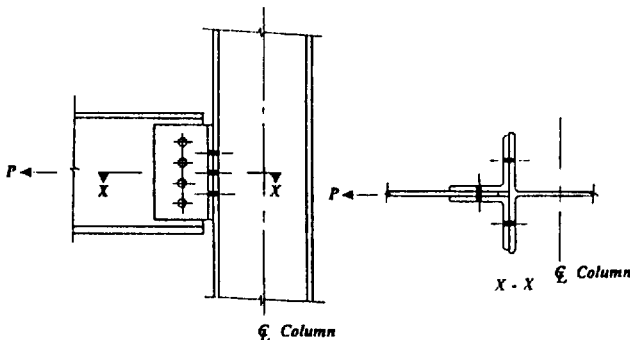
or

- (2) At the periphery, the general tying force or an anchor force of 1% of the factored vertical load in the column whichever is the greater.

$$\text{Max. column force} = 7309 \text{ kN} \therefore \text{anchor force} = 73.1 \text{ kN}$$

Design connection for  $P = \pm 383 \text{ kN}$

(NB these forces should not be considered as additive to other loads.)



# Chapter 3

## Industrial steelwork

by JOHN ROBERTS

### 3.1 Range of structures and scale of construction

#### 3.1.1 Introduction

Structural steelwork for industrial use is characterized by its function, which is primarily concerned with the support, protection and operation of plant and equipment. In scale it ranges from simple support frameworks for single tanks, motors or similar equipment, to some of the largest integrated steel structures, for example, complete electric power-generating facilities.

Whereas conventional single- and multi-storey structures provide environmental protection to space enclosed by walls and roof and, for multi-storey buildings, support of suspended floor areas, these features are never dominant in industrial steelwork. Naturally, in many industrial structures, the steel framework also provides support for wall and roof construction to give weather protection, but where this does occur the wall and roof profiles are designed to fit around and suit the industrial plant and equipment, frequently providing lower or different standards of protection in comparison with conventional structures. Many plant installations are provided only with rain shielding; high levels of insulation are unusual and some plant and equipment are able to function and operate effectively without any weather protection at all. In such circumstances the requirements for operational and maintenance personnel dictate the provision of cladding, sheeting or decking.

Similarly, most industrial steelwork structures have some areas of conventional floor construction, but this is not a primary requirement and the flooring is incidental to the plant and equipment installation.

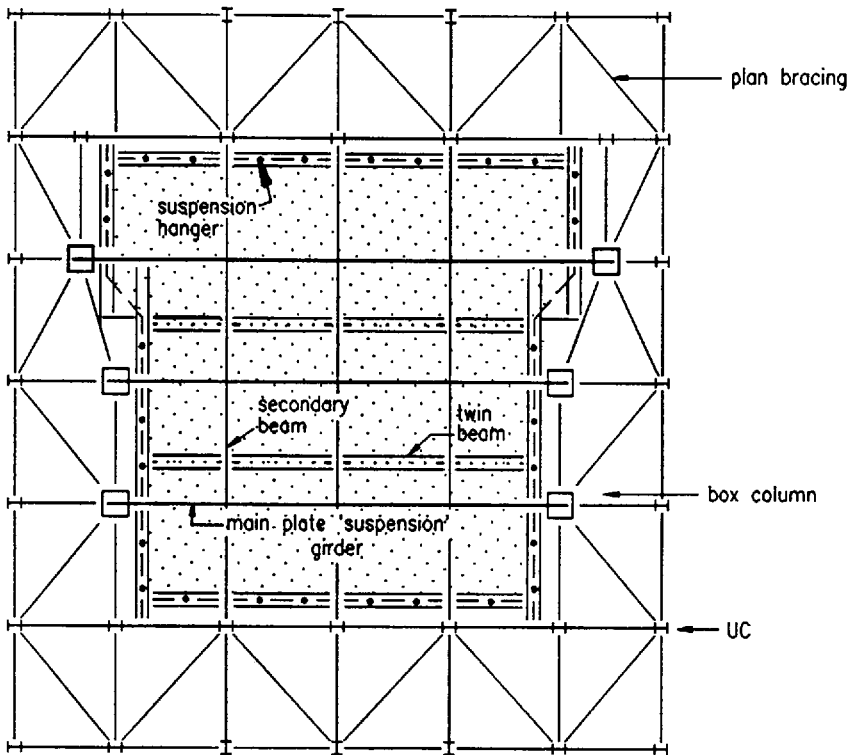
Floors are provided to allow access to and around the installation, being arranged to suit particular operational features. They are therefore unlikely to be constructed at constant vertical spacing or to be laid out on plan in any regular repetitive pattern. Steelwork designers must be particularly careful not to neglect the importance of two factors. First, floors cannot automatically be assumed to provide a horizontal wind girder or diaphragm to distribute lateral loadings to vertical-braced or framed bays; openings, missing sections or changes in levels can each destroy this action. Secondly, column design is similarly hampered by the lack of frequent and closely-spaced two-directional lateral support commonly available in normal multi-storey structures.

Floors require further consideration regarding the choice of construction (see section 3.2.3) and loading requirements (see section 3.3.1).

### 3.1.2 Power station structures

Industrial steelwork for electrical generating plants varies considerably depending on the size of station and the fuel being used. These variations are most marked in boiler house structures; whereas coal-fired and oil-fired boilers are similar, nuclear power station boilers (reactors) are generally constructed in concrete for biological shielding purposes, steel being used normally in a secondary building envelope role. Turbine halls are, in principle, largely independent of fuel type and many of the other plant structures (mechanical annexes, electrical switchgear buildings, coal hoppers, conveyors, pump-houses) are common in style to other industrial uses and so brief descriptions of the salient design features are of general interest.

*Boiler houses* (coal- or oil-fired) (Fig. 3.1) have to solve one overriding design criterion and as a result can be considered exercises in pure structural design.



boiler shown shaded  
vertical bracing not shown

Fig. 3.1 Plan of boiler house framing



Modern boilers are huge single pieces of plant with typical dimensions of 20 m × 20 m × 60 m high for a single 500 MW coal boiler. Where poor-quality coal is burnt or higher capacities are required, the dimensions can be even larger, up to about 25 m × 25 m × 80 m high for 900 MW size sets. As may be anticipated, the weights are equally massive, typically in the range of 7000–10 000 t for the plant sizes noted above. Boilers are always *top-suspended* from the supporting structures and not built directly from foundation level upwards, nor carried by a combination of top and bottom support. This is because the thermal expansion of the boiler prevents dual support systems; unsurmountable buckling and stability problems on the thin-walled-tube structure of the casing would arise if the boiler was bottom-supported and hence in compression, rather than top-suspended and hence in tension. For obvious reasons no penetrations of the boiler can be acceptable and therefore no internal columns can be provided. The usual structural system is to provide an extremely deep and stiff system of suspension girders (plate or box) spanning across the boiler with an extensive framework of primary, secondary and tertiary beams terminating in individual suspension rods or hangers which support the perimeter walls and roof of the boiler itself.

Columns are massively loaded from the highest level and so are usually constructed from welded box-sections since their loading will be considerably above the capacity of any rolled section. It is usual practice for a perimeter strip some 5–10 m wide to be built around the boiler itself allowing a structural grid to be provided with an adequate bay width for bracing to be installed for lateral stability. It also provides support for ancillary plant and equipment adjacent to specific zones of the boiler, for pipework and valves, for personnel access walkways or floor zones.

The pipework support requirements are often onerous and in particular the pipework designers may require restrictive deflection limitations that are sometimes set as low as 50 mm maximum deflection under wind loadings at the top of 90 m high structures.

*Turbine halls* (Fig. 3.2) support and house turbo-generating machines that operate on steam produced by the boiler, converting heat energy into mechanical energy of rotation and then into electrical energy by electromagnetic induction. Turbo-generators are linear in layout, built around a single rotating shaft, typically some 25 m long for 500 MW units. The function of a steel-framed turbine hall is to protect and allow access to the generator, to support steam supply and condensed water return pipework and numerous other items of ancillary plant and equipment. Heavy crane capacity is usually provided since generators are working machines that require routine servicing as well as major overhaul and repairs. They are probably the largest rotating machines in common use and dynamic analysis of turbine generator support steelwork is imperative. Fortunately they operate at a sensibly constant speed and so design of the support steelwork is amenable to an analytical examination of dynamic frequencies of motion of the whole support structure with plant loading in each possible mode, with similar consideration of any local frequency effect, such as vibration of individual elements of the structure or its framework.

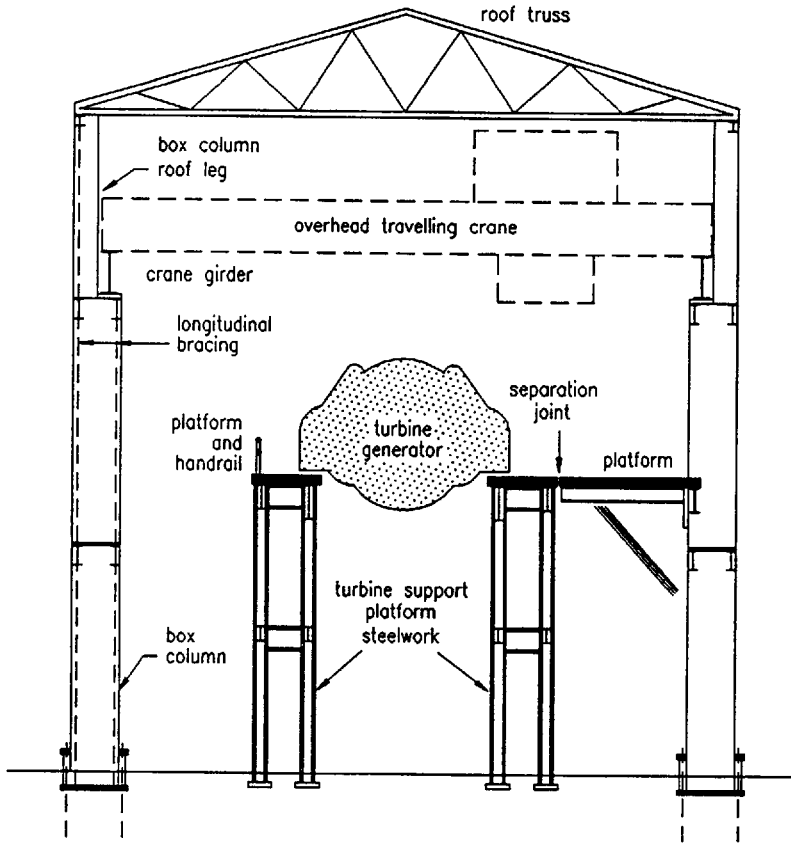


Fig. 3.2 Cross section through turbine hall

These frequencies of response are compared to the forcing frequency of motion of the machine, the design being adjusted so that no response frequencies exist in a band either side of the forcing frequency, to avoid resonance effects.

A complete physical separation is provided between the generator support steelwork and any adjoining main frame, secondary floor or support steel to isolate vibration effects. Zones on adjoining suspended floors are set aside for strip-down and servicing and specific 'laydown' loading rates are allowed in the design of these areas to cater for heavy point and distributed loads.

### 3.1.3 Process plant steelwork

Steelwork for process and manufacturing plants varies across a wide spectrum of different industrial uses. Here it is considered to be steelwork that is intimately

connected with the support and operation of plant and equipment, rather than a steel-framed building envelope constructed over a process plant.

Although the processes and plant vary widely, the essential features of this type of industrial steelwork are common to many applications and are conveniently examined by reference to some typical specific examples. There are many similarities with power station boiler house and turbine house steelwork described in section 3.1.2.

*Cement manufacturing plant.* Typical cement plants are an assembly of functional structures arranged in a manufacturing flow sequence, with many short-term storage and material transfer facilities incorporated into the processes. The physical height and location of the main drums are likely to dictate the remaining plant orientation.

*Vehicle assembly plants.* Substantial overhead services to the various assembly lines characterize vehicle assembly plants. It is normal to incorporate a heavy-duty and closely-spaced grid roof structure which also will support the roof covering. Reasonably large spans are needed to allow flexibility in arranging assembly line layouts without being constrained by column locations. Automation of the assembly process brings with it stiffness requirements to allow use of robots for precise operations such as welding and bonding. Open trusses in two directions are likely to satisfy most of these requirements, providing structural depth for deflection control and a zone above bottom boom level that can be used for service runs. Building plans are normally regular with rectangular type plan forms and uniformly regular roof profiles.

*Nuclear fuel process and treatment plants.* Steelwork for nuclear fuel process and treatment plants is highly dependent on the actual process involved, and often has to incorporate massive concrete sections for biological radiation shielding purposes. Particular points to note are the importance of the paint or other finishes, both from the point of view of restricted access in certain locations, leading to maintenance problems, and also from the necessity for finishes in some areas to be capable of being decontaminated. Specialized advice is needed for the selection of suitable finishes or to give guidance on whether, for example, structural stainless steels would be appropriate. In addition, certain nuclear facilities must be designed for extreme events, the most relevant of which is seismic loading set by the statutory regulatory body. Frequently designs will have to be undertaken to comply with well-established Codes of Practice for seismically active zones in, for example, America. Seismic design requires the establishment of ductile structures to allow high levels of energy absorption prior to collapse, and local stability and ductile connection behaviour become of critical importance. It follows that joint and connection design has to be fully integrated with the structural steel design generally; the normal responsibilities of joint design assumed by the steelwork fabricator may have to be altered on these projects.

*Petrochemical plants.* Petrochemical plants tend to be open structures with little or no weather protection. The steelwork required is dedicated to providing support to plant and pipework, and support for access walkways, gangways, stairs and ladders. Plant layouts are relatively static over long periods of use and the

steelwork is relatively economic in relation to the equipment costs. It is normal therefore to design the steelwork in a layout exactly suited to the plant and equipment without regard for a uniform structural grid. Benefits can still be gained from standardization of sizes or members and from maintaining an orthogonal grid to avoid connection problems. The access floors and interconnecting walkways and stairways must be carefully designed for all-weather access; use of grid flooring is almost universal. Protection systems for the steelwork should acknowledge both the threat from the potentially corrosive local environment due to liquid or gaseous emissions and the requirements to prevent closing down the facility for routine maintenance of the selected protection system.

Careful account needs to be taken of wind loading in terms of the loads that occur on an open structure and the lack of well-defined horizontal diaphragms from conventional floors. These two points are discussed further in sections 3.3.4 and 3.2.2.

### **3.1.4 Conveyors, handling and stacking plants**

Many industrial processes need bulk or continuous handling of materials with a typical sequence as follows:

- (1) loading from bulk delivery or direct from mining or quarrying work
- (2) transportation from bulk loading area to short-term storage (stacking or holding areas)
- (3) reclaim from short-term storage and transport to process plant.

Structural steelwork for the industrial plant which is utilized in these operations is effectively part of a piece of working machinery (Fig. 3.3). Design and construction standards must recognize the dynamic nature of the loadings and particularly must cater for out-of-balance running, overload conditions and plant fault or machinery failure conditions, any of which can cause stresses and deflections significantly higher than those resulting from normal operation. Most designers would adopt slightly lower factors of safety on loading for these conditions, but decisions need to be based on engineering judgement as to the relative frequency and duration of these types of loadings. The plant designer may well be unaware that such design decisions can be made for the steelwork and frequently will provide single maximum loading parameters that could incorporate a combination of all such possible events rather than a separate tabulation; the structural steelwork designer who takes the trouble to understand the operation of the plant can therefore ask for the appropriate information and use it to the best advantage.

A further feature of this type of steelwork is the requirement for frequent relocation of the loading area and hence the transportation equipment. Practical experience suggests that precise advance planning for specific future relocation is rarely feasible, so attention should be directed to both design and detailing so that future moves can cause the least disruption.

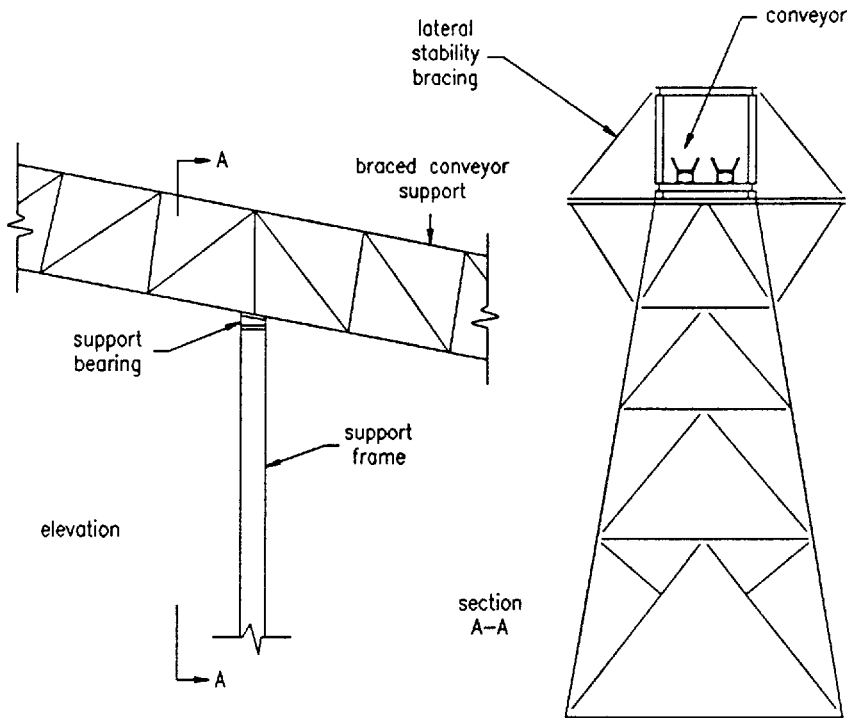


Fig. 3.3 Typical details of conveyor support

Foundation levels can be set at constant heights; or, if variations have to occur, then modular steps above or below a standard height should be adopted. The route should utilize standard plan angles between straight sections, and uniform vertical sloping sections between horizontal runs. Common base plate details and foundation bolt details can be utilized, even where this may be uneconomic for the initial layout installation. Some consideration should be given to allowing the supporting structure to be broken down into conveniently handled sections rather than into individual elements; the break-down joints can be permanently identified, for example, by painting in different colours.

### 3.1.5 General design requirements

Fatigue loadings must be considered, but even where fatigue turns out not to be a design criterion, it is vital to protect against vibration and consequent loosening of bolted assemblies. In this respect HSFG bolts are commonly used as they dispense with the necessity to provide a lock-nut; when correctly specified and installed they also display good fatigue-resistance.

However, just as plant engineers can display a lack of understanding about the necessity to design supporting steelwork afresh for each different structure even though the 'same' plant is being built, structural steelwork engineers must be aware that seemingly identical or repeat pieces of plant or equipment can in fact vary in significant details. Most plant installations are designed to order and the layout and loadings are often provided initially to the structural engineer in terms of estimated or approximate values. It is vital to be aware of the accuracy of the information being used for design at any stage, and to avoid carrying out designs at an inappropriately high level. A considerable margin should be allowed, provided that it is established that the plant designers have not allowed a margin already in estimating the plant loadings. Experience shows that loadings are often over-estimated at the preliminary design stage, but that this is compensated for by new loadings at new locations that were not originally envisaged.

## **3.2 Anatomy of structure**

### **3.2.1 Gravity load paths**

Vertical loadings on industrial steelwork can be extraordinarily heavy; some individual pieces of plant have a mass of 10 000 t or more. Furthermore, by their very nature these loadings generally act as discrete point loads or line loads rather than uniformly distributed loadings. Load values are often ill-defined (see section 3.3.1) at the steelwork design stage and frequently additional vertical loadings are introduced at new locations late in the design process.

For these reasons, the gravity load paths must be established at an early stage to provide a simple, logical and well-defined system. The facility should exist to cater for a new load location within the general area of the equipment without the need to alter all existing main structural element locations. Typically this means that it is best to provide a layered system of beams or trusses with known primary span directions and spacings, and then with secondary (or sometimes in complex layouts, tertiary as well) beams, which actually provide vertical support to the plant.

While simplicity and a uniform layout of structure are always attractive to a structural designer, the non-uniform loadings and layout of plant mean that supporting columns may have to be positioned in other than a completely regular grid to provide the most direct and effective load path to the foundations. It is certainly preferable to compromise on a layout that gives short spans and a direct and simple route of gravity load to columns than to proceed with designing on a regular grid of columns only to lead to a large range of member sizes and even types of beams, girders or trusses (Fig. 3.4).

Similarly, although it is clearly preferable for columns to run consistently down to foundation level, interference at low levels by further plant or equipment is quite common, which may make it preferable to transfer vertical loading to an

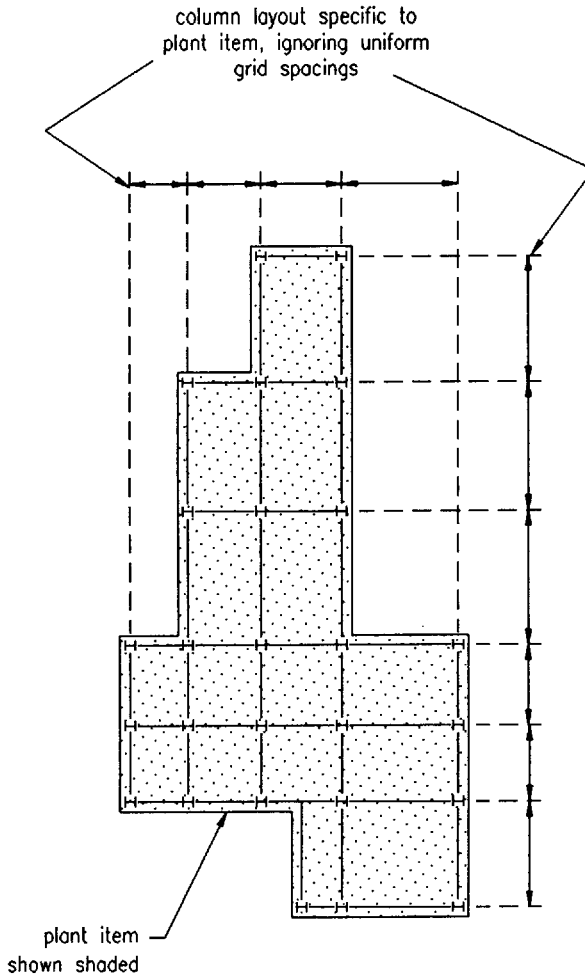


Fig. 3.4 Support steelwork for an unsymmetrical plant item

offset column rather than use much larger spans at all higher levels in the structure. A conscious effort to be familiar with all aspects of the industrial process, and close liaison with the plant designers so that they are aware of the importance of an early and inviolate scheme for column locations, are both necessary to overcome this problem.

It is worth remembering that different plant designers may be handling the equipment layout at differing levels in the structure and ensuring that a briefing from all parties is received before the crucial decision on column spacings is made.

If a widely variable layout of potential loading attachment points exists, then consideration must be given to hanging or top-supporting certain types of plant. A typical example of this is a vehicle assembly line structure, where the overhead

assembly line system of conveyors can sensibly be supported on a deep truss roof with a regular column system. If this is contrasted with the multitude of columns and foundations that would be needed to support such plant from below and the prospect of having to reposition these supports during the design stage as more accurate information on the plant becomes available, then it can be an appropriate, if unorthodox, method of establishing a gravity load path.

### **3.2.2 Sway load paths**

For two fundamental reasons sway load paths require particular consideration in industrial steelwork. First, the plant or equipment itself can produce lateral loading on the structure in addition to wind or seismic load where applicable. Therefore, higher total lateral loadings can exist whose points of application may differ from the usual cladding and floor intersection locations. The type and magnitudes of such additional loads are covered in section 3.3.3.

Second, many industrial steelwork structures lack a regular and complete (in plan) floor construction that provides a convenient and effective horizontal diaphragm. Therefore, the lateral load transfer mechanism must be considered deliberately and carefully at a very early stage in the design (Fig. 3.5).

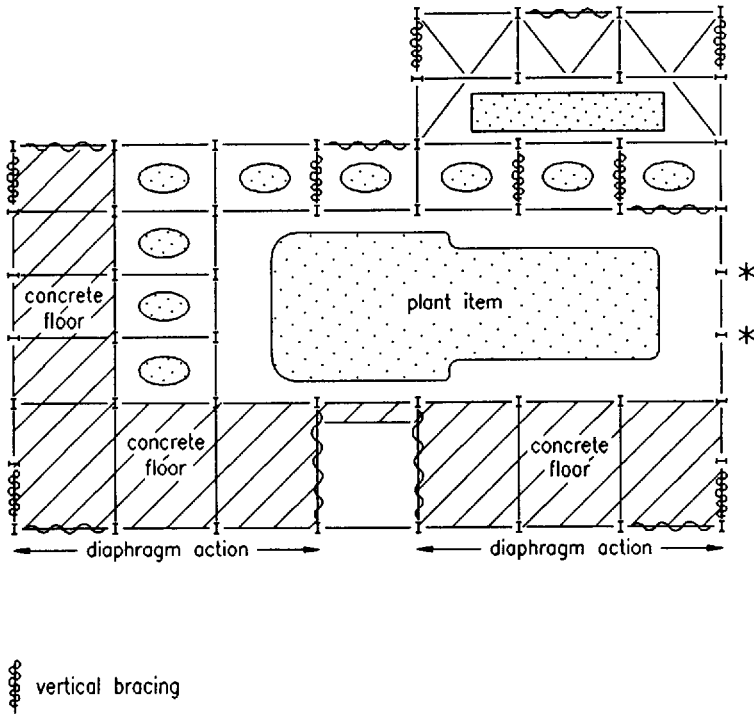
Naturally, there are many different methods of achieving lateral stability. Where floor construction is reasonably complete and regular through the height of the structure, then the design can be based on horizontal diaphragms transferring load to vertical stiff elements at intervals along the structure length or width. Where large openings or penetrations exist in otherwise conventional concrete floors, then it is important to design both the floor itself and the connections between the floor and steelwork for the forces acting, rather than simply relying automatically on the provision of an effective diaphragm as would often and justifiably occur in the absence of such openings.

It can be worthwhile deliberately to influence the layout to allow for at least a reasonable width of floor along each external face of building, say of the order of  $\frac{1}{10}$  of the horizontal spacing between braced bays or other vertical stiff elements.

When concrete floors as described above are wholly or sensibly absent, then other types of horizontal girders or diaphragms can be developed. If solid plate or open mesh steel flooring is used, then it is possible, in theory at least, to design such flooring as a horizontal diaphragm, usually by incorporating steel beams as boom members of an idealized girder where the floor steel acts as the web. However, in practice, this is usually inadvisable as the flooring plate fixings are rarely found to be adequate for load transfer and indeed it may be a necessary criterion that some or all of the plates can be removable for operational or similar purposes. A further factor is that any line of beams used as an assumed truss boom must be checked for additional direct compression or tension loadings; the end connections also have to be designed to transfer these axial forces.

It is therefore normal to provide plan bracing in steelwork in the absence of





\* lateral stability provided at other levels

Fig. 3.5 Establishment of sway load paths

concrete floor construction. The influence that this will have on plant penetrations, pipework routing and many other factors must be considered at an early stage in the liaison with the plant engineers. Naturally, the design considerations of steel beams serving a dual function as truss boom members are exactly as set out above and must not be neglected. Indeed, it may be preferable to separate totally the lateral load restraint steelwork provided on plan from other steelwork in the horizontal plane. This will avoid such clashes of purposes and clearly signal to the plant designers the function of the steelwork, as a result preventing its misuse or abuse at a later stage. Many examples exist where plan bracing members have been removed due to subsequent plant modifications. A practical suggestion to further minimize the possibility of this happening is to paint such steelwork a completely different colour as well as to separate it completely from any duality of function with respect to plant support or restraint.

Where it proves impossible to provide any type of horizontal girder, then each and every frame can be vertically braced or rigid-framed down to foundations. It is best not to mix these two systems if possible, since they have markedly differing stiffnesses and will thus deflect differently under loading.

If diaphragms or horizontal girders are used, then the vertical braced bays that receive lateral loading as reactions from them are usually braced in steelwork. In conventional structures tension-only 'X' bracing is frequently used and whereas this may be satisfactory for some straightforward industrial structures such as tank support frames and conveyor support legs, it often proves necessary to design combined tension/compression bracing in 'N', 'K', 'M' or similar layouts depending on the relative geometry of the height to width of the bay and on what obstruction the bracing members cause to plant penetrations. Indeed, it is sound advice initially to provide significantly more bracing than may be considered necessary, for example, by bracing in two, three or more bays on one line. When later developments in the plant and equipment layout mean that perhaps one or more panels must be altered or even removed, it is then still possible to provide lateral stability by redesigning the bracing using linear elastic plane frame computing techniques, without a major change in bracing location.

One particular aspect of vertical bracing design that requires care is in the evaluation of uplift forces in the tension legs of braced frames. Where plant and equipment provide a significant proportion of the total dead load, then it is important that *minimum* dead weights of the plant items are used in calculations. For virtually every other design requirement it is likely that rounding-up or contingency additions to loadings will have been made, especially at the early stages of the design. It is also important to establish whether part of the plant loading is a variable contents weight and, if so, to deduct this when examining stability of braced frames. In some cases, for example, in hoppers, silos, tanks, this is obvious, but boilers or turbines which normally operate on steam may have weights expressed in a hydraulic test condition when flooded with water. The structural engineer has to be aware of these plant design features in order to seek out the correct data for design (see section 3.3.2).

### 3.2.3 Floors

As has already been discussed in section 3.2.2, full conventional concrete floors are not usual in industrial steelwork structures. The following floor constructions are in common use:

- (1) In situ concrete (cast on to removable formwork)
- (2) In situ concrete (cast on to metal deck formwork)
- (3) Fully precast flooring (no topping)
- (4) Precast concrete units with in situ concrete topping
- (5) Raised pattern 'Durbar' solid plate
- (6) Flat solid steel plate
- (7) Open grid steel flooring.

Some typical sections of floor construction are shown in Fig. 3.6.

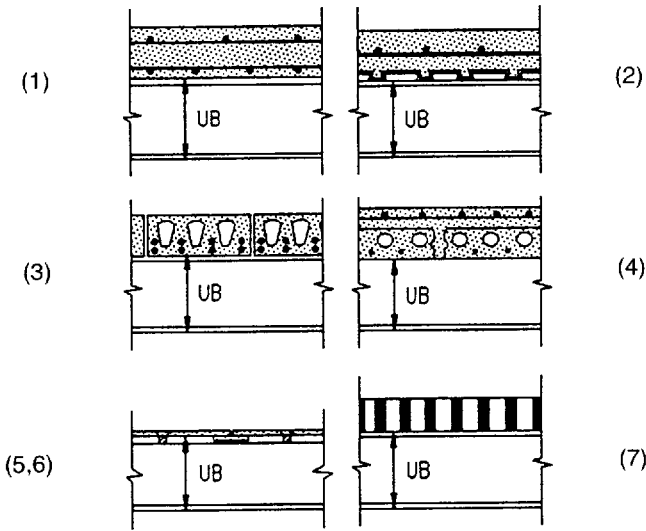


Fig. 3.6 Typical sections of floor construction

The selection of floor type depends on the functional requirements and anticipated usage of the floor areas. Solid steel plates are used where transit or infrequent access is required or where the floor must be removable for future access to plant or equipment. They are normally used only internally (at least in the UK) to avoid problems with wet or waterlogged surfaces.

Open grid flooring is used inside for similar functions as solid steel plate, but with additional functional requirements where the flooring is subjected to spillage of liquids or where air flow through the floor is important. It is also used for stair treads and landings. Consideration should be given to making, say, landings and access strips from solid plate at intervals to assist in promoting a feeling of security among users. It is also in common use externally due to its excellent performance in wet weather.

Concrete floors are in use where heavy-duty non-removable floor areas are necessary. It is not normally advisable to use beam-and-pot-type floorings in any heavy industrial environment due to the damage that can be suffered by lightweight thin walled blocks. For similar reasons, where precast concrete floors require a topping for finishes or to act as a structural diaphragm, it is advisable to use a fully-bonded small aggregate concrete topping with continuous mesh reinforcement, with a typical minimum thickness of 75–100 mm.

A particular advantage of both precast flooring and metal deck permanent formwork is that in many industrial structures the floor zones are irregular in plan and elevation and therefore cheap repetitive formwork is often not practicable.

Even where formwork can sensibly be used, the early installation of major

plant items as steel frame erection proceeds can complicate in situ concrete formwork.

Floors must be able to accept holes, openings and plant penetrations on a random layout, and often must accept them very late in the design stage or as an alteration after construction. This provides significant problems for certain flooring, particularly precast concrete. In situ concrete can accept in a convenient manner most types of openings prior to construction, but it may be prudent deliberately to allow for randomly positioned holes up to a certain size by oversizing reinforcement in both directions to act as trimming around holes within the specified units without extra reinforcement.

Metal deck formwork is not so adaptable as regards large openings and penetrations, since it is usually one-way spanning, especially where the formwork is of a type that can also act as reinforcement. If there is sufficient depth of concrete above the top of the metal deck profile, then conventional reinforcing bars can be used to trim openings. Many designers use bar reinforcement as a matter of course with metal deck formwork to overcome this problem and also to overcome fire protection problems that sometimes occur with unprotected metal decks used as reinforcement.

Steel-plate flooring should be designed to span two ways where possible, adding to its flexibility in coping with openings since it can be altered to span in one direction locally if required. Open-grid flooring is less adaptable in this respect as it only spans one way and therefore openings will usually need special trimming and support steelwork. Early agreement with plant and services engineers is vital to establish the likely maximum random opening required, and any structure-controlled restraint on location.

Other policy matters that should be agreed at an early stage are the treatment of edges of holes, edges of floor areas, transition treatments between different floor constructions and plant plinth or foundation requirements.

This last item is extremely important as many plant items have fixings or bearings directly on to steel and the exact interface details and limit of supply of structural steelwork must be agreed. Tolerances of erected structural steelwork are sometimes much larger than anticipated by plant and equipment designers and some method of local adjustment in both position and level must normally be provided. Where plant sits on to areas of concrete flooring then plinths are usually provided to raise equipment above floor level for access and pipe or cable connections. It is convenient to cast plinths later than the main floor but adequate connection, for example, by means of dowelled vertical bars and a scabbled or hacked surface, should always be provided. It is usually more practical to drill and fix subsequently all dowel bars, anchor bolts for small-scale steelwork and for holding-down plant items, and similar fixings, than to attempt to cast them into the concrete floor.

Except in particularly aggressive environments, floor areas are usually left unfinished in industrial structures. For concrete floors hard trowelled finishes, floated finishes and ground surfaces are all used; selection depends on the use and wear that will occur. Steel plate (solid or open-grid) is normally supplied with

either paint or hot-dip galvanized finishes depending on the corrosiveness of the environment; further guidance is given in BS 4592: Part 1<sup>1</sup> and by floor plate manufacturers.

Steel-plate floors are fixed to supporting steelwork by countersunk set screws, by countersunk bolts where access to nuts on the underside is practicable for removal of plates or by welding where plates are permanent features and unlikely to require replacement following damage.

Alternatively, proprietary clip fixings can be used for open-grid flooring plates to secure the plates to the underside of support beam or joist flanges.

### **3.2.4 Main and secondary beams**

The plan arrangement of main and secondary beams in industrial steelwork structures normally follows both from the layout of the main items of plant and from the column locations. Thus a sequence of design decisions often occurs in which main beam locations dictate the column locations and not vice versa. If major plant occurs at more than one level then some compromise on column position and hence beam layout may be needed.

Since large plant items normally impose a line or point loading there are clear advantages in placing main or secondary beams directly below plant support positions. Brackets, plinths or bearings may be fitted directly to steelwork and for major items of plant this is preferable to allowing the plant to sit on a concrete or steel floor. Where plant or machinery requires a local floor zone around its perimeter for access or servicing, it is common practice to leave out the flooring below the plant for access or because the plant protrudes below the support level.

Deflection requirements between support points should be ascertained. They may well control the beam design since stringent limits, for example, relative deflections of 1 in 1000 of support spans, may apply. In addition when piped services are connected to the plant then total deflections of the support structure relative to the beam-to-column intersections may also need to be limited. Relative deflections can best be controlled by the use of deep beams in lower-grade steel, grade 43 rather than 50; total deflections by placing columns as close as possible to the support positions.

It is preferable to avoid the necessity for load-bearing stiffeners at support points unless the plant dimensions are fixed before steelwork design and detailing take place. Where this is not possible then stiffened zones to prevent secondary bending of top (or bottom if supports are hung) flanges should be provided, even if the design requirements do not require load-bearing stiffeners. This then allows a measure of tolerance for aligning the support positions without causing local overstressing problems.

The stiffness of major plant items should be considered, at least qualitatively, in the steelwork design. Deep-walled tanks, bunkers or silos for example may well be an order of magnitude stiffer than the steel supporting structure.

The loading distribution given by the plant design engineers will automatically assume fully stiff (zero deflection) supports. When the stiffness of the supporting structure is not uniform in relation to the support point locations and loadings, then significant redistribution of loads can take place as the structure deflects. Where the plant support positions and loads and the structural steel layout are symmetrical then engineering judgement can be applied without quantitative evaluation. In extreme cases, however, a plant-structure interaction analysis may be required to establish the loadings accurately.

When hanger supports are required then pairs of beams or channels are a convenient solution which allows for random hanger positioning in the longitudinal direction (Fig. 3.7). Many hanger supports have springs bearings to minimize variations in support conditions due to plant temperature changes or to avoid the plant stiffness interactions described above.

The method of installation or removal of major items of plant frequently requires that beams above or, less commonly, below the plant must be designed to cater for hoisting or jacking-up the installed plant sections. Structural designers should query the exact method and route of plant installation to ensure that the temporary hoisting, jacking, rolling or set-down loads are catered for by the steel beam framework. Experience suggests that these data are not provided as a matter of course, and plant designers commonly believe that the steel structure can support these loads anywhere. Where, to ease the problems, plant installation occurs during steel erection then the method of removing plant during the building life-span may be the most significant temporary loading for the beam framework.

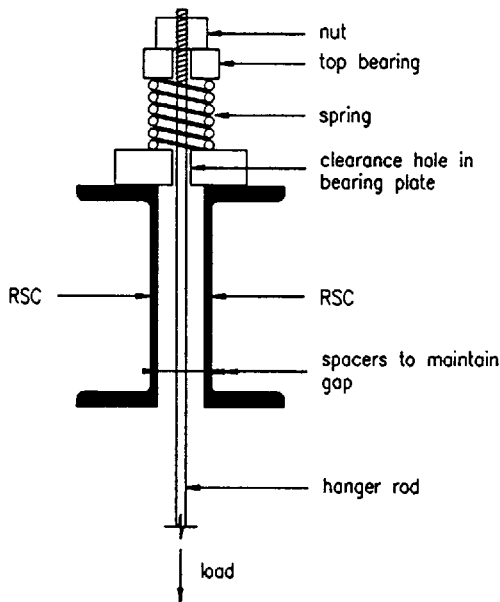


Fig. 3.7 Detail at hanger support

When main or secondary beams are specifically designed for infrequent but heavy lifting operations, it is good practice to fit a lifting connection to the beam to give positive location to the lifting position and to allow it to be marked with a safe working load. For design, smaller load safety factors are appropriate in these circumstances.

### 3.2.5 Columns

Column location in industrial buildings must be decided on practical considerations. Although regular grid layouts are desirable in normal structures, it is sometimes impossible to avoid an irregular layout which reflects the major plant and equipment location, the irregular floor or walkway layouts and an envelope with irregular wall and roof profiles to suit. Obviously some degree of regularity is of considerable benefit in standardizing as many secondary members as possible; a common method of achieving this is to lay out the columns on a line-grid basis with a uniform spacing between lines. This compromise will allow standard lengths for beam or similar components in one direction while giving the facility to vary spans and provide direct plant support at least in the other direction. The line-grids should be set out perpendicular to the longer direction of the structure if possible.

When vertical loadings are high and the capacity of rolled sections is exceeded, several types of built-up columns are available. Where bending capacity is also of importance, large plate I-sections are appropriate, for example, in frameworks where rigid frame action is required in one direction. However, if high vertical loads dominate then fabricated box columns are often employed (Fig. 3.8). Design of box columns is principally constrained by practical fabrication and erection considerations. Internal access during fabrication is usually necessary for fitting of internal stiffeners and similarly internal access may be needed during erection for making splice connections between column lengths, or for beam-to-column connections. Preferred minimum dimensions are of the order of 1 m with absolute minimum dimensions of about 900 mm. Whenever possible, column plates should be sized to avoid the necessity of longitudinal and transverse stiffeners to control plate buckling. The simpler fabrication that results from the use of thick plates without stiffeners should lead to overall economies and the increased weight of the member is not a serious penalty to pay in columns; the same argument does not apply to long-span box girders where increases in self-weight may well be of overriding importance. Under most conditions of internal exposure no paint protection to the box interior is necessary. If erection access is needed then simple fixed ladders should be provided. Transverse diaphragms are necessary at intervals (say 3–4 times the minimum column dimension) to assist in maintaining a straight, untwisted profile, and also at splices and at major beam-to-column intersections even if, as is usually the case, rigid connections are not being used. Diaphragms should be welded to all four box sides and be provided with manhole cut-outs if internal access is needed.

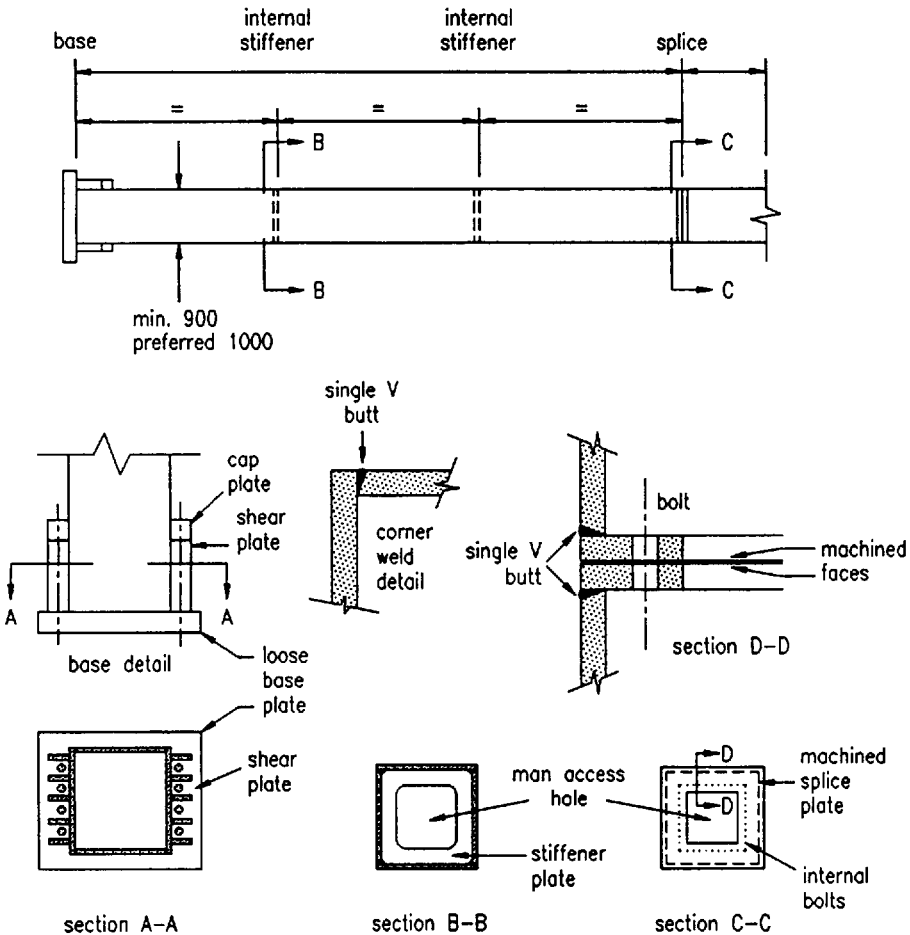


Fig. 3.8 Typical details of box columns

### 3.2.6 Connections

Connections between structural elements are similar to those in general structural practice. Specific requirements relating to industrial steel structures are considered here.

On occasions industrial plant and equipment may impose significant load variations on the structure and so consideration must be given to possible fatigue effects. Since basic steel members themselves are not susceptible to fatigue failure in normal conditions, attention must be focused on fatigue-susceptible details, particularly those relating to welded and other connections. Specific guidance for certain types of structure is available; and where this is not relevant, general fatigue design guidance can be used.



Of general significance is the question of vibration and the possible damage to bolted connections that this can cause. It should be common practice for steelwork in close contact with any moving machinery to have vibration-resistant fixings. For main steelwork connections there is a choice between using HSFG bolts which are inherently vibration-resistant, or using normal bolts with lock-nuts or lock-washer systems. A wide variety of locking systems is available which can be selected after consultation with the various manufacturers.

Connection design for normally-sized members should not vary from established practice, but for the large box and plate I-section members that are used in major industrial steel structures, connections must be designed to suit both the member type and the design assumptions about the joints. For particularly deep beam members, where plate girders are several times deeper than the column dimensions, assumed pin or simple connections must be carefully detailed to prevent inadvertent moment capacity. If this care is not taken, significant moments can be introduced into column members even by notional simple connections due to the relative scale of the beam depth.

In certain cases it will be necessary to load a column centrally to restrict bending on it; a typical example is where deep suspension girders on power station boilers apply very high vertical loadings to their supporting columns. Here, a rocker cap plate detail is often used to assure centroidal load transfer into the column (Fig. 3.9). Conventional connections on smaller scale members would

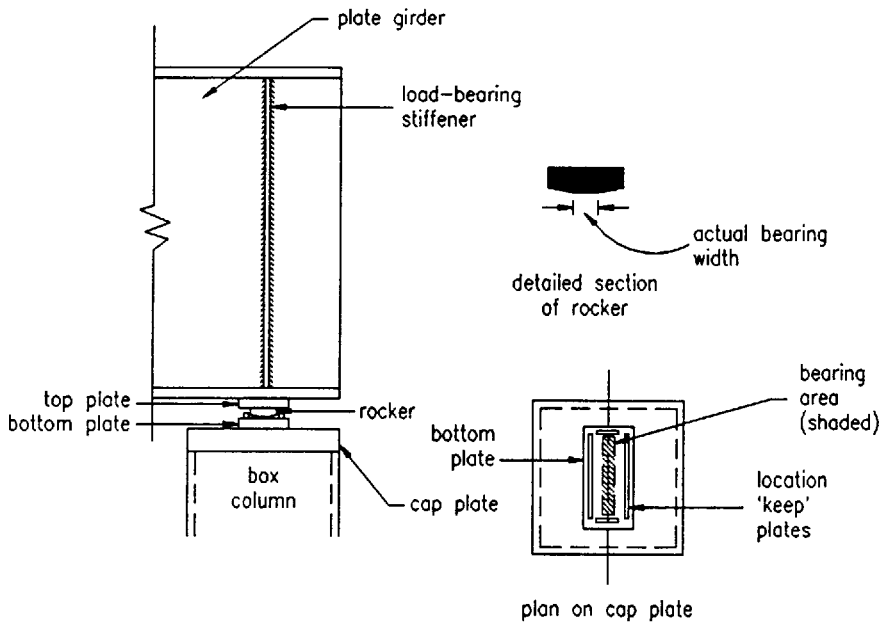


Fig. 3.9 Rocker bearing – plate girder to box column

not usually require such a precise connection as load eccentricities would be allowed for in the design.

### **3.2.7 Bracing, stiff walls or cores**

Section 3.2.2 discusses the particular features of industrial steel structures in relation to achieving a horizontal or sway load path and describes the various methods by which horizontal loads can be satisfactorily transferred to braced bays or other vertical stiff elements. General design requirements and some practical suggestions are also given in section 3.2.2 for braced steel bay design.

The layout on plan of vertically stiff elements is frequently difficult even in conventional and regularly framed structures. General guiding principles are that the centre of resistance of the bracing system in any direction should be coincident with the centre of action of the horizontal forces in that direction. In practice this means that the actions and resistances should be evaluated, initially qualitatively, in the two directions perpendicular to the structural frame layout.

Another desirable feature which is also common to many structures is that the braced bays or stiff cores should be located centrally on the plan rather than at the extremities. This is to allow for expansion and contraction of the structure without undue restraint from the stiff bays, and applies equally to a single structure or to an independent part of a structure separated by movement joints from other parts. It is difficult to achieve this ideal in a regular and uniform structure, and almost impossible in a typically highly irregular industrial steelwork structure. Fortunately, steelwork buildings, particularly those without extensive reinforced concrete floors and with lightweight cladding, are extremely tolerant of temperature movements and rarely suffer distress from what may be considered to be a less than ideal stiff bay layout.

The procedure for design purposes should be as follows; first a basic means of transferring horizontal loading to foundation level must be decided, and guidance on this is given in section 3.2.2. In either or both directions, where discrete braced bays or stiff walls or cores are being utilized, then initially a geometric apportionment of the total loading should be made by an imaginary division of the structure on plan into sections that terminate centrally between the vertically stiff structural element. The loadings thus obtained are used to design each stiff element.

When this process has been completed and if the means exist, by horizontal diaphragm or adequate plan bracing, to force equal horizontal deflections on to each element, a second-stage appraisal may be needed to investigate the relative stiffness of each stiff element. Then the horizontal loading can be distributed between vertical stiff elements on a more accurate basis and the step process repeated.

Considerable judgement can be applied to this procedure, since it is usually only of significance when fundamentally differing stiff elements are used together

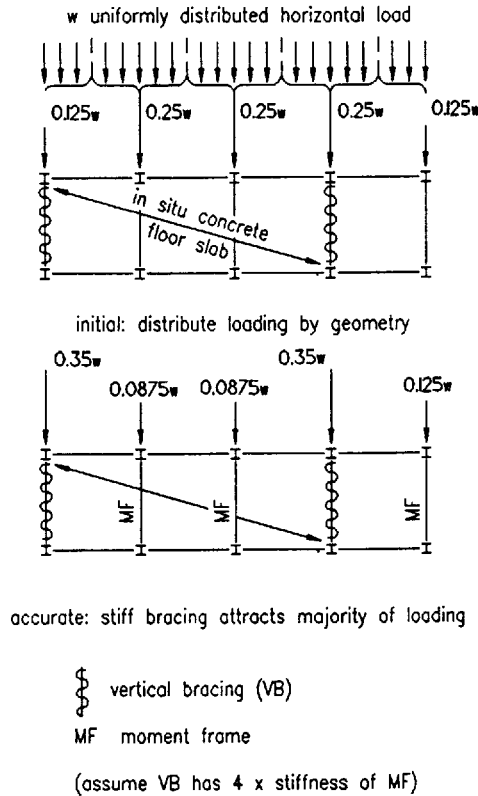


Fig. 3.10 Apportioning horizontal loads to vertical stiff elements

in one direction on the same structure. For example, where a horizontal diaphragm or plan bracing exists and where some of the stiff elements are braced steelwork and some are rigid frames, it will normally be found that the braced frames are relatively stiffer and will therefore carry proportionately more load than the rigid frames. Similarly, where a combination of concrete shear walls (or cores) and braced frames is used, then a relative stiffness distribution will be needed if an effective horizontal diaphragm or plan bracing ensures sensibly constant horizontal deflection or sway (Fig. 3.10).

### 3.3 Loading

#### 3.3.1 General

Two difficulties exist in defining the appropriate loadings on industrial buildings. First, the actual weight, and particularly the details of the position and method of

load application, of items of plant or equipment must be established. Even for routine or replicated plant this information is difficult to obtain in a form that suits the structural engineer. When the plant or equipment is being custom-built then the problem becomes one of timing; information from the plant designer may not be available early enough for the structural design.

The second difficulty that frequently occurs is in the choice of a general, uniformly distributed imposed loading for any remaining floor areas not occupied by items of plant or equipment. Guidance from Codes of Practice must be used carefully when it is applied only to circulation spaces between all the fixed items of plant which are known and whose loading has been evaluated and is considered separately as dead load. Further advice on both these problems is given in section 3.3.2.

The structural steelwork designer must take an open-minded approach to the loading information. It must be appreciated that early information from the plant designers will represent only estimated loadings, and an uncertainty allowance may well already be included in the values supplied, so that further allowances may be unnecessary. However, it frequently turns out that many secondary plant items are added at a later stage in the information process. The loadings from these should be satisfactorily absorbed into an initial uniformly distributed loading allowance provided that a logical scheme for dealing with loading is established at an early stage.

### **3.3.2 Process plant and equipment**

The most important advice to the structural designer of steelwork for an industrial purpose is to ensure reasonable familiarity with the entire process or operation involved. Existing facilities can be visited and the plant designers and operators will normally be more than willing to give a briefing which provides the opportunity to describe the form of structure envisaged to the plant designer at an early stage so avoiding later misunderstandings.

Some attempt should also be made to understand the jargon of the industry in question in order to gain the confidence of the plant designers and to allow effective intercommunication.

Particular examples of structural requirements which are not easily recognized as important by plant designers, and which should therefore be fully explained, are as follows:

- (1) The physical space requirements of bracing members and the fact that they cannot be moved locally to give clearances.
- (2) The actual size of finished steelwork taking account of splice plates, bolt heads and fittings projecting from the section sizes noted on drawings.
- (3) The fact that a steel structure is not 100% stiff and that all loads cause deflections.

- (4) The fact that a steel structure may interact with a dynamic loading and that dynamic overload multipliers calculated or allowed on the assumption of a fully rigid or infinite mass support are not always appropriate.

The basis of loading information for plant and equipment must be critically examined. Frequently loadings are given as a single all-up value, the components of which may not all act together or have only a very small probability of so doing. Alternatively, the maximum loadings may represent a peak testing condition or a fault, overload condition, whereas normal operating loadings may be considerably less in value. Worthwhile and justifiable savings in steelwork can be made if a statistically based examination of the expected frequency and duration of such unusual conditions is made, leading to the adoption of reduced load factors without reducing the overall factor of safety. Comparisons with, for example, wind loading, can be used to establish on a reasonably logical basis the appropriate load factors.

By definition, items of fixed plant can be treated as dead load in accordance with BS 6399: Part 1<sup>2</sup> when specific location and loads are known. At the early stages of design it is usual to adopt a relatively large imposed loading which will have to cater for fixed items of plant or equipment, the existence of which may not even be known at this stage and certainly not the location and loading data. The choice of what imposed loading to use at this stage can be assisted by the following guidance:

|                                     |                         |
|-------------------------------------|-------------------------|
| very light industrial processes     | 7.5 kN/m <sup>2</sup>   |
| medium/average industrial processes | 10–15 kN/m <sup>2</sup> |
| very heavy industrial processes     | 20–30 kN/m <sup>2</sup> |

One factor which will influence the choice within these values is the timing of the release of final plant and equipment design data in relation to the steelwork design and fabrication detailing process. If a second-stage design is possible then a lower imposed load can be allowed since local variations needed to account for specific items of fixed plant which exceed the imposed plan loading allowance can be accommodated.

Under these conditions it can also be worthwhile, particularly for designers with previous experience of the industrial process, to design columns and foundations for a lower imposed loading than beams. In certain layouts with long span main beams or girders at wide spacings this preliminary reduction can also be used for these members. It should be stressed that these proposals are not intended to contradict or override the particular reduced loading clauses in BS 6399,<sup>2</sup> but are a practical suggestion for the preliminary design stage.

When detailed plant layouts with location and loading data become available, fixed plant and equipment can be considered as dead load and subject therefore to the appropriate load factor, 1.4 instead of 1.6. Remaining zones of floor space without major items of plant should be allocated an imposed load which should reflect only the access and potential use of the floor and may therefore vary

well be reduced from the preliminary imposed loading, often in the range of 5–10 kN/m<sup>2</sup>.

Specific laydown areas for removal, replacement or maintenance of heavy plant are the only likely exceptions to this range of loading.

An alternative scheme for dealing with the second stage of loading information is to institute a checking procedure where the equivalent loading intensity of plant and equipment is calculated for each item as follows:

$$\frac{1.4}{1.6} \times \frac{\text{weight (kN)}}{\text{plan area (m}^2\text{)}}$$

the factor 1.4/1.6 being introduced to cater for the reclassification from imposed load to dead load.

Only in bays where this equivalent loading intensity exceeds the preliminary imposed loading will further evaluation be required, unless a scheme of reduced imposed loading for long span beams and columns has been adopted in which case a rigorous check on actual loading intensity must be carried out.

Many items of plant contain moving parts which are always liable to exert dynamic or vibratory loadings on to the structure. Assessing the structural response to these loadings is never easy, particularly when as is usually the case, the plant and the structure are being designed out of sequence and by different designers.

Many rule-of-thumb approximations exist, in which dynamic effects are allowed for by percentage increases to dead load. Some instances of this are codified, for example, crane vertical loadings are factored by 1.25 (see BS 6399: Part 1<sup>2</sup>). Similar multipliers to static loading can be provided by plant suppliers but these must be used with great care and the limitations of such an approach should be appreciated. The dynamic load from one-off impact-type actions or from successive load applications at irregular time intervals depends both on the characteristics of the plant itself *and* the mass and stiffness of the structure to which they are applied. Any dynamic load calculated independently from a knowledge of the structure will be based on assumed structure properties and often on limit values such as zero mass or infinite stiffness. Providing that the structure remains elastic and that resonance or similar frequency-related amplification does not occur the approximate dynamic factors normally represent upper limits. If more accurate evaluations are warranted for major items of plant, a plant–structure interaction dynamic analysis must be undertaken.

Vibrating plant or equipment will transmit vibrations to the structure, the effects of which can be dramatic. The frequency of vibration of the plant can induce resonance in the structure if the natural frequency of vibration of the whole or any part of the structure subjected to the vibrating force is equal or very close to the forcing frequency. Considerable judgement is needed to identify all possible modes of natural vibration that could be excited by the vibrating equipment or machinery. To safeguard against a resonant response there should be no natural frequency of vibration within the range of 0.5–1.5 times the forcing frequency. Useful guidance on calculating natural frequencies of structures is given by Bolton.<sup>3</sup>

A useful initial step is to calculate the lowest natural frequency of vertical motion of the floor construction and to ensure that it is higher than 3–4 Hz (cycles per second). This should avoid problems of response to human-induced vibration, the so-called ‘springiness’ of floors, caused by resonant amplification of footfalls, which lie in the range of 1–2 Hz. Then only plant-induced vibrations of lower than 1 Hz or higher than 2 Hz need to be investigated. Anti-vibration mountings for plant can be specified but these are not an automatic success as they only filter the induced forces and some form of variable loading will still be transmitted to the structure. Various types and grades of anti-vibration mountings are available; information on their suitability can be obtained from the manufacturers, based on details of both the item of plant and the structure.

Many of these devices are intended to reduce vibration of the plant or equipment itself. Care is required to ensure that the altered forcing vibrations which are imposed on to the structure do not have a secondary adverse effect of inducing resonant vibrations into it.

### 3.3.3 Lateral loadings from plant

Lateral loadings imposed by plant on the structure derive from three sources. These are considered separately although there is a common theme throughout that the operating process undergoes a change in regime which is the cause of loading. Many of the actions which give rise to horizontal loads also cause vertical loads or at least vertical loading components which must be incorporated into the design. However, whereas vertical loadings are usually readily understood and allowed for in loadings provided by plant designers, one feature of the horizontal components of such loadings that causes confusion is the fundamental concept of equilibrium. Notwithstanding exotic situations where masses (projectiles) leave or impinge on a structure, or where motion energy is dissipated as heat of friction, equilibrium considerations dictate that lateral components of forces are in balance and consequentially they are often ignored. This is not satisfactory as balancing components may act a considerable distance apart (the load path must be examined in detail) or indeed the balancing components may act at different levels, leading to a more conventionally understood requirement to transfer lateral loading.

The three causes are as follows:

- (1) temperature-induced restraints
- (2) restraint against rotational or (more rarely) linear motion
- (3) restraint against hydraulic or gaseous pressures.

Where plant undergoes a significant change in temperature, plant designers will typically assume that the structure is fully rigid and so can absorb the forces generated by application of restraints at the structure connection points. They will then design the plant itself for the additional stresses that are caused by preventing

free thermal expansion or contraction. This is a safe upper bound procedure since the forces generated in both structure and plant represent maxima, with any deflection at the support reducing forces in both elements. Naturally the structural steelwork designer must be made aware both of the assumption of zero deformation so that the support can be made as stiff as possible in the required direction, and of the forces that are thus imposed.

In spite of the apparent complications of this approach, it is frequently adopted by plant designers for convenience on small items, and to avoid complexities in interconnection between plant items and with piped and ducted services on larger items.

The alternative approach, common on major plant subjected to significant thermal variation such as boilers and ovens, is to assume completely free supports with zero restraint against expansion or contraction. This is a lower bound solution which needs some rational assessment of possible forces that could result from bearing or guide misalignment, malfunction or simple inefficiency. Where large plant items are involved the forces even at such guides or bearings can be significant if the balancing reaction is, for example, at ground level or even outside the structure itself.

The lateral forces from constant speed, rotating machinery, which are usually relatively low, are generally balanced by an essentially equal and opposite set of forces coming from the source of motive power. Nevertheless, their point of application must be considered and a load path established which either transfers them back to balance each other or alternatively down to foundation level in the conventional way. The structural steel designer must have a completely clear and unambiguous understanding of the source and effect of all the moving plant forces, to ensure that all of them are accounted for in the crucial interface between plant and equipment.

The start-up forces when inertia of the plant mass is being overcome, and the fault or 'jamming' loads which can apply when rotating or linear machinery is brought to a rapid halt, need consideration. They are obviously of short duration and so can justifiably be treated as special cases with a lower factor of safety. At the same time the load combinations that can actually co-exist should be established to avoid any loss of economy in design.

Pressure pipe loadings, significant in many plant installations, occur wherever there are changes in direction of pipework and associated pipework supports or restraints. Thermal change must also be considered. Pipework designers may well combine the effects to provide a schedule of the total forces acting at each support position. Since pipework forces are normally *not* reversible in direction, then on major installations the pipework designer may wish to make the installation by 'forcing' the pipework configuration, deliberately making sections too short or too long and then prestressing the pipework so that when installation is complete the operating conditions take the internal pipework stresses through a neutral stress zone and then reverse them.

Forcing is a complex procedure sensitive to lack of fit at the pipework supports and restraints and often to other factors such as the ambient temperature during



installation and the exact sequence of connections. Where major pipe installations are planned and where the pipework designers are adopting these techniques, the structural steelwork designer should acknowledge that the loading values quoted may not be achieved in practice and make a further allowance.

### 3.3.4 Wind loadings

Wind loadings on fully enclosed industrial structures do not differ from wind loadings on conventional structures. The only special consideration that must be given applies to the assessment of pressure or force coefficients on irregular or unusual shaped buildings. A number of sources give guidance on this topic and specific advice can be sought from the Building Research Establishment (BRE) Advisory Service.

However on partly or wholly open structures with exposed plant or equipment great care must be exercised in dealing with wind loading.

It is frequently the case that the total wind loads are higher than on a fully clad building of the same size, due to two causes. First, small structural elements attract a higher force than equivalent exposed areas which form part of a large façade. Secondly, repetitive structural elements of plant items which are nominally shielded by any particular wind direction are not actually shielded and each element is subjected individually to a wind load. The procedure for carrying out this assessment is set out in Section 8 of CP3: Chapter V: Part 2.<sup>4</sup>

Loading on particularly large individual pieces of plant or equipment exposed to wind can be calculated by considering them to be small buildings and deriving overall force coefficients that relate to their size.

For smaller or more complex shapes, such as ductwork, conveyors and individual smaller plant items, it is sensible to take a conservative and easy to apply rule-of-thumb and use an overall force coefficient  $C_f = 2.0$  applied to the projected exposed area. The point of application of wind loadings from plant items on to the structure may be different from the vertical loading transfer points if sliding bearings or guides are being used.

### 3.3.5 Blast loadings

This section deals only with blast loadings from industrial processes and not with any generalized design requirements to survive blast loadings from unspecified sources or of unspecified values.

Varying requirements exist for blast loadings. Typical examples are:

- (1) transformers, where the requirement is usually to deflect any blast away from other vulnerable pieces of plant but where frequently one or more walls and

the roof are open, serving to dissipate much of the energy discharged  
 (2) dust or fine particle enclosures, which are often wholly inside enclosed buildings.

The decisions to be made are as follows.

- (1) Can the potential source of the blast be relocated outside the building altogether, in a separate enclosure?
- (2) If not, can it be placed against the external wall with arrangements to have a major permanent vented area or a specially designed blow-off panel, both of which will limit loadings on the remaining structure?
- (3) Where the location cannot be controlled, it must be established which direction or directions require full protection against damage and which can tolerate certain degrees of damage.

Loading data given by plant designers are usually stated in terms of peak pressures to be applied to projected areas in line with the potential source of the blast. The validity of the data must be treated as being highly suspect since blast loadings are classic examples of true dynamic loading where the time-dependent response of the structure actually determines the loading that is imposed. Quoted blast pressures, which are probably derived from theoretical considerations of high-rigidity high-mass targets fully enclosing the source, may be invalid for steel structures which have tremendous capacity to deform rapidly, absorbing energy and thereby reducing and smoothing out peak blast pressures. Whatever results are obtained from analysis or calculation, it is good practice to use Grade 43 steel which has such good ductility, a lower yield stress from which to commence ductile behaviour and a long and reliable extensibility prior to fracture. While this will ensure reasonable material behaviour, overall ductility of the structure also depends on stability against premature buckling and the ductile behaviour of connections.

Steelwork designers should acknowledge the very imprecise nature of most blast loading data, even when the potential source of the blast is precisely located and specified. They should thus direct their attention to ensuring that collapse does not occur until major deflections and rotations have occurred, following normal guidelines for achieving plastic behaviour.

### **3.3.6 Thermal effects**

This section deals with thermal effects from environmental factors; specific consideration of plant induced thermal effects is given in section 3.3.3. Conventional guidance on the provision of structural expansion or contraction joints is often inappropriate and impractical to implement, and indeed joints frequently fail to perform as intended.

The key to avoiding damage or problems from thermal movements is to consider

carefully the detailing of vulnerable finishes (for example, brickwork, blockwork, concrete floors, large glazing areas and similar rigid or brittle materials). Provided that conventional guidance is followed in the movement provisions for these materials, then structural joints in steel frames can usually be avoided unless there is particularly severe restraint between foundations and low-level steelwork.

Many industrial structures with horizontal dimensions of 100–200 m or more have been constructed without thermal movement joints, usually with lightweight, non-brittle cladding and roofing, and a lack of continuous suspended concrete floors.

When high restraint close to foundations or vulnerable plant or finishes are present, a thermal analysis can be carried out on the steel framework to examine the induced stresses and deflections and to evaluate options such as the introduction of joints or altering the structural restraints. Where steelwork is externally exposed in the UK, the conditions vary locally but a minimum of  $-5^{\circ}\text{C}$  to  $+35^{\circ}\text{C}$  suffices for an initial sensitivity study. For many of the likely erection conditions a median temperature of  $15^{\circ}\text{C}$  can be assumed, and a range of  $\pm 20^{\circ}\text{C}$  can thus be examined. Where the effects of initial investigations based on these values highlight a potential problem, more specific consideration can be given to the actual characteristic minimum and maximum temperatures (advice in the UK is available from the Meteorological Office), and steps may need to be taken to control erection, particularly foundation fixing, to take place at specified median temperatures.

### **3.4 Structure in its wider context**

Industrial structural steelwork is inherently inflexible, being purpose-designed for a particular function or process, and indeed often being detailed to suit quite specific items of major plant and equipment. Nevertheless, it is important to try to cater for at least local flexibility to allow minor alterations in layout, upgrading or replacement of plant items. The most appropriate way to ensure this is to repeat the advice that has been given on numerous occasions already in this chapter. The designer must understand the industrial process involved and be aware of both structural and layout solutions that have been adopted elsewhere for similar processes. Previous structural solutions may not be right, but it is preferable to be aware of them and positively to reject them for a logical reason, than to reinvent the wheel at regular intervals.

General robustness in industrial buildings may be difficult to achieve by the normal route of adopting simple, logical shapes and structural forms, with well-defined load-paths and frequent effective bracing or other stability provisions. Instead of these provisions, then, it is sensible to ensure that a reasonable margin exists on element and connection design. Typically, planning for a 60–80% capacity utilization at the initial design stages will be appropriate, so that even when these allowances are reduced, as so frequently occurs, during the final design and checking stages, adequate spare capacity still exists to ensure that no

individual element or joint can weaken disproportionately the overall structural strength of the building.

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# Chapter 4

## Bridges

by ALAN HAYWARD

### 4.1 Introduction

Use of structural steel in bridges exploits its advantageous properties of economically carrying heavy loads over long spans with the minimum dead weight. Steel is however suitable for all span ranges, categorized in Table 4.1.

**Table 4.1** Span ranges of bridges

|        |               |
|--------|---------------|
| Short  | Up to 30 m    |
| Medium | 30 m to 150 m |
| Long   | 150 m         |

For long spans steel has been the natural solution since 1890 when the Firth of Forth cantilever railway bridge, the world's first major steel bridge was completed. For short and medium spans concrete bridges held a monopoly from 1950 to 1980 because of the introduction of prestressing and precasting. Developments in steel during this period such as higher tensile strength and improved welding techniques were applied mainly to long spans. However, improvements in construction methods from 1980 have enabled steel to restore its market share within Europe and other continents including North America.<sup>1</sup> Contributing factors to this trend are shown in Table 4.2.

**Table 4.2** Factors contributing to the improved market share for steel in short and medium spans from 1980

| Factor  | Reasons   |
|---|---|
| (1) Stability in price of rolled steel products   | Stability worldwide   |
| (2) Automation of fabrication processes           | Mechanized equipment for preparation, welding and girder assembly |
| (3) Faster erection with larger components        | Availability of high-capacity cranes                              |
| (4) Improved design codes                         | Easier methods of design based on research                        |
| (5) Evidence of durability problems with concrete | Life expiry of concrete bridges under 30 years old                |
| (6) Better education in steel design              | Reversal of earlier trend which favoured concrete                 |

Where traffic disruption during construction must be minimized then steel is always suitable. Most bridgework is likely to be carried out under these conditions in the future so that structural steel will continue as a primary choice. Steel has an advantage where speed of construction is vital; it is no coincidence that this usually results in cost economies. If rapidly erected steelwork is used as a skeleton from which the slab and finishes can be carried out without need for falsework then the advantages (summarized in Table 4.3) are fully realized.

For short and medium span highway bridges composite deck construction is economic because the slab contributes to the capacity of the primary members.<sup>2</sup> For continuous spans it uses the attributes of steel and concrete to best advantage. In cases where construction depth is restricted, for example, in developed areas, then half-through or through construction is convenient; this is common for railway and pedestrian bridges.

For long spans, including suspension or cable-stayed bridges, orthotropic plate decks are used. Although the intrinsic costs of a steel orthotropic plate are higher (about four times more) than an equivalent concrete slab, the advantage in dead weight reduction (approximately 1:3 ratio) may more than offset this when the overall economy is considered. Steel decks are also employed when erection must be completed in limited occupations, such as for railway bridges on existing

**Table 4.3** Advantages of Steel Bridges

| Feature                                    | ... leading to ...   | Advantages   |
|--|--|--|
| (1) Low weight of deck                     | Smaller foundations. Typical 30%–50% reduction of weight compared with concrete decks. | Economy  |
| (2) Light units for erection               | Erection by mobile cranes  | Rapid construction                                 |
| (3) Bolted site connections                | Minimal site inspection  | Flexible site planning                             |
| (4) Prefabrication in factory              | Effective quality control  | More reliable product                              |
| (5) Modern methods of protective treatment | Application of treatment before erection. Long life to first maintenance.              | Predictable whole life cost of structure           |
| (6) Use of weathering steel                |  | Minimum whole life cost                            |
| (7) Shallow construction depth             | Minimum length of approach grades  | Overall economy of highway. Slender appearance.    |
| (8) Self-supporting steel                  | Elimination of falsework   | Easier construction especially for high structures |
| (9) Continuous spans                       | Fewer bearings and joints  | Slender appearance. Reduced maintenance cost.      |

routes. Moving bridges of swing, lift, or rolling-lift ('bascule') type usually employ steel decks to rationalize the amount of counterweighting and the mechanical equipment. For long spans of suspension or cabled-stayed form then special considerations affect the design including aerodynamic behaviour, the feasibility of deep foundations in estuarial conditions, cables with anchorages, non-linear structural behaviour and the absolute necessity to include the effects of the erection procedure in the design process.

This chapter on bridges gives emphasis to initial design, an important stage of the process, because the basic decisions as to member proportions, spacings and splice positions vitally affect economy of the structure. It is essential that the detailed analysis is based upon optimized sizes which are as accurate as possible. If this is not achieved then the detailed design will be inefficient because time consuming repetitive work will have been expended, adversely affecting the economy of the design and the construction costs. Guidance is given on the initial design of highway bridges using composite deck construction, which is a significant proportion of the number of steel bridges built.

## 4.2 Selection of span

The majority of bridges fall within the category of short span because for many crossings of rivers, railways or secondary highways a single span of less than 30 m is sufficient. For multiple-span viaducts a decision on span length must be made, which depends on factors shown in Table 4.4.

For long viaducts it is necessary to carry out comparative estimates for different spans to determine the optimum choice, as shown in Fig. 4.1.

**Table 4.4** Factors which decide choice of span for viaducts

| Factor  | Reasons  |
|---|--|
| Location of obstacles   | Pier positions are often dictated by rivers, railway tracks and buried services  |
| Construction depth  | Span length may be limited by the maximum available construction depth   |
| Relative superstructure and substructure costs                    | Poor ground conditions require expensive foundations; economy favours longer spans   |
| Feasibility of constructing intermediate piers in river crossings | (a) Tidal or fast-flowing rivers may preclude intermediate piers<br>(b) For navigable waterways, accidental ship impact may preclude mid-river piers |
| Height of deck above ground                                       | Where the height exceeds about 15 m, costs of piers are significant, encouraging longer spans  |
| Loading   | Heavier loadings such as railways encourage shorter spans  |

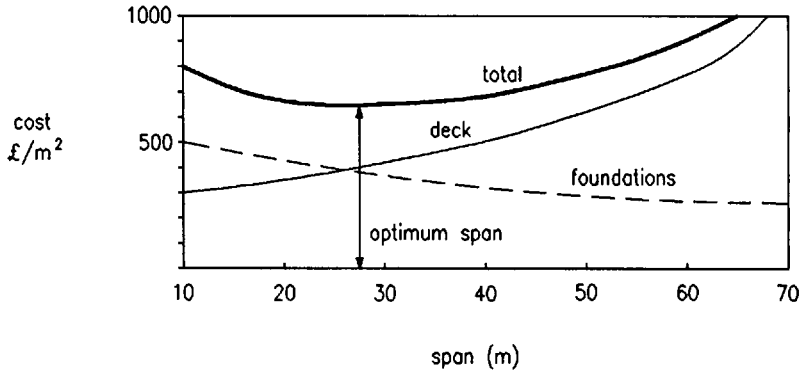


Fig. 4.1 Choice of optimum span for viaducts

Typical optimum spans are shown in Table 4.5.

**Table 4.5** Typical optimum span ranges (m) for viaducts

| Conditions  | Highway | Railway |
|---|---------|---------|
| Simple foundations<br>(spread footing or short piles) | 25–45   | 20–30   |
| Difficult foundations<br>(piles 20 m long)            | 35–55   | 25–40   |
| Piers 15 m high                                       | 45–65   | 30–45   |

Bridges of medium span exceeding 100 m and those of long span are usually only adopted when a larger number of shorter spans are precluded by restriction of the site. This is because the material content and cost per unit length of long spans is much greater. Therefore the bridging of a wide river or estuary should generally use a number of medium spans. Only if there is a high risk of shipping collision, or if the depth and speed of water flow is such as to make foundation construction very difficult, should a long-span bridge be chosen.

### 4.3 Selection of type

Suspension or cable-stayed bridges are suitable for the longest spans, but are less suitable to support heavy loading across short or medium spans. At the same time medium-span footbridges can appropriately be suspension or cable-stayed types because concentrated loading is absent. Some of the considerations given to long spans such as aerodynamics need to be applied to footbridges. Other bridge types such as arches or portals may be suitable in special locations. For example, an arch is a logical solution for a medium span across a steep-sided ravine.



Through trusses are suitable where the available construction depth is limited. The vast majority of short and medium span highway bridges are formed with composite construction because the highway profile can be arranged to suit the depth available.

For short and medium spans the most important factor which influences the type is the available construction depth. Where depth is limited then types such as arch, portal or truss offer an alternative solution. Types of steel bridge are shown in Fig. 4.2 with their normal economic span range and the world's longest. Each is briefly described below.

### 4.3.1 Suspension bridges

Suspension bridges (Fig. 4.3) are used for the longest spans across river estuaries where intermediate piers are not feasible. The cables form catenaries supporting both sides of the deck and are tied to the ground usually by gravity foundations sometimes combined with rock anchors. Thus ground conditions with rock at or close to the surface of the ground are essential. Towers are usually of twin steel box members which are braced together above the roadway level. They are designed so as to be freestanding under wind loading during construction until the cables are installed. Cables are either a compacted bundle of parallel high tensile steel strands (commonly 5 mm diameter) installed progressively by 'spinning' or may be formed from a group of wire ropes. Deck hangers are wire ropes (or round steel rods for light loading as for a footbridge) clamped to the cable and connected to the deck at a spacing equal to the length of each deck unit erected, typically 18 m. The construction process for suspension bridges is more time consuming than for other types because the deck cannot be installed until the towers, anchorages, cable and hangers are completed.

Depending upon ground conditions, the cables can be catenaries supporting the side spans. Cables may alternatively be straight from tower top to the ground anchorages and merely support a main span, side spans being non-existent or formed as short-span viaducts. Decks are usually trusses with a steel orthotropic plate floor spanning between. Footways are often cantilevered outside the two sets of cables.

Aerodynamic behaviour must be considered in design because of the tendency for the deck and cables to oscillate in flexure and torsion under 'vortex shedding' and other wind effects. This is due to the flexible nature and light weight of suspension bridges illustrated by the collapse of the USA Tacoma Narrows Bridge in 1940 which had a very flexible narrow deck consisting of twin plate girders forming a torsionally weak deck of 'bluff' shape prone to wind vortex shedding. Aerodynamic considerations often justify wind tunnel testing of models. In the Severn Bridge of 1966 the deck is a steel box girder with integral orthotropic floor having an aerofoil cross section which discourages vortex shedding and reduces the drag coefficient. This and the Bosphorus Bridge of 1970 use inclined hangers

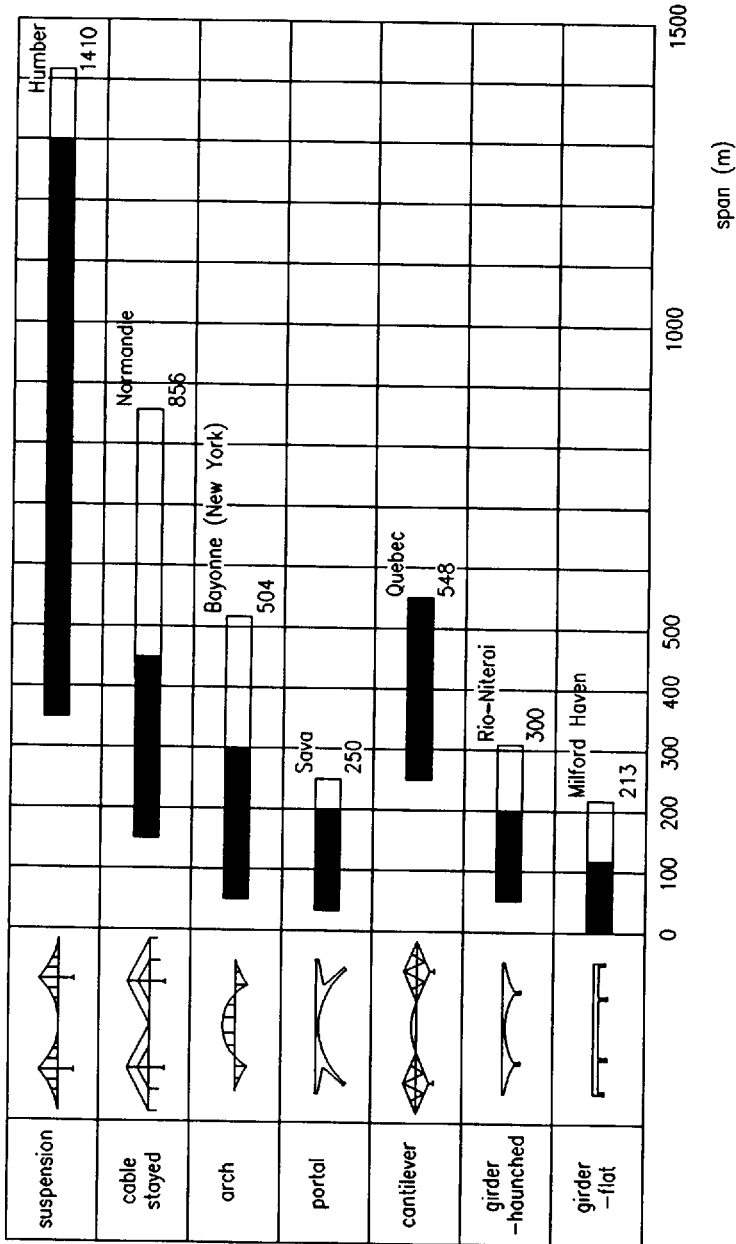


Fig. 4.2 Normal span range of bridge types

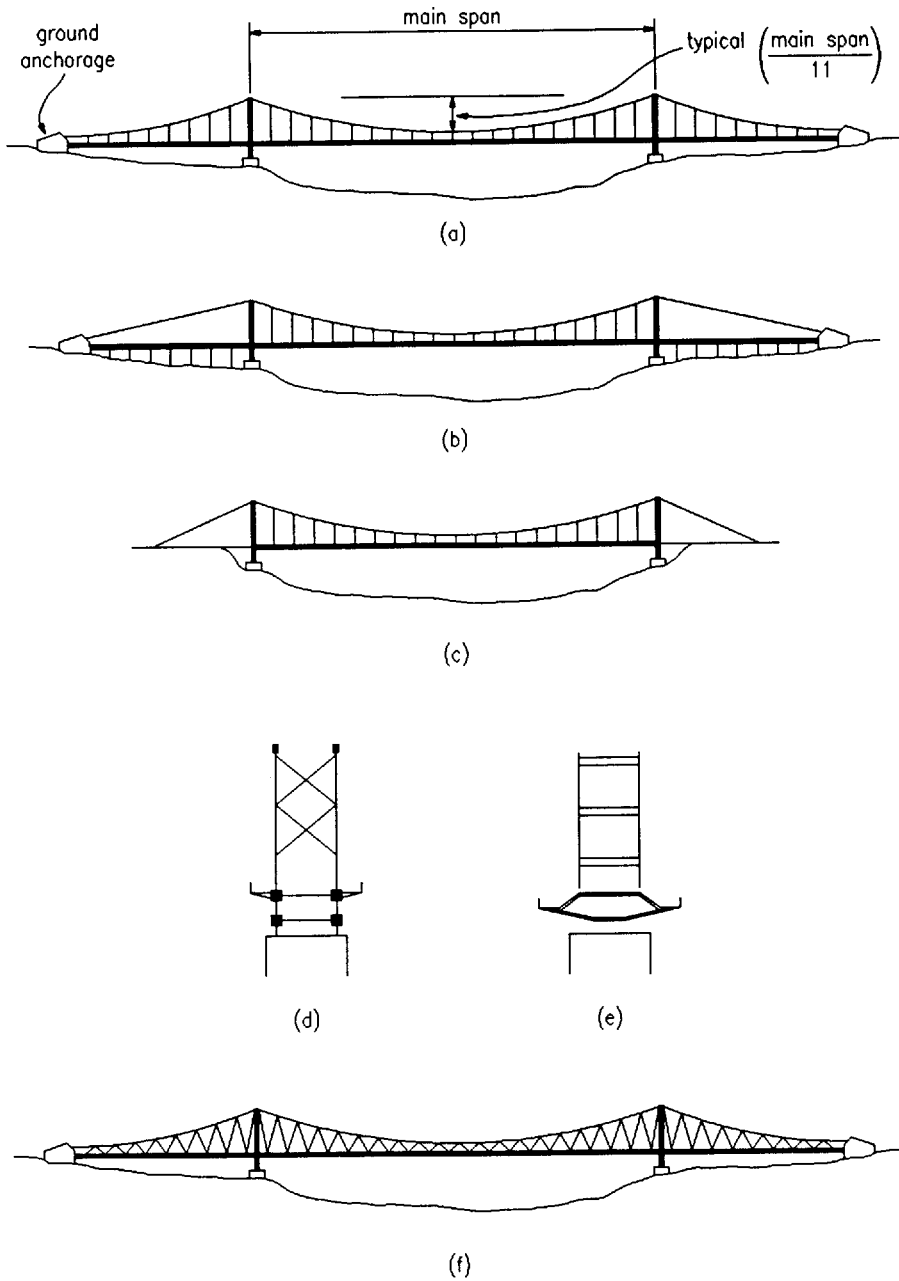


Fig. 4.3 Suspension bridges. (a) Three-span suspended; (b) straight back stays, viaduct side spans; (c) straight back stays, no side spans; (d) truss deck; (e) aerofoil box deck; (f) inclined hangers

that form a truss system which helps to reduce any tendency to oscillate. Suspension bridges behave as non-linear structures under asymmetric deck loading so that deflections may be large. Behaviour under such loading depends upon the combined gravity stiffness and the flexural rigidity of the deck or stiffening girder. The type is less suitable for heavy loading such as railway traffic, especially for short spans. Suspension bridges are sometimes suitable for medium spans carrying pedestrian or light traffic.

### **4.3.2 Cable-stayed bridges**

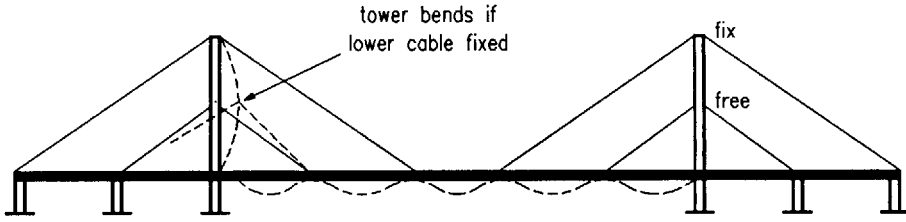
Cable-stayed bridges (Fig. 4.4) are of a suspension form using straight cables which are directly connected to the deck. The structure is self-anchoring and therefore less dependent upon good foundation conditions, but the deck must be designed for the significant axial stress from the horizontal component of the cable forces. The construction process is quicker than for a suspension bridge because the cables and deck are erected at the same time and the amount of temporary works is reduced. Either twin sets of cables are used or alternatively for dual carriageways a single plane of cables and tower can be located in the central reserve space. Two basic forms of cable configurations are used, either 'fan' or 'harp'. A fan layout minimizes bending effects in the structure due to its better triangulation but anchorages can be less easy to incorporate into the towers. The harp form is often preferred where there are more than say, four cables. The number of cables depends on the span and cable size, which is often selected such that each fabricated length of deck (say, 20 m) contains an anchorage at one end to suit a cantilever erection method. Bridges either have two towers and are symmetrical in elevation or have a single tower as suited to the site.

Decks are generally an orthotropic steel plate but composite slabs can be used for spans up to about 250 m. A box girder is essential for bridges having a single plane of cables to achieve torsional stability, but otherwise either box girders or plate girders are suitable. Aerodynamic oscillation is a much less serious problem than with suspension bridges but must be considered. Some bridges with plate girders incorporate non-structural aerodynamic edge fairings.

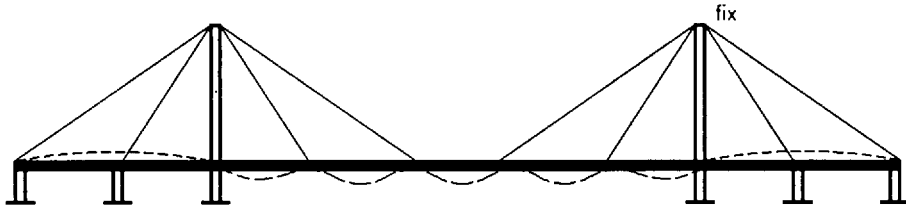
It is essential to use cables of maximum strength and modulus at a high working stress so that sag due to self-weight, which produces non-linear effects, is negligible. Cables are normally of parallel wires or prestretched locked coil wire rope. During erection the cable lengths are adjusted or prestressed so as to counteract the dead load deflections of the deck arising from extension of the cables.

### **4.3.3 Arch bridges**

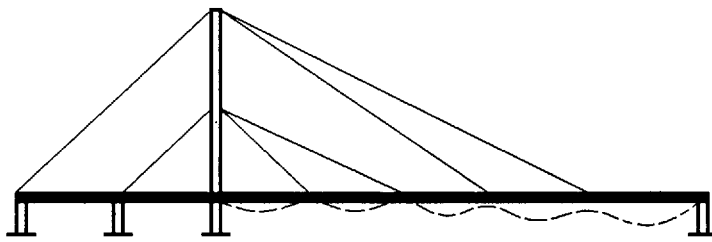
Arch bridges (Fig. 4.5) are suitable in particular site conditions. An example is a medium single span over a ravine where an arch with spandrel columns will



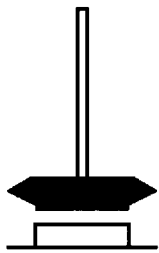
(a)



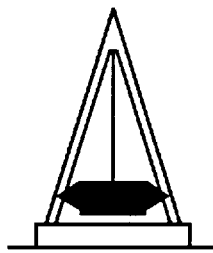
(b)



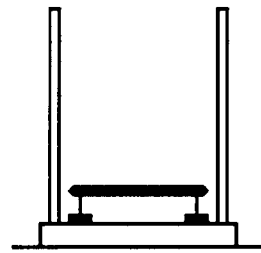
(c)



(d)

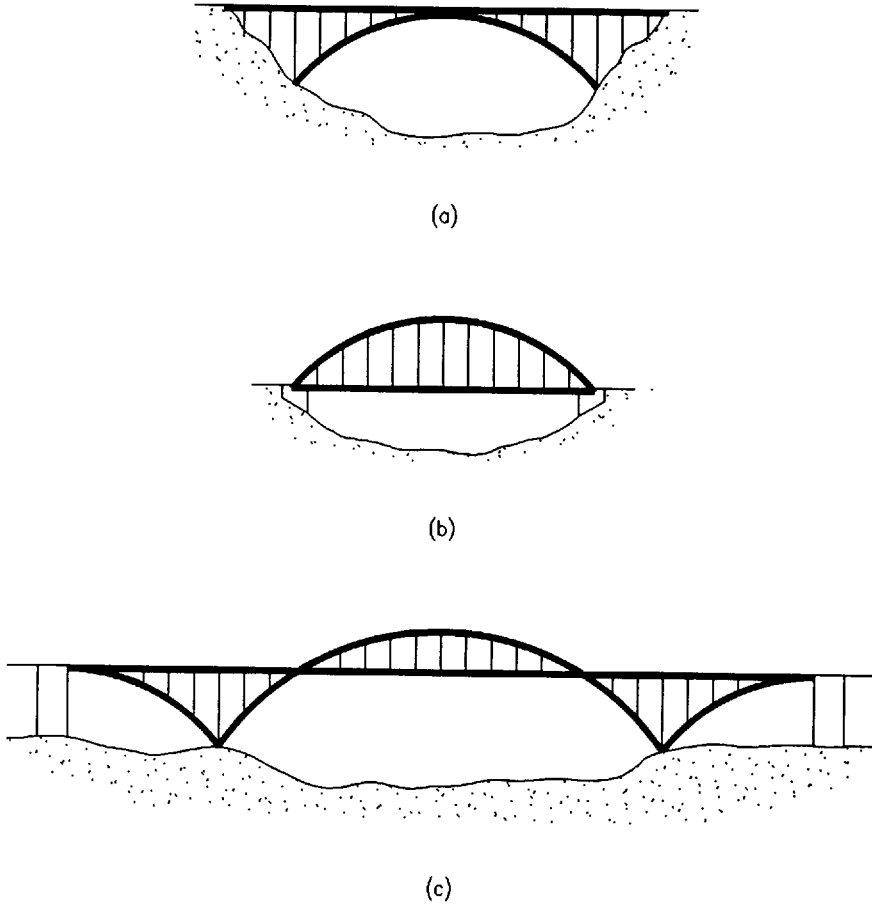


(e)



(f)

Fig. 4.4 Cable-stayed bridges. (a) Harp; (b) fan; (c) single tower; (d) single plane; (e) single plane; (f) twin plane



*Fig. 4.5* Arch bridges. (a) Spandrel post arch; (b) tied arch; (c) part tied arch

efficiently carry a deck with the horizontal thrust taken directly to rock. A tied arch is suitable for a single span where construction depth is limited and presence of curved highway geometry or other obstruction to the approaches conflicts with the back stays of a cable-stayed bridge.

#### 4.3.4 Portal frame bridges

Portal frame bridges (Fig. 4.6) are mainly suitable for short or medium spans. In a three-span form with sloping legs they can provide an economic solution by offering a reduction in span and have an attractive appearance. The risk of shipping collision with sloping legs must be considered for bridges over navigable

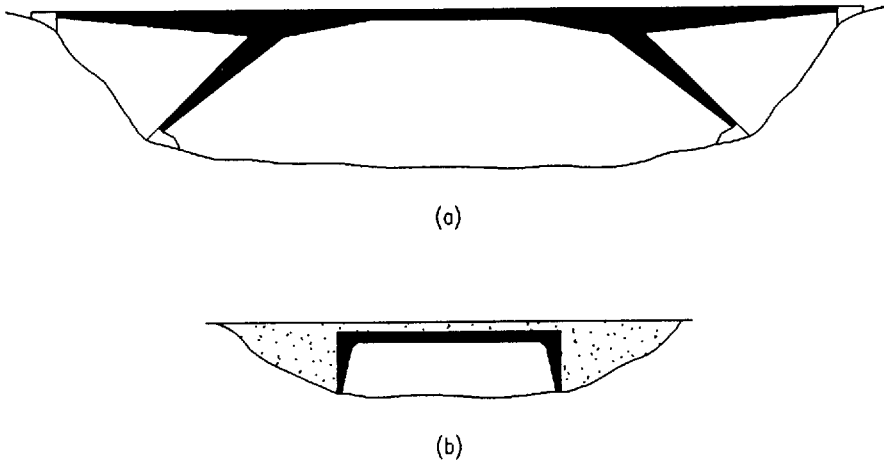


Fig. 4.6 Portal frame bridges. (a) Three-span inclined legs; (b) single span

riders. Portal bridges tend to be less economic than beam bridges because the foundations must be designed to resist horizontal thrust, complex details can be required at the joints and erection is more complicated.

#### 4.3.5 Truss bridges

Through trusses are used for medium spans where a limited construction depth precludes use of a composite deck bridge. They are suitable in flat terrain to reduce the height and length of approach embankments and for railway bridges where existing gradients cannot be modified. A truss may be unacceptable visually; a bowstring truss is an alternative solution. For short spans and medium spans up to 50 m, trusses are generally less economic than girders because of higher fabrication cost. They are therefore adopted only where the available construction depth is not sufficient for composite beams. (See Fig. 4.7.)

#### 4.3.6 Girder type

Girder bridges (Fig. 4.8) predominate over the previously described types for short and medium spans, and generally provide the most economic solution. For highway bridges composite deck construction is generally used unless the depth is very critical in which case half-through girders or through trusses may be necessary. Railway bridges frequently require to be of half-through or through form because of depth limitations and are more suitable, being generally narrower. Pedestrian

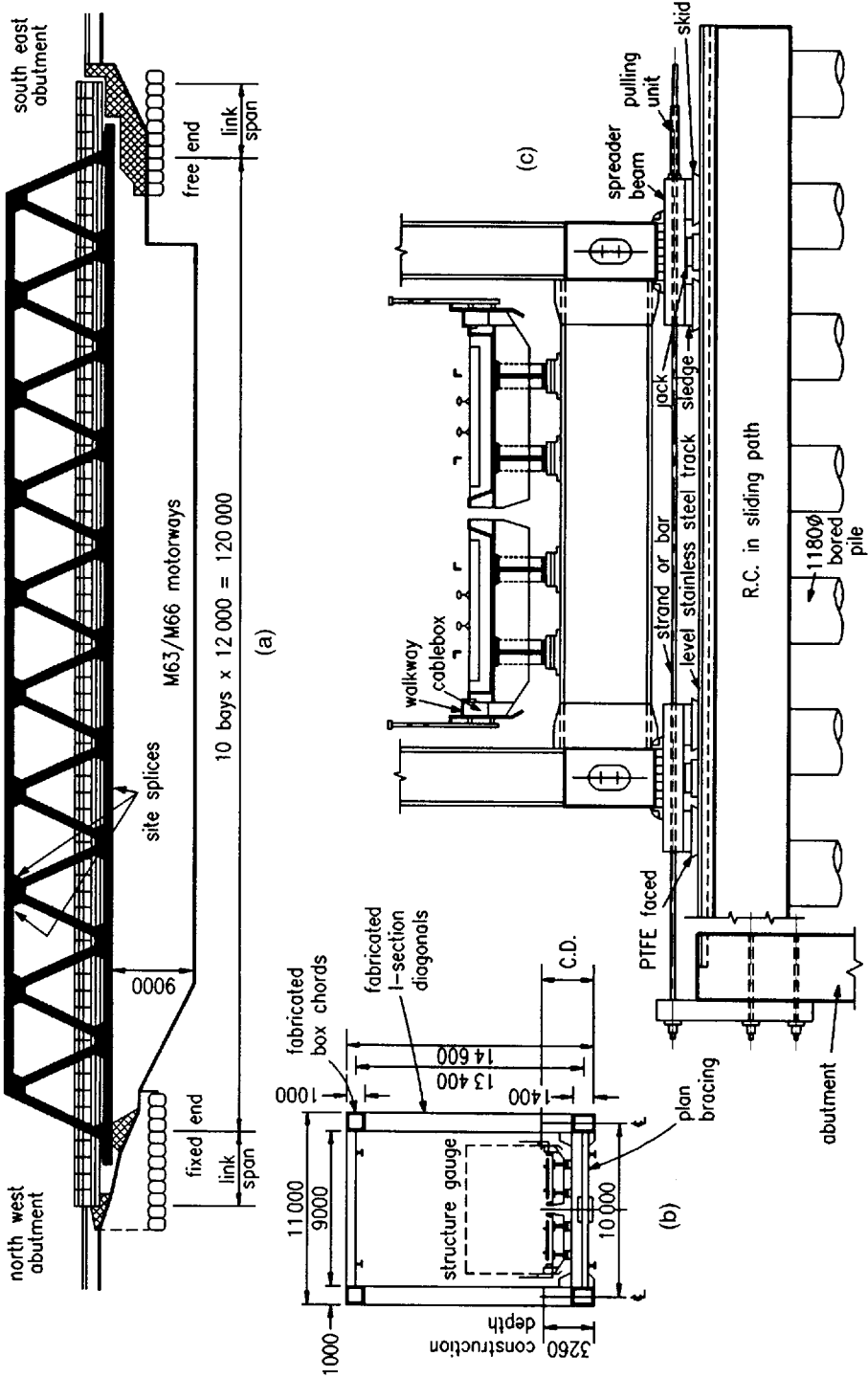


Fig. 4.7 Truss bridge: (a) elevation (b) cross section (c) arrangements for sliding into position



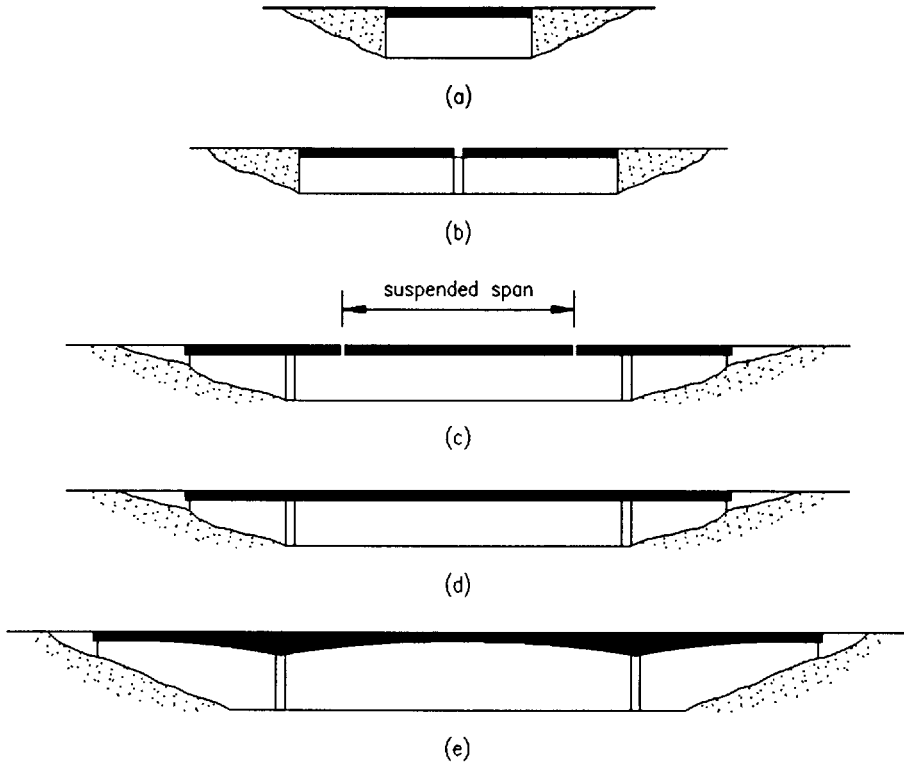


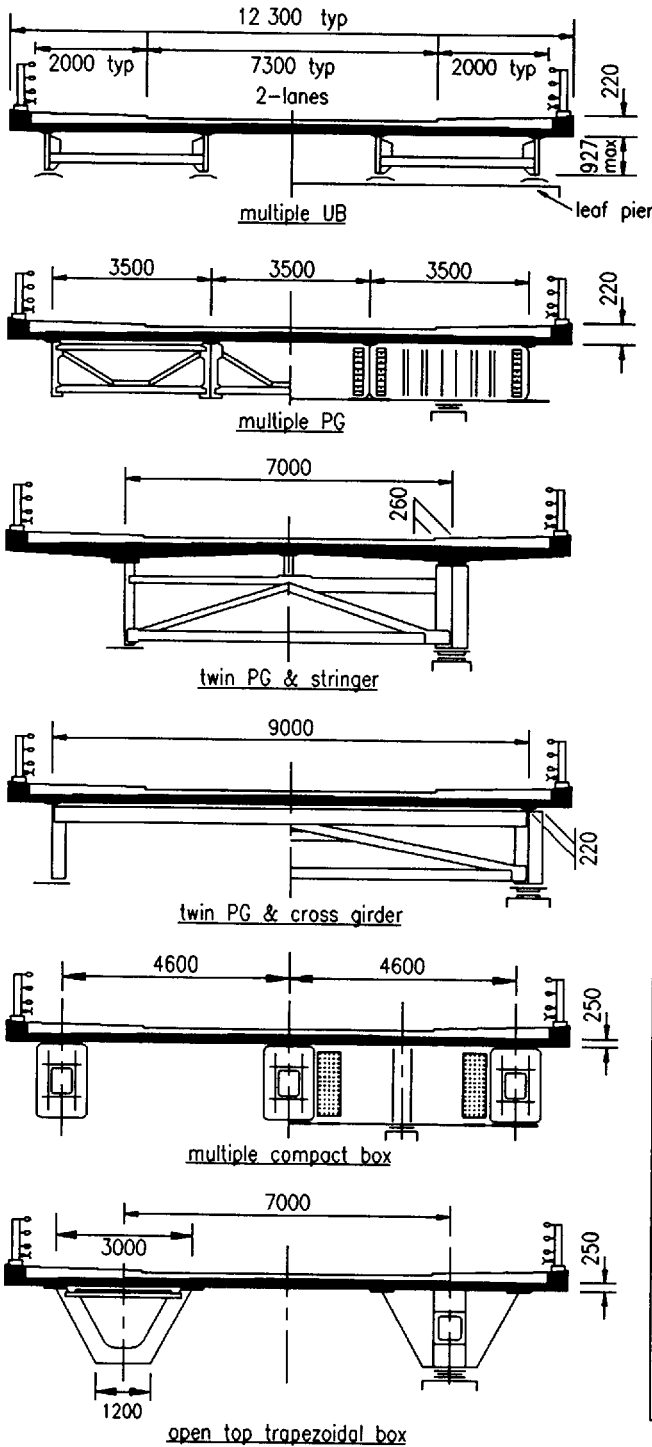
Fig. 4.8 Girder type bridges. (a) Single span; (b) simply-supported spans; (c) cantilever and suspended span; (d) continuous; (e) continuous – curved soffit

bridges are similarly suited to a half-through form. Highway, railway and pedestrian bridges of girder type for short and medium spans are further described below.

#### 4.3.6.1 Highway bridges – composite deck construction

(see also Chapter 17)

Composite deck construction (Fig. 4.9) should be used wherever the construction depth will permit. If possible multiple spans should be made continuous over the intermediate supports so reducing the number of bearings and expansion joints. Continuity gives economies throughout the structure and reduces traffic disruption arising from the maintenance needs of these vulnerable elements. A number of options are available for maintaining continuity over intermediate supports. If ground conditions are poor such that the predicted differential settlement of the supports is significant (say, exceeding  $(\text{span}/1000)$ ) then to avoid overstress the structure should be made statically determinate by use of simply-supported spans.



| span range | remarks   |
|------------|---|
| > 25       | use plastic stress analysis for economy         |
|            | may use pier cross-head as below                |
| 25 to 100  | steel cross-head shown to reduce no. of columns |
|            | may use leaf pier as above                      |
| 35 to 90   | unsuitable curved soffit                        |
| 35 to 90   | suitable curved soffit                          |
| 35 to 100  | no bracing up to 60 m span                      |
|            | uneconomic unless aesthetics govern             |
|            | steel cross-head shown to reduce no. of columns |
| 35 to 100  | no bracing up to 60 m span                      |
|            | temporary plan bracing required                 |

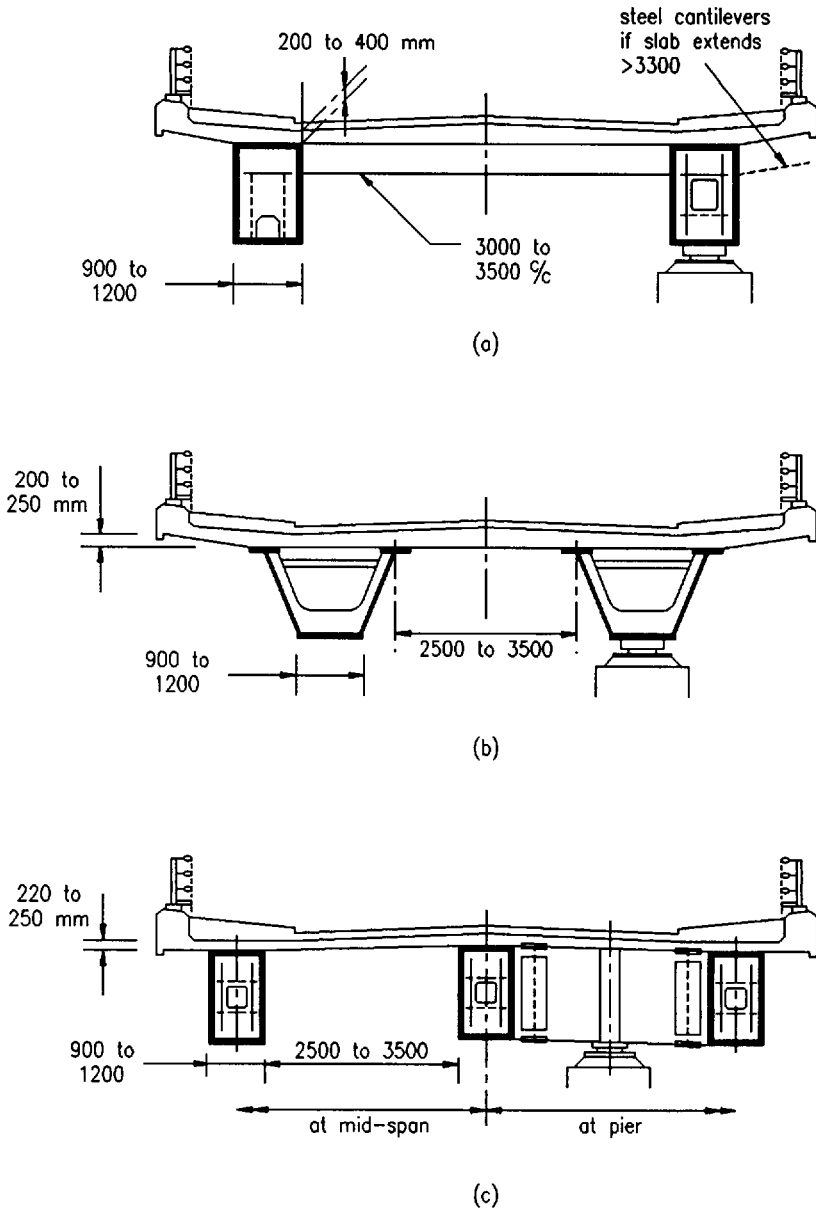
Fig. 4.9 Highway bridges – composite deck construction

Cantilever and suspended spans are alternative options which retain some of the advantages of continuity. A girder depth of  $(\text{span}/20)$  (girder depth excludes floor slab) is generally economic although shallow girders can be used down to a depth of  $(\text{span}/30)$  or less.

Rolled sections, available up to 914 mm  $\times$  419 mm serial size, are appropriate for short spans up to 25 m span if simply supported and about 33 m when continuous. For continuous spans exceeding about 22 m, fabricated plate girders will show economy because lighter flanges and webs can be inserted in the mid-span regions. Automated manufacture of plate girders means that they are highly economic when compared with box girders. Normally a girder spacing of 2.5–3.5 m is optimum with a floor slab of about 200–240 mm thick. Edge cantilevers should not exceed 50% of the beam spacing and to simplify falsework should where possible be less than 1.5 m. An even number of girders (i.e. 2, 4, 6, 8, etc.) achieves better optimization for material ordering and permits girders to be braced in pairs for erection.

For medium spans exceeding 40 m where adequate construction depth is available it may be economic to use twin girders only. A number of variants are available as shown in Fig. 4.9, using a thickened haunched slab, longitudinal stringers and cross girders to support the slab intermediately. For narrow bridges the complete precasting of composite floors may offer advantages in speed of construction.<sup>3</sup> Use of girders with a curved soffit becomes economical for medium spans exceeding 45 m and efficiently achieves maximum headroom if required over the central portions of a span (see Fig. 4.9). Plate girder flanges should be proportioned so as to be as wide as possible consistent with outstand limit to reduce the number of intermediate bracings. For practical reasons a desirable minimum flange width is about 400 mm to accommodate shear connections and to permit the possible use of permanent formwork. A maximum flange thickness of 65 mm is recommended as a guide to avoid heavy butt welds, but thicker flanges can be used where necessary, up to say 100 mm maximum.

For medium spans exceeding 100 m, box girders (see Fig. 4.10) are more suitable than plate girders for which flange sizes would be excessive. Other reasons for using box girders at these spans may include a need to improve aerodynamic stability, the presence of severe plan curvature, a requirement for single column supports or very limited construction depth. However for spans less than 100 m, box girders are generally less economic because, although a reduction in flange sizes may be possible due to superior load distribution properties, this is more than offset by the amount of internal diaphragms and stiffening and the extra costs in manufacture. Fabrication costs are high because the assembly and welding processes are less amenable to automation than with plate girders. Also access must be permitted inside box girders for welding, protective treatment processes, and permanent inspection. However erection of box girders is often easier because they require minimal external bracing to maintain overall stability. Multiple compact section box girders have proved to be economic for spans of up to 50 m in particular situations where longitudinal stiffeners can be eliminated. Open-top trapezoidal box girders (known as 'bath tubs') are widely used in North



*Fig. 4.10* Highway bridges – box girders. (a) Twin box and cross girders (spans 40–150 m); (b) open top box (spans 40–100 m); (c) multiple box (spans 30–60 m)

America and possess some of the advantages of plate girders. However temporary bracing is required during construction to maintain shape and relative twist of the sections until the concrete slab is placed and the full torsional rigidity achieved. Following a number of problems this subject has been researched in Canada.<sup>4</sup>

#### 4.3.6.2 Railway bridges – girder type (Fig. 4.11)

Many existing small-span railway bridges weather cast or wrought iron girders to which rails are fixed directly without use of ballast or half-through girders with trough floors. As these bridges have reached the end of their lives they have been replaced in steelwork in modern form with ballasted track. The legacy of the original decks with their very shallow construction depth has influenced modern under-line bridge practice in replacements and new bridges. The majority of railway underline bridges therefore tend to be of half-through type. The direct fastening of track without ballast gives the cheapest possible form of railway bridge and is appropriate for carrying sidings where accuracy and adjustment of the track are less critical.

Girder depths are generally greater than for highway bridges due to the heavier loading and because limits for deformation are necessary on high-speed routes. A span-to-girder depth ratio of 12 to 15 is typical. For short spans half-through plate girders are used with composite steel cross girders forming rigid U-frames and supporting a concrete floor with ballasted single or double track. Through construction is appropriate for medium spans exceeding 50 m using trusses. For spans up to 39 m, British Rail use a standard box girder design with a steel ribbed floor of minimal depth which is achieved by spanning between the inner webs of trapezoidal box girders proportioned so as to fit closely within the station platform space. The type has advantages in using components entirely of steel which are bolted together at site and commissioned during temporary possession of existing tracks. Where sufficient depth is available then deck construction is preferable and more economic, with either twin plate girders or a box girder beneath each rail track.

Simply-supported spans are widely used for railway bridges because:

- (a) individual spans can be erected or replaced quickly during temporary track possession,
- (b) uplift is more likely to occur if spans are unequal under heavy railway loading,
- (c) fatigue is less critical.

#### 4.3.6.3 Pedestrian bridges (Fig. 4.12)

A minimum clear deck width of 1.8 m is usual, increased to 3.0 m or 4.0 m in busy areas or if a cycleway is also present. Steel provides an efficient solution

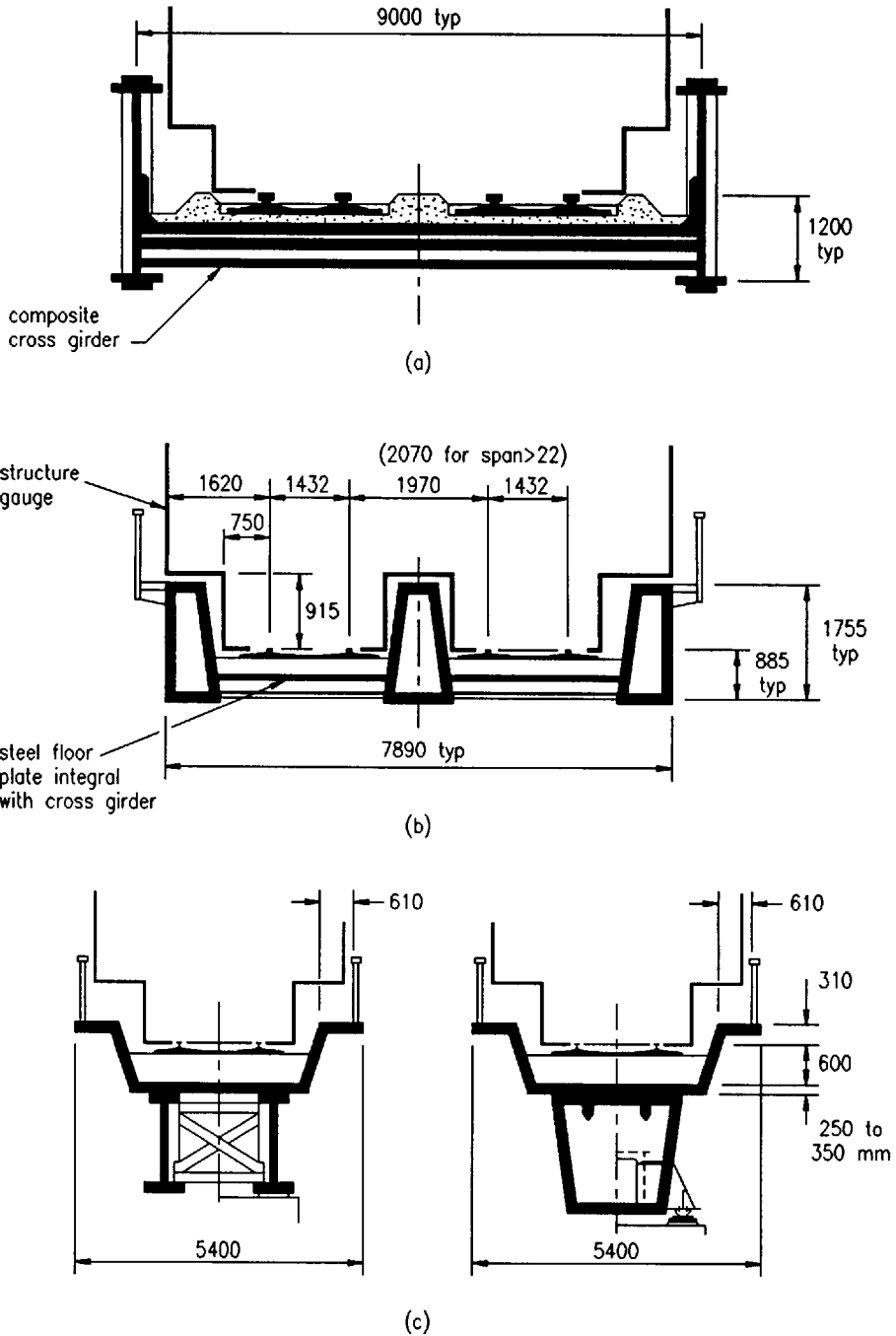


Fig. 4.11 Railway bridges. (a) Half-through plate girders; (b) half-through box girders; (c) composite deck type (spans > 30 m)

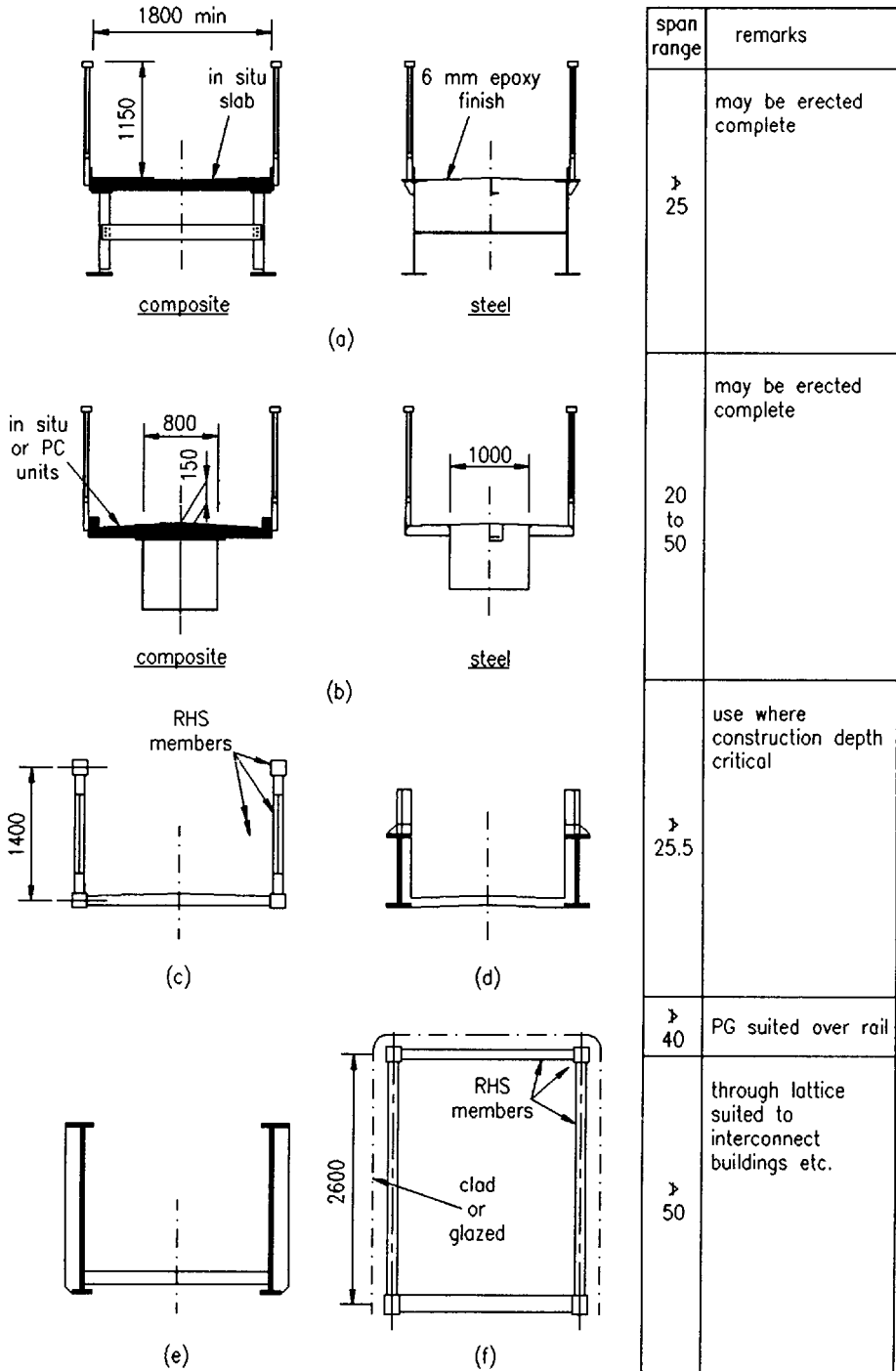


Fig. 4.12 Pedestrian bridges. (a) Twin universal beam; (b) box; (c) Vierendeel or Warren girder; (d) half-through universal beam; (e) half-through plate girder; (f) through lattice

because the entire cross section including parapets may be fabricated and erected in one unit. For this reason multiple spans tend to be simply supported and not continuous. Staircase and sloping or stepped ramp spans are also erected as complete units and columns are often of steel.

Half-through cross sections are often used because the shallow construction depth is able to provide the shortest lengths of staircase or ramp approaches in urban areas. Either half-through rolled beams, Warren truss or Vierendeel girders are used with rolled hollow (square or rectangular) members. Floors are steel stiffened plate often surfaced with a factory-applied epoxy non-slip surfacing approximately 5 mm thick. Rigid connections between floor and girders provide for U-frame stability. Staircase approaches may be either steel stringers supporting steel plate treads or a central spine box with cantilever treads of steel or precast concrete. Ramps may be similarly formed, but where the span exceeds about 10 m then half-through construction tends to be used. Spiral approach ramps are popular, formed in steel using twin rolled sections curved in plan supporting a composite or steel plate floor. Where adequate construction depth is available, for example, when a pedestrian bridge is required across a motorway or railway cutting, then deck cross sections are appropriate with a composite or steel plate floor. Precast concrete floor units are also suitable. Primary members may be a single box girder, twin plate girders or twin rolled beams. A single box girder provides a structure of neat appearance.

#### **4.4 Codes of Practice**

At present BS 5400<sup>5</sup> is used in the UK for the design of all bridges. Part 3 deals with the design of steel bridges and if composite construction is used then Part 5 must also be referred to. The Department of Transport has particular requirements in the form of Technical Memoranda which implement and sometimes vary the clauses in BS 5400. Eurocode 3 (EC3) for the design of steel structures is in preparation. Other Eurocodes relevant to composite bridges will be EC2 and EC4. Although the Eurocodes will refer mainly to the design of buildings their extension to the design of bridges is a further objective.

Eurocode 3 will contain basic rules which, although intended primarily for buildings, can also be used for the design of steel bridges. Though the rules for bridges need further amplification, the existing draft design rules are already applicable to some bridge structures such as simply-supported steel and composite spans, simple trusses and for connections. Rules for plate girders exceeding 1.5 m depth, longitudinally stiffened girders, box girders, orthotropic steel floors, U-frames, restraints at supports and serviceability limit state checks are not yet available.

Both BS 5400 and the Eurocodes are based on the limit state design concept, which means that the verification is carried out for serviceability and ultimate limit states. The Eurocode on actions deals with general rules for the determination



**Table 4.6** Eurocode 1: Actions on Structures

| List of contents  | Structure of the chapters   |
|---|---|
| <p><i>Chapter</i></p> <p>1 <i>General rules</i></p> <p>2 <i>Density of materials</i></p> <p>3 <i>Self-weight</i></p> <p>4 <i>Soil and water pressure</i></p> <p>5 <i>Imposed deformations</i></p> <p>6 <i>Imposed loads on floors and roofs</i></p> <p>7 <i>Snow and ice</i></p> <p>8 <i>Wind loads</i> →</p> <p>9 <i>Water and wave loads</i></p> <p>10 <i>Thermal actions</i></p> <p>11 <i>Silo and tank loads</i></p> <p>12 <i>Road bridges</i></p> <p>13 <i>Railway bridges</i></p> <p>14 <i>Crane actions</i></p> <p>15 <i>Actions from machinery</i></p> <p>16 <i>Construction loads</i></p> <p>17 <i>Impact</i></p> <p>18 <i>Explosion</i></p> <p>19 <i>Seismic action</i></p> | <p style="text-align: center;">example wind loads</p> <div style="border: 1px solid black; padding: 5px; margin: 5px auto; width: fit-content;"> <p style="text-align: center;">basic part<br/>rigid structures, flexible structures</p> </div> <p style="text-align: center;">+</p> <div style="border: 1px solid black; padding: 5px; margin: 5px auto; width: fit-content;"> <p style="text-align: center;">specific rules for</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid black; padding: 2px 5px; margin: 2px;">buildings</div> <div style="border: 1px solid black; padding: 2px 5px; margin: 2px;">bridges</div> <div style="border: 1px solid black; padding: 2px 5px; margin: 2px;">towers</div> <div style="margin: 2px;">etc.</div> </div> </div> |

of the design loads and the load combinations and gives information on the characteristic values of the loads (see Table 4.6).

The first steps for the preparation of the rules for the traffic loads for bridges, particularly for road bridges, have been undertaken. For the traffic loads on railway bridges the harmonized uniform load model UIC 71<sup>6</sup> has been previously adopted by the different national railway authorities.

## 4.5 Traffic loading

### 4.5.1 Highway bridges

Highway bridges in the UK are currently designed for HA loading (a uniformly distributed loading plus knife edge load) together with HB (abnormal vehicle) loading for structures carrying main highways. For design to Eurocodes it is intended to adopt a unified loading model.

Although great differences in the national regulations for loads, resistances and safety factors exist, these differences appear to compensate one another and the resulting designs in all countries are generally similar.

### 4.5.2 Railway bridges

The uniform load model UIC 71<sup>6</sup> used by the European national railway authorities is shown in Fig. 4.13; it is also used in BS 5400: Part 2. Where specified this

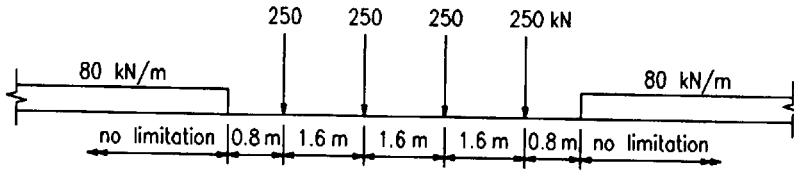


Fig. 4.13 UIC and BS 5400 load model (excluding impact)

loading is multiplied by a factor for bridges on lines carrying heavier or lighter traffic.

Dynamic factors are applied as shown in Table 4.7. Dimension  $L$  is the length (m) of the influence line for deflection of the element under consideration.

**Table 4.7** Dynamic factors for railway loading

| Dimension $L$<br>(m) | Dynamic factor                       |                                      |
|----------------------|--------------------------------------|--------------------------------------|
|                      | Bending moment                       | Shear                                |
| $\leq 3.6$           | 2.00                                 | 1.67                                 |
| $> 3.6$ to 67        | $0.73 + \frac{2.16}{\sqrt{L} - 0.2}$ | $0.82 + \frac{1.44}{\sqrt{L} - 0.2}$ |
| $> 67$               | 1.00                                 | 1.00                                 |

Other loads arising from railway traffic are:

- centrifugal forces on curved track
- nosing – 100 kN force acting transversely at rail level
- traction and braking
- derailed vehicles (for overturning consider 80 kN/m over 20 m lengths acting on the edge of the structure).

Fatigue is important for the design of railway bridges because a higher proportion of regular traffic attains the maximum loading compared with highway bridges and the vehicles are constrained to run in the same lateral paths. Typically it is necessary to reduce the working stresses of grade 50 steel for main girders of spans less than about 24 m so that grade 43 or even lower stresses are used. For floor members including cross girders, trimmers, rail bearers and floor plating it is nearly always necessary to use reduced working stresses in a similar manner.

#### 4.6 Other actions

Actions other than traffic loading which may need to be considered in one or more combinations are shown in Table 4.8.

**Table 4.8** Summary of actions other than those due to traffic loading

| Action                               | Comments   |
|--------------------------------------|--|
| Dead loads <sup>a</sup>              | Weight of the structure  |
| Superimposed dead loads <sup>a</sup> | Finishes and surfacings<br>Services  |
| Wind                                 | Transverse, longitudinal and vertical<br>Consider in presence of live load or otherwise                                  |
| Temperature                          | Restraint and movement (e.g. flexure of columns)<br>Frictional restraint of bearings<br>Effect of temperature difference |
| Differential settlement              | Foundation movements   |
| Earth pressure                       | Vertical and horizontal pressures from retained material   |
| Erection effects <sup>a</sup>        | Strength during construction, e.g. stability of steelwork before composite floor slab cast                               |
| Snow load                            | May be relevant to moving bridges  |
| Seismic                              | As may be specified by the national authority  |
| Water flow                           | Flow against bridge supports   |

<sup>a</sup> These actions must be considered during initial design. For most bridge decks actions other than those from vertical traffic loading, dead and superimposed dead loads are unlikely to have a fundamental effect.

## 4.7 Steel grades

Steels to BS EN 10025 grade 50 are usual for bridges as they offer a lower cost-to-strength ratio than grade 43. All parts subject to tensile stress are required to achieve a specified notch toughness, depending upon design minimum temperature, stress level and material thickness.

Special consideration may be needed if tensile stresses occur only during erection, for example, arising from lateral bending in girders due to wind loading, or during lifting of components. Judgement is necessary but it is often accepted that modest values of tensile stress can be permitted in such cases without the need for specific notch toughness provided that the work is not carried out during very low temperatures. In all other cases appropriate grades having specified notch toughness are necessary.

### *Weather-resistant steel*

To eliminate the need for painting, weather-resistant (WR) grades in BS 4360 should be considered. Although it can be shown that the commuted costs of repainting are less than 1% of the initial bridge cost, weather-resistant steel is

particularly useful in eliminating maintenance where access is difficult – over a railway for example. Weather-resistant steel is not suitable at or near the coast (i.e. within about one mile of the sea). The Department of Transport requires sacrificial thickness to be added to all exposed surfaces for possible long-term corrosion of 2 mm per face in a severe industrial environment, 1 mm otherwise.

## 4.8 Overall stability and articulation

It is important to consider overall stability of the bridge and its articulation under temperature effects (see Fig. 4.14). For simply-supported bridges each span must transfer longitudinal and transverse loads to the foundations while being able to accommodate movement with suitable bearings and expansion joints. For continuous spans the deck must be pinned at one support with free bearings elsewhere. Normally only one bearing within the deck width should be pinned longitudinally so that each girder is free to articulate under traffic loading independently, unless the pier consists of a separate column beneath each bearing which gives flexibility. A number of choices are open to the designer but the system used will affect the design of bearings, bearing stiffeners, expansion joints and the foundations.

*For temperature movements:*

Movement range:  $(12 \times 10^{-6} \text{ per } ^\circ\text{C}) \times \text{temperature range} \times \text{length from pinned bearing}$ .

For typical conditions in Europe, for steel or composite decks, ultimate movement =  $\pm 4.5 \text{ mm per } 10 \text{ m of length from mean temperature}$ .

## 4.9 Initial design

### 4.9.1 Suspension bridges

For initial design Fig. 4.15 gives approximate formulae<sup>7</sup> for making first estimates of cable size and bending of the stiffening girders. The most severe condition for the stiffening girder is with approximately one half of the main span loaded asymmetrically.

### 4.9.2 Cable-stayed bridges

Cable-stayed bridges virtually behave as continuous beams with elastic supports at the cable anchorage points. Cable lengths are adjusted during construction so that the effect of cable extension under dead load conditions is cancelled out. Provided that high tensile material is used for the cables then non-linear effects

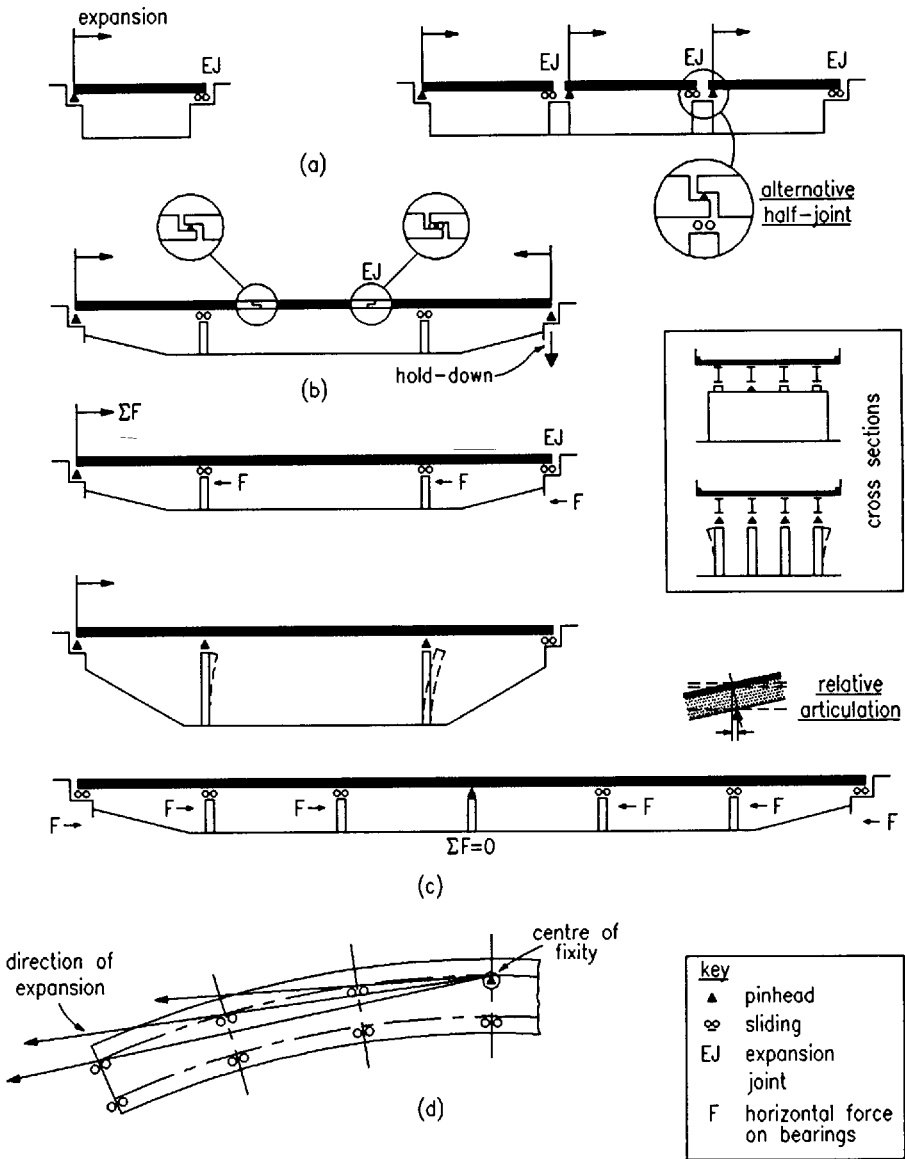


Fig. 4.14 Overall stability and articulation. (a) Simply supported, (b) cantilever and suspended span, (c) continuous, (d) curved viaducts

due to self-weight can be shown to be negligible.<sup>8</sup> For initial design the deck may be proportioned as a continuous beam, as shown in Fig. 4.16, to which are added:

- (a) deck deflections at the cable positions due to extension,
- (b) axial forces due to horizontal component of the cable forces.

$$\ell = L \left( 1 + \frac{8}{3} \left( \frac{d}{L} \right)^2 \right)$$

$$H = \frac{wL^2}{8d}$$

$$T = H \left( 1 + \frac{64 d^2 x^2}{L^4} \right)^{1/2}$$

$$\Delta \ell = \frac{H \ell}{AE} \left( 1 + \frac{16}{3} \frac{d^2}{L^2} \right)$$

$$\Delta d = \frac{\Delta \ell}{\frac{16 d}{15 L} \left( 5 - \frac{24 d^2}{L^2} \right)}$$

$$\Delta d = \frac{\Delta L \left( 15 - 40 \frac{d^2}{L^2} + 288 \frac{d^4}{L^4} \right)}{16 \frac{d}{L} \left( 5 - 24 \frac{d^2}{L^2} \right)}$$

$$M_{\max.} = 0.161 pL^2 \left( \frac{4}{\alpha} \frac{EId}{wL^4} \right)^{1/2}$$

where  $\alpha$  is the equivalent modulus of foundation, approximately 1100 kN/m<sup>2</sup>

$$M_{\max.} \text{ occurs when } \frac{2a}{L} = \frac{\pi}{4} \left( \frac{4}{\alpha} \frac{EId}{wL^4} \right)^{1/4}$$

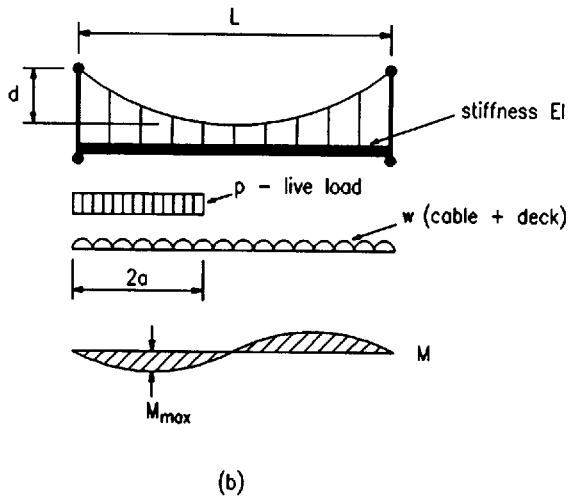
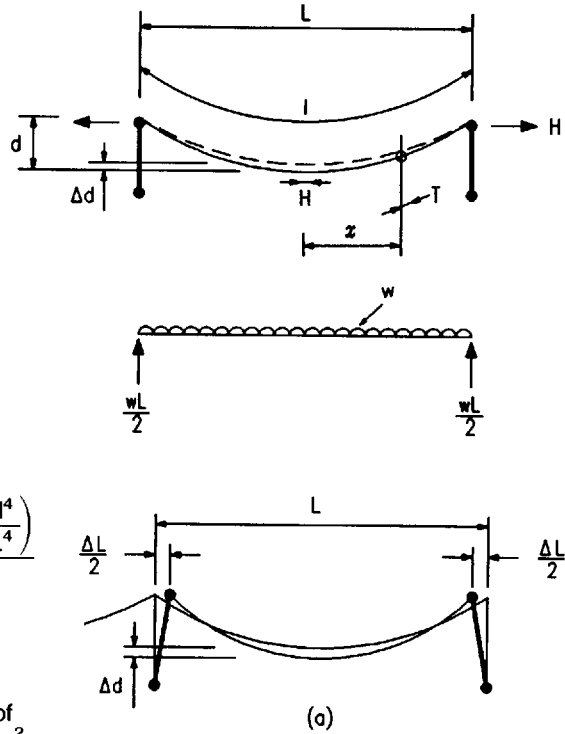


Fig. 4.15 Suspension bridges, approximate formulae (Pugsley). (a) Neglecting stiffness of deck; (b) including deck stiffness

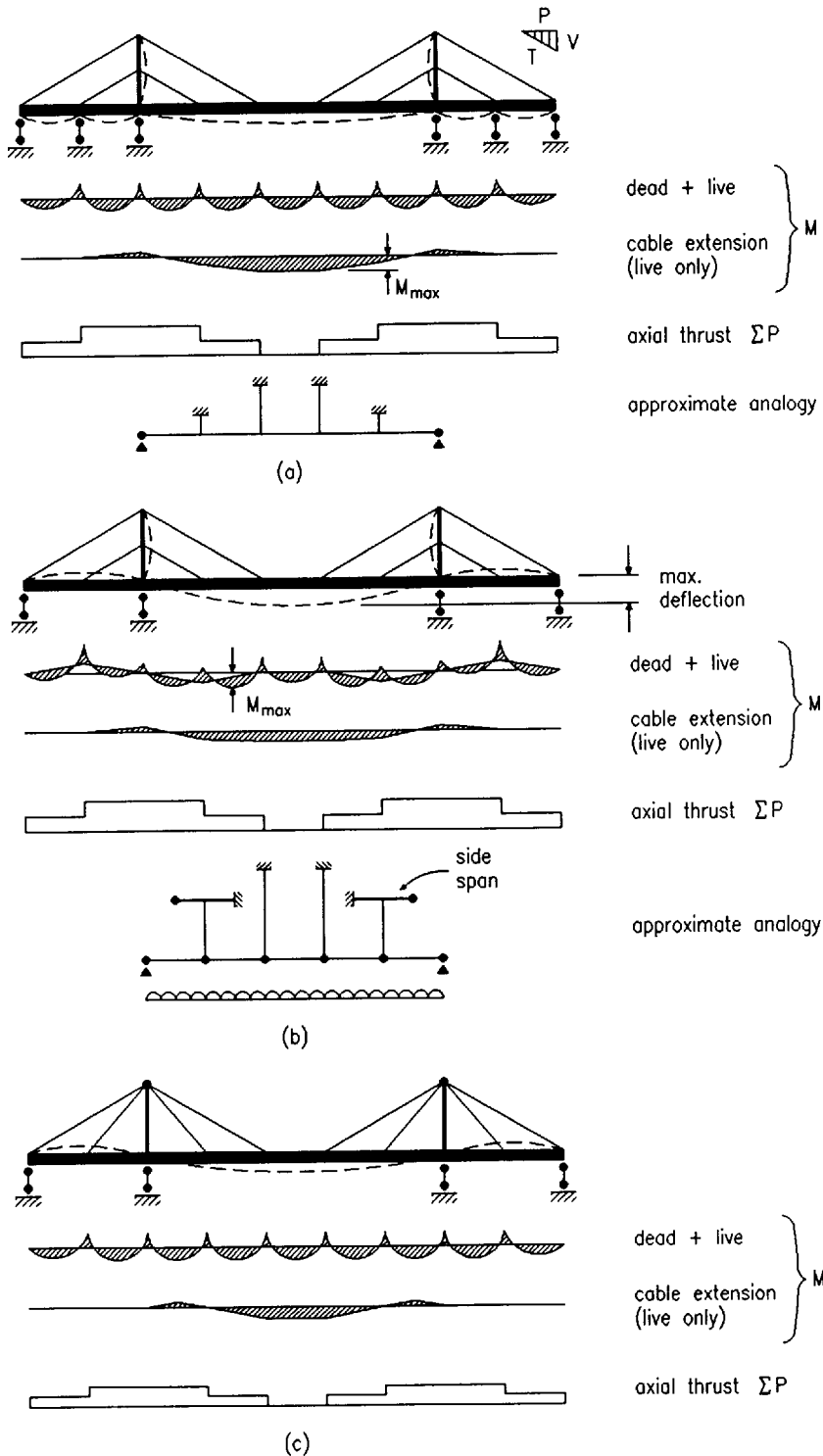


Fig. 4.16 Cable-stayed bridges, initial analysis. (a) Anchored side spans (harp shown); (b) harp; (c) fan

Where a single plane of cables is used then an initial design check must be made to ensure that sufficient torsional rigidity is provided (using single or twin box girders) to control transverse tilt of the deck at mid-span when traffic loading occupies one carriageway.

### **4.9.3 Highway bridges – composite deck construction**

#### **4.9.3.1 General**

Bridges with composite deck construction (Fig. 4.17) represent a high proportion of the total number of steel bridges built in Europe since 1960. Generally a floor slab 220 mm to 250 mm thick is used composite with rolled sections or plate girders at spacings up to 3.5 m and depth between (span/20) and (span/30). For spans exceeding 40 m where adequate construction depth is available then twin girders can offer advantages with typical depth (span/18) to (span/25), and the floor slab is either haunched over the girders or supported by subsidiary stringers or cross girders. The slab thickness is determined by its requirement to resist local bending and punching shear effects from heavy wheel loads and needs to be reinforced in both directions; elastic design charts by Pucher are suitable.<sup>9</sup> In the hogging regions of continuous spans the slab will crack and be ineffective in overall flexure unless it is prestressed. The longitudinal reinforcement may however be assumed to act as part of the composite section. Most composite bridges are designed as 'unpropped' i.e. the erected steelwork supports its own weight and the concrete slab (including formwork allowance) until hardened with composite action only being assumed for superimposed dead and live loads. Box girders tend to be used for the longer spans especially those exceeding 100 m. Popular forms include twin box girders, multiple compact boxes or open top trapezoidal boxes.

Plate girder flanges should be made as wide as possible, consistent with outstand limitations, to give the best achievable stability during erection and to reduce the number of intermediate bracings. For practical reasons a desirable minimum width is about 400 mm. A maximum flange thickness of 65 mm is recommended to avoid heavy welds.

#### **4.9.3.2 Intermediate supports**

Intermediate supports often take the form of reinforced concrete walls, columns or portals. Steel supports may alternatively be used and tubular columns are efficient, especially if filled with concrete and designed compositely. Where fewer columns are required for multiple girders then integral steel crossheads at the supports are sometimes used.



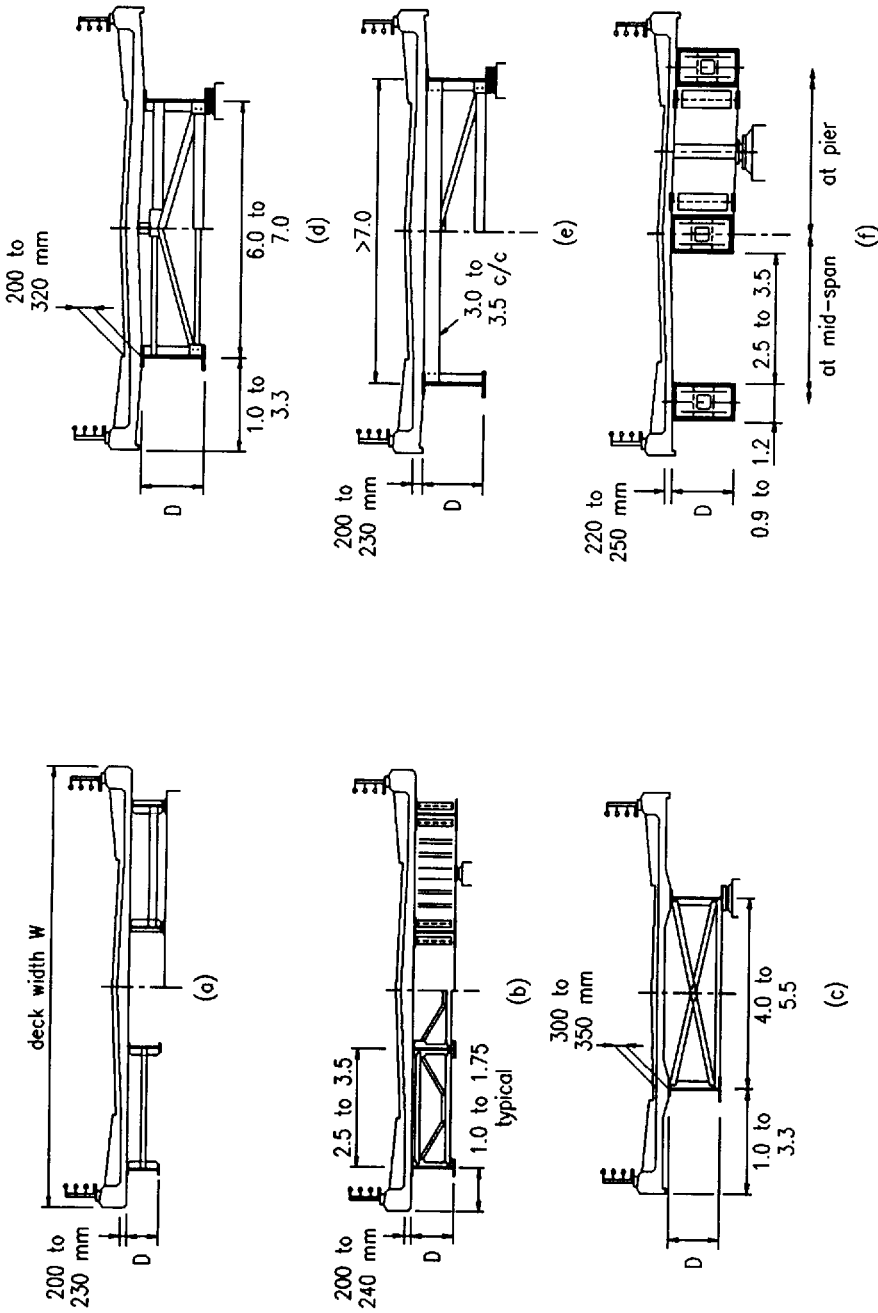


Fig. 4.17 Highway bridges – composite deck construction. (a) Multiple universal beam ( $N = 4$ ); (b) multiple plate girder ( $N = 4$ ); (c) twin plate girder, haunched slab ( $N = 2$ ); (d) twin plate girder and stringer ( $N = 2$ ); (e) twin plate girder and cross girder ( $N = 2$ ); (f) multiple box ( $N = 6$ )

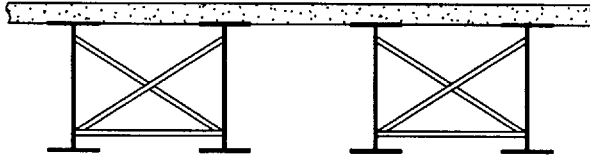


Fig. 4.18 Lateral bracing of bridge girders

#### 4.9.3.3 *Bracings*

For rolled beam or plate girder bridges, lateral bracings are necessary for stability during erection and concreting of the slab. The bracings are required at all supports and within the hogging regions of continuous spans. If required by the designer they may be assumed to contribute to the transverse rigidity of the deck when carrying out an analysis of the transverse distribution of concentrated live loads. At the abutments the bracing can be a rolled section trimmer composite with the slab and supporting its free end. Over intermediate supports a channel section can be used between each pair of girders up to about 1.2 m depth. For deeper girders triangulated bracings are necessary.

Intermediate bracings in hogging regions are typically spaced at about  $12 \times$  (bottom flange width). Where bracing is provided across the full width of the bridge, i.e. between all girders, it increases transverse stiffness significantly. Because of this stiffness, such bracing will attract high stresses under loading that varies across the width of the bridge. The effect of this behaviour on the fatigue life of the bracing needs to be considered. Alternatively bracing should only be provided between neighbouring pairs of girders. This reduces the transverse stiffness considerably and alleviates the problem of fatigue. Such a structure is also likely to be easier to erect (Fig. 4.18). If the bridge is curved in plan with girders fabricated in straight chords they should be located adjacent to the site splices where torsion is induced. Bracings may be of a triangulated form or of single channel sections between each pair of girders where up to 1.2 m depth. Bracings are usually bolted to vertical web stiffeners in the main girders which may need to be increased in size to accommodate the bolted connections. Angle sections are commonly used with lapped single shear connections which permit tolerance in accommodating camber difference between adjacent girders.

Plan bracing systems may be required for spans exceeding 55 m for temporary stability; they may be removed after the floor slab is cast.

#### 4.9.3.4 *Locations of splices and change of section*

Where rolled beams up to 1.0 m deep are used then for the maximum span range of about 33 m it is convenient to use a constant section with one splice within each span located at about  $0.1$  to  $0.2 \times$  span from the internal supports. The beam size

$$L \text{ (m)} = \frac{r \times 10^3}{7.85 (t_1 - t_2)} \quad \text{where } r = \frac{\text{cost/m weld}}{\text{cost/tonne of steel}}$$

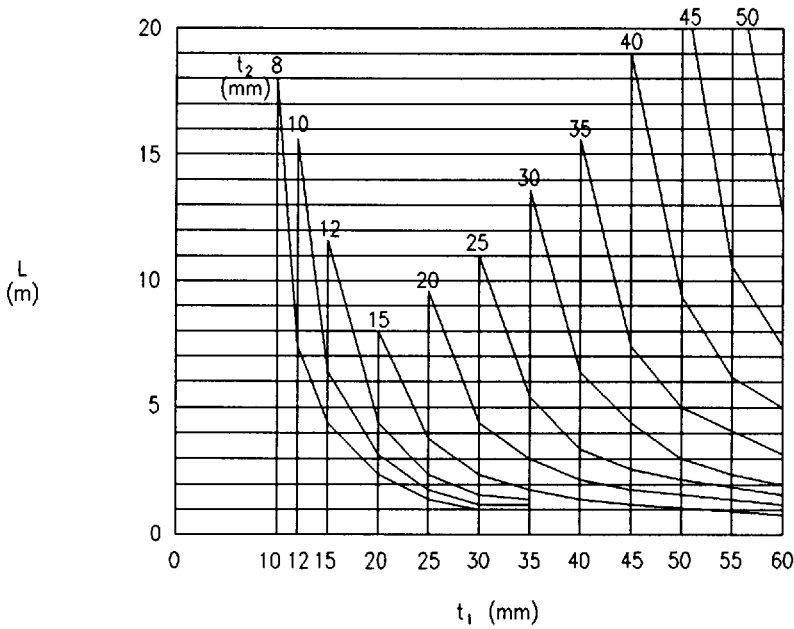
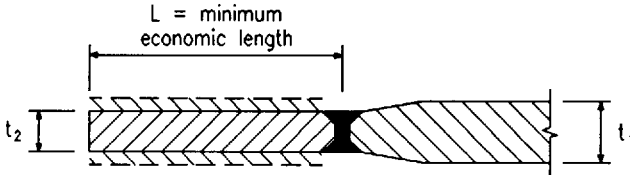


Fig. 4.19 Economy of flange and web thickness changes. The figure gives an indication of the minimum length ( $L$ ) for which a selected thickness change will be economic for flanges and webs of girders. Below this length it will be more economic to continue the thicker plate ( $t_1$ )

will be determined by the maximum bending and shear effects at the supports where the slab is cracked.

For plate or box girders the component lengths for shop fabrication should be the maximum possible consistent with delivery and site restrictions to reduce the amount of site assembly. For spans up to about 55 m two splices per span are

generally suitable, located at  $0.15$  to  $0.25 \times$  span from the internal supports, at which changes of flanges and web thickness should be made. A minimum number of other flange or web workshop joints should be made, consistent with plate length availability. The decision whether to introduce thickness changes within a fabricated length should take account of the cost of butt welds compared with the potential for material saving. Figure 4.19 indicates a basis for considering this optimization.

#### **4.9.3.5 Curved bridge decks**

Bridges which are curved in plan may be formed using straight fabricated girders, with direction changes introduced at each site splice. Alternatively the steel girders can also be truly curved in plan in which case the secondary stresses which arise from torsion must be evaluated. It is likely that additional transverse bracings will be needed to reduce these stresses.

#### **4.9.3.6 Initial sizes – composite plate girders**

For economic design an analysis should be carried out of the transverse distribution of concentrated live loads between the main girders of the cross section. The floor slab together with any continuous transverse bracing will significantly redistribute the maximum load applied to the most severely loaded girders. Prior to this the designer will wish to select initial sizes and make an estimate of the total weight of structural steel. Figures 4.20–4.24<sup>10</sup> provide initial estimates of flange area, web thickness and overall unit weight of steelwork ( $\text{kg/m}^2$ ) for typical composite bridge cross sections as shown in Fig. 4.17.

The figures were derived from approximate designs using simplifying assumptions for loads and transverse distribution and to achieve correlation with actual UK bridges.

The sizes indicated do not represent final design, which must be checked by a form of distribution analysis using the actual specified loads. A two-dimensional grid analysis is usually employed with any out-of-plane effects being ignored. Comparison with three-dimensional analyses has shown that out-of-plane effects are generally negligible for most composite bridge decks. The following assumptions apply to use of Figs 4.20–4.24.

Deck slab 230 mm average thickness ( $5.75 \text{ kN/m}^2$ ).

Superimposed dead loads equivalent to 100 mm of finishes ( $2.40 \text{ kN/m}^2$ ).

Formwork weight  $0.50 \text{ kN/m}^2$  of slab soffit area.

Steel grade 50 (yield strength  $355 \text{ N/mm}^2$ ).

Span-to-girder-depth ratios of 20 and 30.

Webs have vertical stiffeners at approximately 2.0 m centres where such stiffening is required.

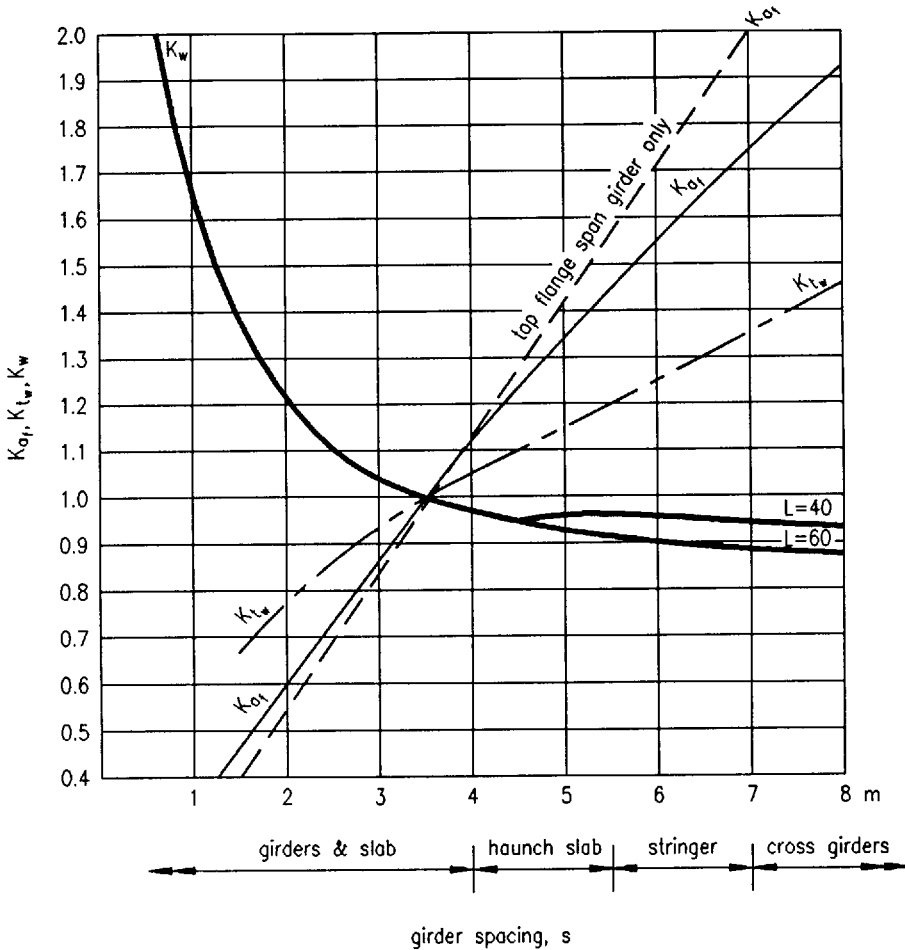


Fig. 4.20 Girder spacing factors

Elastic stress analysis is used for plate girders. If however the plastic modulus is used for compact cross sections, then economies are possible.

Steelwork is unpropped during casting of the floor slab.

Sufficient transverse bracings are used such that stresses are not significantly reduced due to buckling criteria.

Top flanges in sagging regions are dictated by a maximum stress during concreting allowing for formwork and concreting effects.

Live loading is approximately equivalent to United Kingdom 45HB or HA as indicated.

Continuous spans are approximately equal in length.

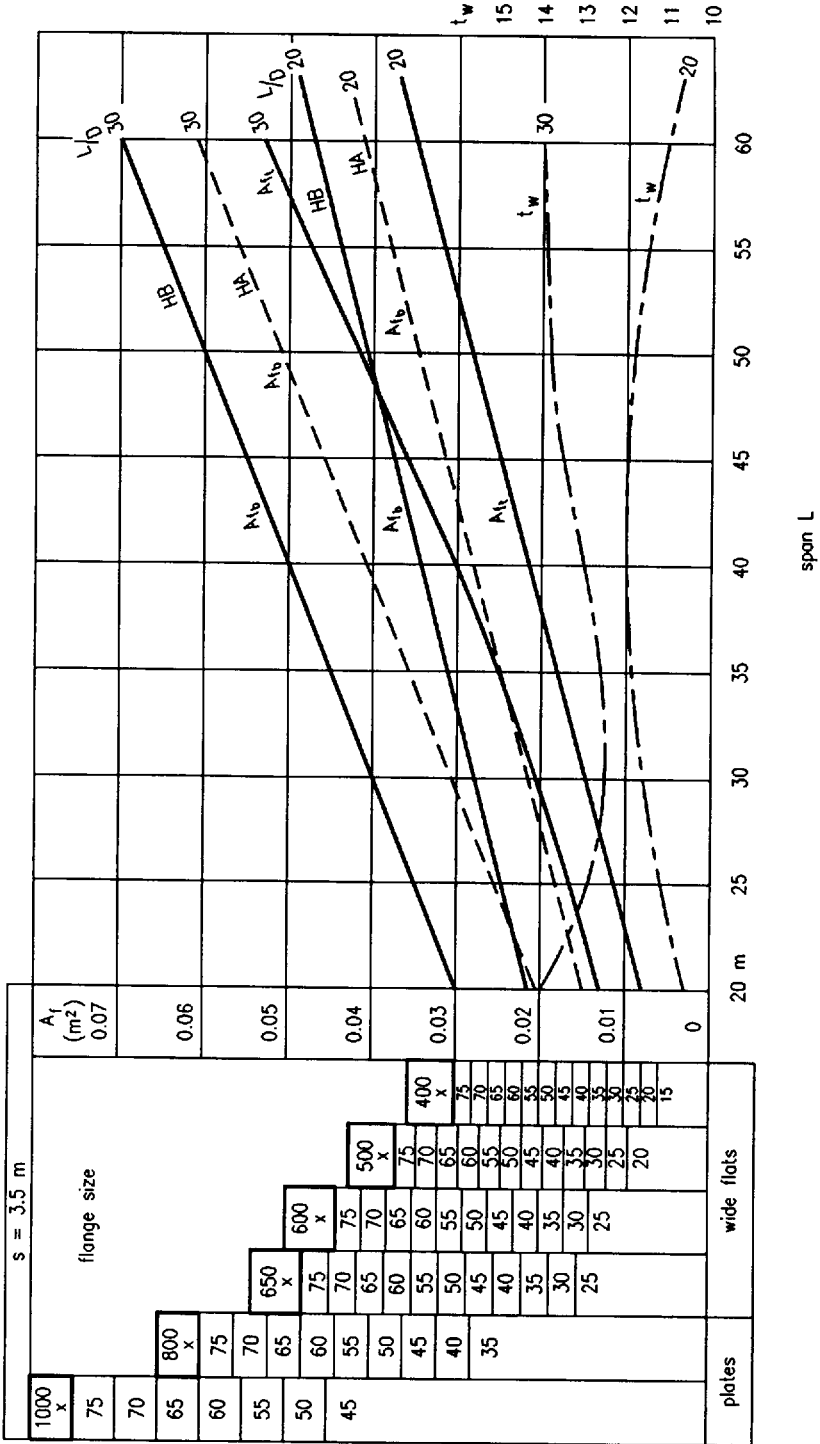


Fig. 4.2/ Flange and web sizes – simply-supported bridges

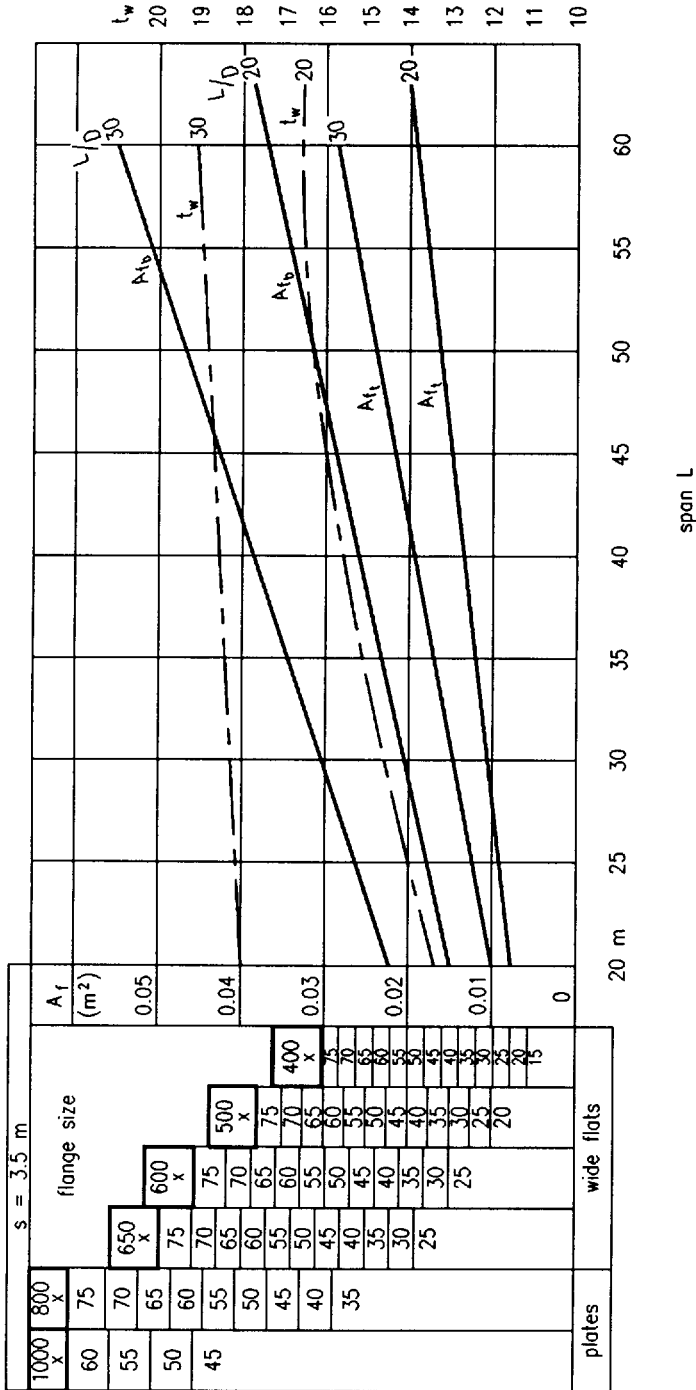


Fig. 4.22 Flange and web sizes – continuous bridges, pier girders

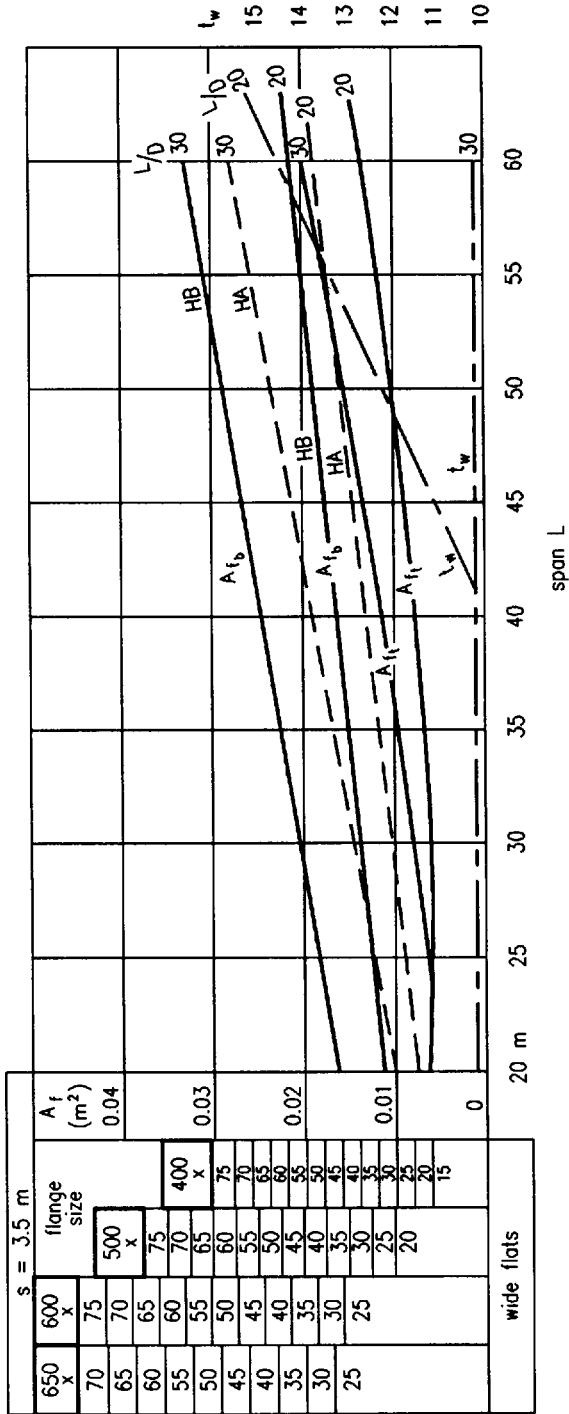


Fig. 4.23 Flange and web sizes – continuous bridges span girders



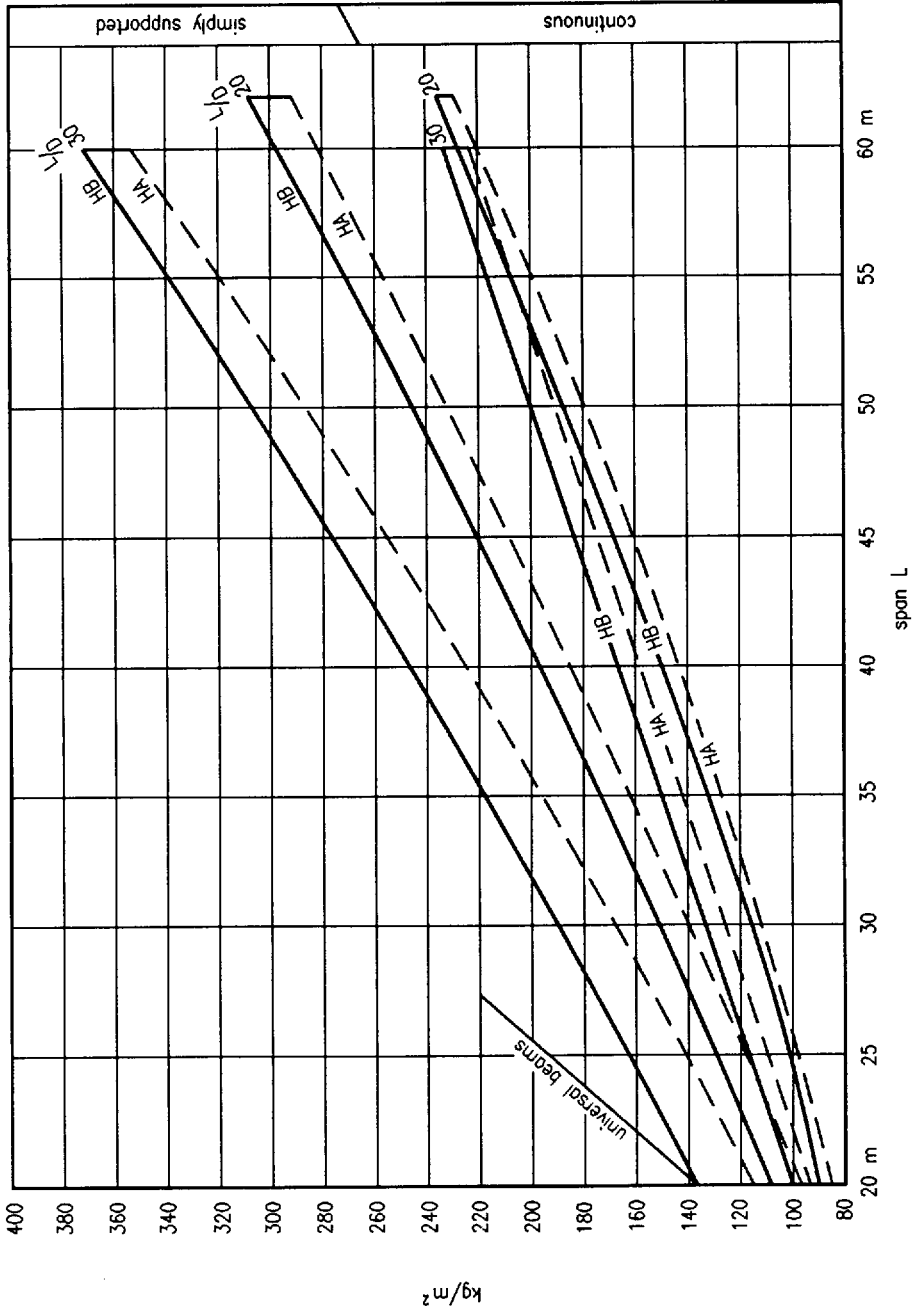


Fig. 4.24 Overall unit weights – plate girder bridges

*Flange sizes*

Figures 4.21–4.23 are applicable to an average girder spacing  $s$  of 3.5 m. Figure 4.20 gives a girder spacing factor  $K_a$ , which is multiplied by the flange areas, obtained above, to give values appropriate to the actual spacing,

$$\text{e.g. top flange area, } A_f = A_f \quad \times K_a$$

(Figs 4.21–4.23)      (Fig. 4.20)

The figures also show actual flange sizes, ranging from  $400 \times 15$  mm to  $1000 \times 75$  mm. The flange area of pier girders of continuous unequal spans may be approximately estimated by assuming the greater of the two adjacent spans. End spans of continuous bridges may be estimated using  $L = 1.25 \times$  actual span.

*Web thickness*

Web thicknesses are obtained using Figs 4.21–4.23 applicable to  $s = 3.5$  m. Adjustment for the actual girder spacing  $s$  is obtainable from Fig. 4.20,

$$\text{i.e. web thickness, } t_w = t_w \quad \times K_{t_w}$$

(Figs 4.21–4.23)      (Fig. 4.20)

The thickness obtained may be regarded as typical. However, designers may prefer to opt for thicker webs to reduce the number of web stiffeners. Consideration should also be given to the use of unstiffened webs of appropriate thickness, i.e.  $d/t \leq 60$ – $100$  depending on shear.

*Overall unit weight*

Overall unit weight ( $\text{kg/m}^2$  of gross deck area) is read against the span  $L$  from Fig. 4.24 for simply-supported or continuous bridges with  $L/D$  ratios of 20 or 30, under HB or alternatively HA loading and applicable to  $s = 3.5$  m.

Adjustment for average girder spacing  $s$  other than 3.5 m is obtainable from Fig. 4.20,

$$\text{i.e. } \text{kg/m}^2 = \text{kg/m}^2 \quad \times K_w$$

(Fig. 4.24)      (Fig. 4.20)

The unit weight provides an approximate first estimate of steelwork weight allowing for all stiffeners, bracings, shear connectors, etc.

For continuous bridges with variable depth, Figs 4.21 and 4.23 may be used to provide a rough guide, assuming a span-to-depth ratio ( $L/D$ ) for each span based upon the average girder depth.

For box-girder bridges a rough estimate may be obtained by replacing each box girder with an equivalent pair of plate girders.

The mean span for use in Fig. 4.24 should be determined as follows:

$$\text{mean span, } L = \sqrt[4]{\left(\frac{L_1^4 + L_2^4 + \dots + L_n^4}{n}\right)}$$

where  $n$  is the number of spans.

#### 4.9.3.7 Initial sizes – rolled section beams

An estimate of size for simply-supported spans only may be obtained from Figs 4.25 and 4.26<sup>10</sup> for elastic or plastic stress analysis respectively, using universal beams up to 914 × 419 × 388 kg/m size. For an estimate of the total weight of structural steel a factor of 1.1 applied to the main beams provides a reasonable allowance for bracings, bearing stiffeners and shear connectors. Figures 4.25 and 4.26 are based upon a concrete strength of 37.5 N/mm<sup>2</sup>, and show the required mass per metre of universal beam. Table 4.9 gives reference to the relevant serial size.

**Table 4.9** Universal beam sizes

| Reference<br>Figs 4.25 & 4.26 | Universal beam size |                        | Actual<br>depth<br>(mm) |
|-------------------------------|---------------------|------------------------|-------------------------|
|                               | Serial size         | Mass per metre<br>(kg) |                         |
| 388                           | 914 × 419           | 388                    | 920.5                   |
| 343                           |                     | 343                    | 911.4                   |
| 289                           | 914 × 305           | 289                    | 926.6                   |
| 253                           |                     | 253                    | 918.5                   |
| 224                           |                     | 224                    | 910.3                   |
| 201                           |                     | 201                    | 903.0                   |
| 226                           |                     | 226                    | 850.9                   |
| 194                           | 838 × 292           | 194                    | 840.7                   |
| 176                           |                     | 176                    | 834.9                   |
| 197                           |                     | 197                    | 769.6                   |
| 173                           | 762 × 267           | 173                    | 762.0                   |
| 147                           |                     | 147                    | 753.9                   |
| 170                           |                     | 170                    | 692.9                   |
| 152                           | 686 × 254           | 152                    | 687.6                   |
| 140                           |                     | 140                    | 683.5                   |
| 125                           |                     | 125                    | 677.9                   |
| 238                           |                     | 238                    | 633.0                   |
| 179                           | 610 × 305           | 179                    | 617.5                   |
| 149                           |                     | 149                    | 609.6                   |
| 140                           |                     | 140                    | 617.0                   |
| 125                           | 610 × 229           | 125                    | 611.9                   |
| 113                           |                     | 113                    | 607.3                   |
| 101                           |                     | 101                    | 602.2                   |
|                               |                     |                        |                         |

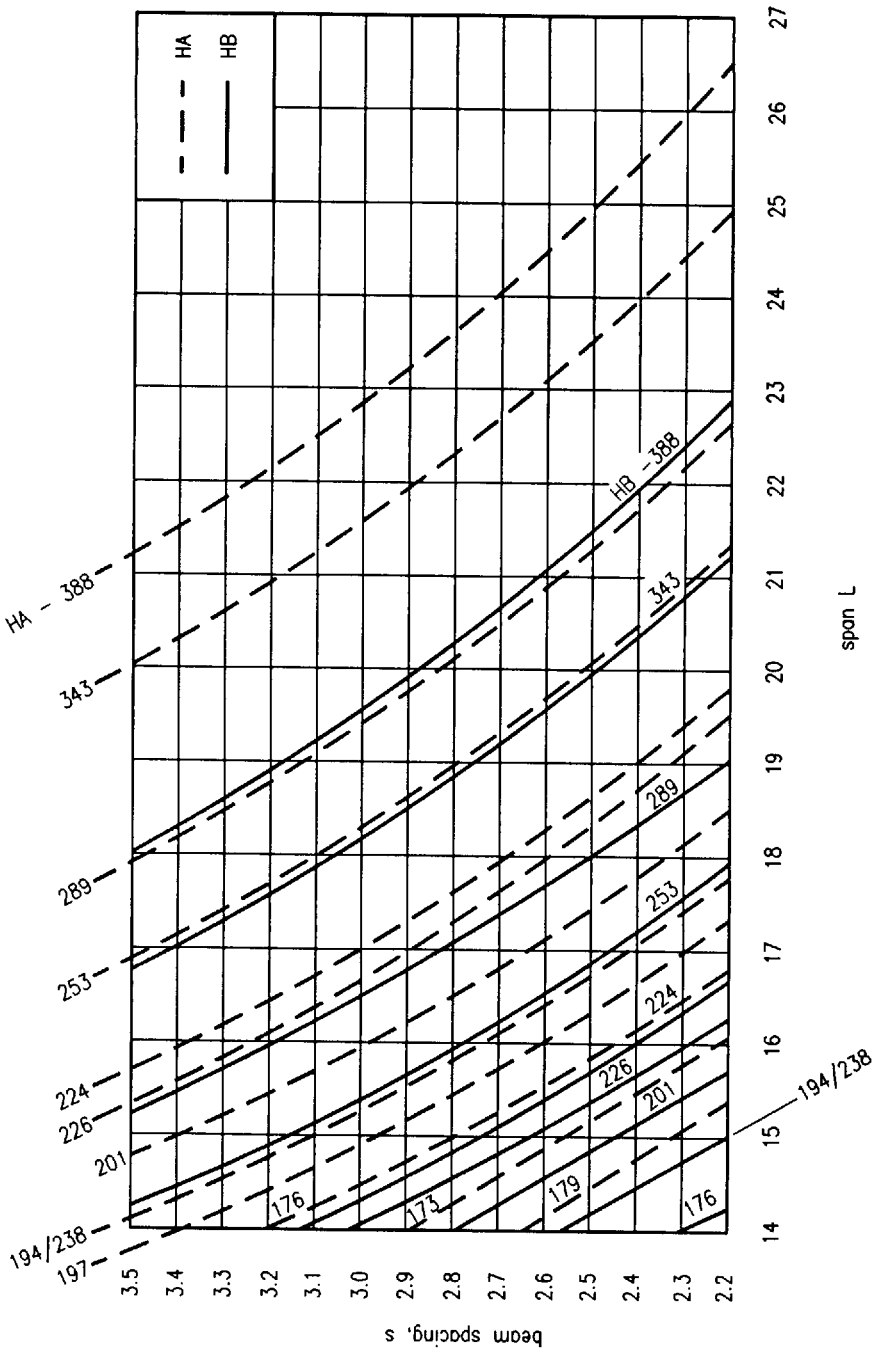


Fig. 4.25 Universal beam sizes – simply-supported bridges – elastic design

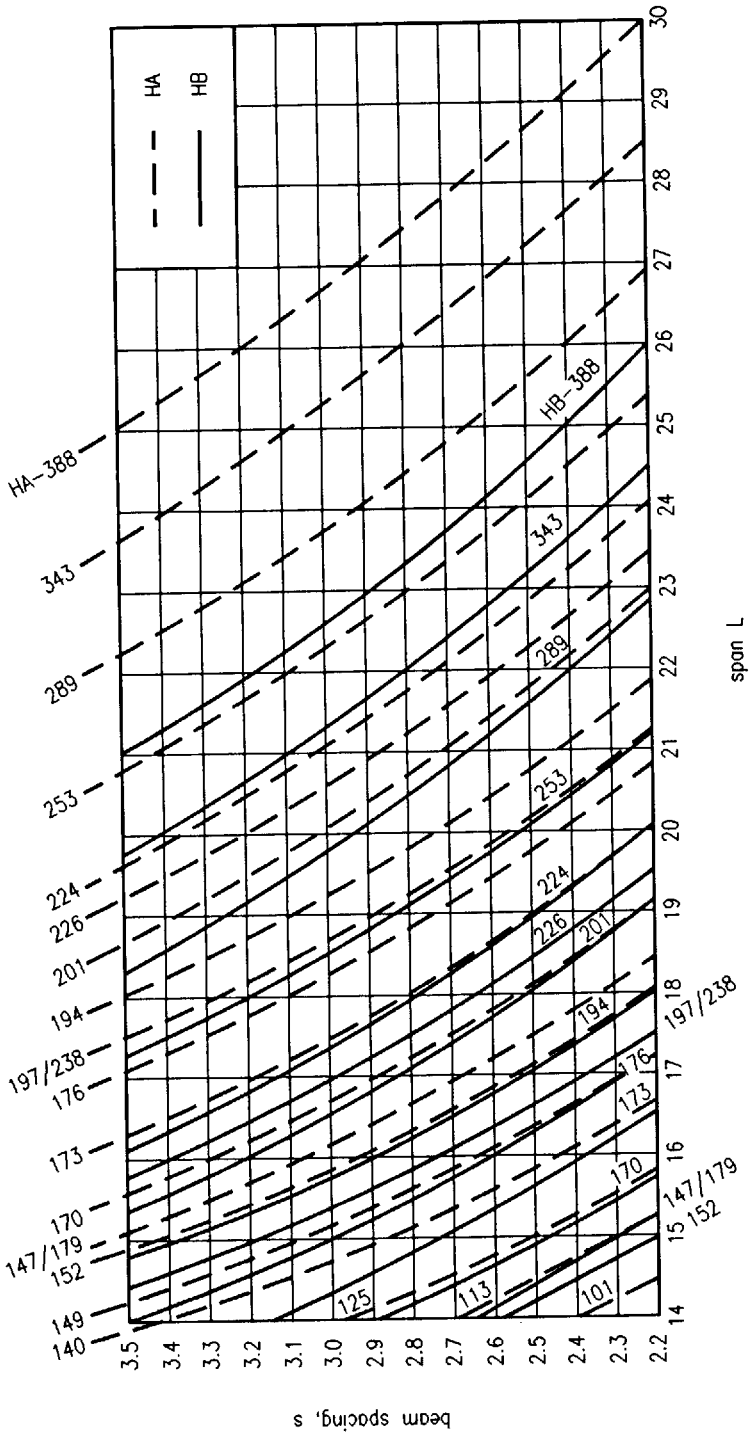


Fig. 4.26 Universal beam sizes – simply-supported bridges – plastic design


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3. Hayward A.C.G. (1987) Composite pedestrian and cycle bridge at Welham Green. *Steel Construction Today*, 1, No. 1, Feb. (The journal of the Steel Construction Institute, UK.)
4. Branco F.A. & Green R. (1982) Construction bracing for composite box girder bridges. *International Conference on Short and Medium Span Bridges*, Toronto, Canada. Canadian Society for Civil Engineering
5. British Standards Institution. *Steel, concrete and composite bridges: Parts 1–10*. BS 5400, BSI, London.

| BS 5400:<br>Part | Date | Title   | UK Department of<br>Transport Standard |
|------------------|------|---|--|
| 1                | 1988 | General statement   | BD15/82                                |
| 2                | 1978 | Specification for loads   | BD14/82 & IRLS<br>(Sept. 1983)         |
| 3                | 1982 | Code of practice for design of steel bridges  | BD13/82                                |
| 4                | 1990 | Code of practice for design of concrete bridges   | BD24/84                                |
| 5                | 1979 | Code of practice for design of composite bridges  | BD16/82                                |
| 6                | 1980 | Specification for materials and workmanship, steel  | BD11/82                                |
| 7                | 1978 | Specification for materials and workmanship, concrete, reinforcement and prestressing tendons   | —                                      |
| 8                | 1978 | Recommendations for materials and workmanship, concrete, reinforcement and prestressing tendons | —                                      |
| 9                | 1983 | Bridge bearings   | BD10/83                                |
| 10               | 1980 | Code of practice for fatigue  | BD9/81                                 |

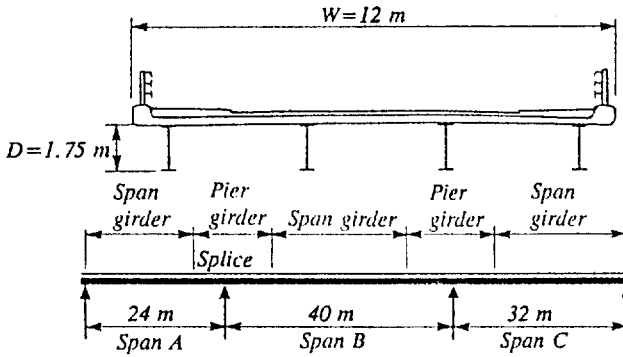
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A worked example follows which is relevant to Chapter 4.

|  |   |  |  |                          |
|--|---|--|--|--------------------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>INITIAL DESIGN OF HIGHWAY BRIDGE</b> |  | Chapter ref.<br><b>4</b> |
|  |   | Design code<br><b>BS5400</b>                       | Made by<br><b>ACGH</b><br>Checked by<br><b>GWO</b> | Sheet no.<br><b>1</b>    |

**Problem**

A composite highway bridge has 3 continuous spans of 24, 40 and 32 m as shown. Overall deck width is 12 m and it carries 45 units of IHB loading. There are 4 plate girders in the cross-section of 1.75 m depth. Estimate the main girder sizes and the weight of structural steel.



$$\text{Average girder spacing 's'} = \frac{12}{4} = 3.0 \text{ m}$$

**Flange and web sizes**

From Figure 4.20

$$\begin{aligned}
 k_{af} &= 0.85 \text{ (top flange span girders)} \\
 k_{af} &= 0.87 \text{ (generally)} \\
 k_{tw} &= 0.95
 \end{aligned}$$


**SPAN A:**

This is an end span so take


$$L = 1.25 \times 24 \text{ m} = 30 \text{ m}$$

$$\text{therefore } L/D = \frac{30 \text{ m}}{1.75 \text{ m}} = 17$$

$$\text{so assume } L/D = 20$$

|  |  |  |                          |
|--|--|--|--------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN   | Subject<br><b>INITIAL DESIGN OF HIGHWAY BRIDGE</b> |  | Chapter ref.<br><b>4</b> |
|  | Design code<br><b>BS5400</b>                       | Made by <b>ACGH</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>       |
| <p><i>Top Flange, <math>A_{ft}</math></i> = <math>A_f</math> (from Figure 4.23) <math>\times K_{af}</math></p> <p>= <math>0.006 \times 0.85 = 0.0051 \text{ m}^2</math> <span style="float: right;"><u>400 <math>\times</math> 15</u></span></p> <p><i>Bottom Flange, <math>A</math></i> = <math>A_f</math> (from Figure 4.23) <math>\times K_{af}</math></p> <p>= <math>0.014 \times 0.87 = 0.012 \text{ m}^2</math> <span style="float: right;"><u>500 <math>\times</math> 25</u></span></p> <p><i>Web, <math>t_w</math></i> = <math>t_w</math> (from Figure 4.23) <math>\times K_{tw}</math></p> <p>= <math>10 \times 0.95 = 9.5 \text{ mm}</math> <span style="float: right;"><u>10 mm web</u></span></p> <p><b><u>SPAN B:</u></b></p> <p><i>Span girder</i></p> <p><math>L/D = \frac{40 \text{ m}}{1.75 \text{ m}} = 22.9</math></p> <p><i>Top Flange, <math>A_{ft}</math></i> = <math>A_f</math> (from Figure 4.23) <math>\times K_{af}</math></p> <p>= <math>0.009 \times 0.85 = 0.0077 \text{ m}^2</math> <span style="float: right;"><u>400 <math>\times</math> 20</u></span></p> <p><i>Bottom Flange, <math>A_{fb}</math></i> = <math>A_f</math> (from Figure 4.23) <math>\times K_{af}</math></p> <p>= <math>0.020 \times 0.87 = 0.0174 \text{ m}^2</math> <span style="float: right;"><u>500 <math>\times</math> 35</u></span></p> <p><i>Web, <math>t_w</math></i> = <math>t_w</math> (see Figure 4.23) <math>\times K_{tw}</math></p> <p>= <math>10 \times 0.95 = 9.5 \text{ mm}</math> <span style="float: right;"><u>10 mm web</u></span></p> <p><b><u>SPAN C:</u></b></p> <p><i>This is an end span so take</i></p> <p><math>L = 1.25 \times 32 \text{ m} = 40 \text{ m}</math></p> <p><i>Therefore sizes as Span B.</i></p> |  |  |                          |



|  |   |  |  |                          |
|--|---|--|--|--------------------------|
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|  |   | Design code<br><b>BS5400</b>                       | Made by<br><b>ACGH</b><br>Checked by<br><b>GWO</b> | Sheet no.<br><b>3</b>    |

**Pier Girders**

Take  $L$  as the greater of the two adjacent spans  
 i.e. assume  $L = 40$  m at both supports.

Therefore  $L/D = 40/1.75 = 22.9$

Top Flange,  $A_{ft} = A_{ft} \text{ (see Figure 4.22)} \times K_{af}$   
 $= 0.015 \times 0.87 = 0.0131 \text{ m}^2$  400 × 35

Bottom Flange,  $A_{fb} = A_{fb} \text{ (see Figure 4.22)} \times K_{af}$   
 $= 0.030 \times 0.87 = 0.026 \text{ m}^2$  500 × 55

Web,  $t_w = t_w \text{ (see Figure 4.22)} \times K_{tw}$   
 $= 16.5 \times 0.95 = 15.7 \text{ mm}$  18 mm web

**Steel Weight**

Span A:  $L = 1.25 \times 24 \text{ m} = 30 \text{ m}$   
 Span B:  $L = 40 \text{ m}$   
 Span C:  $L = 1.25 \times 32 \text{ m} = 40 \text{ m}$


Mean Span  $= \left[ \frac{L^4 + L_2^4 \dots L_n^4}{n} \right]^{1/4} = \left[ \frac{30^4 + 40^4 + 40^4}{3} \right]^{1/4}$   
 $= \underline{37.5}$

$L/D = 37.5/1.75 = 21$

$\text{kg/m}^2 = \text{kg/m}^2 \text{ (from Figure 4.24)} \times K_w \text{ (from Figure 4.20)}$   
 $= 142 \text{ kg/m}^2 \times 1.03 = \underline{146 \text{ kg/m}^2}$

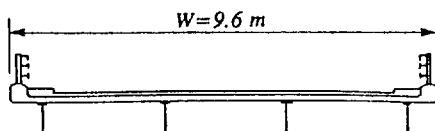
Therefore steel weight

$= \frac{146 \text{ kg/m}^2}{1000} \times (24 \text{ m} + 40 \text{ m} + 32 \text{ m}) \times 12 \text{ m wide} = \underline{168 \text{ tonnes}}$

|  |  |  |                          |
|--|--|--|--------------------------|
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|  | Design code<br><b>BS5400</b>                       | Made by<br><b>ACGH</b><br>Checked by<br><b>GWO</b> | Sheet no.<br><b>4</b>    |

***Problem***

*A composite bridge has a simply supported span of 24 m. Overall deck width is 9.6 m and it carries HA loading only. Estimate the beam sizes and total weight of structural steel assuming that there are 4 beams in the cross-section.*

**a) Elastic Design**

$$\text{For 4 beams, } s = 9.6/4 = 2.4 \text{ m}$$

*From Figure 4.25 use section no. 343  
(914 × 419 × 343 kg/m universal beam)*

$$\text{Total steel weight, } 343 \times 4 \times 24 \times 1.08/1000 = 36 \text{ tonnes} = 154 \text{ kg/m}^2$$

*(1.08 factor allows for bracing and stiffeners)*

**b) Plastic Design**

*From Figure 4.26 use section no. 253  
(914 × 305 × 253 kg/m universal beam)*

$$\text{Total steel weight, } 253 \times 4 \times 24 \times 1.08/1000 = 26 \text{ tonnes} = 114 \text{ kg/m}^2$$

*Plastic design gives a significant reduction in the steel weight, subject to a satisfactory check of the serviceability limit state.*

## Chapter 5

# Other structural applications of steel

Edited by IAN DUNCAN with contributions from MICHAEL GREEN, ERIC HINDHAUGH, IAN LIDDELL, GERARD PARKE and JOHN TYRRELL

## 5.1 Towers and masts

### 5.1.1 Introduction

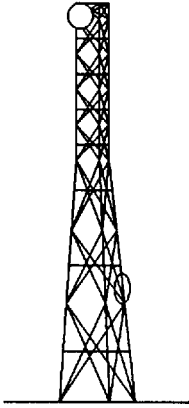
Self-supporting and guyed towers have a wide variety of uses, from broadcasting of television and radio, telecommunications for telephone and data transmission to overhead power lines, industrial structures, such as chimneys and flares, and miscellaneous support towers for water supply, observation or lighting. These structures range from minor lighting structures, where collapse might have almost no further consequences, to major telecommunications links passing thousands of telephone calls or flare structures on which the safety of major chemical plant can depend. The term 'mast' describes a tower which depends for its stability on cable guys.

### 5.1.2 Structural types

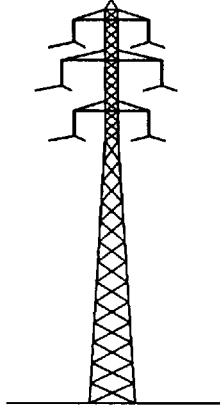
Steel towers can be constructed in a number of ways but the most efficient use of material is achieved by using an open steel lattice. Typical arrangements for microwave radio and transmission towers are shown in Fig. 5.1. The use of an open lattice avoids presenting the full width of structure to the wind but enables the construction of extremely lightweight and stiff structures. Most power transmission, telecommunication and broadcasting structures fall into this class.

Lattice towers are typically square or triangular and have low redundancy. The legs are braced by the main bracings; both of these are often propped by additional secondary bracing to reduce the effective buckling lengths. The most common forms of main bracing are shown in Fig. 5.2.

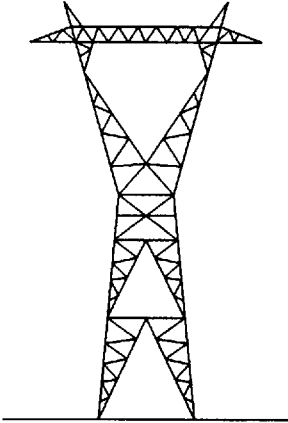
Lattice towers for most purposes are made of bolted angles. Tubular legs and bracings can be economic, especially when the stresses are low enough to allow relatively simple connections. Towers with tubular members may be less than half the weight of angle towers because of the reduced wind load on circular sections. However the extra cost of the tube and the more complicated connection details can exceed the saving of steel weight and foundations.



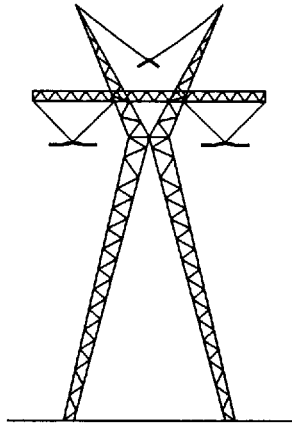
(a)



(b)



(c)



(d)

*Fig. 5.1* Lattice towers: (a) microwave tower, (b), (c) and (d) transmission towers

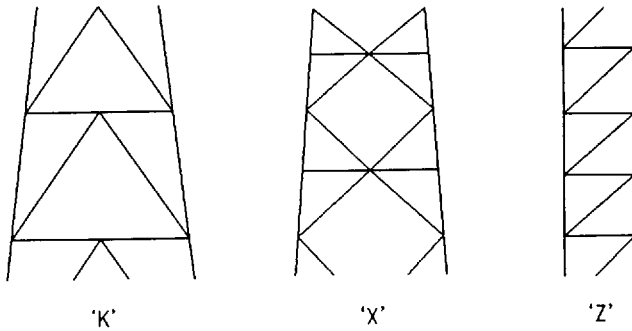


Fig. 5.2 Main bracing arrangements

Connections are usually arranged to allow site bolting and erection of relatively small components. Angles can be cut to length and bolt holes punched by machines as part of the same operation. Where heavy-lift cranes are available much larger segments of a tower can be erected but often even these are site bolted together.

Guyed towers provide height at a much lower material cost than self-supporting towers due to the efficient use of high-strength steel in the guys. Guyed towers are normally guyed in three directions over an anchor radius of typically  $\frac{2}{3}$  of the tower height and have a triangular lattice section for the central mast. Tubular masts are also used, especially where icing is very heavy and lattice sections would ice up fully. A typical example of a guyed tower is shown in Fig. 5.3.

The range of structural forms is wide and varied. Other examples are illustrated in Figs 5.4 and 5.5. Figure 5.4 is a modular tower arrangement capable of extension for an increased number of antennas. The arrangement shown in Fig. 5.5 is adopted for supporting flare risers where maintenance of the flare tip is carried out at ground level.

A significant influence on the economics of tower construction is the method of erection which should be carefully considered at the design stage.

### 5.1.3 Environmental loading

The primary environmental loads on tower structures are usually due to wind and ice, sometimes in combination. Earthquakes can be important in some parts of the world for structures of high mass, such as water towers. Loading from climatic temperature variations is not normally significant but solar radiation may induce local stresses or cause significant deflections and temperatures can influence the choice of ancillary materials.

Most wind codes use a simple quasi-static method of assessing the wind loads which has some limitations for calculating the along-wind responses but is adequate

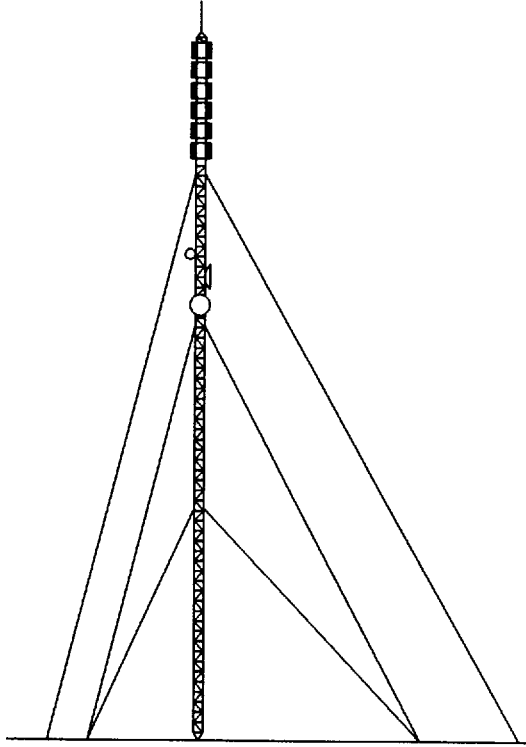


Fig. 5.3 Guyed tower

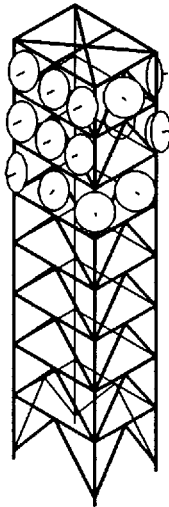


Fig. 5.4 Modular tower

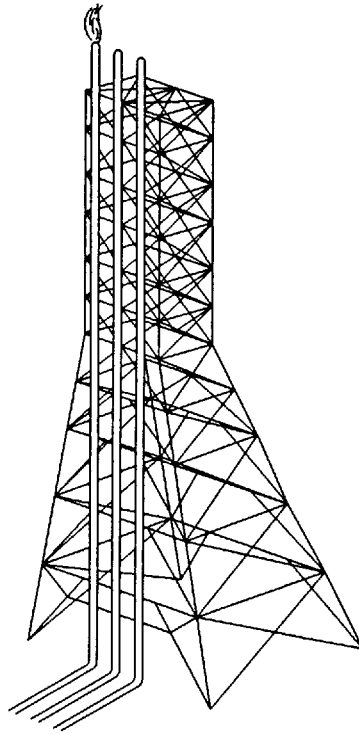


Fig. 5.5 Flare tower

for the majority of structures. Tower structures with aerodynamically solid sections and some individual members can be subject to aeroelastic wind forces caused by vortex shedding, galloping, flutter and a variety of other mechanisms which are either poorly covered or ignored by current codes of practice. Such factors have been responsible for more tower collapses and serviceability failures worldwide than any shortfall in resistance to along-wind loads.

CP3<sup>1</sup> specifies wind loads in the UK in terms of design gust wind speeds that will recur on average once in a 50-year period (i.e. with an annual probability of 2%). Guidance is given on wind shape factors for typical sections and lattices. There is no consideration of dynamic response to the wind. It is assumed that the loads will be used with working stresses in the members.

BS 8100<sup>2</sup> is a more recent code in a limit state format specifically written for towers. Wind loads are specified in terms of a '50-year return' mean hourly wind pressure together with gust factors which convert the forces to an equivalent static gust. The overall wind forces calculated using BS 8100 are substantially similar to those that would be obtained using CP3 but forces near the tops of towers are relatively higher due to an allowance for dynamic response. The code also gives

guidance on means of allowing for the importance of particular structures by adjusting the partial factor on the design wind speed.

Guidance is limited for structures that have a significant dynamic response at their natural frequencies and gust factors for guyed towers are specifically excluded from the scope of the code. Part 4 of BS 8100 is intended to address these aspects.

The influence of height and topography on wind speed can be significant; this is covered in some detail in both codes. Ice loads and types of ice are also covered but neither mentions the very significant influence of topography on the formation of ice. This has not yet been subject to systematic study but some hill sites are known to be subject to icing well in excess of the code requirements. The combination of wind and ice loads is even less well understood although some guidance is given.

#### **5.1.4 Analysis**

In the analysis of towers the largest uncertainty is accurate knowledge of the wind loads. Highly sophisticated methods of analysis cannot improve this. A static linear three-dimensional structural analysis is sufficient for almost all lattice tower structures.

For transmission towers, line break conditions can also be critical. Line breakage will in general induce dynamic loads in addition to any residual static loads. Detailed consideration of transmission tower loading is outside the scope of this section.

For lattice towers with large complicated panel bracing, the secondary bracing forces can be significantly altered by non-linear effects caused by curvature of the panels under the influence of the design loads. Generally the rules in the codes are sufficient, but where structures are of particular importance or where there is much repetition of a design, a non-linear analysis may be necessary.

Dynamic analyses of self-supporting lattice towers are rarely necessary unless there are special circumstances such as high masses at the top, use as a viewing platform or circular or almost solid sections of mast which could be responsive to vortex shedding or galloping. Knowledge of the dynamic response is also necessary for assessment of fatigue of joints if this is significant.

For guyed towers the non-linear behaviour of the guys is a primary influence and cannot be ignored. The choice of initial tension, for example, can have a very great effect on the deflections (and dynamic behaviour). The effects of the axial loads in the mast on column stiffness can be significant. Methods of static analysis are given in the main international codes for the design of guyed towers. Guyed towers can also be particularly sensitive to dynamic wind effects especially those with cylindrical or solid sections.<sup>2</sup>

General guidance on the dynamic responses and aerodynamic instabilities of towers can be obtained from References 3, 4, 5 and 6.



### 5.1.5 Serviceability

Serviceability requirements vary greatly depending on the purpose of the structure and its location.

Steel towers and connections are normally galvanized and are also painted with a durable paint system if the environment is likely to be polluted or otherwise corrosive. It is important that regular maintenance is carried out; climbing access is normally provided for inspections.

Deflections of towers are generally significant only if they would result in a loss of serviceability. This can be critical for the design of telecommunication structures using dish antennas. In the past signal losses due to deflection have often been assessed on the misunderstanding that the deflections under the design wind storm would occur sufficiently often to affect the signals. Studies have demonstrated that short periods of total loss of signal during storms smaller than the design wind storm have a negligible effect on the reliability of microwave links compared to losses due to regular atmospheric conditions.

### 5.1.6 Masts and towers in building structures

Consideration of a masted solution arises from the need to provide a greater flexibility in the plan or layout of the building coupled with its aesthetic value to the project as a whole. At the same time it offers the opportunity to utilize structural materials in their most economic and effective tensile condition. The towers or masts can also provide high-level access for maintenance and plant support for services. The plan form resulting from a mast structure eliminates the need for either internal support or a deeper structure to accommodate the clear span. By providing span assistance via suspension systems the overall structural depth is minimized giving a reduction in the clad area of the building perimeter. The concentration of structural loads to the mast or towers can also benefit substructure particularly in poor ground conditions where it is cost effective to limit the extent of substructures (Figs 5.6 and 5.7). However, differential settle-

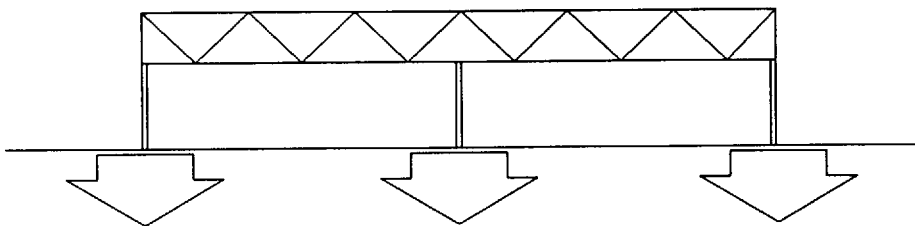


Fig. 5.6 Traditional long-span structure

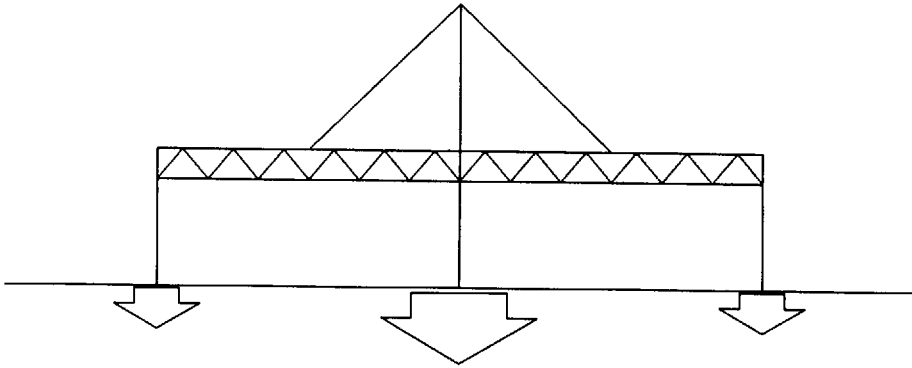


Fig. 5.7 Suspension structure

ment can have a significant effect on the structure by relaxing ties on suspension systems. The consequent load redistribution must be considered.

Most tension structure building forms consist of either central support, perimeter support or a mixture of the two. Any other solutions are invariably a variation on a theme. Plan form tends to be either linear or a series of repetitive squares.

The forces and loads experienced by towers and masts are illustrated in Figs 5.8 and 5.9. In all cases it is advantageous but not essential that forces are balanced

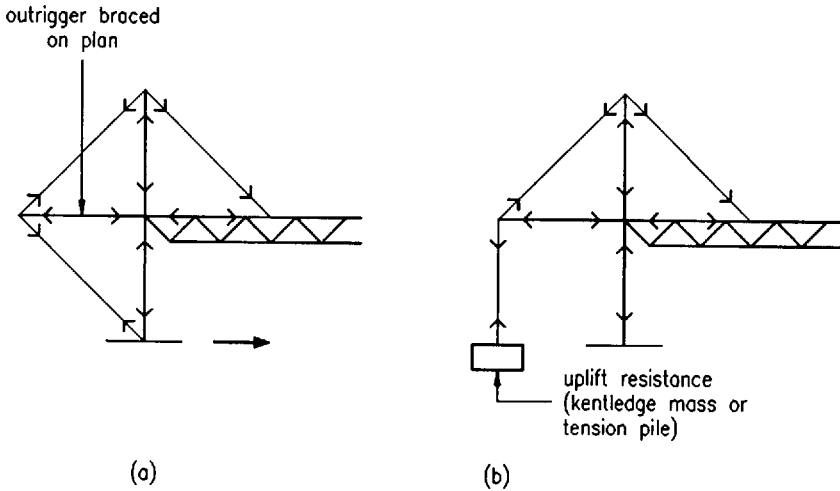


Fig. 5.8 Types of perimeter support

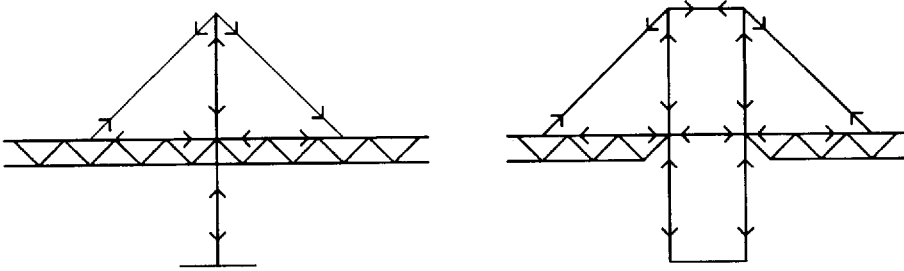


Fig. 5.9 Central support

about the mast. Out-of-balance loads will obviously generate variable horizontal and vertical forces which require resolution in the assessment of suitable structural sections.

Suspension ties must be designed not only to resist tension but also the effects of vibration, ice build-up and catenary sag. Ties induce additional compressive forces in the members they assist. These forces require careful consideration, often necessitating additional restraints in the roof plane in either the open sections or top chord of any truss.

Longitudinal stability is created by either twinning the masts and creating a vertical truss or by cross bracing preferably to ground (Fig. 5.10).

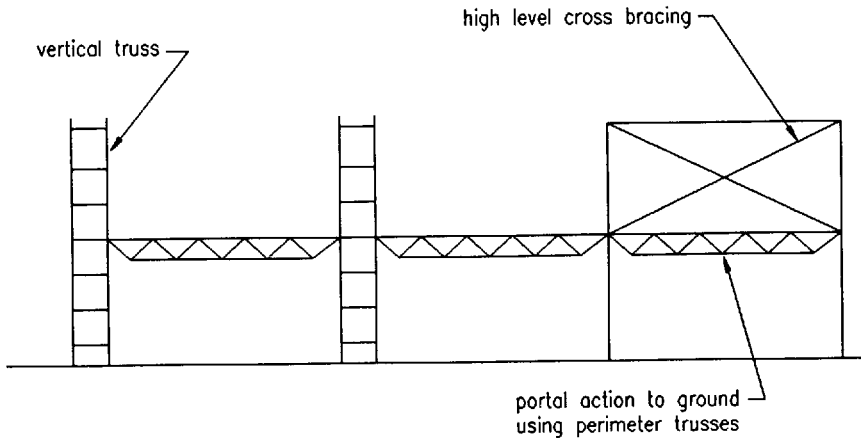


Fig. 5.10 Longitudinal stability

If outriggers are used as is the case with the majority of masted structures then the lateral stability of the outrigger can be resolved in a similar form to the masts by a stiff truss or Vierendeel section in plan or by plan or diagonal bracing at the extremity. (Fig. 5.11.)

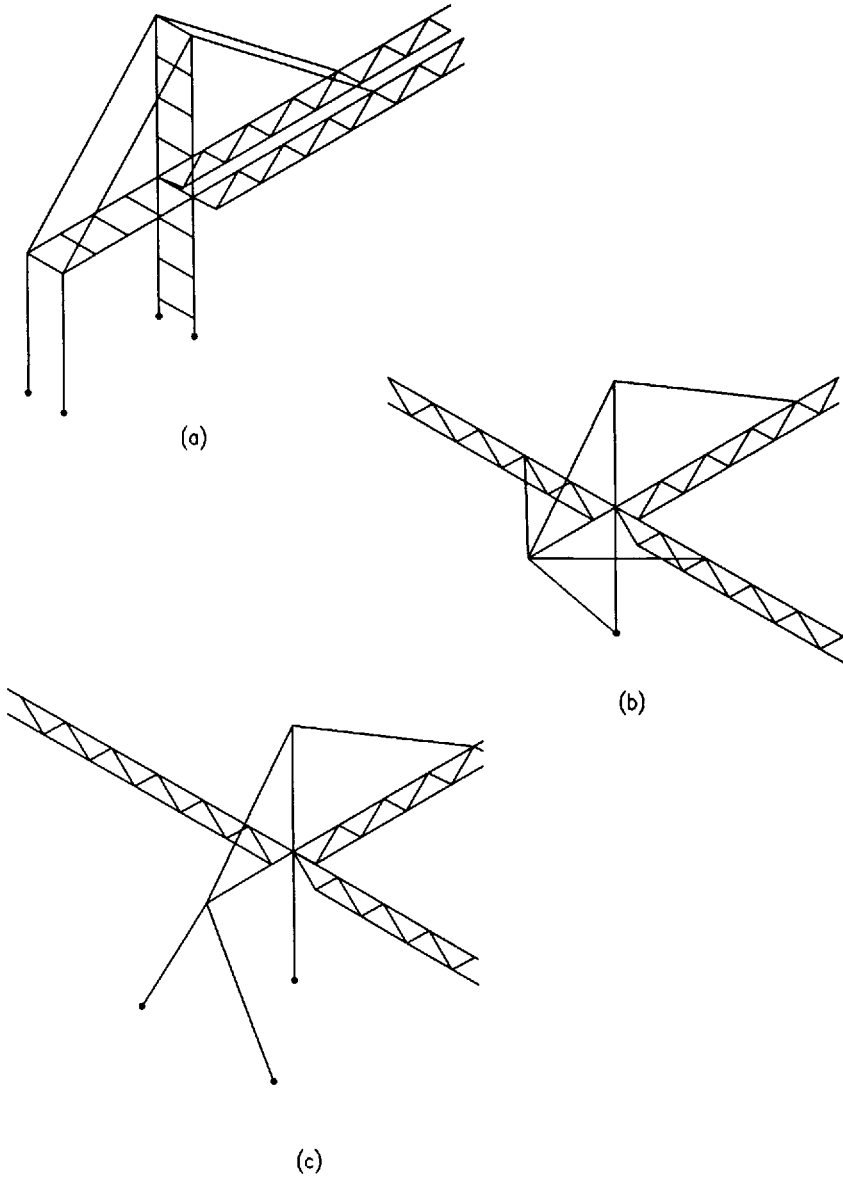


Fig. 5.11 Outrigger stability: (a) Vierendeel, (b) plan bracing, (c) diagonal bracing

## 5.2 Space frames

### 5.2.1 Introduction

Steel skeletal space frames are three-dimensional structures capable of very large column-free spans. These structures constructed from either individual elements or prefabricated modules possess a high strength-to-weight ratio and stiffness. Steel space frames may be used efficiently to form roofs, walls and floors for projects such as shopping arcades but their real supremacy is in providing roof cover for sports stadia, exhibition halls, aircraft hangars and similar major structures.

### 5.2.2 Structural types

Space frames are classified as single-, double- or multi-layered structures which may be flat, resulting in grid structures, or may be curved in one or two directions, forming barrel vaults and dome structures. Grid structures can be further categorized into lattice and space grids in which the members may run in two, three or four principal directions. In double-layer lattice grids the top and bottom grids are identical, with the top layer positioned directly over the bottom layer. Double-layer space grids are usually formed from pyramidal units with triangular or square bases resulting in either identical parallel top and bottom grids offset horizontally to each other, or parallel top and bottom grids each with a different configuration interconnected at the node points by inclined web members to form a regular stable structure.

Single-layer grids are primarily subject to flexural moments, whereas the members in double- and triple-layer grids are almost entirely subject to axial tensile or compressive forces. These characteristics of single-, double- and triple-layer grids determine to a very large extent their structural performance. Single-layer grids, developing high flexural stresses are suitable for clear spans up to 15 m while double-layer grids have proved to be economical for clear spans in excess of 100 m. The main types of double-layer grids in common use are shown in Fig. 5.12.

Skeletal space frames curved in one direction forming single- or double-layer barrel vaults also provide elegant structures capable of covering large clear spans. Single-layer vaults are suitable for column-free spans of up to 40 m which may be substantially increased by incorporating selected areas of double-layer structure forming stiffening rings. Double-layer barrel vaults are normally capable of clear spans in excess of 120 m. Figure 5.13 shows the main types of bracing used for single-layer barrel vaults.

Dome structures present a particularly efficient and graceful way of providing cover to large areas. Single-layer steel domes have been constructed from tubular members with spans in excess of 50 m while double-layer dome structures have been constructed with clear spans slightly greater than 200 m. Skeletal dome

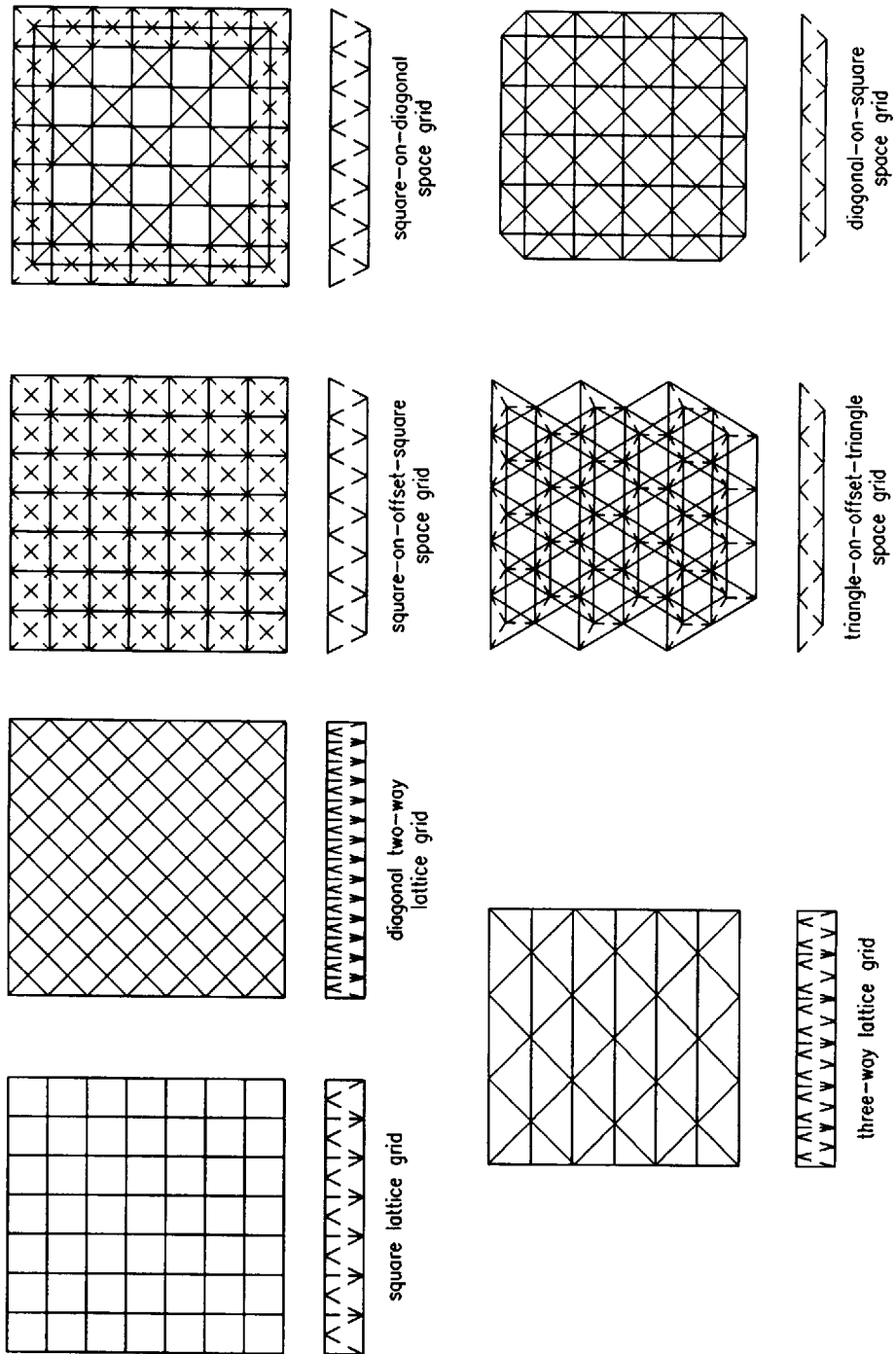


Fig. 5.12 Lattice and space grids

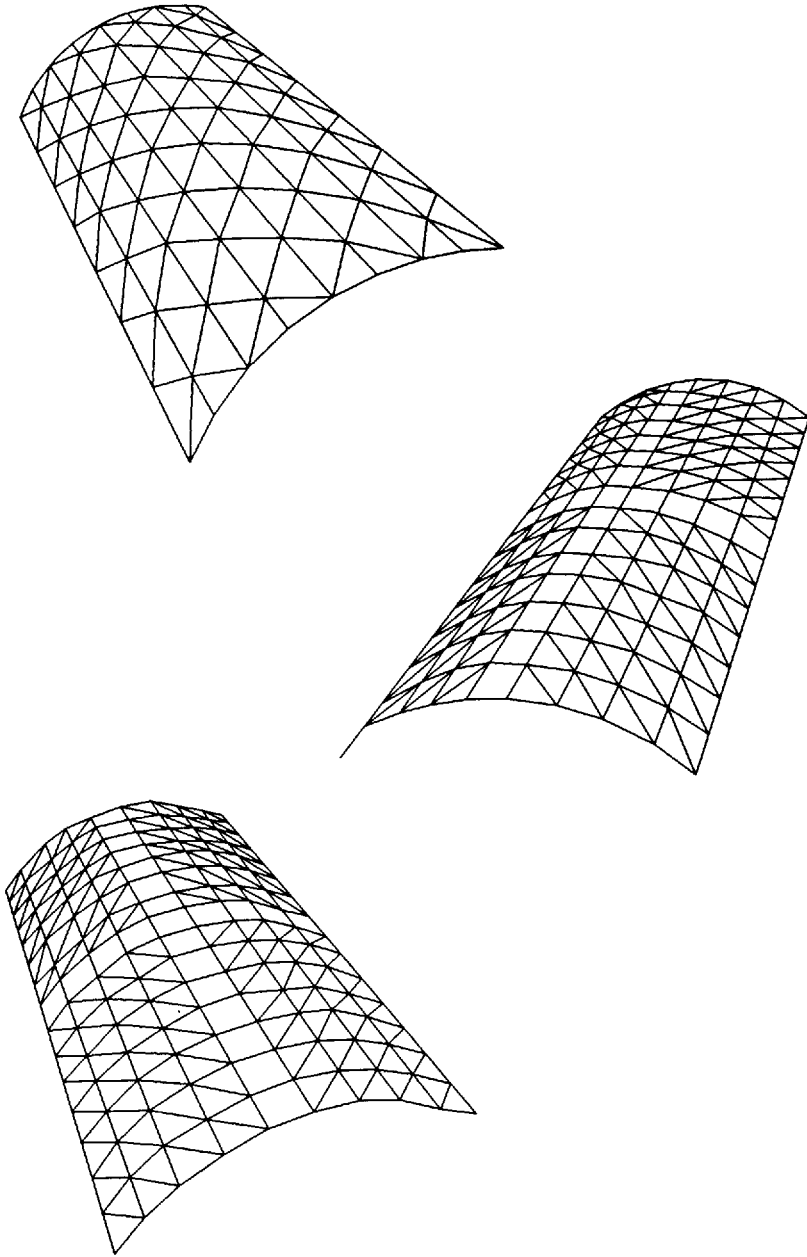


Fig. 5.13 Bracing of single-layer barrel vaults

structures can be classified into several categories depending on the orientation and position of the principal members. The four most popular types usually constructed in steel are ribbed domes, Schwedler domes, three-way grid domes and parallel lamella domes.

Ribbed domes, as the name suggests, are formed from a number of identical rib members which follow the meridian line of the dome and span from the foundations up to the top of the structure. The individual rib members may be of tubular lattice construction and are usually interconnected at the crown of the dome using a small diameter ring beam.

The Schwedler dome is also formed from a series of meridional ribs but unlike the ribbed dome, these members are interconnected along their length by a series of horizontal rings. In order to resist unsymmetric loads the structure is braced by diagonal members positioned on the surface of the dome bisecting each trapezium formed by the meridional ribs and horizontal rings.

Three-way grid domes are formed from three principal sets of members arranged to form a triangular space lattice. This member topology is ideally suited to both single-layer and double-layer domes and numerous beautiful large-span steel three-way domes have been constructed throughout the world.

The steel lamella dome is formed from a number of 'lozenge'-shaped lamella units which are interconnected together to form a diamond or rhombus arrangement. The spectacular Houston Astrodome is an excellent example of this type of construction. This impressive steel double-layer dome was constructed from lamella units 1.52 m deep and has an outside diameter of 217 m with an overall height of 63.4 m. Figure 5.14 shows the four main dome configurations now in prominent use worldwide.

### 5.2.3 Special features

The inherent characteristics of steel skeletal space frames facilitate their ease of fabrication, transportation and erection on site. There are two main groups into which the majority of space frames may be classified for assembly purposes; the particular structure may be assembled from a number of individual members connected together by purpose-made nodes or alternatively may be constructed by joining together modular units which have been accurately fabricated in a factory before transportation to site.

There are numerous examples of 'chord and joint' space frame systems available for immediate construction. These systems offer full flexibility of member lengths and intersecting angles required in the construction of skeletal dome structures. Many jointing systems are available; Figs 5.15 and 5.16 show a typical spherical node used in the MERO system and a cast steel node used in the NODUS system.

The 'modular' systems are usually based on pyramidal units which are prefabricated from channel, angle, circular hollow section or solid bars. The individual



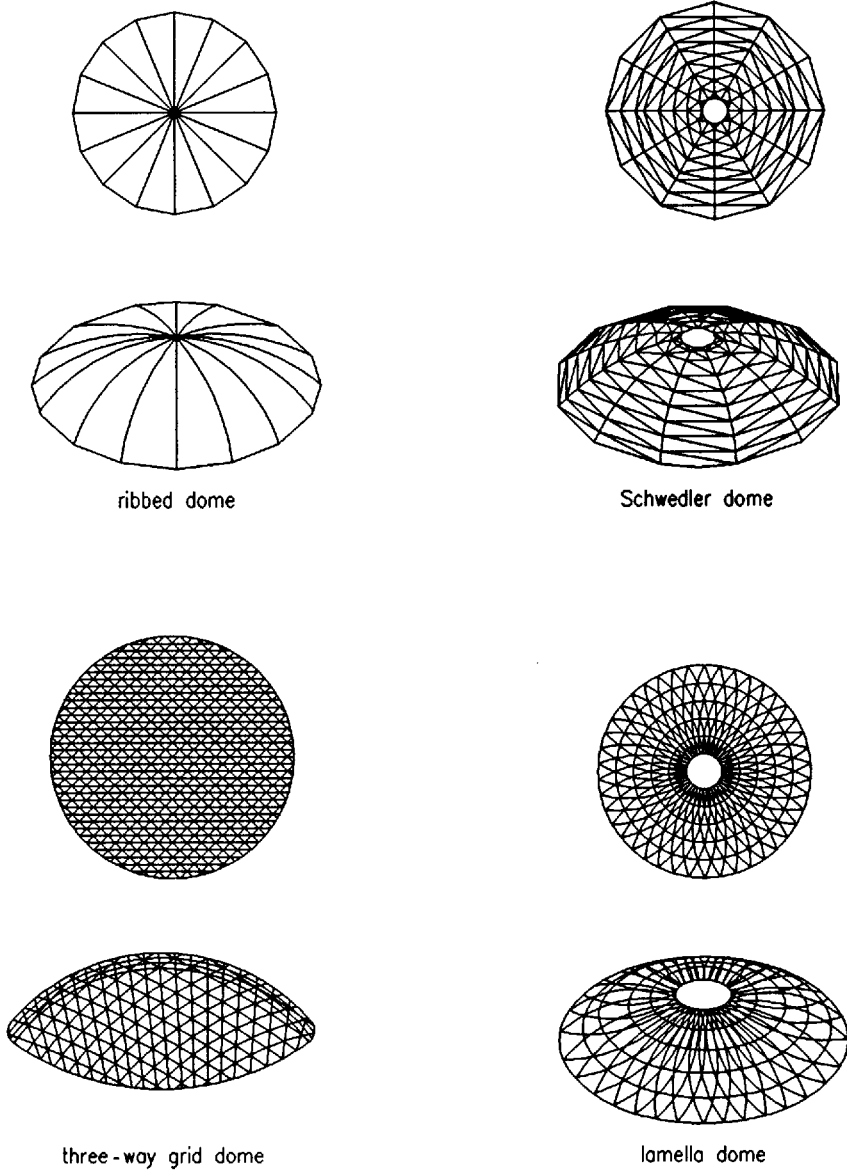
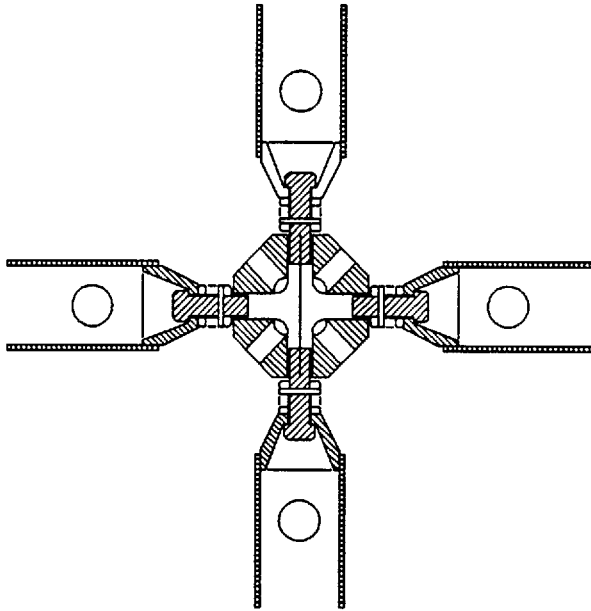


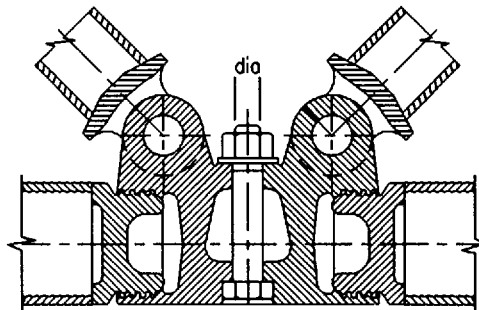
Fig. 5.14 Dome configurations

units are designed to nest together to facilitate storage and transportation by road or sea. Most manufacturers of modular systems hold standard units in stock which greatly enhances the speed of erection. Figure 5.17 shows typical details of the prefabricated steel modular inverted pyramidal units used in the Space Deck System.



*Fig. 5.15* MERO node connector

Steel space frames are generally erected rapidly without the use of falsework. Double-layer grids of substantial span can be constructed entirely at ground level including services and cladding and subsequently lifted or jacked up into the final position. Dome structures can be assembled from the top downwards using a central climbing column or tower. A novel approach adopted for the erection of a dome with a major axis of 110 m and a minor axis of 70 m involved fabrication of the dome on the ground in five sections which were temporarily pinned to each other. The central section was then lifted and the remaining segments of the dome locked into position as shown in Fig. 5.18.



*Fig. 5.16* NODUS node connector

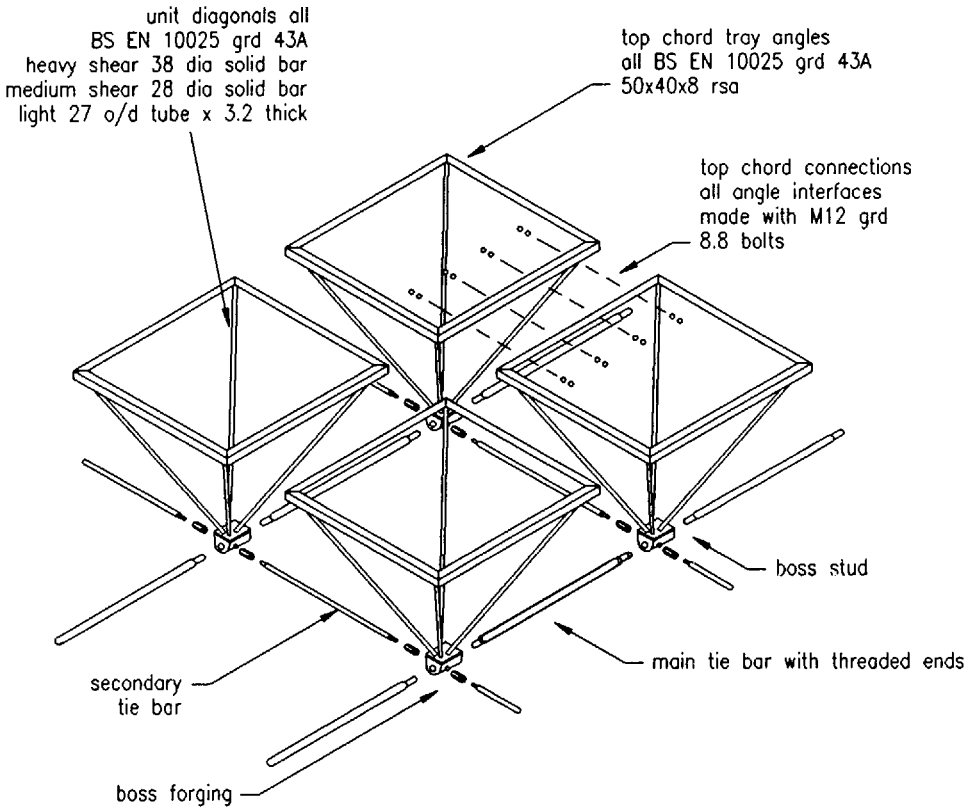


Fig. 5.17 Exploded view of 2.4 m square section of Space Deck

### 5.2.4 Analysis

The analysis of space frames results in the production of large sets of linear simultaneous equations which must inevitably require the use of a computer for their solution. For these equations to be formulated it is necessary to input into the computer significant amounts of information relating to the topology of the structure and properties of the individual members. This operation can be very time-consuming unless modern pre-processing techniques which allow rapid data generation are adopted.<sup>7</sup>

The members forming double-layer space frames are principally stressed in either axial tension or axial compression. Consequently it is usual in the analysis of double-layer space trusses to assume that the members in the structure are pin-jointed, irrespective of the actual joint rigidity. This assumption may lead to the overestimation of node deflections but because only three degrees of freedom are

assembly on the ground, with temporarily pinned joints

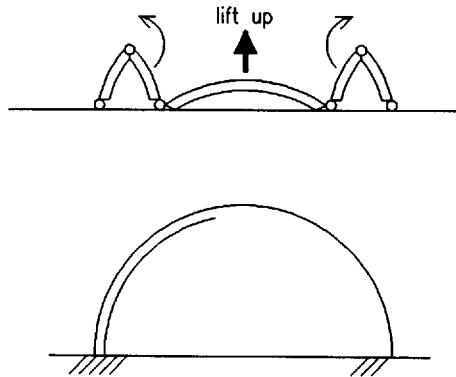


Fig. 5.18 Novel method of dome erection

permitted at each node this approach minimizes computer storage requirements and processing time.

Single-layer grid and barrel vault structures carry the imposed load by flexure of the members so it is important to include in the analysis the flexural, torsional and shear rigidity of the members. Linear analysis only is required for the majority of skeletal space structures but to ensure stability of shallow domes it is essential to undertake a non-linear analysis of these structures. Large-span space structures may benefit from a full collapse analysis where the ultimate load-carrying capacity and collapse behaviour of the structure are determined.<sup>8</sup>

The behaviour of both single-layer and double-layer space trusses is influenced to a great extent by the support positions of the structure. The effects of joint and overall frame rigidity also have a commanding influence and affect the buckling behaviour of the compression members within the structure. Great care must be taken in assessing the effective lengths of compression members and it is unlikely that internal and edge compression members will exhibit similar critical buckling loads.

## 5.3 Cable structures

### 5.3.1 Range of applications

#### 5.3.1.1 Introduction

Most structural elements are able to carry bending forces as well as tension and compression, and are hence able to withstand reversals in the direction of loading. Tension elements are unique in that they can only carry tension. In compressive

or bending elements, the loading capacity is often reduced by buckling effects while tension elements can work up to the full tensile stress of the material. Consequently full advantage can be taken of high-strength materials to create light, efficient and cost-effective long-span structures.

To create useful spanning or space-enclosing structures the tension elements have to work in conjunction with compression elements. From an architectural point of view, the separation of the tension, compression and bending elements leads to a visual expression of the way the structure carries the loads, or at least one set of loads. Tension structures come in a wide range of forms which can be broadly categorized as follows:

- (1) two-dimensional
  - suspension bridges
  - draped cables
  - cable-stayed beams
  - cable trusses
- (2) three-dimensional – cable truss systems
- (3) surface-stressed
  - pneumatically-stressed
  - prestressed.

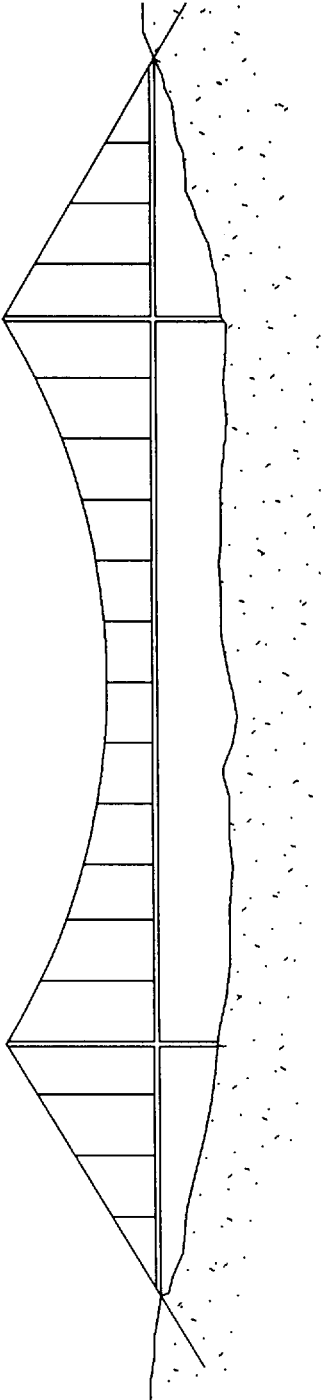
### 5.3.1.2 Structural forms

#### *Suspension bridges (draped cable)*

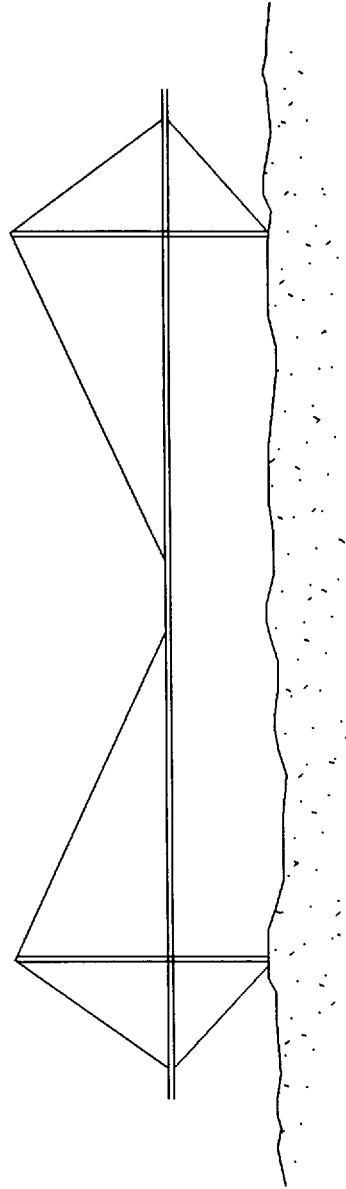
A suspension bridge (Fig. 5.19) is essentially a catenary cable prestressed by dead weight only. Early suspension bridges with flexible decks suffered from large deflections and sometimes from unstable oscillation under wind. A system of inclined hangers proposed originally to reduce deflection under live load has been employed recently also to counteract wind effects. The suspension cable is taken over support towers to ground anchors. The stiffened deck is supported primarily by the vertical or inclined hangers. The system is ideally suited to resisting uniform downward loads. The principle has been used for buildings, mostly as draped cable structures.

#### *Cable-stayed beams*

Cables assist the deck beam by supporting its self-weight. Compression is taken in the deck beam so that ground anchors are not required (Fig. 5.20). The cable-stayed principle has recently been developed for single-storey buildings (see section 5.1 of this chapter). The cable system is designed for and primarily resists gravity loads; in buildings with lightweight roof construction the uplift forces, which are of similar magnitude, are resisted by bending of the stiffening girders. The system is suitable for spans of 30–90 m and has recently been widely used for industrial and sports buildings.



*Fig. 5.19* Suspension bridge



*Fig. 5.20* Cable-stayed beam

### *Cable truss*

The hanging cable resists downloads and the hogging cable resists upload (Fig. 5.21). If diagonal bracing is used, non-uniform load can be resisted without large deflections but with larger fluctuation of force in the cables.

### *Three-dimensional cable truss*

The classic form of this structure is the bicycle wheel roof, in which a circular ring beam is braced against buckling by a radial cable system. These radial cables are divided into an upper and lower set, providing support to the central hub (Fig. 5.22). The system is suitable for spans of 20–60 m diameter. This system has recently been developed (by David Geiger) into a cable dome, having two or three rings of masts (Fig. 5.23). The radial forces at the bases of the masts are resisted by circumferential cables. The masts are also cross-cabled circumferentially to maintain their stability. These structures can span up to 200 m.

### *Surface-stressed structures*

A cable network can be arranged to have a doubly-curved surface either by giving it a boundary geometry which is out-of-plane or by inflating it with air pressure. The cable net must be prestressed either by tensioning the cables to the boundary points or by the inflation pressure. The effect of the double curvature and the prestress is to stiffen the structure to prevent undue deflection and oscillation under loads. Cable net structures can create dramatic wide-span roofs very economically. They can be clad with fabric, transparent foil, metal decking or timber boarding, insulation and tiles.

Low-profile air-supported roofs can provide the most economical structure for covering very large areas (10–50 acres). In designing these structures the aerodynamic profile must be taken into consideration, as must snow loading and the methods of installation and maintenance.

## **5.3.2 Special features**

### *5.3.2.1 Elementary cable mathematics*

#### *Load/extension relationship*

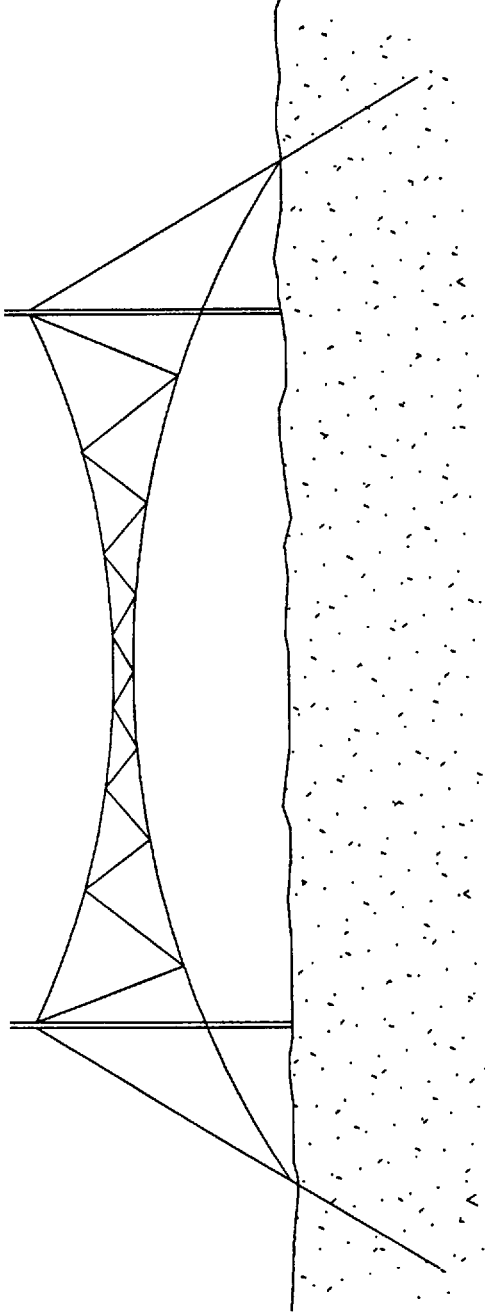
$$\text{Extension} \quad e = \frac{TL}{AE}$$

where  $T$  = load in cable

$L$  = length of cable

$A$  = cross-sectional area

$E$  = Young's modulus.



*Fig. 5.21* Cable truss



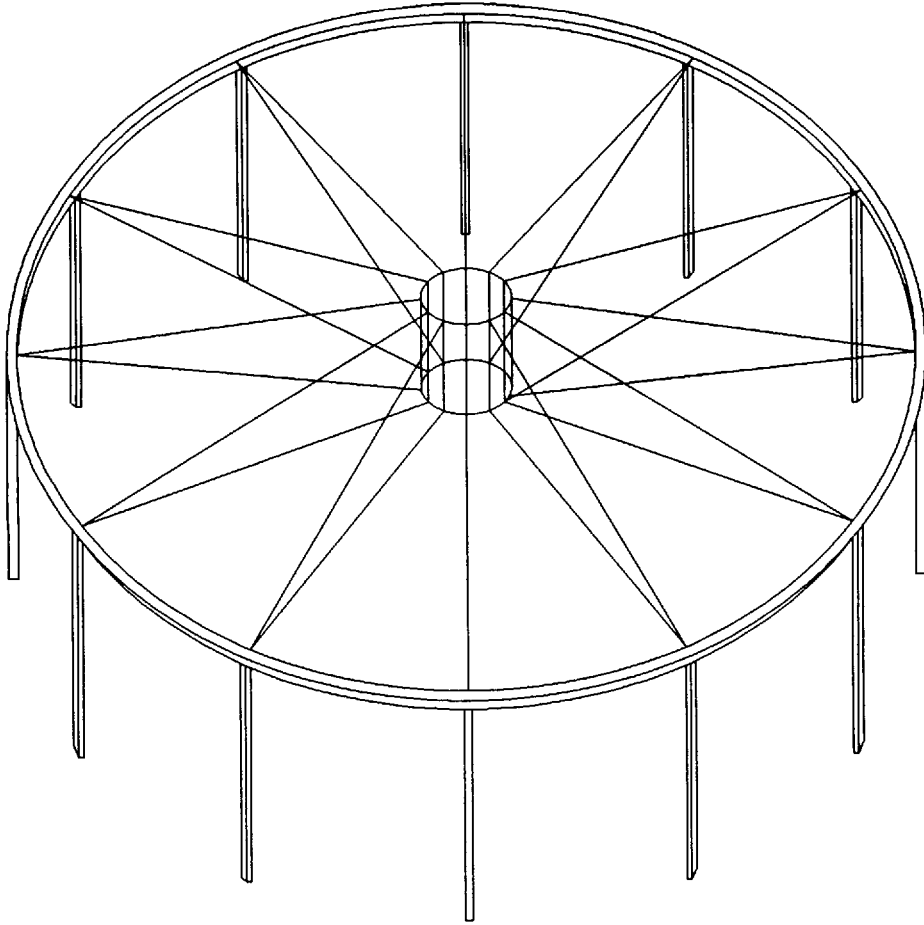
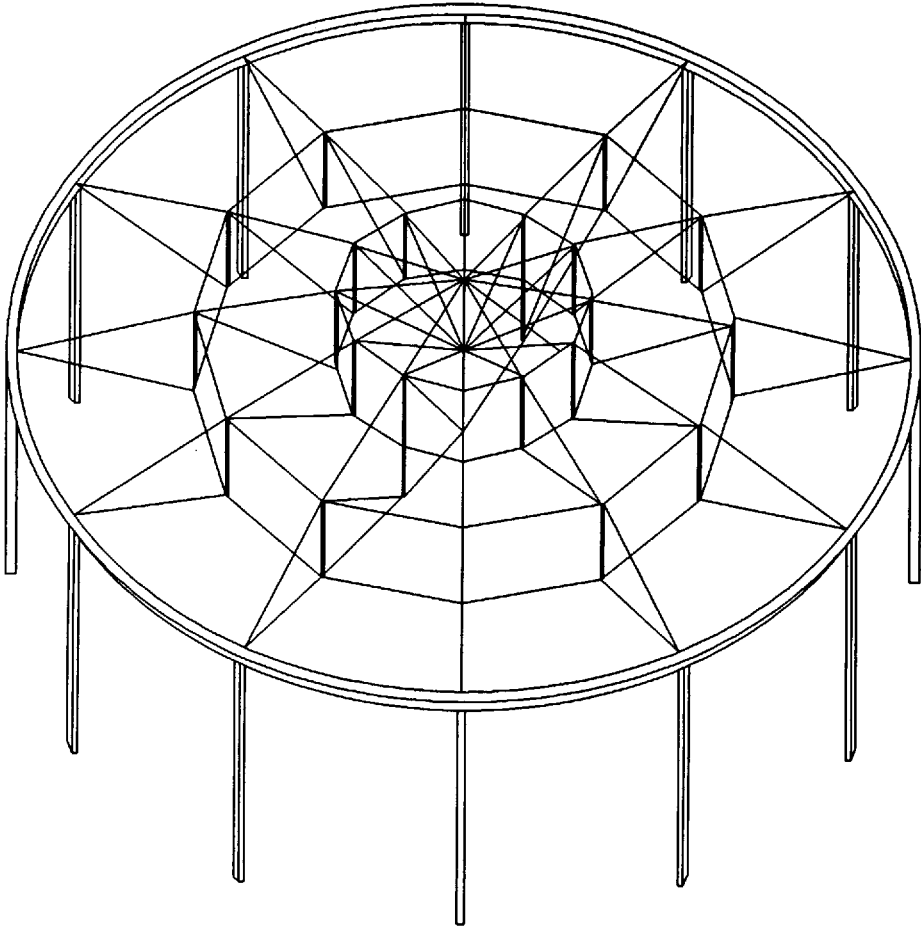


Fig. 5.22 Bicycle wheel roof

Typical values for materials are given in Table 5.1.

**Table 5.1** Material properties

| Material         | $E$<br>(kN/mm <sup>2</sup> ) | Ultimate<br>tensile<br>strength<br>(N/mm <sup>2</sup> ) |
|------------------|------------------------------|---|
| Solid steel      | 210.0                        | 400–2000  |
| Strand           | 150.0                        | 2000  |
| Wire rope        | 112.0                        | 2000  |
| Polyester fibres | 7.5                          | 910   |
| Aramid fibres    | 112.0                        | 2800  |



*Fig. 5.23 Cable dome*

The  $E$  value for wire rope applies after the construction stretch has been pulled out of wire rope by load cycling to 50% of the ultimate tensile strength. In wire rope the construction stretch can be as much as 0.5%. This is of the same order of magnitude as the elastic stretch in the cable at maximum working load.

*Circular arc loaded radially (Fig. 5.24)*

Tension  $T = PR$

where  $P$  = load/unit length radial to cable

$R$  = radius of cable.

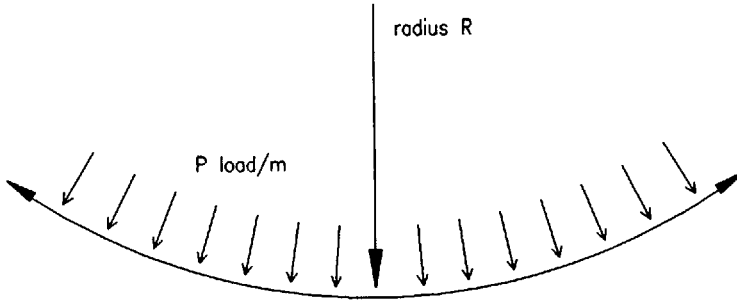


Fig. 5.24 Circular arc loaded radially

Radius of circular arc,  $R$  (Fig. 5.25)

$$\text{Radius } R = \frac{S^2}{8d} + \frac{d}{2}$$

where  $S$  = span  
 $d$  = dip.

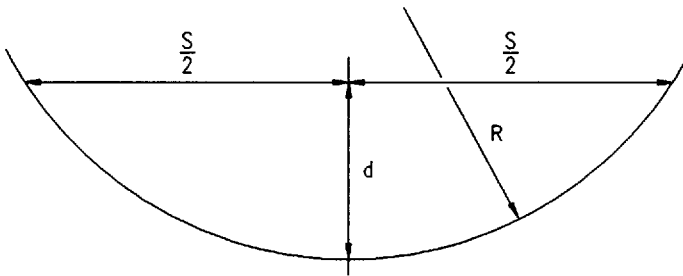


Fig. 5.25 Radius of circular arc

Catenary loaded vertically (Fig. 5.26)

$$\text{Horizontal force } H = \frac{WS^2}{8d}$$

$$\text{Vertical force } V = \frac{WS}{2}$$

$$\text{Maximum tension } T = (H^2 + V^2)^{\frac{1}{2}}$$

where  $S$  = span  
 $d$  = dip  
 $W$  = vertical load/unit length.

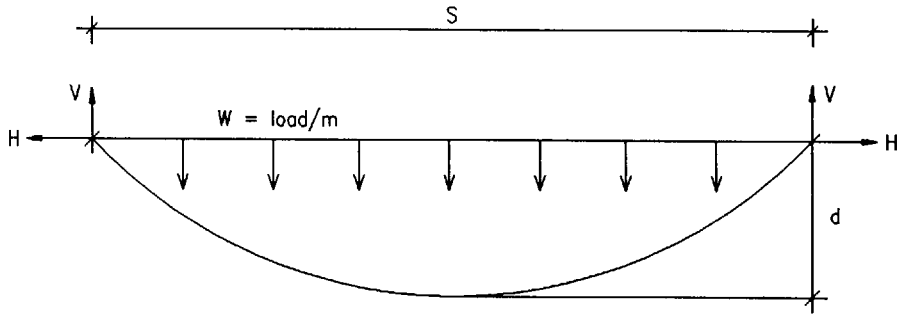


Fig. 5.26 Catenary loaded vertically

These formulae permit initial estimates of forces in cables to be made. For full and accurate analysis it is necessary to use a non-linear computer analysis which takes into account the change of curvature caused by stretch. For well curved cables the hand analysis is accurate enough and gives a useful guide to the forces involved and hence the sizes of cables and fittings.

*Prestressed cable*

The straight cable (or flat fabric) is a special problem. To be straight, the cable must have an initial or prestress tension and theoretically zero weight. In order to carry load the cable must stretch and sag to a radius  $R$ .

For

- span  $= S$
- load/unit length  $= W$
- stiffness  $= EA$
- pre-tension  $= T_0$
- tension under load  $= T$

Equilibrium equation  $T = RW$  (5.1)

New length  $L = 2R \sin^{-1} (S/2R)$  (5.2)

Strain  $= (L - S)/S$  (5.3)

Tension  $T = T_0 + EA (L - S)/S$  (5.4)

Eliminating  $R$  between Equations (5.1) and (5.2), substituting for  $L$  in Equation (5.4) and rearranging gives:

$$\frac{T - T_0}{EA} = \frac{2T}{SW} \sin^{-1} \frac{SW}{2T} - 1$$
 (5.5)

This equation can be solved iteratively for  $T$ . The deflection can be found from the earlier formulae for  $T$  and  $R$  for a circular arc. It should be noted that:

- (1) the extension of a tie with low initial tension is considerably more than  $TL/EA$ .
- (2) straight cables can be used for load carrying, but either the tension will be very high or there will be large deflections.

*Two-way cable net (Fig. 5.27)*

Approximate calculations can be carried out by hand in a similar way to the single cable calculations above. The basic equilibrium equation for two opposing cables is:

$$\frac{t_1}{R_1} + \frac{t_2}{R_2} = P$$

where  $P$  = load/surface area and  $t_1$  and  $t_2$  are the tensions/unit width, i.e.

$$t_1 = \frac{T_1}{a_1} \quad t_2 = \frac{T_2}{a_2}$$

where  $a_1$  and  $a_2$  are the cable spacings and  $T_1$  and  $T_2$  are the cable tensions.

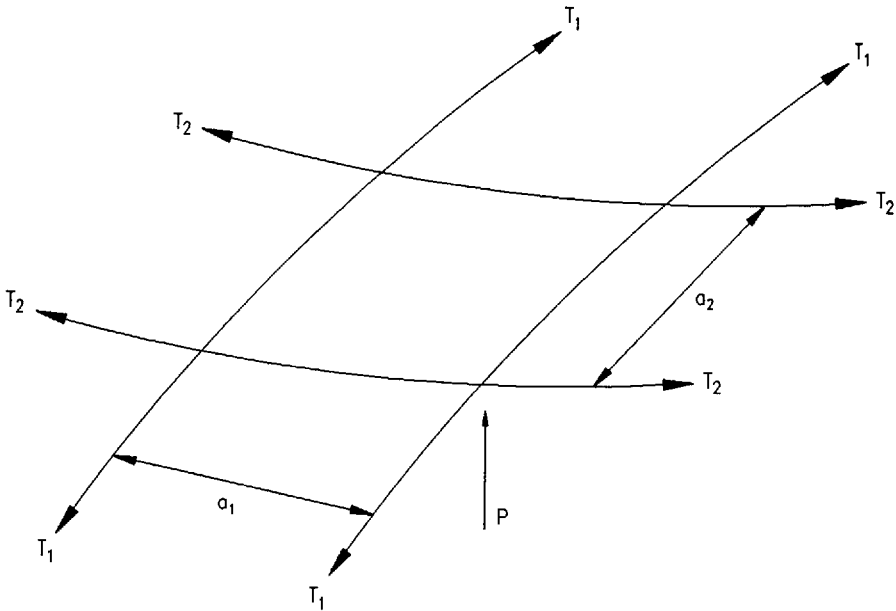


Fig. 5.27 Two-way cable net

The loads on ridge cables and boundaries can be estimated from resolution of the cable forces if the geometry is known.

The full analysis of cable net structures is a specialized and complicated process which requires specially written computer programs. The procedure involves the following stages:

- (1) **Formfinding:** In this stage the cables are treated as constant tension elements and the geometry is allowed to move into its equilibrium position. On completion of the formfinding stage the cable net geometry under the prestress forces will be defined.
- (2) **Load analysis:** The prestress model is converted into an elastic model. To do this the slack lengths,  $l$ , of all elements must be set so that

$$l_0 = l - \frac{T}{EA}$$

The model is then analyzed for the defined dead, wind and snow loads.

- (3) **Cutting pattern definitions:** Cable net structures are fully prefabricated with exact cable lengths so that the prestressed form can be realized. In this stage the form model will be refined so that the mesh lengths are exactly equal, etc. The offsets for the boundary clamps must be allowed for. The stressed cable lengths can then be defined.

During prefabrication of the cables they must be prestretched to eliminate construction stretch; they must then be marked at the specified tensions. Tolerances in fabrication are of the order of 0.02%.

### 5.3.3 Detailing and construction

#### 5.3.3.1 Cables and fittings

Wire rope cables are spun from high tensile wire. For structural work the cables are multi-strand, typically  $6 \times 19$  or  $6 \times 37$  with independent wire rope core and galvanized to Class A. For increased corrosion-resistance, the largest diameter wire should be used and cables can be filled with zinc powder in a slow-setting polyurethane varnish during the spinning process. For even greater corrosion-resistance, filled strand or locked-coil strand can be used to which a shrunk-on polyurethane or polypropylene sleeve can be fitted. Stainless steel, although apparently highly corrosion-resistant, is affected by some aggressive atmospheres if air is excluded; the resulting corrosion can be more severe than with mild steel.

The simplest and cheapest type of termination is a swaged Talurit Eye made round a thimble (Fig. 5.28(a)) and connected into a clevis type connection or on to the pin of a shackle. The neatest and most streamlined fitting is a swaged eye or jaw end termination (Fig. 5.28(b)). Hot-poured zinc terminations have to be used for very heavy cables of greater diameter than 50 mm (Fig. 5.28(c)). Epoxy

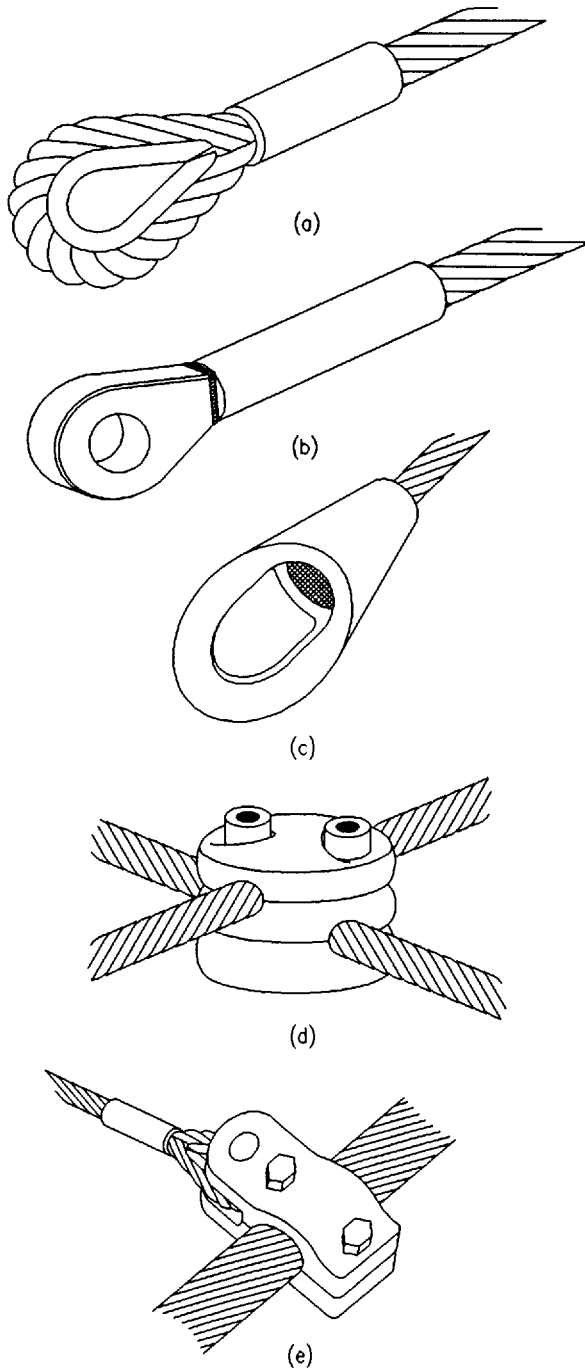


Fig. 5.28 Cable fittings: (a) swaged eye, (b) swaged terminator, (c) hot-poured white metal eye, (d) cross clamp, (e) net and boundary connection

resin with steel balls can be used as a filler in place of zinc, offering an improvement in fatigue life at the termination.

On-site connections can be made with bulldog clips but they are ugly and damage the rope. For cable net construction the standard detail is a three-part forged steel clamp, of which the two outer parts are identical (see Fig. 5.28(d)). Forging is expensive for small numbers and so for smaller structures machined aluminium components may be preferred. Double cables can have a swaged aluminium extrusion prefixed to each pair of cables which can then be connected with a single bolt. For the attachment of net cables to edge cables, forged steel clamps are generally used (Fig. 5.28(e)). Lower cost alternatives are bent plate or machined aluminium clamps.

Cable life is reduced by corrosion and fatigue. Galvanized cables under cover suffer very little corrosion; external cables properly protected should have a life of 50 years. Plastic sheathing has the great disadvantage of making inspection of the cable impossible.

Fatigue investigations have shown that it is wise to limit the maximum tension in a cable to 40% of its ultimate strength for long-life structures. For structures with a design life of up to ten years a limit of 50% is acceptable. Flexing of the cables at clamps or end termination will cause rapid fatigue damage.

### **5.3.3.2 Rods as tension members**

Steel rods are often used as tension members in external situations since they are stiffer and can be given better protection against corrosion. The rods are usually threaded at the ends and screwed into special end fittings. In the case of long rods which can be vibrated by the wind, the end connection must be free to move in two directions, otherwise fatigue damage will occur.

Since tension members are usually critical components of the structural system, consideration should be given to using rods or cables in pairs to provide additional safety.

## **5.4 Steel in housing**

### **5.4.1 Range of application**

Although lightweight steel construction has never had a large share of the UK housing market it has twice in this century expanded considerably to meet demand arising from housing and material shortages at the ends of the two World Wars. Steel houses built just after 1919 are still in occupation and post-1945 prefabs exist in some numbers, although originally intended to be only for short-



term use. Nevertheless, for a variety of reasons, interest in steel-framed housing has waned after the initial enthusiasm of the fruitful periods.

Steel frames have many advantages over other kinds of construction, some of which are:

- (1) They lead to rapid enclosure of the building. Frames can be erected in one day and it is feasible to get the roof waterproofed the following day. Trades can therefore begin interior work within a day or two of the start of building. In contrast the roof of a masonry house cannot be put up until the bricks and blocks have been laid layer by layer up to eaves level.
- (2) Because of (1) the total house-build time can be reduced by several weeks which means that the builder gets a quicker return on his capital.
- (3) They are dimensionally stable and are manufactured to tight geometric tolerances.

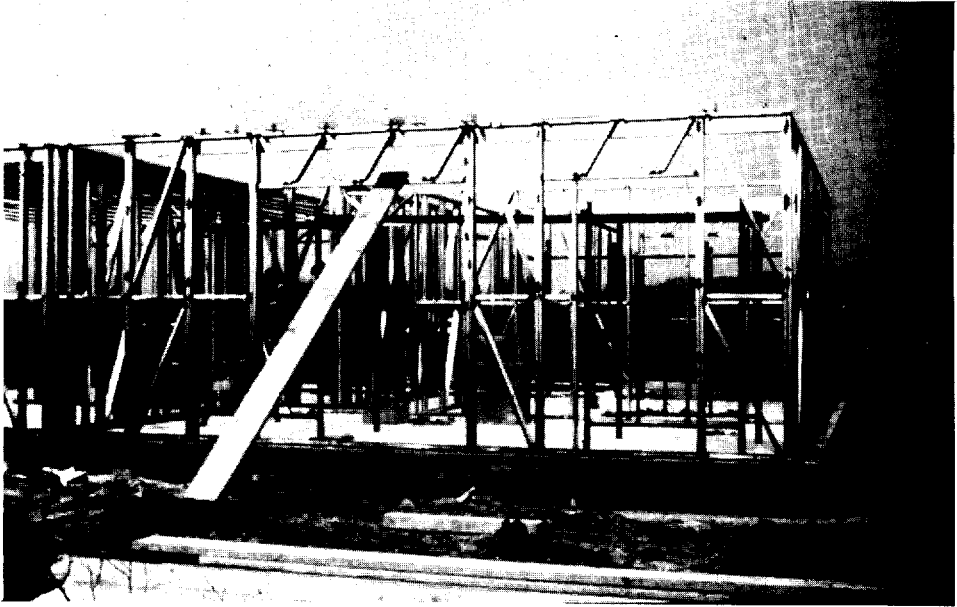
The obvious competitor in the framed house market is the timber-framed house which shares the same advantage of rapid construction. However timber is very much affected by dimensional changes caused by moisture, which have to be considered in detailing. In contrast steel does not shrink or creep; it is therefore possible to design the fabric more simply as allowance does not have to be made for dimensional change, other than for completely predictable deflections within the elastic limit. The lengthy maintenance period during which defects caused by movement and shrinkage are put right, inevitable in traditional housing, is not necessary for a steel-framed house.

#### **5.4.2 Current systems**

Most houses built today are for sale; the purchase is generally funded by mortgage. With few exceptions the mortgage making agencies (building societies, banks) will not fund new construction unless it has been approved by the National House Building Council (NHBC). The NHBC has not published design and construction codes for steel-framed houses. Any steel system has therefore to be assessed and approved by the British Board of Agrément (BBA).

The cost of approval is quite large, which acts as a deterrent to poorly thought out systems, but does to some extent restrict the number of entrants to the market. The quality control and restricted number are beneficial as they guarantee that future steel houses will not exhibit the weaknesses of some earlier systems. The major faults were corrosion of the frame and internal condensation, the latter often the cause of the former. Proper protective coating of the steel and adequate thermal insulation external to the frame are now seen to be essential.

Figure 5.29 shows a modern steel-framed house under construction and Fig. 5.30 shows the attractive overall appearance that can be achieved.



*Fig. 5.29* Frame during construction



*Fig. 5.30* Completed house

### 5.4.3 Other uses of steel in housing

Development programmes are in hand for the following:

- (1) soffits, fascias and bargeboards
- (2) suspended ground floors
- (3) door frames and doors
- (4) window sills and surrounds
- (5) window frames
- (6) infill panels
- (7) insulation systems
- (8) roofing systems.

The steel-framed housing systems of the past and present are, in many ways, substitutes for timber frames and so do not exploit the properties of steel to the full. Studies are in hand to examine the possibilities of a panel-based building system.

## 5.5 Atria

### 5.5.1 Introduction

#### 5.5.1.1 General

Structural engineers, architects, environmental and fire safety engineers all have a significant contribution to make when planning the concept and subsequent detail of intermediate spaces such as atria, arcades, malls and covered courtyards. It is important that all disciplines take a wide view and understand the total problem to ensure a balanced design consistent with all of the technical criteria, without compromising the fundamental requirements of providing an agreeable, comfortable and safe environment.

A number of criteria affect the design:

- (1) The enclosure to be readily maintained
- (2) Environmental design to minimize or eliminate major mechanical plant and hence servicing
- (3) The safety of potentially large numbers of the public
- (4) Fire safety
- (5) Erection of structure and cladding
- (6) Internal and external cleaning.

It may not be essential to design for minimum cost since the result must reflect the visual requirements of the enclosure elegantly, economically and in a form which

is readily constructed. Nevertheless it is important to understand the philosophy behind the funding of the enclosure in developing designs which can be radically different if the improvement of the surrounding accommodation is the aim rather than the provision of additional accommodation. If for example an atrium deck is simply a space with no direct revenue-earning capacity, its cost must be offset by the enhancement of the value of the surrounding accommodation.

### 5.5.1.2 Structural aspects

The structures in Figs 5.31 to 5.35 are very simple in concept, but effectively illustrate a series of solutions in which there is a generally decreasing reliance on the perimeter structure.

As a group the arch, the beam and the dome are potentially the most economic solutions, but rely totally on the support provided by the perimeter structure. This is simple for a new development, which can be designed relatively easily to support the resultant vertical and horizontal loads, but for existing buildings it may not be so straightforward, since strengthening works or evidence that increased loads can be supported will be required. In the case of an existing building, unless considerable party wall structures are available for support, it may be easier to set the roof at a lower level where the percentage increase in vertical load will be

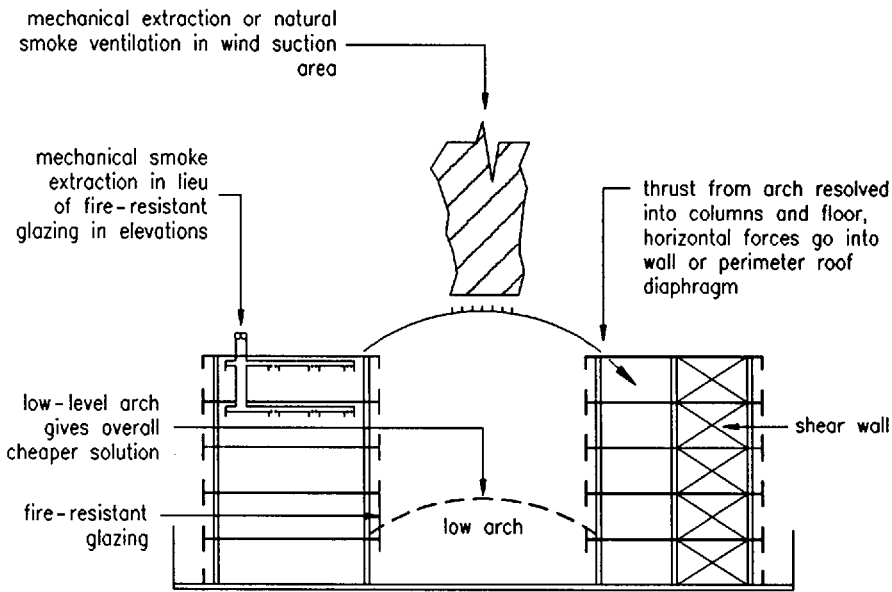


Fig. 5.31 Arch

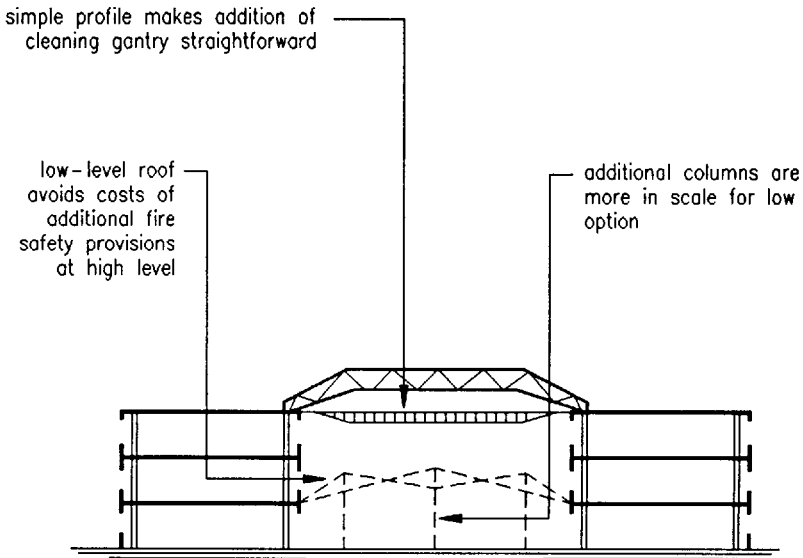


Fig. 5.32 Beam or truss

much smaller or where horizontal thrusts from an arch will have a smaller resultant overturning effect.

As our town centres and streets are redeveloped to compete with out-of-town shopping the need for enclosure is a common solution often considered. In these cases, it is often not practical to gain support from a wide variety of constructions

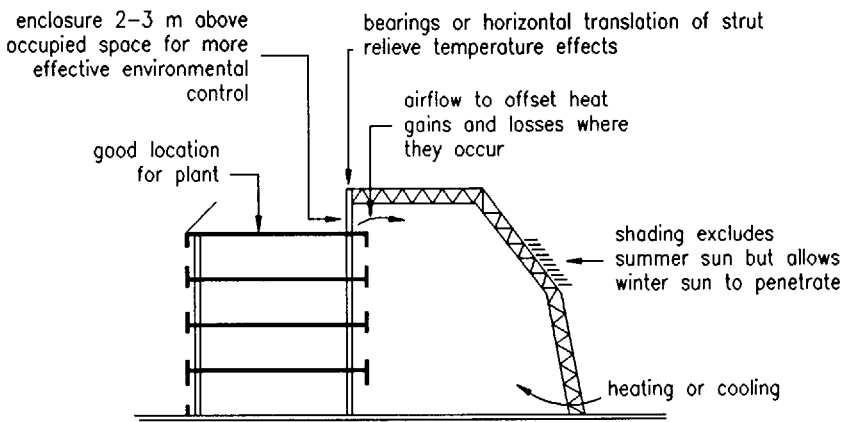


Fig. 5.33 Half portal

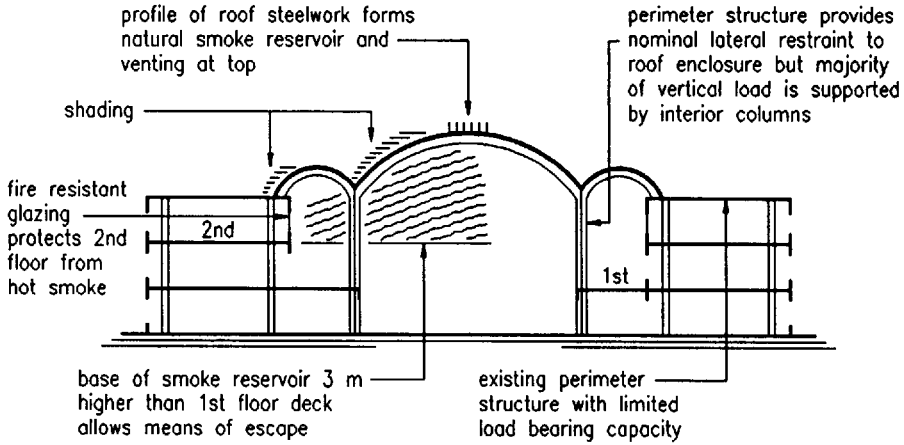


Fig. 5.34 Beam and column

of various heights and condition and therefore the solutions defined in Fig. 5.34 are more appropriate. The perimeter structure is required to support a small proportion of the vertical load and relatively small horizontal loads from wind and stabilizing forces for the new columns, which does not generally pose a problem

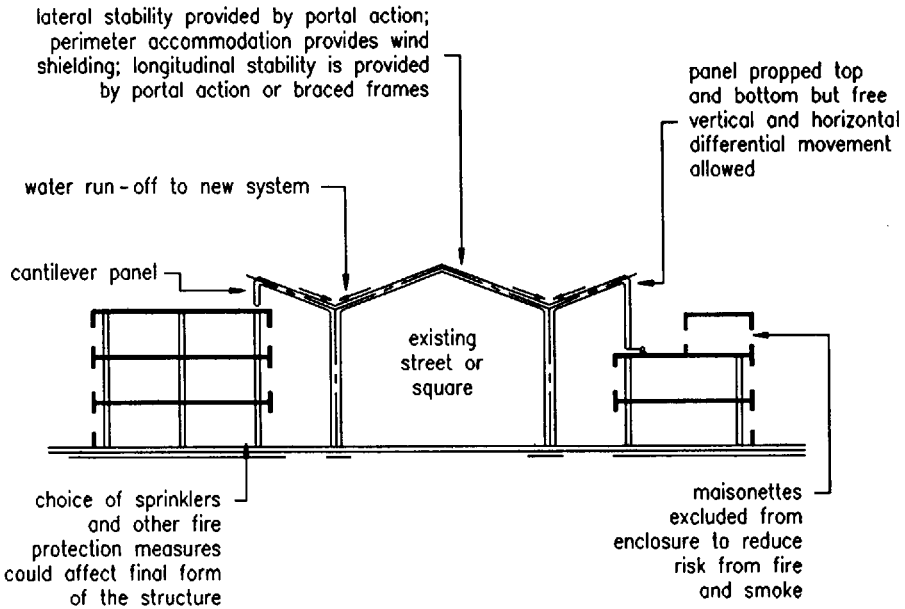
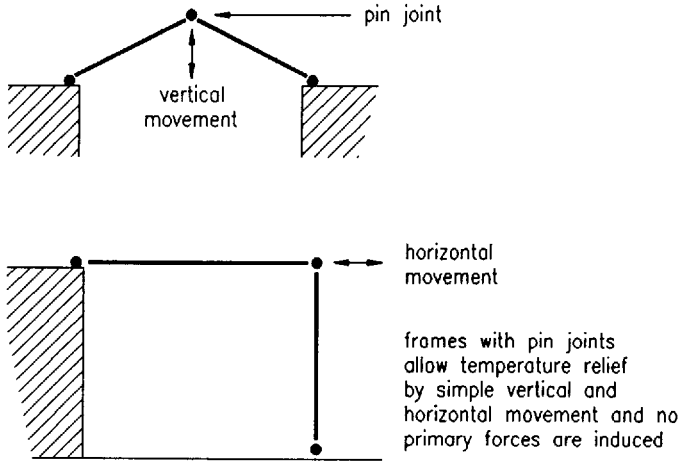
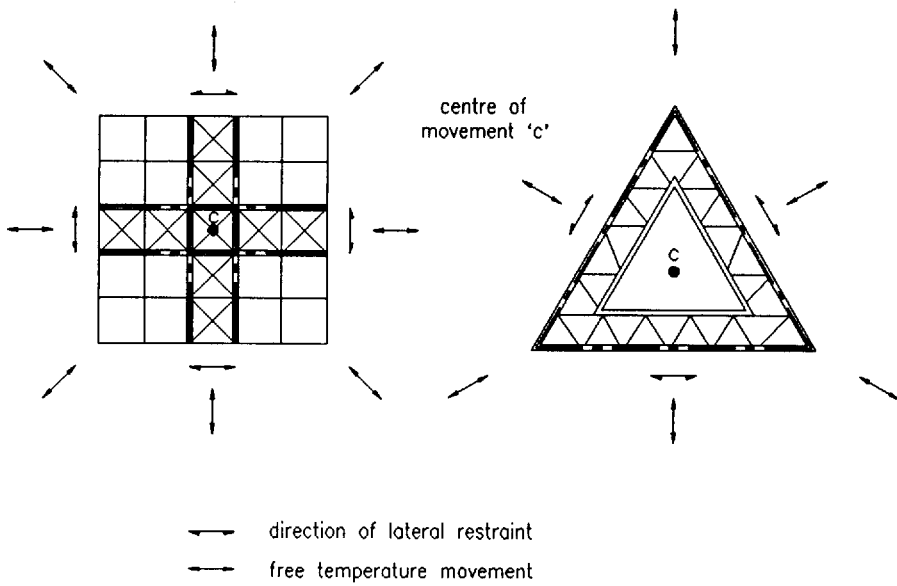


Fig. 5.35 Portal frame



(a)



(b)

Fig. 5.36 Movements caused by temperature changes

since there is usually some redundant horizontal capacity due to the wind-shielding effect of the new enclosure. The portal style solution Fig. 5.35 is substantially self-supporting, and is therefore likely to be expensive compared to the arch or beam solution but may be the only satisfactory option when an existing street is to be covered.

The provision of restraint for stability or to resist wind loads needs careful study since this restraint can be incompatible with the need to allow movement of the steelwork caused by large temperature differentials. Temperatures in the steel could be 30°C higher in black painted steel compared to white if unshaded and directly exposed to the sun's radiation and also depend on the extent of ventilation provisions. One approach is to allow the movement to take place without inducing temperature stress (Fig. 5.36(a)). Alternatively, lateral restraints can be arranged to allow the roof to expand freely about centre of movement yet provide adequate support (Fig. 5.36(b)).

### ***5.5.1.3 Form of members and connections***

The shape and connections of the individual structural members which form the basic framework can be a significant contributory feature to an enclosure and are also an important aspect of the architectural treatment. This framework will be required to perform a range of functions over and above the need to span and carry the primary loads. Ideally, the modulation of the primary and secondary structure should be organized to support glazing/cleaning gantries, walkways, lighting, as well as shading and other equipment, without the provision of layers of additional structure which would obscure a well-designed primary framework.

It is desirable that the design of these 'clip-on' items should be under the direct control and co-ordination of the overall fabrication drawing process is essential to some extent if the design of individual items passes on to sub-contractors. Careful control and co-ordination to the overall fabrication drawing process is essential to avoid unnecessary visual distractions.

Methods of jointing steelwork to meet the structural, architectural and aesthetic requirements are numerous. Their development requires a degree of creativity, which can be improved by a study of the actual projects, the technical journals and the architectural press.

### ***5.5.1.4 Paint systems***

The paint system is an important factor in the visual quality of the structure. The choice of a paint system is always difficult due to a number of conflicting requirements. Paint technology provides an ever-increasing number of options. However, the choice can be guided by consideration of the following criteria:



- (1) the steelwork fabricator who delivers and erects the steel will inevitably damage any paint applied at the works no matter how carefully the protection measures are prepared
- (2) a contractor who has a very tight programme may like to see primer, undercoat and finish coat on the steelwork applied at the works since it may be very difficult to apply the finish on high-level steelwork without extensive temporary works
- (3) very hard paint finishes are more difficult to damage although when the inevitable damage occurs they are usually more difficult to repair to a good standard
- (4) if the finish-coat is applied on site, some parts of the steelwork may be difficult to reach and the standard of finish will not be as good as that achieved in the paint shop
- (5) unless touching up to damaged areas is very minor, the result is unlikely to be satisfactory and therefore a full site applied decorative finish may prove necessary
- (6) the choice of system will also depend on the fabricator's paint shop and its relationship with the paint supplier.

## 5.5.2 Special features

### 5.5.2.1 Fire engineering

The addition of a roof to enclose a number of levels linked by a central void through which fire and smoke can spread is alien to traditional fire safety regulations and therefore each case requires careful and individual attention if a safe solution is to be achieved. The Building Regulations are not directly applicable, there are no current British Standards and therefore reliance is placed on research papers and the practical experience of the designers and controlling officers to determine a safe solution.

The considerations for fire safety can influence the structure in two ways:

- (1) the effect of fire on the structure itself must be considered by reviewing the risk and extent of failure and the resultant consequences of that failure
- (2) the fire engineering requirements on the surrounding accommodation can influence the level and form of an enclosure or alternatively the shape can be affected if there is a requirement for smoke control.

It takes considerable build-up of heat or a weak local condition to cause failure of an unprotected atrium roof structure during a fire and therefore the risk of failure is low. However, even though the Building Regulations do not require a roof to have fire-resistance, it is sensible to review each case to limit the risks and consequences of failure. No definitive standard has been set for the required

performance of such a roof although a supporting strategy for the provision of an unprotected roof structure can be prepared from the following set of recommendations.

- (1) For small enclosed areas everyone within the space is likely to be fully aware of a fire and be able to escape accordingly. The complexity of the planning and the means of escape influence this decision. However, 2000 m<sup>2</sup> is suggested as a preliminary maximum for the application of this principle, although variations could be expected depending on the complexity of the space.
- (2) Smoke control schemes and the failure of the glazing can prevent a general build-up of heat and inhibit global failure of the structure.
- (3) Direct flame impingement on the structure from a fire on the atrium deck or high-level perimeter accommodation can be limited by the provision of sprinklers which reduce the risk of spread of fire. Alternatively fire-resistant construction or glazing can be used to isolate the steel from the fire.
- (4) Provide a structure for which local failure will not cause collapse of the whole.
- (5) If it is felt necessary, due to exceptionally large fire loads, and very large numbers of people at risk, it is possible to assess the fire-resistance of unprotected steelwork by analytical techniques.

The fire engineering design can also influence the height and shape of the roof enclosure when the interaction of fire protection measures for the enclosure and surrounding accommodation are considered. For every level attached to the enclosure there is a direct cost which can be directly attributed to fire safety provisions such as ductwork, fans, louvres, fire-resistant glazing, detection and control systems. It would be cheaper and safer to exclude residential accommodation from the enclosure whereas it may be desirable to enclose multi-level shopping facilities thus providing a high profile to form a smoke reservoir for venting to allow safe means of escape.

#### ***5.5.2.2 The influence of environmental engineering***

The provision of intermediate space as an extra attraction with earning power requires that the building physics be considered and an appropriate environment achieved. At the simplest level the enclosure may only provide protection from the rain or at the other extreme may be fully conditioned to performance criteria similar to those of the surrounding accommodation. However, it is in the intermediate environment, somewhere between indoors and outdoors, commonly called a buffer zone, that the total engineering technology starts to interface with the fire and structural design of the enclosure.

The height and form of the roof, and the arrangement of shading, will influence the solar heat gains and the cooling effect of the natural ventilation and consequently the risk of condensation affecting the atrium floor. Internal shading or

walkway shading systems are easier to maintain but are not as effective as the more expensive external shading systems.

The natural light and the acoustic performance also contribute to a stimulating and fresh environment. The complexity of the permutations of how for example natural ventilation can be influenced by the smoke ventilation, which in turn affects the structural form, ensures that every design is different. Similarly, the thermal physics design may indicate that structural fabrics which generally allow a larger structural modulation (e.g. PVC-coated polyester, PTFE-coated fibreglass, ET foil) meet the performance specification most suitably, although care must be taken to ensure that the fire performance of these fabrics is satisfactory.

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# Chapter 6

## Applied metallurgy of steel

by MICHAEL BURDEKIN

### 6.1 Introduction

The versatility of steel for structural applications rests on the fact that it can be readily supplied at a relatively cheap price in a wide range of different product forms, and with a useful range of material properties. The key to understanding the versatility of steel lies in its basic metallurgical behaviour. Steel is an efficient material for structural purposes because of its good strength-to-weight ratio. A diagram of strength-to-weight ratio against cost per unit weight for various structural materials is shown in Fig. 6.1. Steel can be supplied with strength levels from about  $250 \text{ N/mm}^2$  up to about  $2000 \text{ N/mm}^2$  for common structural applications,

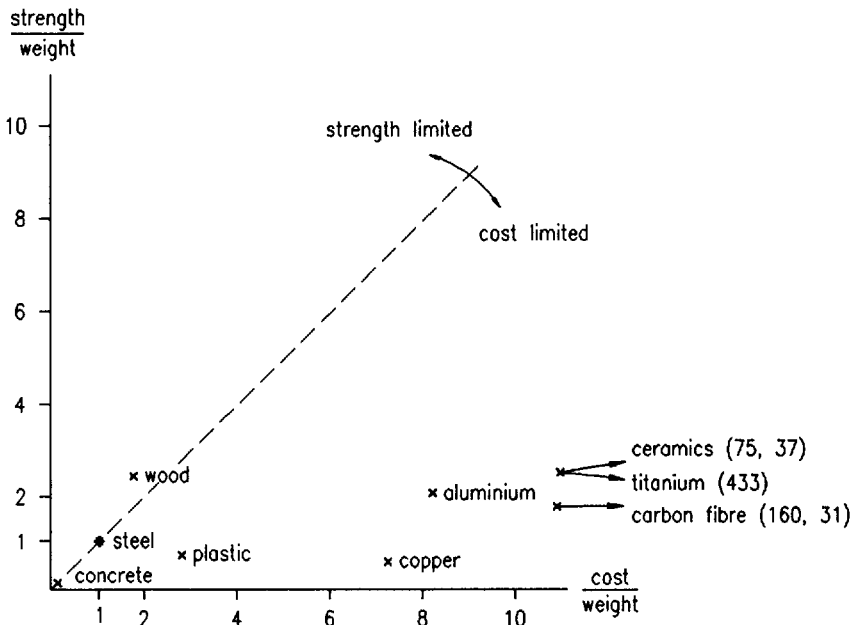


Fig. 6.1 Strength/weight and cost/weight ratios for different materials normalized to steel (1,1)

although the strength requirements may limit the product form. The material is normally ductile with good fracture toughness for most practical applications. Product forms range from thin sheet material, through optimized structural sections and plates, to heavy forgings and castings of intricate shape. Although steel can be made to a wide range of strengths it generally behaves as an elastic material with a high (and relatively constant) value of the elastic modulus up to the yield or proof strength. It also usually has a high capacity for accepting plastic deformation beyond the yield strength, which is valuable for drawing and forming of different products, as well as for general ductility in structural applications.

Steel derives its mechanical properties from a combination of *chemical composition*, *heat treatment* and *manufacturing processes*. While the major constituent of steel is always iron the addition of very small quantities of other elements can have a marked effect upon the type and properties of steel. These elements also produce a different response when the material is subjected to heat treatments involving cooling at a prescribed rate from a particular peak temperature. The manufacturing process may involve combinations of heat treatment and mechanical working which are of critical importance in understanding the subsequent performance of steels and what can be done satisfactorily with the material after the basic manufacturing process.

Although steel is such an attractive material for many different applications, two particular problems which must be given careful attention are those of corrosion behaviour and fire resistance, which are dealt with in detail in Chapters 35 and 34 respectively. Corrosion performance can be significantly changed by choice of a steel of appropriate chemical composition and heat treatment, as well as by corrosion protection measures. Although normal structural steels retain their strength at temperatures up to about 300°C, there is a progressive loss of strength above this temperature so that in an intense fire, bare steel may lose the major part of its structural strength. Although the hot strength and creep strength of steels at high temperature can be improved by special chemical formulation, it is usually cheaper to provide fire protection for normal structural steels by protective cladding.

## **6.2 Chemical composition**

### **6.2.1 General**

The key to understanding the effects of chemical composition and heat treatment on the metallurgy and properties of steels is to recognize that the properties depend upon the following factors:

- (1) microstructure
- (2) grain size

- (3) non-metallic inclusions
- (4) precipitates within grains or at grain boundaries
- (5) the presence of absorbed or dissolved gases.

Steel is basically iron with the addition of small amounts of carbon up to a maximum of 1.67% by weight, and other elements added to provide particular mechanical properties. Above 1.67% carbon the material generally takes the form of cast iron. As the carbon level is increased, the effect is to raise the strength level, but reduce the ductility and make the material more sensitive to heat treatment. The cheapest and simplest form is therefore a plain carbon steel commonly supplied for the steel reinforcement in reinforced concrete structures, for wire ropes, for some general engineering applications in the form of bars or rods, and for some sheet/strip applications. However, plain carbon steels at medium to high carbon levels give rise to problems where subsequent fabrication/manufacturing takes place, particularly where welding is involved, and more versatility can be obtained by keeping carbon to a relatively low level and adding other elements in small amounts. When combined with appropriate heat treatments, addition of these other elements produces higher strength while retaining good ductility, fracture toughness, and weldability, or the development of improved hot strength, or improved corrosion-resistance. The retention of good fracture toughness with increased strength is particularly important for thick sections, and for service applications at low temperatures where brittle fracture may be a problem. Hot strength is important for service applications at high temperatures such as pressure vessels and piping in the power generation and chemical process plant industries. Corrosion-resistance is important for any structures exposed to the environment, particularly for structures immersed in sea water. Weathering grades of steel are designed to develop a tight adherent oxide layer which slows down and stifles continuing corrosion under normal atmospheric exposure of alternate wet and dry conditions. Stainless steels are designed to have a protective oxide surface layer which re-forms if any damage takes place to the surface, and these steels are therefore designed not to corrode under oxidizing conditions. Stainless steels find particular application in the chemical industry.

### 6.2.2 Added elements

The addition of small amounts of carbon to iron increases the strength and the sensitivity to heat treatment (or hardenability, see later). Other elements which also affect strength and hardenability, although to a much lesser extent than carbon, are *manganese*, *chromium*, *molybdenum*, *nickel* and *copper*. Their effect is principally on the microstructure of the steel, enabling the required strength to be obtained for given heat treatment/manufacturing conditions, while keeping the carbon level very low. Refinement of the grain structure of steels leads to an

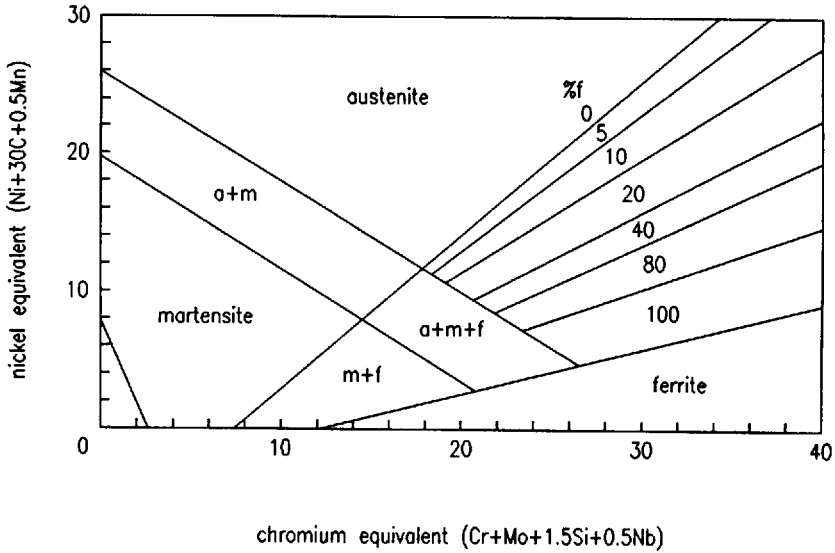


Fig. 6.2 Constitution (Schaeffler) diagram for stainless steels

increase in yield strength and improved fracture toughness and ductility at the same time, and this is therefore an important route for obtaining enhanced properties in steels. Although heat treatment and in particular cooling rate are key factors in obtaining grain refinement, the presence of one or more elements which promote grain refinement by aiding the nucleation of new grains during cooling is also extremely beneficial. Elements which promote grain refinement, and which may be added in small quantities up to about 0.050%, are *niobium*, *vanadium* and *aluminium*.

The major elements which may be added for hot strength and also for corrosion-resistance are chromium, nickel and molybdenum. Chromium is particularly beneficial in promoting corrosion-resistance as it forms a chromium oxide surface layer on the steel which is the basis of stainless steel corrosion protection in oxidizing environments. When chromium and nickel are added in substantial quantities with chromium levels in the range 12% to 25%, and nickel content up to 20%, different types of stainless steel can be made. As with the basic effect of carbon in the iron matrix, certain other elements can have a similar effect to chromium or nickel but on a lesser scale. From the point of view of the effects of chemical composition, the type of stainless steel formed by different combinations of chromium and nickel can be shown on the Schaeffler diagram in Fig. 6.2. The three basic alternative types of stainless steel are ferritic, austenitic and martensitic stainless steels, which have different inherent lattice crystal structures and microstructures, and hence may show significantly different performance characteristics.



### 6.2.3 Non-metallic inclusions

The presence of non-metallic inclusions has to be carefully controlled for particular applications. Such inclusions arise as a residue from the ore in the steelmaking process, and special steps have to be taken to reduce them to the required level. The commonest impurities are *sulphur* and *phosphorus*, high levels of which lead to reduced resistance to ductile fracture and the possibility of cracking problems in welded joints. For weldable steels the sulphur and phosphorus levels must be kept less than 0.050%, and with modern steel-making practice should now preferably be less than 0.010%. They are not always harmful however and in cases where welding or fracture toughness are not important, deliberate additions of sulphur may be made up to about 0.15% to promote free machining qualities of steel, and small additions of phosphorus may be added to non-weldable weathering grade steels. Other elements which may occur as impurities and may sometimes have serious detrimental effects in steels are *tin*, *antimony* and *arsenic* which in certain steels may promote a problem known as temper embrittlement, in which the elements migrate to grain boundaries if the steel is held in a temperature range between about 500°C and 600°C for any length of time. At normal temperature steels in this condition can have very poor fracture toughness, with failure occurring by inter-granular fracture. It is particularly important to ensure that this group of *tramp elements* is eliminated from low alloy steels.

Steels with a high level of dissolved gases, particularly oxygen and nitrogen, can behave in a brittle manner. The level of dissolved gases can be controlled by addition of small amounts of elements with a particular affinity for them so that the element combines with the gas and either floats out in the liquid steel at high temperature or remains as a distribution of solid non-metallic inclusions. A steel with no such additions to control oxygen level is known as a *rimming steel*, but for most structural applications the elements *silicon* and/or *aluminium* are added as deoxidants. Aluminium also helps in controlling the free nitrogen level which it is important to keep to low levels in cases where the phenomenon of strain ageing embrittlement may be important.

## 6.3 Heat treatment

### 6.3.1 Effect on microstructure and grain size

During the manufacture of steel the required chemical composition is achieved while it is in the liquid state at high temperature. As the steel cools, it solidifies at the melting temperature at about 1350°C, but substantial changes in structure take place during subsequent cooling and may also be affected by further heat treatments. If the steel is cooled slowly, it is able to take up the equilibrium type of lattice crystal structure and microstructure appropriate to the temperature and chemical composition.

These conditions can be summarized on a phase or equilibrium diagram for the particular composition; the equilibrium diagram for the iron–iron carbide system is shown in Fig. 6.3. Essentially this is a diagram of temperature against percentage of carbon by weight in the iron matrix. At 6.67% carbon, an inter-metallic compound called *cementite* is formed which is an extremely hard and brittle material. At the left-hand end of the diagram, with very low carbon contents, the equilibrium structure at room temperature is *ferrite*. At carbon contents between these limits the equilibrium structure is a mixture of ferrite and cementite in proportion depending on the carbon level. On cooling from the melting temperature, at low carbon levels a phase known as *delta ferrite* is formed first, which then transforms to a different phase called *austenite*. At higher carbon levels, the melting temperature drops with increasing carbon level and the initial transformation may be direct to austenite. The austenite phase has a face-centred cubic lattice crystal structure which is maintained down to the lines AE and BE on Fig. 6.3. As cooling proceeds slowly the austenite then starts to transform to the mixture of ferrite and cementite which results at room temperature. However point E on the diagram represents a eutectoid at a composition of 0.83% carbon at which ferrite

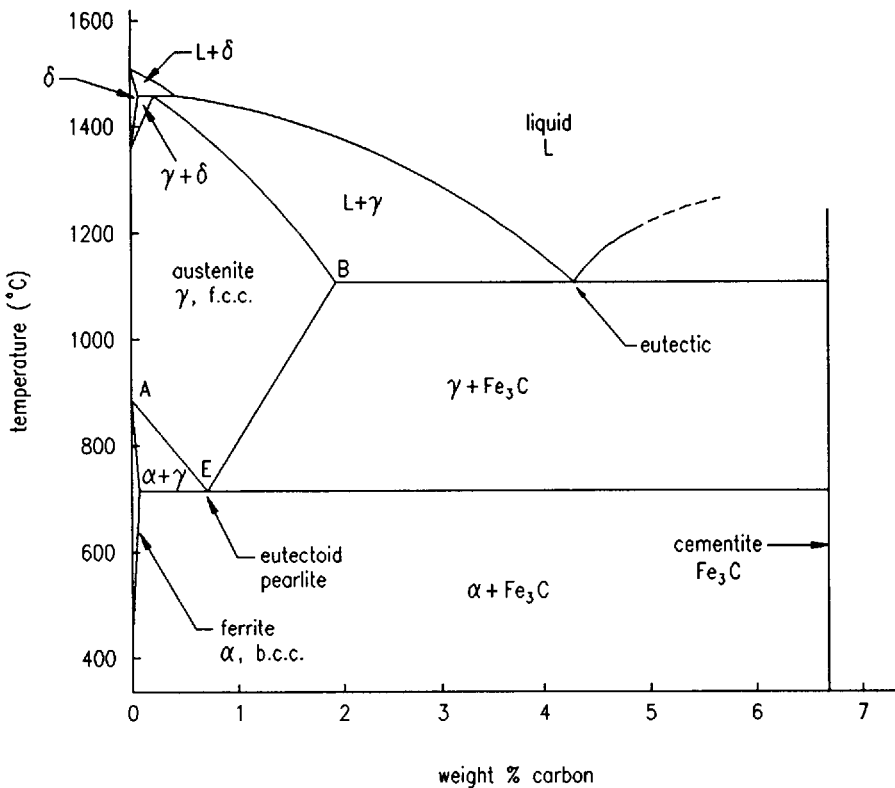


Fig. 6.3 Equilibrium phase diagram for iron – iron carbide system (f.c.c. face-centred cubic; b.c.c. body-centred cubic)

and cementite precipitate alternately in thin laths to form a structure known as *pearlite*. At compositions less than 0.83% carbon, the type of microstructure formed on slow cooling transformation from austenite is a mixture of ferrite and pearlite. Each type of phase present at its appropriate temperature has its own grain size, and the ferrite/pearlite grains tend to precipitate in a network within and based on the previous austenite grain boundary structure. The lattice crystal structure of the ferrite material which forms the basic matrix is essentially a body-centred cubic structure. Thus in cooling from the liquid condition, complex changes in both lattice crystal structure and microstructure take place dependent on the chemical composition. For the equilibrium diagram conditions to be observed, cooling must be sufficiently slow to allow time for the transformations in crystal structure and for the diffusion/migration of carbon to take place to form the appropriate microstructures.

If a steel is cooled from a high temperature and held at a lower constant temperature for sufficient time, different conditions may result; these are represented on a diagram known as the *isothermal transformation diagram*. The form of the diagram depends on the chemical analysis and in particular on the carbon or related element content. In plain carbon steels the isothermal transformation diagram typically has the shape of two letters C each with a horizontal bottom line as shown in Fig. 6.4. The left-hand/upper curve on the diagram of temperature against time represents the start of transformation, and the right-hand/lower curve represents the completion of transformation with time. For steels with a carbon content below the eutectoid composition of 0.83% carbon, holding at a temperature to produce isothermal transformation through the top half of the letter C, leads to the formation of a ferrite/pearlite microstructure. If the transformation temperature is lowered to pass through the lower part of the C curves, but above the bottom horizontal lines, a new type of microstructure is obtained, which is called *bainite*, which is somewhat harder and stronger than pearlite, but also tends to have poorer fracture toughness. If the transformation temperature is dropped further to lie below the two horizontal lines, transformation takes place to a very hard and brittle substance called *martensite*. In this case the face-centred cubic lattice crystal structure of the austenite is not able to transform to the body-centred cubic crystal structure of the ferrite, and the crystal structure becomes locked into a distorted form known as a body-centred tetragonal lattice. Bainite and martensite do not form on equilibrium cooling but result from quenching to give insufficient time for the equilibrium transformations to take place.

The position and shape of the C curves on the time axis depend on the chemical composition of the steel. Higher carbon contents move the C curve to the right on the time axis, making the formation of martensite possible at slower cooling rates. Alloying elements change the shape of the C curves and an example for a low-alloy steel is shown in Fig. 6.5. Additional effects on microstructure, grain size and resultant properties can be obtained by combinations of mechanical work at appropriate temperatures during manufacture of the basic steel.

In addition to the effect of cooling rate on microstructure, the grain size is significantly affected by time at high temperatures and subsequent cooling rate.

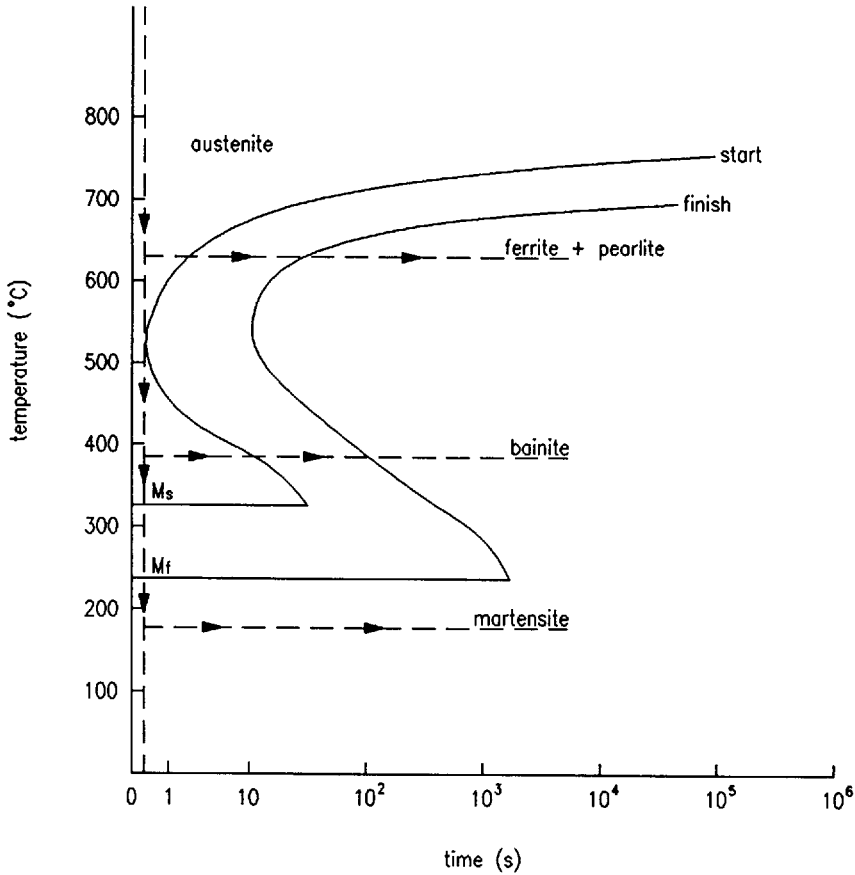


Fig. 6.4 Isothermal transformation diagram for 0.2% C, 0.9% Mn steel

Long periods of time at higher temperatures within a particular phase lead to the merging of the grain boundaries and growth of larger grains. For ferritic crystal structures, grain growth starts at temperatures above about 600°C and hence long periods in the temperature range 600°C to 850°C with slow cooling will tend to promote coarse grain size ferrite/pearlite microstructures. Faster cooling through the upper part of the C curves will give a finer grain structure but still of ferrite/pearlite microstructure.

The type of microstructure present in a steel can be shown and examined by the preparation of carefully polished and etched samples viewed through a microscope. Etching with particular types of reagent attacks different parts of the microstructure preferentially and the etched parts are characteristic of the type of microstructure. Examples of some of the more common types of microstructure mentioned above are shown in Fig. 6.6. The basic microstructure of the steel is usually shown by examination in the microscope to magnifications of from 100 to about 500 times.

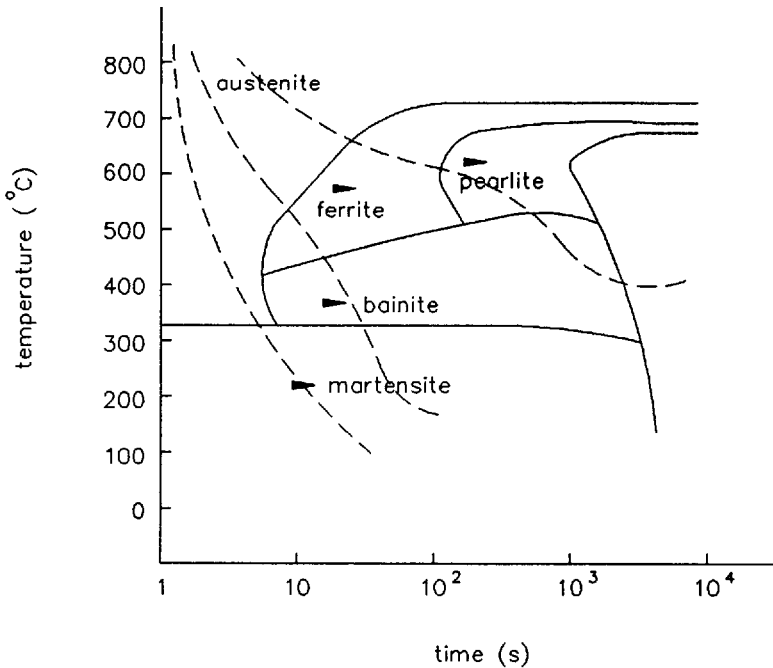


Fig. 6.5 Continuous cooling transformation diagram for 0.4% C, 0.8% Mn, 1% Cr, 0.2% Mo steel

Where it is necessary to examine the effects of very fine precipitates or grain boundary effects, it may be necessary to go to higher magnifications. With the electron microscope it is possible to reach magnifications of many thousands and, with specialized techniques, to reach the stage of seeing dislocations and imperfections in the crystal lattice itself.

### 6.3.2 Heat treatment in practice

In practical steelmaking or fabrication procedures cooling occurs continuously from high temperatures to lower temperatures. The response of the steel to this form of cooling can be shown on the continuous cooling transformation diagram (CCT diagram) of Fig. 6.7. This resembles the isothermal transformation diagram, but the effect of cooling rate can be shown by lines of different slopes on the diagram. For example, slow cooling, following line (a) on Fig. 6.7 passes through the top part of the C curve and leads to the formation of a ferrite/pearlite mixture. Cooling at an intermediate rate, following line (b), passes through pearlite/ferrite transformation at higher temperatures, but changes to bainite

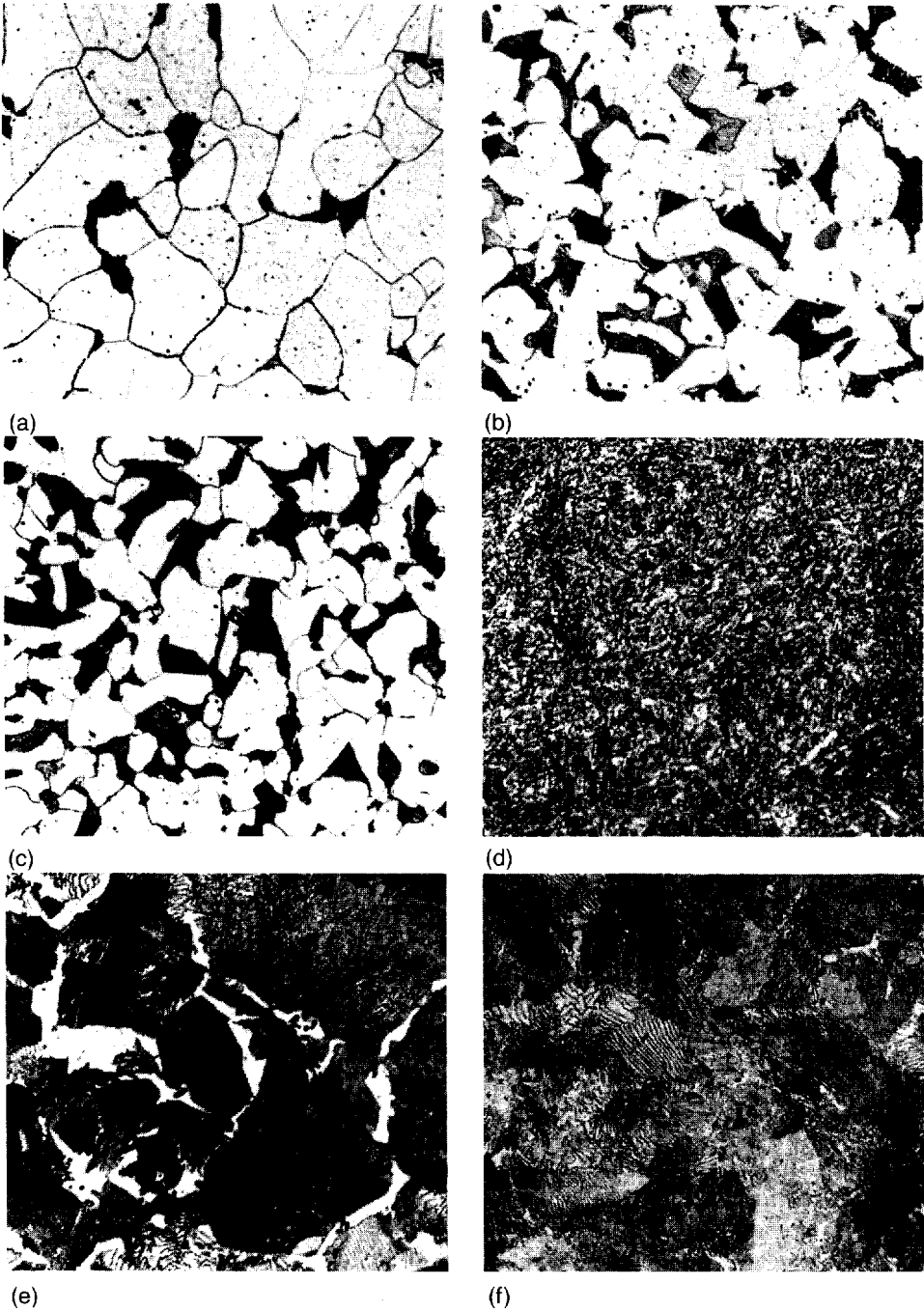


Fig. 6.6 Examples of common types of microstructure in steel (magnification  $\times 500$ ) (courtesy of Manchester Materials Science Centre, UMIST)

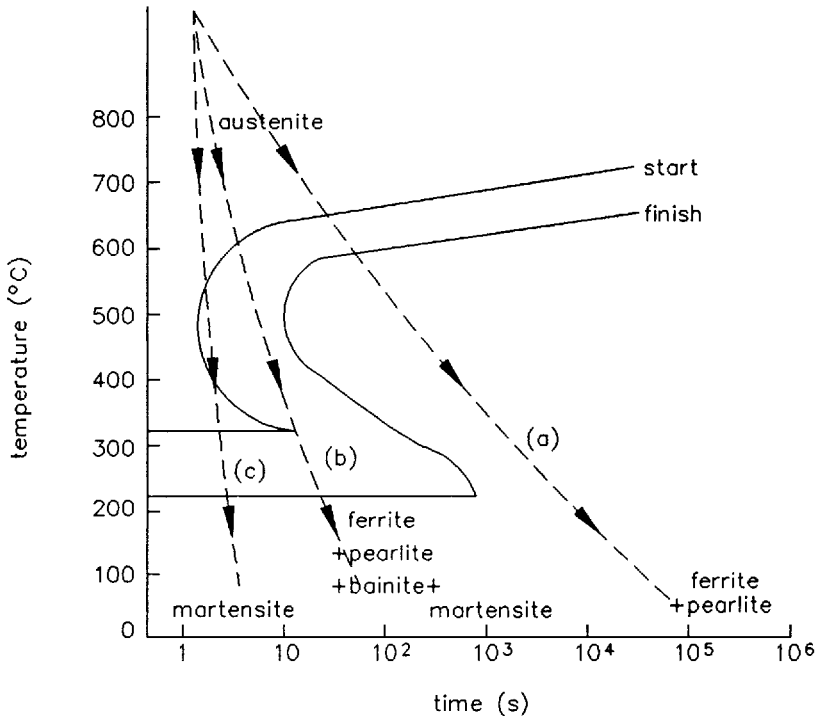


Fig. 6.7 Continuous cooling transformation diagram for 0.2% C, 0.9% Mn steel

transformation at lower temperatures so that a mixture of pearlite and bainite results. Rapid cooling following line (c) misses the C curves completely and passes through the two horizontal lines to show transformation to martensite. Thus in practice for any given composition of steel different microstructures and resultant properties can be produced by varying the cooling rate.

The microstructure and properties of a steel can be changed by carefully chosen heat treatments after the original manufacture of the basic product form. A major group of heat treatments is effected by heating the steel to a temperature such that it transforms back to austenite, this temperature being normally in the range 850°C to 950°C. It is important to ensure that the temperature is sufficient for full transformation to austenite, otherwise a very coarse-grained ferritic structure may result. It is also important that the austenitizing temperature is not too high, and that the time at this temperature is not too long otherwise a coarse-grained austenite structure will form, making subsequent transformation to fine grains more difficult. A heat treatment in which cooling is slow and essentially carried out in a furnace is known as *annealing*. This tends to lead to a relatively coarse-grained final structure, as predicted by the basic equilibrium phase diagram and is used to put materials into their softest condition. If the steel is allowed to cool

freely in air from the austenitizing temperature, the heat treatment is known as *normalizing* which gives a finer grain size and hence tends to higher yield strength and better toughness for a given composition of steel. Normalizing may be combined with rolling of a particular product form over a relatively narrow band of temperatures, followed by natural cooling in air, in which case it is known as *controlled rolling*. When the steel product form is cooled more rapidly by immersing it directly into oil or water, the heat treatment is known as *quenching*. Quenching into a water bath is generally more severe than quenching into an oil bath.

A second stage heat treatment to temperatures below the austenitizing range is frequently applied, known as *tempering*. This has the effect of giving more time for the transformation processes which were previously curtailed to develop further, and can permit changes in the precipitation of carbides allowing them to merge together and develop into larger or spheroidal forms. These thermally activated events are highly dependent on temperature and time for particular compositions. The net effect of tempering is to soften previously hardened structures and make them tougher and more ductile.

Both plain carbon and low alloy steels can be supplied in the quenched and tempered condition for plates and engineering sections to particular specifications. The term 'hardenability' is used to describe the ability of steel to form martensite to greater depths from the surface, or greater section sizes. There are, therefore, practical limits of section thickness or size at which particular properties can be obtained.

In BS 970 a range of compositions of engineering steels is given, together with the choice of heat treatments and limiting section sizes for which different properties can be supplied. The heat treatment condition is represented by a letter in the range P to Z. The more commonly supplied conditions are in the range P to T. It should be noted that the term 'hardenability' does not refer to the absolute hardness level which can be achieved, but to the ability to develop uniform hardening throughout the cross section. Cooling rates vary at different positions in the cross section as heat is conducted away in a quenching operation from the surface. Examples are given in the Appendix *Physical chemical and mechanical properties of steel* of some of the more common compositions and heat treatment conditions of general engineering steels in BS 970.

It is sometimes necessary to apply heat treatment to components or structures after fabrication, particularly when they have been welded. The aim is mainly to relieve residual stresses but heat treatment may also be required to produce controlled metallurgical changes in the regions where undesirable effects of welding have occurred. Applications at high temperatures may also lead to metallurgical changes taking place in service. It is vitally important that where any form of heat treatment is applied the possible metallurgical effects on the particular type of steel are taken into account.

Heat treatments are sometimes applied to produce controlled changes in shape or correction of distortion and again temperatures and times involved in these heat treatments must be carefully chosen and controlled for the particular type of steel being used.



## 6.4 Manufacture and effect on properties

### 6.4.1 Steelmaking

Manufacture of steel takes place mainly in massive integrated steelworks. The first stage starts with iron ore and coke which are mixed and heated to produce a sinter. This mixture then has limestone added to form the burden or raw material fed into a blast furnace. Reactions which take place at high temperature in the blast furnace lead to the formation of iron; the molten iron is tapped continuously from the bottom of the blast furnace. The molten metal at this stage is approximately 90% to 95% iron, the remainder being impurities which have to be removed or reduced to acceptable levels at the next stage, that of steelmaking. This material is fed together with recovered scrap iron or steel into the steelmaking furnace, the common types of which are known as either a basic oxygen furnace or an electric arc furnace. In the basic oxygen furnace oxygen is blown on to the molten metal by a water-cooled lance. In the electric arc furnace heat is produced by an arc between electrodes over the metal surface and the molten metal itself conducting electricity. Chemical reactions take place following additions of selected materials to the molten metal, which lead to the reduction of the impurities and to the achievement of the required controlled chemical composition of the steel. The impurities are reduced by addition of elements which combine and float out to the surface of the molten metal in the slag or dross waste material on the surface. Deoxidation or killing of the steel takes place in the final stages before the furnace is tapped. Older steel manufacturing practice was to tap the steel from the furnace into ladles and then pour the molten steel into large moulds to produce ingots. These ingots would normally be allowed to solidify and cool before reprocessing at a later stage by rolling into the required product form. Modern steelmaking practice has now moved much more to a process known as *continuous casting*, in which molten steel is poured at a steady rate into a mould to form a continuous solid strand from which lengths of semi-finished product are cut for subsequent processing. Semi-finished products take the form of *slabs*, *billets* or *blooms*. Continuous casting has the advantage of eliminating the reheating and first stage rolling required in the ingot production route, and is generally more efficient, but ingot production is still required for some product forms.

### 6.4.2 Casting and forging

If the final product form is a casting the liquid steel is poured direct into a mould of the required geometry and shape. Steel castings provide a versatile way of achieving the required finished product, particularly where either many items of the same type are required and/or complex geometries are involved. Special skills are required in the design and manufacture of the moulds in order to ensure that good quality castings are obtained with the required mechanical properties and

freedom from significant imperfections or defects. High-integrity castings for structural applications have been successfully supplied for critical components in bridges, such as the major cable saddles for suspension bridges, cast node and tubular sections for offshore structures, and the pump bowl casings for pressurized water reactor systems. The size of component which can be made in cast form is limited to a maximum of some 30 t – 50 t however, and only a small proportion of total steel production is completed as castings for direct application.

Another specialist route to the finished steel product is by forging, in which a bloom is heated to the austenitizing temperature range and formed by repeated mechanical pressing in different directions to achieve the required shape. The combination of temperature and mechanical work enables high-quality products with good mechanical properties to be obtained. An example of high-integrity forgings is the production of steel rings to form the shell/barrel of the reactor pressure vessel in a pressurized water reactor system. Again the proportion of steel production as forgings is a relatively small and specialized part of overall steel production.

### **6.4.3 Rolling**

By far the largest amount of finished steel production is achieved by rolling. The semi-finished products cast from the steelmaking furnace are reheated to the austenitizing range and passed through a series of mills with rolls of the required profile to force the hot steel into the finished shape. An example of the distribution of steel products produced by British Steel (BS) in 1987/88 is shown in the pie chart of Fig. 6.8. It can be seen that a major part of the BS's production goes into strip or sheet material which is produced by continuous rolling from slabs down to sheet of the required width and thickness which is first collected as a coil at the end of the rolling process, and subsequently cut into required lengths. This sheet material is typically used in the motor car industry, for containers and packaging including the food industry, and for domestic household equipment. The sheet material can be supplied either in bare steel form or with different types of coating. For example, it is possible to obtain steel sheet with a continuous galvanizing (zinc) coating for corrosion protection and it is also possible to obtain it with integral plastic coatings of different colours and patterns for decorative finish as well as corrosion protection.

For the structural industry steel slabs can be rolled into plates of the required thickness, or into structural sections such as universal columns, universal beams, angle sections, rail sections, etc. Round blooms or ingots can be processed by a seamless tube rolling mill into seamless tubes of different diameters and thicknesses or solid bar subsequently drawn out into wire. Tubes can be used either for carrying fluids in small-diameter pipelines or as structural hollow sections of circular or rectangular shape. The shape of engineering structural sections is determined by the required properties of the cross section such as cross-sectional

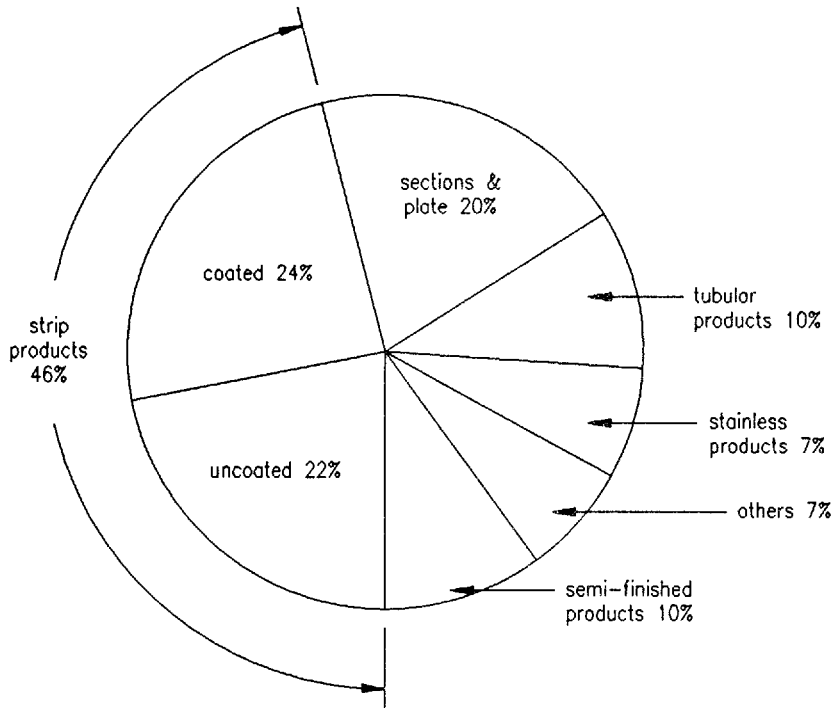


Fig. 6.8 British Steel distribution of turnover by product group 1987/88

area and moments of inertia about different axes to give an effective distribution of the weight of the material for structural purposes. Rolled structural sections are supplied in a standard range of shapes detailed in BS 4: Part 1 and a selection of typical shapes and section properties is given in the Appendix *Geometrical properties of plane sections*.

#### 6.4.4 Defects

In any bulk manufacturing process, such as the manufacture of steel, it is inevitable that a small proportion of the production will have imperfections which may or may not be harmful from the point of view of intended service performance of the product. In general the appropriate applications Standards have clauses which limit any such imperfections to acceptable and harmless levels. In castings a particular family of imperfections can occur which are dependent on the material and the geometry being manufactured. The most serious types of imperfection are cracks caused by shrinkage stresses during cooling, particularly at sharp changes

in cross section. A network of fine shrinkage cracks or tears can sometimes develop, again particularly at changes in cross section where the metal is subjected to a range of different cooling rates. The second type of imperfection in castings is solid inclusions, particularly in the form of sand where this medium has been used to form the moulds. Porosity, or gaseous inclusions, is not uncommon in castings to some degree and again tends to occur at changes in cross section. There is usually appreciable tolerance for minor imperfections such as sand inclusions or porosity provided these do not occur to extreme levels.

In rolled or drawn products, the most common types of defect are either cold laps or rolled-in surface imperfections. A lap is an imperfection which forms when the material has been rolled back on to itself but has not fully fused at the interface. Surface imperfections may occur from the same cause where a tongue of material is rolled down but does not fuse fully to the underlying material. Both of these faults are normally superficial and in any serious cases ought to be eliminated by final inspection at the steel mills. A third form of imperfection which can occur in plates, particularly when produced from the ingot route, is a *lamination*: the failure of the material to fuse together, usually at the mid-thickness of the plate. Laminations tend to arise from the rolling-out of pipes, or separation on the centreline of an ingot at either top or bottom which formed at the time of casting the ingot. Normal practice is that sufficient of the top and bottom of an ingot is cut off before subsequent processing to prevent laminations being rolled into subsequent products, but nevertheless they do occur from time to time. Fortunately the development of cracks in rolled products is relatively rare although it may occasionally occur in drawn products or as a result of quenching treatments in heat-treated products.

Since much of the manufacture of steels involves processing at, and subsequent cooling from, high temperatures it will be appreciated that high thermal stresses can develop during differential cooling and these can lead to residual stresses in the finished product. In many cases these residual stresses are of no significance to the subsequent performance of the product but there are situations where their effect must be taken into account. The two in which residual stresses from the steel manufacture are most likely to be of importance are where close tolerance machining is required, or where compression loading is being applied to slender structural sections. For the machining case it may be necessary to apply a stress relief treatment, or alternatively to carry out the machining in a series of very fine cuts. The effect of the inherent manufacturing residual stresses on structural sections is taken account of in the design codes such as BS 5950 for steel buildings, by giving a varying factor on the limiting permissible stresses depending on the product shape. These factors have been determined by a series of research programmes on the buckling behaviour of different shaped sections coupled to measurements of the inherent residual stresses present.

## 6.5 Engineering properties and mechanical tests

As part of the normal quality control procedures of the steel manufacturer, and as laid down in the different Specifications for manufacture of steel products, tests are carried out on samples representing each batch of steel and the results recorded on a test certificate. At the stage when the chemical analysis of the steel is being adjusted in the steelmaking furnace, samples are taken from the liquid steel melt at different stages to check the analysis results. Samples are also taken from the melt just before the furnace is tapped, and the analysis of these test results is taken to represent the chemical composition of the complete cast. The results of this analysis are given on Test Certificates for all products which are subsequently made from the same initial cast. The Test Certificate will normally give analysis results for C, Mn, Si, S and P for all steels, and where the Specification requires particular elements to be present in a specific range the results for these elements will also be given. Even when additional elements are not specified, the steel manufacturer will often provide analysis results for residual elements which may have been derived from scrap used or which could affect subsequent fabrication of performance during fabrication particularly welding. Thus steel supplied to the *Specification for weldable structural steels*, BS 4360, will often have Test Certificates giving Cr, Ni, Cu, V, Mo and Al, as well as the main basic five elements.

In some Specifications, the requirement is given for additional chemical analysis testing on each item of the final product form and this is presented on the Test Certificates as product analysis in addition to the cast analysis. This does however incur additional costs. The *Specification for weldable structural steels* gives the opportunity for requiring the steelmaker to supply information on the carbon equivalent to assist the fabricator on deciding about precautions during welding (see later). In low-alloy and stainless steels, the Test Certificates will of course give the percentage of the alloying elements such as chromium, nickel, etc.

The Test Certificates should also give the results of mechanical tests on samples selected to represent each product range in accordance with the appropriate Specification. The mechanical test results provided will normally include tensile tests giving the yield strength, ultimate strength and elongation to failure. In structural steels, where the fracture toughness is important, Specifications include requirements for Charpy V-notch impact tests to BS 131: Part 2. The Charpy test is a standard notched bar impact test of 10 mm square cross section with a 2 mm deep V-notch in one face. A series of specimens is tested under impact loading either at one Specification temperature or over a range of temperatures, and the energy required to break the sample is recorded. In the Eurocode and BS 4360 *Specification for weldable structural steels*, these notch ductility requirements are specified by letter grades A to F. Essentially these requirements are that the steel should show a minimum of 27 J energy absorption at a specified testing temperature corresponding to the letter grade. Grade A is no requirement, grade B requires testing at room temperature (+20°C), C at 0°C, D at -20°C, E at -50°C, and F at -60°C.

Charpy test requirements are also included in some of the general engineering steel Specifications (BS 970) for pressure vessel steels and other important structural applications, particularly where welded structures are used.

The Specifications normally require the steelmaker to extract specimens with their length parallel to the main rolling direction. In fact it is unlikely that the steel will be wholly isotropic, and significant differences in material properties may occur under different testing directions, which would not be evident from the normal Test Certificates unless special tests were carried out. It is possible in some Specifications to have material tests carried out both transverse to the main rolling direction, and in the through-thickness direction of rolled products. Testing in the through-thickness direction is particularly important where the material may in fact be loaded in this direction in service by welded attachments. Since such tests are additional to the normal routine practice of the steel manufacturer, and cost extra both for the tests themselves and for the disruption to main production, it is not unexpected that steels required to be tested to demonstrate properties in other directions are more expensive than the basic quality of steel tested in one standard direction only. The quality-control system at the steel manufacturers normally puts markings in the form of stamped numbers or letters on each length or batch of products so that it can be traced back to its particular cast and manufacturing route. In critical structural applications it is important that this numbering system is transferred on through fabrication to the finished structure so that each piece can be identified and confirmed as being of the correct grade and quality. The Test Certificate for each batch of steel is therefore a most important document to the steel manufacturer, to the fabricator, and to the subsequent purchaser of the finished component or structure. In addition to the chemical composition and mechanical properties, the Test Certificate should also record details of the steelmaking route and any heat treatments applied to the material by the steel manufacturer.

It is not uncommon for some semi-finished products to be sold by the steel manufacturer to other product finishers, or to stockholders. Unless these parties retain careful records of the supply of the material it may be difficult to trace specific details of the properties of steel bought from them subsequently, although some stockholders do maintain such records.

Where products are manufactured from semi-finished steel and subsequently given heat treatment for sale to the end user, the intermediate manufacturer should produce his own Test Certificates detailing both the chemical analysis of the steel and the mechanical properties of the finished product. For example, bolts used for structural connections are manufactured from bar material and are normally stamped with markings indicating the grade and type of bolt. Samples of bolts are taken from manufactured batches after heat treatment and subjected to mechanical tests to give reassurance that the correct strength of steel and heat treatment have been used.

## **6.6 Fabrication effects and service performance**

Basic steel products supplied from the steel manufacturer are rarely used directly without some subsequent fabrication. The various processes involved in fabrication may influence the suitability for service of the steel and over the years established procedures of good practice have been developed which are acceptable for particular industries and applications.

### **6.6.1 Cutting, drilling, forming and drawing**

Basic requirements in the fabrication of any steel component are likely to be cutting and drilling. In thin sections, such as sheet material, steel can be cut satisfactorily by guillotine shearing and although this may form a hardened edge it is usually of little or no consequence. Thicker material in structural sections up to about 15 mm thickness can also be cut by heavy-duty shears, useful for small part pieces such as gussets, brackets, etc. Heavier section thicknesses will usually have to be cut by cold saw or abrasive wheel or by flame cutting. Cold saw and abrasive wheel cutting produce virtually no detrimental effects and give good clean cuts to accurate dimensional tolerances. Flame cutting is carried out using an oxyacetylene torch to burn the steel away in a narrow slit and this is widely used for cutting of thicker sections in machine-controlled cutting equipment. The intense heating in flame cutting does subject the edge of the metal to rapid heating and cooling cycles and so produces the possibility of a hardened edge in some steels. This can be controlled by either preheating just ahead of the cutting torch, or using slower cutting speeds, or alternatively, if necessary, any hardened edge can be removed by subsequent machining. In recent years laser cutting has become a valuable additional cutting method for thin material, in that intricate shapes and patterns can be cut out rapidly by steering a laser beam around the required shape.

Drilling of holes presents little problem and there are now available numerical/computer controlled systems which will drill multiple groups of holes to the required size and spacing. For thinner material hole punching is commonly used and although this, like shearing, can produce a hardened edge, provided the punch is sharp no serious detrimental effects occur in thinner material.

It is sometimes necessary to bend, form or draw steel into different shapes. Reinforcing steel for reinforced concrete structures commonly has to be bent into the form of hooks and stirrups. The curved sections of tubular members of offshore structures or cylindrical parts of pressure vessels are often rolled from flat plate to the required curvature. In these cases yielding and plastic strain take place as the material is deformed beyond its elastic limit. This straining moves the material condition along its basic stress/strain curve, and it is therefore important to limit the amount of plastic strain used up in the fabrication process so that that available for subsequent service is not diminished to an unacceptable extent. The important variable in limiting the amount of plastic strain which occurs during

cold forming is usually the ratio of the radius of any bend to the thickness or diameter of the material. Provided this ratio is kept high the amount of strain will be limited. Where the amount of cold work which has been introduced during fabrication is excessive, it may be necessary to carry out a reheat treatment in order to restore the condition of the material to give its required properties.

In the manufacture of wire, the steel is drawn through a series of dies gradually reducing its diameter and increasing the length from the initial rod sample. This cold drawing is equivalent to plastic straining and has the effect of both increasing the strength of the material and reducing its remaining ductility as the material moves along its stress/strain curve. In certain types of wire manufacture, intermediate heat treatments are necessary in order to remove damaging effects of cold work and enhance and improve the final mechanical properties.

### **6.6.2 Welding**

One of the most important fabrication processes for use with steel is welding. There are many different types of welding and this subject is itself a fascinating multi-disciplinary world involving combined studies in physics, chemistry, electronics, metallurgy, and mechanical, electrical and structural engineering. Most welding processes involve fusion of the material being joined, by raising the temperature to the melting point of the material, either with or without the addition of separate filler metal. Although there is a huge variety of different welding processes, probably the most common and most important ones for general applications are the group of arc welding processes and the group of resistance welding processes. Among the newer processes are the high energy density beam processes such as electron beam and laser welding.

Arc welding processes involve the supply of an intense heat source from an electric arc which melts the parent material locally, and may provide additional filler metal by the melting of a consumable electrode. These processes are extensively used in the construction industry, and for any welding of material thicknesses above the range of sheets. The resistance group of welding processes involve the generation of heat at the interface between two pieces of material by the passage of very heavy current directly between opposing electrodes on each face. The resistance processes do not involve additional filler metal, and can be used to produce local joints as spot welds, or a series of such welds to form a continuous seam. This group of processes is particularly suitable for sheet material and is widely used in the automotive and domestic equipment markets.

It will be appreciated that fusion welding processes involve rapid heating and cooling locally at the position where a joint is to be made. The temperature gradients associated with welding are intense, and high thermal stresses and subsequent residual stresses on cooling are produced. The residual stresses associated with welding are generally much more severe than those which result during the basic steel manufacturing process itself as the temperature gradients are more

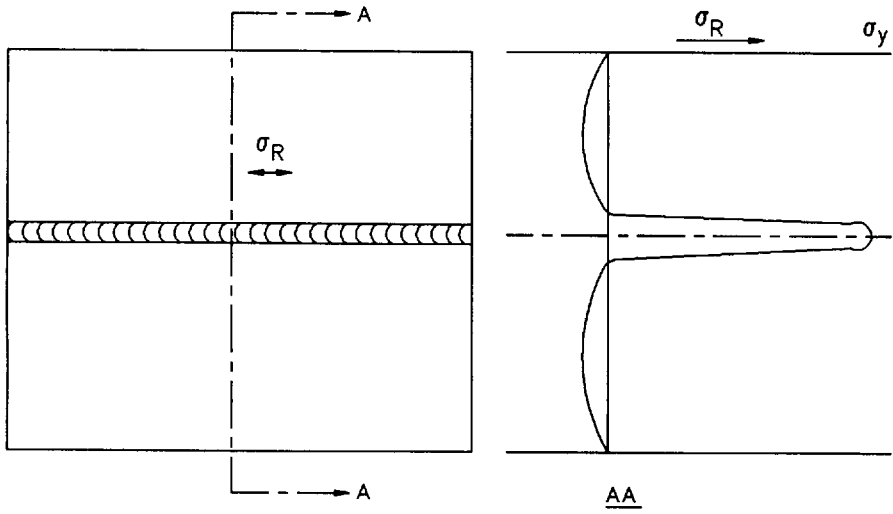


localized and intense. Examples of the residual stress distribution resulting from the manufacture of a butt weld between two plates, and a T-butt weld with one member welded on to the surface of a second, are shown in Fig. 6.9. As will be seen from other chapters, residual stresses can be important in the performance of steel structures because of their possible effects on brittle fracture, fatigue and distortion. If a steel material has low fracture toughness, and is operating below its transition temperature, residual stresses may be very important in contributing to failure by brittle fracture at low applied stresses. If on the other hand the material is tough and yields extensively before failure, residual stresses will be of little importance in the overall structural strength. These effects are summarized in Fig. 6.10.

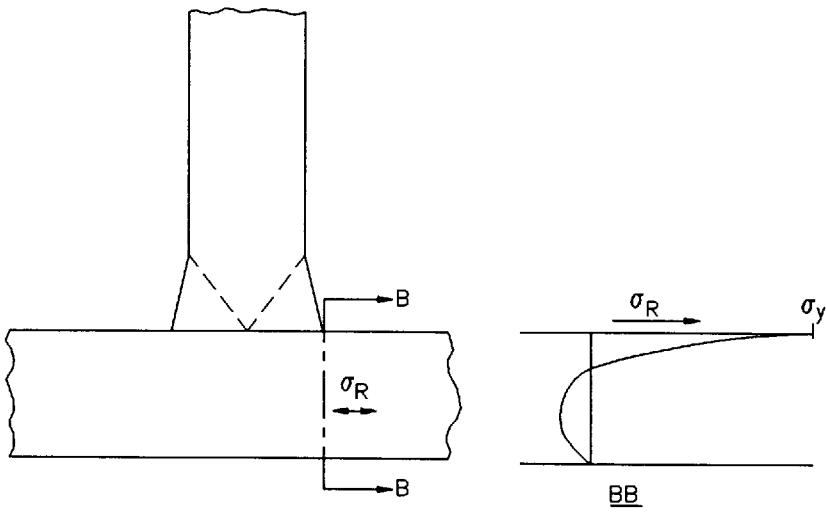
In fatigue-loaded structures residual stresses from welding are important in altering the mean stress and stress ratio. Although these are secondary factors compared to the stress range in fatigue, the residual stress effect is sufficiently important that it is now commonly assumed that the actual stress range experienced at a weld operates with an upper limit of the yield strength due to locked-in residual stresses at this level. Thus although laboratory experiments demonstrate different fatigue performance for the same stress range at different applied mean stress in plain unwelded material, the trend in welded joints is for the applied stress ratio effect to be overridden by locked-in residual stresses.

The effect of welding residual stresses on distortion can be significant both at the time of fabrication, and in any subsequent machining which may be required. The forces associated with shrinkage of welds are enormous, and will produce overall shrinkage of components and bending/buckling deformations out of a flat plane. These effects have to be allowed for either by pre-setting in the opposite direction to compensate for any out-of-plane deformations, or by making allowances with components initially over-length to allow for shrinkage.

Just as the basic steel manufacturing process can lead to the presence of imperfections, welding also can lead to imperfections which may be significant. The types of imperfection can be grouped into three main areas: planar discontinuities, non-planar (volumetric) discontinuities, and profile imperfections. By far the most serious of these are planar discontinuities, as these are sharp and can be of a significant size. There are four main types of weld cracking which can occur in steels as planar discontinuities. These are *solidification (hot) cracking*, *hydrogen-induced (cold) cracking*, *lamellar tearing*, and *reheat cracking*. Examples of these are shown in Fig. 6.11. *Hot cracking* occurs during the solidification of a weld due to the rejection of excessive impurities to the centreline. Impurities responsible are usually sulphur and phosphorus, and the problem is controlled by keeping them to a low level and avoiding deep narrow weld beads. *Cold cracking* is due to the combination of a susceptible hardened microstructure and the effects of hydrogen in the steel lattice. The problem is avoided by control of the steel chemistry, arc energy heat input, preheat level, quenching effect of the thickness of joints being welded, and by careful attention to electrode coatings to keep hydrogen potential to very low levels. Guidance on avoiding this type of cracking in the heat affected zones of weldable structural steels is given in BS 5135.



(a)



(b)

Fig. 6.9 Typical weld residual stress distributions: (a) butt weld, (b) T-butt weld ( $\sigma_R$  residual stress;  $\sigma_y$  yield stress)

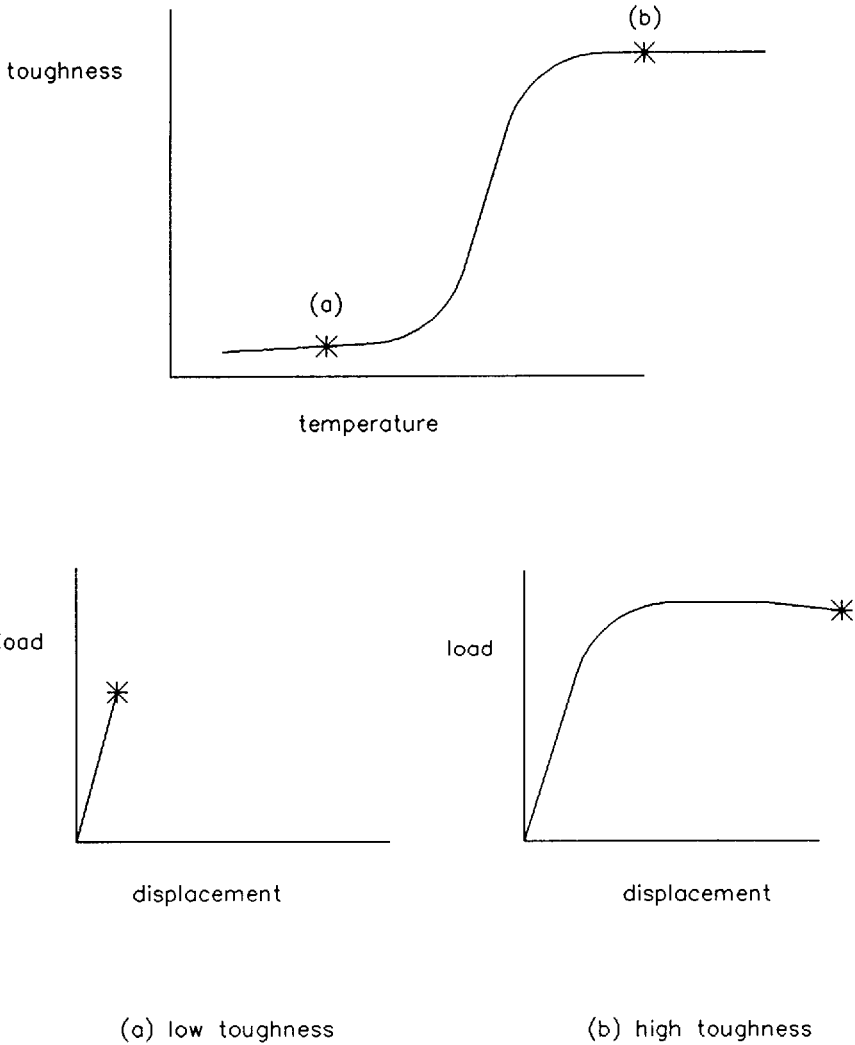


Fig. 6.10 Effects of toughness and residual stresses on strength in tension

*Lamellar tearing* is principally due to the presence of excessive non-metallic inclusions in rolled steel products resulting in the splitting open of these inclusions under the shrinkage forces of welds made on the surface. The non-metallic inclusions usually responsible are either sulphides or silicates; manganese sulphides are probably the most common. The problem is avoided by keeping the impurity content low, particularly the sulphur level to below about 0.010%, and by specifying tensile tests in the through-thickness direction to show a minimum ductility by reduction of area dependent on the amount of weld shrinkage anticipated (i.e. size of welded attachment, values of R of A of 10% to 20% are usually adequate).

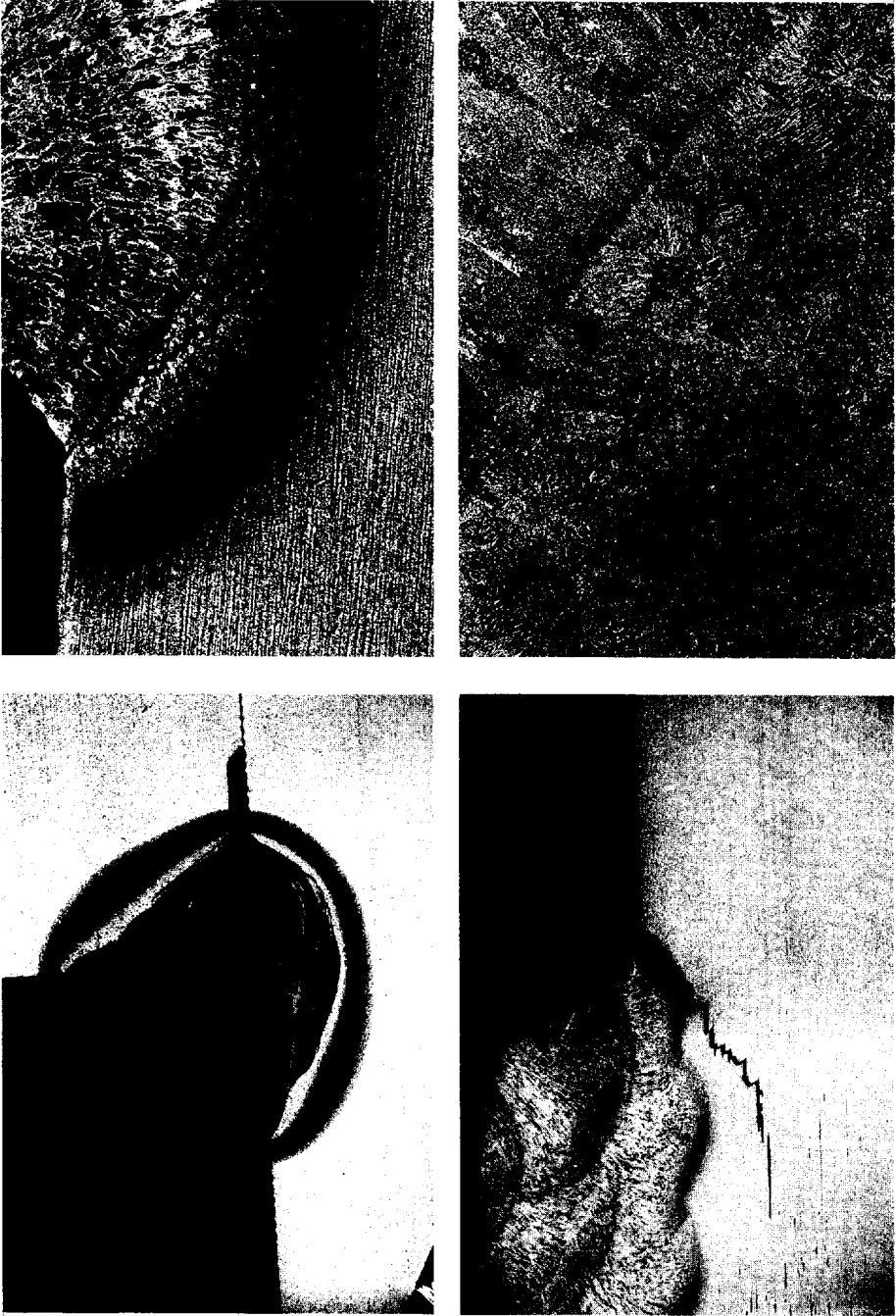


Fig. 6.11 Examples of different types of cracking which may occur in welded steel joints (courtesy of The Welding Institute)

*Reheat cracking* is a form of cracking which can develop during stress relief heat treatment or during high temperature service in particular types of steel (usually molybdenum or vanadium bearing) where secondary precipitation of carbides develops before relaxation of residual stresses has taken place.

Other forms of planar defect in welds are the operator or procedure defects of *lack of penetration* and *lack of fusion*. The volumetric/non-planar imperfections divide into the groups of *solid inclusions* and *gaseous inclusions*. The solid inclusions are usually slag from the electrode/flux coating and the gaseous inclusions result from porosity trapped during the solidification of the weld. In general the non-planar defects are much less critical than planar defects of the same size and are usually limited in their effect because their size is inherently limited by their nature.

## 6.7 Summary

### 6.7.1 Criteria influencing choice of steel

The basic requirement in the choice of a particular steel is that it must be fit for the product application and design conditions required. It must be available in the product form and shape required and it should be at the minimum cost for the required application. Clearly before the generic type of material is chosen as steel, it must be shown to be advantageous to use steel over other contending materials, and therefore the strength-to-weight ratio and cost ratios must be satisfactory.

The steel must have the required strength, ductility and long-term service life in the required environmental service conditions. For structural applications the steel must also have adequate fracture toughness, this requirement being implemented by standard Charpy test quality control levels.

Where the steel is to be fabricated into components or structures, its ability to retain its required properties in the fabricated condition must be clearly established. One of the most important factors in this respect for a number of industries is the weldability of steel, and in this respect the chemical composition of the steel must be controlled within tight limits, and the welding processes and procedures adopted must be compatible with the material chosen.

The corrosion-resistance and potential fire-resistance/high temperature performance of the steel may be important factors in some applications. A clear decision has to be taken at the design stage as to whether resistance to these effects is to be achieved by external or additional protection measures, or inherently by the chemical composition of the steel itself. Stainless steels with high quantities of chromium and nickel are significantly more expensive than ferritic carbon or carbon manganese steels. Particular application standards generally specify the range of material types which are considered suitable for their particular application.

Increased strength of steels can be obtained by various routes, including increased alloying content, heat treatment, or cold working. In general as the strength increases so does the cost and there may be little advantage in using high-strength steels in situations where either fatigue or buckling are likely to be ruling modes of failure. It should not be overlooked that although there is some increase in cost of the basic raw material with increasing strength, there is likely to be a significant increase in fabrication costs with additional precautions necessary for the more sophisticated types of higher-strength material.

Certain product forms are only available in certain grades of steel. It may not be possible to achieve high strength in some product shapes and retain dimensional requirements through the stage of heat treatment because of distortion problems.

Wherever possible, guidance should be sought on the basis of similar previous experience or prototype trials to ensure that the particular material chosen will be suitable for its required application.

### 6.7.2 Steel specifications and choice of grade

Structural steelwork, comprising rolled products of plate, sections and hollow sections, is normally of a weldable carbon or carbon-manganese structural steel to BS 4360 or to the new European based standard, BS EN 10025. Two strength grades are most commonly used, grade 43 (or Fe 430) and grade 50 (or Fe 510), having yield strengths typically of  $275 \text{ N/mm}^2$  or  $355 \text{ N/mm}^2$  respectively. In buildings grade 43 is more common, though columns and composite beams in multi-storey buildings will often be grade 50. In bridges and other major structures grade 50 is more common. The design codes for buildings and bridges require that structural steelwork subject to tensile stresses have adequate notch toughness at the *minimum service temperature* of the structure. This temperature is specified as  $-5^\circ\text{C}$  for internal building steelwork,  $-15^\circ\text{C}$  for external building steelwork and typically between  $-15^\circ\text{C}$  and  $-25^\circ\text{C}$  for bridge steelwork, depending on location and exposure. The subgrade of steel needed to achieve the required toughness is then usually C or D (i.e. grades 43C, 43D, or Fe 430C, Fe 510D), or possibly higher subgrades for thicker material.

Weather resistant steels in the form of rolled sections and plate are also covered by BS 4360.

Cold reduced hot-rolled steel is produced in accordance with BS 1449: Part 1, but for most structural applications it is used in the form of galvanized cold formed steel supplied in accordance with BS 2989 and BS EN 10142. Two strength grades are most commonly specified, grades Z28 and Z35, with yield strengths of  $280 \text{ N/mm}^2$  and  $350 \text{ N/mm}^2$  respectively. Cold formed steel is extensively used as profiled cladding sheets and its support members.

Stainless steel is specified by BS 1449: Part 2 for flat products and by BS 970: Part 1 for bars. Simple sections can be formed by cold rolling; hot rolled sections are not commonly available in stainless steel. For structural use, austenitic steels are required, usually of grades 304 or 316. The former is more common; the latter

has superior corrosion resistance and is used in more aggressive environments. Stainless steel generally has good notch toughness, even at very low temperatures.

Castings are manufactured in accordance with BS 3100. This specification covers all type of casting for engineering purposes, including carbon and stainless steels. Castings can be welded, subject to appropriate post-welding heat treatment.

Wrought or forged steels are required where particularly thick sections or higher strength components are needed. BS 970 covers a wide range of alloys, though only a small number of them are appropriate for normal structural use. Components are normally machined from the solid bar, and since the high strengths depend on special heat treatment, little or no welding is possible on such wrought steel parts.

Steel wire ropes are normally made with cold drawn galvanised steel wires, which are manufactured according to BS 2763. The ultimate strengths of individual wires can be as high as  $1700 \text{ N/mm}^2$ . The design of wire ropes depends on their usage and is covered by a range of design standards.

### Further reading for Chapter 6

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# Chapter 7

# Fatigue

by ROBERT SIMPSON

## 7.1 Introduction

A component or structure which survives a single application of load may fracture if the application is repeated a large number of times. This would be classed as fatigue failure. Fatigue failure can be defined as the number of cycles and hence the time taken to reach a pre-defined failure criterion. Fatigue failure is by no means a rigorous science and the idealizations and approximations inherent in it prevent the calculation of an absolute fatigue life for even the simplest joint.

In the analysis of a structure for fatigue there are three main areas of difficulty in prediction:

- (1) The operational environment of a structure and the relationship between the environment and the actual forces on it
- (2) The internal stresses at a critical point in the structure induced by external forces acting on the structure
- (3) The time to failure due to the accumulated stress history at the critical point.

There are two basic approaches for the assessment of fatigue life of structural components. The first method, which is currently in general use, relies on empirically derived relationships between applied stress ranges and fatigue life commonly called the  $S-N$  approach. The second method, based on fracture mechanics, considers the growth rate of an existing defect at each stage in its propagation.

## 7.2 Loadings for fatigue

Examples of structures and the loads which can cause fatigue are:

Bridges: commercial vehicles, goods trains

Cranes: lifting, rolling and inertial loads

Offshore structures: waves

Slender towers: wind gusting.

The designer's objective is to anticipate the sequence of service loading throughout the structure's life. The magnitude of the peak load, which is vital for static design



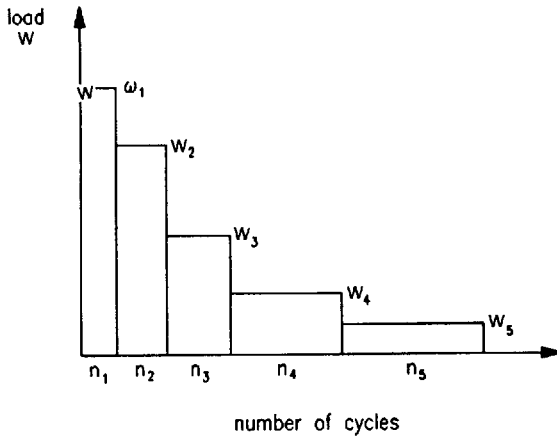


Fig. 7.1 Typical load spectrum for design

purposes, is generally of little concern as it only represents one cycle in millions. For example, highway bridge girders may experience 100 million significant cycles in their lifetime. The sequence is important because it affects the stress range, particularly if the structure is loaded by more than one independent load system.

For convenience, loadings are usually simplified into a load spectrum, which defines a series of bands of constant load levels and the number of times that each band is experienced, as shown in Fig. 7.1.

Slender structures, with natural frequencies low enough to respond to the loading frequency, may suffer dynamic magnification of stress. This can shorten the life considerably.

References 1–4 are useful sources of information on fatigue loading.

## 7.3 The nature of fatigue

### 7.3.1 Introduction

Materials subject to a cyclically variable stress of a sufficient magnitude change their mechanical properties. In practice a very high percentage of all engineering failures are due to fatigue. Most of these failures can be attributed to poor design or subsequent manufacture. The fatigue process is not a single mechanism but the result of several mechanisms operating in sequence during the life of a structure: initiation of a microscopic defect, slow incremental crack propagation and final unstable fracture. In most steel structures which are welded the initiation phase is not necessary for crack growth as existing defects are already likely to be present.

**7.3.2 *S-N* curves**

The most common form of presentation of fatigue data is the *S-N* curve, where the total cyclic stress range (*S*) is plotted against the number of cycles to failure (*N*). A typical curve is shown in Fig. 7.2.

These data are obtained experimentally. For a particular welded joint configuration, a series of specimens is subject to cycles of constant amplitude to failure. Sufficient specimens are tested for statistical analysis to be carried out to determine both mean fatigue strength and its standard deviation. Depending on the design philosophy adopted, design strength is taken as mean minus an appropriate number of standard deviations.

Logarithmic scales are conventionally used for both axes, and the *S-N* curves are based on test data. To carry out fatigue life predictions a linear fatigue damage mode is used in conjunction with the relevant *S-N* curve. One such fatigue damage model is that postulated by Miner. In essence, the model assumes that irreversible damage accumulates linearly to a fixed level, at which failure

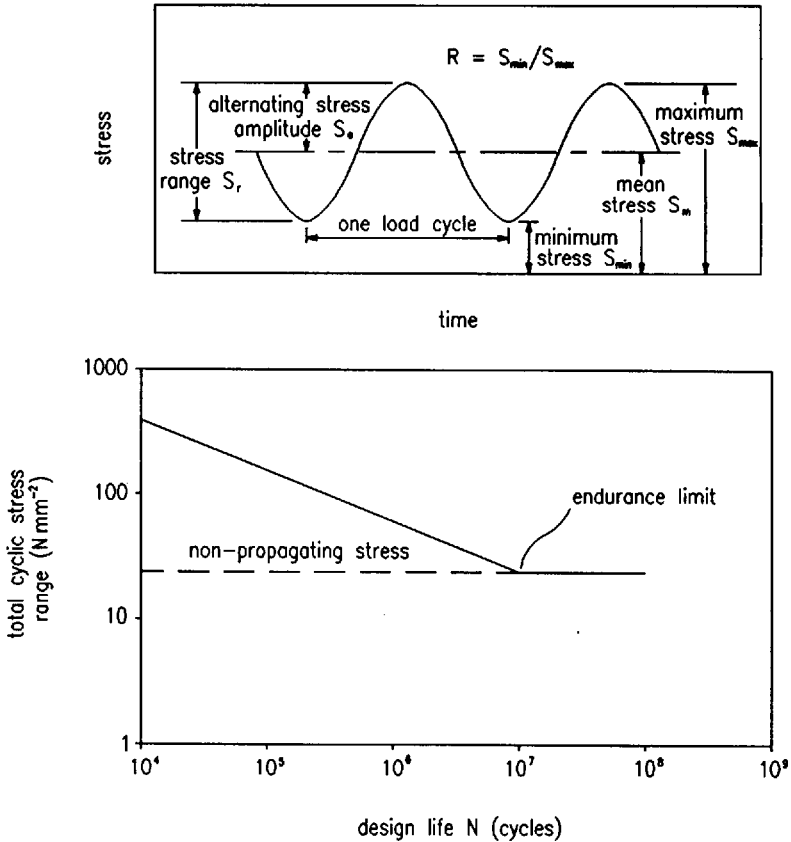


Fig. 7.2 Typical *S-N* curve and nomenclature used in fatigue

occurs. For welded joints the relationship between fatigue life and applied stress range is linear over a wide range of stress and takes the form

$$NS_r^m = A \tag{7.1}$$

where  $N$  = number of cycles to failure,  $S_r$  = applied stress range and  $m, A$  = constants depending on joint type. Figure 7.3 presents a series of  $S-N$  curves which have been defined by taking different values of  $m$  and  $A$ , applicable to most common welded joint configurations. The curves have been established empirically from a large number of small-scale laboratory tests. For the purposes of fatigue design constructional details are grouped in eight classes designated B, C, D, E, F, F2, G and W. Details of these groupings are given in BS 5400: Part 10.

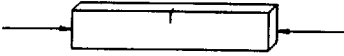
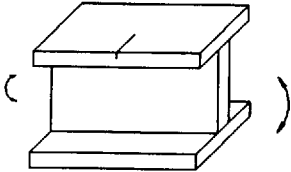
Examples of the classification of some joints are given in Table 7.1. In any welded joint there are at least five potential locations at which fatigue cracks may develop. These are at the weld toe in each of the two parts joined, at the two ends, and in the weld itself. Each must be classified separately.

**Table 7.1** Fatigue: joint classification

*Type 1 Material free from welding*

Notes on potential modes of failure

In plain steel, fatigue cracks initiate at the surface, usually either at surface irregularities or at corners of the cross section. In welded construction, fatigue failure will rarely occur in a region of plain material since the fatigue strength of the welded joints will usually be much lower. In steel with rivet or bolt holes or other stress concentrations arising from the shape of the member, failure will usually initiate at the stress concentration.

| Type and description  | Class | Explanatory comments  | Examples, including failure modes  |
|---|-------|---|--|
| 1.1 Plain steel   |       |   |  |
| (a) In the as-rolled condition, or with cleaned surfaces but with no flame-cut edges of re-entrant corners.                   | B     | Beware of using Class B for a member which may acquire stress concentrations during its life, e.g. as a result of rust pitting. In such an event Class C would be more appropriate.   |  |
| (b) As (a) but with any flame-cut edges subsequently ground or machined to remove all visible sign of the drag lines.         | B     | Any re-entrant corners in flame-cut edges should have a radius greater than the plate thickness.  |  |
| (c) As (a) but with the edges machine flame-cut by a controlled procedure to ensure that the cut surface is free from cracks. | C     | Note, however, that the presence of a re-entrant corner implies the existence of a stress concentration so that the design stress should be taken as the net stress multiplied by the relevant stress concentration factor. |  |

**Table 7.1** Continued

*Type 2 Continuous welds essentially parallel to the direction of applied stress*

Notes on potential modes of failure

With the excess weld metal dressed flush, fatigue cracks would be expected to initiate at weld defect locations. In the as-welded condition, cracks might initiate at stop-start positions or, if these are not present, at weld surface ripples.

General comments

(1) Backing strips

If backing strips are used in making these joints: (a) they must be continuous, and (b) if they are attached by welding those welds must also comply with the relevant Class requirements (note particularly that tack welds, unless subsequently ground out or covered by a continuous weld, would reduce the joint to Class F, (see joint Type 6.5 (not shown here)).

(2) Edge distance

An edge distance criterion exists to limit the possibility of local stress concentrations occurring at unwelded edges as a result, for example, of undercut, weld spatter, or accidental overweave in manual fillet welding (see also notes on joint Type 4). Although an edge distance can be specified only for the 'width' direction of an element, it is equally important to ensure that no accidental undercutting occurs on the unwelded corners of, for example, cover plates or box girder flanges. If it does occur it should subsequently be ground smooth.

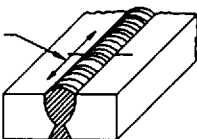
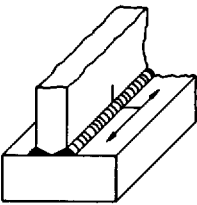
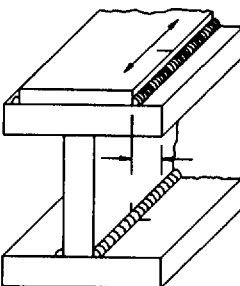
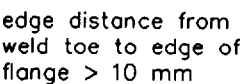
| Type and description  | Class | Explanatory comments  | Examples, including failure modes  |
|---|-------|---|--|
| <p>2.1 Full or partial penetration butt welds, or fillet welds: parent or weld metal in members, without attachments, built up of plates or sections, and joined by continuous welds.</p>   |       |   |    |
| <p>(a) Full penetration butt welds with the weld overfill dressed flush with the surface and finish-machined in the direction of stress, and with the weld proved free from significant defects by non-destructive examination.</p> | B     | <p>The significance of defects should be determined with the aid of specialist advice and/or by the use of fracture mechanics analysis. The NDT technique must be selected with a view to ensuring the detection of such significant defects.</p> |   |
| <p>(b) Butt or fillet welds with the welds made by an automatic submerged or open arc process and with no stop-start positions within the length.</p>   | C     | <p>If an accidental stop-start occurs in a region where Class C is required, remedial action should be taken so that the finished weld has a similar surface and root profile to that intended.</p>   |    |
| <p>(c) As (b) but with the weld containing stop-start positions within the length.</p>  | D     | <p>For situation at the ends of flange cover plates see joint Type 6.4 (not shown here).</p>  |  <p>edge distance from weld toe to edge of flange &gt; 10 mm</p> |

Table 7.1 Continued

Type 3 Transverse butt welds in plates (i.e. essentially perpendicular to the direction of applied stress)

Notes on potential modes of failure

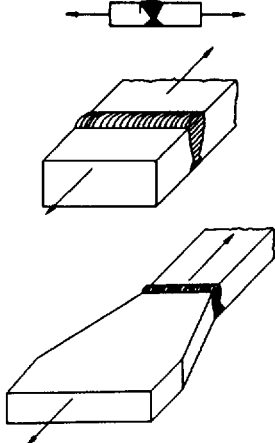
With the weld ends machined flush with the plate edges, fatigue cracks in the as-welded condition normally initiate at the weld toe, so that the fatigue strength depends largely upon the shape of the weld overfill. If this is dressed flush the stress concentration caused by it is removed and failure is then associated with weld defects. In welds made on a permanent backing strip, fatigue cracks initiate at the weld metal/strip junction, and in partial penetration welds (which should not be used under fatigue conditions) at the weld root.

Welds made entirely from one side, without a permanent backing, require care to be taken in the making of the root bead in order to ensure a satisfactory profile.

Design stresses

In the design of butt welds of Types 3.1 or 3.2 which are not aligned, the stresses must include the effect of any eccentricity. An approximate method of allowing for eccentricity in the thickness direction is to multiply the normal stress by  $(1 + 3e/t)$ , where  $e$  is the distance between centres of thickness of the two abutting members; if one of the members is tapered, the centre of the untapered thickness must be used; and  $t$  is the thickness of the thinner member.

With connections which are supported laterally, e.g. flanges of a beam which are supported by the web, eccentricity may be neglected.

| Type and description  | Class | Explanatory comments  | Examples, including failure modes  |
|---|-------|---|--|
| <p>3.1 Parent metal adjacent to, or weld metal in, full penetration butt joints welded from both sides between plates of equal width and thickness or where differences in width and thickness are machined to a smooth transition not steeper than 1 in 4.</p> |       | <p>Note that this includes butt welds which do not completely traverse the member, such as circular welds used for inserting infilling plates into temporary holes.</p>   |  |
| <p>(a) With the weld overfill dressed flush with the surface and with the weld proved free from significant defects by non-destructive examination.</p>   | C     | <p>The significance of defects should be determined with the aid of specialist advice and/or by the use of fracture mechanics analysis. The NDT technique must be selected with a view to ensuring the detection of such significant defects.</p> |  |
| <p>(b) With the welds made, either manually or by an automatic process other than submerged arc, provided all runs are made in the downhand position.</p>   | D     | <p>In general welds made by the submerged arc process, or in positions other than downhand, tend to have a poor reinforcement shape, from the point of view of fatigue strength. Hence such welds are downgraded from D to E.</p>                 |  |

**Table 7.1** Continued

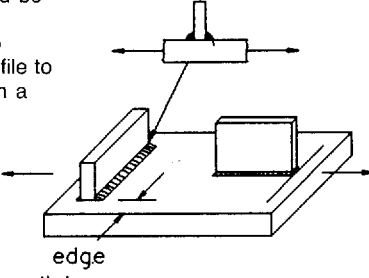
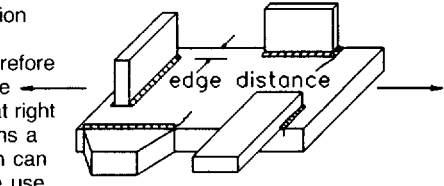
| Type and description  | Class | Explanatory comments  | Examples, including failure modes |
|---|-------|---|-----------------------------------|
| <p><i>Type 3.1 cont.</i><br/>                     (c) Welds made other than in (a) or (b).</p>  | E     | <p>In both (b) and (c) the corners of the cross section of the stressed element at the weld toes should be dressed to a smooth profile.<br/>                     Note that step changes in thickness are in general not permitted under fatigue conditions, but that where the thickness of the thicker member is not greater than <math>1.15 \times</math> the thickness of the thinner member, the change can be accommodated in the weld profile without any machining. Step changes in width lead to large reductions in strength (see joint Type 3.3).</p> |                                   |
| <p>3.2 Parent metal adjacent to, or weld metal in, full penetration butt joints made on a permanent backing strip between plates of equal width and thickness or with differences in width and thickness machined to a smooth transition not steeper than 1 in 4.</p> | F     | <p>Note that if the backing strip is fillet welded or tack welded to the member the joint could be reduced to Class G (joint Type 4.2).</p>   |                                   |
| <p>3.3 Parent metal adjacent to, or weld metal in, full penetration butt welded joints made from both sides between plates of unequal width, with the weld ends ground to a radius not less than 1.25 times the thickness <math>t</math>.</p>                         | F2    | <p>Step changes in width can often be avoided by the use of shaped transition plates, arranged so as to enable butt welds to be made between plates of equal width.<br/>                     Note that for this detail the stress concentration has been taken into account in the joint classification.</p>  |                                   |

**Table 7.1** Continued

*Type 4 Welded attachments on the surface or edge of a stressed member*

Notes on potential modes of failure

When the weld is parallel to the direction of the applied stress fatigue cracks normally initiate at the weld ends, but when it is transverse to the direction of stressing they usually initiate at the weld toe; for attachments involving a single, as opposed to a double, weld cracks may also initiate at the weld root. The cracks then propagate into the stressed member. When the welds are on or adjacent to the edge of the stressed member the stress concentration is increased and the fatigue strength is reduced; this is the reason for specifying an 'edge distance' in some of these joints (see also note on edge distance in joint Type 2).

| Type and description   | Class | Explanatory comments  | Examples, including failure modes  |
|--|-------|---|--|
| 4.1 Parent metal (of the stressed member) adjacent to toes or ends of bevel-butt or fillet welded attachments, regardless of the orientation of the weld to the direction of applied stress, and whether or not the welds are continuous round the attachment. |       | Butt welded joints should be made with an additional reinforcing fillet so as to provide a similar toe profile to that which would exist in a fillet welded joint.  |    |
| (a) With attachment length (parallel to the direction of the applied stress) $\leq 150$ mm and with edge distance $\geq 10$ mm.  | F     | The decrease in fatigue strength with increasing attachment length is because more load is transferred into the longer gusset giving an increase in stress concentration.   |  |
| (b) With attachment length (parallel to the direction of the applied stress) $> 150$ mm and with edge distance $\leq 10$ mm.   | F2    |   |  |
| 4.2 Parent metal (of the stressed member) at the toes or the ends of butt or fillet welded attachments on or within 10 mm of the edges or corners of a stressed member, and regardless of the shape of the attachment.   | G     | Note that the classification applies to all sizes of attachment. It would therefore include, for example, the junction of two flanges at right angles. In such situations a low fatigue classification can often be avoided by the use of a transition plate (see also joint Type 3.3). |  |

**Table 7.1** Continued

| Type and description   | Class | Explanatory comments  | Examples, including failure modes |
|--|-------|---|-----------------------------------|
| 4.3 Parent metal (of the stressed member) at the toe of a butt weld connecting the stressed member to another member slotted through it.               |       | Note that this classification does not apply to fillet welded joints (see joint Type 5.1b (not shown here)). However it does apply to loading in either direction (L or T in the sketch). |                                   |
| (a) With the length of the slotted-through member, parallel to the direction of the applied stress, $\leq 150$ mm and with edge distance $\geq 10$ mm. | F     |   |                                   |
| (b) With the length of the slotted-through member, parallel to the direction of the applied stress, $> 150$ mm and with edge distance $\geq 10$ mm.    | F2    |   |                                   |
| (c) With edge distance $< 10$ mm.  | G     |   |                                   |

**Type 5 Load-carrying fillet and *t* butt welds**

## Notes on potential modes of failure

Failure in cruciform or T joints with full penetration welds will normally initiate at the weld toe, but in joints made with load-carrying fillet or partial penetration butt welds cracking may initiate either at the weld toe and propagate into the plate or at the weld root and propagate through the weld. In welds parallel to the direction of the applied stress, however, weld failure is uncommon; cracks normally initiate at the weld end and propagate into the plate perpendicular to the direction of applied stress. The stress concentration is increased, and the fatigue is therefore reduced, if the weld end is located on or adjacent to the edge of a stressed member rather than on its surface.

**7.3.3 Variable-amplitude loading**

For constant-amplitude loading, the permissible stress range can be obtained directly from Fig. 7.3 by considering the required design life. In practice it is more common for structures to be subjected to a loading spectrum of varying amplitudes or random vibrations. In such cases use is made of Miner's rule. For a joint subjected to a number of repetitions,  $n_i$ , of each of several stress ranges  $S_{ri}$ , the value of  $n_i$  corresponding to each  $S_{ri}$  should be determined from stress spectra measured on similar equipment or by making reasonable assumptions as to the expected service history. The permissible number of cycles,  $N_i$ , at each stress range,  $S_{ri}$ , should then be determined from Fig. 7.3 for the relevant joint class, and the stress range adjusted so that the cumulative damage summation



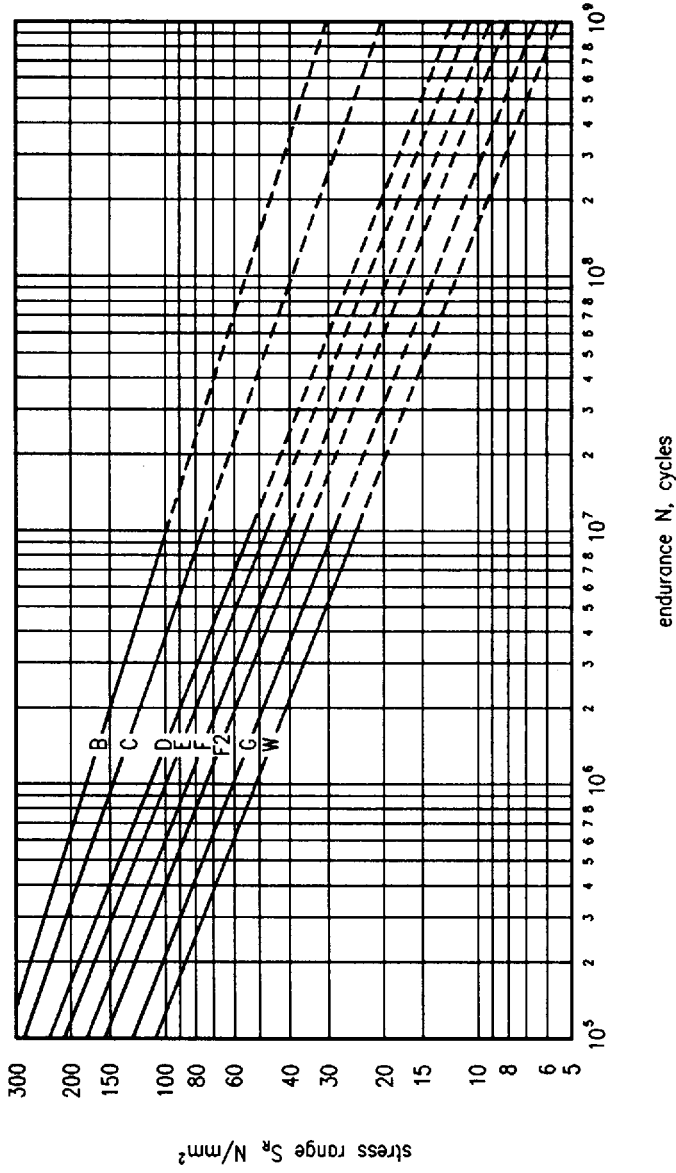


Fig. 7.3 Design S-N curves used for steel

$$\frac{n_1}{N_1} + \frac{n_2}{N_2} + \frac{n_3}{N_3} + \frac{n_4}{N_4} + \dots = \sum \frac{n}{N} < 1.0 \quad (7.2)$$

The order in which the variable amplitude stress ranges occur in a structure is not a relevant factor.

Various methods exist to sum the spectrum of stress cycles. The 'rainflow' counting method is probably the most widely used for analyzing long stress histories using a computer. This method separates out the small cycles that are often superimposed on larger cycles, ensuring both are counted. The procedure involves the simulation of a time history, or use of measure sequences, with appropriate counting algorithms. Once the spectrum of stress cycles has been determined, the load sequence is broken down into a number of constant load range segments. Reference 2 describe the 'reservoir' method which is easy to use by hand for short stress histories.

#### 7.4 Fracture mechanics analysis

Fatigue life assessment using fracture mechanics is based on the observed relationship between the change in the stress intensity factor,  $\Delta K$ , and the rate of growth of fatigue cracks,  $da/dN$ . This approach was first formulated by Paris who proposed the power law relations of the form:

$$da/dN = C(\Delta K)^n \quad (7.3)$$

where  $da/dN$  is the crack extension per cycle,  $C$ ,  $n$  are crack growth constants, and

$$\Delta K = K_{\max} - K_{\min}$$

where  $K_{\max}$  and  $K_{\min}$  are the maximum and minimum stress intensities respectively in each cycle. Since the crack growth rate is related to  $\Delta K$  raised to an exponent, the exponent having a range 3–4, it is important that  $\Delta K$  should be known accurately if meaningful crack growth predictions are to be made.

Values of  $C$  and  $n$  can be obtained from specific tests on the materials under consideration. From published data the upper limits on growth rates for ferritic steels are given by

$$\begin{aligned} n &= 3 \\ C &= 3 \times 10^{-13} \quad \text{for non-aggressive environments at temperatures up to } 100^\circ\text{C} \\ C &= 3 \times 10^{-12} \quad \text{for marine environments at temperatures up to } 20^\circ\text{C} \end{aligned}$$

If  $da/dN$  versus  $\Delta K$  for an actual crack is plotted on a logarithmic scale, an approximate sigmoidal curve results as shown in Fig. 7.4. Below a threshold stress intensity factor range,  $\Delta K_{\text{th}}$ , no growth occurs. For intermediate values of  $\Delta K$ , growth rate is idealized by a straight line.

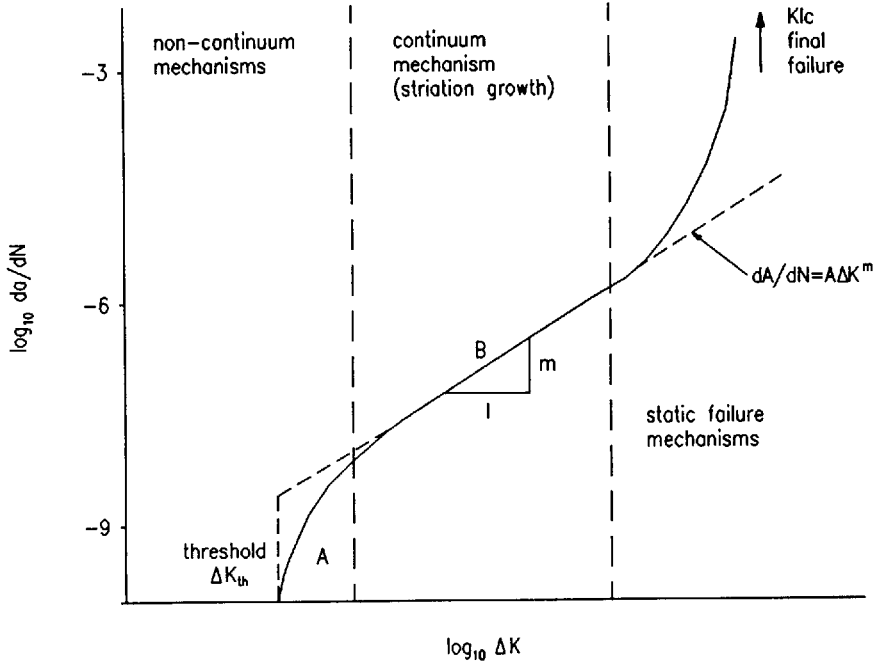


Fig. 7.4 Schematic presentation of crack growth

For a crack at the toe of a welded joint

$$\Delta K = M_K Y \Delta S_r \sqrt{(\pi a)} \tag{7.4}$$

where  $S_r$  = applied stress range

$a$  = crack depth

$Y$  = a correction factor dependent on crack size, shape and loading

$M_K$  = a function which allows for the stress concentration effect of the welded joint and depends on crack site, plate thickness, joint geometry and loading.

Substituting Equation (7.4) in Equation (7.1), rearranging and integrating gives:

$$\int_{a_i}^{a_f} \frac{da}{[M_K Y \sqrt{(\pi a)}]^a} = C A S_r^a N \tag{7.5}$$

where  $a_i$  is the initial crack depth and  $a_f$  is the final crack depth corresponding to failure. Thus, if a welded joint contains a crack or crack-like flaw, equations can be used to predict its fatigue strength, assuming that the life consists of crack growth from a pre-existing crack and the initial crack size is known.

## 7.5 Improvement techniques

### 7.5.1 Introduction

The fatigue performance of a joint can be enhanced by the use of weld improvement techniques. There is a large amount of data available on the influence of weld improvement techniques on fatigue life but as yet little progress has been made into developing practical design rules. Modern steelmaking has led to the production of structural steels with excellent weldability. The low fatigue strength of a welded connection is generally attributed to a short crack initiation period.

An extended crack initiation life can be achieved by:

- (1) reducing the stress concentration of the weld,
- (2) removing crack-like defects at the weld toe,
- (3) reducing tensile welding residual stresses or introducing compressive stresses.

The methods employed fall broadly into two categories as illustrated below:

*weld geometry improvement:* grinding; weld dressing; profile control

*residual stress reduction:* peening; thermal stress relief

Most of the current information relating to weld improvement has been obtained from small-scale specimens. When considering actual structures one important factor is size. In a large structure long range residual stresses due to the assembly of the members are present and will influence the fatigue life. In contrast to small joints where peak stress is limited to the weld toe, the peak stress region in a large multi-pass joint may include several weld beads and cracks may initiate anywhere in this highly stressed area.

However, it is good practice not to seek benefit from improvement techniques in the design office.

#### 7.5.1.1 Grinding

The improvement of the weld toe profile and the removal of slag inclusions can be achieved by grinding either with a rotary burr or with a disc. To obtain the maximum benefit from this type of treatment it is important to extend the grinding to a sufficient depth to remove all small undercuts and inclusions. The degree of improvement achieved increases with the amount of machining carried out and the care taken by the operator to produce a smooth transition.

The performance of toe-ground cruciform specimens is fully investigated in Reference 1. Under freely corroding conditions the benefit from grinding is minimal. However, in air, the results appear to fall on the safe side of the mean curve; endurance is altered by a factor of 2.2. It is therefore recommended that an

increase in fatigue life by a factor of 2.2 can be taken if controlled local machining or grinding is carried out.

### **7.5.1.2 Weld toe remelting**

Weld toe remelting by TIG and plasma arc dressing are performed by remelting the toe region with a torch held at an angle of 50° or 90° to the plate (without the addition of filler material). The difference between TIG and plasma dressing is that the latter requires a higher heat input.

Weld toe remelting can result in large increases in fatigue strength, due to the effect of providing low contact angle in the transition area between the weld and the plate, and by the removal of slag inclusions and undercuts at the toe.

### **7.5.1.3 Hammer peening**

Improved fatigue properties of peened welds are obtained by extensive cold working of the toe region. These improved fatigue properties are due to:

- (1) introduction of high compressive residual stresses,
- (2) a flattening of crack-like defects at the toe,
- (3) an improved toe profile.

It can be shown that weld improvement techniques greatly improve the fatigue life of weldments. For weldments subject to bending and axial loading, peening appears to offer the greatest improvement in fatigue life, followed by grinding and TIG dressing.

## **7.6 Fatigue-resistant design**

The nature of fatigue is well understood and the analytical tools are available to calculate the fatigue life of complex structures. The accuracy of any fatigue life calculation is highly dependent on a good understanding of the expected loading sequence during the whole life of a structure. Once a global pattern has been developed then a more detailed inspection of particular areas of a structure, where the effects of loading may be more important, due to the geometries of joints for example, should be carried out.

Data have been gathered for many years on the performance of bridges, towers, cranes and offshore structures where fatigue is a major design consideration. Codes of Practice such as BS 5400 for bridges and the various offshore codes give details for the estimation of fatigue lives. Where a structure is subjected to fatigue it is important that welded joints are considered carefully. Fatigue and brittle

fractures can be initiated at discontinuities of shape, at notches and cracks which give rise to high local stress. Avoidance of local structural and notch peak stresses by good design is the most effective means of increasing fatigue life. It is important that during the design process consideration is given to the manner in which the structure is to be fabricated. Acute-angled welds of less than  $30^\circ$  are difficult to fabricate, particularly in tubular structures. This could lead to defects in the weld. Furthermore it is also difficult to carry out non-destructive testing on such welds. Despite these problems, some recently designed structures have incorporated such features.

Repairs carried out to structures in service are expensive, and in the worst case may require that a facility is closed down temporarily. Care needs to be taken when specifying secondary attachments to main primary steelwork. These are often not considered in detail during the design process as they themselves are not complex. However, there have been a number of failures in offshore structures due to fatigue crack growth resulting from a welded attachment. The following general suggestions can assist in the development of an appropriate design of a welded structure with respect to fatigue strength:

- (1) Adopt butt or single and double bevel butt welds in preference to fillet welds
- (2) Use double-sided in preference to single-sided fillet welds
- (3) Aim to place weld, particularly toe, root and weld end in area of low stress
- (4) Ensure good welding procedures are adopted and adequate non-destructive testing (NDT) undertaken
- (5) Consider the effects of localized stress concentration factors
- (6) Consider potential effects of residual stresses.

## References to Chapter 7

1. American Society for Testing and Materials (1982) *Design of Fatigue and Fracture Resistant Structures*. ASTM STP 761.
2. British Standards Institution (1980) *Steel, concrete and composite bridges*. Part 10: *Code of practice for fatigue*. BS 5400, BSI, London.
3. Department of Energy (1990) *Offshore Installations: Guidance Design Construction and Certification*, 4th edn. HMSO.
4. British Standards Institution (1983 & 1980) *Rules for the design of cranes*. Part 1: *Specification for classification, stress calculations and design criteria for structures*. Part 2: *Specification for classification, stress calculations and design of mechanisms*. BS 2573, BSI, London.

**Further reading for Chapter 7**

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Gurney T.R. (1979) *Fatigue of Welded Structures*, 2nd edn. Cambridge University Press.

Pellini W.S. (1983) *Guidelines for Fracture-Safe and Fatigue-Reliable Design of Steel Structures*. The Welding Institute.

Radaj D. (1990) *Design and Analysis of Fatigue Resistant Welded Structures*. Abington Publishing.

# Chapter 8

## Brittle fracture

by ROBERT SIMPSON

### 8.1 Introduction

The term brittle fracture is used to describe fast unstable fractures, in contrast to stable fractures of the fatigue type or slow unstable fractures such as plastic yielding. Some metals, such as copper and aluminium, have a crystalline structure that enables them to resist fast fracture under all loading conditions and at all temperatures. This is not the case for many ferrous alloys, particularly structural steels. The consequence of a brittle fracture may be a catastrophic failure; an understanding of the fundamentals of this subject is therefore important for all structural engineers.

The introduction and development of fracture mechanics technology allows the engineer to examine the susceptibility of steel structures, especially their welded joints, to failure assuming a given defect size and operating conditions.

### 8.2 Ductile and brittle behaviour

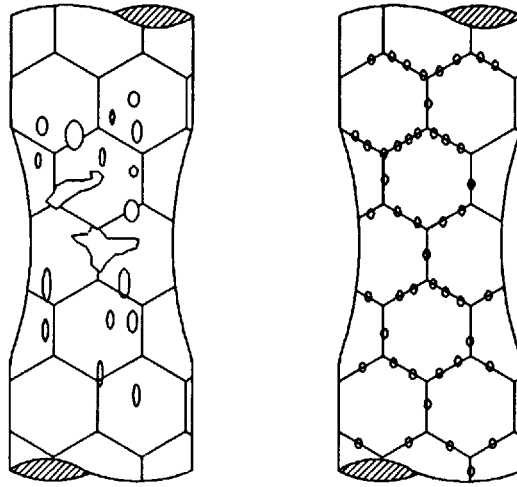
Ductile fracture is normally preceded by extensive plastic deformation. Ductile fracture is slow, and generally results from the formation and coalescence of voids. These voids are often formed at inclusions due to the large tensile stresses set up at the inclusion/metal interface, as seen in Fig. 8.1(a). Ductile fracture usually goes through the grains but, if the density of inclusions or of pre-existing holes is higher on grain boundaries than it is within the grains, then the fracture path may follow the boundaries, giving a fibrous or ductile intergranular fracture. In cases where inclusions are absent, it has been found that voids are formed in severely deformed regions via the presence of localized slip bands and macroscopic instabilities, resulting in either necking or the formation of zones of concentrated shear, as depicted in Fig. 8.1(b).

The fracture path of a ductile crack is often irregular and the presence of a large number of small voids gives the fracture surface a dull fibrous appearance.

The capacity of most metals of engineering interest for plastic deformation and work hardening is extremely valuable as a safeguard against design oversight, accidental overloads or failure by cracking due to fatigue, corrosion or creep.

Brittle fracture is often thought to refer to rapid propagation of cracks without

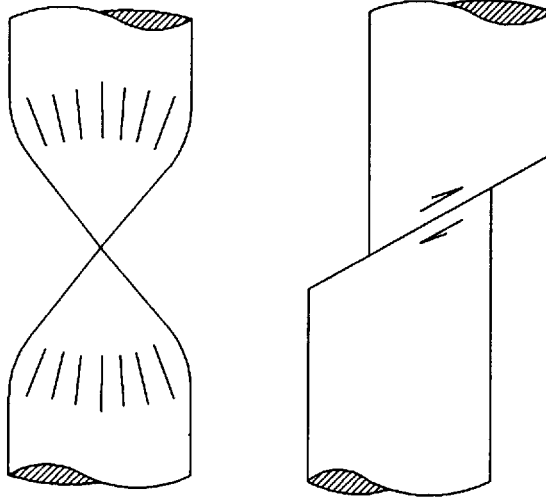




transgranular

intergranular

(a)



necking

shearing

(b)

Fig. 8.1 Plastic deformation (a) by voids growth and coalescence, (b) by necking or shearing

any excessive plastic deformation at a stress level below the yield stress of the material. In practice, however, most brittle fractures show very limited plastic deformation ahead of the crack tip. Brittle fracture may be transgranular (cleavage) or intergranular, as depicted in Fig. 8.2. It is also worth mentioning that metals which often show ductile behaviour can, under certain circumstances, behave in a brittle fashion leading to fast unstable crack growth. This has been clearly demonstrated over the years by some unfortunate accidents involving ships, bridges, offshore structures, gas pipelines, pressure vessels and other major constructions. The Liberty ships and the King Street bridge in Melbourne, Australia, the Sea Gem drilling rig for North Sea gas and the more recent collapse of the Alexander Kielland oil rig are a few examples of the casualties of brittle fracture.

An important feature of steels is the transition temperature between ductile and brittle fracture. Understanding the factors which influence the transition temperature allows designers to be able to select a material which will be ductile at the required operating temperatures for a given structure. This transition is shown in Fig. 8.3: the variation on impact values for small Charpy specimens<sup>1</sup> is plotted against test temperature for a low carbon steel used in offshore applications. BS EN 10025<sup>2</sup> gives temperatures for minimum toughness values to be obtained for a range of structural steel grades.

Impact transition curves are a simple way of defining the effect that variables e.g. heat treatment, alloying elements, effects of welding, etc., have on the fracture behaviour of a steel. Charpy values are useful for quality control but more sophisticated tests<sup>3,4</sup> are required to categorize fully the failure behaviour of

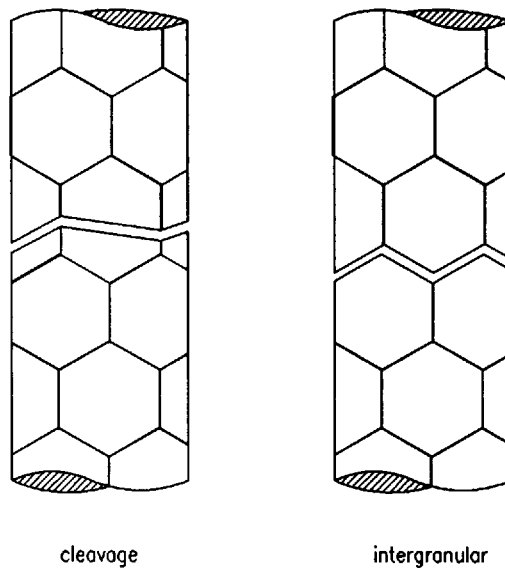


Fig. 8.2 Transgranular and intergranular brittle fracture

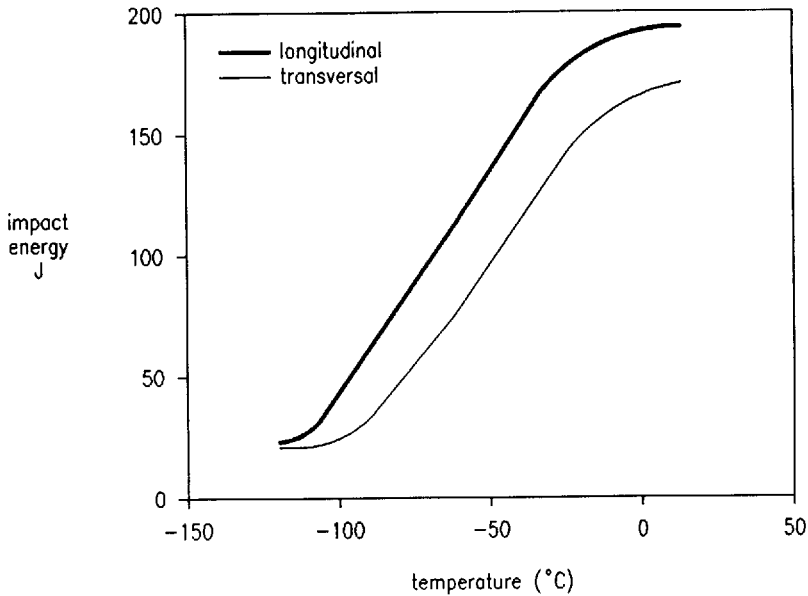


Fig. 8.3 Effects of temperature on impact resistance of steel

a material. Figure 8.4 demonstrates the effect of carbon content on the impact values.

An understanding of the fracture behaviour of steel is particularly important when considering welded structures as welding can considerably reduce the toughness of plate in regions close to the fusion line. This coupled with the likelihood of defects in the weld area can, if not properly controlled, lead to cracking and eventual failure of a joint.

### 8.3 Linear elastic fracture mechanics

A crack in a solid can be stressed in three different modes as shown in Fig. 8.5. Normal stresses give rise to the opening mode denoted as Mode 1. The displacements of the crack surfaces are perpendicular to the plane of the crack. Mode 1 crack opening is the most important in the study of crack growth. If factor  $K$ , the crack tip stress intensity factor, can be derived, it gives the amplitude of the characteristic stress pattern  $K_1$  for Mode 1 crack opening which varies according to applied load, crack size and other geometrical features and can be represented by:

$$K_1 = \sigma \sqrt{(\pi a)} \tag{8.1}$$

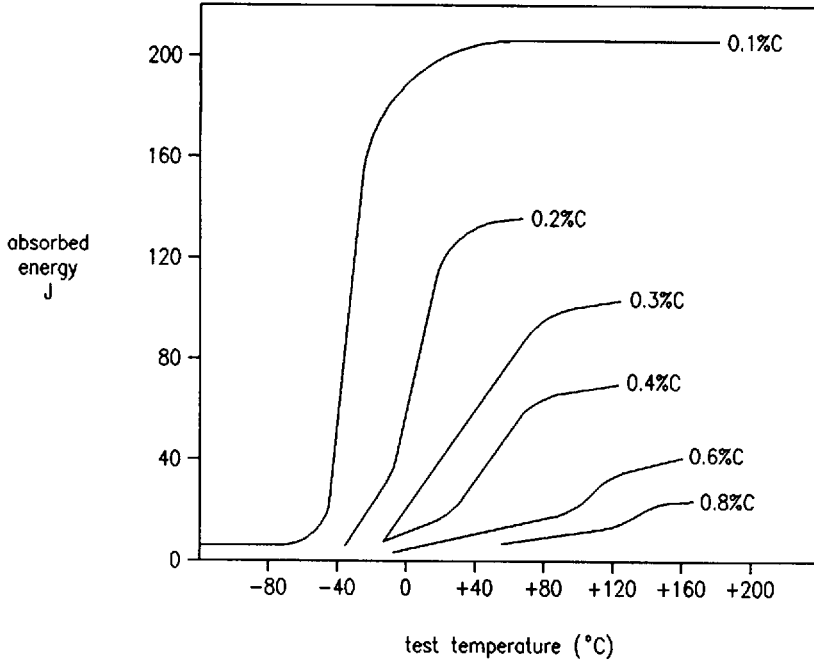


Fig. 8.4 The change in mechanical properties of carbon steels with carbon content

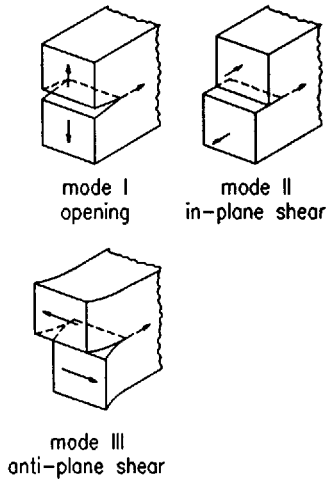


Fig. 8.5 Crack opening modes

where  $\sigma$  is the tensile stress normal to the crack forces and  $a$  is the crack length.

Crack extension will occur when the stresses and strains at the crack tip reach a critical value. This means that fracture will be expected to occur when  $K_I$  reaches a critical value  $K_{Ic}$ .

The fundamental work on fracture mechanics was undertaken by Griffith who published his work in 1924.<sup>5</sup> The basis of his work was to explain why the observed strength of glass was many times lower than the theoretical ultimate strength based on atomic bonding. He postulated that this reduction in strength was due to the presence of small crack-like defects invisible to the naked eye.

Consider an infinite cracked plate of unit thickness with a central transverse crack of length  $2a$ . The plate is stressed to  $\sigma$  and fixed at its ends as in Fig. 8.6. The elastic energy contained in the plate is represented by the area OAB. If the crack extends over a length  $da$  the stiffness of the plate will drop (line OC) which

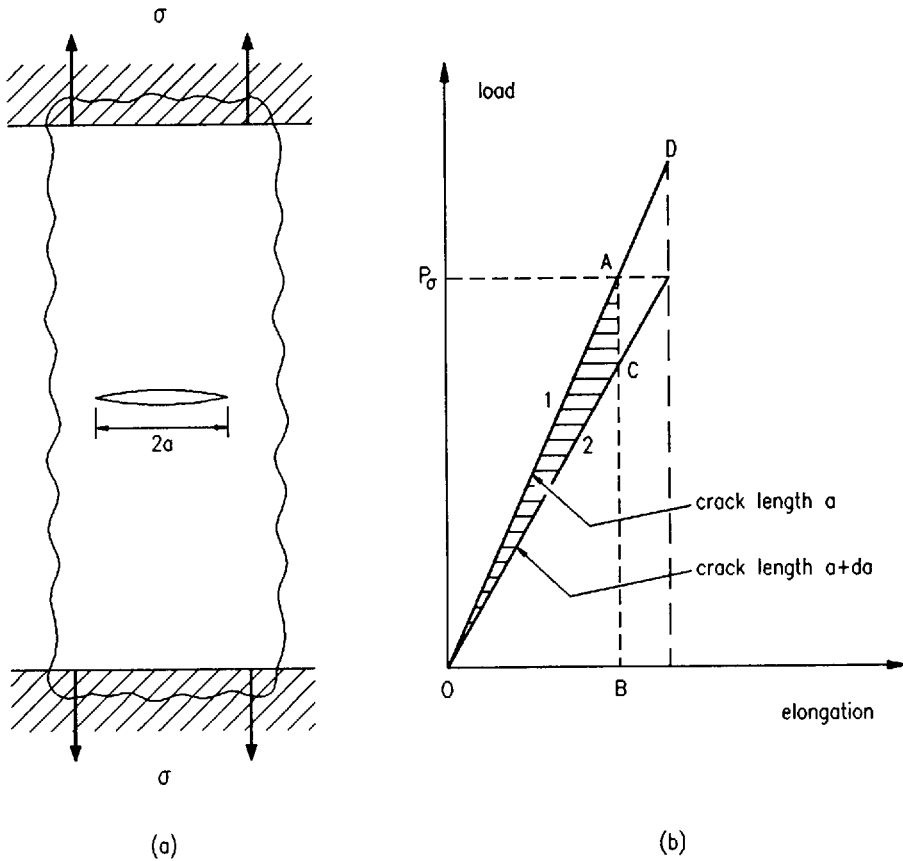


Fig. 8.6 The Griffith criterion for fixed grips. (a) Cracked plate with fixed ends, (b) elastic energy of plate in (a)

means that some load will be relaxed since the ends of the plate are fixed. Consequently, the elastic energy content will drop to a magnitude represented by area OCB. Crack propagation from  $a$  to  $a + da$  will result in an elastic energy release equal in magnitude to area OAC.

If the plate is stressed at a higher stress there is a larger energy release if the crack grows an amount  $da$ . Griffith stated that crack propagation occurs if the energy released upon crack growth is sufficient to provide all the energy that is required for crack growth. If the latter is not the case the stress has to be raised. The triangle ODE represents the amount of energy available if the crack grows.

The condition for crack growth is:

$$\frac{dU}{da} = \frac{dW}{da} \quad (8.2)$$

where  $U$  is the elastic energy and  $W$  is the energy required for crack growth. Based upon stress field calculations for an elliptical flaw by Inglis, Griffiths calculated  $dU/da$  as

$$\frac{dU}{da} = \frac{2\pi\sigma^2 a}{E} \quad (8.3)$$

per unit plate thickness, where  $E$  is Young's modulus. Usually  $dU/da$  is replaced by

$$G = \frac{\pi\sigma^2 a}{E} \quad (8.4)$$

where  $G$  is the so-called 'elastic energy release rate' per crack tip. It is also called the crack driving force: its dimensions of energy per unit plate thickness and per unit crack extension are also the dimensions of force per unit crack extension.

The energy consumed in crack propagation is denoted by  $R = dW/da$  which is called the crack resistance. To a first approximation it can be assumed that the energy required to produce a crack by the decohesion of atomic bonds is the same for each increment  $da$ . This means that  $R$  is a constant.

The energy condition given in Equation (8.2) now states that  $G$  must be at least equal to  $R$  before crack propagation can occur. If  $R$  is a constant, this means that  $G$  must exceed a certain critical value  $G_{1c}$ . Hence crack growth occurs when

$$\frac{\pi\sigma_c^2 a}{E} = G_{1c} \quad \text{or} \quad \sigma_c = \sqrt{\left(\frac{EG_{1c}}{\pi a}\right)} \quad (8.5)$$

The critical energy release rate  $G_{1c}$  can be determined by measuring the stress  $\sigma_c$  required to fracture a plate with a crack of size  $2a$ , and by calculating from Equation (8.5).

Griffith derived his equation for glass which is a very brittle material. Therefore he assumed that  $R$  consisted of surface energy only. In ductile materials, such as metals, plastic deformation occurs at the crack tip. Much work is required in producing a new plastic zone at the tip of the advancing crack. Since this plastic zone has to be produced upon crack growth the energy for its formation can be

considered as energy required for crack propagation. This means that for metals,  $R$  is mainly plastic energy; the surface energy is so small that it can be neglected. The energy criterion is necessary for crack extension. It need not be a sufficient criterion. Even if sufficient energy for crack propagation can be provided, the crack will not propagate unless the material at the crack tip is ready to fail: the material should be at the end of its capacity to take load and to undergo further straining. However, the latter criterion is equivalent to the energy criterion and therefore

$$G = \frac{K^2}{E} \tag{8.6}$$

Apparently the stress criterion and the energy criterion are fulfilled simultaneously. Hence Equations (8.1) and (8.5) are equivalent. It can be shown that Equation (8.6) is valid for plane stress and that a term  $(1 - \nu^2)$  has to be added in the case of plane strain, leading to

$$G_1 = \frac{K_1^2}{(1 - \nu^2)E} \quad \text{and} \quad G_{1c} = \frac{K_{1c}^2}{(1 - \nu^2)E} \tag{8.7}$$

It is found experimentally that the critical value  $K_{1c}$  is dependent on geometric effects of thickness, reaching a minimum value for thick materials under plane strain conditions. The least thickness to give this minimum value is found to be, for material yield stress  $\sigma_y$ ,

$$B \geq 2.5 \left( \frac{K_{1c}}{\sigma_y} \right)^2$$

### 8.4 General yielding fracture mechanics

The need to consider fracture resistance of materials outside the limits of validity of plane strain linear elastic fracture mechanics (LEFM) where the plastic zone size becomes large compared to the critical crack size is important for most engineering designs. To obtain valid  $K_{1c}$  results for relatively tough materials it would be necessary to use a test piece of dimensions so large that they would not be representative of the sections actually in use.

Significant yielding at a crack tip leads to the physical separation of the surfaces of a crack, and the magnitude of this separation is termed crack tip opening displacement (CTOD), and has been given the symbol  $\delta$ . The CTOD approach enables critical toughness test measurements to be made in terms of  $\delta_c$ , and then applied to determine allowable defect sizes for structural components. CTOD design curves have been developed using

$$\begin{aligned} \frac{\delta_c}{2\pi e_y a} &= \left( \frac{e}{e_y} \right)^2 && \text{for } \frac{e}{e_y} \leq 0.5 \\ &= \frac{e}{e_y} - 0.25 && \text{for } \frac{e}{e_y} > 0.5 \end{aligned}$$

where  $\delta_c$  = critical crack tip opening displacement

$a$  = allowable crack size

$e_y$  = material yield strain.

Reference 6 provides procedures for implementing this method.

## 8.5 Material testing

### 8.5.1 Charpy test

Reference 1 specifies the procedure for the Charpy V-notch impact test. The test consists of measuring the energy absorbed in breaking a notched bar specimen by one blow from a pendulum as shown in Fig. 8.7. The test can be carried out at a range of temperatures to determine the transition between ductile and brittle behaviour for the material.

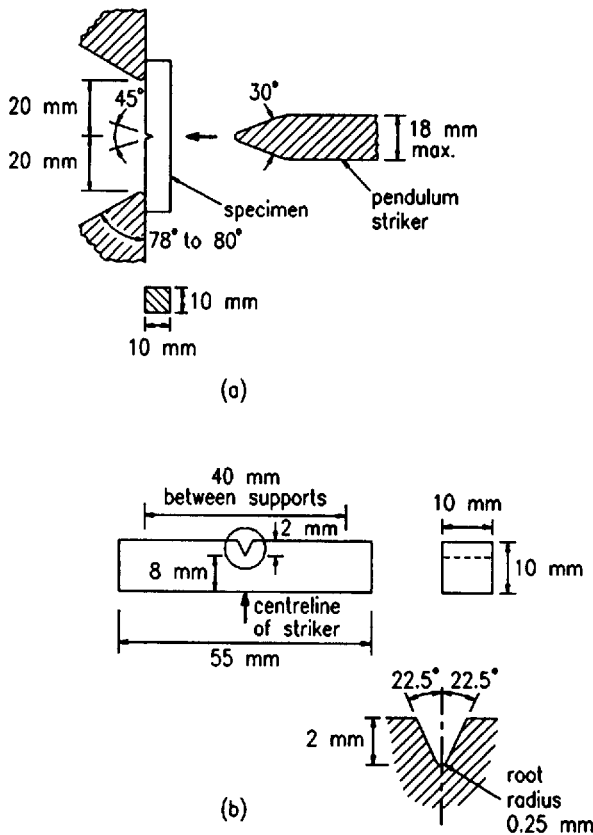


Fig. 8.7 Charpy test. (a) Test arrangement; (b) specimen



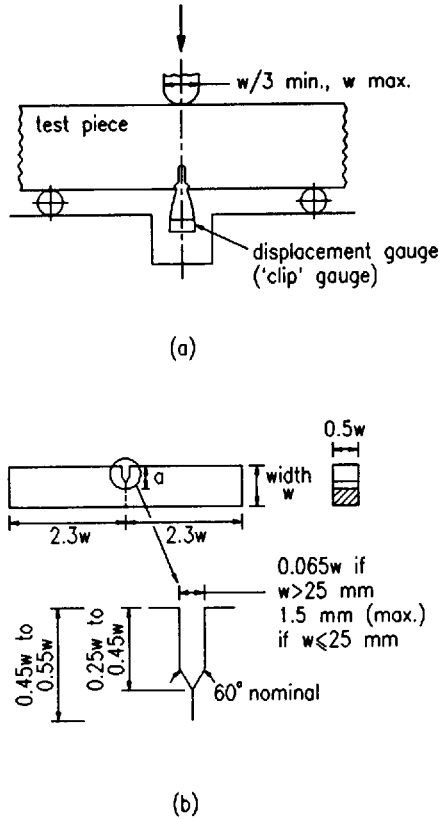


Fig. 8.8 CTOD test. (a) Test arrangement (preferred); (b) typical specimen dimensions

### 8.5.2 Crack tip opening displacement

Reference 4 specifies methods for CTOD tests, including the requirements for specimens, equipment, data analysis and recording of results. Figure 8.8 gives the test specimen dimensions.

The object of the test is to determine crack opening displacement values at the tip of a defect under various loads. The CTOD value is obtained indirectly by a 'clip' gauge suitably calibrated and linked to a data recording facility. The test is carried out in three-point bending over a loading span of  $4w$ .

CTOD tests are conducted on pre-cracked specimens. The procedure for obtaining the crack is outlined in Section 7 of BS 5762: 1979. Once the fatigue crack has been formed it is inspected to ensure compliance with the Code. The test piece is then loaded, typically at a rate of increase of stress intensity factor in the range  $15-80 \text{ N/mm}^{-3/2}$  during the initial elastic stage. The test yields a plot of load versus clip gauge reading, from which the CTOD values can be calculated.

On completion of the test the fracture surface is examined to determine the type of fracture.

### 8.5.3 Other tests

There are other tests that can be carried out such as the wide plate test used for testing welded plate joints which was developed by Wells at the Welding Institute.<sup>7,8</sup> A large full-thickness plate, typically one metre square, is butt welded using the process and treatments to be used in the production weld. This test has the advantage of representing failure of an actual welded joint without the need for machining prior to testing.

While CTOD testing was being developed in the UK an alternative approach, the J integral method, was developed in the USA,<sup>3</sup> mainly for the nuclear industry where operating temperatures are well above the transition temperatures of the materials concerned. A particular difference between the two methods is in the specimen size. The small-scale sample for J integral tests may not adequately predict brittle fracture in real structures.

### 8.5.4 Test specimens

As has already been described each test procedure requires a sample of a certain size. Besides this feature the position of a sample in relation to a weld or, in the case of a thick plate, its position through the thickness is important. In modern structural steels toughness of the parent plate is rarely a problem. However, once a weld is deposited the toughness of the plate surrounding the weld, particularly in the heat-affected zone (HAZ), will be reduced. Although lower than for the parent plate the  $C_v$  or CTOD values that can be obtained should still provide adequate toughness at all standard operating temperatures. In the case of thicker joints then appropriate post-weld heat treatments should be carried out.

## 8.6 Fracture-safe design

The design requirements for steel structures in which brittle fracture is a consideration are given in most structural codes. There are several key factors which need to be considered when determining the risk of brittle fracture in a structure. These are:

- (1) minimum operating temperature
- (2) loading, in particular, rate of loading

- (3) metallurgical features, i.e. parent plate, weld metal, HAZ
- (4) thickness of material to be used.

Each of these factors influences the likelihood of brittle fracture occurring.

From experimental data and parametric studies examining the maximum tolerable defect sizes in steels under various operating conditions, Codes such as BS 5950, BS 5400 and EC3 provide tables giving the maximum permissible thickness of steel at given operating temperatures. Where a design does not fit into these broad categories attempts have been made to use fracture mechanics to provide a criterion for material selection in terms of Charpy test energy absorption. These relationships have been developed for structural steels, as at normal operating temperatures and slow rates of loading valid  $K_{Ic}$  values are not normally obtained. Critical CTOD tests have been widely used in the offshore and nuclear industries. However, all forms of fracture mechanics testing are expensive compared to routine quality control tests such as Charpy testing.

In general, the fracture toughness of structural steel increases with increasing temperature and decreasing loading rates. The effect of temperature on fracture toughness is well known. The effect of loading rate may be equally important not only in designing new structures but in understanding the behaviour of existing ones which may have been built from material with low toughness at their service temperature. The shift in the ductile/brittle transition temperature for structural steels can be considerable when comparing loading rates used in slow bend tests to those in Charpy tests. Results from experimental work have shown that the transition temperature for a BS 4360 grade 50 type steel can change from around 0°C to -60°C with decreasing loading rate.

Materials Standards set limits for the transition temperatures of various steel grades based on Charpy tests. When selecting an appropriate steel for a given structure it must be remembered that the Charpy values noted in the Standards apply to parent plate. Material toughness varies in the weld and heat affected zones of welded joints and where necessary these should be checked for adequate toughness. Furthermore, larger defects may be present in the weld area; appropriate procedures should be adopted to ensure that a welded structure will perform as designed. These could involve non-destructive testing including visual examination. In situations where defects are found, procedures such as those in Reference 6 can be used to assess their significance.

## References to Chapter 8

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## Chapter 9

# Introduction to manual and computer analysis

by RANGACHARI NARAYANAN

### 9.1 Introduction

The analysis of structures consists essentially of mathematical modelling of the response of a structure to the applied loading. Such models are based on idealizations of the structural behaviour of the material and of the components. They are, therefore, imperfect to a larger or smaller degree, depending upon the extent of inaccuracy built into the assumptions in modelling. This is not to imply that the calculations are meaningless, rather to emphasize the fact that the assessment of structural responses is the best estimate that can be obtained in the light of the assumptions implicit in the modelling of the system. Some of these assumptions are necessary in the light of inadequate data; others are introduced to simplify the calculation procedure to economic levels.

There are several idealizations introduced in the modelling process.

- Firstly, the physical dimensions of the structural components are idealized. For example, skeletal structures are represented by a series of line elements and joints are assumed to be of negligible size. The imperfections in the member straightness are ignored or at best idealized.
- Material behaviour is simplified. For example, the stress–strain characteristic is assumed to be linearly elastic, and then perfectly plastic. No account is taken of the variation of yield stress along or across the member. The influence of residual stresses due to thermal processes (such as hot rolling and flame cutting), as well as that due to cold working and roller straightening, is ignored.
- The implications of actions which are included in the analytical process itself are frequently ignored. For example, the development of local plasticity at connections or possible effects of change of geometry causing local instability are rarely, if ever, accounted for in the analysis.

However it must be recognized that the design loads employed in assessing structural response are themselves approximate. The analysis chosen should therefore be adequate for the purpose and should be capable of providing the solutions at an economical cost.

The fundamental concepts employed in mathematical modelling are discussed next.

### 9.1.1 Equations of static equilibrium

From Newton's law of motion, the conditions under which a body remains in static equilibrium can be expressed as follows:

- The sum of the components of all forces acting on the body, resolved along any arbitrary direction is equal to zero. This condition is completely satisfied if the components of all forces resolved along the  $x$ ,  $y$ ,  $z$  directions individually add up to zero. (This can be represented by  $\Sigma P_x = 0$ ,  $\Sigma P_y = 0$ ,  $\Sigma P_z = 0$ , where  $P_x$ ,  $P_y$  and  $P_z$  represent forces resolved in the  $x$ ,  $y$ ,  $z$  directions.) These three equations represent the condition of zero translation.
- The sum of the moments of all forces resolved in any arbitrarily chosen plane about any point in that plane is zero. This condition is completely satisfied when all the moments resolved into  $xy$ ,  $yz$  and  $zx$  planes all individually add up to zero. ( $\Sigma M_{xy} = 0$ ,  $\Sigma M_{yz} = 0$  and  $\Sigma M_{zx} = 0$ .) These three equations provide for zero rotation about the three axes.

If a structure is planar and is subjected to a system of coplanar forces, the conditions of equilibrium can be simplified to *three* equations as detailed below:

- The components of all forces resolved along the  $x$  and  $y$  directions will individually add up to zero ( $\Sigma P_x = 0$  and  $\Sigma P_y = 0$ ).
- The sum of the moments of all the forces about any arbitrarily chosen point in the plane is zero (i.e.  $\Sigma M = 0$ ).

### 9.1.2 The principle of superposition

This principle is only applicable when the displacements are linear functions of applied loads. For structures subjected to multiple loading, the total effect of several loads can be computed as the sum of the individual effects calculated by applying the loads separately. This principle is a very useful tool in computing the combined effects of many load effects (e.g. moment, deflection, etc.). These can be calculated separately for each load and then summed.

## 9.2 Element analysis

Any complex structure can be looked upon as being built up of simpler units or components termed 'members' or 'elements'. Broadly speaking, these can be classified into *three* categories:

- *Skeletal structures* consisting of members whose one dimension (say, length) is much larger than the other two (viz. breadth and height). Such a *line element* is

variously termed as a bar, beam, column or tie. A variety of structures are obtained by connecting such members together using rigid or hinged joints. Should all the axes of the members be situated in one plane, the structures so produced are termed *plane structures*. Where all members are not in one plane, the structures are termed *space structures*.

- Structures consisting of members whose two dimensions (viz. length and breadth) are of the same order but much greater than the thickness, fall into the second category. Such structural elements are called *plated structures*. Such structural elements are further classified as plates and shells depending upon whether they are plane or curved. In practice these units are used in combination with beams or bars. Slabs supported on beams, cellular structures, cylindrical or spherical shells are all examples of plated structures.
- The third category consists of structures composed of members having all the three dimensions (viz. length, breadth and depth) of the same order. The analysis of such structures is extremely complex, even when several simplifying assumptions are made. Dams, massive raft foundations, thick hollow spheres, caissons are all examples of three-dimensional structures.

For the most part the structural engineer is concerned with skeletal structures. Increasing sophistication in available techniques of analysis has enabled the economic design of plated structures in recent years. Three-dimensional analysis of structures is only rarely carried out. Under incremental loading, the initial deformation or displacement response of a steel member is elastic. Once the stresses caused by the application of load exceed the yield point, the cross section gradually yields. The gradual spread of plasticity results initially in an elasto-plastic response and then in plastic response, before ultimate collapse occurs.

### 9.3 Line elements

The deformation response of a line element is dependent on a number of cross-sectional properties such as area,  $A$ , second moment of area ( $I_{xx} = \int y^2 dA$ ;  $I_{yy} = \int x^2 dA$ ) and the product moment of area ( $I_{xy} = \int xy dA$ ). The two axes  $xx$  and  $yy$  are orthogonal. For doubly symmetric sections, the axes of symmetry are those for which  $\int xy dA = 0$ . These are known as *principal axes*. For a plane area, the principal axes may be defined as a pair of rectangular axes in its plane and passing through its centroid, such that the product moment of area  $\int xy dA = 0$ , the co-ordinates referring to the principal axes. If the plane area has an axis of symmetry, it is obviously a principal axis (by symmetry  $\int xy dA = 0$ ). The other axis is at right angles to it, through the centroid of the area.

Tables of properties of the section (including the centroid and shear centre of the section) are available as published data (e.g. SCI Steelwork Design Guide, Vol. 1).<sup>1</sup>

If the section has no axis of symmetry (e.g. an angle section) the principal axes

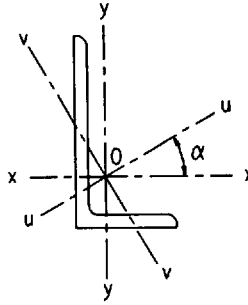


Fig. 9.1 Angle section (no axis of symmetry)

will have to be determined. Referring to Fig. 9.1, if *uou* and *vov* are the principal axes, the angle  $\alpha$  between the *uu* and *xx* axes is given by

$$\tan 2\alpha = \frac{-2 I_{xy}}{I_{xx} - I_{yy}}$$

$$I_{uu} = \frac{I_{xx} + I_{yy}}{2} + \frac{I_{xx} - I_{yy}}{2} \cos 2\alpha - I_{xy} \sin 2\alpha \tag{9.1}$$

$$I_{vv} = \frac{I_{xx} + I_{yy}}{2} - \frac{I_{xx} - I_{yy}}{2} \cos 2\alpha + I_{xy} \sin 2\alpha \tag{9.2}$$

The values of  $\alpha$ ,  $I_{uu}$  and  $I_{vv}$  are available in published Steel Design Guides (e.g. Reference 1).

### 9.3.1 Elastic analysis of line elements under axial loading

When a cross section is subjected to a compressive or tensile axial load,  $P$ , the resulting stress is given by the load/area of the section, i.e.  $P/A$ . Axial load is defined as one acting at the centroid of the section. When loads are introduced into a section in a uniform manner (e.g. through a heavy end-plate), this represents the state of stress throughout the section. On the other hand, when a tensile load is introduced via a bolted connection, there will be regions of the member where stress concentrations occur and plastic behaviour may be evident locally, even though the mean stress across the section is well below yield.

If the force  $P$  is not applied at the centroid, the longitudinal direct stress distribution will no longer be uniform. If the force is offset by eccentricities of  $e_x$  and  $e_y$  measured from the centroidal axes in the  $y$  and  $x$  directions, the equivalent set of actions are (1) an axial force  $P$ , (2) a bending moment  $M_x = P e_x$  in the  $yz$  plane and (3) a bending moment  $M_y = P e_y$  in the  $xz$  plane (see Fig. 9.2). The method of evaluating the stress distribution due to an applied moment is given in



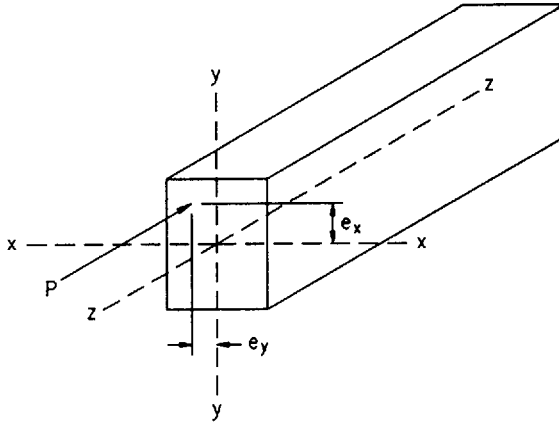


Fig. 9.2 Compressive force applied eccentrically with reference to the centroidal axis

a later section. The total stress at any section can be obtained as the algebraic sum of the stresses due to  $P$ ,  $M_x$  and  $M_y$ .

### 9.3.2 Elastic analysis of line elements in pure bending

For a section having at least one axis of symmetry and acted upon by a bending moment in the plane of symmetry, the Bernoulli equation of bending may be used as the basis to determine both stresses and deflections within the elastic range. The assumptions which form the basis of the theory are:

- The beam is subjected to a pure moment (i.e. shear is absent). (Generally the deflections due to shear are small compared with those due to flexure; this is not true of deep beams.)
- Plane sections before bending remain plane after bending.
- The material has a constant value of modulus of elasticity ( $E$ ) and is linearly elastic.

The following equation results (see Fig. 9.3).

$$\frac{M}{I} = \frac{f}{y} = \frac{E}{R} \quad (9.3)$$

where  $M$  is the applied moment;  $I$  is the second moment of area about the neutral axis;  $f$  is the longitudinal direct stress at any point within the cross section;  $y$  is the distance of the point from the neutral axis;  $E$  is the modulus of elasticity;  $R$  is the radius of curvature of the beam at the neutral axis.

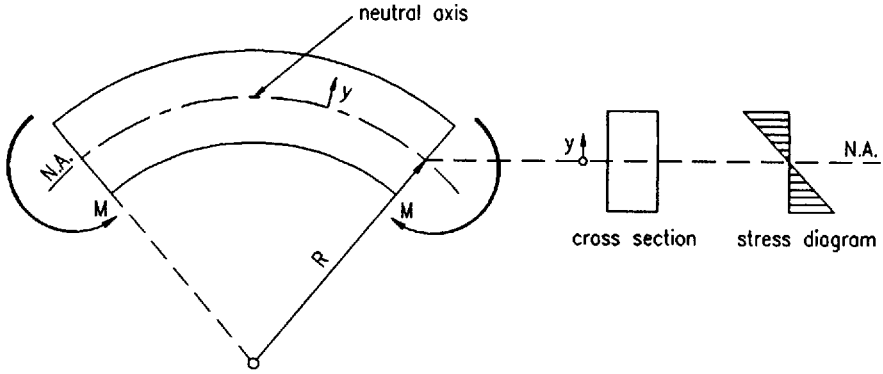


Fig. 9.3 Pure bending

From the above, the stress at any section can be obtained as

$$f = \frac{M y}{I}$$

For a given section (having a known value of  $I$ ) the stress varies linearly from zero at the neutral axis to a maximum at extreme fibres on either side of the neutral axis.

$$f_{\max} = \frac{M y_{\max}}{I} = \frac{M}{Z} \tag{9.4}$$

where  $Z = \frac{I}{y_{\max}}$ .

The term  $Z$  is known as the ‘elastic section modulus’ and is tabulated in section tables.<sup>1</sup> The elastic moment capacity of a given section may be found directly as the product of the elastic section modulus,  $Z$ , and the maximum allowable stress.

If the section is doubly symmetric, then the neutral axis is mid-way between the two extreme fibres. Hence, the maximum tensile and compressive stresses will be equal. For an unsymmetric section, this will not be the case as the value of  $y$  for the two extreme fibres will be different.

For a monosymmetric section, such as the T-section shown in Fig. 9.4, subjected to a moment acting in the plane of symmetry, the elastic neutral axis will be the centroidal axis. The above equations are still valid. The values of  $y_{\max}$  for the two extreme fibres (one in compression and the other in tension) are different. For an applied sagging (positive) moment shown in Fig. 9.4, the extreme fibre stress in the flange will be compressive and that in the stalk will be tensile. The numerical values of the maximum tensile and compressive stresses will differ. In the case sketched in Fig. 9.4, the magnitude of the tensile stress will be greater, as  $y_{\max}$  in tension is greater than that in compression.

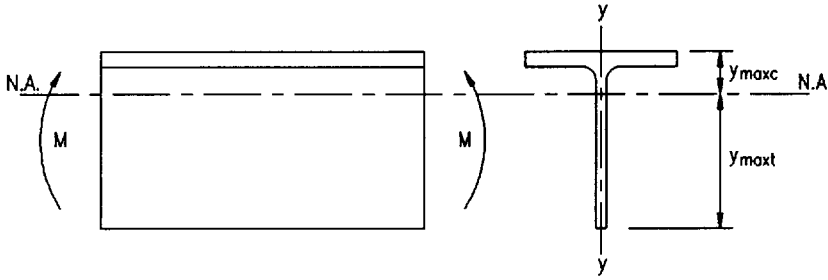


Fig. 9.4 Monosymmetric section subjected to bending

Caution has to be exercised in extending the pure bending theory to asymmetric sections. There are two special cases where no twisting occurs:

- Bending about a principal axis in which no displacement perpendicular to the plane of the applied moment results.
- The plane of the applied moment passes through the shear centre of the cross section.

When a cross section is subjected to an axial load and a moment such that no twisting occurs, the stresses may be determined by resolving the moment into components  $M_{uu}$  and  $M_{vv}$  about the principal axes  $uu$  and  $vv$  and combining the resulting longitudinal stresses with those resulting from axial loading:

$$f_{u,v} = \pm \frac{P}{A} \pm \frac{M_{uu} v}{I_{uu}} \pm \frac{M_{vv} u}{I_{vv}} \quad (9.5)$$

For a section having two axes of symmetry (see Fig. 9.2) this simplifies to

$$f_{x,y} = \pm \frac{P}{A} \pm \frac{M_{xx} y}{I_{xx}} \pm \frac{M_{yy} x}{I_{yy}}$$

Pure bending does *not* cause the section to twist. When the shear force is applied eccentrically in relation to the shear centre of the cross section, the section twists and initially plane sections no longer remain plane. The response is complex and consists of a twist and a deflection with components in and perpendicular to the plane of the applied moment. This is not discussed in this chapter. A simplified method of calculating the elastic response of cross sections subjected to twisting moments is given in an SCI publication.<sup>2</sup>

### 9.3.3 Elastic analysis of line elements subject to shear

Pure bending discussed in the preceding section implies that the shear force applied on the section is zero. Application of transverse loads on a line element

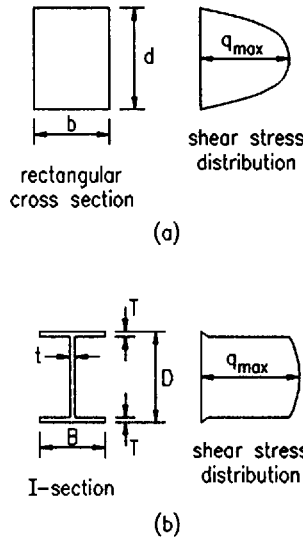


Fig. 9.5 Shear stress distribution: (a) in a rectangular cross section and (b) in an I-section

will, in general, cause a bending moment which varies along its length, and hence a shear force which also varies along the length is generated.

If the member remains elastic and is subjected to bending in a plane of symmetry (such as the vertical plane in a doubly symmetric or monosymmetric beam), then the shear stresses caused vary with the distance from the neutral axis.

For a narrow rectangular cross section of breadth  $b$  and depth  $d$ , subjected to a shear force  $V$  and bent in its strong direction (see Fig. 9.5(a)), the shear stress varies parabolically from zero at the lower and upper surfaces to a maximum value,  $q_{max}$ , at the neutral axis given by

$$q_{max} = \frac{3V}{2bd}$$

i.e. 50% higher than the average value.

For an I-section (Fig. 9.5(b)), the shear distribution can be evaluated from

$$q = \frac{V}{IB} \int_{y=h}^{y=h_{max}} by \, dy \tag{9.6}$$

where  $B$  is the breadth of the section at which shear stress is evaluated. The integration is performed over that part of the section remote from the neutral axis, i.e. from  $y = h$  to  $y = h_{max}$  with a general variable width of  $b$ .

Clearly, for the I-(or T-) section, at the web/flange interface, the value of the integral will remain constant. As the section just inside the web becomes the section just inside the flange, the value of the vertical shear abruptly changes as  $B$  changes from web thickness to flange width.

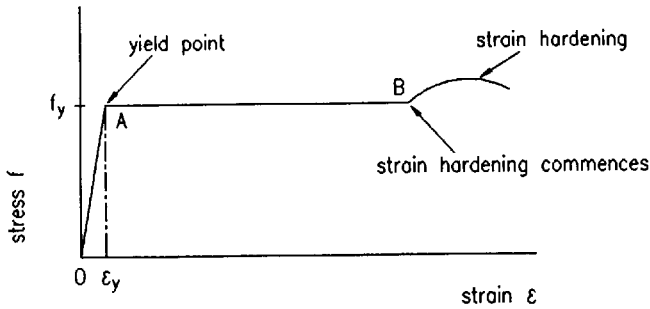


Fig. 9.6 Idealized stress–strain relationship for mild steel

### 9.3.4 Elements stressed beyond the elastic limit

The most important characteristic of structural steels (possessed by no other material to the same degree), is their capacity to withstand considerable deformation without fracture. A large part of this deformation occurs during the process of ‘yielding’, when the steel extends at a constant and uniform stress known as the ‘yield stress’.

Figure 9.6 shows, in its idealized form, the stress–strain curve for structural steels subjected to direct tension. The line 0A represents the elastic straining of the material in accordance with Hooke’s law. From A to B, the material yields while the stress remains constant and is equal to the yield stress,  $f_y$ . The strain occurring in the material during yielding remains after the load has been removed and is called ‘plastic strain’. It is important to note that this plastic strain AB is at least ten times as large as the elastic strain,  $\epsilon_y$ , at yield point.

When subjected to compression, various grades of structural steel behave in a similar manner and display the same property of yield. This characteristic is known as *ductility of steel*.

### 9.3.5 Bending of beams beyond the elastic limit

For simplicity, the case of a beam symmetrical about both axes is considered first. The fibres of the beam subjected to bending are stressed in tension or compression according to their position relative to the neutral axis and are strained as shown in Fig. 9.7.

While the beam remains entirely elastic, the stress in every fibre is proportional to its strain and to its distance from the neutral axis. The stress,  $f$ , in the extreme fibres cannot exceed the yield stress,  $f_y$ .

When the beam is subjected to a moment slightly greater than that which first

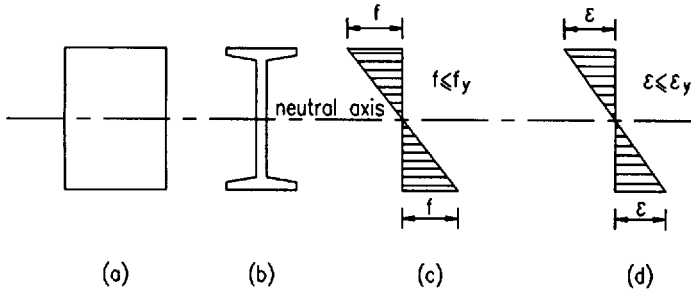


Fig. 9.7 Elastic distribution of stress and strain in a symmetric beam. (a) Rectangular section, (b) I-section, (c) stress distribution for (a) or (b), (d) strain distribution for (a) or (b)

produces yield in the extreme fibres, it does not fail. Instead, the outer fibres yield at constant stress,  $f_y$ , while the fibres nearer to the neutral axis sustain increased elastic stresses. Figure 9.8 shows the stress distribution for beams subjected to such moments. Such beams are said to be 'partially plastic' and those portions of their cross sections which have reached the yield stress are described as 'plastic zones'.

The depths of the plastic zones depend upon the magnitude of the applied moment. As the moment is increased, the plastic zones increase in depth, and, it is assumed that plastic yielding will continue to occur at yield stress,  $f_y$ , resulting in two stress blocks, one zone yielding in tension and one in compression. Figure 9.9 represents the stress distribution in beams stressed to this stage. The plastic zones occupy the whole area of the sections, which are then described as

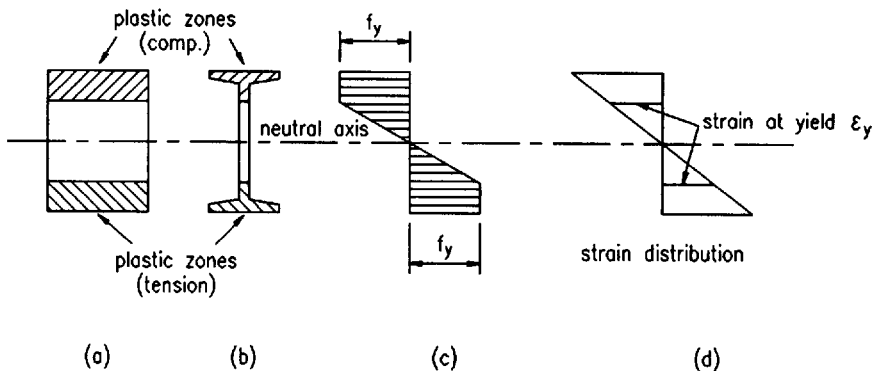


Fig. 9.8 Distribution of stress and strain beyond the elastic limit for a symmetric beam. (a) Rectangular section, (b) I-section, (c) stress distribution for (a) or (b), (d) strain distribution for (a) or (b)

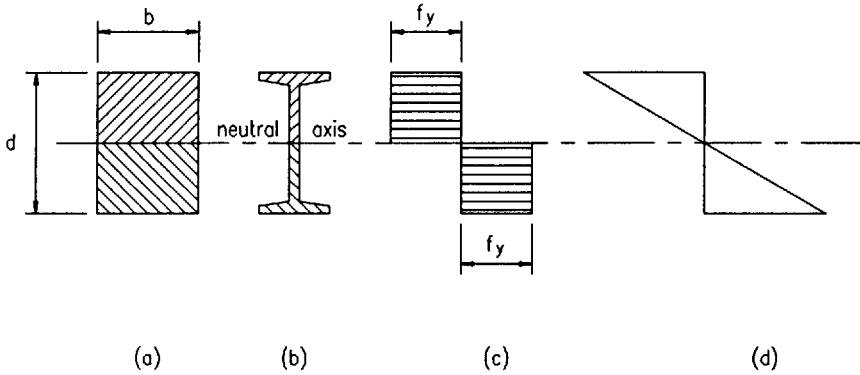


Fig. 9.9 Distribution of stress and strain in a fully plastic cross section. (a) Rectangular section, (b) I-section, (c) stress distribution for (a) or (b), (d) strain distribution for (a) or (b)

being 'fully plastic'. When the cross section of a member is fully plastic under a bending moment, any attempt to increase this moment will cause the member to act as if hinged at that point. This point is then described as a 'plastic hinge'.

The bending moment producing a plastic hinge is called the 'fully plastic moment' and is denoted by  $M_p$ . As the total compressive force and the total tensile force on the cross section must be equal, it follows that the plastic neutral axis is also the equal area axis, i.e. half the area of section is plastic in tension and the other half is plastic in compression. This is true for monosymmetric or unsymmetrical sections as well.

### Shape factor

As described previously there will be two stress blocks, one in tension, the other in compression, each at yield stress. For equilibrium of the cross section, the areas in compression and tension must be equal. For a rectangular section the plastic moment can be calculated as

$$M_p = 2b \frac{d}{2} \frac{d}{4} f_y = \frac{bd^2}{4} f_y$$

which is 1.5 times the elastic moment capacity.

It will be noted that in developing this increased moment, there is large straining in the external fibres of the section together with large rotations and deflections. The behaviour may be plotted as a moment-rotation curve. Curves for various sections are shown in Fig. 9.10.

The ratio of the plastic modulus,  $S$ , to the elastic modulus,  $Z$ , is known as the shape factor,  $v$ , and it will govern the point in the moment-rotation curve when

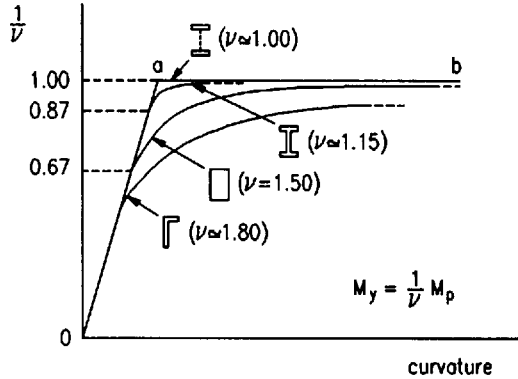


Fig. 9.10 Moment-rotation curves

non-linearity starts. For the ideal section in bending, i.e. two flange plates, this will have a value of unity. The value increases for more material at the centre of the section. For a universal beam, the value is about 1.15 increasing to 1.5 for a rectangle.

*Plastic hinges and rigid plastic analysis*

In deciding the manner in which a beam may fail it is desirable to understand the concept of how plastic hinges form when the beam becomes fully plastic. The number of hinges necessary for failure does not vary for a particular structure subject to a given loading condition, although a part of a structure may fail independently by the formation of a smaller number of hinges. The member or structure behaves in the manner of a hinged mechanism and in doing so, adjacent hinges rotate in opposite directions.

As the plastic deformations at collapse are considerably larger than elastic ones, it is assumed that the line element remains rigid between supports and hinge positions i.e. all plastic rotation occurs at the plastic hinges.

Considering a simply-supported beam subjected to a point load at mid-span (Fig. 9.11), the maximum strain will take place at the centre of the span where a plastic hinge will be formed at yield of full section. The remainder of the beam will remain straight: thus the entire energy will be absorbed by the rotation of the plastic hinge.

Work done at the plastic hinge =  $M_p (2\theta)$

Work done by the displacement of the load =  $W \left( \frac{L}{2} \theta \right)$



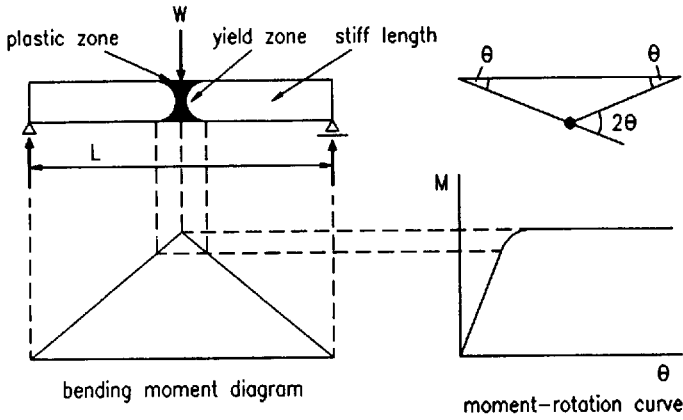


Fig. 9.11 Centrally-loaded simply-supported beam

At collapse, these two must be equal

$$2M_p \theta = \frac{WL}{2} \theta$$

$$W = 4M_p/L \quad \text{or} \quad M_p = WL/4$$

The moment at collapse of an encastré beam with a uniformly distributed load ( $w = W/L$ ), is worked out in a manner similar to the above from Fig. 9.12.

$$\text{Work done at the three plastic hinges} = M_p (\theta + 2\theta + \theta) = 4M_p \theta$$

$$\text{Work done by the displacement of the load } (W) = \frac{WL}{L} \frac{L}{2} \frac{L}{2} \theta = \frac{WL}{4} \theta$$

Equating the two,

$$\frac{WL}{4} \theta = 4M_p \theta$$

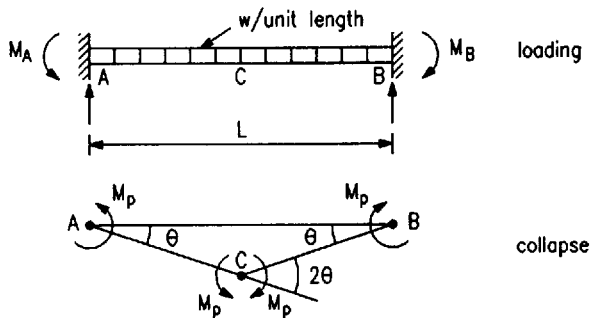


Fig. 9.12 Encastré beam with a uniformly distributed load

$$W = 16 M_p/L$$

or  $M_p = WL/16$

The moments at collapse for other conditions of loading can be worked out by a similar procedure.

### 9.3.6 Load factor and theorems of plastic collapse

The load factor at rigid plastic collapse,  $\lambda_p$ , is defined as the lowest multiple of the design loads which will cause the whole structure, or any part of it, to become a mechanism.

In the limit-state approach, the designer seeks to ensure that at the appropriate factored loads the structure will *not* fail. Thus the rigid plastic load factor,  $\lambda_p$ , must not be less than unity, under factored loads.

The number of independent mechanisms,  $n$ , is related to the number of possible plastic hinge locations,  $h$ , and the degree of redundancy,  $r$ , of the skeletal structure, by the equation

$$n = h - r$$

The three theorems of plastic collapse are given below for reference

(1) *Lower bound or static theorem*

A load factor,  $\lambda_s$ , computed on the basis of an *arbitrarily assumed* bending moment diagram which is *in equilibrium with the applied loads and where the fully plastic moment of resistance is nowhere exceeded*, will always be less than, or at best equal to, the load factor at rigid plastic collapse,  $\lambda_p$ .

$\lambda_p$  is the highest value of  $\lambda_s$  which can be found.

(2) *Upper bound or kinematic theorem*

A load factor,  $\lambda_k$ , computed on the basis of an *arbitrarily assumed* mechanism will always be greater than, or at best equal to, the load factor at rigid plastic collapse,  $\lambda_p$ .

$\lambda_p$  is the lowest value of  $\lambda_k$  which can be found.

(3) *Uniqueness theorem*

If *both* the above criteria ((1) and (2)) are satisfied, then  $\lambda = \lambda_p$ .

### 9.3.7 Effect of axial load and shear

If a member is subjected to the combined action of bending moment and axial force, the plastic moment capacity will be reduced.

The presence of an axial load implies that the sum of the tension and compression forces in the section is not zero (see Fig. 9.13). This means that the neutral axis

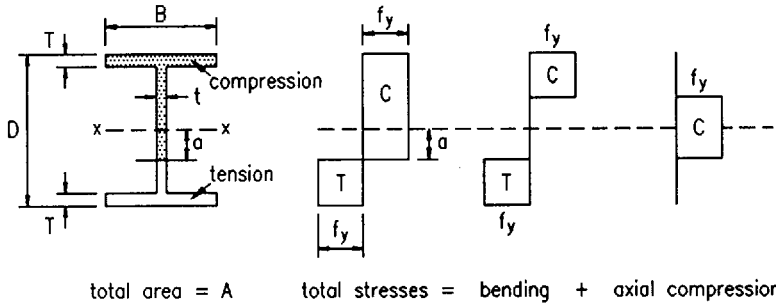


Fig. 9.13 The effect of combined bending and compression

moves away from the equal area axis providing an additional area in tension or compression depending on the type of axial load. The presence of shear forces will also reduce the moment capacity. For the beam sketched in Fig. 9.13,

$$\text{axial load resisted} = 2a t f_y$$

Defining 
$$n = \frac{\text{axial force resisted}}{\text{axial capacity of section}} = \frac{2at}{A},$$

$$a = \frac{n A}{2t}$$

For a given cross section, the plastic moment capacity,  $M_p$ , can be evaluated as explained previously. The reduced moment capacity,  $M'_p$ , in the presence of the axial load can be calculated as follows:

$$\begin{aligned} M'_p &= M_p - t a^2 f_y \\ &= M_p - t \frac{n^2 A^2}{4t^2} f_y = \left( S - \frac{n^2 A^2}{4t} \right) f_y \end{aligned} \tag{9.7}$$

where  $S$  is the plastic modulus of the section.

Section tables provide the moment capacity for available steel sections using the approach given above.<sup>1</sup> Similar expressions will be obtained for minor axis bending.

### 9.3.8 Plastic analysis of beams subjected to shear

Once the material in a beam has started to yield in a longitudinal direction, it is unable to sustain applied shear. When a shear,  $V$ , and an applied moment,  $M$ , are applied simultaneously to an I-section, a simplifying assumption is employed to reduce the complexity of calculations; shear resistance is assumed to be provided by the web, hence the shear stress in the web is obtained as a constant value of  $V$  divided by the web area (see Fig. 9.14). The longitudinal direct stress to cause

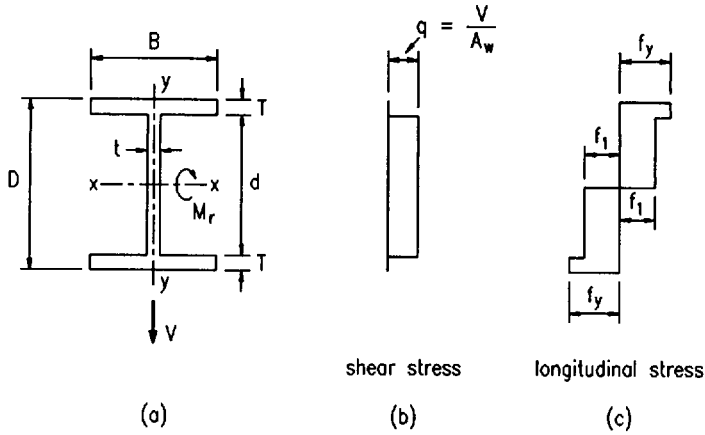


Fig. 9.14 Combined bending and shear

yield,  $f_1$ , in the presence of this shear stress,  $q$ , is obtained by using the von Mises yield criterion.<sup>3</sup>

$$f_y^2 = f_1^2 + 3q^2$$

The reduced plastic moment capacity is given by

$$M_r = M_p - \left( \frac{f_y - f_1}{f_y} \right) M_{pw} \tag{9.8}$$

where  $M_{pw}$  is the fully plastic moment of resistance of the web.

The addition of an axial load to the above condition can be dealt with by shifting the neutral axis as was done in Fig. 9.13. The web area required to carry the axial load is now given by  $P/f_1$  and the depth of the web,  $d_a$ , corresponding to this is given by

$$d_a = \frac{P}{f_1 t_w}$$

A further reduction in moment due to the introduction of the axial load is given by

$$\frac{t_w d_a^2 f_1}{4}$$

Hence the reduced moment capacity of the section is given by

$$M_1 = M_p - \left( \frac{f_y - f_1}{f_y} \right) M_{pw} - \frac{t_w d_a^2 f_1}{4} \tag{9.9}$$

where  $f_1 = \sqrt{(f_y^2 - 3q^2)}$ .

### 9.3.9 Plastic analysis for more than one condition of loading

When more than one condition of loading is to be applied to a line element, it may not always be obvious which is critical. It is necessary then to perform separate calculations, one for each loading condition, the section being determined by the solution requiring the largest plastic moment.

Unlike the elastic method of design in which moments produced by different loading systems can be added together, the opposite is true for the plastic theory. Plastic moments obtained by different loading systems *cannot* be combined, i.e. the plastic moment calculated for a given set of loads is only valid for that loading condition. This is because the 'principle of superposition' becomes *invalid* when parts of the structure have yielded.

## 9.4 Plates

Most steel structures consist of members which can be idealized as line elements. However, structural components having significant dimensions in two directions (viz. plates) are also encountered frequently. In steel structures, plates occur as components of I-, H-, T- or channel sections as well as in structural hollow sections. Sheets used to enclose lift shafts or walls or cladding in framed structures are also examples of plates.

With plane sheets, the stiffness and strength in all directions is identical and the plate is termed 'isotropic'. This is no longer true when stiffeners or corrugations are introduced in one direction. The stiffnesses of the plate in the  $x$  and  $y$  directions are substantially different. Such a plate is termed 'orthotropic'.

The  $x$  and  $y$  axes for the analysis of the plate are usually taken in the plane of the plate, as shown in Fig. 9.15, while the  $z$  axis is perpendicular to that plane. An element of the plate will be subjected to six stress components, viz. *three* direct stresses ( $\sigma_x$ ,  $\sigma_y$  and  $\sigma_z$ ) and *three* shear stresses ( $\tau_{xy}$ ,  $\tau_{yz}$  and  $\tau_{zx}$ ). There are

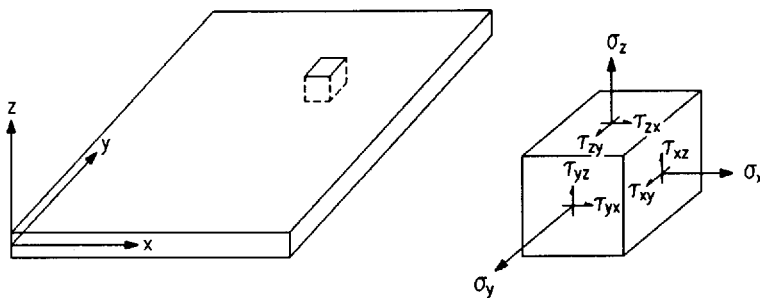


Fig. 9.15 Stress components on an element

six corresponding strains, viz. three direct strains ( $\epsilon_x$ ,  $\epsilon_y$  and  $\epsilon_z$ ) and three shear strains ( $\gamma_{xy}$ ,  $\gamma_{yz}$  and  $\gamma_{zx}$ ). These stresses and strains are related in the elastic region by the material properties Young's modulus ( $E$ ) and Poisson's ratio ( $\nu$ ).

When considering the response of the plate, the approach customarily employed is termed 'plane stress idealization'. As the thickness,  $t$ , of the plate is small compared with its other two dimensions in the  $x$  and  $y$  directions, the stresses having components in the  $z$  direction are negligible (i.e.  $\sigma_z$ ,  $\tau_{yz}$  and  $\tau_{zx}$  are all zero). This implies that the out-of-plane displacement is *not* zero and this condition is referred to as plane stress idealization.

For an isotropic plate, the general equation relating the displacement,  $w$ , perpendicular to the plane of the plate element is given by

$$\frac{\partial^4 w}{\partial x^4} + 2\frac{\partial^4 w}{\partial x^2 \partial y^2} + \frac{\partial^4 w}{\partial y^4} = \frac{q}{D} \quad (9.10)$$

where  $q$  is the normal applied load per unit area in the  $z$  direction which will, in general, vary with  $x$  and  $y$ . The term  $D$  is the flexural rigidity of the plate, given by

$$D = \frac{E t^3}{12 (1 - \nu^2)} \quad (9.11)$$

The main difficulty in using this approach lies in the choice of a suitable displacement function,  $w$ , which satisfies the boundary conditions. For loading conditions other than the simplest, an exact solution of this differential equation is virtually impossible. Hence approximate methods (e.g. multiple Fourier series) are utilized. Once a satisfactory displacement function,  $w$ , is obtained, the moments per unit width of the plate may be derived from

$$\begin{aligned} M_x &= -D \left( \frac{\partial^2 w}{\partial x^2} + \nu \frac{\partial^2 w}{\partial y^2} \right) \\ M_y &= -D \left( \frac{\partial^2 w}{\partial y^2} + \nu \frac{\partial^2 w}{\partial x^2} \right) \\ M_{xy} &= -M_{yx} = D (1 - \nu) \frac{\partial^2 w}{\partial x \partial y} \end{aligned} \quad (9.12)$$

For orthotropic plates, the stiffness in  $x$  and  $y$  directions is different and the equations are suitably modified as given below

$$D_x \frac{\partial^4 w}{\partial x^4} + 2D_{xy} \frac{\partial^4 w}{\partial x^2 \partial y^2} + D_y \frac{\partial^4 w}{\partial y^4} = q \quad (9.13)$$

where  $D_x$  and  $D_y$  are the flexural rigidities in the two directions.

In view of the difficulty of using classical methods for the solution of plate problems, finite element methods have been developed in recent years to provide satisfactory answers.

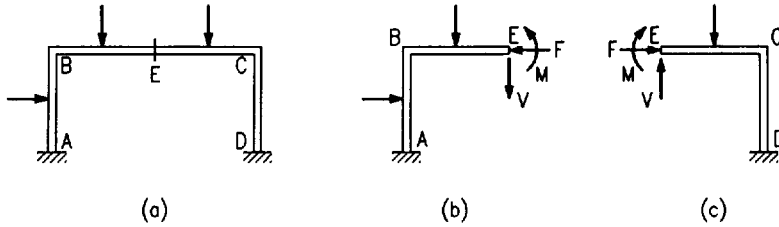


Fig. 9.16 Free body diagram

## 9.5 Analysis of skeletal structures

The evaluation of the stress resultants in members of skeletal frames involves the solution of a number of simultaneous equations. When a structure is in equilibrium, every element or constituent part of it is also in equilibrium. This property is made use of in developing the concept of the *free body diagram* for elements of a structure.

The portal frame sketched in Fig. 9.16 will now be considered for illustrating the concept. Assuming that there is an imaginary cut at E on the beam BC, the part ABE continues to be in equilibrium if the two forces and moment which existed at section E of the uncut frame are applied externally. The internal forces which existed at E are given by (1) an axial force  $F$ , (2) a shear force  $V$  and (3) a bending moment  $M$ . These are known as 'stress resultants'. The external forces on ABE, together with the forces  $F$ ,  $V$  and  $M$ , keep the part ABE in equilibrium; Fig. 9.16(b) is called the free body diagram. On a rigid jointed plane frame there are three stress resultants at each imaginary cut. The part ECD must also remain in equilibrium. This consideration leads to a similar set of forces  $F$ ,  $V$  and  $M$  shown in Fig. 9.16(c). It will be noted that the forces acting on the cut face E are equal and opposite. If the two free body diagrams are moved towards each other, it is obvious the internal forces  $F$ ,  $V$  and  $M$  cancel out and the structure is restored to its original state of equilibrium. As previously stated, equilibrium implies  $\Sigma P_x = 0$ ;  $\Sigma P_y = 0$ ;  $\Sigma M = 0$  for a planar structure. These equations can be validly applied by considering the structure as a whole, or by considering the free body diagram of a part of a structure.

In a similar manner, it can be seen that a three-dimensional rigid-jointed frame has six stress resultants across each section. These are, the axial force, two shears in two mutually perpendicular directions and three moments, as shown in Fig. 9.17.

With pin-jointed frames, be they two- or three-dimensional, there is only one stress resultant per member, viz. its axial load. When forces act on an elastic structure, it undergoes deformations, causing displacements at every point within the structure.

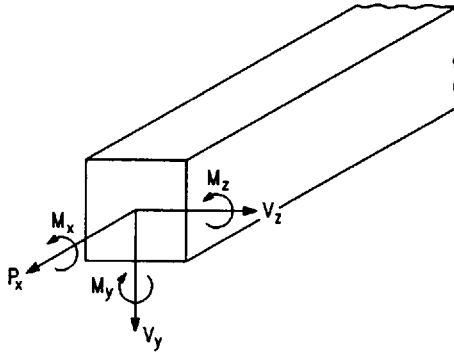


Fig. 9.17 Force and moments in  $x$ ,  $y$  and  $z$  directions

The solution of forces in the frames is accomplished by relating the stress resultants to the displacements. The number of equations needed is governed by the 'degrees of freedom', i.e. the number of possible component displacements. At one end of the member of a pin-jointed plane frame, the member displacement has translational components in the  $x$  and  $y$  directions only, and no rotational displacement. The number of degrees of freedom is two. By similar reasoning it will be apparent that the number of degrees of freedom for a rigid-jointed plane frame member is three. For a member of a three-dimensional pin-jointed frame, it is also three, and for a similar rigid-jointed frame, it is six.

### 9.5.1 Stiffness and flexibility

Forces and displacements have a vital and interrelated role in the analysis of structures. Forces cause displacements and the occurrence of displacements implies the existence of forces. The relationship between forces and displacements is defined in one of two ways, viz. *flexibility* and *stiffness*.

*Flexibility* gives a measure of displacements associated with a given set of forces acting on the structure. This concept will be illustrated by considering the example of a spring loaded at one end by a static load  $P$  (see Fig. 9.18).

As the spring is linearly elastic, the extension,  $\Delta$ , produced is directly proportional to the applied load,  $P$ . The deflection produced by a unit load (defined as the *flexibility* of the spring) is obviously  $\Delta/P$ . Figure 9.18(b) illustrates the deflection response of a beam to an applied load  $P$ . Once again the flexibility of the beam is  $\Delta/P$ .

In the simple cases considered above, flexibility simply gives the load–displacement response at a point. A more generalized definition applicable to the displacement response at a number of locations will now be obtained by considering a beam sketched in Fig. 9.19.



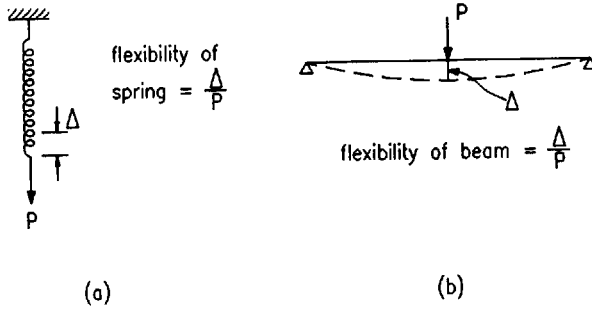


Fig. 9.18 Flexibility

Considering a unit load acting at point 1 (Fig. 9.19(b)), the corresponding deflections at points 1, 2 and 3 are denoted as  $f_{11}$ ,  $f_{21}$  and  $f_{31}$  (the first subscript denotes the point at which the deflection is measured; the second subscript refers to the point at which the unit load is applied). The terms  $f_{11}$ ,  $f_{21}$ ,  $f_{31}$  are called flexibility coefficients. Figure 9.19(c) and (d) give the corresponding flexibility

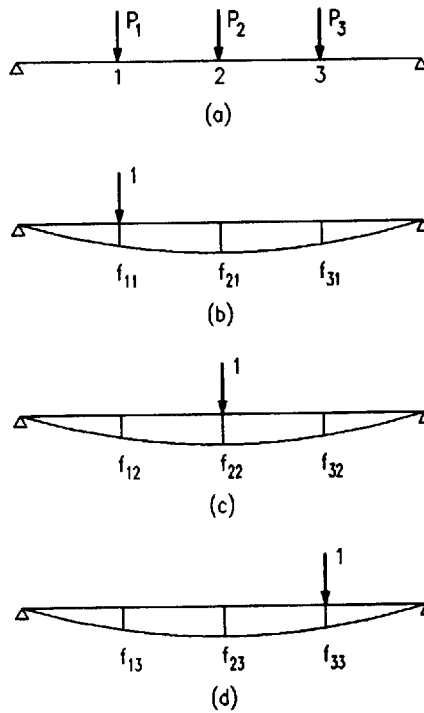


Fig. 9.19 Flexibility coefficients for a loaded beam

coefficients for load positions 2 and 3 respectively. By the principle of superposition, the total deflections at points 1, 2 and 3 due to  $P_1$ ,  $P_2$  and  $P_3$  can be written as

$$\begin{aligned} \Delta_1 &= P_1 f_{11} + P_2 f_{12} + P_3 f_{13} \\ \Delta_2 &= P_1 f_{21} + P_2 f_{22} + P_3 f_{23} \\ \Delta_3 &= P_1 f_{31} + P_2 f_{32} + P_3 f_{33} \end{aligned}$$

Written in matrix form, this becomes

$$\begin{Bmatrix} \Delta_1 \\ \Delta_2 \\ \Delta_3 \end{Bmatrix} = \begin{bmatrix} f_{11} & f_{12} & f_{13} \\ f_{21} & f_{22} & f_{23} \\ f_{31} & f_{32} & f_{33} \end{bmatrix} \begin{Bmatrix} P_1 \\ P_2 \\ P_3 \end{Bmatrix} \tag{9.14}$$

or  $\{\Delta\} = [F] \{P\}$

where  $\{\Delta\}$  = displacement matrix  
 $[F]$  = flexibility matrix relating displacements to forces  
 $\{P\}$  = force matrix

Hence  $\{P\} = [F]^{-1} \{\Delta\}$

*Stiffness* is the inverse of flexibility and gives a measure of the forces corresponding to a given set of displacements. Considering the spring illustrated in Fig. 9.18(a), it is noted that the deflection response is directly proportional to the applied load,  $P$ . The force corresponding to unit displacement is obviously  $P/\Delta$ . Likewise in Fig. 9.18(b), the load to be applied on the beam to cause a unit displacement at a point below the load is  $P/\Delta$ . In its simplest form, stiffness coefficient refers to the load corresponding to a unit displacement at a given point and can be seen to be the reciprocal of flexibility. The concept is explained further using Fig. 9.20.

First the locations 2 and 3 are restrained from movement and a unit displacement is given at 1. This implies a downward force  $k_{11}$  at 1, an upward force  $k_{21}$  at 2 and a downward force  $k_{31}$  at 3. The forces at points 2 and 3 are necessary as otherwise there will be displacements at the locations 2 and 3.

The forces  $k_{11}$ ,  $k_{21}$  and  $k_{31}$  are designated as stiffness coefficients. In a similar manner, the stiffness coefficients corresponding to unit displacements at points 2 and 3 are obtained.

The stiffness coefficients and the corresponding forces are linked by the following equations

$$\begin{aligned} P_1 &= k_{11} \Delta_1 + k_{12} \Delta_2 + k_{13} \Delta_3 \\ P_2 &= k_{21} \Delta_1 + k_{22} \Delta_2 + k_{23} \Delta_3 \\ P_3 &= k_{31} \Delta_1 + k_{32} \Delta_2 + k_{33} \Delta_3 \end{aligned}$$

or  $\begin{Bmatrix} P_1 \\ P_2 \\ P_3 \end{Bmatrix} = \begin{bmatrix} k_{11} & k_{12} & k_{13} \\ k_{21} & k_{22} & k_{23} \\ k_{31} & k_{32} & k_{33} \end{bmatrix} \begin{Bmatrix} \Delta_1 \\ \Delta_2 \\ \Delta_3 \end{Bmatrix} \tag{9.15}$

or  $\{P\} = [K] \{\Delta\}$

where  $[K]$  is the stiffness matrix relating forces and displacements.

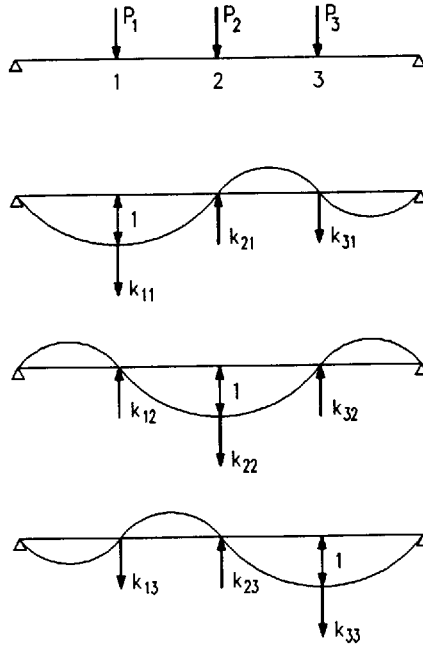


Fig. 9.20 Stiffness coefficients

### 9.5.2 Introduction to statically indeterminate skeletal structures

A structure for which the external reactions and internal forces and moments can be computed by using only the three equations of statics ( $\Sigma P_x = 0$ ,  $\Sigma P_y = 0$  and  $\Sigma M = 0$ ) is known as ‘statically determinate’. A structure for which the forces and moments cannot be computed from the principles of statics alone is ‘statically indeterminate’. Examples of statically determinate skeletal structures are shown in Fig. 9.21.

In structures shown in Fig. 9.21(a), (b) and (c), the supporting forces and moments are just sufficient in number to withstand the external loading. For example, if one of the supports of (b) were to fail or if one of the members of (c) were to be removed, the structure would collapse.

However, when the beam or frame is provided with additional supports (see Fig. 9.21(d), (e)) or if the pin-jointed truss has more members than are required to make it ‘perfect’ (Fig. 9.21b), the structure becomes statically indeterminate.

The degree of indeterminacy (also termed ‘the degree of redundancy’) is obtained by the number of member forces or reaction components (viz. moments or forces) which should be ‘released’ to convert a statically indeterminate structure to a determinate one. If  $n$  forces or moments are required to be so released, the

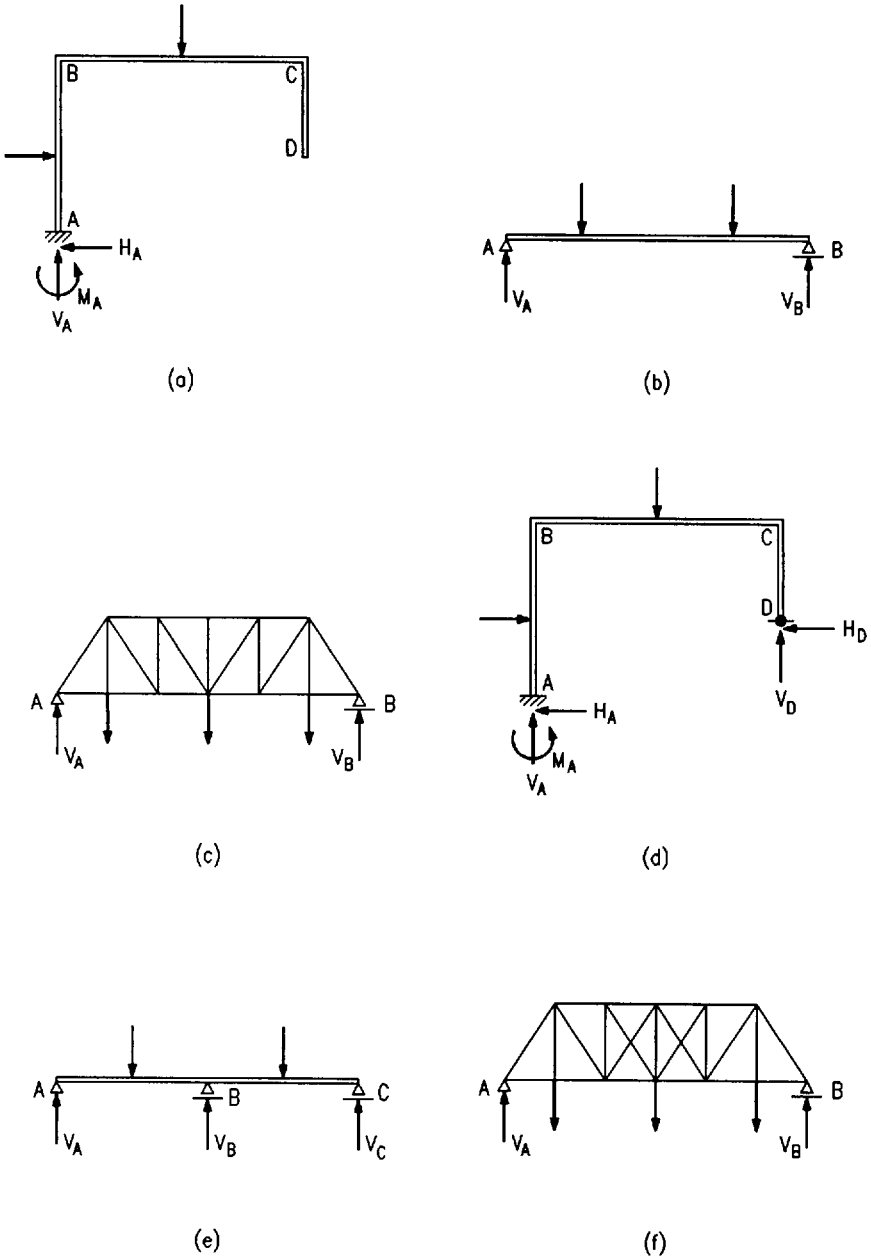


Fig. 9.21 Statically determinate and indeterminate skeletal structures. (a), (b) and (c) are determinate; (d), (e) and (f) are indeterminate

degree of indeterminacy is  $n$ . We need  $n$  independent equations (in addition to three equations of statics for a planar structure) to solve for forces and moments at all locations in the structure. The additional equations are usually written by considering the deformations or displacements of the structure. This means that the section properties (viz. area, second moment of area, etc.) have an important effect in evaluating the forces and moments of an indeterminate structure. Also, the settlement of a support or a slight lack of fit in a pin-jointed structure contributes materially to the internal forces and moments of an indeterminate structure.

### 9.5.3 The area moment method

The simplest technique of analyzing a beam which is indeterminate to a low degree is by the area moment method. The method is based on two theorems (see Fig. 9.22):

- *Area Moment Theorem 1:* The change in slope (in radians) between two points of the deflection curve in a loaded beam is numerically equal to the area under the  $M/EI$  diagram between these two points.
- *Area Moment Theorem 2:* The vertical intercept on any chosen line between the tangents drawn to the ends of any portion of a loaded beam, which was originally straight and horizontal, is numerically equal to the first moment of the area under the  $M/EI$  diagram between the two ends taken about that vertical line.

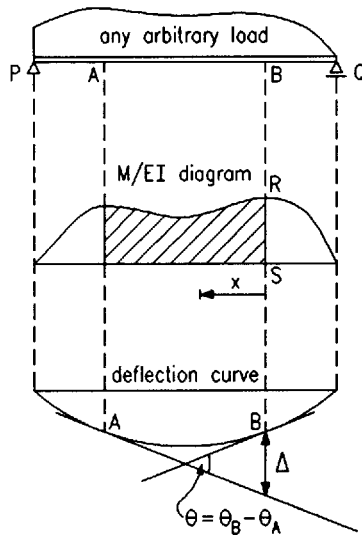


Fig. 9.22 Area moment theorems

$$\theta_B - \theta_A = \text{area of } \frac{M}{EI} \text{ diagram between A and B}$$

$$= \int_A^B \frac{M}{EI} dx \quad (9.16)$$

$$\Delta = \text{moment of the } \frac{M}{EI} \text{ diagram between A and B taken about the}$$

$$\text{vertical line RS}$$

$$= \int_A^B \frac{Mx}{EI} dx \quad (9.17)$$

(*Caution:* The vertical intercept is *not* the deflection of the beam from its original position.)

The area moment method can be used for solving problems like encastré beams, propped cantilevers, etc. The procedure is as follows:

- (1) The redundant supports are removed thereby releasing the redundant forces and moments. The statically determinate  $M/EI$  diagram for externally applied loads can then be drawn.
- (2) The externally applied loads are removed and the redundant forces and moments are introduced one at a time and the  $M/EI$  diagrams corresponding to each of these forces and moments are drawn.
- (3) The slopes at supports and intercepts on a vertical axis passing through the supports are then calculated.
- (4) A number of expressions are obtained. These are then equated to known values of slopes or displacements at supports. The equations so obtained can then be solved for the unknown redundant reactions. This enables the evaluation of the forces and moments in the structure.

#### 9.5.4 The slope–deflection method

The slope–deflection method can be used to analyze all types of statically indeterminate beams and rigid frames. In this method all joints are considered rigid and the angles between members at the joints are considered not to change as the loads are applied. When beams or frames are deformed, the rigid joints are considered to rotate as a whole.

In the slope–deflection method, the rotations and translations of the joints are the unknowns. All end moments are expressed in terms of end rotations and translations. In order to satisfy the conditions of equilibrium, the sum of end moments acting on a rigid joint must total zero. Using this equation of equilibrium, the unknown rotation of each joint is evaluated, from which the end moments are computed.

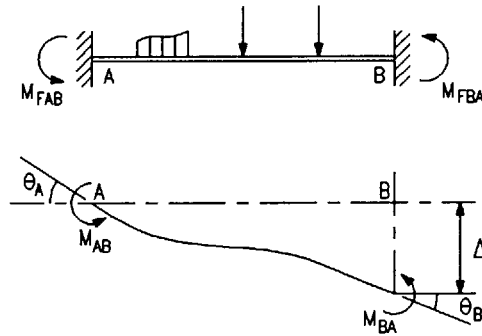


Fig. 9.23 Slope–deflection method

For the span AB shown in Fig. 9.23, the object is to express the end moments  $M_{AB}$  and  $M_{BA}$  in terms of end rotations  $\theta_A$  and  $\theta_B$  and translation  $\Delta$ .

With the applied loading on the member, fixed end moments  $M_{FAB}$  and  $M_{FBA}$  are required to hold the tangents at the ends fixed in direction. (Counter clockwise end moments and rotations are taken as positive.) The slope–deflection equations for the case sketched in Fig. 9.23 are

$$\begin{aligned}
 M_{AB} &= M_{FAB} + \frac{2EI}{L} \left( -2\theta_A - \theta_B + \frac{3\Delta}{L} \right) \\
 M_{BA} &= M_{FBA} + \frac{2EI}{L} \left( -2\theta_B - \theta_A + \frac{3\Delta}{L} \right)
 \end{aligned}
 \tag{9.18}$$

where  $M_{FAB}$ ,  $M_{FBA}$  are the fixed end moments at A and B due to loading and settlement of supports (counter clockwise positive);  $\theta_A$  and  $\theta_B$  are end rotations; and  $\Delta$  is the downward settlement of support B relative to support A.

### 9.5.5 The moment-distribution method

The moment-distribution method can be employed to analyze continuous beams or rigid frames. Essentially it consists of solving the simultaneous equations in the slope–deflection method by successive approximations. Since the solution is by successive iteration, it is not even necessary to determine the degree of redundancy.

Two facets of the method must be appreciated (see Fig. 9.24):

- When a stiff joint in a structural system absorbs an applied moment with rotational movement only (i.e. no translation), Fig. 9.24(a), the moment resisted by the various members meeting at the joint is in proportion to their respective stiffnesses (Fig. 9.24(b)).
- When a member is fixed at one end and a moment,  $M$ , is applied at the other freely supported end, the moment induced at the fixed end is half the applied

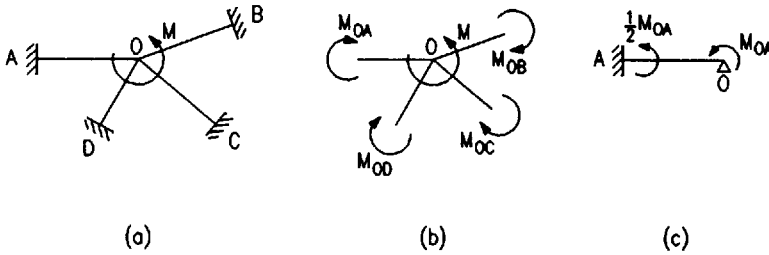


Fig. 9.24 Moment-distribution method

moment and acts in the same direction as  $M$ . (This is frequently referred to as the carry over.) (Fig. 9.24(c).)

Figure 9.25 shows the sign conventions employed in the moment-distribution method and Fig. 9.26 illustrates the moment-distribution procedure.

The moment-distribution method consists of locking all joints first and then releasing them one at a time. To begin with, all joints are locked, which implies that the fixed end moments due to applied loading will be applied at each joint. By releasing one joint at a time, the unbalanced moment at each joint is distributed to the various members meeting at the joint. Half of these applied moments are then carried over to the other end of each member. This creates a further imbalance at each joint and the unbalanced moments are once again distributed to all members meeting at each joint in proportion to their respective stiffnesses.

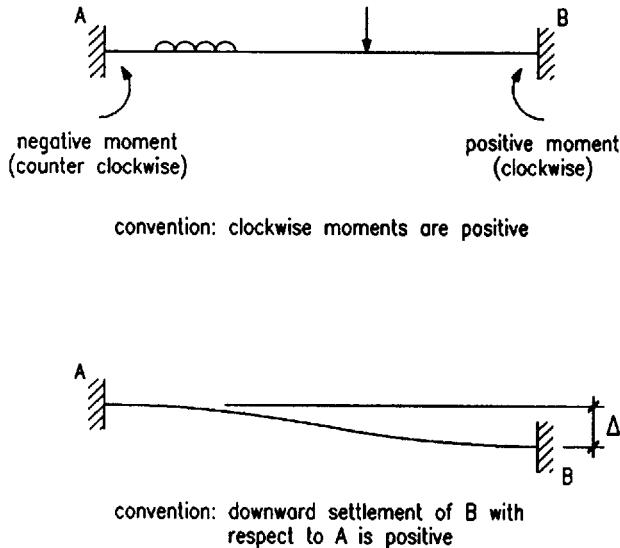


Fig. 9.25 Sign conventions used in moment-distribution method



|  |                    |  |                    |   |
|--|--------------------|--|--------------------|---|
|  |                    |  |                    | the problem   |
| $\frac{4EI/L_1}{\left(\frac{4EI}{L_1} + \frac{3EI}{L_2}\right)}$ |                    | $\frac{3EI/L_2}{\left(\frac{4EI}{L_1} + \frac{3EI}{L_2}\right)}$ |                    | step 1: calculate the distribution factor for BC is = $\frac{3EI}{L_2}$ as propped cantilever |
| A ————— 4:3  |                    |  |                    |   |
| $-\frac{wL^2}{12}$   | $+\frac{wL^2}{12}$ | $-\frac{wL^2}{12}$   | $+\frac{wL^2}{12}$ | step 2: calculate the fixed end moments<br>caution: pay attention to signs                    |
| -16  | +16                | -16  | +16                |   |
|  |                    |  | -16                | step 3: release joint C (simply supported)  |
|  |                    | -8   |                    | step 4: carry over to B   |
|  | +4.57              | +3.43  |                    | step 5: release joint B and distribute  |
| +2.28  |                    |  | 0                  | step 6: carry over to A (note: no carry over to C is possible)                                |
| -13.72   | +20.57             | -20.57   | 0                  | step 7: sum up the moments after repeating distribution and carry overs if necessary          |

Fig. 9.26 An example of moment-distribution procedure

This procedure is repeated until the totals of all moments at each joint are sufficiently close to zero. At this stage the moment-distribution process is stopped and the final moments are obtained by summing up all the numbers in the respective columns.

### 9.5.6 Unit load method

Energy methods provide powerful tools for the analysis of structures. The unit load method can be directly derived from the complementary Energy Theorem

which states that for any elastic structure in equilibrium under loads  $P_1, P_2, \dots$ , the corresponding displacements  $x_1, x_2, \dots$  are given by the partial derivatives of the complementary energy,  $C$ , with respect to the loads  $P_1, P_2$ , etc. In other words,

$$\frac{\partial C}{\partial P_1} = x_1 \quad \frac{\partial C}{\partial P_2} = x_2 \tag{9.19}$$

For a linearly elastic system, the complementary energy is equal to the strain energy,  $U$ , hence

$$x_1 = \frac{\partial U}{\partial P_1} \quad x_2 = \frac{\partial U}{\partial P_2} \tag{9.20}$$

The total strain energy of an elastic system is given by the sum of the strain energies stored in each member due to bending, shear, torsion and axial loading.

The use of this will be illustrated by considering a simply-supported beam of length  $l$  subject to an external loading (see Fig. 9.27). Strain energy stored in the beam is predominantly flexural and is given by

$$\int_0^l \frac{M^2 dx}{2EI}$$

$$x_1 = \text{deflection under } P_1 = \frac{\partial}{\partial P_1} \left( \int_0^l \frac{M^2 dx}{2EI} \right) = \int_0^l \frac{M}{EI} \frac{\partial M}{\partial P_1} dx \tag{9.21}$$

$\frac{\partial M}{\partial P_1}$  is the bending moment due to a unit load and is denoted by  $m$

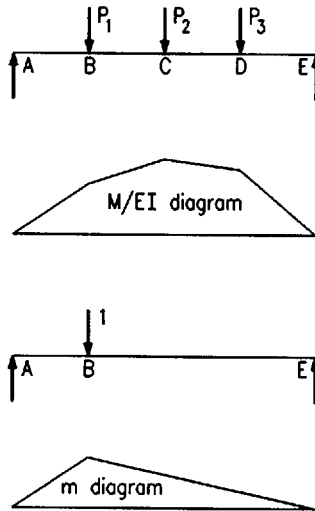


Fig. 9.27 Unit load method

Hence the procedure of the unit load method can be outlined (see Fig. 9.27):

- (1)  $\frac{M}{EI}$  diagram due to the external loading is obtained.
- (2) The external loads are now removed and the moment diagram ( $m$ ) due to a unit load applied at the point of required deflection is drawn.
- (3) These two diagrams should now be integrated; in other words, the ordinates of the two diagrams are multiplied to obtain the deflection, given by

$$x = \int_0^l \frac{M}{EI} m \, dx$$

The same principle can be employed to determine the displacement due to other causes, viz. axial load or shear or torsion.

## 9.6 Finite element method

The advent of high-speed electronic digital computers has given tremendous impetus to numerical methods for solving engineering problems. Finite element methods form one of the most versatile classes of such methods which rely strongly on the matrix formulation of structural analysis. The application of finite elements dates back to the mid-1950s with the pioneering work by Argyris,<sup>4</sup> Clough and others.

The finite element method was first applied to the solution of plane stress problems and subsequently extended to the analysis of axisymmetric solids, plate bending problems and shell problems. A useful listing of elements developed in the past is documented in text books on finite element analysis.<sup>5</sup>

Stiffness matrices of finite elements are generally obtained from an assumed displacement pattern. Alternative formulations are equilibrium elements and hybrid elements. A more recent development is the so-called strain based elements. The formulation is based on the selection of simple independent functions for the linear strains or change of curvature; the strain–displacement equations are integrated to obtain expressions for the displacements.

The basic assumption in the finite element method of analysis is that the response of a continuous body to a given set of applied forces is equivalent to that of a system of discrete elements into which the body may be imagined to be subdivided. From the energy point of view, the equivalence between the body and its finite element model is therefore exact if the strain energy of the deformed body is equal to that of its discrete model.

The energy due to straining of the element,  $U$ , written in two-dimensional form is

$$U = \frac{1}{2} \iiint (\varepsilon_x \sigma_x + \varepsilon_y \sigma_y + \gamma_{xy} \tau_{xy}) \, d(\text{vol})$$

or in matrix form

$$U = \frac{1}{2} \iiint \{\varepsilon\}^T \{\sigma\} d(\text{vol}) \quad (9.22)$$

$$\begin{aligned} \text{in which } \{\varepsilon\}^T &= \{\varepsilon_x, \varepsilon_y, \gamma_{xy}\} \\ \{\sigma\} &= \{\sigma_x, \sigma_y, \tau_{xy}\}^T \end{aligned} \quad (9.23)$$

$$\begin{aligned} \text{and } \{\varepsilon\} &= [f] \{\delta^e\} \\ \{\delta^e\} &= \{u_1, u_2, \dots, u_n\}^T \end{aligned} \quad (9.24)$$

where  $\{\delta\}$  is the nodal displacement vector,  $[f]$  is a function defining the strain distribution and  $e$  refers to a typical finite element. When the strain distribution within the model is exactly the same as that prevailing within the body, then the energy equation will be exactly satisfied.

The exact determination of the strain distribution function  $[f]$  in Equation (9.24) presents considerable difficulties, since this can only be done by a rigorous solution of the equations of linear elasticity. It may not always be possible to obtain an *exact* shape function for the solution; however, a suitable function which is *adequate* to model strains can usually be selected. The derivation of simple membrane elements for plate problems is presented in the following pages.

### 9.6.1 Finite element procedure

As mentioned above, the basic concept of the finite element method is the idealization of the continuum as an assemblage of discrete structural elements. The stiffness properties of each element are then evaluated and the stiffness properties of the complete structure are obtained by superposition of the individual element stiffnesses. This gives a system of linear equations in terms of nodal point loads and displacements whose solution yields the unknown nodal point displacements.

The idealization governs the type of element which must be used in the solution. In many cases only one type of element is used for a given problem, but sometimes it is more convenient to adopt a 'mixed' subdivision in which more than one type of element is used.

The elements are assumed to be interconnected at a discrete number of nodal points or nodes. The nodal degrees of freedom normally refer to the displacement functions and their first partial derivatives at a node but very often may include other terms such as stresses, strains and second or even higher partial derivatives. For example, the triangular and rectangular membrane elements of Fig. 9.28(a) and (b) have 6 and 8 degrees of freedom respectively, representing the translations  $u$  and  $v$  at the corner nodes in the  $x$  and  $y$  directions.

A displacement function in terms of the co-ordinate variables  $x$ ,  $y$  and the nodal displacement parameters (e.g.  $u_i$ ,  $v_i$ , or  $\delta_i$ ) are chosen to represent the displacement variations within each element. By using the principle of virtual work or the

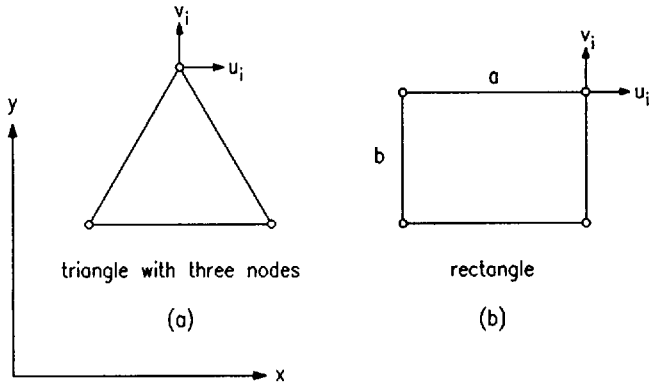


Fig. 9.28 Triangular and rectangular membrane elements

principle of minimum total potential energy, a stiffness matrix relating the nodal forces to the nodal displacements can be derived. Hence the choice of suitable displacement functions is the most important part of the whole procedure. A good displacement function leads to an element of high accuracy with converging characteristics; conversely, a wrongly chosen displacement function yields poor or non-converging results.

A displacement function may conveniently be established from simple polynomials or interpolation functions. The displacement field in each element must be expressed as a function of nodal point displacements only, and this must be done in such a way as to maintain inter-element compatibility, since this condition is necessary to establish a bound on the strain energy. Therefore, the displacement pattern and the nodal point degrees of freedom must be selected properly for each problem considered.

In general, it is not *always* necessary that the compatibility must be satisfied in order to achieve convergence to the true solution. If complete compatibility is not achieved, there exists an uncertainty as to the bound on the strain energy of the system. Therefore, in order to justify the performance and the ability of these elements to converge to the true solution, a critical test which indicates the performance in the limit must be carried out; that is, a convergence test with decreasing mesh size. If the performance is adequate, then convergence to the true solution is achieved within a reasonable computational effort, and the requirement for the complete compatibility can be relaxed.

Besides satisfying the compatibility requirement, the assumed displacement functions should include the following properties:

- (1) Rigid body modes
- (2) Constant strain and curvature states
- (3) Invariance of the element stiffnesses.

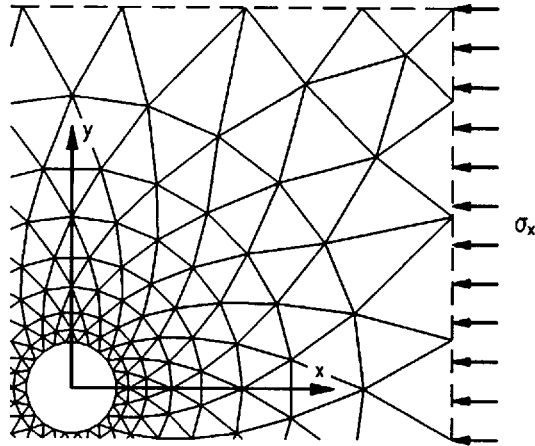


Fig. 9.29 Circular hole in uniform stress field

### 9.6.2 Idealization of the structure

The finite element idealization should represent the real structure as closely as possible with regard to geometrical shape, loading and boundary conditions. The geometrical form of the structure is the major factor to be considered when deciding the shape of elements to be used. In two-dimensional analyses the most frequently used elements are triangular or rectangular shapes. The triangular element has the advantage of simplicity in use and the ability to fit into irregular boundaries. Figure 9.29 shows an example using triangular elements and Fig. 9.30 shows a combination of triangular and rectangular elements. These figures also demonstrate the need to use relatively small elements in areas where high stress gradients occur. In many such cases the geometrical shape of the structure is such that a fine mesh of elements is required in order to match this shape.

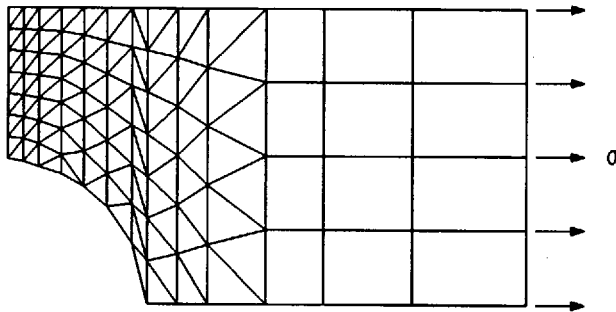


Fig. 9.30 Perforated tension strip (plane stress) – a quarter of a plate is analyzed

### 9.6.3 Procedure for evaluating membrane element stiffness

The formulation of the stiffness matrix  $[K^c]$  of the membrane element is briefly discussed below.

The energy due to straining of the element is given by Equation (9.22). The stress components are shown in Fig. 9.31 and  $\epsilon_x, \epsilon_y, \gamma_{xy}$  are the corresponding strain components. For the state of plane stress, the stress components are related to the strain components as given below

$$\begin{Bmatrix} \sigma_x \\ \sigma_y \\ \tau_{xy} \end{Bmatrix} = \frac{E}{1-\nu^2} \begin{bmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{1-\nu}{2} \end{bmatrix} \begin{Bmatrix} \epsilon_x \\ \epsilon_y \\ \gamma_{xy} \end{Bmatrix} \tag{9.25}$$

where  $E$  and  $\nu$  are Young's modulus and Poisson's ratio respectively.

$$\therefore \{\sigma\} = [D] \{\epsilon\}$$

The matrix  $[D]$  is referred to as the elasticity or property matrix. The strain energy of the element is given by Equation (9.22) as

$$U = \frac{1}{2} \iiint \{\epsilon\}^T [D] \{\epsilon\} d(\text{vol}) \tag{9.26}$$

Denoting the generalized nodal displacement by the vector  $\{\delta^c\}$ ,

$$\{\delta^c\} = [C] \{A\} \tag{9.27}$$

where  $\{A\} = [a_1, a_2, \dots, a_n]^T$ , which is a vector of polynomial constants, and  $[C]$  is a transformation matrix.

The strains are obtained through making appropriate differentiations of the displacement function with respect to the relevant co-ordinate variable  $x$  or  $y$ . Thus,

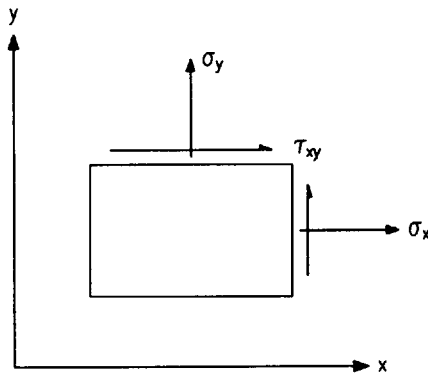


Fig. 9.31 Stress components on a plane element

$$\{\varepsilon\} = \begin{Bmatrix} \varepsilon_x \\ \varepsilon_y \\ \gamma_{xy} \end{Bmatrix} = \begin{Bmatrix} \frac{\partial u}{\partial x} \\ \frac{\partial v}{\partial y} \\ \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \end{Bmatrix} \quad (9.28)$$

$$\therefore \{\varepsilon\} = [B] \{A\} = [B] [C]^{-1} \{\delta^e\} \quad (9.29)$$

where  $[B]$  is the transformation matrix.

Using Equations (9.26) and (9.29), the following expression for  $U$  in terms of the nodal point displacement vector  $\{\delta^e\}$  is obtained:

$$U = \frac{1}{2} \{\delta^e\}^T [C]^{-1,T} \left[ \iint [B]^T [D] [B] d(\text{vol}) \right] [C]^{-1} \{\delta^e\} \quad (9.30)$$

Differentiation of  $U$  with respect to the nodal displacements yields the stiffness matrix  $[K^e]$ .

$$[K^e] = t [C]^{-1,T} \left[ \int_A [B]^T [D] [B] dA \right] [C]^{-1} \quad (9.31)$$

where  $t$  is the thickness of the element (assumed constant).

The calculation of the stiffness matrices is generally carried out in two stages. The first stage is to calculate the terms inside the square brackets of Equation (9.31) i.e. the integration part. The second stage is to multiply the resulting integrations by the inverse of the transformation matrix  $[C]$  and its transpose.

Equation (9.31) can now be written as

$$[K^e] = t [C]^{-1,T} [Q] [C]^{-1} \quad (9.32)$$

where  $[Q] = \int_A [B]^T [D] [B] dA$

The simplest elements for plane stress analysis have nodal points at the corners only and have two degrees of kinematic freedom at each nodal point, i.e.  $u$  and  $v$ . This type of element proves simple to derive and has been widely used. The simplest elements of this type are rectangular and triangular in shape.

A triangular element with nodal points at the corners is shown in Fig. 9.28(a). The displacement function of this element has two degrees of freedom at each nodal point and the displacements are assumed to vary linearly between nodal points. This results in constant values of the three strain components over the entire element; the displacement functions are

$$\begin{aligned} u &= a_1 + a_2x + a_3y \\ v &= a_4 + a_5x + a_6y \end{aligned} \quad (9.33)$$

The rectangular element with sides  $a$  and  $b$ , shown in Fig. 9.28(b), is used with the following displacement functions



$$\begin{aligned} u &= a_1 + a_2x + a_3y + a_4xy \\ v &= a_5 + a_6x + a_7y + a_8xy \end{aligned} \quad (9.34)$$

### 9.6.4 Procedure for evaluating plate bending element stiffness

The energy due to straining (bending) of the element is

$$U_b = \frac{1}{2} \int_A (\chi_x M_x + \chi_y M_y + 2 \chi_{xy} M_{xy}) dA \quad (9.35)$$

or in matrix form

$$\begin{aligned} U_b &= \frac{1}{2} \int_A \{\chi_x, \chi_y, 2\chi_{xy}\} \begin{Bmatrix} M_x \\ M_y \\ M_{xy} \end{Bmatrix} dA \\ &= \frac{1}{2} \int_A [\chi]^T \{M\} dA \end{aligned}$$

where the moments  $M_x$ ,  $M_y$ ,  $M_{xy}$  are given in Fig. 9.32 and  $\chi_x$ ,  $\chi_y$  and  $\chi_{xy}$  are the corresponding curvatures, i.e.

$$\chi_x = \frac{\partial^2 w}{\partial x^2} \quad \chi_y = \frac{\partial^2 w}{\partial y^2} \quad \chi_{xy} = \frac{\partial^2 w}{\partial x \partial y} \quad (9.36)$$

where  $w$  is the transverse displacement of the plate element.

The conventional relationship between curvatures and moment is

$$\begin{Bmatrix} M_x \\ M_y \\ M_{xy} \end{Bmatrix} = [\bar{D}] \begin{Bmatrix} \chi_x \\ \chi_y \\ 2\chi_{xy} \end{Bmatrix} \quad (9.37)$$

or

$$\{M\} = [\bar{D}]\{\chi\}$$

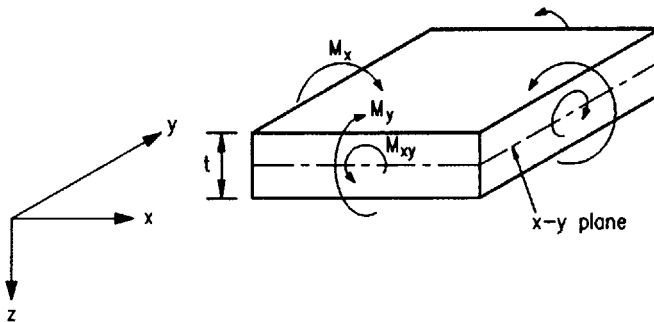


Fig. 9.32 Moments acting on a plane element

For an isotropic plate, the rigidity matrix,  $[\bar{D}]$ , may be written as

$$[\bar{D}] = \begin{bmatrix} D_1 & \nu D_1 & 0 \\ \nu D_1 & D_1 & 0 \\ 0 & 0 & D_{xy} \end{bmatrix}$$

and

$$D_x = D_y = D_1 = \frac{Et^3}{12(1 - \nu^2)}$$

$$D_{xy} = \frac{1}{2}(1 - \nu) D_1$$

Finally the strain energy can be written as

$$U_b = \frac{1}{2} \int_A [\chi]^T [\bar{D}] [\chi] dA \quad (9.38)$$

Denoting the generalized nodal displacement by the vector  $\{\bar{\delta}^e\}$ ,

$$\{\bar{\delta}^e\} = [\bar{C}]\{\bar{A}\} \quad (9.39)$$

where  $\{\bar{A}\}$  is a vector of polynomial constants.

From Equations (9.36) and (9.39),

$$\{\chi\} = [\bar{B}]\{\bar{A}\} = [\bar{B}][\bar{C}]^{-1}\{\bar{\delta}^e\} \quad (9.40)$$

Using Equations (9.38) and (9.40), the following equation for  $U_b$  in terms of nodal point displacement parameters  $\{\bar{\delta}^e\}$  is obtained

$$U_b = \frac{1}{2} \{\bar{\delta}^e\}^T [\bar{C}]^{-1,T} \left[ \int_A [\bar{B}]^T [\bar{D}] [\bar{B}] dA \right] [\bar{C}]^{-1} \{\bar{\delta}^e\} \quad (9.41)$$

Differentiation of  $U$  with respect to the nodal displacements yields the stiffness matrix  $[\bar{K}^e]$

$$[\bar{K}^e] = [\bar{C}]^{-1,T} \left[ \int_A [\bar{B}]^T [\bar{D}] [\bar{B}] dA \right] [\bar{C}]^{-1} \quad (9.42)$$

Equation (9.42) can now be written as

$$[\bar{K}^e] = [\bar{C}]^{-1,T} [\bar{Q}] [\bar{C}]^{-1} \quad (9.43)$$

where

$$[\bar{Q}] = \int_A [\bar{B}]^T [\bar{D}] [\bar{B}] dA \quad (9.44)$$

As mentioned before, the accuracy is dependent on choosing a large number of elements. Many refined elements giving greater accuracy are described in standard books on finite element methods, which also provide details of assembling the elements and analyzing the structure.<sup>5-7</sup> These methods are used for solving a wide range of problems.

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# Chapter 10

## Beam analysis

by JOHN RIGHINIOTIS

### 10.1 Simply-supported beams

The calculations required to obtain the shear forces (SF) and bending moments (BM) in simply-supported beams form the basis of many other calculations required for the analysis of built-in beams, continuous beams and other indeterminate structures.

Appropriate formulae for simple beams and cantilevers under various types of loads are presented in the Appendix *Bending moment, shear and deflection tables for cantilevers and simply-supported beams*.

In the case of simple beams it is necessary to calculate the support reactions before the bending moments can be evaluated; the procedure is reversed for built-in or continuous beams. The following rules relate to the SF and BM diagrams for beams:

- (1) the shear force at any section is the algebraic sum of normal forces acting to one side of the section
- (2) shear is considered positive when the shear force calculated as above is upwards to the left of the section
- (3) the BM at any section is the algebraic sum of the moments about that section of all forces to one side of the section
- (4) moments are considered positive when the middle of a beam sags with respect to its ends or when tension occurs in the lower fibres of the beam
- (5) for point loads only the SF diagram will consist of a series of horizontal and vertical lines, while the BM diagram will consist of sloping straight lines, changes of slope occurring only at the loads
- (6) for uniformly distributed loads (UDL) the SF diagram will consist of sloping straight lines, while the BM diagram will consist of second-degree parabolas
- (7) the maximum BM occurs at the point of zero shear, where such exists, or at the point where the shear force curve crosses the base line.

### 10.2 Propped cantilevers

Beams which are built-in at one end and simply-supported at the other are known as propped cantilevers. Normally, the ends of the beams are on the same level, in

which case bending moments and reactions may be derived in two ways: by employing the Theorem of Three Moments or by deflection formulae. Appropriate formulae for propped cantilevers under various types of loading are presented in the Appendix *Bending moment, shear and deflection tables for propped cantilevers*.

### 10.2.1 Solution by the Theorem of Three Moments

Consider the propped cantilever AB in Fig. 10.1.

The bending moment at B may be found by using the Theorem of Three Moments, and assuming that AB is one span of a two-span continuous beam ABC which is symmetrical in every way about B.

Then the loads on AB and BC will produce free BM diagrams whose areas are  $A_1$  and  $A_2$  respectively, the centres of gravity (CG) of the areas being distances  $x_1$  and  $x_2$  from A and C respectively.

$$\text{Now } M_A L_1 + 2M_B(L_1 + L_2) + M_C L_2 = 6 \left( \frac{A_1 x_1}{L_1} + \frac{A_2 x_2}{L_2} \right)$$

where  $M_A$ ,  $M_B$  and  $M_C$  are the numerical values of the hogging moments at the supports A, B and C.

But  $L_1 = L_2 = L$   
 $M_A = M_C = 0$   
 $A_1 = A_2 = A$   
 and  $x_1 = x_2 = x$

Hence  $2M_B(2L) = 6 \times 2 \left( \frac{Ax}{L} \right)$

and  $M_B = \frac{3Ax}{L^2}$

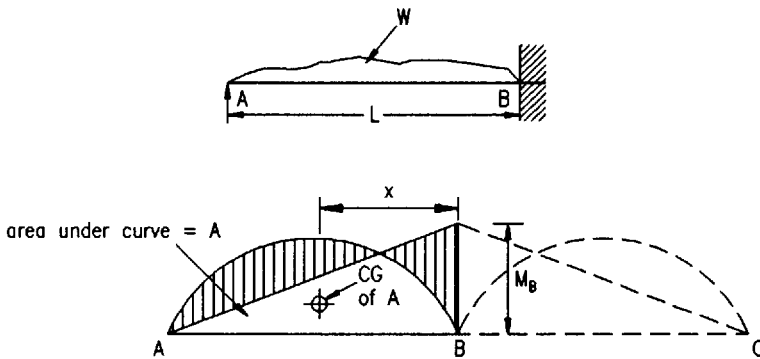


Fig. 10.1 Bending moment diagram for propped cantilever

Therefore the moment at the fixed end of a propped cantilever

$$= 3Ax/L^2$$

where  $A$  = the area of the free BM diagram, AB being considered as a simply-supported beam

$x$  = the distance from the prop to the CG of the free BM diagram

and  $L$  = the span.

The reactions at each support may be found by employing a modified form of the formula used for beams built-in at both ends

$$SF_A = \text{the simple support reaction at A} = -\frac{M_B}{L}$$

$$SF_B = \text{the simple support reaction at B} = +\frac{M_B}{L}$$

where A is the propped end and B is built-in.

### 10.2.2 Sinking of supports

When the supports for a loaded propped cantilever do not maintain the same relative levels as in the unloaded condition, the BM and SF may be obtained by using the deflection method (Fig. 10.2). When the prop, B, sinks the load which it takes is reduced, while the fixing moment at the other end is increased. Two special cases arise: the first when the prop sinks so much that no load is taken by the prop, and the second when the built-in end sinks so much that the fixing moment is reduced to zero, i.e. the cantilever resembles a simple support beam. The two special cases are shown in Fig. 10.2.

### 10.3 Fixed, built-in or encastré beams

When the ends of a beam are firmly held so that they cannot rotate under the action of the superimposed loads, the beam is known as a fixed, built-in or encastré beam. The BM diagram for such a beam is in two parts: the free or positive BM diagram, which would have resulted had the ends been simply-supported, i.e. free to rotate, and the fixing or negative BM diagram which results from the restraints imposed upon the ends of the beam.

Normally, the supports for built-in beams are at the same level and the ends of the beams are horizontal. This type will be considered first.

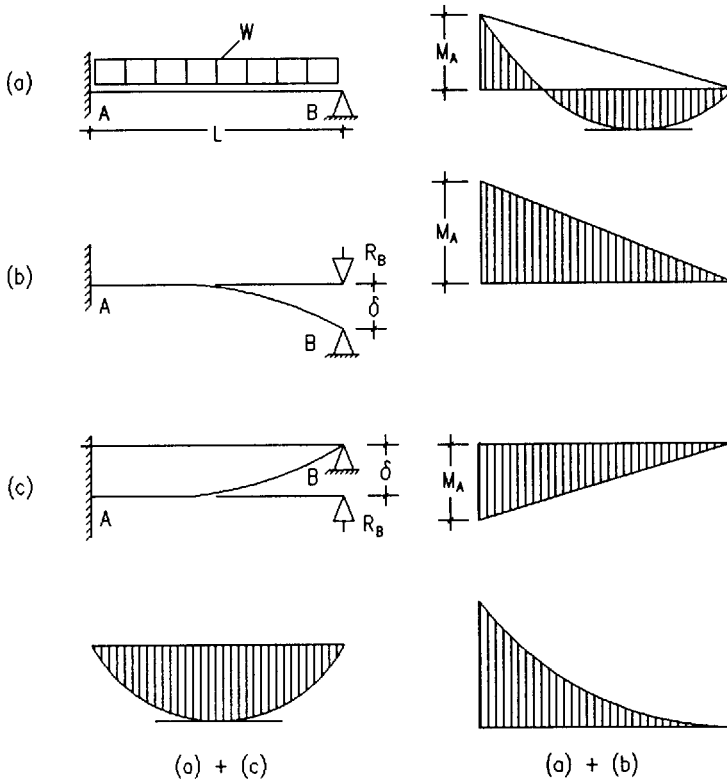


Fig. 10.2 Bending moment diagram for propped cantilever with sinking support

### 10.3.1 Beams with supports at the same level

The two conditions for solution, derived by Mohr, are:

- (1) the area of the fixing or negative BM diagram is equal to that of the free or positive BM diagram
- (2) the centres of gravity of the two diagrams lie in the same vertical line, i.e. are equidistant from a given end of the beam.

Figure 10.3 shows a typical BM diagram for a built-in beam.

ACDB is the diagram of the free moment  $M_s$  and the trapezium AEFB is the diagram of the fixing moment  $M_i$ , the portions shaded representing the final diagram.

Let  $A_s$  = the area of the free BM diagram  
 and  $A_i$  = the area of the fixing moment diagram.

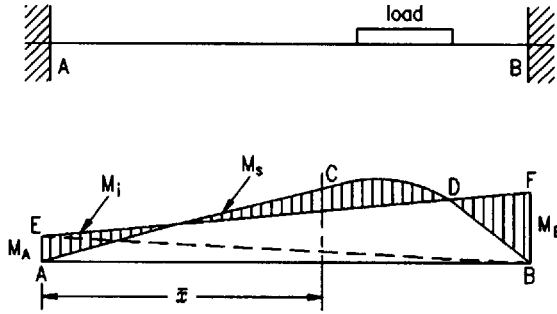


Fig. 10.3 Bending moment diagram for fixed-end beam

Then from condition (1) above,  $A_s = A_i$ , while from condition (2) their centres of gravity lie in the same vertical line, say, distance  $\bar{x}$  from the left-hand support A.

Now AE = the fixing moment  $M_A$   
and BF = the fixing moment  $M_B$ .

Therefore 
$$\frac{M_A + M_B}{2} \times L = A_i$$

and 
$$M_A + M_B = \frac{2A_i}{L} \tag{10.1}$$

Divide the trapezium AEFB by drawing the diagonal EB and take area moments about the support A.

Then 
$$A_i \bar{x} = \left( \frac{M_A \times L}{2} \times \frac{L}{3} \right) + \left( \frac{M_B \times L}{2} \times \frac{2L}{3} \right)$$

$$= \frac{L^2}{6} (M_A + 2M_B)$$

$$M_A + 2M_B = \frac{6A_i \bar{x}}{L^2} \tag{10.2}$$

But 
$$M_A + M_B = \frac{2A_i}{L} \tag{10.3}$$

Also 
$$A_s = A_i$$

Subtracting Equation (10.1) from Equation (10.2) and substituting  $A_s$  for  $A_i$  gives

$$M_B = \frac{6A_s \bar{x}}{L^2} - \frac{2A_s}{L}$$

Similarly 
$$M_A = \frac{4A_s}{L} - \frac{6A_s \bar{x}}{L^2}$$



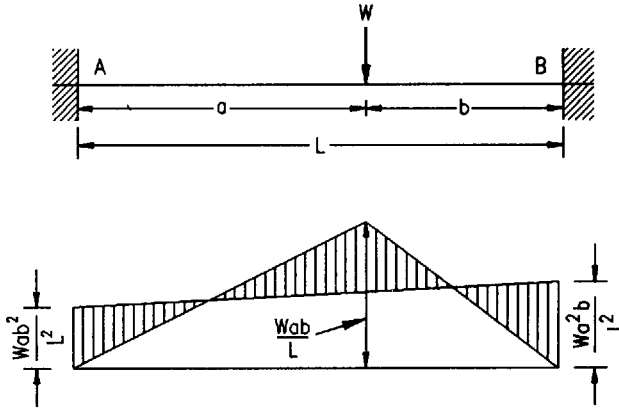


Fig. 10.4 Bending moment diagram for point load on fixed-end beam

It will be seen, therefore, that the fixing moments for any built-in beam on level supports can be calculated provided that the area of the free BM diagram and the position of its centre of gravity are known.

For point loads, however, the principle of reciprocal moments provides the simplest solution.

With reference to Fig. 10.4,

$$M_A = \frac{Wab}{L} \times \frac{b}{L} = \frac{Wab^2}{L^2}$$

$$M_B = \frac{Wab}{L} \times \frac{a}{L} = \frac{Wa^2b}{L^2}$$

i.e. the fixing moments are in reciprocal proportion to the distances of the ends of the beam from the point load.

In the case of several isolated loads, this principle is applied to each load in turn and the results summed.

It should be noted that appropriate formulae for built-in beams are given in the Appendix *Bending moment, shear and deflection tables for built-in beams*.

### 10.3.2 Beams with supports at different levels

The ends are assumed, as before, to be horizontal.

The bent form of the unloaded beam as shown in Fig. 10.5 is similar to the bent form of two simple cantilevers which can be achieved by cutting the beam at the centre \$C\$, and placing downward and upward loads at the free ends of the cantilevers such that the deflection at the end of each cantilever is \$d/2\$.

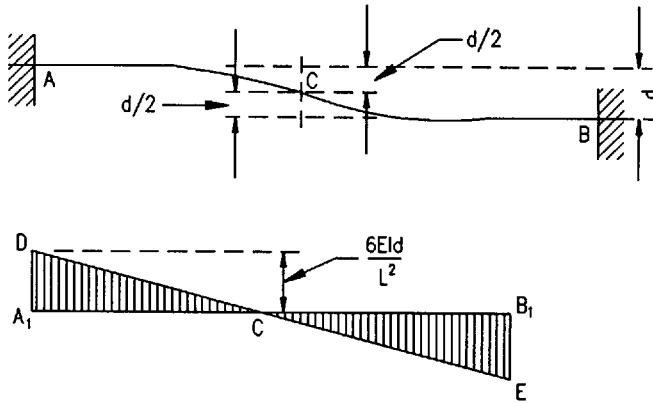


Fig. 10.5 Bending moment diagram for fixed-end beam with supports at different levels

Therefore  $\frac{d}{2} = \frac{P(L/2)^3}{3EI}$  (being the standard deflection formula)

or  $P = \frac{12EId}{L^3}$

This load would cause a BM at A or B equal to

$$P \times \frac{L}{2} = \frac{12EId}{L^3} \times \frac{L}{2} = \frac{6EId}{L^2}$$

The solution in any given case consists of adding to the ordinary diagram of BM, the BM diagram  $A_1DCEB_1$ .

*Shear forces in fixed beams*

In the case of fixed beams it is necessary to evaluate the BM before the SF can be determined. This is the converse of the procedure for the case of simply-supported beams.

The SF at the ends of a beam is found in the following manner:

$$SF_A = \text{the simple support reaction at A} = +\frac{M_A - M_B}{L}$$

$$SF_B = \text{the simple support reaction at B} = +\frac{M_B - M_A}{L}$$

where  $M_A$  and  $M_B$  are the numerical values of the moments at the ends of the beam.

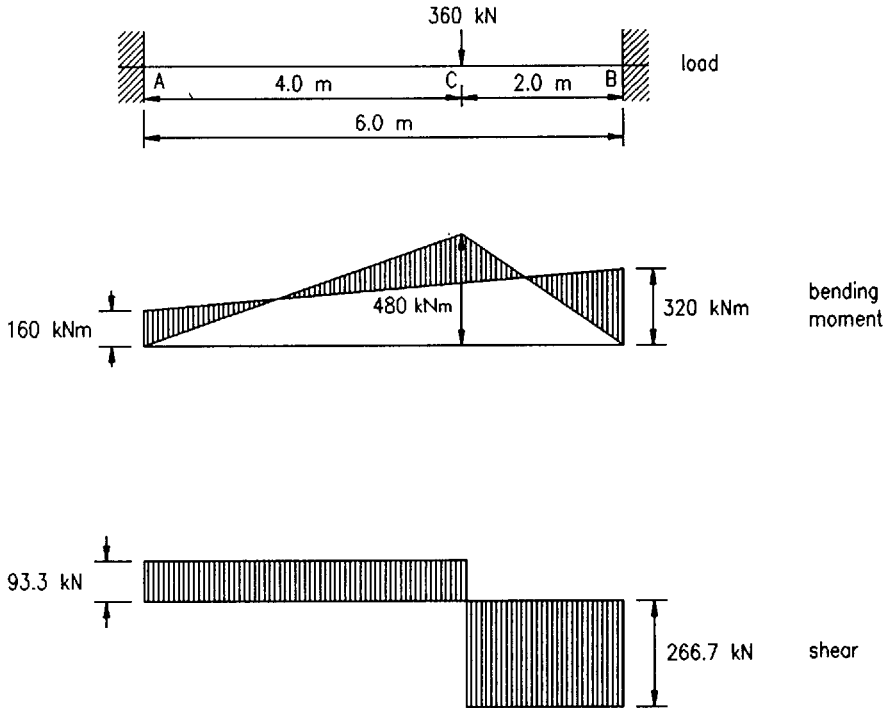


Fig. 10.6 Bending moment and shear force diagrams for fixed-end beam

These formulae must be followed exactly with respect to the signs shown since if  $M_A$  is smaller than  $M_B$  the signs will adjust themselves.

It will be seen that for symmetrical loads, where  $M_A = M_B$ , the reactions will be the same as for simply-supported beams.

An example of bending moment and shear force diagrams for a built-in beam carrying a point load is given in Fig. 10.6.

### 10.4 Continuous beams

The solution of this type of beam consists, in the first instance, of the evaluation of the fixing or negative moments at the supports.

The most general method is the use of Clapeyron's Theorem of Three Moments.

The theorem applies only to any two adjacent spans in a continuous beam and in its simplest form deals with a beam which has all the supports at the same level, and has a constant section throughout its length.

The proof of the theorem results in the following expression:

$$M_A \times L_1 + 2M_B (L_1 + L_2) + M_C \times L_2 = 6 \left( \frac{A_1 \times x_1}{L_1} + \frac{A_2 \times x_2}{L_2} \right)$$

where  $M_A$ ,  $M_B$  and  $M_C$  are the numerical values of the hogging moments at the supports A, B and C respectively, and the remaining terms are illustrated in Fig. 10.7.

In a continuous beam the conditions at the end supports are usually known, and these conditions provide starting points for the solution.

The types of end conditions are three in number:

- (1) simply supported
- (2) partially fixed, e.g. a cantilever
- (3) completely fixed, i.e. the end of the beam is horizontal as in the case of a fixed beam.

The SF at the end of any span is calculated after the support moments have been evaluated, in the same manner as for a fixed beam, each span being treated separately.

It is essential to note the difference between SF and reaction at any support, e.g. with reference to Fig. 10.7 the SF at support B due to span AB added to the SF at B due to span BC is equal to the total reaction at the support.

If the section of the beam is not constant over its whole length, but remains constant for each span, the expression for the moments is rewritten as follows:

$$M_A \times \frac{L_1}{I_1} + 2M_B \left( \frac{L_1}{I_1} + \frac{L_2}{I_2} \right) + M_C \times \frac{L_2}{I_2} = 6 \left( \frac{A_1 \times x_1}{L_1 \times I_1} + \frac{A_2 \times x_2}{L_2 \times I_2} \right)$$

in which  $I_1$  is the second moment of area for span  $L_1$  and  $I_2$  is the second moment of area for span  $L_2$ .

### *Example*

A two-span continuous beam ABC, of constant cross section, is simply supported at A and C and loaded as shown in Fig. 10.8.

Applying Clapeyron's theorem,

$$L_1 = 2.0 \text{ m}$$

$$L_2 = 3.0 \text{ m}$$

$$A_1 = \frac{10 \times 2}{8} \times \frac{2 \times 2}{3} = \frac{10}{3} \text{ kNm}^2$$

$$A_2 = \frac{200 \times 1 \times 2}{3} \times \frac{3}{2} = 200 \text{ kNm}^2$$

$$x_1 = 1.0 \text{ m}$$

$$x_2 = \frac{4.0}{3} \text{ m}$$

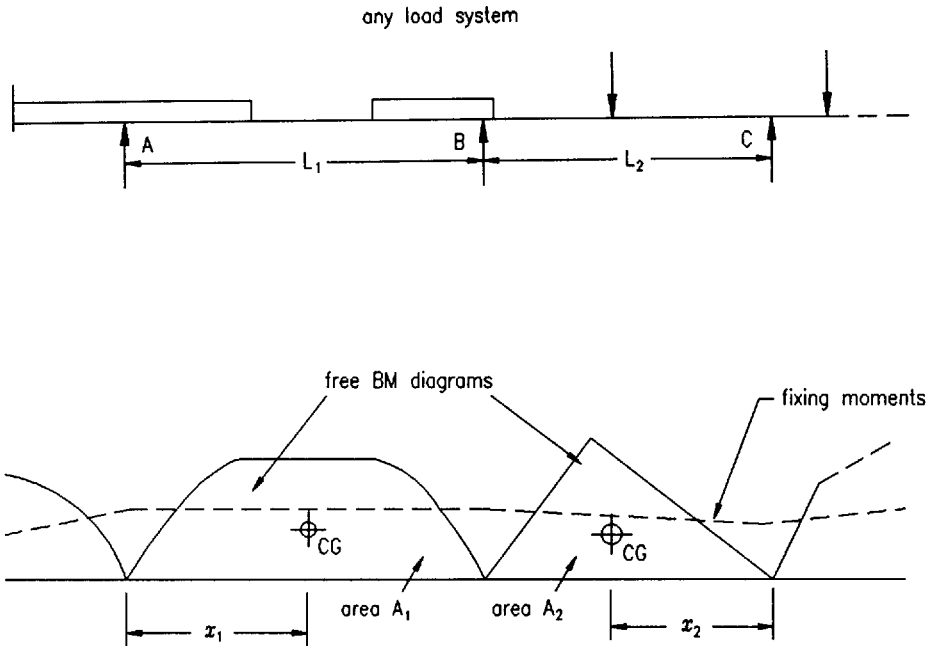


Fig. 10.7 Clapeyron's Theorem of Three Moments

Therefore  $M_A \times 2 + 2M_B (2 + 3) + M_C \times 3 = 6 \left( \frac{10 \times 1}{3 \times 2} + \frac{200 \times 4}{3 \times 3} \right)$

Since A and C are simple supports

$M_A = M_C = 0$

Therefore  $M_B = \frac{6}{10} \left( \frac{10}{6} + \frac{800}{9} \right) = \frac{6}{10} (90.56) = 54.33 \text{ kNm}$

$SF_A = 5 + \frac{0 - 54.33}{2} = 5 - 27.17 = -22.17 \text{ kN}$

$SF_B \text{ for span AB} = 5 + 27.17 = 32.17 \text{ kN}$

$SF_C = \frac{200 \times 2}{3} + \frac{0 - 54.33}{3} = 133.33 - 18.11 = 115.22 \text{ kN}$

$SF_B \text{ for span BC} = \frac{200}{3} + 18.11 = 66.67 + 18.11 = 84.78 \text{ kN}$

Note that the negative reaction at A means that the end A will tend to lift off its support and will have to be held down.

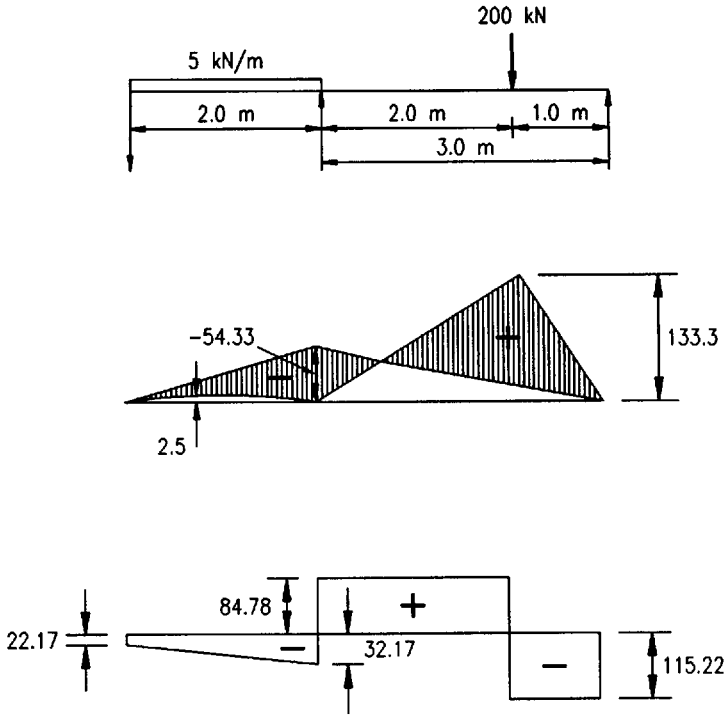


Fig. 10.8 Bending moment and shear force diagrams for two-span beam

### 10.5 Plastic failure of single members

The concept of the plastic hinge, capable of undergoing large rotation once the applied moment has reached the limiting value  $M_p$ , constitutes the basis of plastic design. This concept may be illustrated by examining the development of the collapse mode of a fixed-end beam subjected to a uniformly distributed load of increasing intensity  $w$  (Fig. 10.9(a)). Such a member is statically indeterminate, having three redundancies which however reduce to two unknowns if the axial thrust in the member is assumed to be zero. It will be assumed that the two unknown quantities are the fixing moments  $M_A$  and  $M_B$ . As the load increases, the beam initially behaves in an elastic manner and the value of the redundant moments can be derived by applying the three general conditions used in elastic structural analysis, namely those of

- (1) equilibrium (application of statics)
- (2) moment-curvature ( $EI \frac{d^2y}{dx^2} = M$ )
- (3) compatibility condition (continuity, including geometric conditions at the supports).

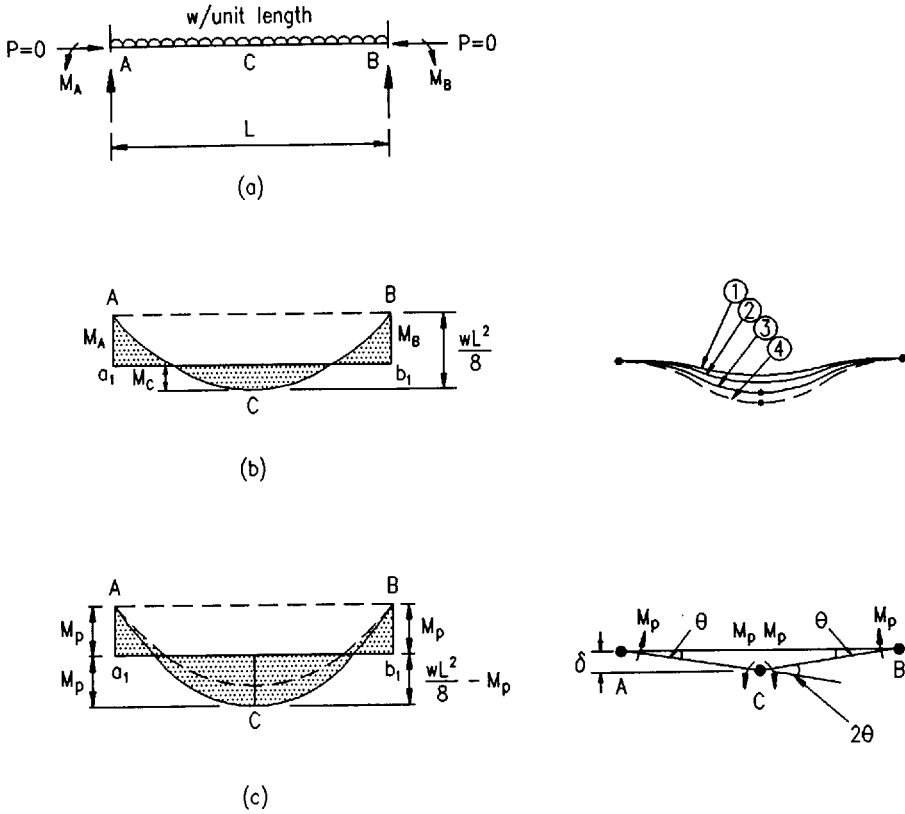


Fig. 10.9 Plastic failure of a fixed-end beam

For the beam in Fig. 10.9(a), the first condition (equilibrium) is satisfied by drawing the bending moment diagram (shaded in Fig. 10.9(b)) as a superposition of the simply-supported sagging parabolic moment diagram ACB (peak value of  $wL^2/8$ ) on the uniform moment diagram  $Aa_1b_1B$  due to the end hogging moments  $M_A$  and  $M_B$ . From the moment–curvature relation applied over the full length of the beam, it is readily deduced, by any one of a number of standard methods, that the rotations of the end sections at A ( $\theta_A$  clockwise) and at B ( $\theta_B$  anti-clockwise) and the central deflection  $\Delta_C$  are given by

$$\theta_A = \frac{wL^3}{24EI} - \frac{M_AL}{3EI} - \frac{M_B L}{6EI} \tag{10.4}$$

$$\theta_B = \frac{wL^3}{24EI} - \frac{M_AL}{6EI} - \frac{M_B L}{3EI} \tag{10.5}$$

$$\Delta_C = \frac{5}{384} \frac{wL^4}{EI} - \frac{M_AL^2}{16EI} - \frac{M_B L^2}{16EI} \tag{10.6}$$

The compatibility conditions that now have to be satisfied are the directional restraint of the end sections of the beam, i.e.  $\theta_A = \theta_B = 0$ , giving the well-known result  $M_A = M_B = wL^2/12$ . Equilibrium considerations now lead to the derivation of the central sagging moment,  $M_C$ . It follows from Fig. 10.9(b) that

$$M_C = \frac{wL^2}{8} - \left( \frac{M_A}{2} + \frac{M_B}{2} \right) \quad (10.7)$$

whence  $M_C = wL^2/24$ , i.e. the end moments are twice the central moment. Finally, application of Equation (10.3) gives the central deflection as  $wL^4/384EI$ .

Suppose the load intensity  $w$  is increased until the fibres yield at some point in the beam. It is assumed that the cross section has an idealized moment–curvature relationship, i.e. the shape factor is unity (see Section 9.3.5). Up to this stage the ratio of the end to central moments remains at 2, as represented by the dashed line in Fig. 10.9(c). Due to the symmetry of the structure and loading, plastic hinges will develop simultaneously at the fixed ends, i.e. at the points of maximum moment. At the moment when the hinges form at the ends, the fixing moments have become equal to the  $M_p$  of the beam and the loading intensity  $w$  has reached a value of  $12M_p/L^2$ . A slight load increase then causes the plastic hinges to rotate while sustaining this constant moment  $M_p$ . This means that thereafter the beam behaves as a simply-supported beam with constant end moments of  $M_p$ . The structure is now statically determinate, and therefore the two degrees of redundancy in the original problem no longer exist. In other words, two plastic hinges have formed, eliminating a corresponding number of redundancies. At the same time two compatibility requirements have been eliminated; the condition that end slopes are zero is no longer correct because the ends of the member are now rotating as plastic hinges.

The central deflection at this stage, derived from Equation (10.6) has the value

$$\Delta_C = \frac{5}{384} \left( \frac{12M_p}{L^2} \right) \frac{L^4}{EI} - \frac{M_p L^2}{8EI} = \frac{M_p L^2}{32EI}$$

and, from Equation (10.7), the central sagging moment  $M_C$  becomes  $[(wL^2/8) - M_p]$ . Further increases in the load intensity cause a third plastic hinge to form at mid-span, see the full line in Fig. 10.9(c). This means that the moment  $M_C$  attains a value of  $M_p$  and therefore at C

$$M_p = \frac{wL^2}{8} - M_p$$

hence

$$M_p = wL^2/16 \quad \text{or} \quad w = 16M_p/L^2$$

The ratio of the end and central moments is now unity; as a result of the formation of the plastic hinges there has been a redistribution of moments.

Substituting  $w = 16M_p/L^2$  and  $M_A = M_B = M_p$  in Equation (10.6) gives a central deflection of  $\Delta_C = M_p L^2/12EI$ . When the final hinge has formed the



deflection increases rapidly without any further increase in the load. The beam is said to have failed as a hinged mechanism.

Now consider the same fixed-end beam with an initial settlement of  $wL^4/144EI$  at end A (see Fig. 10.10(a)). The results derived from moment–curvature considerations [Equations (10.1)–(10.3)] can still be applied provided  $\theta_A$ ,  $\theta_B$  and  $\Delta_C$  are taken with reference to the chord AB between the ends of the member, the chord having rotated through an angle  $wL^3/144EI$  relative to its initial position  $A_0B$ . Thus the compatibility conditions at the ends of the member are now

$$\theta_A = -\theta_B = wL^3/144EI$$

whence, by substitution in Equations (10.4), (10.5) and (10.7),

$$M_A = wL^2/24 \quad M_B = wL^2/8 \quad M_C = wL^3/24$$

The largest elastic moment occurs at B and therefore the first hinge starts there at a load intensity given by  $M_p = wL^2/8$ , i.e.  $w = 8M_p/L^2$ . Equation (10.6) shows that the central deflection is  $M_pL^2/144EI$ .

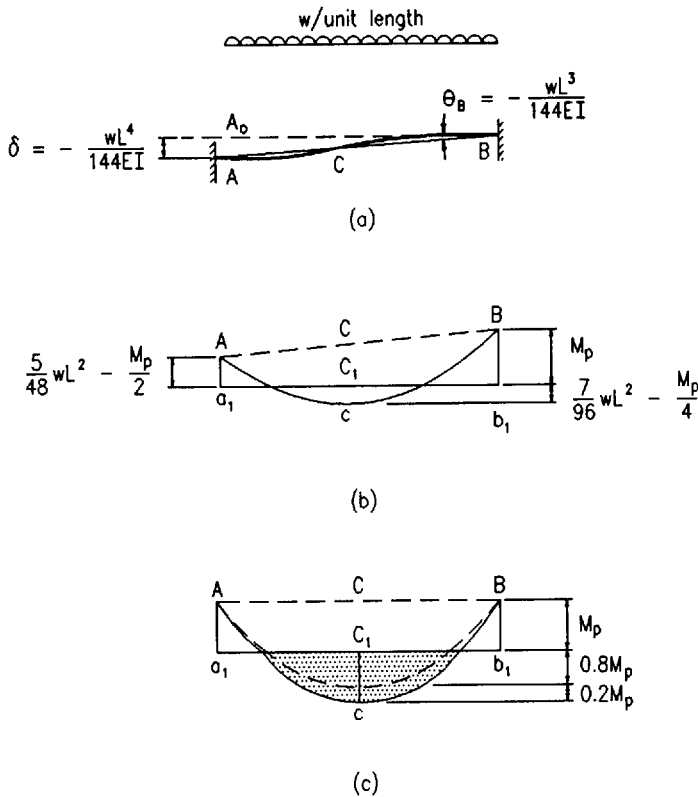


Fig. 10.10 Plastic failure of a fixed-end beam with initial settlement

The number of redundancies has now been reduced by one (since  $M_B = M_p$ ) while the compatibility condition represented by Equation (10.7) no longer applies. Substitution of  $\theta_A = wL^3/144EI$  and  $M_B = M_p$  in Equations (10.4) and (10.7) gives

$$M_A = \frac{5wL^2}{48} - \frac{M_p}{2}$$

$$M_C = \frac{7wL^2}{96} - \frac{M_p}{4}$$

Using these new values for  $M_A$  and  $M_C$  the bending-moment diagram Fig. 10.10(b) is obtained and inspection of the diagram shows that the second plastic hinge can be expected to occur at end A. Putting  $M_A = M_p$  gives

$$w = \frac{3M_p}{2} \times \frac{48}{5L^2} = \frac{14.4M_p}{L^2} \quad M_c = 0.8M_p$$

while Equation (10.3) gives  $\Delta_C = M_p L^2/16EI$ . The beam is now statically determinate with  $M_A = M_B = M_p$ , and eventually the third hinge forms at C when  $w$  reaches  $16M_p/L^2$  (see Fig. 10.10(c)) and  $\Delta_C = M_p L^2/12EI$ . The important point to note is that, despite the difference in initial conditions, the failure pattern, the failure load and the deflection at the point of failure (relative to the ends) are the same for the two cases. The uniqueness of the plastic limit load, i.e. its independence of initial conditions of internal stress or settlement of supports, is a general feature of plastic analysis. Deflections at the point of collapse can however be affected, as indeed they are in the second case just described, when considered relative to the original support position  $A_0B$  (Fig. 10.10(a)).

## 10.6 Plastic failure of propped cantilevers

The case of the propped cantilever under a uniformly distributed load, Fig. 10.11(a), cannot be solved quite so simply and both upper and lower bound methods described in Chapter 9 have to be used. A possible equilibrium condition is shown in Fig. 10.11(b) where the reactant line  $a_1B$  has been arranged so that the co-ordinate at the left-hand support is equal to the co-ordinate of the resultant moment diagram at mid-span. At the right-hand support the condition of zero resultant moment has to be satisfied. If the equal moments at A and C are regarded as plastic hinge ( $M_p$ ) values, the mechanism condition is satisfied. Hence  $M_p$  is an upper bound (unsafe) value and should be denoted by  $M_u$ . Considering the geometry of the moment diagram at mid-span,

$$\frac{\lambda w L^2}{8} = Cc_1 + c_1c = \frac{M_u}{2} + M_u \quad (M_u = M_p)$$

where  $\lambda$  is the load factor at rigid plastic collapse (see Section 9.3.6)

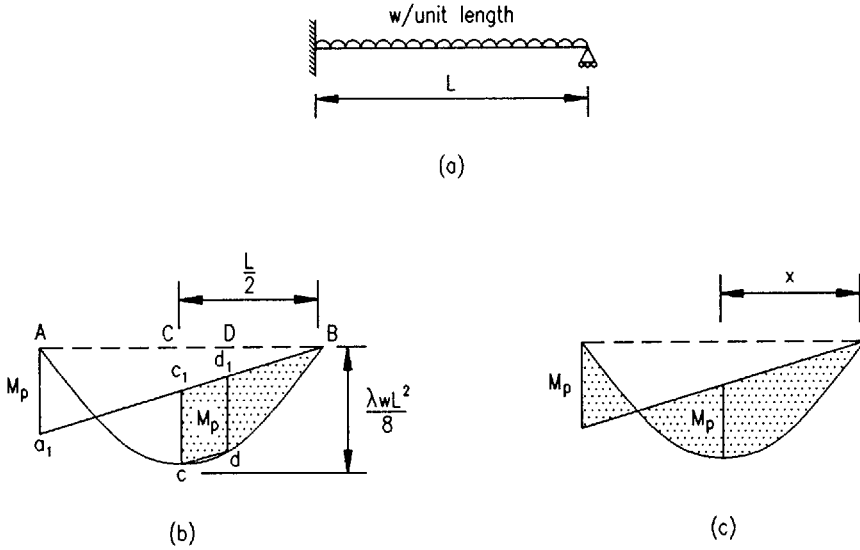


Fig. 10.11 Plastic failure of a propped cantilever

whence

$$M_c = \frac{\lambda w L^2}{12} = 0.0833 \lambda w L^2$$

By a closer inspection of the resultant moment diagram, it is readily shown that the maximum resultant moment does not occur at the mid-span, but between C and D, at  $5L/12$  from the propped support. The value of this moment is  $\lambda w L^2/11.52 (= 0.0868 \lambda w L^2)$ , which is in excess of  $M_u$ . Note that this value is based on the moment at the fixed end being  $\lambda w L^2/12$ . By making the plastic moment of the beam equal to this higher value, a bending moment diagram satisfying the equilibrium and plastic moment condition is derived, i.e. a static solution  $M_1 = 0.0868 \lambda w L^2$ . The required  $M_p$  lies between these limits,  $M_1$  and  $M_u$ , i.e.

$$0.0833 \lambda w L^2 \leq 0.0868 \lambda w L^2$$

To obtain the exact value of  $M_p$ , the sagging hinge is positioned at an unknown distance  $x$  from the right-hand support (Fig. 10.11(c)). Considering the total ordinate of the free-moment diagram at this hinge position, then

$$\frac{x}{L} M_p + M_p = \frac{\lambda w L}{2} x - \frac{\lambda w}{2} x^2$$

whence

$$M_p = \frac{\lambda w L}{2} x \left( \frac{L - x}{L + x} \right) \tag{10.8}$$

As the mechanism condition is satisfied, then any value of  $x$  inserted into Equation (10.8) will give an upper bound solution, but the safest design will be achieved when  $M_p$  is a maximum. By differentiating with respect to  $x$ , the solution  $x = (\sqrt{2} - 1)L = 0.414L$  is obtained; substituting for  $x$  in Equation (10.5) gives  $M_p = \lambda wL^2/11.66 (= 0.0858\lambda wL^2)$ . Note that this exact value of  $M_p$  lies within the range indicated by the upper and lower bounds previously calculated. This particular result is useful and can be applied directly to continuous beam problems where an end span carries a uniformly distributed load.

### Further reading for Chapter 10

- Horne M.R. & Morris L.J. (1981) *Plastic Design of Low-Rise Frames*. Constrado Monograph, Collins, London.
- Kleinlogel A. (1931) *Mehrstielige Rahmen*. Ungar, New York.
- Neal B.G. (1956) *Plastic Methods of Structural Analysis*. Chapman & Hall.

# Chapter 11

## Plane frame analysis

by JOHN RIGHINIOTIS

### 11.1 Formulae for rigid frames

#### 11.1.1 General

The formulae given in this section are based on Professor Kleinlogel's *Rahmenformeln* and *Mehrstielige Rahmen*.<sup>1</sup> The formulae are applicable to frames which are symmetrical about a central vertical axis, and in which each member has constant second moment of area.

Formulae are given for the following types of frame:

- Frame I Hingeless rectangular portal frame.
- Frame II Two-hinged rectangular portal frame.
- Frame III Hingeless gable frame with vertical legs.
- Frame IV Two-hinged gable frame with vertical legs.

The loadings are so arranged that dead, snow and wind loads may be reproduced on all the frames. For example, wind suction acting normal to the sloping rafters of a building may be divided into horizontal and vertical components, for which appropriate formulae are given, although all the signs must be reversed because the loadings shown in the tables act inwards, not outwards as in the case of suction.

It should be noted that, with few exceptions, the loads between node or panel points are uniformly distributed over the whole member. It is appreciated that it is normal practice to impose loads on frames through purlins, siderails or beams. By using the coefficients in Fig. 11.1, however, allowance can be made for many other symmetrically placed loads on the cross-beams of frames I and II shown, where the difference in effect is sufficient to warrant the corrections being made. The indeterminate BMs in the whole frame are calculated as though the loads were uniformly distributed over the beam being considered, and then all are adjusted by multiplying by the appropriate coefficient in Fig. 11.1. It may be of interest to state why these adjustments are made. In any statically indeterminate structure the indeterminate moments vary directly with the value of the following quantity:

$$\frac{\text{area of the free BM diagram}}{EI}$$

Where the loaded member is of constant cross section,  $EI$  may be ignored.

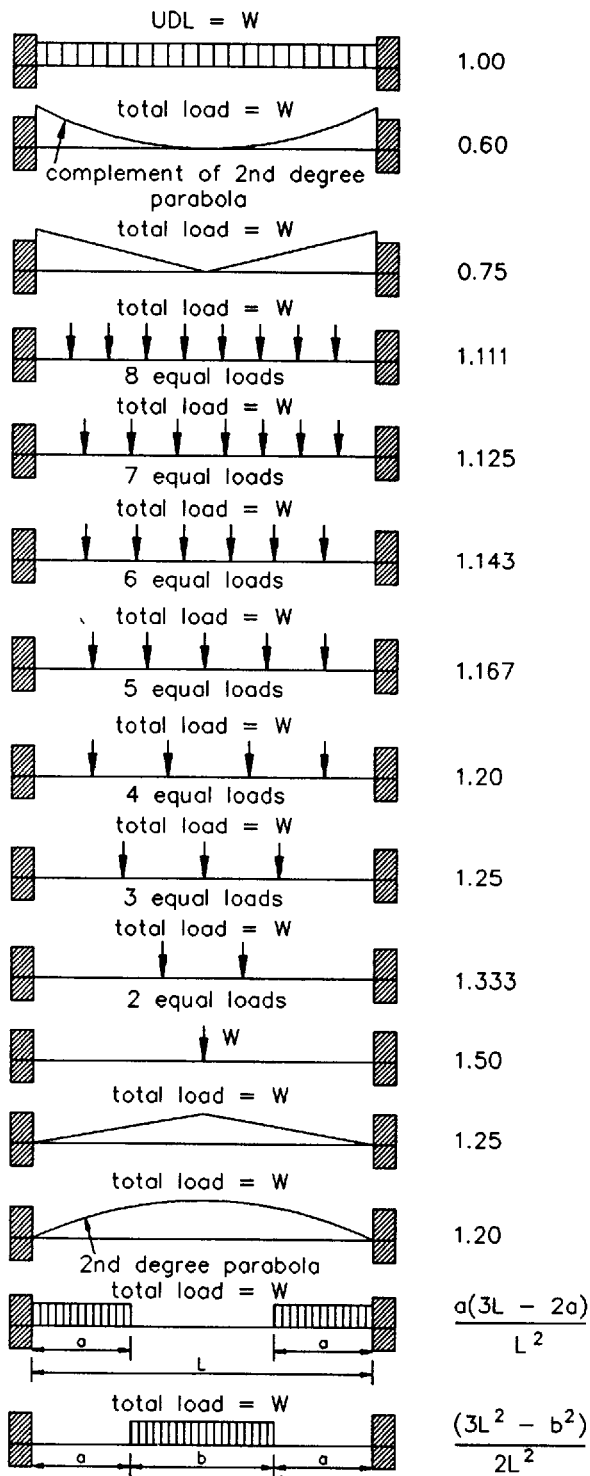


Fig. 11.1 Conversion coefficients for symmetrical loads

Consider, as an example, the case of an encastré beam of constant cross section and of length  $L$  carrying a UDL of  $W$ . Then the area of the free BM diagram is

$$\frac{WL}{8} \times \frac{2L}{3} = \frac{WL^2}{12}$$

If, however,  $W$  is a central point load, the area of the free BM diagram is

$$\frac{WL}{4} \times \frac{L}{2} = \frac{WL^2}{8}$$

The fixed end moments (FEM) due to the two types of loadings are  $WL/12$  and  $WL/8$  respectively, thus demonstrating that the indeterminate moments vary with the area of the free BM diagram and proving that the indeterminate moments are in the proportion of 1:1.5.

No rules can be laid down for the effect on the reactions of a change in the mode of application of the load, although sometimes they will vary with the indeterminate moments. Consider a simple rectangular portal with hinged feet. If a UDL placed over the whole of the beam is replaced by a central point load of the same magnitude, then the knee moments will increase by 50% with a corresponding increase in the horizontal thrusts  $H$ , while the vertical reactions  $V$  will remain the same.

Although the foregoing remarks relating to the indeterminate moments resulting from symmetrical loads apply to all rectangular portals, the rule applies for asymmetrical loads imposed upon the cross-beam of a rectangular portal frame with hinged feet. If a vertical UDL on the cross-beam is replaced by any vertical load of the same magnitude, then the indeterminate moments vary with the areas of the respective free BM diagram.

No doubt readers who use the tables frequently will learn short cuts, but it is not inappropriate to mention some. For example, if a UDL of  $W$  over the whole of a single-bay symmetrical frame is replaced by a UDL of the same magnitude of  $W$  over either the left-hand or right-hand half of the frame, the horizontal thrust at the feet is unaltered. If the frame has a pitched roof then the ridge moment will also be unaltered.

The charts in the Appendix have been prepared to assist in the design of rectangular frames or frames with a roof pitch of 1 in 5.

### 11.1.2 Arrangement of formulae

Each set of formulae is treated as a separate section. The data required for each frame, together with the constants to be used in the various formulae, are given on the first page. This general information is followed by the detailed formulae for the various loading conditions, each of which is illustrated by two diagrams placed side-by-side; the left-hand diagram giving a loading condition and the right-hand one giving the appropriate BM and reaction diagram. It should be

noted, however, that some BMs change their signs as the frames change their proportions. This will be appreciated by examining the charts.

For simple frames, i.e. for single-storey frames, the formulae for reactions immediately follow the formulae for BMs for each load.

Considering the simple frames only, the type of formula depends on the degree of indeterminacy and the shape of the frame. Auxiliary coefficients  $X$  are introduced whenever the direct expressions become complicated or for other reasons of expediency.

No hard and fast rules can be laid down for the notation and it must be noted that each set of symbols and constants applies only to the particular frame under consideration, although, of course, an attempt has been made to produce similarity in the types of symbols.

### 11.1.3 Sign conventions

All computations must be carried out algebraically, hence every quantity must be given its correct sign. The results will then be automatically correct in sign and magnitude.

The direction of the load or applied moment shown in the left-hand diagram for each load condition is considered to be positive. If the direction of the load or moment is reversed, the signs of all the results obtained from the formulae as printed must be reversed.

For simple frames, the moments causing tension on the inside faces of the frame are considered to be positive. Upward vertical reactions and inward horizontal reactions are also positive.

For multi-storey or multi-bay frames the same general rules apply to moments and vertical reactions.

### 11.1.4 Checking calculations for indeterminate frames

Calculations for indeterminate frames may be checked by using some other method of analysis, but it is also possible to check any frame or portion of a frame, such as that above the line AB in Fig. 11.2, by ensuring that the following rules are obeyed:

- (1) the three fundamental statical equations, i.e.  $\Sigma H = 0$ ,  $\Sigma V = 0$  and  $\Sigma M = 0$ , have been satisfied, and, in addition, either that
- (2) the sum of the areas of the  $M/EI$  diagram above any line, such as AB, is zero if A and B are fully fixed; or



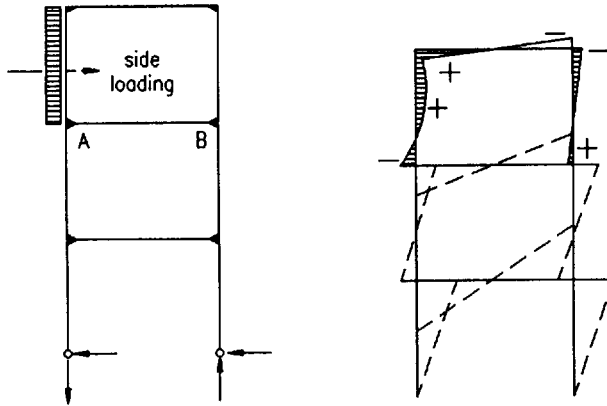


Fig. 11.2 Checking an indeterminate frame

- (3) the sum of the moments, with respect to the base AB, of the areas of the  $M/EI$  diagram above the line AB is zero if A and B are partially restrained (as shown in Fig. 11.2) or are hinged.

The underlying principles in rules (2) and (3) above are those used in the application of the 'column analogy' method of analysis.

As an example of rule (2), consider the frame in Fig. 11.3 where  $EI$  is constant.

Then the sum of the areas of the  $M/EI$  diagram, considering the legs first is,

$$\frac{2}{EI} \left[ \frac{(+0.0736 - 0.0826) \times 6.0}{2} \right] + \frac{2}{EI} \left[ \frac{(-0.0826 + 0.0893) \times 8.078}{2} \right]$$

$$= \frac{-0.054 + 0.054}{EI} = 0$$

Thus demonstrating that the moments calculated are correct.

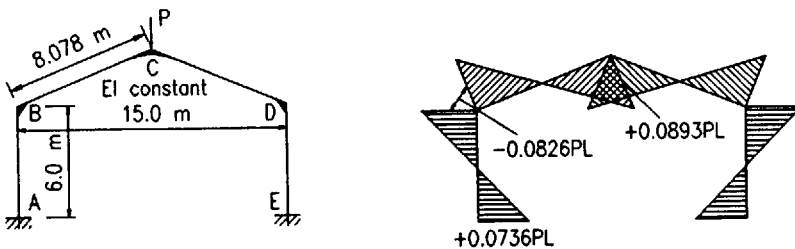


Fig. 11.3 Checking a single-bay portal – rule (2)

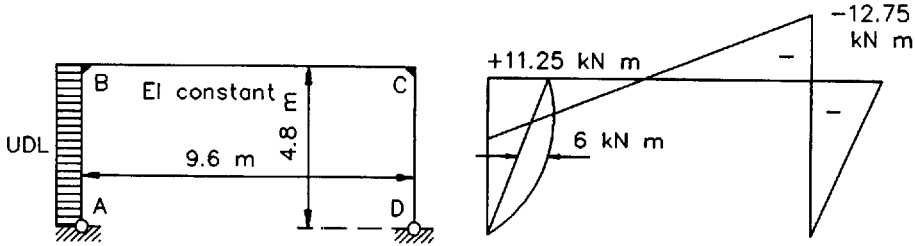


Fig. 11.4 Checking a rectangular portal – rule (3)

Now consider the frame in Fig. 11.4 as an example for rule (3).

Then the sum of the moments of the areas of the  $M/EI$  diagram, working from A round to D, is

$$\frac{1}{EI} \left\{ \left[ \frac{11.25 \times 4.8}{2} \times \frac{2 \times 4.8}{3} \right] + \left[ \frac{6 \times 4.8 \times 2}{3} \times \frac{4.8}{2} \right] \right. \\ \left. + \left[ \left( \frac{11.25 - 12.75}{2} \right) 9.6 \times 4.8 \right] + \left[ \frac{-12.75 \times 4.8}{2} \times \frac{2 \times 4.8}{3} \right] \right\} = 0 \\ \frac{1}{EI} \left[ \frac{4.8^2 \times 2}{2 \times 3} (11.25 + 6 - 4.5 - 12.75) \right] = 0$$

Demonstrating again that the calculations are correct.

## 11.2 Portal frame analysis

The design process explained here assumes that the reader is familiar with the basic concepts of limit state steel design, and the basic analysis and design of continuous beams. These notes take the form of a worked example. A method of determining preliminary member sizes has been included.

### 11.2.1 Methods of analysis

BS 5950: Part 1<sup>2</sup> allows two main methods of analysis of a structure.

- (1) *Linear elastic.* The frame is analyzed by either hand or computer assuming linear elastic behaviour. Once the forces, moments and shears have been derived by elastic analysis the ultimate capacity of each section is checked using the rules given in Section 4 of the Code.
- (2) *Simple plastic theory.* The frame is analyzed using the basic principles of

simple plastic theory. Once the forces, moments and shears have been derived by analysis the member capacities are checked. Those containing plastic hinges are checked in accordance with Section 4.

### *Elastic analysis*

Using elastic analysis it is to be expected that the structure will be heavier than that designed by plastic methods, but less stability bracing will be needed. It may well be that the final details will also be more simple.

It will remain the engineer's responsibility to ensure that stability is provided both locally and in the overall condition. BS 5950: Part 1<sup>2</sup> provides no specific rules regarding the stability of the frame as a whole; this means that the engineer must ensure that the stability is checked using the general rules for all frames. He must also check that the movement of the frame under all loading cases is not sufficient to cause damage to adjacent construction, i.e. brick walls or cladding, the serviceability limit state of deflection.

### *Plastic analysis*

The method of calculating the ultimate load of a portal frame is described in many publications. The main essence of the method is to assume that plastic 'hinges' occur at points in the frame where the value of  $M/M_p$  is at its highest value; the load being considered as increasing proportionally until the failure or ultimate state is reached. Because of the straining at the hinge points it is essential that the local buckling and lateral distortion do not occur before failure. Failure is deemed to have taken place when sufficient hinges have formed to create a mechanism.

The member capacities are calculated using the rules given in Section 4 of the Code but with the additional restrictions applied to hinge positions. In addition, positive requirements are put on checking frame stability for both single-bay and multi-bay frames. Plastic designed frames are lighter than elastic designed frames, providing deflection is not a governing point; however, additional bracing may well be required.

## **11.2.2 Stability**

With the use of lighter frames, various aspects of stability take a more prominent part in the design procedures. As far as portal frames are concerned the following areas are important:

- (1) overall frame stability, in that the strength of the frame should not be affected by changes in geometry during loading ( $P\Delta$  effect)

- (2) snap-through stability, in multi-bay frames (three or more), where the effects of continuity can result in slender rafters
- (3) plastic hinge stability, where the member must be prevented from moving out of plane or rotating at plastic hinges
- (4) rafter stability, ensuring that the rafter is stable in bending as an unrestrained beam
- (5) leg stability, where the leg below the plastic hinge must be stable
- (6) haunch stability, where the tapered member is checked to ensure that the inner (compression flange) is stable.

### 11.2.3 Selecting suitable members for a trial design

The design of a portal frame structure is in reality a process of selecting suitable members and then proving their ability to perform in a satisfactory manner. Inexperienced engineers can be given some guidance to estimate initial member sizes. In order to speed the initial selection of members, three graphs have been produced to enable simple pin-based frames to be sized quickly.

These graphs have been prepared making the following assumptions:

- (1) plastic hinges are formed at the bottom of the haunch in the leg and near the apex in the rafter, the exact position being determined by the frame geometry
- (2) the depth of the rafter is approximately span/55 and the depth of the haunch below the eaves intersection is 1.5 times rafter depth
- (3) the haunch length is 10% of the span of the frame, a limit generally regarded as providing a balance between economy and stability
- (4) the moment in the rafter at the top of the haunch is  $0.87M_p$ , i.e. it is assumed that the haunch area remains elastic
- (5) the calculations assume that the calculated values of  $M_p$  are provided exactly by the sections and that there are no stability problems. Clearly these conditions will not be met and it is the engineer's responsibility to ensure that the chosen sections are fully checked for all aspects of behaviour.

The graphs cover the range of span/eaves height between 2 and 5 and rise/span of 0 to 0.2 (where 0 is a flat roof). Interpolation is permissible but extrapolation is not. The three graphs give:

Figure 11.5: the horizontal force at the feet of the frame as a proportion of the total factored load  $wL$ , where  $w$  is the load/unit length of rafter and  $L$  is the span of the frame

Figure 11.6: the value of the moment capacity required in the rafters as a proportion of the load times span  $wL^2$

Figure 11.7: the value of the moment capacity required in the legs as a proportion of the load times span  $wL^2$ .

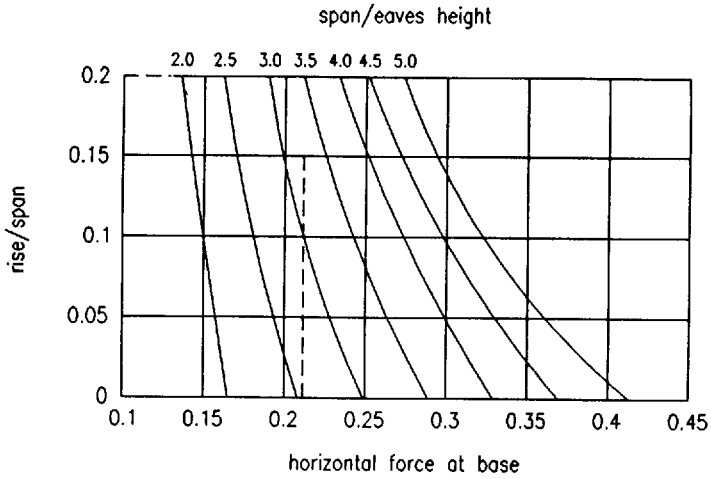


Fig. 11.5 Rise/span against horizontal force at base for various span/eaves heights

The graphs are non-dimensional and may be used with any consistent set of units. In the worked example kilonewtons and metres are used.

*Method of use of the graphs*

- (1) Determine the ratio span/height to eaves.
- (2) Determine the ratio rise/span.

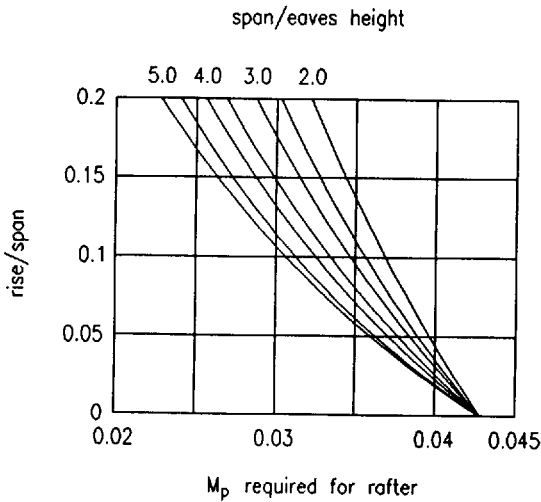


Fig. 11.6 Rise/span against required  $M_p$  of rafter for various span/eaves heights

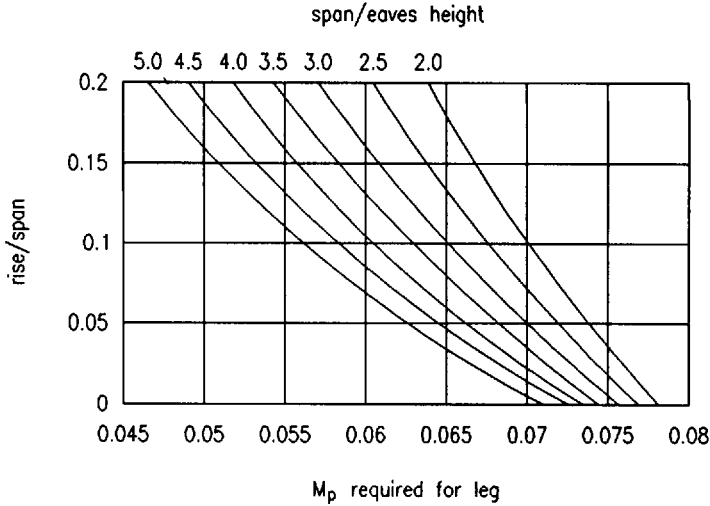


Fig. 11.7 Rise/span against required  $M_p$  of leg for various span/eaves heights

- (3) Calculate  $wL$  (total load) and  $wL^2$ .
- (4) Look up the values from the graphs.
- (5) Horizontal force at root of frame = value from Fig. 11.5  $\times wL$ .
- (6)  $M_p$  required in rafter = value from Fig. 11.6  $\times wL^2$ .
- (7)  $M_p$  required in leg = value from Fig. 11.7  $\times wL^2$ .

### 11.2.4 Worked example of plastic design (see Fig. 11.8)

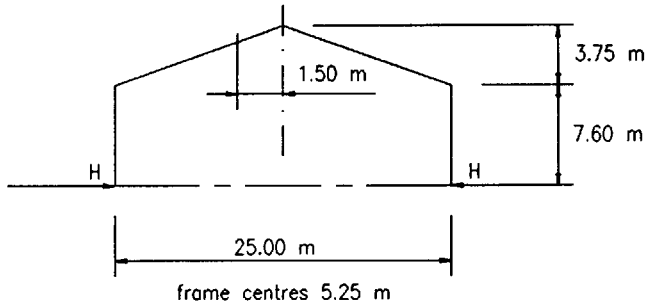
#### Determination of member sizes

Although the engineer may use his experience or other methods to determine preliminary member sizes, the graphs in Figs 11.5, 11.6 and 11.7 will be used for this example. In order to use these graphs, four parameters are required:

|                            |                                 |             |
|----------------------------|---------------------------------|-------------|
| span/height to eaves       | = 25/7.6                        | = 3.29      |
| rise/span                  | = 3.75/25                       | = 0.15      |
| $wL$ (total load on frame) | = 9.48 $\times$ 25              | = 237 kN    |
| $wL^2$                     | = 9.48 $\times$ 25 <sup>2</sup> | = 5925 kN m |

Horizontal thrust at feet of frame (Fig. 11.5)  
 = 0.21  $\times$  237 = 49.8 kN

Moment capacity of rafter (Fig. 11.6)  
 = 0.0305  $\times$  5925 = 181 kN m



| loading | unfactored design      | load factor | factored load         | total factored load |
|---------|------------------------|-------------|-----------------------|---------------------|
| imposed | 0.75 kN/m <sup>2</sup> | 1.6         | 1.2 kN/m <sup>2</sup> | 158 kN              |
| dead    | 0.43 kN/m <sup>2</sup> | 1.4         | 0.6 kN/m <sup>2</sup> | 79 kN               |
| total   |                        |             |                       | 237 kN              |

factored load/m (*w*) = 237/25 = 9.48 kN/m

Fig. 11.8 Portal frame design example

Moment capacity of leg (Fig. 11.7)  
 $= 0.059 \times 5925 = 350 \text{ kN m}$

Assuming a design strength of 275 N/mm<sup>2</sup> (grade 43 steel):

$S_x$  required for rafter =  $181 \times 1000/275 = 658 \text{ cm}^3$   
 $S_x$  required for leg =  $350 \times 1000/275 = 1270 \text{ cm}^3$

Trial sections (*NB* these are first trials and may not be adequate):

Rafter 406 × 140 × 39 kg UB (grade 43 steel);  
 $S_x = 721 \text{ cm}^3, I_x = 12\,500 \text{ cm}^4$

Leg 457 × 152 × 60 kg UB (grade 43 steel);  
 $S_x = 1280 \text{ cm}^3, I_x = 25\,500 \text{ cm}^4$

It is suggested that the next stage is to check the overall stability of the frame. The main reason for this is that the only way to correct insufficient stability is to change the main member sizes. If any other checks are not satisfied, additional bracing can frequently be used to rectify the situation, without altering the member sizes.

## References to Chapter 11

1. Kleinlogel A. (1931) *Mehrstielige Rahmen*. Ungar, New York.
2. British Standards Institution (1990) *Structural use of steelwork in building*. Part 1: *Code of practice for design in simple and continuous construction: hot rolled sections*. BS 5950, BSI, London.

## Further reading for Chapter 11

- Baker J.F. (1954) *The Steel Skeleton, Vol. 1*, 1st edn. Cambridge University Press.
- Baker J.F., Horne M.R. & Heyman J. (1956) *The Steel Skeleton, Vol. 2*. Cambridge University Press.
- Horne M.R. & Morris L.S. (1981) *Plastic Design of Low-Rise Frames*. Constrado Monograph, Collins, London.
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# Chapter 12

## Applicable dynamics

by MICHAEL WILLFORD

### 12.1 Introduction

The dynamic performance of steel structures has traditionally only been an area of interest for special classes of structure, particularly slender wind-sensitive structures (masts, towers and stacks), structures supporting mechanical equipment, offshore structures and earthquake-resistant structures. However, a wider interest in dynamic behaviour has recently come about as a result of the widespread adoption of long span composite floors in buildings, for which vibration criteria must be satisfied.

Dynamic loads in structures may arise from a number of sources including the following:

- Forces generated inside a structure – Machinery
  - Impacts
  - Human activity (walking, dancing, etc.)
- External forces
  - Wind buffeting and other aerodynamic effects
  - Waves (offshore structures)
  - Impacts from vehicles, etc.
- Ground motions
  - Earthquakes
  - Ground-borne vibration due to railways, roads, pile driving, etc.

The principal effects of concern are:

- Strength – The structure must be strong enough to resist the peak dynamic forces that arise.
- Fatigue – Fatigue cracks can initiate and propagate when large numbers of cycles of vibration inducing significant stress are experienced, leading to reduction in strength and failure.
- Perception – Human occupants of a building can perceive very low amplitudes of vibration, and, depending on the circumstances, may find vibration objectionable. Certain items of precision equipment are also extremely sensitive to vibration. Perception will generally be the most onerous dynamic criterion in occupied buildings.

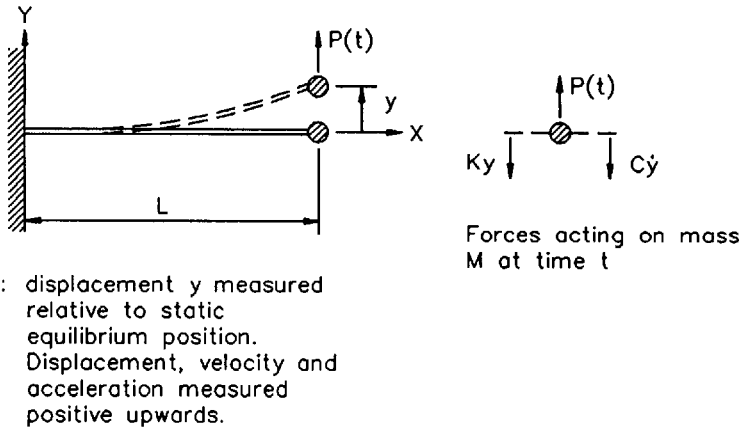


Fig. 12.1 Example of a dynamic system

It is beyond the scope of this book to address all these issues, and references are suggested for more detailed guidance. The following sections are intended to give an overview of the fundamental features of dynamic behaviour and to introduce some of the terminology employed and analysis procedures available. It must be borne in mind that dynamic behaviour is influenced by a larger number of parameters than static behaviour, and that some of the parameters cannot be predicted precisely at the design stage. It is often advisable to investigate the effects of varying initial assumptions to ensure that the most critical situations that may occur have been examined.

## 12.2 Fundamentals of dynamic behaviour

The principal features of dynamic behaviour may be illustrated by the examination of a very simple dynamic system, a concentrated mass  $M$  supported on a light cantilever of flexural rigidity  $EI$  and length  $L$  as illustrated in Fig. 12.1. The mass is subjected to forces  $P$  which vary with time  $t$ .

### 12.2.1 Dynamic equilibrium

One of the basic methods of dynamic analysis is the examination of dynamic equilibrium to formulate an equation of motion. Consider the dynamic equilibrium of the mass illustrated in Fig. 12.1. If at some time  $t$  the mass is displaced upwards from its static equilibrium position by  $y$ , and has velocity  $\dot{y}$  and acceleration  $\ddot{y}$  (positive upwards) the mass is in general subjected to the following forces:

Table 12.1

| Mass   | Force | Displacement | Time |
|--------|-------|--------------|------|
| kg     | N     | m            | s    |
| tonnes | kN    | m            | s    |

External force  $P(t)$   
 Stiffness force  $Ky$  ( $K = 3EI/L$  for uniform cantilever)  
 Damping force  $C\dot{y}$  (a dissipative force assumed to act in the opposite direction to the velocity).

The resultant of these forces will cause the mass to accelerate according to Newton's 2nd law of motion. Hence the dynamic equilibrium equation may be written as:

$$M\ddot{y} = P(t) - Ky - C\dot{y}$$

or

$$M\ddot{y} + C\dot{y} + Ky = P(t) \tag{12.1}$$

Equation (12.1) is the general equation of motion for a single degree of freedom dynamic system (a system whose behaviour can be defined by a single quantity, in this case the deflection of the mass,  $y$ ). It is clearly most important that the quantities in this equation are defined in dynamically consistent units. Examples of consistent units are given in Table 12.1.

Various solutions to Equation (12.1) can give an insight into the principal features of dynamic behaviour.

### 12.2.2 Undamped free vibration

In this case it is assumed that the system has been set into motion in some way and is then allowed to vibrate freely in the absence of external forces. It is also assumed initially that there is no damping.

The corresponding equation of motion derived from Equation (12.1) is:

$$M\ddot{y} + Ky = 0 \tag{12.2}$$

By putting  $K/M = \omega_n^2$  it is easily shown that a motion of the form  $y = Y \cos \omega_n t$  satisfies this equation. This is known as simple harmonic motion; the mass oscillates about its static equilibrium position with amplitude  $Y$  as shown in Fig. 12.2.  $\omega_n$  is known as the circular frequency, measured in radians per second. There are  $2\pi$  radians in a complete cycle of vibration and so the vibration frequency,  $f_n$ , is  $\omega_n/2\pi$  cycles per second (hertz). In the absence of damping or external forces the system will vibrate in this manner indefinitely.

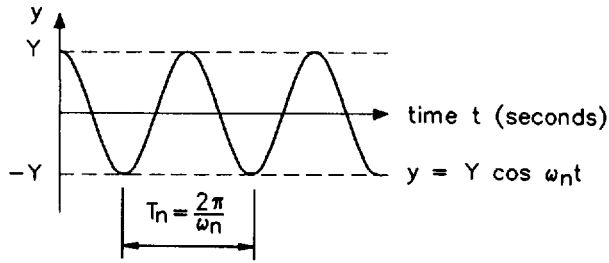


Fig. 12.2 Simple harmonic motion

The amplitude of vibration  $Y$  is the peak displacement of the mass relative to its static equilibrium position. Vibration amplitudes are sometimes referred to as root mean square (rms) quantities, where  $y_{\text{rms}} = \frac{1}{T} \sqrt{\left(\int_0^T y^2 dt\right)}$ , and  $T$  is the total time over which the vibration is considered. For continuous simple harmonic motion  $y_{\text{rms}} = Y/\sqrt{2}$ .

### 12.2.3 Damped free vibration

Energy is always dissipated to some extent during vibration of real structures. Inclusion of the damping force in the free vibration equation of motion leads to:

$$M\ddot{y} + C\dot{y} + Ky = 0 \quad (12.3)$$

The solution to this equation for a lightly damped system when the mass is initially displaced by  $Y$  and then released is:

$$y = Ye^{-\xi\omega_n t} \cos(\omega_d t - \phi) \quad (12.4)$$

The motion takes the form shown in Fig. 12.3(a), and it can be seen that the vibration amplitude decays exponentially with time. The rate of decay is governed by the amount of damping present.

If the damping constant  $C$  is sufficiently large then oscillation will be prevented and the motion will be as in Fig. 12.3(b). The minimum damping required to prevent overshoot and oscillation is known as critical damping, and the damping constant for critical damping is given by  $C_o = 2\sqrt{KM}$ , where  $K$  and  $M$  are the stiffness and mass of the system.

Practical structures are lightly damped and the damping present is often expressed as a proportion of critical. In Equation (12.4)

$$\xi = \text{critical damping ratio} = \frac{C}{C_o}$$

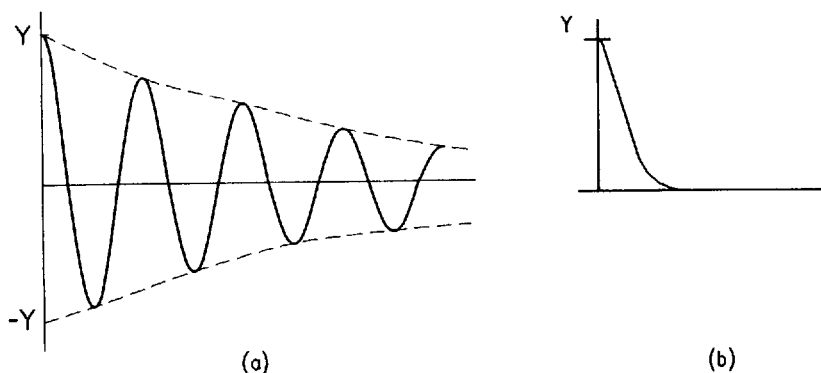


Fig. 12.3 Damped free vibration: (a) lightly damped system, (b) critically damped system

The phase shift angle  $\phi$  is small when the damping is small.

The frequency of damped oscillation is:

$$\omega_d = \omega_n (1 - \xi^2)^{\frac{1}{2}} \text{ radians/s}$$

where  $\omega_n$  is the undamped natural frequency. With low damping ( $\xi \ll 1$ ) the reduction of natural frequency (increase in natural period) resulting from damping is negligible.

#### 12.2.4 Response to harmonic loads

A load which varies sinusoidally with time at a constant frequency is known as a harmonic load. This form of dynamic load is characteristic of machinery operating at constant speed and many other types of continuous vibration can be approximated to this form.

When such a force of amplitude  $P$  and frequency  $f$  Hz (or  $\omega = 2\pi f$  radians/s) is applied to the simple structure described in previous sections the structure will be caused to vibrate. After some time the motions of the structure will reach a steady-state, that is, vibration of a constant amplitude and frequency will be achieved. The dynamic equation of motion is:

$$M\ddot{y} + C\dot{y} + Ky = P \cos \omega t \quad (12.5)$$

and it can be shown that the steady-state response motion is described by:

$$y = Y \cos (\omega t - \phi) \quad (12.6)$$

Note that the steady-state vibration occurs at the frequency of the harmonic force exciting the motion, not at the natural frequency of the structure.

The displacement amplitude  $Y$  can be shown to be:

$$Y = \frac{P}{K} \frac{1}{\left\{ \left[ 1 - \left( \frac{\omega}{\omega_n} \right)^2 \right]^2 + \left( 2\xi \frac{\omega}{\omega_n} \right)^2 \right\}^{\frac{1}{2}}} \quad (12.7)$$

$P/K$  is the deflection of the structure under a static force  $P$ , and the multiplying term can be regarded as a magnification factor. The variation of magnification factor with frequency ratio and damping ratio is shown in Fig. 12.4.

When the dynamic force is applied at a frequency much lower than the natural frequency of the system ( $\omega/\omega_n \ll 1$ ), the response is quasi-static; the response is governed by the stiffness of the structure and the amplitude is close to the static deflection  $P/K$ .

When the dynamic force is applied at a frequency much higher than the natural frequency ( $\omega/\omega_n \gg 1$ ), the response is governed by the mass (inertia) of the structure; the amplitude is less than the static deflection.

When the dynamic force is applied at a frequency close to the natural frequency, the stiffness and inertia forces in the vibrating system are almost equal and opposite at any instant, and the external force is resisted by the damping force. This is the condition known as resonance, when very large dynamic magnification factors are possible. When damping is low the maximum steady-state magnification occurs when  $\omega \approx \omega_n$ , and then

$$Y = \frac{P}{K} \frac{1}{2\xi} \quad (12.8)$$

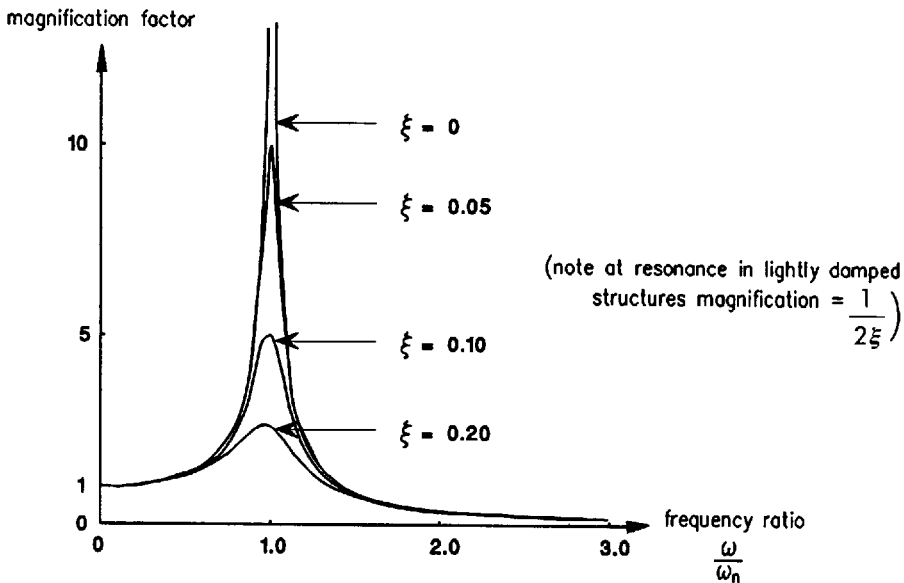


Fig. 12.4 Steady-state response to harmonic loads

Since in many structural systems  $\xi$  is of the order of 0.01, magnification factors of the order of 50 may result. The force in the structure is proportional to the displacement so the same magnification factor applies to structural forces.

Human perception of motion is usually related to acceleration levels rather than displacement. The peak acceleration amplitude at steady-state is given by:

$$\begin{aligned}\hat{a} &= \omega^2 Y \\ &= (2\pi f)^2 Y\end{aligned}\quad (12.9)$$

In practice, there is usually advantage in avoiding the possibility of resonance whenever possible by ensuring that structural frequencies are well away from the frequencies of any known sources of substantial dynamic force.

### 12.2.5 Response to an impact

Another dynamic loading case of interest is the response of a structure to an impact, say from an object falling on to the structure. A full discussion of impact loading is given in Reference 1, but a simple approximate method is useful for many practical situations when the mass of the impacting object is small compared to the mass of the structure, and the impact duration is short compared to the natural period of the structure. In these cases the effect of the impact can be assessed as an impulse  $I$  acting on the structure. The magnitude of  $I$  may be calculated as  $m \Delta v$ , where  $m$  is the mass of the falling object and  $\Delta v$  its change in velocity at impact. If there is no rebound  $\Delta v$  can be taken as the approach velocity. For the simple system discussed in previous sections conservation of momentum at impact requires the initial velocity of the structural mass to be  $I/M$ . A lightly damped system then displays damped free vibration corresponding to an initial displacement amplitude of approximately:

$$Y = \frac{I}{\omega_n M} = \frac{I}{2\pi f_n M} \quad (12.10)$$

### 12.2.6 Response to base motion

The previous sections have illustrated the behaviour of a dynamic system with a fixed base subject to applied forces. When the dynamic excitation takes the form of base motion, as for example in an earthquake, the formulation of the equation of motion and the solutions are slightly modified. Detailed treatment of this type of excitation is beyond the scope of this chapter and References 1 and 2 are recommended for discussion of the solutions.

Although not correct in detail, the general form of response indicated by Fig. 12.4 for harmonic applied forces is still relevant. Resonance occurs for those components of the base motion close in frequency to the natural frequency of the structure.

### 12.2.7 Response to general time-varying loads

Although some dynamic loads (e.g. impacts and harmonic loads) are simple and can be dealt with analytically, many forces and ground motions that occur in practice are complex.

In general, numerical analysis procedures are required for the evaluation of responses to these effects, and these are often available in finite element analysis programs.

The techniques employed include:

- direct step-by-step integration of the equations of motion using small time increments,
- Fourier analysis of the forcing function followed by solution for Fourier components in the frequency domain,
- for random forces, random vibration theory and spectral analysis.

The background and application of these techniques are discussed in References 1 and 3.

## 12.3 Distributed parameter systems

The dynamic system considered in section 12.2 was simple in that its entire mass was concentrated at one point. This enabled Newton's second law and therefore the equation of motion to be written in terms of a single variable.

Although some practical structures can be represented adequately in this way, in other cases it is not realistic to assume that the mass is concentrated at one point. The classical treatment of distributed systems is illustrated below by analysis of a uniform beam; similar techniques can be used for two-dimensional (plate) structures. The analysis calculates the natural frequency of the beam and, by reference to section 12.2.2, this can be done by ignoring external forces and damping forces.

### 12.3.1 Dynamic equilibrium

The beam under consideration is shown in Fig. 12.5. For a small element of the beam of length  $dx$  the variation of shear force  $V$  along the beam results in a net force on the element of  $\frac{\partial V}{\partial x} dx$  which must cause the mass  $m dx$  to accelerate.

Dynamic equilibrium therefore requires:

$$\frac{\partial V}{\partial x} dx = m dx \frac{\partial^2 y}{\partial t^2} \quad (12.11)$$



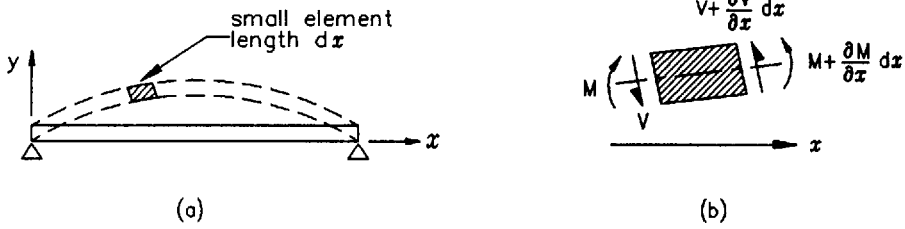


Fig. 12.5 Dynamic equilibrium of vibrating beams. (a) Uniform beam mass/unit length =  $m$ , (b) small element mass =  $m dx$

For a flexural beam the deflection  $y$  is a function of the bending moment distribution, with:

$$\frac{\partial^2 y}{\partial x^2} = \frac{M}{EI}$$

Noting also that for moment equilibrium on the element:

$$V = -\frac{\partial M}{\partial x}$$

$$\frac{\partial V}{\partial x} = -\frac{\partial^2 M}{\partial x^2}$$

Substituting these relationships into Equation (12.11) leads to the equation of motion for a flexural beam:

$$\frac{\partial^4 y}{\partial x^4} + \frac{m}{EI} \frac{\partial^2 y}{\partial t^2} = 0 \tag{12.12}$$

It is sometimes convenient to represent an entire framed structure as a shear beam. In this case the deflection  $y$  is a function of the shear force with:

$$\frac{\partial y}{\partial x} = \frac{V}{GA_s}$$

The equation of motion for a shear beam is therefore:

$$\frac{\partial^2 y}{\partial x^2} - \frac{m}{GA_s} \frac{\partial^2 y}{\partial t^2} = 0 \tag{12.13}$$


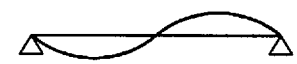


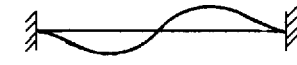


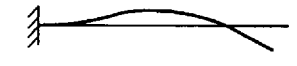
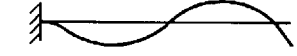
### 12.3.2 Modes of vibration

The partial differential equations derived above can be solved for given sets of boundary conditions. The solution in each case identifies a family of modes of

vibration (eigenvectors) with corresponding natural frequencies (eigenvalues). The mode shape describes the relative displacements of the various parts of the beam at any instant in time.

A number of standard results are given in Tables 12.2 and 12.3, and more comprehensive lists are contained in References 4 and 5.

**Table 12.2** Natural frequencies of uniform flexural beams

|                  |   | Length = $L$ (m) (typical units)   |                                       |  |
|------------------|---|--|---------------------------------------|--|
|                  |   | Flexural rigidity = $EI$ ( $\text{N m}^2$ )  |                                       |  |
|                  |   | Mass/unit length = $m$ (kg/m)  |                                       |  |
|                  |   | $f_n = \frac{k_n}{2\pi} \sqrt{\left(\frac{EI}{mL^4}\right)}$ Hz: values of $k_n$ given below |                                       |  |
| Mode             | Shape   | $k_n$  | Nodal points at $x/L =$               |  |
| Simply-supported |    | 9.87   | 0 1                                   |  |
|                  |    | 39.5   | 0 0.5 1                               |  |
|                  |    | 88.8   | 0 0.333 0.667 1                       |  |
|                  | $x = \sin\left(n\pi\frac{x}{L}\right)$  | $n^2\pi^2$   | $0 \frac{1}{n} \dots \frac{n-1}{n} 1$ |  |
| Encastré         |  | 22.4   | 0 1                                   |  |
|                  |  | 61.7   | 0 0.5 1                               |  |
|                  |  | 121  | 0 0.359 0.641 1                       |  |
| Cantilever       |  | 3.52   | 0                                     |  |
|                  |  | 22.0   | 0 0.774                               |  |
|                  |  | 61.7   | 0 0.5 0.868                           |  |

**Table 12.3** Natural frequencies for uniform shear cantilevers

| Length = $L$ (m) (typical units)<br>Shear rigidity = $GA_s$ (N)<br>Mass/unit length = $m$ (kg/m)<br>$f_n = \frac{k_n}{2\pi} \sqrt{\left(\frac{GA_s}{mL^2}\right)}$ Hz: values of $k_n$ given below |  |                          |   |
|--|--|--------------------------|---|
| Mode   | Shape  | $k_n$                    | Nodal points at $x/L =$   |
| 1  |  | 1.57                     | 0   |
| 2  |  | 4.71                     | 0 0.667   |
| 3  |  | 7.85                     | 0 0.4 0.8   |
| $n$  | $y = \sin\left((2n - 1) \frac{\pi x}{2L}\right)$ | $(2n - 1) \frac{\pi}{2}$ | 0 $\frac{2}{(2n - 1)}$ $\frac{4}{(2n - 1)}$ $\frac{6}{(2n - 1)}$ etc. |

### 12.3.3 Calculation of responses

For linear elastic behaviour, once the mode shapes and frequencies have been established, dynamic responses can be calculated treating each mode as a single degree of freedom system such as the one described in section 12.2.2. In theory distributed systems have an infinite number of modes of vibration, but in practice only a few modes, usually those of lowest frequency, will contribute significantly to the overall response.

It is convenient to describe a mode shape by a displacement parameter  $\phi$  defined (or normalized) such that the maximum value at any point is 1.0. If the mode is excited by dynamic forces resulting in a modal response amplitude of  $Y_m$ , then the displacement amplitude at a point  $i$  on the structure is:

$$y_i = \phi_i Y_m$$

where  $\phi_i$  is the mode shape value at the point.

The magnitude of  $Y_m$  can be calculated for simple dynamic loads treating the mode as a single degree of freedom system having the following properties. These are often referred to as modal or generalized properties:

$$\begin{array}{lll} \text{modal mass} & M^* = \sum M_i \phi_i^2 & \text{sum over whole structure} \\ \text{modal stiffness} & K^* = \omega_n^2 M^* & \\ \text{modal force} & P^* = \sum P_i \phi_i & \text{sum for all loaded points} \end{array}$$

Note that for mode  $n$  of a uniform simply-supported beam of span  $L$  and mass/unit length  $m$  with  $\phi = \sin(n\pi x/L)$ , the modal mass  $M^*$  is:

$$M^* = m \int_0^L [\sin(n\pi x/L)]^2 dx$$

which is  $0.5 mL$  (half the total mass of the beam).

The application of these concepts to the problems of floor vibration and wind-induced vibration is described in References 6 and 7.

### 12.3.4 Approximate methods to determine natural frequency

Approximate methods are useful for estimating the natural frequencies of structures not conforming with one of the special cases for which standard solutions exist, and for checking the predictions of computer analyses when these are used.

One of the most useful approximate methods relates the natural frequency of a system to its static deflection under gravity load,  $\delta$ . With reference to section 12.2.2 the natural frequency of a single lumped mass system is:

$$f_n = \frac{1}{2\pi} \sqrt{\left(\frac{K}{M}\right)}$$

This may be rewritten, replacing the mass term  $M$  by the corresponding *weight*  $Mg$  as:

$$f_n = \frac{\sqrt{g}}{2\pi} \sqrt{\left(\frac{K}{Mg}\right)}$$

Since  $Mg/K$  is the static deflection under gravity load ( $\delta$ )

$$\begin{aligned} f_n &= \frac{\sqrt{g}}{2\pi \sqrt{\delta}} \\ &= 15.76/\sqrt{\delta} \quad \text{when } \delta \text{ is measured in mm} \end{aligned} \tag{12.14}$$

This formula is exact for any single lumped mass system.

For distributed parameter systems a similar correspondence is found, although the numerical factor in Equation (12.14) varies from case to case, generally between 16 and 20. For practical purposes a value of 18 will give results of sufficient accuracy.

When applying these formulae the following points should be noted.

- (1) The static deflection should be calculated assuming a weight corresponding to the loading for which the frequency is required. This is usually a dead load with an allowance for expected imposed load.

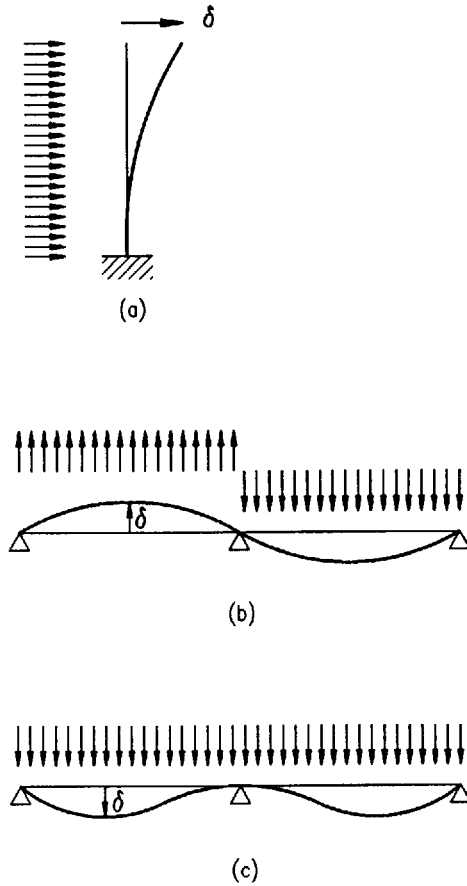


Fig. 12.6 Use of gravity deflections to estimate natural frequencies. (a) For a vertical structure the gravity load is applied horizontally:  $f_n \approx 18/\sqrt{\delta}$ . (b) Continuous structure gravity load applied in opposite directions on alternate spans:  $f_n \approx 18/\sqrt{\delta}$ . (c) Continuous structure – symmetric mode has higher frequency:  $f_n \approx 18/\sqrt{\delta}$

- (2) For horizontal modes of vibration (e.g. lateral vibration of an entire structure) the gravity force must be applied laterally to obtain the appropriate lateral deflection, as shown in Fig. 12.6(a).
- (3) The mode shape required must be carefully considered in multi-span structures. In the two-span beam of Fig. 12.6(b) the lowest frequency will correspond to an asymmetrical mode as illustrated; the corresponding  $\delta$  must be obtained by applying gravity in opposite directions on the two spans. The normal gravity deflection will correspond to the symmetrical mode with a higher natural frequency, Fig. 12.6(c).

These concepts can be extended to estimating the natural frequencies of primary beam – secondary beam systems. If the static deflection of the primary beam is  $\delta_p$  and the static deflection of a secondary beam is  $\delta_s$  (relative to the primary) the combined natural frequency is approximately:

$$f_n = \frac{18}{\sqrt{(\delta_p + \delta_s)}}$$

from which it can be shown that

$$\frac{1}{f_n^2} = \frac{1}{f_p^2} + \frac{1}{f_s^2} \quad (12.15)$$

where  $f_p$  and  $f_s$  are the natural frequencies of the primary and secondary beams alone.

Care must always be taken in using these formulae so that a realistic mode shape is implied. There will generally be continuity between adjacent spans at small amplitudes even in simply-supported designs and in many situations a combined mode where both the primaries and secondaries are vibrating together in a 'simply-supported' fashion is not possible.

## 12.4 Damping

Damping arises from the dissipation of energy during vibration. A number of mechanisms contribute to the dissipation, including material damping, friction at interfaces between components and radiation of energy from the structure's foundations.

Material damping in steel provides a very small amount of dissipation and in most steel structures the majority of the damping arises from friction at bolted connections and frictional interaction with non-structural items, particularly partitions and cladding. Damping is found to increase with increasing amplitude of vibration.

The amount of damping that will occur in any particular structure cannot be calculated or predicted with a high degree of precision, and design values for damping are generally derived from dynamic measurements on structures of a corresponding type.

Damping can be measured by a number of methods, including:

- rate of decay of free vibration following an impact (Fig. 12.3(a))
- forced excitation by mechanical vibrator at varying frequency to establish the shape of the steady-state resonance curve (Fig. 12.4)
- spectral methods relying on analysis of response to ambient random vibration such as wind loading.

**Table 12.4**

| Structure type  | Structure damping (% critical)                                |
|---|---|
| Unclad welded steel structures<br>(e.g. steel stacks) | 0.3%  |
| Unclad bolted steel structures                        | 0.5%  |
| Floor (fitted out), composite and<br>non-composite    | 1.5% – 3%<br>(may be higher when many<br>partitions on floor) |
| Clad buildings (lateral sway)                         | 1%  |

All these methods can run into difficulty when several modes close in frequency are present. One result of this is that on floor structures where there are often several closely spaced modes the apparent damping seen in the initial rate of decay after impact can be substantially higher than the true modal damping.

Damping is usually expressed as a fraction or percentage of critical ( $\xi$ ), but the logarithmic decrement ( $\delta$ ) is also used. The relationship between the two expressions is  $\xi = \delta/2\pi$ .

Table 12.4 gives values of modal damping that are suggested for use in calculations when amplitudes are low (e.g. for occupant comfort). Somewhat higher values are appropriate at large amplitudes where local yielding may develop, e.g. in seismic analysis.

## 12.5 Finite element analysis

Many simple dynamic problems can be solved quickly and adequately by the methods outlined in previous sections. However there are situations where more detailed numerical analysis may be required and finite element analysis is a versatile technique widely available for this purpose. Numerical analysis is often necessary for problems such as:

- (1) determination of natural frequencies of complex structures
- (2) calculation of responses due to general time-varying loads or ground motions
- (3) response spectrum analysis to determine seismic design forces.

### 12.5.1 Basis of the method

As explained in Chapter 9 the finite element method describes the state of a structure by means of deflections at a finite number of node points. Nodes are connected by elements which represent the stiffness of the structural components.

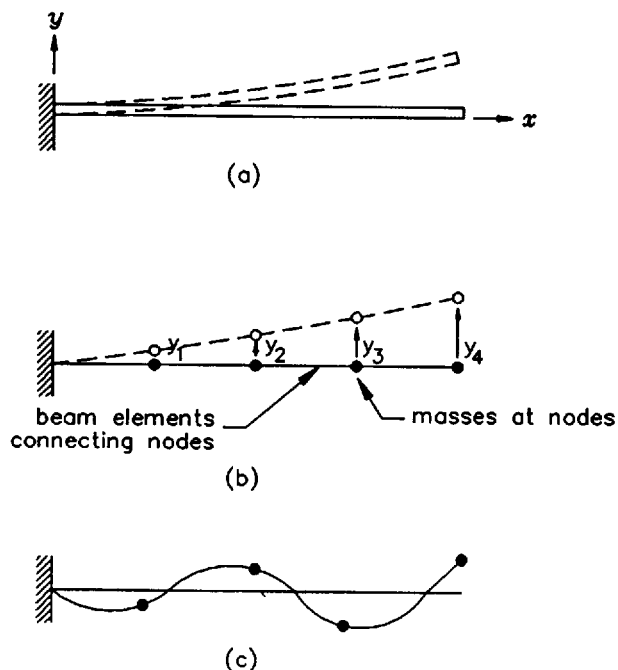


Fig. 12.7 Finite element idealization. (a) Uniform beam in free vibration, (b) finite element representation, (c) fourth mode not accurately represented

In static problems the equilibrium of every degree of freedom at the nodes of the idealization is described by the stiffness equation:

$$F = KY$$

where  $F$  is the vector of applied forces,  $Y$  is the vector of displacements for every degree of freedom, and  $K$  is the stiffness matrix. Solution of unknown displacements for a known force vector involves inversion of the stiffness matrix.

The extension of the method to dynamic problems can be visualized in simple terms by considering the dynamic equilibrium of a vibrating structure.

Figure 12.7(a) shows the instantaneous deflected shape of a vibrating uniform cantilever, and Fig. 12.7(b) shows a finite element idealization of this condition. The shape is described by the deflections of the nodes,  $Y$ , and a mass is associated with each degree of freedom of the idealization.

At the instant considered when the deflection vector is  $Y$  the forces at the nodes provided by the stiffness elements must be  $KY$ .

These forces may in part be resisting external instantaneous nodal forces  $P$  and may in part be causing the mass associated with each node to accelerate. The equations of motions of all the nodes may therefore be written as:

$$P - M\ddot{Y} = KY$$



or

$$KY + M\ddot{Y} = P$$

where  $M$  is the mass matrix,  $\ddot{Y}$  is the acceleration vector, and  $P$  is the external force vector.

The natural frequencies and mode shapes are obtained by solving the undamped free vibration equations:

$$KY + M\ddot{Y} = 0$$

Assuming a solution of the form  $y = Y \cos \omega_n t$ , it follows that  $\ddot{Y} = -\omega_n^2 Y$  and hence:

$$[K - \omega_n^2 M]Y = 0$$

This is a standard eigenvalue problem of matrix algebra for which various numerical solution techniques exist. The solution provides a set of mode shape vectors  $Y$  with corresponding natural frequencies  $\omega_n$ . The number of modes possible will be equal to the number of degrees of freedom in the solution.

### 12.5.2 Modelling techniques

Dynamic analysis is more complex than static analysis and care is required so that results of appropriate accuracy are obtained at reasonable cost when using finite element programs. It is often advisable to investigate simple idealizations initially before embarking upon detailed models. As problems and programs vary it is possible to give only broad guidance; individual program manuals must be consulted and experience with the program being used is invaluable. More detailed background is given in Reference 8.

The first stage in any dynamic analysis will invariably be to obtain the natural frequencies and mode shapes of the structure. As can be seen from Fig. 12.7(c) a given finite element model will represent higher modes with decreasing accuracy. If it is only necessary to obtain a first mode frequency accurately then a relatively coarse model, such as that illustrated in Fig. 12.7(b) will be perfectly adequate. In order to obtain an accurate estimate of the fourth mode a greater subdivision of the structure would be necessary, since the distribution of inertia load along the uniform beam in this mode is not well represented by just four masses.

As models increase in size and complexity, the solution of the eigenvalue problem for all the degrees of freedom of the structure becomes prohibitive and unnecessary. It is usual in these cases to select a limited number of 'master' degrees of freedom (which become the effective degrees of freedom in the analysis). These may be selected manually, or automatic procedures are available in most programs. In either case the number and distribution of masters must be sufficient to enable the mode shapes required to be defined. It is generally better to retain translational degrees of freedom as masters rather than rotational.

Displacements for the remaining 'slave' nodes are obtained by interpolation. An eigensolution based on  $N$  master degrees of freedom will yield  $N$  modes of vibration, though only a limited number of these will be of high accuracy. Examination of the mode shapes and the distribution of master degrees of freedom (as in Figs 12.7(b) and 12.7(c)) will indicate which of the higher modes are well represented.

Clearly dynamically consistent units must be used throughout, and these units may not be the same as those used for a static analysis using the same model. A hand check of the first mode frequency using an approximate or empirical method is strongly advisable to ensure that the results are realistic. In addition, there is even more need than with static analysis to view computer analysis results as approximate. It is very difficult to predict natural frequencies of real structures with a high degree of precision unless the real boundary conditions and structural stiffness can be defined with confidence. This is rarely the case and these are uncertainties that finite element analysis cannot resolve.

## References to Chapter 12

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## Chapter 13

# Local buckling and cross-section classification

by DAVID NETHERCOT

### 13.1 Introduction

The efficient use of material within a steel member requires those structural properties which most influence its load-carrying capacity to be maximized. This, coupled with the need to make connections between members, has led to the majority of structural sections being thin-walled as illustrated in Fig. 13.1. Moreover, apart from circular tubes, structural steel sections (such as universal beams and columns, cold-formed purlins, built-up box columns and plate girders) normally comprise a series of flat plate elements. Simple considerations of minimum material consumption frequently suggest that some plate elements be made extremely thin but limits must be imposed if certain potentially undesirable structural phenomena are to be avoided. The most important of these in everyday steelwork design is local buckling.

Figure 13.2 shows a short UC section after it has been tested as a column. Considerable distortion of the cross-section is evident with the flanges being deformed out of their original flat shape. The web, on the other hand, appears to be comparatively undeformed. The buckling has therefore been confined to certain plate elements, has not resulted in any overall deformation of the member and its centroidal axis has not deflected. In the particular example of Fig. 13.2, local buckling did not develop significantly until well after the column had sustained its 'squash load' equal to the product of its cross-sectional area times its material strength. Local buckling did not affect the load-carrying capacity because the proportions of the web and flange plates are sufficiently compact. The fact that the local buckling appeared in the flanges before the web is due to these elements being the more slender.

Terms such as *compact* and *slender* are used to describe the proportions of the individual plate elements of structural sections based on their susceptibility to local buckling. The most important governing property is the ratio of plate width to plate thickness,  $\beta$ , often referred to as the '*b/t* ratio'. Other factors that have some influence are material strength, the type of stress system to which the plate is subjected, the support conditions provided and whether the section is produced by hot-rolling or welding.

Although the rigorous treatment of plate buckling is a mathematically complex topic,<sup>1</sup> it is possible to design safely and in most cases economically with no direct consideration of the subject. For example, the properties of the majority of

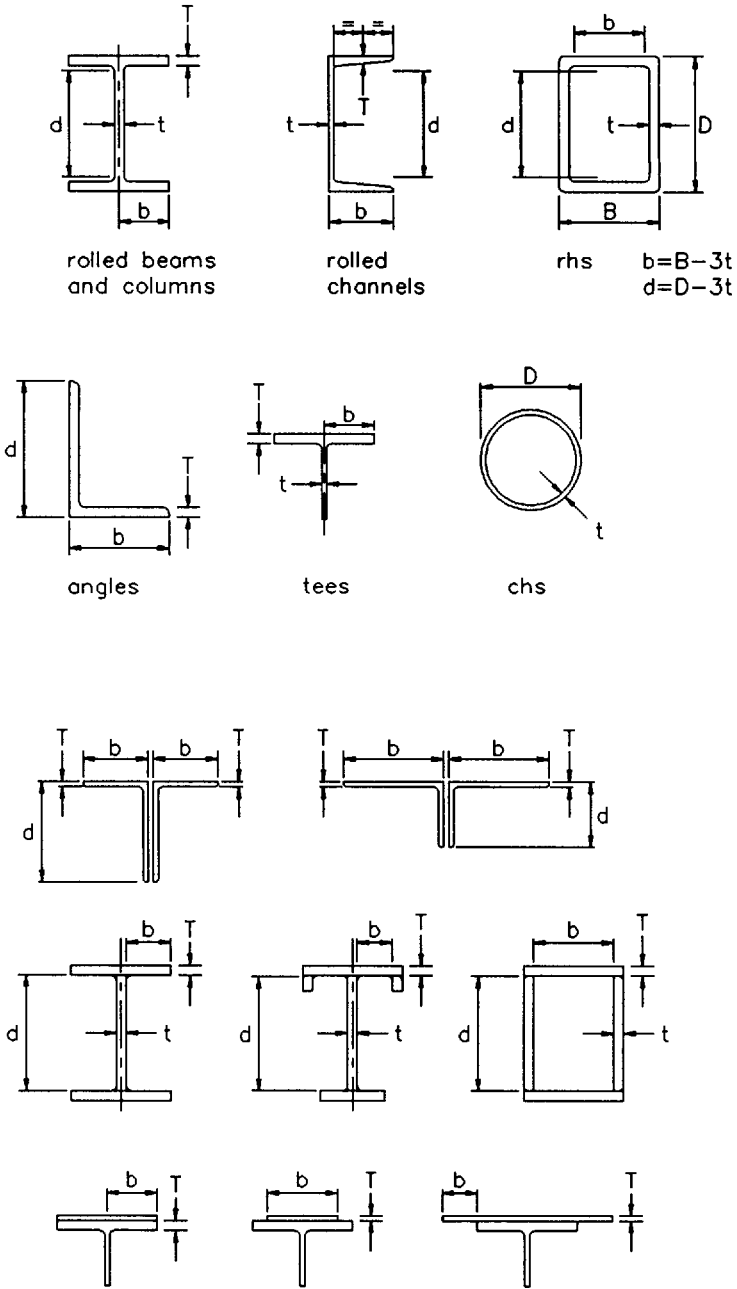


Fig. 13.1 Structural cross sections

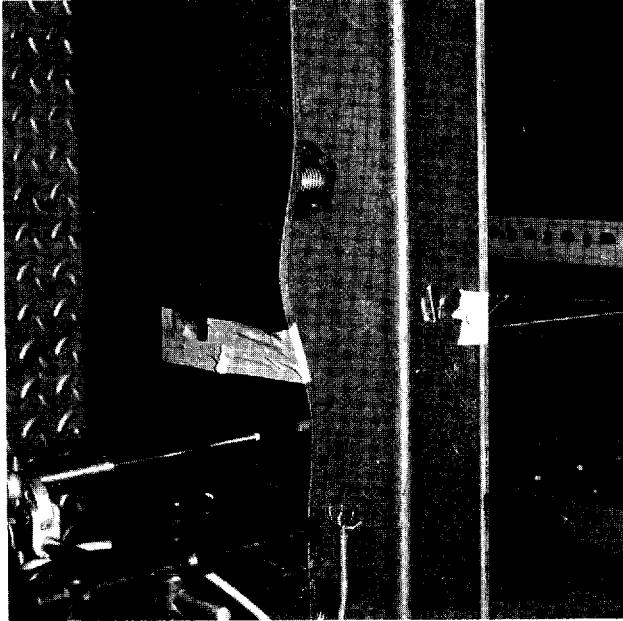


Fig. 13.2 Local buckling of column flange

standard hot-rolled sections have been selected to be such that local buckling effects are unlikely to affect significantly their load-carrying capacity when used as beams or columns. Greater care is, however, necessary when using fabricated sections for which the proportions are under the direct control of the designer. Also cold-formed sections are often proportioned such that local buckling effects must be accounted for.

### 13.2 Cross-sectional dimensions and moment–rotation behaviour

Figure 13.3 illustrates a rectangular box section used as a beam. The plate slenderness ratios for the flanges and webs are  $b/T$  and  $d/t$  and elastic stress diagrams for both components are also shown. If the beam is subject to equal and opposite end moments  $M$ , Fig. 13.4 shows in a qualitative manner different forms of relationship between  $M$  and the corresponding rotation  $\theta$ .

Assuming  $d/t$  to be such that local buckling of the webs does not occur, which of the four different forms of response given in Fig. 13.4 applies depends on the compression flange slenderness  $b/T$ . The four cases are defined as:

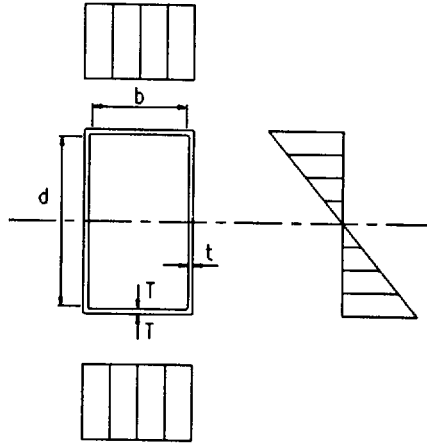


Fig. 13.3 Rectangular hollow section used as a beam

- (a)  $b/T \leq \beta_1$ , full plastic moment capacity  $M_p$  is attained and maintained for large rotations and the member is suitable for plastic design – *plastic* cross-section (Class 1).
- (b)  $\beta_1 < b/T < \beta_2$ , full plastic moment capacity  $M_p$  is attained but is only maintained for small rotations and the member is suitable for elastic design using its full capacity – *compact* cross-section (Class 2).
- (c)  $\beta_2 < b/T \leq \beta_3$ , full elastic moment capacity  $M_y$  (but not  $M_p$ ) is attained and the member is suitable for elastic design using this limited capacity – *semi-compact* cross-section (Class 3).
- (d)  $\beta_3 < b/T$ , local buckling limits moment capacity to less than  $M_y$  – *slender* cross-section (Class 4).

The relationship between moment capacity  $M_u$  and compression flange slenderness  $b/T$  indicating the various  $\beta$  limits is illustrated diagrammatically in Fig. 13.5. In the figure the value of  $M_u$  for a semi-compact section is conservatively taken as the moment corresponding to extreme fibre yield  $M_y$  for all values of  $b/T$  between  $\beta_2$  and  $\beta_3$ . This is more convenient for practical calculation than the more correct representation shown in Fig. 13.4 in which a moment between  $M_y$  and  $M_p$  is indicated. Since the classification of the section as plastic, compact, etc., is based on considerations of the compression flange alone, the assumption concerning the web slenderness  $d/t$  is that its classification is the same as or better than that of the flange. For example, if the section is semi-compact, governed by the flange proportions, then the web must be plastic, compact or semi-compact; it cannot be slender.

If the situation is reversed so that the webs are the controlling elements, then the same four categories, based on the same definitions of moment–rotation

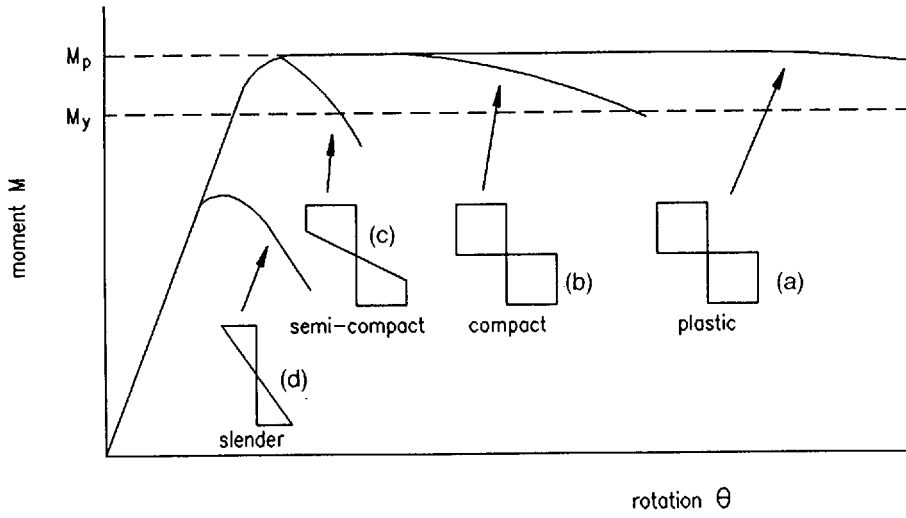


Fig. 13.4 Behaviour in bending of different classes of section

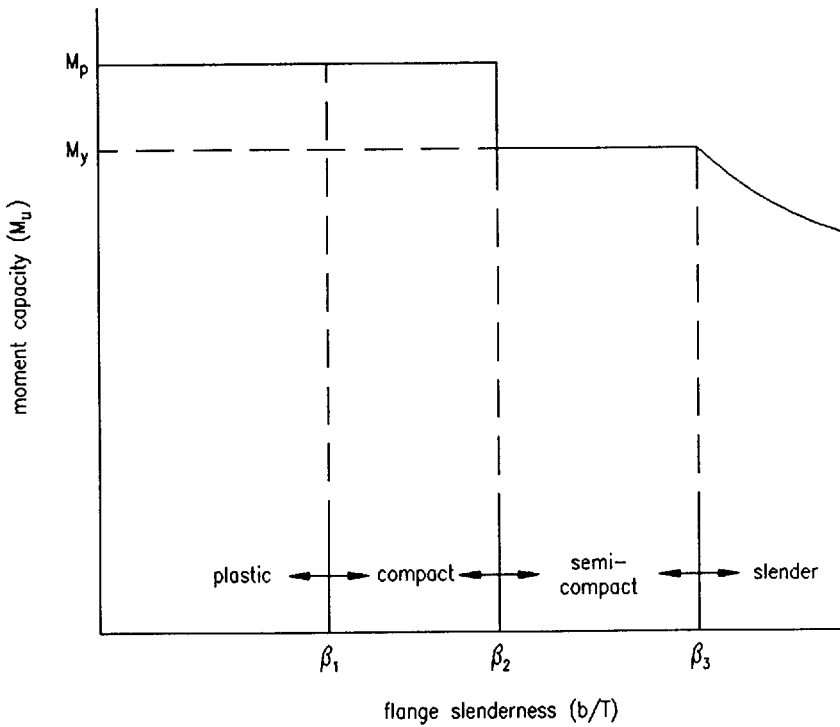
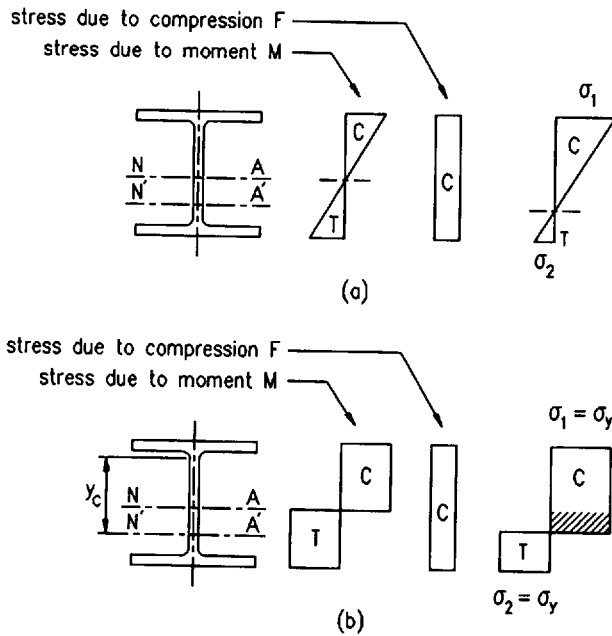


Fig. 13.5 Moment capacity as a function of flange slenderness

behaviour, are now determined by the value of web slenderness  $d/t$ . However, the governing values of  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  change since the web stress distribution differs from the pure compression in the top flange. Since the rectangular fully plastic condition, the triangular elastic condition and any intermediate condition contain less compression, the values of  $\beta$  are larger. Thus section classification also depends upon the type of stress system to which the plate element under consideration is subjected. If, in addition to the moment  $M$ , an axial compression  $F$  is applied to the member, then for elastic behaviour the pattern of stress in the web is of the form shown in Fig. 13.6(a). The values of  $\sigma_1$  and  $\sigma_2$  are dependent on the ratio  $F/M$  with  $\sigma_2$  approaching  $\sigma_y$ , if  $F$  is large and  $M$  is small. In this case it may be expected that the appropriate  $\beta$  limits will be somewhere between the values for pure compression and pure bending, approaching the former if  $\sigma_2 \approx \sigma_y$ , and the latter if  $\sigma_2 \approx -\sigma_1$ . A qualitative indication of this is given in Fig. 13.7 which shows  $M_u$  as a function of  $d/t$  for three different  $\sigma_2/\sigma_1$  ratios corresponding to pure compression,  $\sigma_2 = 0$  and pure bending. If the value of  $d/t$  is sufficiently small that the web may be classified as compact or plastic, then the stress distribution will adopt the alternative plastic arrangement of Fig. 13.6(b).

For a plate element in a member which is subject to pure compression the load-carrying capacity is not affected by the degree of deformation since the scope for



*Fig. 13.6* Stress distributions in webs of symmetrical sections subject to combined bending and compression. (a) Semi-compact, elastic stress distribution. (b) Plastic or compact, plastic stress distribution



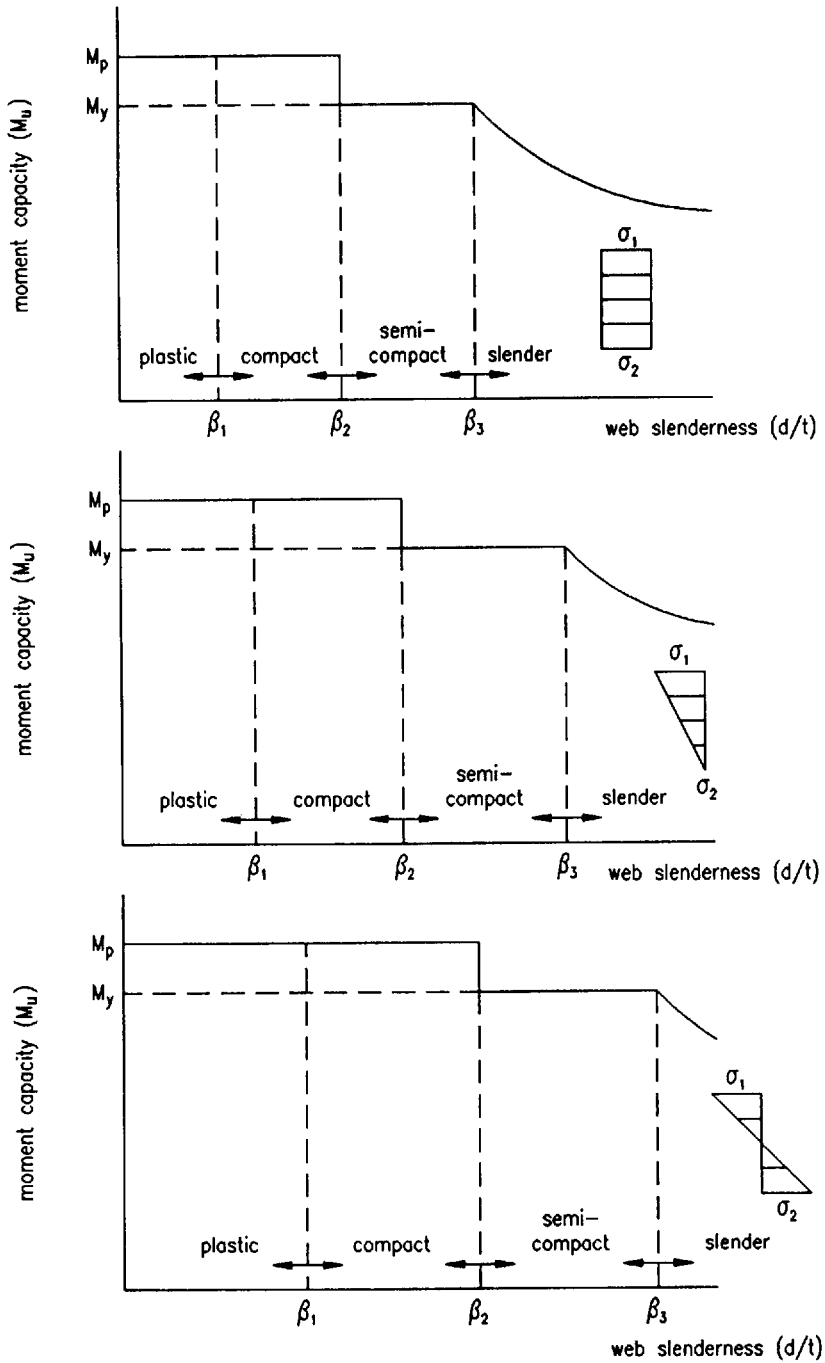


Fig. 13.7 Moment capacity as a function of  $d/t$  for different web stress patterns

a change in strain distribution as the member passes from a wholly elastic to a partially plastic state, as illustrated in Fig. 13.4 for pure bending, does not exist. The plastic and compact classifications do not therefore have any meaning; the only decision required is whether or not the member is slender and specific values are only required for  $\beta_3$ .

In the introduction to this chapter several other factors which affect local buckling are listed. These have a corresponding influence on  $\beta$  limits. As an example, the flanges of an I-section receive support along one longitudinal edge only, with the result that their buckling resistance is less than that of the flange of a box section and lower  $\beta$  values may be expected. Similarly the plate elements in members fabricated by welding generally contain a more severe pattern of residual stress, again leading to reduced  $\beta$  values.

One special case is the webs of beams and girders subject to shear. Although  $\beta$  limits for the purpose of section classification are normally provided for designers, the efficient design of plate girder webs may well require these to be exceeded. Special procedures (see Chapter 17) are, however, normally provided for such members.

### **13.3 Effect of moment–rotation behaviour on approach to design and analysis**

The types of member present in a structure must be compatible with the method employed for its design. This is particularly important in the context of section classification.

Taking the most restrictive case first, for a plastically-designed structure, in which plastic hinge action in the members is being relied upon as the means to obtain the required load-carrying capacity, only plastic sections are admissible. Members which contain any plate elements that do not meet the required  $\beta_1$  limit for the stress condition present are therefore unsuitable. This restriction could be relaxed for those members in a plastically-designed structure not required to participate in plastic hinge action; members other than those in which the plastic hinges corresponding to the collapse mechanism form. However, such an approach could be considered unsound on the basis of the effects of overstrength material, changes in the elastic pattern of moments due to settlement or lack of fit, and so on. Something less than a free choice of member types in structures designed plastically is required and BS 5950: Part 1 therefore generally restricts the method to structures in which only plastic or compact sections are present.

When elastic design – in the sense that an elastically determined set of member forces forms the basis for member selection – is being used, any of compact, semi-compact or plastic sections may be used, providing member strengths are properly determined. This point is discussed more fully in Chapters 14–18 which deal with different types of member. As a simple illustration, however, for members subject to pure bending the available moment capacity  $M_u$  must be

taken as  $M_p$  or  $M_y$ . If slender sections are being used the loss of effectiveness due to local buckling will reduce not just their strength but also their stiffness. Moreover, reductions in stiffness are dependent upon load level, becoming greater as stresses increase sufficiently to cause local buckling effects to become more significant. Strictly speaking, such changes should be included when determining member forces. However, any attempt to do this would render design calculations prohibitively difficult and it is therefore usual to make only a very approximate allowance for the effect. It is of most importance for cold-formed sections.

In practice the designer, having decided upon the design approach (essentially either elastic or plastic), should check section classification first using whatever design aids are available to him. Since most hot-rolled sections are at least compact in both grade 43 and grade 50 steel, this will normally be a relatively trivial task. When using cold-formed sections, which will often be slender, sensible use of manufacturer's literature will often eliminate much of the actual calculation. Greater care is required when using sections fabricated from plate, for which the freedom to select dimensions and thus  $b/T$  and  $d/t$  ratios means that any class is possible.

### 13.4 Classification table

Part of a typical classification table, extracted from BS 5950: Part 1, is given in Table 13.1. Values of  $\beta_1$ ,  $\beta_2$  and  $\beta_3$  for flanges, defined as plates supported along one longitudinal edge, and webs, defined as plates supported along both longitudinal edges, under pure compression, pure bending and combined compression and bending are listed. While the third case reduces to the second as the compression component reduces to zero, it does not accord with the first case when the web is wholly subject to uniform compression. The reason for this is that the neutral axis of a member subject to bending and compression in which the web is wholly in compression must lie in the flange, or at least at the web/flange junction, with the result that the tensile strains in the flange provide some degree of stabilizing influence. A slightly higher set of limits than those provided for a plate supported by other elements which are themselves in compression, such as the compression flange of a box beam, is therefore appropriate.

**Table 13.1** Extract from table of section classification limits (BS 5950: Part 1)

| Type of element                        | Class of section                        |                              |                             |
|--|---|------------------------------|-----------------------------|
|  | Plastic ( $\beta_1$ )                   | Compact ( $\beta_2$ )        | Semi-compact ( $\beta_3$ )  |
| Outstand element of compression flange | $b/T \leq 7.5\epsilon$                  | $b/T \leq 8.5\epsilon$       | $b/T \leq 13\epsilon$       |
| Internal element of compression flange | $b/T \leq 23\epsilon$                   | $b/T \leq 25\epsilon$        | $b/T \leq 28\epsilon$       |
| Web with neutral axis at mid-depth     | $d/t \leq 79\epsilon$                   | $d/t \leq 98\epsilon$        | $d/t \leq 120\epsilon$      |
| Web, generally                         | $d/t \leq 79\epsilon/(0.4 + 0.6\alpha)$ | $d/t \leq 98\epsilon/\alpha$ | $d/t = f(\alpha, \epsilon)$ |

### 13.5 Economic factors

When design is restricted to a choice of suitable standard hot-rolled sections, local buckling is not normally a major consideration. For plastically designed structures only plastic sections are suitable; thus the designer's choice is slightly restricted, although no UBs and only 6 UCs in grade 43 steel and 11 UBs and 10 UCs in grade 50 steel are outside the limits of BS 5950: Part 1 when used in pure bending. Although considerably more sections are unsatisfactory if their webs are subject to high compression, the number of sections barred from use in plastically designed portal frames is, in practice, extremely small. Similarly for elastic design no UB is other than semi-compact or better, providing it is not required to carry high compression in the web, while all UCs are at least semi-compact even when carrying their full squash load.

The designer should check the class of any trial section at an early stage. This can be done most efficiently using information of the type given in Reference 2. For webs under combined compression and bending the first check should be for pure compression as this is the more severe; providing the section is satisfactory no additional checks are required; if it does not meet the required limit a decision on whether it is likely to do so under the less severe combined load case must be made.

The economic use of cold-formed sections, including profiled sheeting of the type used as decking and cladding, often requires that members are non-compact. Quite often they contain plate elements that are slender, with the forming process being exploited to provide carefully proportioned shapes. Since cold-formed sections are proprietary products, manufacturers normally provide design literature in which member capacities which allow for the presence of slender plate elements are listed. If rigorous calculations are, however, required, then Parts 5 and 6 of BS 5950 contain the necessary procedures.

When using fabricated sections the opportunity exists for the designer to optimize on the use of material. This leads to a choice between three courses of action:

- (1) eliminate all considerations of local buckling by ensuring that the width-to-thickness ratios of every plate element are sufficiently small;
- (2) if employing higher width-to-thickness ratios, use stiffeners to reduce plate proportions sufficiently so that the desired strength is achieved;
- (3) determine member capacities allowing for reductions due to exceeding the relevant compact or semi-compact limits.

Effectively only the first of these is available if plastic design is being used. For elastic design when the third approach is being employed and the sections are slender, then calculations inevitably are more involved as even the determination of basic cross-sectional capacities requires allowances for local buckling effects through the use of concepts such as the effective width technique.<sup>1</sup>

### References to Chapter 13

1. Bulson P.S. (1970) *The Stability of Flat Plates*. Chatto and Windus, London.
2. The Steel Construction Institute (SCI) (1991) *Steelwork Design Guide to BS 5950: Part 1: 1985, Vol. 1: Section Properties, Member Capacities*, 3rd edn. SCI, Ascot, Berks.

# Chapter 14

## Tension members

by JOHN RIGHINIOTIS

### 14.1 Introduction

Theoretically, the tension member transmitting a direct tension between two points in a structure is the simplest and most efficient structural element. In many cases this efficiency is seriously impaired by the end connections required to join tension members to other members in the structure. In some situations (for example, in cross-braced panels) the load in the member reverses, usually by the action of wind, and then the member must also act as a strut. Where the load can reverse, the designer often permits the member to buckle, with the load then being taken up by another member.

### 14.2 Types of tension member

The main types of tension members, their applications and behaviour are:

- (a) open and closed single rolled sections such as angles, tees, channels and the structural hollow sections. These are the main sections used for tension members in light trusses and lattice girders for bracing.
- (b) compound sections consisting of double angles or channels. At least one axis of symmetry is present and so the eccentricity in the end connection can be minimized. When angles or other shapes are used in this fashion, they should be interconnected at intervals to prevent vibration especially when moving loads are present.
- (c) heavy rolled sections and heavy compound sections of built-up H- and box sections. The built-up sections are tied together either at intervals (batten plates) or continuously (lacing or perforated cover plates). Batten plates or lacing do not add any load-carrying capacity to the member but they do serve to provide rigidity and to distribute the load among the main elements. Perforated plates can be considered as part of the tension member.
- (d) bars and flats. In the sizes generally used, the stiffness of these members is very low; they may sag under their own weight or that of workmen. Their small cross-sectional dimensions also mean high slenderness values and, as a consequence, they may tend to flutter under wind loads or vibrate under moving loads.

- (e) ropes and cables. Further discussion on these types of tension members is included in section 14.7 and Chapter 5, section 5.3.

The main types of tension members are shown in Fig. 14.1.

Typical uses of tension members are:

- (a) tension chords and internal ties in trusses and lattice girders in buildings and bridges.
- (b) bracing members in buildings.
- (c) main cables and deck suspension cables in cable-stayed and suspension bridges.
- (d) hangers in suspended structures.

Typical uses of tension members in buildings and bridges are shown in Fig. 14.2.

### 14.3 Design for axial tension

Rolled sections behave similarly to tensile test specimens under direct tension (Fig. 14.1).

For a straight member subject to direct tension,  $F$ :

$$\text{tensile stress, } f_t = \frac{F}{A}$$

$$\text{elongation, } \delta_L = \frac{FL}{AE} \quad (\text{in the linear elastic range})$$

$$\text{load at yield, } P_y = p_y A = \text{load at failure (neglecting strain hardening)}$$

For typical stress–strain curves for structural steel and wire rope see Fig. 14.3.

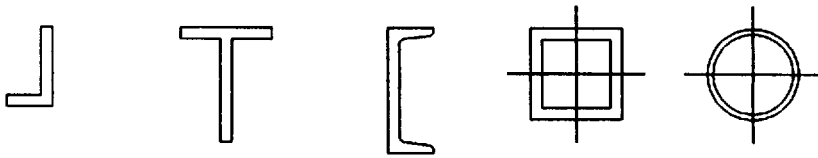
#### 14.3.1 BS 5950: Part 1

The design of axially loaded tension members is given in clause 4.6. The tension capacity is:

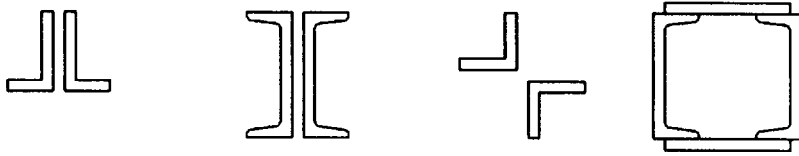
$$P_t = A_c p_y$$

where  $A_c$  is the effective area defined in clause 3.3.3. This clause states that the effective area of a member with holes may be taken as  $K_e$  times its net area but not more than its gross area. The net area is defined as the gross area less deductions for fastener holes. For members with staggered holes reference should be made to Chapter 2, section 2.5.

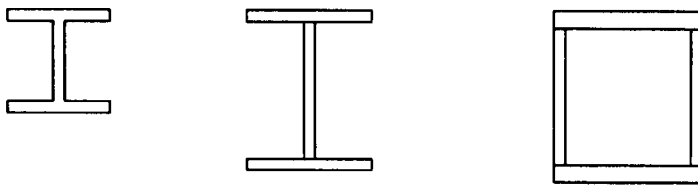
The factor  $K_e$ , values of which are given below for steels complying with BS 4360, has been introduced as a result of tests which show that the presence of



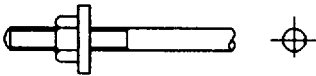
rolled sections



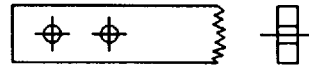
compound sections



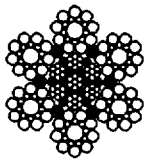
heavy rolled and built-up sections



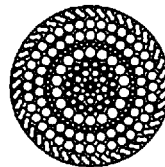
threaded bar



flat



round strand rope



locked coil rope

Fig. 14.1 Tension members



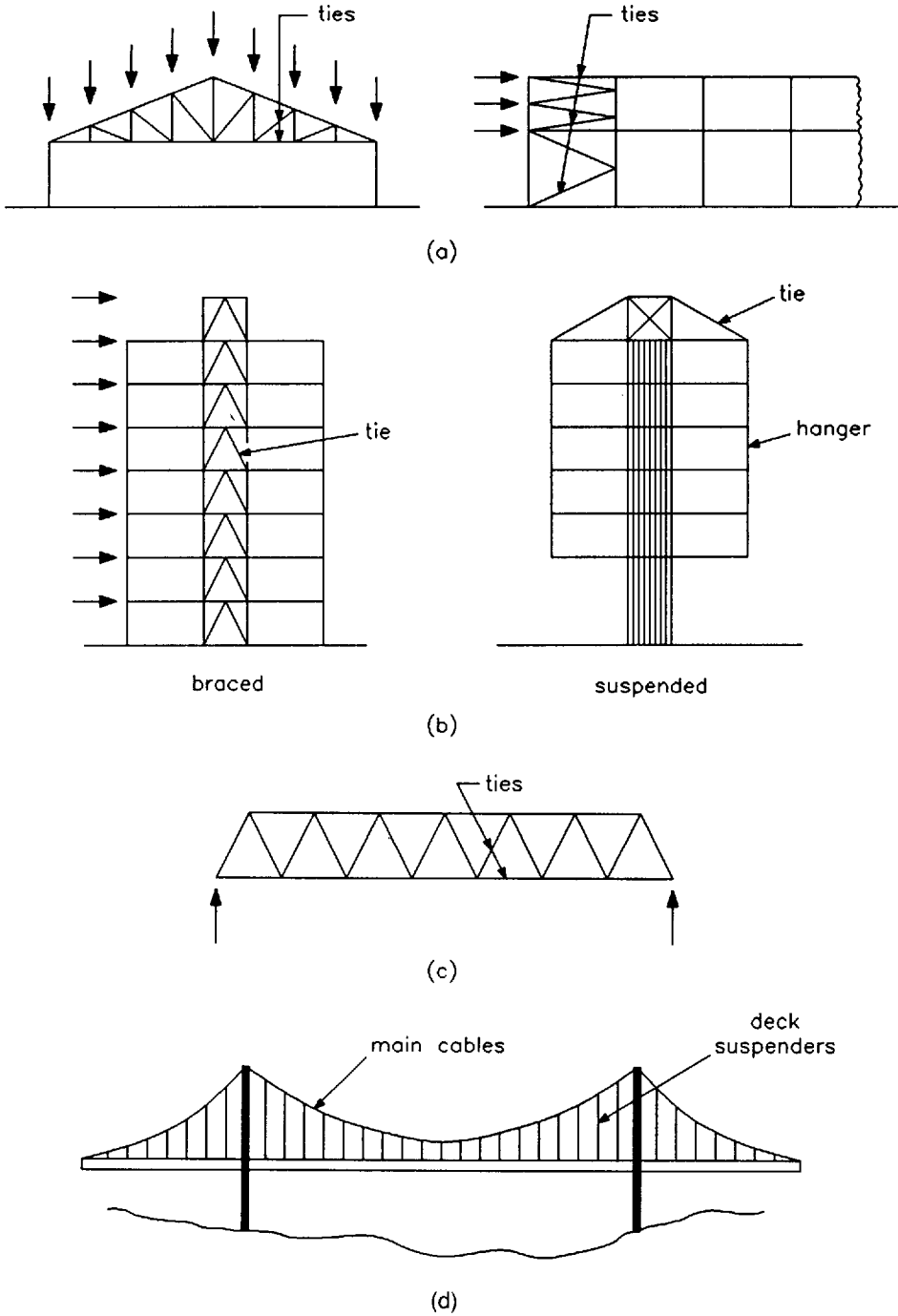


Fig. 14.2 Tension members in buildings and bridges. (a) Single-storey building – roof and truss bracing. (b) Multi-storey building. (c) Bridge truss. (d) Suspension bridge

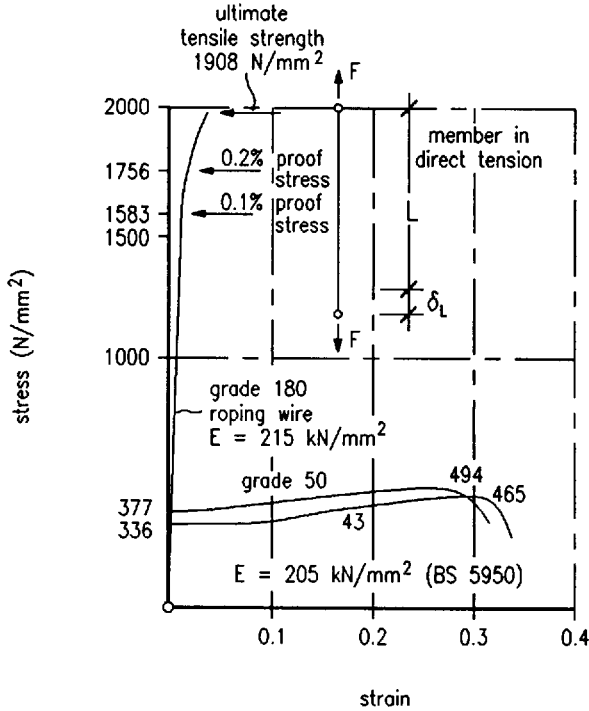


Fig. 14.3 Stress–strain curves for structural steels and wire rope

holes does not reduce the effective capacity of a member in tension provided that the ratio of the net area to the gross area is suitably greater than the ratio of the yield strength to the ultimate strength.

- $K_e = 1.2$  for grade 40 or 43
- $K_e = 1.1$  for grade 50 or WR50
- $K_e = 1.0$  for grade 55

For other steels,  $K_e = 0.75 U_s/Y_s$  but  $\leq 1.2$ , where  $U_s$  is the specified minimum ultimate tensile strength and  $Y_s$  is the specified minimum yield strength.

### 14.3.2 BS 5400: Part 3

The member should be such that the design ultimate axial load does not exceed the tensile resistance  $P_D$ , given by:

$$P_D = \frac{\sigma_y A_e}{\gamma_m \gamma_{t_3}}$$

where  $A_e$  = effective cross-sectional area  
 $= k_1 k_2 A_t$

$A_t$  = net cross-sectional area

$A$  = gross area

$\sigma_y$  = nominal yield stress for steel given in BS 4360

$\gamma_m$  = partial safety factor.<sup>a</sup> Values are given in Table 2 of BS 5400: Part 3. This takes account of material variation.

$\gamma_{t_3}$  = partial safety factor.<sup>a</sup> Values are given in clause 4.3.3. This is often called the 'gap factor'.

$k_1, k_2$  = factors. Values are given in clause 11.

<sup>a</sup> Note that the design ultimate load incorporates other safety factors ( $\gamma_{fL}$ ).

## 14.4 Combined bending and tension

Bending in tension members arises from

- (a) eccentric connections
- (b) lateral loading
- (c) rigid frame action.

If a structural member is subjected to axial tension combined with bending about axes  $xx$  and  $yy$  then:

tensile stress,  $f_t = F/A$   
 bending stress  $xx$  axis,  $f_{bx} = M_x/Z_x$   
 bending stress  $yy$  axis,  $f_{by} = M_y/Z_y$   
 maximum stress,  $f_{max} = f_t + f_{bx} + f_{by}$

The separate stress diagrams are shown in Fig. 14.4(a). The values of the separate actions causing yield are:

tensile load at yield,  $P_y = Y_s A$   
 moment at yield ( $xx$  axis),  $M_{xx} = Y_s Z_x$   
 moment at yield ( $yy$  axis),  $M_{yy} = Y_s Z_y$

The points defined by  $P_y$ ,  $M_{xx}$  and  $M_{yy}$  form an interaction surface. Any point on this surface gives the co-existent values of  $F$ ,  $M_x$  and  $M_y$  for which the maximum stress equals the yield stress.

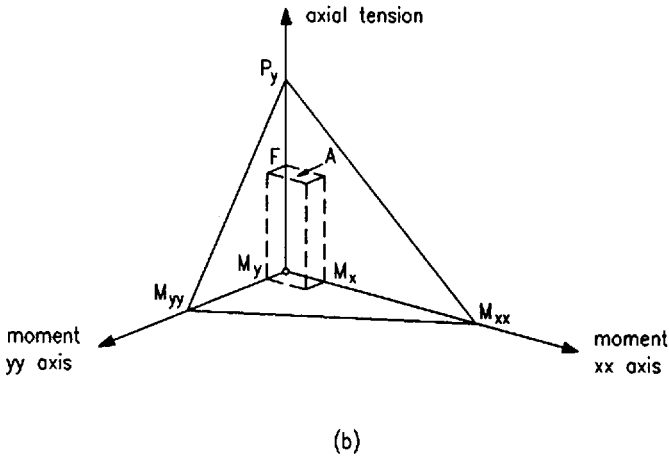
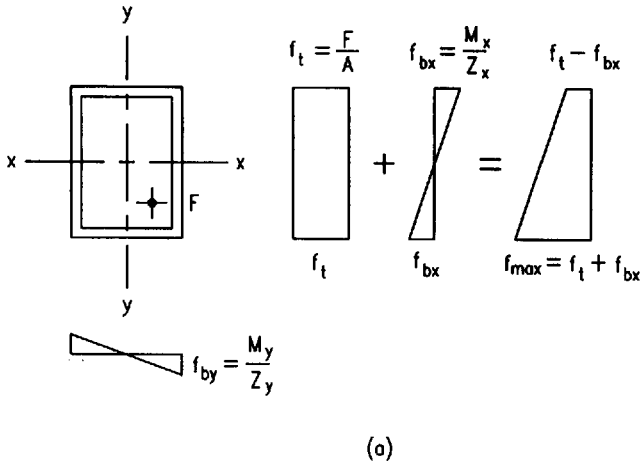


Fig. 14.4 Combined bending and tension – elastic analysis. (a) Stress diagram. (b) Elastic interaction surface

An elastic interaction surface for a rectangular hollow section is shown in Fig. 14.4(b).

The maximum values for axial tension and plastic moment for the same member are:

axial tension,  $P_y = Y_s A$

plastic moment (*xx* axis),  $M_{px} = Y_s S_x$

plastic moment (*yy* axis),  $M_{py} = Y_s S_y$

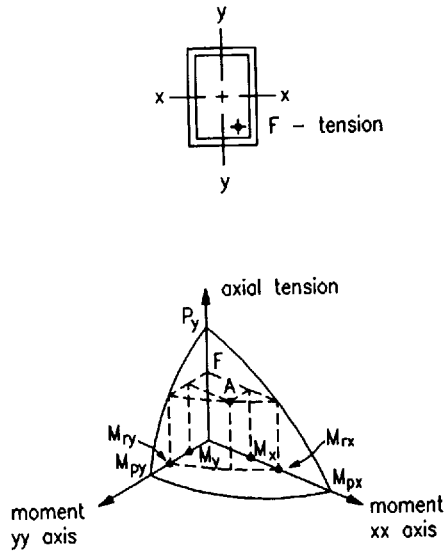


Fig. 14.5 Plastic interaction surface

The difference between the elastic and plastic interaction surfaces represents the additional design strength available if plasticity is taken into account (Fig. 14.5).

**14.4.1 BS 5950: Part 1**

The design of tension members with moments is given in clause 4.8.2. This states that tension members should be checked for capacity at the points of greatest bending moments and axial loads, usually at the ends. The following relationship should be satisfied:

$$\frac{F}{A_e p_y} + \frac{M_x}{M_{cx}} + \frac{M_y}{M_{cy}} \leq 1$$

- where  $F$  = applied axial force in the member
- $A_e$  = effective area
- $p_y$  = design strength
- $M_x$  = applied moment about the major axis at the critical region
- $M_{cx}$  = moment capacity about the major axis in the absence of axial load
- $M_y$  = applied moment about the minor axis
- $M_{cy}$  = moment capacity about the minor axis in the absence of axial load.

For plastic or compact sections with low shear load:

$$M_c = p_y S \leq 1.2 p_y Z$$

where  $S$  = plastic modulus about the relevant axis

$Z$  = elastic modulus about the relevant axis.

Alternatively for greater economy, in plastic or compact cross sections only, the following relationship should be satisfied:

$$\left(\frac{M_x}{M_{rx}}\right)^{z_1} + \left(\frac{M_y}{M_{ry}}\right)^{z_2} \leq 1$$

where  $M_{rx}$ ,  $M_{ry}$  are the reduced moment capacities about their respective axes in the presence of axial load;  $z_1$  is a constant, taken as 2.0 for solid and hollow circular sections, I- and H-sections, 5/3 for solid and hollow rectangular sections and 1.0 for all other cases; and  $z_2$  is a constant, taken as 1.0 for I- and H-sections, 2.0 for solid and hollow circular sections, 5/3 for solid and closed hollow rectangular sections and 1.0 for all other cases.

#### 14.4.2 BS 5400: Part 3

A member subjected to co-existent tension and bending should be such that at all cross sections the following relationship is satisfied:

$$\frac{P}{P_D} + \frac{M_x}{M_{Dxt}} + \frac{M_y}{M_{Dyt}} \leq 1.0$$

where  $P$  = axial tensile force  
 $P_D$  = tensile resistance, see section 14.3.2  
 $M_x, M_y$  = bending moments at the section about  $xx$  and  $yy$  axes, respectively  
 $M_{Dxt}, M_{Dyt}$  = corresponding bending resistances with respect to the extreme tensile fibres.

Additionally, if at any section within the middle third of the length of the member the maximum compressive stress due to bending exceeds the tensile stress due to axial load, the design should be such that:

$$\frac{M_{x\max}}{M_{Dxc}} + \frac{M_{y\max}}{M_{Dyc}} < 1 + \frac{P}{P_D}$$

where  $M_{x\max}, M_{y\max}$  = maximum moments anywhere within the middle third  
 $M_{Dxc}, M_{Dyc}$  = corresponding bending resistances with respect to the extreme compression fibres.

For compact sections the bending resistance is given in clause 9.9.1.2. This is:

$$M_D = \frac{Z_{pc} \sigma_{fc}}{\gamma_m \gamma_{f3}}$$

where  $\sigma_c$  = limiting compressive stress (see clause 9.8)  
 $Z_{pc}$  = plastic modulus of the effective section (see clause 9.4.2).

Clause 9.9.1.3 should be referred to for the resistance of non-compact sections.

## 14.5 Eccentricity of end connections

Simplified design rules are given in both BS 5950 and BS 5400 for the effects of combined tension and bending caused by the eccentric load introduced into the member by the end connection.

### 14.5.1 BS 5950: Part 1

Angles, channels and tees may be designed as axially loaded members following the simplified design rules given below:

- (a) Single angles connected through one leg, single channels connected only through the web and T-sections connected only through the flange have an effective area given by:

$$A_c = a_1 + \left( \frac{3a_1}{3a_1 + a_2} \right) a_2$$

where  $a_1$  is the net sectional area of the connected leg and  $a_2$  is the sectional area of the unconnected leg.

Double angles connected to one side of a gusset or section may be designed individually as given above.

- (b) For back-to-back double angles connected to one side of a gusset or section which is in contact or separated by a distance not exceeding the aggregate thickness of the parts with solid packing pieces or connected by bolts or welding such that the slenderness of the individual component does not exceed 80, then the effective area  $A_c$  may be taken as:

$$A_c = a_1 + \left( \frac{5a_1}{5a_1 + a_2} \right) a_2$$

where  $a_1$  is the net sectional area of the connected leg and  $a_2$  is the sectional area of the unconnected leg.

### 14.5.2 BS 5400: Part 3

The bending moment resulting from an eccentricity of the end connections should be taken into account. For single angles connected by one leg these provisions

may be considered to be met if the effective area of the unconnected leg is taken as:

$$\left( \frac{3A_1}{3A_1 + A_2} \right) A_2$$

where  $A_1$  = net area of the connected leg

$A_2$  = net area of the unconnected leg.

## 14.6 Other considerations

### 14.6.1 Serviceability, fatigue and corrosion

Ropes and bars are not normally used in building construction because they lack stiffness, but they have been used in some cases as hangers in suspended buildings. Very light, thin tension members are susceptible to excessive elongation under direct load as well as lateral deflection under self-weight and lateral loads. Special problems may arise where the members are subjected to vibration or conditions leading to failure by fatigue, such as can occur in bridge deck hangers. Damage through corrosion is undesirable; adequate protective measures must be adopted. All these factors can make the design of tension members a complicated process in some cases.

The light-rolled sections used for tension members in trusses and for bracing are easily damaged during transport. It is customary to specify a minimum size for such members to prevent this happening. For angle ties, a general rule is to make the leg length not less than one-sixtieth of the member length.

To avoid buckling of ties due to reversal of load under wind conditions, BS 5950: Part 1, clause 4.7.3 states that the slenderness value  $\lambda$  for any member acting as a tie but subject to reversal of stress resulting from the action of wind should not exceed 350. Slenderness  $\lambda$  is calculated by dividing the effective length  $L_E$  of a member by the radius of gyration about the relevant axis. The nominal effective length  $L_E$  can be determined from Table 24 of BS 5950: Part 1.

In a fatigue assessment of a member, the stress range considered is the greatest algebraic difference between principal stresses occurring during any one stress cycle. The above applies when the stresses occur on principal planes of more than 45° apart.

The stresses should be calculated using elastic theory and taking account of all axial, bending and shear stresses occurring under the design loadings. Alternatively the design loadings in BS 5400: Part 10 can be used.

In assessing the fatigue behaviour of a member, the following effects have to be included:

- shear lag, restrained torsion and distortion, transverse stresses and flange curvatures,



- effective width of steel plates,
- stresses in triangulated skeletal structures due to load applications away from the joints, member eccentricities to joints and rigidity of joints,
- cracking of concrete in composite elements.

The following effects however, can be ignored:

- residual stresses,
- eccentricities unnecessarily arising in a standard detail,
- plate buckling.

### 14.6.2 Stress concentration factors

In cases of geometrical discontinuity, such as a change of cross section or an aperture, the resulting stress concentrations may be determined either by special analysis or by the use of stress concentration factors. Stress concentrations are not usually important in ductile materials but can be the cause of failure due to fatigue or brittle fracture in certain considerations. A hole in a flat member can increase the stresses locally on the net section by a factor which depends on the ratio of hole diameter to net plate width.

When designing against fatigue it is convenient to consider three levels of stress concentration.

- (a) stress concentrations from structural action due to the difference between the actual structural behaviour and the static model chosen,
- (b) macroscopic stress concentrations due to large scale geometric interruptions to stress flow,
- (c) microscopic and local geometry stress concentrations due to imperfections within the weld or the heat affected zone.

For the design of welded details and connections further reference should be made to BS 5400: Part 10. However, for non-standard situations it may be necessary to determine the stress concentration factor directly from a numerical analysis study or from an experimental model.

In many cases the detail under consideration is very likely not to fit neatly into one of the classes. On site, the actual stress range for a particular loading occurrence is likely to be strongly influenced by detailed fit of the joint and overall fit of the structure. Therefore the overall form should be such that load paths are as smooth as possible and unintended load paths should be avoided, particularly where fit could significantly influence behaviour. Discontinuities must be avoided by tapering and appropriate choice of radii.

Typical stress concentration factor graphs are shown in Fig. 14.6.

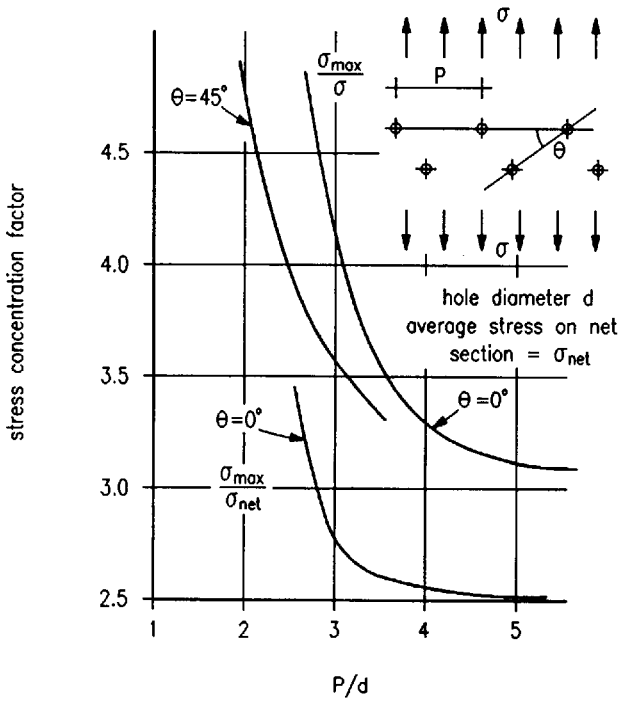
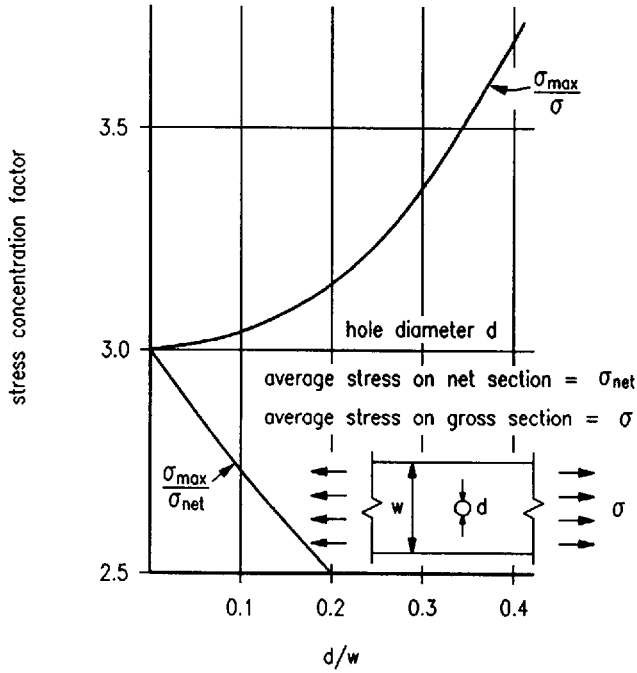


Fig. 14.6 Stress concentration factors

### 14.6.3 Fabrication and erection

The behaviour of tension members in service depends on the fabrication tolerances and the erection sequence and procedure. Provision must be made so that all tension members are immediately active in resisting applied loads in service. For bars or cables used as tension members tensioning up should be ensured through screwed ends.

Bracing members fabricated from rolled sections should be installed and properly tightened before other connections and column base plates are bolted up, to bring the structure into line and square. To enable the bracing members to be immediately effective and to avoid sagging, they are usually specified slightly shorter than the exact length.

Trial shop assembly is often specified for the member in heavy industrial trusses and bridge members to ensure that the fabrication is accurate and that erection is free from problems.

## 14.7 Cables

This section is directed mainly towards bridge cables; see Chapter 5, section 5.3 for cables in building structures.

### 14.7.1 Composition

A cable may be composed of one or more structural ropes, structural strands, locked coil strands or parallel wire strands.

A strand, with the exception of a parallel wire strand, is an assembly of wires formed vertically around a central wire in one or more symmetrical layers. A strand may be used either as an individual load-carrying member, where radius of curvature is not a major requirement, or as a component in the manufacture of structural rope.

A rope is composed of a plurality of strands vertically laid around a core. In contrast to the strand, a rope provides increased curvature capability and is used where curvature of the cable becomes an important consideration. The significant differences between strand and rope are as follows:

- at equal sizes, a rope has lower breaking strength than a strand,
- the modulus of elasticity of a rope is lower than that of a strand,
- a rope has more curvature capability than a strand,
- the wires in a rope are smaller than those in a strand of the same diameter, consequently, a rope for a given size coating is less corrosion-resistant because of the thinner coating on the smaller diameter wires.

### 14.7.2 Application

Cables used in structural applications, namely for suspension systems in bridges, fall into the following categories:

- (a) parallel-bar cables;
- (b) parallel-wire cables;
- (c) stranded cables (see Fig. 14.1);
- (d) locked-coil cables (see Fig. 14.1).

The final choice depends on the properties required by the designer, i.e. modulus of elasticity, ultimate tensile strength, durability. Other criteria include economic and structural detailing, i.e. anchorages, erection, etc.

### 14.7.3 Parallel-bar cables

Parallel-bar cables are formed of steel rods or bars, parallel to each other in metal ducts, kept in position by polyethylene spacers. The process of tensioning the bar or rods individually is simplified by the capability of the bars to slide longitudinally. Cement grout, injected after erection, makes sure that the duct plays its part in resisting the stresses due to live loads.

Transportation in reels is only possible for the smaller diameters while for the larger sizes delivery is made in straight bars of 15.0–20.0 m in length. Continuity of the bars has to be provided by the use of couplers which considerably reduces the fatigue strength of the stay.

The use of mild steel necessitates larger sections than when using high-strength wires or strands. This leads to a reduction in the stress variation and thus lessens the risk of fatigue failure.

### 14.7.4 Parallel-wire cables

Parallel wires are used for cable-stayed bridges and pre-stressed concrete. Their fatigue strength is satisfactory, mainly because of their good mechanical properties.

### 14.7.5 Corrosion protection

Wires in the cables should be protected from corrosion. The most effective protection is obtained by hot galvanizing by steeping or immersing the wires in a

bath of melted zinc, automatically controlled to avoid overheating. A wire is described as 'terminally galvanized' or 'galvanized re-drawn' depending on whether the operation has taken place after drawing or in between two wire drawings prior to the wire being brought to the required diameter. For reinforcing bars and cables, the first method is generally adopted. A quantity of zinc in the range of 250–330 g/m<sup>2</sup> is deposited, providing a protective coating 25–45 microns thick.

#### 14.7.6 Coating

The coating process, used currently for locked-coil cables, consists of coating the bare wires with an anti-corrosion product with a good bond and long service life. The various substances used generally have a high dropping point so as not to run back towards the lower anchorages. They are usually high viscosity resins or oil-based grease, paraffins or chemical compounds.

#### 14.7.7 Protection of anchorages

The details of the connections between the ducts and the anchorages must prevent any inflow or accumulation of water. The actual details depend on the type of anchorages used, on the protective systems for the cables and on their slope. There are different arrangements intended to ensure water tightness of vital zones.

#### 14.7.8 Protection against accidents


Cables should be protected against various risks of accident, such as vehicle impact, fire, explosion and vandalism. Measures to be taken may be based on the following:

- (a) protection of the lower part of the stay, over a height of about 2.0 m, by a steel tube fixed into the deck and fixed into the duct; the tube dimensions (thickness and diameter) must be adequate.
- (b) strength of the lower anchorage against vehicle impact.
- (c) replacement of protective elements possible without affecting the cables themselves and, as far as possible, without interrupting traffic.

**Further reading for Chapter 14**

- Adams P.F., Krentz H.A. & Kulak G.L. (1973) *Canadian Structural Steel Design*. Canadian Institute of Steel Construction, Ontario.
- Bresler B., Lin T.Y. & Scalzi J.B. (1968) *Design of Steel Structures*. Wiley, Chichester.
- Dowling P.J., Knowles P. & Owens G.W. (1988) *Structural Steel Design*. Butterworths, London.
- Horne M.R. (1971) *Plastic Theory of Structures*, 1st edn. Nelson, Walton-on-Thames.
- Owens G.W. & Cheal B.D. (1989) *Structural Steelwork Connections*. Butterworths, London.
- Timoshenko S.P. & Goodier J.N. (1970) *Theory of Elasticity*. McGraw-Hill, Maidenhead, Berks.
- Trahair N.S. (1977) *The Behaviour and Design of Steel Structures*. Chapman and Hall, London.
- Troitsky M.S. (1988) *Cable-Stayed Bridges*, 2nd edn. BSP Professional Books, Oxford.

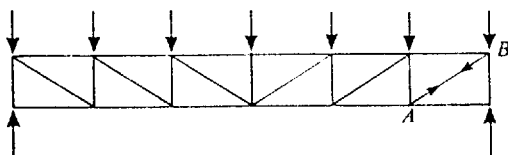
A series of worked examples follows which are relevant to Chapter 14.

|  |   |                                   |  |
|--|---|-----------------------------------|--|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>TENSION MEMBERS</b> | Chapter ref.<br><b>14</b>                  |
|  |   | Design code<br><b>BS5950</b>      | Made by <b>JR</b><br>Checked by <b>GWO</b> |

**Problem**

**BS 5950:  
Part 1**

Design a single angle tie for the member AB shown.



**Tensile force in member AB**

**Dead load** = 144 kN

**Imposed load** = 240 kN

**Total** = 384 kN

**Material:** Use Grade 50 steel


- Connections:** a) Welded  
b) Bolted

**Factored load**

$F = (1.4 \times 144) + (1.6 \times 240) = 585.6 \text{ kN}$  Table 2

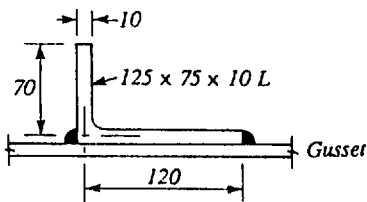
**Material Grade 50 steel, thickness  $\leq 16 \text{ mm}$**  Table 6

**Design strength  $p_y$**  = 355 N/mm<sup>2</sup>

|  |                                   |  |
|--|-----------------------------------|--|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>TENSION MEMBERS</b> | Chapter ref.<br><b>14</b>                  |
|  | Design code<br><b>BS5950</b>      | Made by <b>JR</b><br>Checked by <b>GWO</b> |

a) Welded connections

Try  $125 \times 75 \times 10$  connected by long leg.



Effective Area,  $A_e$

4.6.3.1

$$a_1 = 120 \times 10 = 1200 \text{ mm}^2$$

$$a_2 = 70 \times 10 = 700 \text{ mm}^2$$

$$A_e = a_1 + \left[ \frac{3a_1}{3a_1 + a_2} \right] a_2$$

$$\therefore A_e = 1200 + \left[ \frac{3 \times 1200}{3 \times 1200 + 700} \right] \times 700$$


$$= 1786 \text{ mm}^2$$

Tension capacity  $P_t = A_e p_y$

$$P_t = \frac{1786 \times 355}{10^3} = 634 \text{ kN} > 585.6 \text{ kN OK} \quad 4.6.1$$

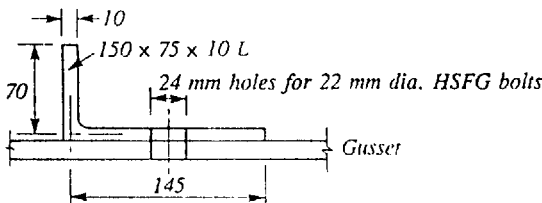
$\therefore$  Use  $125 \times 75 \times 10$  Grade 50



|  |                                   |  |
|--|-----------------------------------|--|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>  | Subject<br><b>TENSION MEMBERS</b> | Chapter ref.<br><b>14</b>                  |
|  | Design code<br><b>BS5950</b>      | Made by <b>JR</b><br>Checked by <b>GWO</b> |

**b) Bolted connections**

Try **150 × 75 × 10** connected by long leg



**Effective Area,  $A_e$**

$$a_1 = 145 \times 10 = 1450 \text{ mm}^2 \quad 4.6.3.1$$

$$a_2 = 70 \times 10 = 700 \text{ mm}^2$$

$$a_{1 \text{ net}} = 1450 - (24 \times 10)$$

$$= 1210 \text{ mm}^2$$

$$A_e = a_1 + \left[ \frac{3a_1}{3a_1 + a_2} \right] \times a_2$$

$$A_e = 1210 + \left[ \frac{3 \times 1210}{3 \times 1210 + 700} \right] \times 700$$


$$= 1797 \text{ mm}^2$$

*Note: Effective area factor  $K_e$  for sections with holes (3.3.3) does not apply in this case.*

**Tension capacity**  $P_t = A_e P_y \quad 4.6.1$

$$P_t = \frac{1797 \times 355}{10^3} = 638 \text{ kN} > 585.6 \text{ kN}$$

$\therefore$  Use **150 × 75 × 10** Grade 50

|  |                                   |  |
|--|-----------------------------------|--|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>TENSION MEMBERS</b> | Chapter ref.<br><b>14</b>                  |
|  | Design code<br><b>BS5950</b>      | Made by <b>JR</b><br>Checked by <b>GWO</b> |

**Efficiency of single angle tie**

**Calculation of the efficiency of a  $150 \times 75 \times 10$  used as a single angle tension member. Gross area =  $21.6 \text{ cm}^2$**

**a) Bolted through the long leg with bolts in 24 mm dia. holes**

**From the above calculations, Net area =  $1797 \text{ mm}^2$**

$$\text{Efficiency} = \left[ \frac{1797}{21.6 \times 10^2} \right] \times 100 = \underline{83\%}$$

**b) Welded through long leg**

$$a_1 = 145 \times 10 = 1450 \text{ mm}^2$$


$$a_2 = 70 \times 10 = 700 \text{ mm}^2$$

**Effective area:**

$$\Lambda_e = 1450 + \left[ \frac{3 \times 1450}{3 \times 1450 + 700} \right] \times 700$$

$$= 2053 \text{ mm}^2$$

$$\text{Efficiency} = \left[ \frac{2053}{21.6 \times 10^2} \right] \times 100 = \underline{95\%}$$

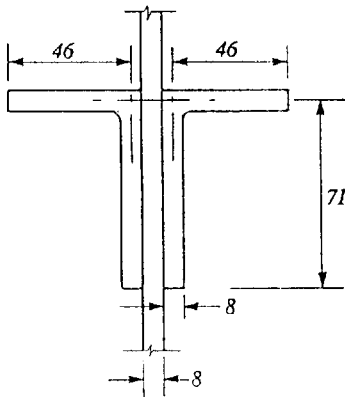
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|--|-----------------------------------|--|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>  | Subject<br><b>TENSION MEMBERS</b> | Chapter ref.<br><b>14</b>                  |
|  | Design code<br><b>BS5950</b>      | Made by <b>JR</b><br>Checked by <b>GWO</b> |

**Problem**

Design a double angle tie for the member AB in the figure on Sheet 1. Assume the use of double angles, connected back to back through a 8 mm gusset. Assume welded connections.

BS 5950:  
Part 1

Try  $2 \times 75 \times 50 \times 8$ , connected through long leg.



Effective Area,  $A_e$

4.6.3.2

$$a_1 = 71 \times 8 = 568 \text{ mm}^2$$

$$a_2 = 46 \times 8 = 368 \text{ mm}^2$$

$$A_e = 2 \times \left[ a_1 + \left( \frac{5 \times a_1}{5 \times a_1 + a_2} \right) \times a_2 \right]$$

$$\therefore A_e = 2 \times \left[ 568 + \left( \frac{5 \times 568}{5 \times 568 + 368} \right) \times 368 \right]$$

$$= 1788 \text{ mm}^2$$

**Tension capacity**

$$P_t = A_e \times p_y \quad 4.6.1$$

$$P_t = \frac{1788 \times 355}{10^3} = 635 \text{ kN} > 585.6 \text{ kN OK}$$

$\therefore$  Use  $2 \times 75 \times 50 \times 8$  Grade 50 4.6.3.2.(b)

Note: The two angles must be connected at intervals so that their individual slenderness does not exceed 80.

# Chapter 15

## Columns and struts

by DAVID NETHERCOT

### 15.1 Introduction

Members subject to compression, referred to as either 'columns' or 'struts', form one of the basic types of load-carrying component. They may be found, for example, as vertical columns in building frames, in the compression chords of a bridge truss or in any position in a space frame.

In many practical situations struts are not subject solely to compression but, depending upon the exact nature of the load path through the structure, are also required to resist some degree of bending. For example, a corner column in a building is normally bent about both axes by the action of the beam loads, a strut in a space frame is not necessarily loaded concentrically, the compression chord of a roof truss may also be required to carry some lateral loads. Thus many compression members are actually designed for combined loading as beam-columns. Notwithstanding this, the ability to determine the compressive resistance of members is of fundamental importance in design, both for the struts loaded only in compression and as one component in the interaction type of approach normally used for beam-column design.

The most significant factor that must be considered in the design of struts is buckling. Depending on the type of member and the particular application under consideration, this may take several forms. One of these, local buckling of individual plate elements in compression, has already been considered in Chapter 13. Much of this chapter is devoted to the consideration of the way in which buckling is handled in strut design.

### 15.2 Common types of member

Various types of steel section may be used as struts to resist compressive loads; Fig. 15.1 illustrates a number of them. Practical considerations such as the methods to be employed for making connections often influence the choice, especially for light members. Although closed sections such as tubes are theoretically the most efficient, it is normally much easier to make simple site connections, using the minimum of skilled labour or special equipment, to open sections. Typical arrangements include:

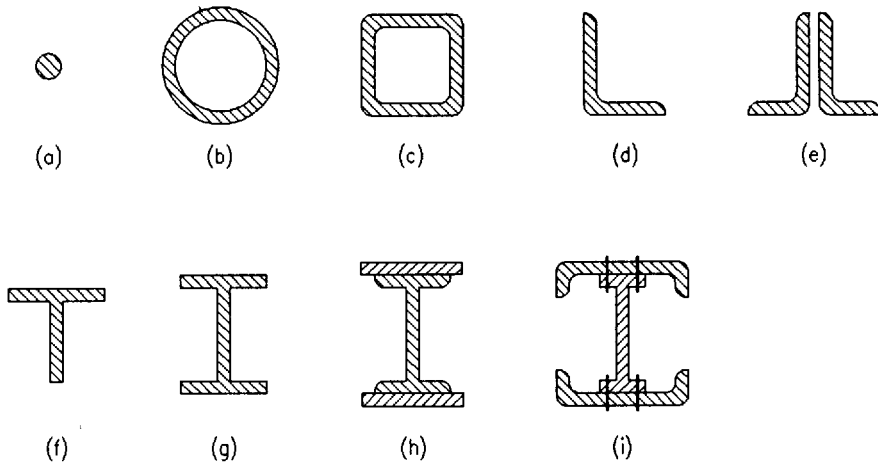


Fig. 15.1 Typical column cross sections

- (1) light trusses and bracing – angles (including compound angles back to back) and tees
- (2) larger trusses – circular hollow sections, rectangular hollow sections, compound sections and universal columns
- (3) frames – universal columns, fabricated sections e.g. reinforced UCs
- (4) bridges – box columns
- (5) power stations – stiffened box columns.

### 15.3 Design considerations

The most important property of a strut as far as the determination of its load-carrying capacity is concerned is its slenderness,  $\lambda$ , defined as the ratio of its effective length,  $L_E$ , divided by the appropriate radius of gyration,  $r$ . Codes of Practice such as BS 5950 place upper limits on  $\lambda$ , as indicated in Table 15.1, so as to avoid the use of flimsy construction, i.e. to ensure that a member which will

Table 15.1 Maximum slenderness values for struts

| Condition  | BS 5950: Part 1 limits | BS 5950: Part 5 |
|--|------------------------|-----------------|
| Members in general   | 180 <sup>a</sup>       | 180             |
| Members resisting self-weight wind loads only                        | 250 <sup>a</sup>       | 250             |
| Members normally in tension but subject to load reversal due to wind | —                      | 350             |

<sup>a</sup> Check for self-weight deflection if  $\lambda > 180$ ; allow for bending effects in design if this deflection  $> L/1000$

**Table 15.2** Upper limits on plate slenderness of BS 5400: Part 3

| $b/t$ or $D/t$<br>limit <sup>a</sup> | Unstiffened<br>outstand | Stiffened<br>outstand | CHS |
|--------------------------------------|-------------------------|-----------------------|-----|
| $p_y = 355 \text{ N/mm}^2$           | 12                      | 14                    | 100 |
| $p_y = 275 \text{ N/mm}^2$           | 14                      | 16                    | 114 |

<sup>a</sup> See Fig. 13.1 for definitions of  $b$ ;  $D$  = outside diameter

ordinarily be subject only to axial load does have some limited resistance to an accidental lateral load, does not rattle, etc. In the case of BS 5400: Part 3, no actual limits are specified; the user is merely provided with a general advisory note to the effect that construction should be suitably robust. By contrast, BS 5950 places upper bounds on local plate slenderness to avoid consideration of local buckling (see Table 15.2).

Strut design will normally require that, once a trial member has been selected and its loading and support conditions determined, attention be given to whichever of the following checks are relevant for the particular application:

- (1) Overall flexural buckling – largely controlled by the slenderness ratio,  $\lambda$ , which is a function of member length, cross-sectional shape and the support conditions provided; also influenced by the type of member
- (2) Local buckling – controlled by the width-to-thickness ratios of the component plate elements (see Chapter 13); with some care in the original choice of member this need not involve any actual calculation
- (3) Buckling of component parts – only relevant for built-up sections such as laced and battened columns; the strength of individual parts must be checked, often by simply limiting distances between points of interconnection
- (4) Torsional or torsional-flexural buckling – for cold-formed sections and in extreme cases of unusually shaped heavier open sections, the inherent low torsional stiffness of the member may make this form of buckling more critical than simple flexural buckling.

In principle, local buckling and overall buckling (flexural or torsional) should always be checked. In practice, providing cross sections that at least meet the semi-compact limits for pure compression are used, then no local buckling check is necessary since the cross section will be fully effective.

## 15.4 Cross-sectional considerations

Since the maximum attainable load-carrying capacity for any structural member is controlled by its local cross-sectional capacity (factors such as buckling may

prevent this being achieved in practice), the first step in strut design must involve consideration of local buckling as it influences axial capacity. Only two classes of section are relevant for purely axially compressed members: either the section is not slender, in which case its full capacity,  $p_y A$ , is available, or it is slender and some allowance in terms of a reduced capacity is required. The distinctions between plastic, compact and semi-compact as described in chapter 13 therefore have no relevance when the type of member under consideration is a strut.

The general approach for a member containing slender plate elements designed in accordance with BS 5950: Part 1 requires the use in all calculations relating to that member, apart from those concerned with components of connections to the member, of a reduced design strength, with the magnitude of the reduction being dependent on the extent to which the semi-compact limits (the boundary between not slender and slender) are exceeded. Effectively this means that the member is assumed to be made of a steel having a lower material strength than is actually the case.

When the cross section is classified as slender because of the proportions of one or more outstand elements, only this reduced strength method is permitted. However, if web proportions control and any outstands present are at least semi-compact, for example, an RHS or a UB with compact flanges, then the following alternatives are available. As noted above, BS 5400: Part 3 does not permit the use of columns with slender outstands.

#### 15.4.1 Columns with slender webs

Reference 1 indicates that most UB and a few RHS, even in grade 43 steel, will be slender according to BS 5950: Part 1 if used as struts. A suitable allowance for the weakening effect of local buckling should therefore be made. Three different procedures are given, outlined in the following example.

Consider a  $406 \times 140 \times 39$  UB (the UB with the highest  $d/t$ ) in grade 43 material. This has a  $d/t$  of 57.1 compared with the limit in Table 7 of 39.

(1) Use clause 3.6.3, limiting  $d/t = 39 (275/p_{yr})^{\frac{1}{2}}$

$$\text{and reduced design strength, } p_{yr} = (39/57.1)^2 \times 275 \\ = 128.3 \text{ N/mm}^2$$

For  $L_E/r_y = 100$ , using Appendix C for  $p_{yr} = 128.3 \text{ N/mm}^2$  and  $a = 3.5$

$$p_c = 89.7 \text{ N/mm}^2 \\ P_c = 49.4 \times 87.7/10 \\ = 433 \text{ kN}$$

(2) Use clause 3.6.4 for Table 8 strength reduction factor  
 $= 31/(d/t\varepsilon - 8)$

$$\text{and } p_{yr} = 275 \times 31 / (57.1 - 8) \\ = 173.6 \text{ N/mm}^2$$

For  $L_E/r_y = 100$ , using Appendix C,  $p_c = 108.9 \text{ N/mm}^2$

$$P_c = 49.4 \times 108.9 / 10 \\ = 538 \text{ kN}$$

These results may be compared with a  $P_c$  value assuming a fully effective section of 697 kN.

(3) *Alternative using footnote to Table 8.*

This permits the effective area method of Part 5 to be employed; a similar approach is adopted in Eurocode 3. It is suitable for the slender webs of UB sections but not for slender flange outstands or for slender webs of unsymmetrical sections such as channels or unequal flange Is.

The method uses a parameter  $Q$  defined as (effective area)/(gross area); for each element of the cross section this corresponds to the strength reduction factor of Table 8. The value of  $P_c$  is then obtained using the effective area and a  $p_c$  value calculated from a slenderness reduced by  $Q^2$ . The following illustration follows the Eurocode 3 presentation rather than that of Part 5.

$$A_w = dt \\ = 359.7 \times 6.3 \\ = 2266 \text{ mm}^2$$

$$\text{Using Table 8, effective web area} = 2266 \times 31 / (57.1 - 8) \\ = 1431 \text{ mm}^2$$

$$\text{Total effective area} = 4940 - (2266 - 1431) \\ = 4105 \text{ mm}^2$$

$$Q\text{-factor} = 4105 / 4940 \\ = 0.831$$

$$\text{For } L_E/r_y = 100, \text{ effective slenderness} = 100 (0.831)^{1/2} \\ = 91.2$$

$$\text{and } p_c = 158 \text{ N/mm}^2 \\ P_c = 4105 \times 158 / 10^3 \\ = 649 \text{ kN}$$

The third method leads to a significantly higher result, being only some 7% below the fully effective figure. The main reason for this is that both the first and second methods apply the same reduction in strength, based on the proportions of the most slender plate element, to the whole of the cross section, whereas the third method makes a reduction only for the plate elements which are slender.

Both BS 5400: Part 3 and BS 5950: Part 5 employ a method for slender sections in compression that uses the concept of effective area. Its implementation for cold-formed sections has been illustrated by the third method of the above



example. The bridge code prohibits the use of slender outstands by specifying the absolute upper limits on  $b/t$  given in Table 15.2 with no procedure to cover arrangements outside these, and determining the effective area of the cross section by summing the full areas of any outstands and compact webs and the effective areas,  $K_c A_c$ , of the slender webs. Values of  $K_c$  are obtained as a function of  $b/t$  from a graph.

It is worth emphasizing that for design using hot-rolled sections the majority of situations may be treated simply by ensuring that the proportions of the cross section lie within the semi-compact limits. Reference 1, in addition to listing flange  $b/T$  and web  $d/t$  values for all standard sections, also identifies those sections that are slender according to BS 5950: Part 1 when used in either grade 43 or grade 50 steel. Table 15.3 lists these.

**Table 15.3** Sections classified as 'slender' when used as struts

| Section             | Grade 43          | Grade 50          |
|---------------------|-------------------|-------------------|
| Universal<br>Beam   | All <i>except</i> | All <i>except</i> |
|                     | 914 × 419UB388    | 610 × 305UB238    |
|                     | 610 × 305UB238    | 356 × 171UB 67    |
|                     | 610 × 305UB179    |                   |
|                     |                   | 305 × 127UB 48    |
|                     | 533 × 210UB122    | 305 × 127UB 42    |
|                     | 457 × 191UB 98    | 254 × 146UB 43    |
|                     | 457 × 191UB 89    | 254 × 146UB 37    |
|                     | 457 × 152UB 82    | 203 × 133UB 30    |
|                     |                   | 203 × 133UB 25    |
|                     | 406 × 178UB 74    |                   |
|                     |                   | 203 × 102UB 23    |
|                     | 356 × 171UB 67    |                   |
|                     |                   | 178 × 102UB 19    |
|                     | 305 × 165UB 54    |                   |
|                     |                   | 152 × 89UB 16     |
|                     | 305 × 127UB 48    |                   |
|                     | 305 × 127UB 42    | 127 × 76UB 13     |
|                     | 305 × 127UB 37    |                   |
|                     | 254 × 146UB 43    |                   |
|                     | 254 × 146UB 37    |                   |
|                     | 254 × 146UB 31    |                   |
|                     | 254 × 102UB 28    |                   |
|                     | 254 × 102UB 25    |                   |
|                     | 254 × 102UB 22    |                   |
|                     | 203 × 133UB 30    |                   |
| 203 × 133UB 25      |                   |                   |
| 203 × 102UB 23      |                   |                   |
| 178 × 102UB 19      |                   |                   |
| 152 × 89UB 16       |                   |                   |
| 127 × 76UB 13       |                   |                   |
| Universal<br>Column | none              | none              |

Table 15.3 Continued

| Section                          | Grade 43         | Grade 50         |
|----------------------------------|------------------|------------------|
| Circular<br>Hollow<br>Section    | none             | none             |
| Rectangular<br>Hollow<br>Section | 300 × 200 × 6.3  | 250 × 250 × 6.3  |
|                                  | 450 × 250 × 10.0 | 400 × 400 × 10.0 |
|                                  |                  | 200 × 100 × 5.0  |
|                                  |                  | 250 × 150 × 6.3  |
|                                  |                  | 300 × 200 × 6.3  |
|                                  |                  | 300 × 200 × 8.0  |
|                                  |                  | 400 × 200 × 10.0 |
|                                  | 450 × 250 × 10.0 |                  |
| Rolled<br>Steel<br>Angle         | 200 × 150 × 15   | 200 × 150 × 15   |
|                                  | 200 × 150 × 12   | 200 × 150 × 12   |
|                                  | 200 × 100 × 12   | 200 × 100 × 15   |
|                                  | 200 × 100 × 10   | 200 × 100 × 12   |
|                                  |                  | 200 × 100 × 10   |
|                                  | 150 × 90 × 10    | 150 × 90 × 10    |
|                                  | 125 × 75 × 8     | 100 × 75 × 10    |
|                                  | 100 × 65 × 7     | 125 × 75 × 8     |
|                                  | 80 × 60 × 6      | 100 × 75 × 8     |
|                                  | 200 × 200 × 16   | 100 × 65 × 8     |
|                                  | 150 × 150 × 12   | 100 × 65 × 7     |
|                                  | 150 × 150 × 10   |                  |
|                                  |                  | 80 × 60 × 6      |
|                                  | 120 × 120 × 10   | 75 × 50 × 6      |
|                                  | 120 × 120 × 8    |                  |
|                                  |                  | 65 × 50 × 5      |
|                                  | 100 × 100 × 8    |                  |
|                                  |                  | 200 × 200 × 18   |
|                                  | 90 × 90 × 7      | 200 × 200 × 16   |
|                                  | 90 × 90 × 6      |                  |
|                                  | 150 × 150 × 12   |                  |
| 80 × 80 × 6                      | 150 × 150 × 10   |                  |
| 70 × 70 × 6                      | 120 × 120 × 10   |                  |
|                                  | 120 × 120 × 8    |                  |
| 60 × 60 × 5                      |                  |                  |
|                                  | 100 × 100 × 8    |                  |
|                                  | 90 × 90 × 8      |                  |
|                                  | 90 × 90 × 7      |                  |
|                                  | 90 × 90 × 6      |                  |
|                                  | 80 × 80 × 6      |                  |
|                                  | 70 × 70 × 6      |                  |
|                                  | 60 × 60 × 5      |                  |

## 15.5 Compressive resistance

The axial load-carrying capacity for a single compression member is a function of its slenderness, its material strength, cross-sectional shape and method of manu-

facture. Using BS 5950: Part 1, the compression resistance,  $P_c$ , is given by clause 4.7.4 as:

$$P_c = A_g p_c$$

in which  $A_g$  is the gross area and  $p_c$  is the compressive strength.

Values of  $p_c$  in terms of slenderness  $\lambda$  and material design strength  $p_y$  are given in Tables 27a–d. Slenderness is defined as the ratio of the effective length,  $L_E$  (taken as the geometrical length  $L$  for the present but see section 15.7), to the least radius of gyration,  $r$ .

The basis for Table 27 is the set of four column curves shown in Fig. 15.2. These have resulted from a comprehensive series of full-scale tests, supported by detailed numerical studies, on a representative range of cross sections.<sup>2</sup> They are often referred to as the 'European Column Curves'. Four curves are used in recognition of the fact that for the same slenderness certain types of cross section consistently perform better than others as struts. This is largely due to the arrangement of the material but is also influenced by the residual stresses that form as a result of differential cooling after hot rolling. It is catered for in design by using the strut curve selection table given as Table 25 in BS 5950: Part 1.

The first step in column design is therefore to consult Table 25 to see which of Tables 27a–d is appropriate. For example, if the case being checked is a UC liable to buckle about its minor axis, Table 27c should be used. Selection of a trial section fixes  $r$  and  $A_g$ ; the geometrical length will be defined by the application required, so  $\lambda$  and thus  $p_c$  and  $P_c$  may be obtained.

The above process should be used for all types of rolled section, including those reinforced by the addition of welded cover plates for which Table 26 should be used to supplement Table 25 when deciding on which of Tables 27a–d to use for determining  $p_c$ . When sections are fabricated by welding plates together, however,

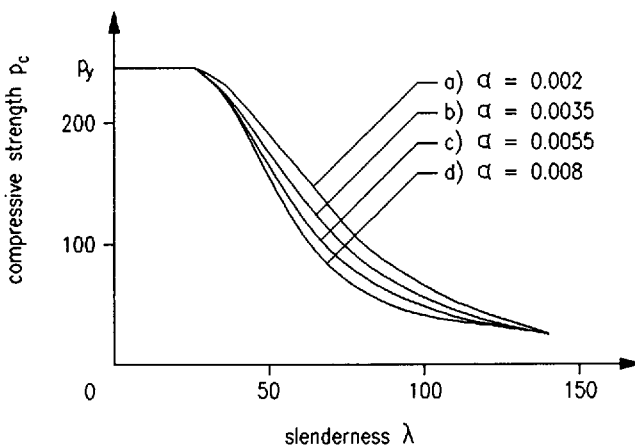


Fig. 15.2 Strut curves of BS 5950

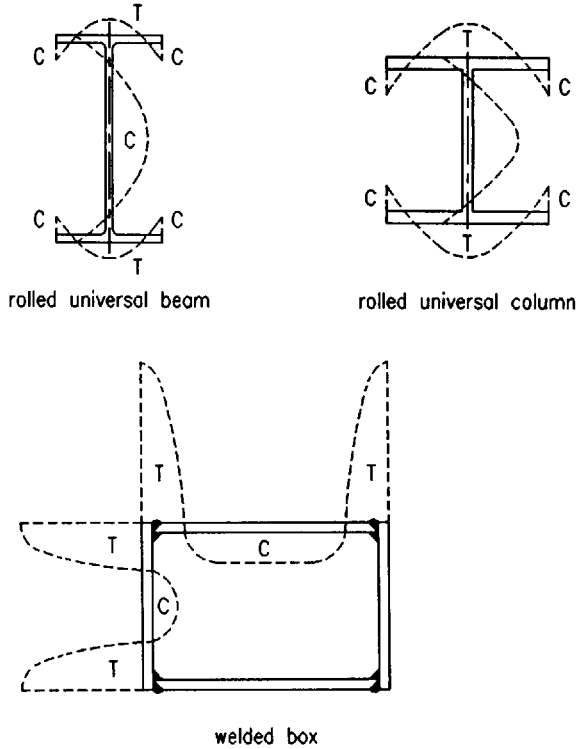


Fig. 15.3 Distribution of residual stresses

the pattern of residual stresses produced by the heating and cooling of the welding process will be rather different from that typically found in a hot-rolled section<sup>3</sup> as illustrated in Fig. 15.3. This tends to produce lower buckling strengths. It is allowed for in BS 5950: Part 1 by the modification to the column curves shown in Fig. 15.4 in which the basic curve of Fig. 15.2 is replotted for a reduced material design strength. This has the effect of reducing the basic curve down to the level of that for the welded member in the important medium slenderness region. Clause 4.7.5 thus requires that when checking the axial resistance of a member that has been fabricated from plate by welding, the value of  $p_c$  be obtained using a  $p_y$  value of 20 N/mm<sup>2</sup> less than the actual figure.

BS 5400: Part 3 is intended to cover a wider range of construction than BS 5950: Part 1. Specifically in this context it recognizes the greater likelihood that struts may contain slender elements (other than outstands) and so it defines compression resistance,  $P_c$ , as

$$P_c = A_c p_c \quad (\text{clause 10.6.1.1})$$

in which  $A_c$  is the effective area defined as

$$A_c = \Sigma K_c (k_h A_c) \quad \text{for members other than CHSs}$$

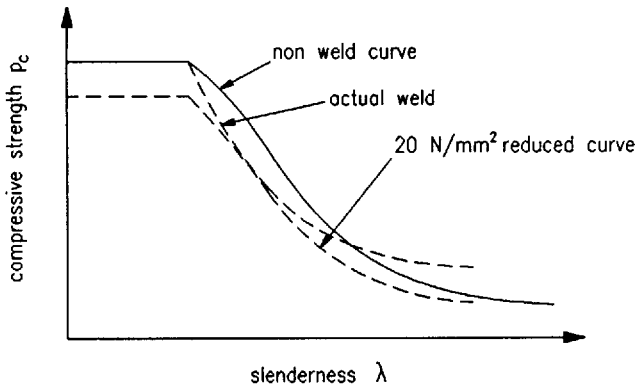


Fig. 15.4 Modified strut curve for welded sections used in BS 5950: Part 1

where  $K_c$  allows for loss of effectiveness in slender plate elements, determined from Figure 36,  $k_h$  allows for the presence of holes, and  $A_c$  is the net area; and

$$A_e = A_c \quad \text{for CHSs for which } \frac{D}{t} \sqrt{\left(\frac{p_y}{355}\right)} \leq 50$$

$$A_e = A_c \left[ 1.15 - 0.003 \frac{D}{t} \sqrt{\left(\frac{p_y}{355}\right)} \right] \quad \text{for CHSs for which } \frac{D}{t} \sqrt{\left(\frac{p_y}{355}\right)} > 50$$

$p_c$  is obtained from a set of curves (Figure 37) similar to Fig. 15.2.

Selection of the appropriate column curve is made using a simpler selection table than that of Part 1 of BS 5950. Essentially it distinguishes between curves on the basis of the ratio of radius of gyration to distance from neutral axis to extreme fibre, apart from heavy sections and hot-finished SHS which are universally allocated to the lowest and highest curves respectively.

### 15.6 Torsional and flexural-torsional buckling

In addition to the simple flexural buckling described in the previous section, struts may buckle due to either pure twisting about their longitudinal axis or a combination of bending and twisting. The first type of behaviour is only possible for centrally-loaded doubly-symmetrical cross sections for which the centroid and shear centre coincide. The second, rather more general form of response, occurs for centrally-loaded struts such as channels for which the centroid and shear centre do not coincide.

In practice pure torsional buckling of hot-rolled structural sections is highly unlikely, the pure flexural mode normally requiring a lower load, unless the strut is of a somewhat unusual shape so that its torsional and warping stiffnesses are

low as for a cruciform section. In such cases a reasonable design approach consists of determining an effective slenderness based on the direct use of the member's elastic critical load for torsional buckling (assuming this to be lower than its elastic critical load for pure flexural buckling) and using this to enter the basic column design curve. This approach is well substantiated for aluminium members for which torsional buckling more commonly controls. Similarly for unsymmetrical sections, use of an effective slenderness based on the member's lowest elastic critical load, corresponding to flexural-torsional buckling in this case, permits the basic column design curve to be retained and used in a more general way. For certain types of section, such as hot-rolled angles, special empirically-based design approaches are provided in BS 5950: Part 1 which recognize the possibility of some torsional influence. They are discussed in detail in section 15.8.

Torsional-flexural buckling is of greater practical significance in the design and use of cold-formed sections. This arises for two reasons:

- (1) Because the torsion constant,  $J$ , depends on  $t^3$ , the use of thin material results in the ratio of torsional to flexural stiffness being much reduced as compared with hot-rolled sections
- (2) The forming process leads naturally to a preponderance of singly-symmetrical or unsymmetrical open sections as these can be produced from a single sheet.

Procedures are given in BS 5950: Part 5 for determining the axial strength of singly-symmetrical sections using a factored effective length  $\alpha L_E$ , in which  $\alpha$  is obtained from

$$\alpha = 1 \quad \text{for } P_{EY} \leq P_{TF}$$

$$\alpha = P_{EY}/P_{TF} \quad \text{for } P_{EY} > P_{TF}$$

Formulae for  $P_{TF}$  in terms of basic cross-sectional properties are also provided. The use of  $\alpha \neq 1$  is only required for those situations illustrated in Fig. 15.5 for which  $P_{TF}$  is the lowest elastic critical load.

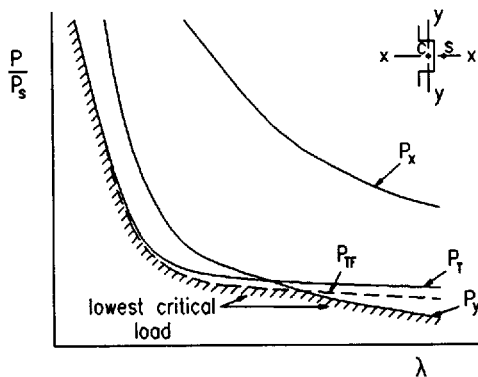


Fig. 15.5 Elastic critical load curves for a member subject to flexural-torsional buckling

### 15.7 Effective lengths

Basic design information relating column strength to slenderness is normally founded on the concept of a pin-ended member, e.g. Fig. 15.2. Stated more precisely, this means a member whose ends are supported such that they cannot translate relative to one another but are able to rotate freely. Compression members in actual structures are provided with a variety of different support conditions which are likely to be less restrictive in terms of translational restraint, giving fixity in position, with or without more restriction in terms of rotational restraint, giving fixity in direction.

The usual way of treating this topic in design is to use the concept of an effective column length which may be defined as ‘the length of an equivalent pin-ended column having the same load-carrying capacity as the member under consideration provided with its actual conditions of support’. This engineering definition of effective length is illustrated in Fig. 15.6 which compares a column strength curve for a member with some degree of rotational end restraint with the basic curve for the same member when pin-ended.

In determining the column slenderness ratio the geometrical length,  $L$ , is replaced by the effective length,  $L_E$ . Values of effective length factors  $k = L_E/L$  for a series of standard cases are provided in BS 5950: Part 1, BS 5400: Part 3, etc.; Fig. 15.7 illustrates typical values. When compared with values given by elastic stability theory,<sup>2</sup> these appear to be high for those cases in which reliance is being placed on externally provided rotational fixity; this is in recognition of the practical difficulties of providing sufficient rotational restraint to approach the condition of full fixity. On the other hand, translational restraints of comparatively

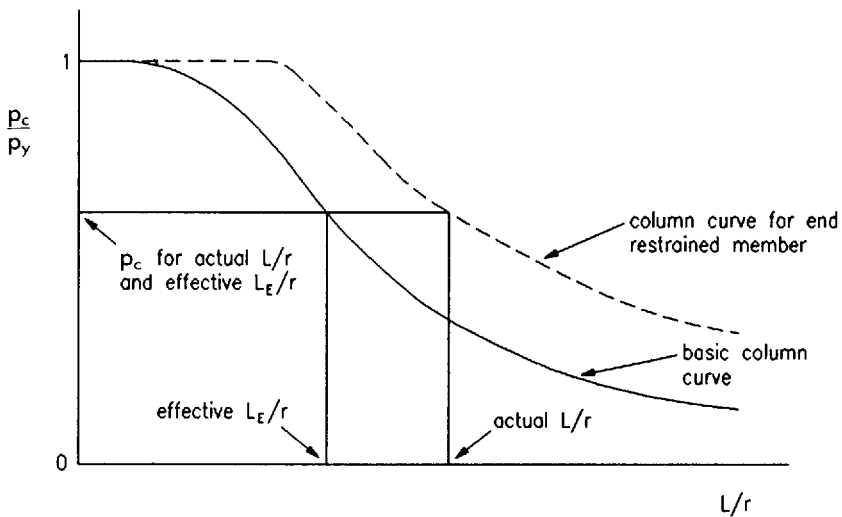


Fig. 15.6 Use of effective length with column curve to allow for end restraint


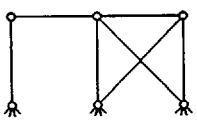
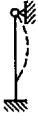
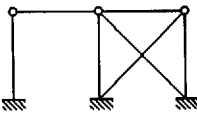

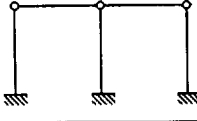
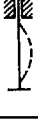
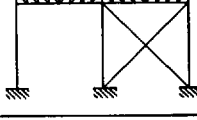
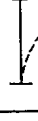
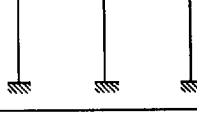
| model   | example   | factor |
|---|---|--------|
|  |  | 1.0    |
|  |  | 0.85   |
|  |  | 2.0    |
|  |  | 0.7    |
|  |  | 1.0    |

Fig. 15.7 Typical effective length factors for use in strut design

modest stiffness are quite capable of preventing lateral displacements. A certain degree of judgement is required of the designer in deciding which of these standard cases most nearly matches his arrangements. In cases of doubt the safe approach is to use a high approximation, leading to an overestimate of column slenderness and thus an underestimate of strength. The idea of an effective column length may also be used as a device to deal with special types of column, such as compound or tapered members, the idea then being to convert the complex problem into one of an equivalent simple column for which the basic design approach of the relationship between compressive strength and slenderness may be employed.

Of fundamental importance when determining suitable effective lengths is the classification of a column as either a sway case for which translation of one end relative to the other is possible or a non-sway case for which end translation is prevented. For the first case, effective lengths will be at least equal to the geometrical length, tending in theory to infinity for a pin-base column with no restraint at its top, while for the non-sway case, effective lengths will not exceed the geometrical length, decreasing as the degree of rotational fixity increases.



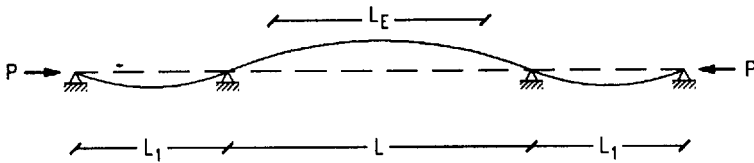


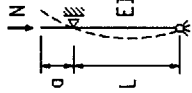
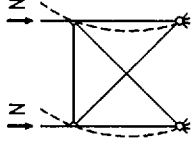
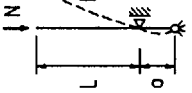
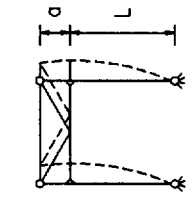
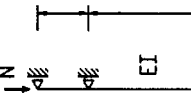
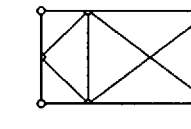
Fig. 15.8 Restraint to critical column segment from adjacent segments

For non-standard cases, it is customary to make reference to published results obtained from elastic stability theory. Providing these relate to cases for which buckling involves the interaction of a group of members with the less critical restraining the more critical, as illustrated in Fig. 15.8, such evidence as is available suggests that the use of effective lengths derived directly from elastic stability theory in conjunction with a column design curve of the type shown in Fig. 15.2 will lead to good approximations of the true load-carrying capacity.

For compression members in rigid-jointed frames the effective length may, in both cases, be directly related to the restraint provided by the surrounding members by using charts presented in terms of the stiffness of these members provided in Appendix E of BS 5950: Part 1. Useful guidance on effective column lengths for a variety of more complex situations is available from several sources.<sup>2-4</sup>

When designing compression members in frames configured on the basis of simple construction, the use of effective column lengths provides a simple means of recognizing that real connections between members will normally provide some degree of rotational end restraint, leading to compressive strengths somewhat in excess of those that would be obtained if columns were treated as pin-ended. If axial load levels and unsupported lengths change within the length of a member that is continuous over several segments such as a building frame column spliced so as to act as a continuous member but carrying decreasing compression with height or a compression chord in a truss, then the less heavily loaded segments will effectively restrain the more critical segments.

Even though the distribution of internal member forces has been made on the assumption of pin joints, some allowance for rotational end restraint when designing the compression members is therefore appropriate. Thus the apparent contradiction of regarding a structure as pin-jointed but using compression member effective lengths that are less than their actual lengths does have a basis founded upon an approximate version of reality. Figure 15.9 presents results obtained from elastic stability theory for columns continuous over a number of storeys which show how the effective length of the critical segment will be reduced if more stable segments (shorter unbraced lengths in this case) are present. A practical equivalent for each case in terms of simple braced frames with pinned beam-to-column connections is also shown. It is also necessary to recognize that practical equivalents of pin joints may also be capable of transferring limited moments. This point is considered explicitly in BS 5950: Part 1 for both building frames and trusses; the effect on the

| column   | frame  | 0    | 0.1  | 0.2  | 0.3  | 0.4  | 0.5  | 0.6  | 0.7  | 0.8  | 0.9  | 1.0  | $a/L$   |
|--|--|------|------|------|------|------|------|------|------|------|------|------|---------|
|   |   | 1.0  | 1.11 | 1.24 | 1.40 | 1.56 | 1.74 | 1.93 | 2.16 | 2.31 | 2.50 | 2.70 | $L_f/L$ |
|   |   | 2.0  | 2.07 | 2.13 | 2.20 | 2.27 | 2.34 | 2.41 | 2.48 | 2.55 | 2.62 | 2.70 | $L_f/L$ |
|  |  | 0.70 | 0.72 | 0.74 | 0.77 | 0.79 | 0.81 | 0.84 | 0.87 | 0.91 | 0.95 | 1.0  | $L_f/L$ |

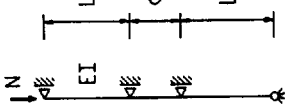
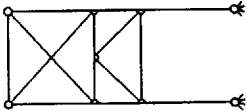
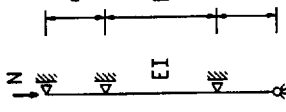
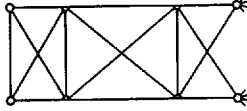
| column  | frame   | 0    | 0.1  | 0.2  | 0.3  | 0.4  | 0.5  | 0.6  | 0.7  | 0.8  | 0.9  | 1.0 | $a/L$   |
|---|---|------|------|------|------|------|------|------|------|------|------|-----|---------|
|  |  | 0.70 | 0.73 | 0.76 | 0.79 | 0.82 | 0.85 | 0.88 | 0.91 | 0.94 | 0.97 | 1.0 | $L_r/L$ |
|  |  | 0.50 | 0.53 | 0.57 | 0.61 | 0.65 | 0.70 | 0.75 | 0.81 | 0.87 | 0.93 | 1.0 | $L_r/L$ |

Fig. 15.9 Effective length factors for continuous columns based on elastic stability theory

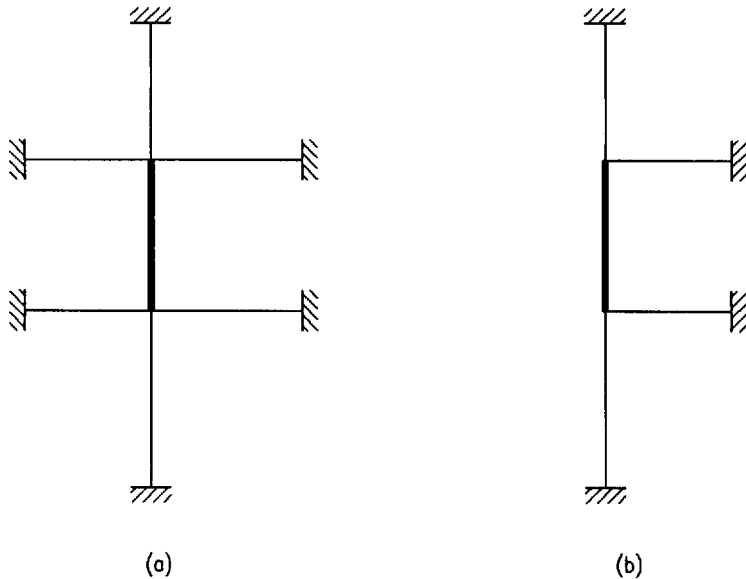


Fig. 15.10 Limited frames. (a) Internal column. (b) External column

design of compression members is considered in detail in Chapter 18 for the former and in Chapter 19 for the latter.

For compression members in rigid-jointed frames the effective length is directly related to the restraint provided by all the surrounding members. Strictly speaking an interaction of all the members in the frame occurs because the real behaviour is one of frame buckling rather than column buckling, but for design purposes it is often sufficient to consider the behaviour of a limited region of the frame. Variants of the 'limited frame' concept are to be found in several Codes of Practice and design guides. That used in BS 5950: Part 1 is illustrated in Fig. 15.10. The limited frame comprises the column under consideration and each immediately adjacent member treated as if its far end were fixed. The effective length of the critical column is then obtained from a chart which is entered with two coefficients  $k_1$  and  $k_2$ , the values of which depend on the stiffnesses of the surrounding members  $K_U$ ,  $K_{TL}$ , etc., relative to the stiffness of the column  $K_C$ , a concept similar to the well-known moment distribution method. Two distinct cases are considered: columns in non-sway frames and columns in frames that are free to sway. Figures 15.11 (a) and (b) and 15.11 (c) and (d) illustrate both cases as well as giving the associated effective length charts. For the former, the factors will vary between 0.5 and 1.0 depending on the values of  $k_1$  and  $k_2$ , while for the latter, the variation will be between 1.0 and  $\infty$ . These end points correspond to cases of: rotationally fixed ends with no sway and rotationally free ends with no sway; rotationally fixed ends with free sway and rotationally free ends with free sway.

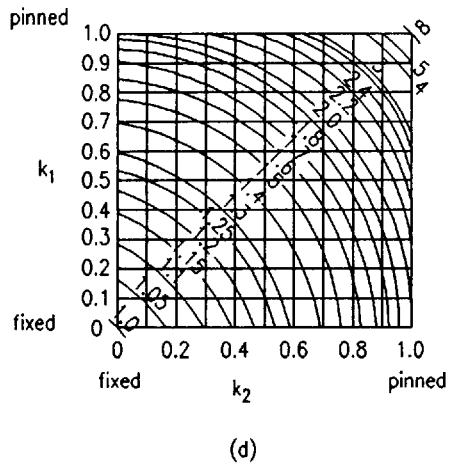
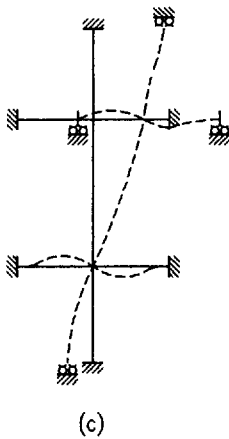
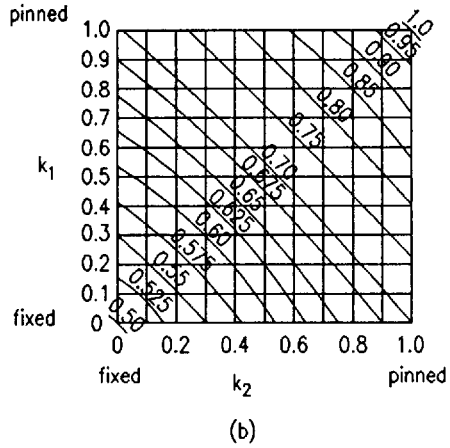
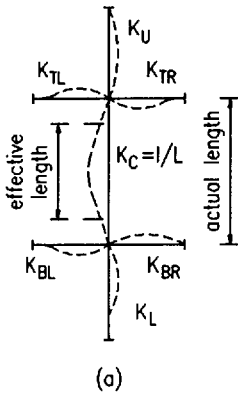


Fig. 15.11 Limited frames and corresponding effective length charts of BS 5950: Part 1. (a) Limited frame and (b) effective length ratios ( $k_3 = \infty$ , for non-sway frames. (c) Limited frame and (d) effective length ratios (without partial bracing,  $k_3 = 0$ ), for sway frames

For beams not rigidly connected to the column or for situations in which significant plasticity either at a beam end or at either column end would prevent the restraint being transferred into the column, the  $K$  (and thus the  $k$ ) values must be suitably modified. Similarly at column bases,  $k_2$  values, in keeping with the degree of restraint provided, should be used. Guidance is also provided on  $K$

values for beams, distinguishing between both non-sway and sway cases and beams supporting concrete floors and bare steelwork. A further pair of charts permits modest degrees of partial restraint against sway, as might be provided for example by infill panels, to be allowed for in slightly reducing effective length values for sway frames. Full details of the background to this approach to the determination of effective lengths in rigidly jointed sway, partially braced and non-sway frames may be found in the work of Wood.<sup>4</sup>

### 15.8 Special types of strut

The design of two types of strut requires that certain additional points be considered:

- (1) built-up sections or compound struts (Fig. 15.12), for which the behaviour of the individual components must be taken into account
- (2) angles, channels and tees (Fig. 15.13), for which the eccentricity of loading produced by normal forms of end connection must be acknowledged.

In both cases, however, it will often be possible to design this more complex type of member as an equivalent single axially-loaded strut.

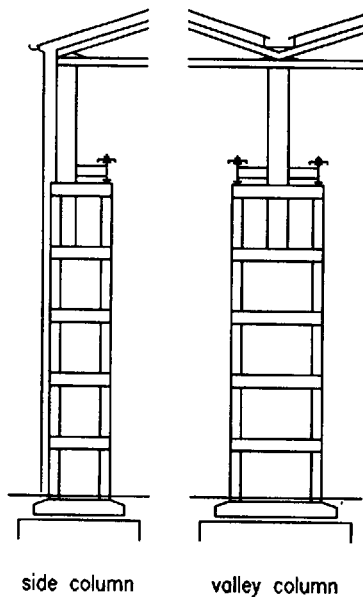
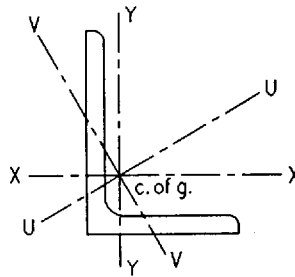


Fig. 15.12 Built-up struts



|          |                        |
|----------|------------------------|
| axis X-X | } rectangular axes     |
| axis Y-Y |                        |
| axis U-U | maximum principal axis |
| axis V-V | minimum principal axis |

Fig. 15.13 Geometrical properties of an angle section

### 15.8.1 Design of compound struts

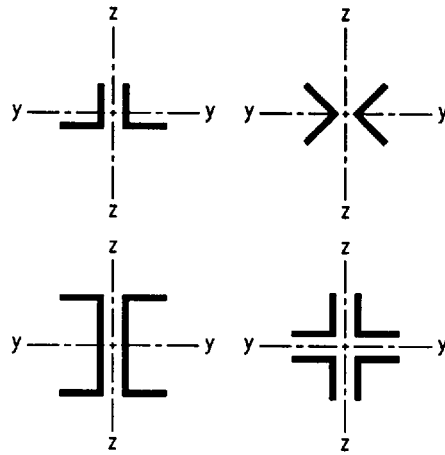
Individual members may be combined in a variety of ways to produce a more efficient compound section. Figure 15.14 illustrates the most common arrangements. In each case the concept is one of providing a compound member whose overall slenderness will be such that its load-carrying capacity will significantly exceed the sum of the axial resistances of the component members, i.e. for the case of Fig. 15.14(b) the laced strut will be stronger than the four corner angles treated separately.

Thus the design approach of BS 5950: Part 1 is to set conditions which when met permit the compound member to be designed as a single integral member. The following cases are considered explicitly:

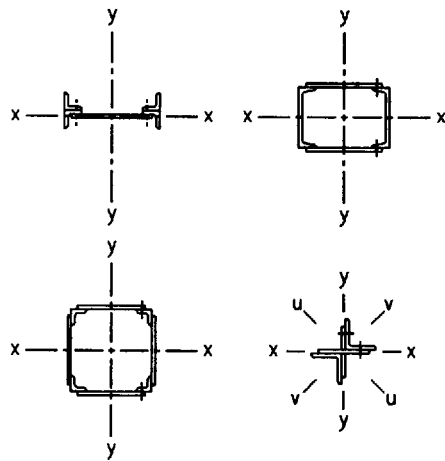
- (1) Laced struts conforming with the provisions of clause 4.7.8
- (2) Battened struts conforming with the provisions of clause 4.7.9
- (3) Batten-starred angles conforming with the provisions of clause 4.7.11, which uses much of clause 4.7.9
- (4) Batten parallel angle struts conforming with the provisions of clause 4.7.12
- (5) Back-to-back struts conforming with the provisions of clause 4.7.13.1 if the components are separated and of clause 4.7.13.2 if the components are in contact.

The detailed rules contained in these clauses are essentially of two types:

- (1) Covering construction details such as the arrangements for interconnection in a general 'good practice' manner



(a)



(b)

Fig. 15.14 Typical arrangements for compound struts: (a) closely spaced, (b) laced or battened

(2) Quantitative rules for the determination of the overall slenderness, limits necessary for component slenderness, forces for which the interconnections should be designed, etc.

BS 5400: Part 3 also contains specific rules for the design of:



- (1) Batten struts (clause 10.8)
- (2) Laced struts (clause 10.9)
- (3) Struts connected by perforated cover plates (clause 10.10)
- (4) Struts consisting of back-to-back components (clause 10.11).

These are somewhat more detailed than those of BS 5950: Part 1, particularly in the matter of determining suitable design forces for the interconnections, i.e. battens, lacings, etc.

### 15.8.2 Design of angles, channels and tees

Four specific cases are covered in detail by BS 5950: Part 1:

- (1) Single angles in clause 4.7.10.2
- (2) Double angles in clause 4.7.10.3
- (3) Single channels in clause 4.7.10.4
- (4) Single tees in clause 4.7.10.5.

In all cases, guidance is provided on the determination of the slenderness to be used when obtaining  $p_c$  for each of the more common forms of fastening arrangement. In cases where only a single fastener is used at each end the resulting value of  $p_c$  should then be reduced to 80% so as to allow for the combined effects of load eccentricity and lack of rotational end restraint. For ease of use the whole set of slenderness relationships is grouped together in Table 28.

BS 5400: Part 3 only gives specific consideration to single angles. This distinguishes between single bolt and 'other' forms of end connection. In both cases load eccentricity may be ignored but for the former only 80% of the calculated resistance may be used.

### 15.9 Economic points

Strut design is a relatively straightforward design task involving choice of cross-sectional type, assessment of end restraint and thus effective length, calculation of slenderness, determination of compressive strength and hence checking that the trial section can withstand the design load. Certain subsidiary checks may also be required part way through this process to ensure that the chosen cross section is not slender (or make suitable allowances if it is) or to guard against local failure in compound members. Thus only limited opportunities occur for the designer to use judgement and to make choices on the grounds of economy. Essentially these are restricted to control of the effective length, by introducing intermediate restraints where appropriate, and the original choice of cross section.

However, certain other points relating to columns may well have a bearing on the overall economy of the steel frame or truss. Of particular concern is the need to be able to make connections simply. In a multi-storey frame, the use of heavier UC sections thus may be advantageous, permitting beam-to-column connections to be made without the need for stiffening the flanges or web. Similarly in order to accommodate beams framing into the column web an increase in the size of UC may eliminate the need for special detailing.

While compound angle members were a common feature of early trusses, maintenance costs due both to the surface area requiring painting and the incidence of corrosion caused by the inherent dirt and moisture traps have caused a change to the much greater use of tubular members. If site joints are kept to the minimum tubular trusses can be transported and handled on site in long lengths and a more economic as well as a visually more pleasing structure is likely to result.


### References to Chapter 15

1. The Steel Construction Institute (SCI) (1991) *Steelwork Design Guide to BS 5950: Part 1: 1985, Vol. 1: Section Properties, Member Capacities*, 3rd edn. SCI, Ascot, Berks.
2. Ballio G. & Mazzolani F.M. (1983) *Theory and Design of Steel Structures*. Chapman and Hall.
3. Allen H.G. & Bulson P.S. (1980) *Background to Buckling*. McGraw-Hill.
4. Wood R.H. (1974) Effective lengths of columns in multi-storey buildings. *The Structural Engineer*, **52**, Part 1, July, 235–44, Part 2, Aug., 295–302, Part 3, Sept., 341–6.

### Further reading for Chapter 15

- ECCS (1986) *Behaviour and Design of Steel Plated Structures* (Ed. by P. Dubas & E. Gehri). ECCS Publication No. 44.
- Galambos T.V. (Ed.) (1988) *Guide to Stability Design Criteria for Metal Structures*, 4th edn. Wiley Interscience.
- Hancock G.J. (1988) *Design of Cold-Formed Steel Structures*. Australian Institute of Steel Construction.
- Kirby P.A. & Nethercot D.A. (1985) *Design for Structural Stability*. Collins, London.
- Trahair N.S. & Nethercot D.A. (1984) *Bracing Requirements in Thin-Walled Structures, Developments in Thin-Walled Structures – 2* (Ed. by J. Rhodes & A.C. Walker), pp. 92–130. Elsevier Applied Science Publishers, Barking, Essex.

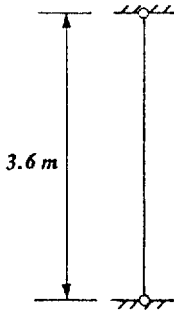
A series of worked examples follows which are relevant to Chapter 15.

|  |  |   |                           |
|--|--|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>COLUMN EXAMPLE 1</b><br><b>ROLLED UNIVERSAL COLUMN</b> |   | Chapter ref.<br><b>15</b> |
|  | Design code<br><b>BS5950: Part 1</b>                                 | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>        |

**Problem**

Check the ability of a 203 × 203 × 52 UC in grade 43 steel to withstand an axial compressive load of 1250 kN over an unsupported height of 3.6 m assuming that both ends are held in position but are provided with no restraint in direction. Design to BS 5950: Part 1.

The problem is as shown in the sketch.



Take effective length  $L_E = 1.0 L$  Table 24

$\therefore L_E = 1.0 \times 3.6 \times 10^3$

$= 3600 \text{ mm}$

On the assumption that weak axis flexural buckling will govern determine compressive strength  $p_c$  from Table 27c. Table 25

$A = 66.4 \text{ cm}^2$   $b/T = 8.16$  Steelwork

$r_y = 5.16 \text{ cm}$   $d/t = 20.1$  Design Guide


Vol 1

Since  $T < 16 \text{ mm}$  take  $p_y = 275 \text{ N/mm}^2$  Table 6

Check section classification for pure compression. 3.5

Need only check section is not slender; Table 7

for outstand  $b/T \leq 15\epsilon$

|   |  |   |                           |
|---|--|---|---------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>COLUMN EXAMPLE 1</b><br><b>ROLLED UNIVERSAL COLUMN</b> |   | Chapter ref.<br><b>15</b> |
|   | Design code<br><b>BSS950: Part 1</b>                                 | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |

for web  $d/t \leq 39\epsilon$

$$\epsilon = \sqrt{(275/p_y)} = 1.0$$

actual  $b/T = 8.16$ , within limit

actual  $d/t = 20.1$ , within limit

$\therefore$  Section is not slender.

$$P_c = A_g p_c \quad 4.7.4$$

$$\lambda = L_E / r_y = 3600 / 51.6 = 70 \quad 4.7.3$$


For  $\lambda = 70$  and  $p_y = 275 \text{ N/mm}^2$  Table 27c

value of  $p_c = 202 \text{ N/mm}^2$

$$\begin{aligned} \therefore P_c &= 6640 \times 202 = 1341 \times 10^3 \text{ N} \\ &= 1341 \text{ kN} \end{aligned}$$

*This exceeds required resistance of 1250 kN and section is therefore OK.*

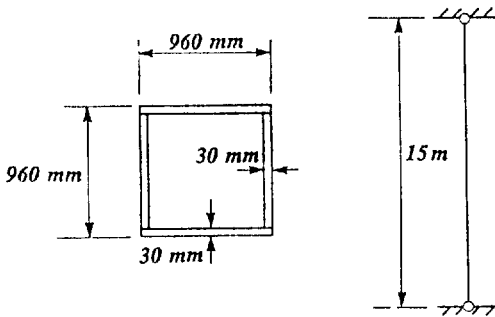
$\therefore$  Use 203 × 203 × 52 UC

|   |  |  |                                      |
|---|--|--|--------------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>COLUMN EXAMPLE 2</b></p> <p><b>WELDED BOX</b></p> |  | <p>Chapter ref.</p> <p><b>15</b></p> |
|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p>                        | <p>Made by <b>DAN</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>1</b></p>            |

**Problem**

Check the ability of a 960 mm square box column fabricated from 30 mm thick grade 50 plate to withstand an axial compressive load of 22000 kN over an unsupported height of 15 m assuming that both ends are held in position but are provided with no restraint in direction. Design to BS 5950: Part 1.

The problem is as shown in the sketches.



Take effective length  $L_E = 1.0 L$  Table 24

$$\begin{aligned} \therefore L_E &= 1.0 \times 15 \times 10^3 \\ &= 15000 \text{ mm} \end{aligned}$$

Determine  $p_c$  from Table 27b Table 25


Since  $T > 16 \text{ mm}$ , take  $p_y = 340 \text{ N/mm}^2$  Table 6


Check section classification for pure compression. 3.5

Need only check section is not slender; Table 7

for flange  $b/T \leq 28\epsilon$

$$\epsilon = \sqrt{(275/340)} = 0.9$$

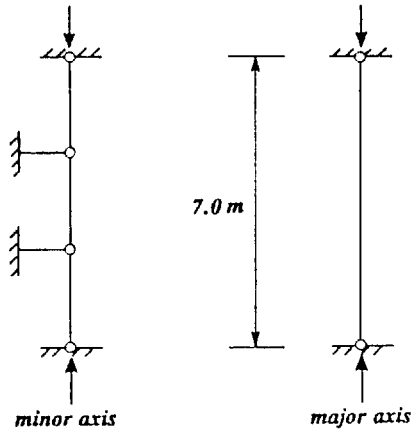
|   |   |   |                           |
|---|---|---|---------------------------|
|  <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7ON</p>  | Subject<br><b>COLUMN EXAMPLE 2<br/>WELDED BOX</b> |   | Chapter ref.<br><b>15</b> |
|   | Design code<br><b>BSS950: Part 1</b>              | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |
| <p><i>actual b/T</i> = (960 - 2 × 30)/30 = 30</p> <p><i>limit</i> = 0.9 × 28 = 25.2</p> <p>∴ <i>Section is slender.</i></p> <p><i>Strength reduction factor</i> = <math>\frac{21}{30/0.9 - 7} = 0.8</math> <span style="float: right;"><i>Table 8</i></span></p> <p><i>Use reduced p<sub>y</sub></i> = 0.8 × 340 = 272 N/mm<sup>2</sup></p> <p><i>I<sub>y</sub></i> = (960 × 960<sup>3</sup> - 900 × 900<sup>3</sup>)/12 = 1.61 × 10<sup>10</sup> mm<sup>4</sup></p> <p><i>A<sub>g</sub></i> = 2 × 30 (960 + 900) = 111600 mm<sup>2</sup></p> <p><i>r<sub>y</sub></i> = <math>\sqrt{1.61 \times 10^{10}/111600} = 380 \text{ mm}</math></p> <p><i>λ</i> = <math>L_E / r_y = 15000/380 = 39.5</math> <span style="float: right;"><i>4.3.7.1</i></span></p> <p><i>Since section fabricated by welding, use Table 27b with</i> <span style="float: right;"><i>4.7.5</i></span></p> <p><i>p<sub>y</sub></i> = 272 - 20 = 252 N/mm<sup>2</sup></p> <p><i>For λ = 39.5 and p<sub>y</sub> = 252 N/mm<sup>2</sup></i> <span style="float: right;"><i>Table 27b</i></span></p> <p><i>value of p<sub>c</sub></i> = 230 N/mm<sup>2</sup></p> <p><i>P<sub>c</sub></i> = <i>A<sub>g</sub> p<sub>c</sub></i> = 111600 × 230 <span style="float: right;"><i>4.7.4</i></span></p> <p style="margin-left: 150px;">= 25.7 × 10<sup>6</sup> N</p> <p style="margin-left: 150px;">= 25700 kN</p> <p><i>This exceeds required resistance of 22000 kN and section is OK.</i></p> <p>∴ <i>Use section shown in figure.</i></p> |   |   |                           |

|  |   |   |                           |
|--|---|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7ON | Subject<br><b>COLUMN EXAMPLE 3<br/>                 ROLLED UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>15</b> |
|  | Design code<br><b>BSS950: Part 1</b>  | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>        |

**Problem**

A 457 × 191 × 89 UB in Grade 43 steel is to be used as an axially loaded column over a free height of 7.0 m. Both ends will be held in position but not direction for both planes. The possibility exists to provide discrete bracing members capable of preventing deflection in the plane of the flanges only. Investigate the advisability of using such bracing.

Clearly strength cannot exceed that for major axis failure. Check no. of intermediate (minor-axis) braces needed to achieve this.



Take  $L_{Ex} = 1.0 L$

$\therefore L_{Ex} = 1.0 \times 7.0 \times 10^3 = 7000 \text{ mm}$

$A = 114 \text{ cm}^2$

$b/T = 5.42$

$r_y = 4.28 \text{ cm}$

$d/t = 38.5$

$r_x = 19.0 \text{ cm}$

$p_y = 265 \text{ N/mm}^2 \text{ (for } T = 17.7 \text{ mm)}$

*Steelwork  
Design Guide  
Vol 1*

Section not slender

Table 7

$P_c = A_g p_c$


4.7.4

$\lambda_x = L_{Ex} / r_x = 7000 / 19.0 = 37$

4.7.3

Use Table 27a for  $p_{cx}$

Table 25

|   |   |   |                           |
|---|---|---|---------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>COLUMN EXAMPLE 3<br/>                 ROLLED UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>15</b> |
|   | Design code<br><b>BS5950: Part 1</b>  | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |

For  $\lambda = 37$  and  $p_y = 265 \text{ N/mm}^2$  Table 27a

value of  $p_{cx} = 253 \text{ N/mm}^2$

$$P_{cx} = 11400 \times 253 = 2.884 \times 10^6 \text{ N} = \underline{2884 \text{ kN}}$$

Use Table 27b for  $p_{cy}$  & Table 25

For a  $p_{cy}$  value of  $253 \text{ N/mm}^2$ , value of  $\lambda_y \neq 30$  Table 27b

$$\therefore L_{Ey} / 42.8 = 30$$

and  $L_{Ey} \neq 1284 \text{ mm}$

$\therefore$  to achieve a minor axis buckling resistance  $\neq 2987 \text{ kN}$  would require 7.0 m height to be provided with  $7000/1284 \rightarrow 5$  restraints

$$L_{Ey} / r_y = (7000/6) / 42.8 = 27$$

$p_{cy} = 256 \text{ N/mm}^2$  Table 27b

$$P_{cy} = 11400 \times 256 = 2.918 \times 10^6 = \underline{2918 \text{ kN}}$$

Note however that substantial improvements on the basic minor axis resistance for  $L_{Ey} = 7.0 \text{ m}$  of  $741 \text{ kN}$  may be achieved for rather less restraints as shown below.

| no. of restraints | $P_{cy}$ (kN) | $P_{cy} / P_{cx}$ |
|-------------------|---------------|-------------------|
| 0                 | 730           | 0.25              |
| 1                 | 1972          | 0.68              |
| 2                 | 2531          | 0.88              |
| 3                 | 2645          | 0.92              |



# Chapter 16

## Beams

by DAVID NETHERCOT

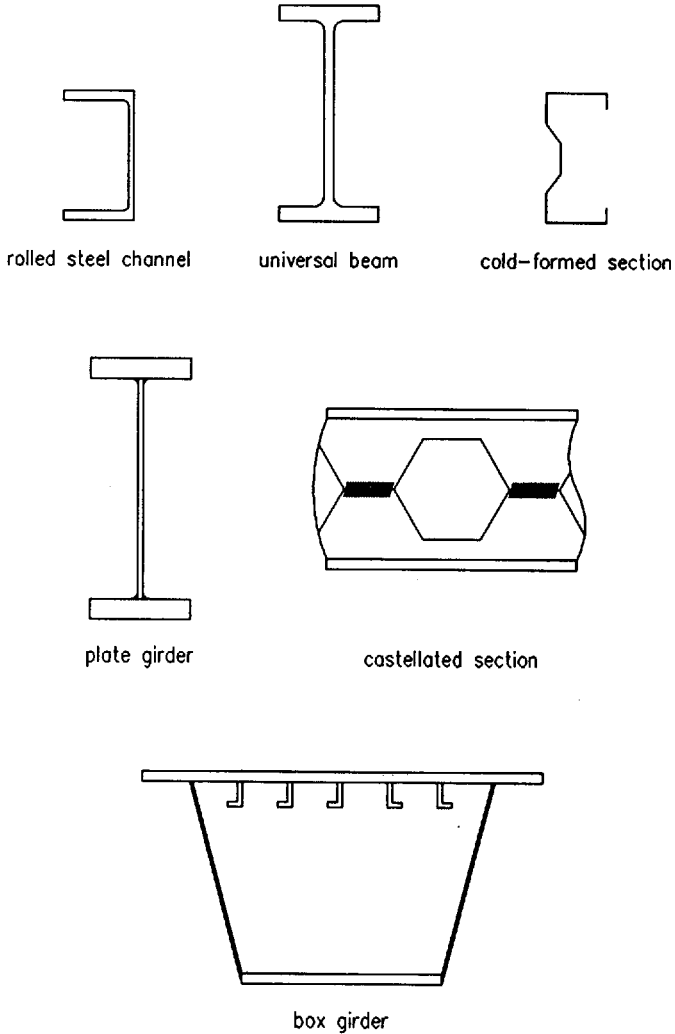
### 16.1 Common types of beam

Beams are possibly the most fundamental type of member present in a civil engineering structure. Their principal function is the transmission of vertical load by means of flexural (bending) action into, for example, the columns in a rectangular building frame or the abutments in a bridge which support them.

Table 16.1 provides some idea of the different structural forms suitable for use as beams in a steel structure; several of these are illustrated in Fig. 16.1. For

**Table 16.1** Typical usage of different forms of beam

| Beam type                                 | Span range (m) | Notes   |
|---|----------------|---|
| (0) Angles                                | 3–6            | Used for roof purlins, sheeting rails, etc., where only light loads have to be carried  |
| (1) Cold-formed sections                  | 4–8            | Used for roof purlins, sheeting rails, etc., where only light loads have to be carried  |
| (2) Rolled sections: UBs, UCs, RSJs, RSCs | 1–30           | Most frequently used type of section; proportions selected to eliminate several possible types of failure                                       |
| (3) Open web joists                       | 4–40           | Prefabricated using angles or tubes as chords and round bar for web diagonals, used in place of rolled sections                                 |
| (4) Castellated beams                     | 6–60           | Used for long spans and/or light loads; depth of UB increased by 50%; web openings may be used for services, etc.                               |
| (5) Compound sections e.g. UB + RSC       | 5–15           | Used when a single rolled section would not provide sufficient capacity; often arranged to provide enhanced horizontal bending strength as well |
| (6) Plate girders                         | 10–100         | Made by welding together 3 plates sometimes automatically; web depths up to 3–4 m sometimes need stiffening                                     |
| (7) Trusses                               | 10–100         | Heavier version of (3); may be made from tubes, angles or if spanning large distances, rolled sections  |
| (8) Box girders                           | 15–200         | Fabricated from plate, usually stiffened; used for OHT cranes and bridges due to good torsional and transverse stiffness properties             |



*Fig. 16.1* Types of beam cross-section

modest spans, including the majority of those found in buildings, the use of standard hot-rolled sections (normally UBs but possibly UCs if minimizing floor depth is a prime consideration or channels if only light loads need to be supported) will be sufficient. Lightly loaded members such as the purlins supporting the roof of a portal-frame building are frequently selected from the range of proprietary cold-formed sections produced from steel sheet only a few millimetres thick, normally already protected against corrosion by galvanizing, in a variety of highly

efficient shapes, advantage being taken of the roll-forming process to produce sections with properties carefully selected for the task they are required to perform. For spans in excess of those that can be achieved sensibly using ready-made sections some form of built-up member is required. Castellated beams, formed by profile cutting of the web and welding to produce a deeper section, typically 50% deeper using the standard UK geometry, are visually attractive but cannot withstand high shear loads unless certain of the castellations are filled in with plate. The range of spans for which UBs may be used can be extended if cover plates are welded to both flanges.

Alternatively a beam fabricated entirely by welding plates together may be employed allowing variations in properties by changes in depth, for example, flange thickness, or, in certain cases where the use of very thin webs is required, stiffening to prevent premature buckling failure is necessary. A full treatment of the specialist aspects of plate-girder design is provided in Chapter 17. If spans are so large that a single member cannot economically be provided, then a truss may be a suitable alternative. In addition to the deep truss fabricated from open hot-rolled sections, SHS or both, used to provide long clear spans in sports halls and supermarkets, smaller prefabricated arrangements using RHS or CHS provide an attractive alternative to the use of standard sections for more modest spans. Truss design is discussed in Chapter 19.

Since the principal requirement of a beam is adequate resistance to vertical bending, a very useful indication of the size of section likely to prove suitable may be obtained through the concept of the span to depth ratio. This is simply the value of the clear span divided by the overall depth. An average figure for a properly designed steel beam is between 15 and 20, perhaps more if a particularly slender form of construction is employed or possibly less if very heavy loadings are present.

When designing beams, attention must be given to a series of issues, in addition to simple vertical bending, that may have some bearing upon the problem. Torsional loading may often be eliminated by careful detailing or its effects reasonably regarded as of negligible importance by a correct appreciation of how the structure actually behaves; in certain instances it should, however, be considered. Section classification (allowance for possible local buckling effects) is more involved than is the case for struts since different elements in the cross-section are subject to different patterns of stress; the flanges in an I-beam in the elastic range will be in approximately uniform tension or compression while the web will contain a stress gradient. The possibility of members being designed for an elastic or a plastic state, including the use of a full plastic design for the complete structure, also affects section classification. Various forms of instability of the beam as a whole or of parts subject to locally high stresses, such as the web over a support, also require attention. Finally certain forms of construction may lend themselves to the appearance of unacceptable vibrations; although this is likely to be affected by the choice of beams, its coverage is left to Chapter 20 on floors.

## 16.2 Cross-section classification and moment capacity, $M_c$

The possible influences of local buckling on the ability of a particular cross-section to attain, and where appropriate also to maintain, a certain level of moment are discussed in general terms in Chapter 13. In particular, section 13.2 covers the influence of flange ( $b/T$ ) and web ( $d/t$ ) slenderness on moment–rotation behaviour (Fig. 13.4) and moment capacity (Fig. 13.5). When designing beams it is usually sufficient to consider the web and the compression flange separately using the appropriate sets of limits.<sup>1</sup>

In building design when using hot-rolled sections, for which relevant properties are tabulated,<sup>2</sup> it will normally be sufficient to ascertain a section's classification and moment capacity simply by referring to the appropriate table. An example illustrates the point.

### Example

Using BS 5950: Part 1<sup>1</sup> determine the section classification and moment capacity for a 533 × 210 UB82 when used as a beam in (1) grade 43 steel and (2) grade 50 steel.

- (1) From Reference 2, p. 129, section is 'plastic' and  $M_{cx} = 566 \text{ kN m}$   
 Alternatively, from Reference 2, p. 26,  $b/T = 7.91$ ,  $d/t = 49.6$   
 Since  $T = 13.2 \text{ mm}$  from Reference 1, Table 6,  $p_y = 275 \text{ N/mm}^2$  and  $\epsilon = (275/p_y)^{1/2} = 1.0$   
 From Reference 1, Table 7, limits for plastic section are  $b/t \leq 8.5\epsilon$ ,  $d/t \leq 79\epsilon$ ; actual  $b/t$  and  $d/t$  are within these limits and section is plastic.  
 From Reference 1, clause 4.2.5,  $M_c = p_y S$   

$$= 275 \times 2060 \times 10^{-3}$$

$$= 566.5 \text{ kN m}$$
- (2) From Reference 2, p. 303, section is compact and  $M_{cx} = 731 \text{ kN m}$   
 Alternatively, from Reference 2, p. 26,  $b/T = 7.91$ ,  $d/t = 49.6$   
 Since  $T = 13.2 \text{ mm}$  from Reference 1, Table 6,  $p_y = 355 \text{ N/mm}^2$  and  $\epsilon = (275/p_y)^{1/2} = 0.88$   
 From Reference 1, Table 7, limits for plastic section are  $b/T \leq 8.5\epsilon$ ,  $d/t = 79\epsilon$ , which give  $b/T \leq 7.48$ ,  $d/t \leq 70$ ; actual  $b/T$  of 7.91 exceeds 7.48 so check compact limits of  $b/T \leq 9.5\epsilon$ , which gives  $b/T \leq 8.36$ ; actual  $b/T$  of 7.91 meets this and section is compact.  
 From Reference 1, clause 4.2.5,  $M_c = p_y S$   

$$= 355 \times 2060 \times 10^{-3}$$

$$= 731.3 \text{ kN m}$$

Thus whichever grade of steel is being used, the moment capacity,  $M_c$ , will be the maximum attainable value corresponding to the section's full plastic moment capacity,  $M_p$ . Provided that grade 43 material is used, the beam is capable of redistributing moments, since the plastic cross section behaves as illustrated in Fig. 13.4(a) and so could be used in a plastically designed frame. Use of the higher strength grade 50 material, while not affecting the beam's ability to attain  $M_p$ , precludes the use of plastic design since redistribution of moments cannot occur due to the lack of rotation capacity implied by the behaviour illustrated in Fig. 13.4(b). For a continuous structure designed on the basis of elastic analysis to determine the distribution of internal forces and moments or for simple construction, the question of rotation capacity is not relevant and in both cases moment capacity should be taken as  $M_p$ . The fact that the section is plastic for grade 43 material is then of no particular relevance; a more appropriate classification would be to regard the section as compact or better.

Inspection of the relevant tables in Reference 2 shows that when used as beams:

*Grade 43 steel*

all but 2 UBs are plastic

all but 6 UCs are plastic

of these 6, 3 are compact and 3 are semi-compact

*Grade 50 steel*

all but 11 UBs are plastic

of these 11, 8 are compact and 3 are semi-compact

all but 10 UCs are plastic

of these 10, 4 are compact and 6 are semi-compact

In those cases of semi-compact sections, moment capacities based on  $M_y$  are listed. The full list of non-plastic beam sections is given as Table 16.2.

When using fabricated sections individual checks on the web and compression flange using the actual dimensions of the trial section must be made. It normally proves much simpler if proportions are selected so as to ensure that the section is compact or better since the resulting calculations need not then involve the various complications associated with the use of non-compact sections. This point is particularly noticeable when designing bridge beams to BS 5400: Part 3. When slender sections are used the amount of calculation increases considerably due to the need to consider loss of effectiveness of some parts of the cross section due to local buckling when determining  $M_c$ . Probably the most frequent use of slender sections involves cold-formed shapes used for example as roof purlins. Because of their proprietary nature, the manufacturers normally provide design information, much of it based on physical testing, listing such properties as moment capacity. In the absence of design information, reference should be made to Part 5 of BS 5950 for suitable calculation methods.

**Table 16.2** Non-plastic UBs and UCs in bending

|          | Compact  | Semi-compact   |
|----------|--|--|
| Grade 43 |  |  |
| UB       | 356 × 171 × 44<br>203 × 133 × 25   |  |
| UC       | 356 × 368 × 153<br>254 × 254 × 73<br>203 × 203 × 46  | 356 × 368 × 129<br>305 × 305 × 97<br>152 × 152 × 23  |
| Grade 50 |  |  |
| UB       | 838 × 292 × 176<br>686 × 254 × 125<br>610 × 305 × 149<br>610 × 229 × 101<br>533 × 210 × 82<br>406 × 178 × 54<br>406 × 140 × 38<br>305 × 165 × 40 | 356 × 171 × 45<br>254 × 146 × 31<br>203 × 133 × 25   |
| UC       | 356 × 368 × 177<br>305 × 305 × 118<br>203 × 203 × 52<br>152 × 152 × 30   | 356 × 368 × 153<br>356 × 368 × 129<br>305 × 305 × 97<br>254 × 254 × 73<br>203 × 203 × 46<br>152 × 152 × 23 |

Although the part of the web between the flange and the horizontal edge of the castellation in a castellated beam frequently exceeds the compact limit for an outstand, sufficient test data exist to show that this does not appear to influence the moment capacity of such sections. Section classification should therefore be made in the same way as for solid web beams, the value of  $M_c$  being obtained using the net modulus value for the section at the centre of a castellation.

### 16.3 Basic design

One (or more) of a number of distinct limiting conditions may, in theory, control the design of a particular beam as indicated in Table 16.3, but in any particular practical case only a few of them are likely to require full checks. It is therefore convenient to consider the various possibilities in turn, noting the conditions under which each is likely to be important. For convenience the various phenomena are first considered principally within the context of using standard hot-rolled sections i.e. UBs, UCs, RSJs and channels; other types of cross-section are covered in the later parts of this chapter.

**Table 16.3** Limiting conditions for beam design

| Ultimate   | Serviceability  |
|--|---|
| Moment capacity, $M_e$ (including influence of local buckling) | Deflections due to bending (and shear if appropriate) |
| Shear capacity, $P_v$  | Twist due to torsion                                  |
| Lateral-torsional buckling, $M_b$                              | Vibration   |
| Web buckling, $P_w$  |   |
| Web bearing, $P_{yw}$  |   |
| Moment-shear interaction                                       |   |
| Torsional capacity, $M_T$                                      |   |
| Bending-torsion interaction                                    |   |

### 16.3.1 Moment capacity, $M_c$

The most basic design requirement for a beam is the provision of adequate in-plane bending strength. This is provided by ensuring that  $M_c$  for the selected section exceeds the maximum moment produced by the factored loading. Determination of  $M_c$ , which is linked to section classification, is fully covered in section 16.2.

For a statically determinate structural arrangement, simple considerations of statics provide the moment levels produced by the applied loads against which  $M_c$  must be checked. For indeterminate arrangements, a suitable method of elastic analysis such as moment distribution or slope deflection is required. The justification for using an elastically obtained distribution of moments with, in the case of compact or plastic cross-sections, a plastic cross-sectional resistance has been fully discussed by Johnson and Buckby.<sup>3</sup>

### 16.3.2 Effect of shear

Only in cases of high coincident shear and moment, found for example at the internal supports of continuous beams, is the effect of shear likely to have a significant influence on the design of beams.

Shear capacity  $P_v$  is normally calculated as the product of a shear strength  $p_v$ , often taken for convenience as  $0.6p_y$  which is close to the yield stress of steel in shear of  $1/\sqrt{3}$  of the uniaxial tensile yield stress, and an appropriate shear area  $A_v$ . The process approximates the actual distribution of shear stress in a beam web as well as assuming some degree of plasticity. While suitable for rolled sections, it may not therefore be applicable to plate girders. An alternative design approach, more suited to webs containing large holes or having variations in thickness, is to work from first principles and to limit the maximum shear stress to

a suitable value; BS 5950: Part 1 uses  $0.7p_y$ . In cases where  $d/t > 63$ , shear buckling limits the effectiveness of the web and reference to Chapter 17 should be made for methods of determining the reduced capacity.

In principle the presence of shear in a section reduces its moment capacity. In practice the reduction may be regarded as negligibly small up to quite large fractions of the shear capacity  $P_v$ . For example, BS 5950: Part 1 only requires a reduction in  $M_c$  for plastic or compact sections when the applied shear exceeds  $0.6P_v$  and permits the full value of  $M_c$  to be used for all cases of semi-compact or slender sections.

Figure 16.2 illustrates the application of the BS 5950: Part 1 rule for plastic or compact sections to a typical UB and UC having approximately equal values of plastic section modulus  $S_x$ . Evaluation of the formula in cases where  $F_v/P_v > 0.6$ , first requires that the value of  $S_v$ , the plastic modulus of the shear area  $A_v$  (equal to  $tD$  in this case), be determined. This is readily obtained from the tabulated values of  $S$  for rectangles given in Reference 2 corresponding to a linear reduction from  $S_x$  to  $(S_x - S_v)$ .

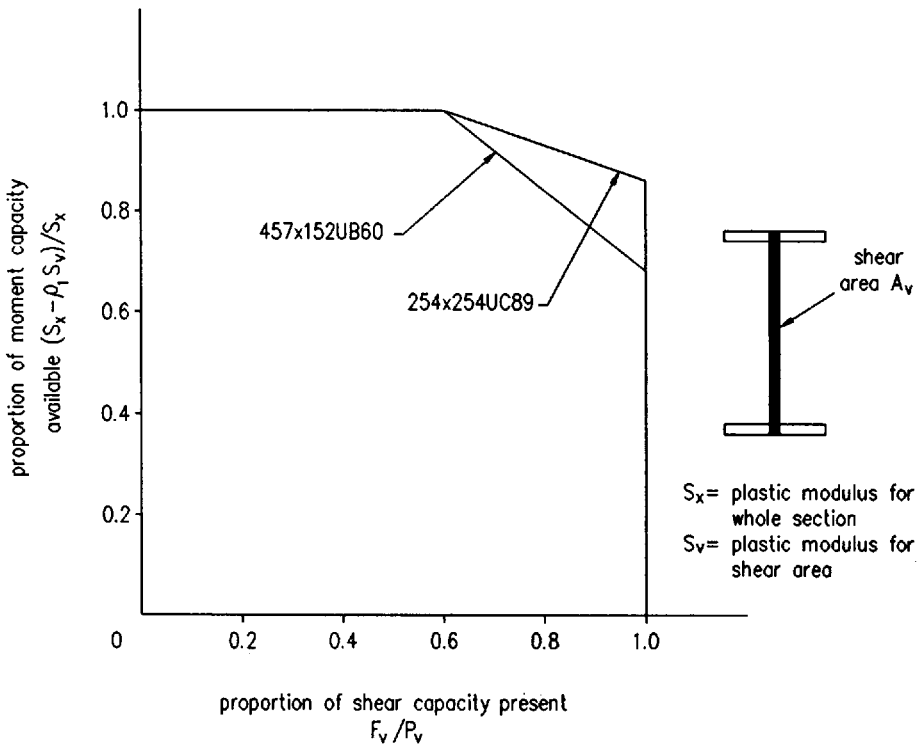


Fig. 16.2 Moment–shear interaction for plastic or compact sections to BS 5950: Part 1



### 16.3.3 Deflection

When designing according to limit states principles it is customary to check that deflections at working load levels will not be such as to impair the proper function of the structure. For beams, examples of potentially undesirable consequences of excessive serviceability deflections include:

- cracking of plaster ceilings
- allowing crane rails to become misaligned
- causing difficulty in opening large doors.

Although earlier codes of practice specified limits for working load deflections, the tendency with more recent documents<sup>1</sup> is to draw attention to the need for deflection checks and to provide advisory limits to be used only when more specific guidance is not available. Table 5 of BS 5950: Part 1 gives 'recommended limitations' for certain types of beams and crane gantry girders and states that 'Circumstances may arise where greater or lesser values would be more appropriate.' Not surprisingly surveys of current practice<sup>4</sup> reveal large variations in what is considered appropriate for different circumstances.

When checking deflections of steel structures under serviceability loading, the central deflection  $\Delta_{\max}$  of a uniformly-loaded simply-supported beam, assuming linear-elastic behaviour, is given by

$$\Delta_{\max} = \frac{5}{384} \frac{WL^3}{EI} 10^{12}(\text{mm}) \quad (16.1)$$

in which  $W$  = total load (kN)

$E$  = Young's modulus (N/mm<sup>2</sup>)

$I$  = second moment of area (mm<sup>4</sup>)

$L$  = span (m).

If  $\Delta_{\max}$  is to be limited to a fraction of  $L$ , Equation (16.1) may be rearranged to give

$$I_{\text{reqd}} = 0.62 \times 10^{-2} \alpha WL^2 \quad (16.2)$$

in which  $\alpha$  defines the deflection limit as

$$\Delta_{\max} = L/\alpha$$

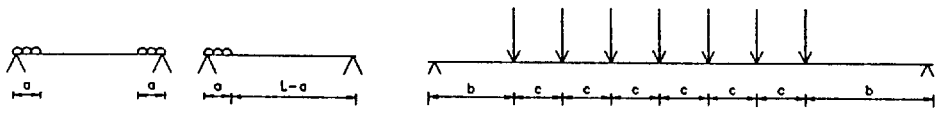
and  $I_{\text{reqd}}$  is now in cm<sup>4</sup>.

Writing  $I_{\text{reqd}} = KWL^2$ , Table 16.4 gives values of  $K$  for a range of values of  $\alpha$ .

**Table 16.4** Minimum  $I$  values for uniformly-loaded simply-supported beams for various deflection limits

|          |      |      |      |      |      |      |      |      |      |      |
|----------|------|------|------|------|------|------|------|------|------|------|
| $\alpha$ | 200  | 240  | 250  | 325  | 360  | 400  | 500  | 600  | 750  | 1000 |
| $K$      | 1.24 | 1.49 | 1.55 | 2.02 | 2.23 | 2.48 | 3.10 | 3.72 | 4.65 | 6.20 |

**Table 16.5** Equivalent UDL coefficients



| $a/L$ | $K_{\Delta}$ | No. of equal loads | $b/L$ | $c/L$ | $K$  |
|-------|--------------|--------------------|-------|-------|------|
| 0.5   | 1.0          | 2                  | 0.2   | 0.6   | 0.91 |
| 0.4   | 0.86         |                    | 0.25  | 0.5   | 1.10 |
|       |              |                    | 0.333 | 0.333 | 1.3  |
| 0.375 | 0.82         | 3                  | 0.167 | 0.333 | 1.05 |
|       |              |                    | 0.2   | 0.3   | 1.14 |
| 0.333 | 0.74         |                    | 0.25  | 0.25  | 1.27 |
| 0.3   | 0.68         | 4                  | 0.125 | 0.25  | 1.03 |
|       |              |                    | 0.2   | 0.2   | 1.21 |
| 0.25  | 0.58         | 5                  | 0.1   | 0.2   | 1.02 |
|       |              |                    | 0.167 | 0.167 | 1.17 |
| 0.2   | 0.47         | 6                  | 0.083 | 0.167 | 1.01 |
|       |              |                    | 0.143 | 0.143 | 1.15 |
| 0.1   | 0.24         | 7                  | 0.071 | 0.143 | 1.01 |
|       |              |                    | 0.125 | 0.125 | 1.12 |
|       |              | 8                  | 0.063 | 0.125 | 1.01 |
|       |              |                    | 0.111 | 0.111 | 1.11 |



$$K_{\Delta} = 1.6 \frac{a}{L} \left[ 3 - 4 \left( \frac{a}{L} \right)^2 \right]$$

|              |      |      |      |      |      |      |      |      |      |      |      |
|--------------|------|------|------|------|------|------|------|------|------|------|------|
| $a/L$        | 0.01 | 0.05 | 0.1  | 0.15 | 0.2  | 0.25 | 0.3  | 0.35 | 0.4  | 0.45 | 0.5  |
| $K_{\Delta}$ | 0.05 | 0.24 | 0.47 | 0.70 | 0.91 | 1.10 | 1.27 | 1.41 | 1.51 | 1.58 | 1.60 |

Since deflection checks are essentially of the ‘not greater than’ type, some degree of approximation normally is acceptable, particularly if the calculations are reduced as a result. Converting complex load arrangements to a roughly equivalent UDL permits Table 16.4 to be used for a wide range of practical situations. Table 16.5 gives values of the coefficient  $K$  by which the actual load arrangement shown should be multiplied in order to obtain an approximately equal maximum deflection.

Tables of deflections for a number of standard cases are provided in the Appendix.

### 16.3.4 Torsion

Beams subjected to loads which do not act through the point on the cross-section known as the shear centre normally suffer some twisting. Methods for locating the shear centre for a variety of sectional shapes are given in Reference 5. For doubly symmetrical sections such as UBs and UCs it coincides with the centroid while for channels it is situated on the opposite side of the web from the centroid; for rolled channels its location is included in the tables of Reference 2. Figure 16.3 illustrates its position for a number of standard cases.

The effects of torsional loading may often be minimized by careful detailing, particularly when considering how loads are transferred between members. Proper attention to detail can frequently lead to arrangements in which the load transfer is organized in such a way that twisting should not occur.<sup>5</sup> Whenever possible this approach should be followed as the open sections normally used as beams are inherently weak in resisting torsion. In circumstances where beams are required to withstand significant torsional loading, consideration should be given to the use of a torsionally more efficient shape such as a structural hollow section.

### 16.3.5 Local effects on webs

At points within the length of a beam where vertical loads act, the web is subject to concentrations of stresses, additional to those produced by overall bending. Failure by buckling, rather in the manner of a vertical strut, or by the development of unacceptably high bearing stresses in the relatively thin web material immediately adjacent to the flange, is a possibility. Methods for assessing the likelihood of both types of failure are given in BS 5950: Part 1 and tabulated data to assist in the evaluation of the formulae required are provided for rolled sections in Reference 2. The parallel approach for cold-formed sections is discussed in section 16.7.

In cases where the web is found to be incapable of resisting the required level of load, additional strength may be provided through the use of stiffeners. The design of load-carrying stiffeners (to resist web buckling) and bearing stiffeners is covered in both BS 5950 and BS 5400. However, web stiffeners may be required to resist shear buckling, to provide torsional support at bearings or for other reasons; a full treatment of their design is provided in Chapter 17.

### 16.3.6 Lateral–torsional buckling

Beams for which none of the conditions listed in Table 16.6 are met (explanation of these requirements is delayed until section 16.3.7 so that the basic ideas and parameters governing lateral–torsional buckling may be presented first) are liable to have their load-carrying capacity governed by the type of failure illustrated in

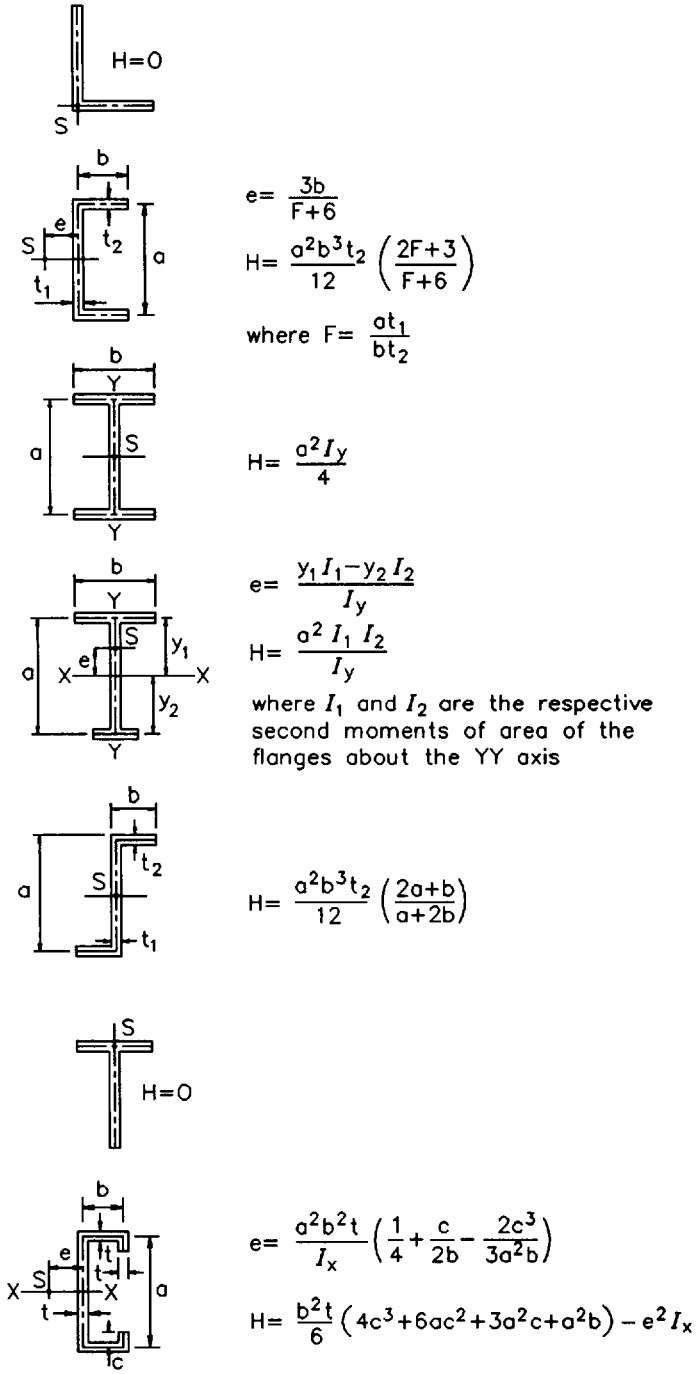


Fig. 16.3 Location of shear centre for standard sections ( $H$  is warping constant)

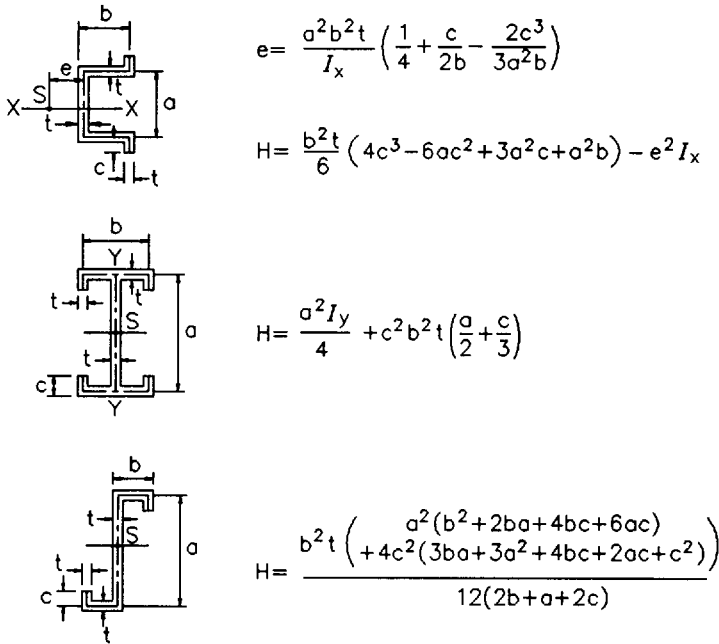


Fig. 16.3 (continued)

**Table 16.6** Types of beam not susceptible to lateral–torsional buckling

|   |
|---|
| loading produces bending about the minor axis                     |
| beam provided with closely spaced or continuous lateral restraint |
| closed section  |

Fig. 16.4. Lateral–torsional instability is normally associated with beams subject to vertical loading buckling out of the plane of the applied loads by deflecting sideways and twisting; behaviour analogous to the flexural buckling of struts. The presence of both lateral and torsional deformations does cause both the governing mathematics and the resulting design treatment to be rather more complex.

The design of a beam taking into account lateral–torsional buckling consists essentially of assessing the maximum moment that can safely be carried from a knowledge of the section’s material and geometrical properties, the support conditions provided and the arrangement of the applied loading. Codes of practice, such as BS 5400: Part 3, BS 5950: Parts 1 and 5, include detailed guidance on the

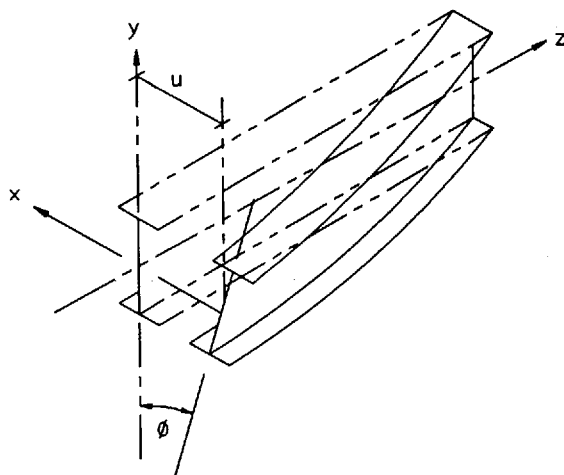


Fig. 16.4 Lateral-torsional buckling

subject. Essentially the basic steps required to check a trial section (using BS 5950: Part 1 for a UB as an example) are:

- (1) assess the beam's effective length  $L_E$  from a knowledge of the support conditions provided (clause 4.3.5 and 4.3.6)
- (2) determine beam slenderness  $\lambda_{LT}$  using the geometrical parameters  $u$  (tabulated in Reference 2),  $L_E/r_y$ ,  $v$  (Table 14 of BS 5950: Part 1) using values of  $x$  (tabulated in Reference 2), and  $n$  (clause 4.3.6)
- (3) obtain corresponding bending strength  $p_b$  (Table 11)
- (4) calculate buckling resistance moment  $M_b = p_b S_x$ , where  $S_x$  is the plastic section modulus (tabulated in Reference 2).

The central feature in the above process is the determination of a measure of the beam's lateral-torsional buckling strength ( $p_b$ ) in terms of a parameter ( $\lambda_{LT}$ ) which represents those factors which control this strength. Modifications to the basic process permit the method to be used for unequal flanged sections including tees, fabricated I's for which the section properties must be calculated, sections containing slender plate elements, members with properties that vary along their length, closed sections and flats. Various techniques for allowing for the form of the applied loading are also possible; some care is required in their use.

The relationship between  $p_b$  and  $\lambda_{LT}$  of BS 5950: Part 1 (and between  $\sigma_{li}/\sigma_{yc}$  and  $\lambda_{LT} \sqrt{(\sigma_{yc}/355)}$  in BS 5400: Part 3) assumes the beam between lateral restraints to be subject to uniform moment. Other patterns, such as a linear moment gradient reducing from a maximum at one end or the parabolic distribution produced by a uniform load, are generally less severe in terms of their effect on lateral stability; a given beam is likely to be able to withstand a larger peak

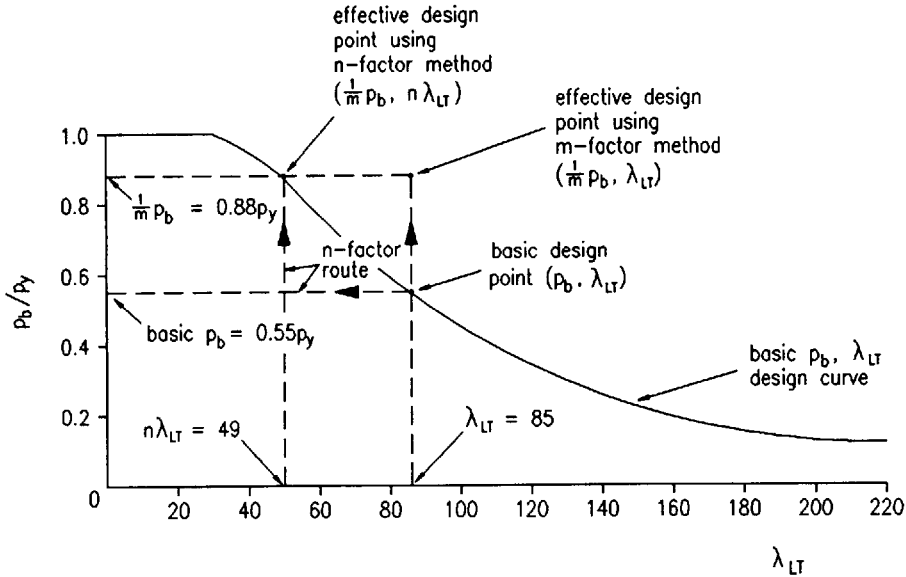


Fig. 16.5 Design modifications using *m*-factor or *n*-factor methods

moment before becoming laterally unstable. One means of allowing for this in design is to adjust the beam's slenderness by a factor (*n* in BS 5950: Part 1), the value of which has been selected so as to ensure that the resulting value of  $p_b$  correctly reflects the enhanced strength due to the non-uniform moment loading. An alternative approach consists of basing  $\lambda_{LT}$  on the geometrical and support conditions alone but making allowance for the beneficial effects of non-uniform moment by comparing the resulting value of  $M_b$  with a suitably adjusted value of design moment  $\bar{M}$ .  $\bar{M}$  is taken as a factor *m* times the maximum moment within the beam  $M_{max}$ ;  $m = 1.0$  for uniform moment and  $m < 1.0$  for non-uniform moment. Provided that suitably chosen values of *m* and *n* are used, both methods can be made to yield identical results; the difference arises simply in the way in which the correction is made, whether on the slenderness axis of the  $p_b$  versus  $\lambda_{LT}$  relationship for the *n*-factor method or on the strength axis for the *m*-factor method. Figure 16.5 illustrates both concepts, although for the purpose of the figure the *m*-factor method has been shown as an enhancement of  $p_b$  by  $1/m$  rather than a reduction in the requirement of checking  $M_b$  against  $\bar{M} = m M_{max}$ . However, BS 5950: Part 1 restricts the use of the *m*-factor method to beams loaded only at points of effective lateral restraint having moment diagrams of the sort shown as Fig. 16.6(a), while BS 5400: Part 3 only includes the *n*-factor method. Even a modest allowance for beam self-weight causes the moment diagram of Fig. 16.6(a) to alter to that of Fig. 16.6(b) and so apparently contravenes the requirement concerning loading between points of effective lateral restraint.

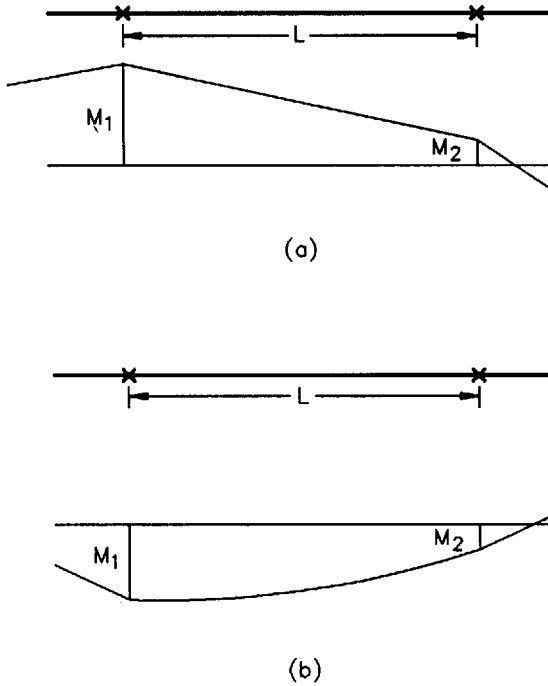


Fig. 16.6 Beam segment between points of effective lateral restraint (a) subject to moment gradient, (b) subject to moment gradient plus a modest UDL

Some degree of judgement is therefore required and it is suggested that where the additional parabolic component of the moment diagram does not exceed 15% of the larger end moment  $M_1$  the  $m$ -factor method may be used. As a final caution on the use of  $m$  and  $n$  factors, it is always safe to set  $m = n = 1$  basing design on the uniform moment case. There is no situation for which both  $m \neq 1$  and  $n \neq 1$  should be used together; only one method should be used for any situation.

When the  $m$ -factor method is used the buckling check is conducted in terms of a moment  $\bar{M}$  less than the maximum moment in the beam segment  $M_{\max}$ , then a separate check that the capacity of the beam cross-section  $M_c$  is at least equal to  $M_{\max}$  must also be made. In cases where  $\bar{M}$  is taken as  $M_{\max}$ , then the buckling check will be more severe than (or in the case of a stocky beam for which  $M_b = M_c$ , identical to) the cross-section capacity check.

Allowance for non-uniform moment loading on cantilevers is normally treated somewhat differently. For example, the set of effective length factors given in Table 10 of Reference 1 includes allowances for the variation from the arrangement used as the basis for the strength-slenderness relationship due to both the lateral support conditions and the form of the applied loading. When a cantilever is subdivided by one or more intermediate lateral restraints positioned between its root and tip, then segments other than the tip segment should be treated as



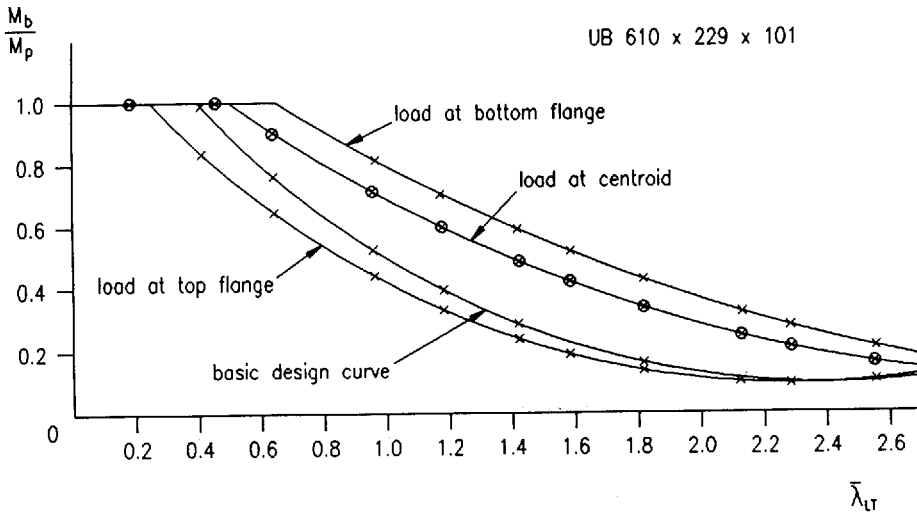


Fig. 16.7 Lateral-torsional buckling of a tip-loaded cantilever

ordinary beam segments when assessing lateral-torsional buckling strength. Similarly a cantilever subject to an end moment such as horizontal wind load acting on a façade, should be regarded as an ordinary beam since it does not have the benefit of non-uniform moment loading.

For more complex arrangements that cannot reasonably be approximated by one of the standard cases covered by correction factors, codes normally permit the direct use of the elastic critical moment  $M_E$ . Values of  $M_E$  may conveniently be obtained from summaries of research data.<sup>6</sup> For example, BS 5950: Part 1 permits  $\lambda_{LT}$  to be calculated from

$$\lambda_{LT} = \sqrt{(\pi^2 E/p_y)} \sqrt{(M_p/M_E)} \tag{16.3}$$

As an example of the use of this approach Fig. 16.7 shows how significantly higher load-carrying capacities may be obtained for a cantilever with a tip load applied to its bottom flange, a case not specifically covered by BS 5950: Part 1.

### 16.3.7 Fully restrained beams

The design of beams is considerably simplified if lateral-torsional buckling effects do not have to be considered explicitly; a situation which will occur if one or more of the conditions of Table 16.6 are met.

In these cases the beam's buckling resistance moment  $M_b$  may be taken as its moment capacity  $M_c$  and, in the absence of any reductions in  $M_c$  due to local

buckling, high shear or torsion, it should be designed for its full in-plane bending strength. Certain of the conditions corresponding to the case where a beam may be regarded as ‘fully restrained’ are virtually self-evident but others require either judgement or calculation.

Lateral-torsional buckling cannot occur in beams loaded in their weaker principal plane; under the action of increasing load they will collapse simply by plastic action and excessive in-plane deformation. Much the same is true for rectangular box sections even when bent about their strong axis. Figure 16.8,

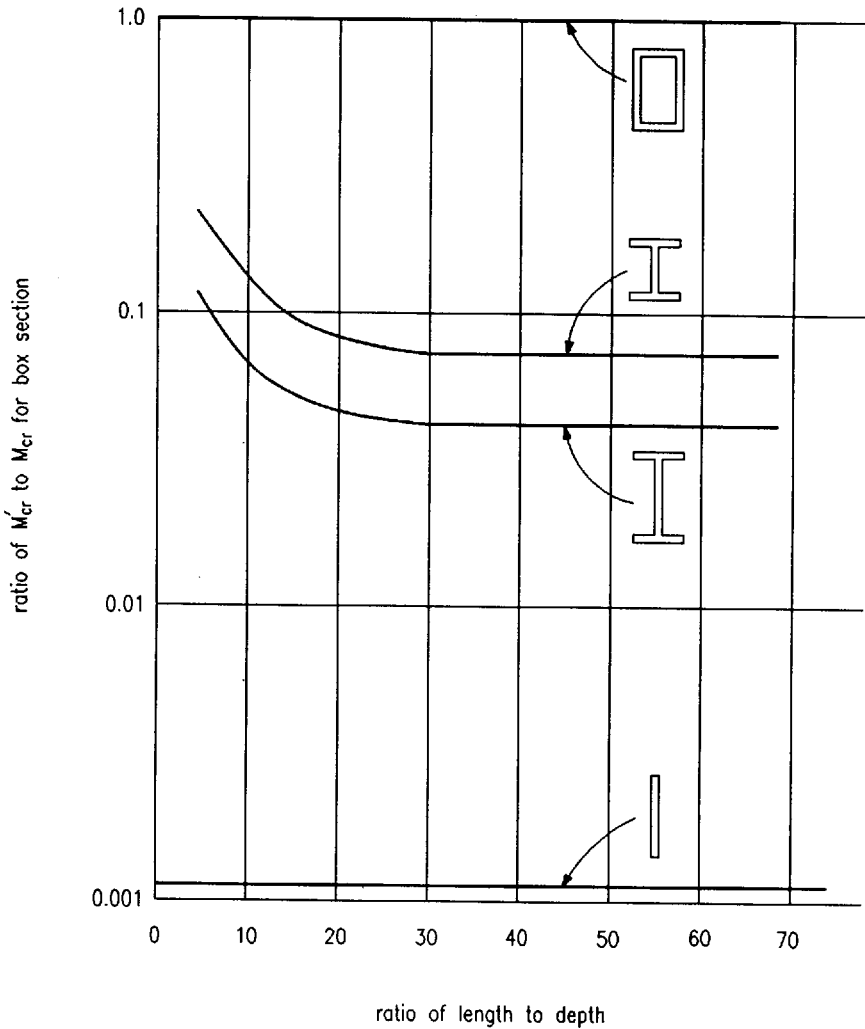


Fig. 16.8 Effect of type of cross-section on theoretical elastic critical moment

which is based on elastic critical load theory analogous to the Euler buckling of struts, shows that typical RHS beams will be of the order of ten times more stable than UB or UC sections of the same area. The limits on  $\lambda$  below which buckling will not affect  $M_b$  of Table 38 of BS 5950: Part 1, are sufficiently high ( $\lambda = 350, 225$  and  $170$  for  $D/B$  ratios of 2, 3 and 4, and  $p_y = 275 \text{ N/mm}^2$ ) that only in very rare cases will lateral–torsional buckling be a design consideration.

Situations in which the form of construction employed automatically provides some degree of lateral restraint or for which a bracing system is to be used to enhance a beam's strength require careful consideration. The fundamental requirements of any form of restraint if it is to be capable of increasing the strength of the main member is that it limits the buckling type deformations. An appreciation of exactly how the main member would buckle if unbraced is a prerequisite for the provision of an effective system. Since lateral–torsional buckling involves both lateral deflection and twist as shown in Fig. 16.4, either or both deformations may be addressed. Clauses 4.3.2 and 4.3.3 of BS 5950: Part 1 set out the principles governing the action of bracing designed to provide either lateral restraint or torsional restraint. In common with most approaches to bracing design these clauses assume that the restraints will effectively prevent movement at the braced cross-sections, thereby acting as if they were rigid supports. In practice, bracing will possess a finite stiffness. A more fundamental discussion of the topic, which explains the exact nature of bracing stiffness and bracing strength may be found in References 7 and 8. Noticeably absent from the code clauses is a quantitative definition of 'adequate stiffness', although it has subsequently been suggested that a bracing system that is 25 times stiffer than the braced beam would meet this requirement. Examination of Reference 7 shows that while such a check does cover the majority of cases, it is still possible to provide arrangements in which even much stiffer bracing cannot supply full restraint.

## 16.4 Lateral bracing

For design to BS 5950: Part 1, unless the engineer is prepared to supplement the code rules with some degree of working from first principles, only restraints capable of acting as rigid supports are acceptable. Despite the absence of a specific stiffness requirement, adherence to the strength requirement together with an awareness that adequate stiffness is also necessary, avoiding obviously very flexible yet strong arrangements, should lead to satisfactory designs. Doubtful cases will merit examination in a more fundamental way.<sup>7,8</sup> Where properly designed restraint systems are used the limits on  $\lambda_{L,T}$  for  $M_b = M_c$  (or more correctly  $p_b = p_y$ ) are given in Table 16.7.

For beams in plastically-designed structures it is vital that premature failure due to plastic lateral–torsional buckling does not impair the formation of the full plastic collapse mechanism and the attainment of the plastic collapse load. Clause 5.3.5 provides a basic limit on  $L/r_y$  to ensure satisfactory behaviour; it is not

**Table 16.7** Maximum values of  $\lambda_{LT}$  for which  $\rho_b = \rho_y$  for rolled sections

| $\rho_y$ (N/mm <sup>2</sup> ) | Value of $\lambda_{LT}$<br>up to which $\rho_b = \rho_y$ |
|-------------------------------|--|
| 245                           | 37   |
| 265                           | 35   |
| 275                           | 34   |
| 325                           | 32   |
| 340                           | 31   |
| 365                           | 30   |
| 415                           | 28   |
| 430                           | 27   |
| 450                           | 26   |

necessarily compatible with the elastic design rules of section 4 of the code since acceptable behaviour can include the provision of adequate rotation capacity at moments slightly below  $M_p$ .

The expression of clause 5.3.5 of BS 5950: Part 1,

$$L_m \leq \frac{38r_y}{[f_c/130 + (p_y/275)^2 (x/36)^2]^{\frac{1}{2}}} \quad (16.4)$$

makes no allowance for either of two potentially beneficial effects:

- (1) moment gradient
- (2) restraint against lateral deflection provided by secondary structural members attached to one flange as by the purlins on the top flange of a portal frame rafter.

The first effect may be included in Equation (16.4) by adding the correction term of Brown,<sup>9</sup> the basis of which is the original work on plastic instability of Horne.<sup>10</sup> A method of allowing for both effects when the beam segment being checked is either elastic or partially plastic is given in Appendix G of BS 5950: Part 1; alternatively the effect of intermittent tension flange restraint alone may be allowed for by replacing  $L_m$  with an enhanced value  $L_t$  obtained from clause 5.5.3.5 of BS 5950: Part 1.

In both cases the presence of a change in cross-section, for example, as produced by the type of haunch usually used in portal frame construction, may be allowed for. When the restraint is such that lateral deflection of the beam's compression flange is prevented at intervals, then Equation (16.4) applies between the points of effective lateral restraint. A discussion of the application of this and other approaches for checking the stability of both rafters and columns in portal frames designed according to the principles of either elastic or plastic theory is given in section 18.7.

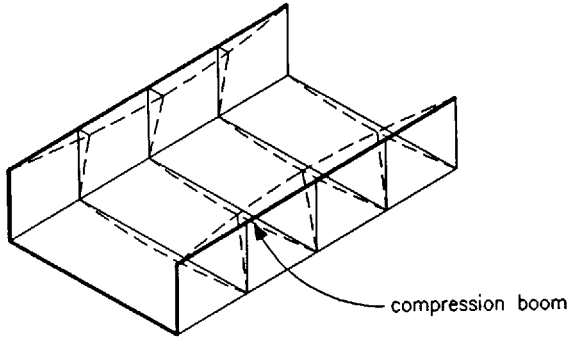


Fig. 16.9 Buckling of main beams of half-through girder

### 16.5 Bracing action in bridges – U-frame design

The main longitudinal beams in several forms of bridge construction will, by virtue of the structural arrangement employed, receive a significant measure of restraint against lateral–torsional buckling by a device commonly referred to as ‘U-frame action’. Figure 16.9 illustrates the original concept based on the half-through girder form of construction. (See Chapter 4 for a discussion of different bridge types.) In a simply-supported span, the top (compression) flanges of the main girders, although laterally unbraced in the sense that no bracing may be attached directly to them, cannot buckle freely in the manner of Fig. 16.4 since their lower flanges are restrained by the deck. Buckling must therefore involve some distortion of the girder web into the mode given in Fig. 16.9. An approximate way of dealing with this is to regard each longitudinal girder as a truss in which the tension chord is fully laterally restrained and the web members, by virtue of their lateral bending stiffness, inhibit lateral movement of the top chord. It is then only a small step to regard this top chord as a strut provided with a series of intermediate elastic spring restraints against buckling in the horizontal plane. The stiffness of each support corresponds to the stiffness of the U-frame comprising the two vertical web stiffeners and the cross-girder and deck shown in Fig. 16.10.

The elastic critical load for the top chord is:

$$P_{cr} = \pi^2 EI / L_E^2 \tag{16.5}$$

in which  $L_E$  is the effective length of the strut.

If the strut receives continuous support of stiffness  $(1/\delta L_u)$  per unit length, in which  $L_u$  is the distance between U-frames and buckles in a single half-wave, this load will be increased to:

$$P_{cr} = (\pi^2 EI / L^2) + (L^2 / \pi^2 \delta L_u) \tag{16.6}$$

which gives a minimum value when

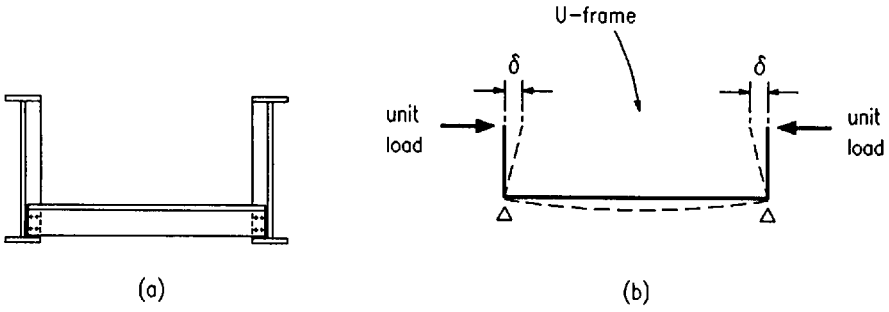


Fig. 16.10 U-frame restraint action. (a) Components of U-frame. (b) U-frame elastic support stiffness.

$$L = \pi(EI\delta L_u)^{0.25} \tag{16.7}$$

giving

$$P_{cr} = 2(EI/\delta L_u)^{0.5} \tag{16.8}$$

or

$$L_E = (\pi/\sqrt{2}) (EI\delta L_u)^{0.25} \tag{16.9}$$

In clause 9.6.5 of BS 5400: Part 3, this is rounded up to

$$L_E = 2.5(EI_c L_u \delta)^{0.25}$$

If lateral movement at the ends of the girder is not prevented by sufficiently stiff end U-frames as shown in Fig. 16.11, then the effective length is

$$L_E = \pi(EI \delta L_u)^{0.25} \tag{16.10}$$

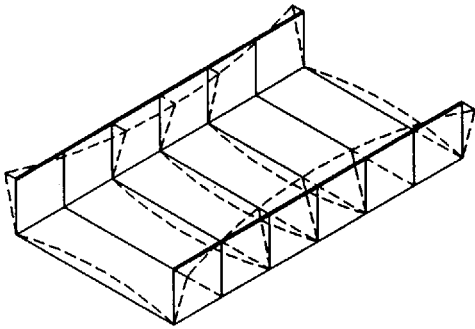


Fig. 16.11 Buckling mode for half-through construction with flexible end frames

In both Equations (16.9) and (16.10) a coefficient  $K_3$  may be inserted, with values less than unity being adopted if some resistance to rotational restraint in plan of the top flange is present.

For unstiffened girders a similar approach is possible with the effective U-frame now comprising a unit length of girder web plus the cross-member. In all cases the assessment of U-frame stiffness via the  $\delta$  parameter is based on summing the deflections due to bending of the horizontal and vertical components, including any flexibility of the upright to cross-frame connections. Clauses 9.6.5 and 9.6.6 deal respectively with the cases where actual vertical members are either present or absent.

Because the U-frames are required to resist the buckling deformations, they will attract forces which may be estimated as the product of the additional deformation, as a proportion of the initial lateral deformation of the top chord, and the U-frame stiffness as

$$F_u = \left( \frac{1}{1 - \sigma_{fc}/\sigma_{ci}} - 1 \right) \frac{L_E}{667\delta} \quad \text{or} \quad F_u = \left( \frac{\sigma_{fc}}{\sigma_{ci} - \sigma_{fc}} \right) \frac{L_E}{667\delta} \quad (16.11)$$

in which the assumed initial bow over an effective length of flange ( $L_E$ ) has been taken as  $L_E/667$  and  $1/(1 - \sigma_{fc}/\sigma_{ci})$ , is the amplification which depends in a non-linear fashion on the level of stress  $\sigma_{fc}$  in the flange.

For a frame spacing  $L_u$  and a flange critical stress  $\sigma_{ci}$  corresponding to a force level of  $\pi^2 EI_c/L_u^2$ , the maximum possible value of  $F_u$  given in clause 9.12.2 of BS 5400: Part 3 is

$$F_u = \left( \frac{\sigma_{fc}}{\sigma_{ci} - \sigma_{fc}} \right) EI_c/16.7 L_u^2 \quad (16.12)$$

Additional forces in the web stiffeners are produced by rotation  $\theta$  of the ends of the cross beam to give (clause 9.12.2.3 of BS 5400: Part 3):

$$F_c = 3EI_1 \theta/d_2^2 \quad (16.13)$$

However, the code rule assumes that the top flange is restrained in position by neighbouring unloaded U-frames; this is conservative in regions away from the stiff end frames and for approximately uniform bridge loadings. One possible approach consists of redefining  $\theta$  as the rotation of the base of the stiffener, allowing for fixity reducing the cross-beam rotation and arriving at the expression for  $F_c$  of

$$F_c = \frac{\theta_o}{d_2} \left( \frac{1}{d_1/3EI_1 + B/4EI_2 + f} \right) \quad (16.14)$$

in which  $\theta_o$  is the cross-beam rotation determined as if it were simply supported. An alternative is to accept that transverse flexibility of the top flange allows the stiffener to deflect and shed some of its moment, leading to

$$F_c = \theta_o d \left( \frac{1}{\delta + L_u^3/15EI_c} \right) \quad (16.15)$$

### 16.6 Design for restricted depth

Frequently beam design will be constrained by a need to keep the beam depth to a minimum. This restriction is easy to understand in the context of floor beams in a multi-storey building for which savings in overall floor depth will be multiplied several times over, thereby permitting the inclusion of extra floors within the same overall building height or effecting savings on expensive cladding materials by reducing building height for the same number of floors. Within the floor zone of buildings with large volumes of cabling, ducting and other heavy services, only a fraction of the depth is available for structural purposes.

Such restrictions lead to a number of possible solutions which appear to run contrary to the basic principles of beam design. However, structural designers should remember that the main framing of a typical multi-storey commercial building typically represents less than 10% of the building cost and that factors such as the efficient incorporation of the services and enabling site work to proceed rapidly and easily are likely to be of greater overall economic significance than trimming steel weight.

An obvious solution is the use of universal columns as beams. While not as structurally efficient for carrying loads in simple vertical bending as UB sections, as illustrated by the example of Table 16.8, their design is straightforward. Problems of web bearing and buckling at supports are less likely due to the reduced web  $d/t$  ratios. Lateral-torsional buckling considerations are less likely to control the design of laterally unbraced lengths because the wider flanges will provide greater lateral stiffness ( $L/r_y$  values are likely to be low). Wider flanges are also advantageous for supporting floor units, particularly the metal decking used frequently as part of a composite floor system.

**Table 16.8** Comparison of use of UB and UC for simple beam design

|   |                                  |
|---|----------------------------------|
|   |                                  |
| 6 m   |                                  |
| 71 kN/m   |                                  |
| beams at 3 m spacing  |                                  |
| $M_{max} = 320 \text{ kN m}$  |                                  |
| $F_v = 213 \text{ kN}$  |                                  |
| 457 × 152 × UB 60   | 254 × 254 × UC 89                |
| $M_c = 352 \text{ kN m}$  | $M_c = 326 \text{ kN m}$         |
| $P_v = 600 \text{ kN}$  | $P_v = 435 \text{ kN}$           |
| $F_v < 0.6 P_v$ – no interaction  | $F_v < 0.6 P_v$ – no interaction |
| From Equation (16.2) and Table 16.5, assuming deflection limit is $L/360$ and service load is 47 kN m |                                  |
| $I_{reqd} = 2.23 (47 \times 3) 6^2 = 11\,319 \text{ cm}^4$  |                                  |
| $I_x = 25\,500 \text{ cm}^4$  | $I_x = 14\,300 \text{ cm}^4$     |



Difficulties can occur, because of the reduced depth, with deflections, although dead load deflections may be taken out by precambering the beams. This will not assist in limiting deflections in service due to imposed loading, although composite action will provide a much stiffer composite section. Excessive deflection of the floor beams under the weight of wet concrete can significantly increase slab depths at mid-span, leading to a substantially higher dead load. None of these problems need cause undue difficulty providing they are recognized and the proper checks made at a sufficiently early stage in the design.

Another possible source of difficulty arises in making connections between shallow beams and columns or between primary and secondary beams. The reduced web depth can lead to problems in physically accommodating sufficient bolts to carry the necessary end shears. Welding cleats to beams removes some of the dimensional tolerances that assist with erection on site as well as interfering with the smooth flow of work in a fabricator's shop that is equipped with a dedicated saw and drill line for beams. Extending the connection beyond the beam depth by using seating cleats, is one solution, although a requirement to contain the connection within the beam depth may prevent their use.

Beam depths may also be reduced by using moment-resisting beam-to-column connections which provide end fixity to the beams; a fixed end beam carrying a central point load will develop 50% of the peak moment and only 20% of the central deflection of a similar simply-supported beam. Full end fixity is unlikely to be a realistic proposition in normal frames but the replacement of the notionally pinned beam-to-column connection, provided by an arrangement such as web cleats, with a substantial end plate that functions more or less as a rigid connection permits the development of some degree of continuity between beams and columns. These arrangements will need more careful treatment when analyzing the pattern of internal moments and forces in the frame since the principles of simple construction will no longer apply.

An effect similar to the use of UC sections may be achieved if the flanges of a UB of a size that is incapable of carrying the required moment are reinforced by welding plates over part of its length. Additional moment capacity can be provided where it is needed as illustrated in Fig. 16.12; the resulting non-uniform section is

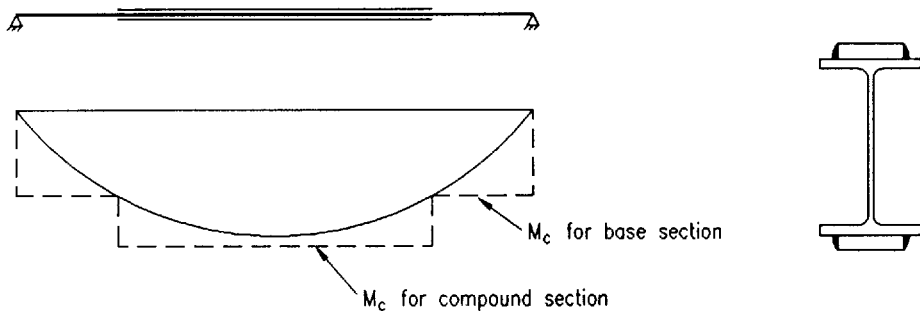


Fig. 16.12 Selective increase of moment capacity by use of a plated UB

stiffer and deflects less. Plating of the flanges will not improve the beam's shear capacity since this is essentially provided by the web and the possibility of shear or indeed local web capacity governing the design must be considered. A further development of this idea is the use of tapered sections fabricated from plate.<sup>11</sup> To be economic tapered sections are likely to contain plate elements that lie outside the limits for compact sections.

Because of the interest in developing longer spans for floors and the need to improve the performance of floor beams, a number of ingenious arrangements have developed in recent years.<sup>12</sup> Since these all utilize the benefits of composite action with the floor slab, they are considered in Chapter 21.

### 16.7 Cold-formed sections as beams

In situations where a relatively lightly loaded beam is required such as a purlin or sheeting rail spanning between main frames supporting the cladding in a portal frame, it is common practice to use a cold-formed section produced cold from flat steel sheet, typically between about 1 mm and 6 mm in thickness, in a wide range of shapes of the type shown in Fig. 16.13. A particular feature is that normally each section is formed from a single flat bent into the required shape; thus most available sections are not doubly symmetric but channels, zeds and other singly symmetric shapes. The forming process does, however, readily permit the use of quite complex cross-sections, incorporating longitudinal stiffening ribs and lips at the edges of flanges. Since the original coils are usually galvanized, the members do not normally require further protective treatment.

The structural design of cold-formed sections is covered by BS 5950: Part 5, which permits three approaches:

- (1) design by calculation using the procedures of the code, section 5, for members in bending
- (2) design on the basis of testing using the procedures of section 10 to control the testing; section 10.3 for members in bending
- (3) for three commonly used types of member (zed purlins and sheeting rails and lattice joists), design using the simplified set of rules given in section 9.

In practice, option (2) is the most frequently used with all the major suppliers providing design literature, the basis of which is usually extensive testing of their product range, design being often reduced to the selection of a suitable section for a given span, loading and support arrangement using the tables provided.

Most cold-formed section types are the result of considerable development work by their producers. The profiles are therefore highly engineered so as to produce a near optimum performance, a typical example being the ranges of purlins produced by the leading UK suppliers. Because of the combination of the thin material and the comparative freedom provided by the forming process, this

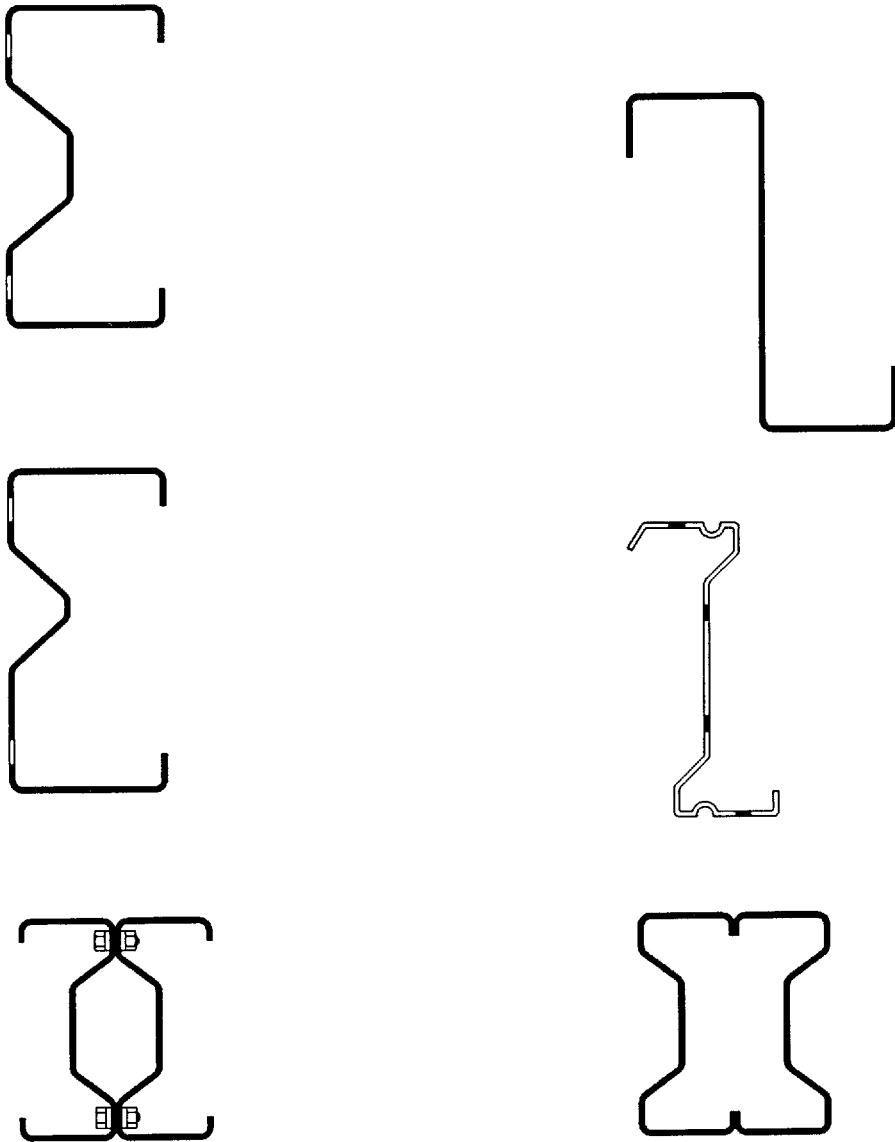


Fig. 16.13 Typical cold-formed section beam shapes

means that most sections will contain plate elements having high width-to-thickness ratios. Local buckling effects, either due to overall bending because the profile is non-compact, or due to the introduction of localized loads, are of greater importance than is usually the case for design using hot-rolled sections. BS 5950: Part 5 therefore gives rather more attention to the treatment of slender cross-sections

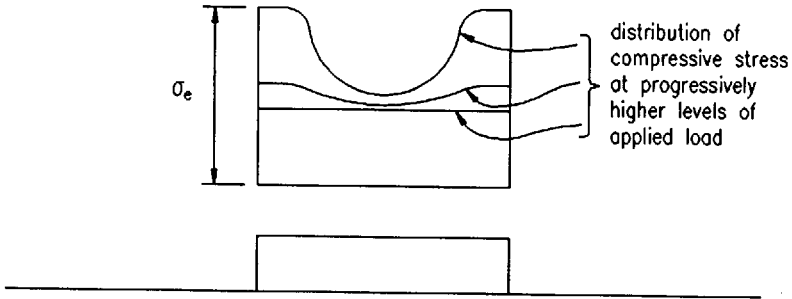


Fig. 16.14 Loss of plating effectiveness at progressively higher compressive stress

than does BS 5950: Part 1. In addition, manufacturers' design data normally exploit the post-buckling strength observed in their development tests.

The approach used to deal with sections containing slender elements in BS 5950: Part 5 is the well accepted effective width technique. This is based on the observation that plates, unlike struts, are able to withstand loads significantly in excess of their initial elastic buckling load, providing some measure of support is available to at least one of their longitudinal edges. Buckling then leads to a redistribution of stress with the regions adjacent to the supported longitudinal edges attracting higher stresses and the other parts of the plate becoming progressively less effective as shown in Fig. 16.14. A simple design representation of the condition of Fig. 16.14 consists of replacing the actual post-buckling stress distribution with the approximation shown in Fig. 16.15. The structural properties of the member (strength and stiffness) are then calculated for this effective cross-section as illustrated in Fig. 16.16. Tabulated information in BS 5950: Part 5 for steel of yield strength  $280 \text{ N/mm}^2$  makes the application of this approach simpler in the sense that effective widths may readily be determined, although cross-sectional properties have still to be calculated. The use of manufacturer's literature removes this requirement. For beams, Part 5 also covers the design of reinforcing lips on the usual basis of ensuring that the free edge of a flange supported by a

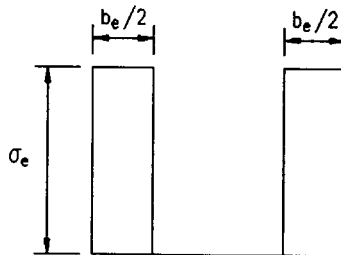


Fig. 16.15 Effective width design approximation

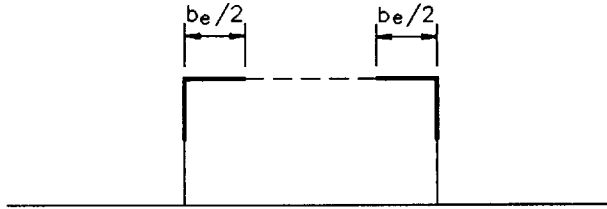


Fig. 16.16 Effective cross-section

single web behaves as if both edges were supported; web crushing under local loads, lateral–torsional buckling and the approximate determination of deflections take into account any loss of plating effectiveness.

For zed purlins or sheeting rails section 9 of BS 5950: Part 5 provides a set of simple empirically based design rules. Although easy to use, these are likely to lead to heavier members for a given loading, span and support arrangement than either of the other permitted procedures. A particular difference of this material is its use of unfactored loads, with the design conditions being expressed directly in member property requirements.

## 16.8 Beams with web openings

One solution to the problem of accommodating services within a restricted floor depth is to run the services through openings in the floor beams. Since the size of hole necessary in the beam web will then typically represent a significant proportion of the clear web depth, it may be expected that it will have an effect on structural performance. The easiest way of visualizing this is to draw an analogy between a beam with large rectangular web cut-outs and a Vierendeel girder. Figure 16.17 shows how the presence of the web hole enables the beam to deform locally in a similar manner to the shear type deformation of a Vierendeel panel. These deformations, superimposed on the overall bending effects, lead to increased deflection and additional web stresses.

A particular type of web hole is the castellation formed when a UB is cut, turned and rewelded as illustrated in Fig. 16.18. For the normal UK module geometry this leads to a 50% increase in section depth with a regular series of hexagonal holes. Other geometries are possible, including a further increase in depth through the use of plates welded between the two halves of the original beam. Some aspects of the design of castellated beams are covered by the provisions of BS 5950: Part 1, while more detailed guidance is available in a Constrado publication.<sup>13</sup>

Based on research conducted in the USA, a comparatively simple elastic method for the design of beams with web holes, including a fully worked example, is

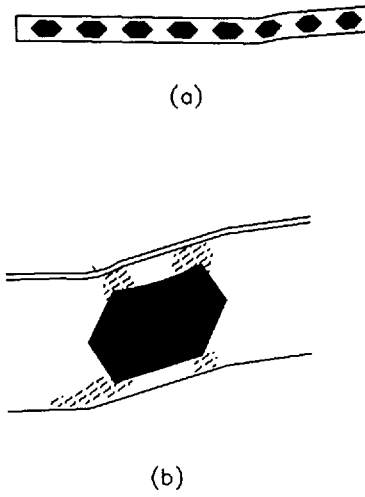


Fig. 16.17 Vierendeel-type action in beam with web openings: (a) overall view, (b) detail of deformed region

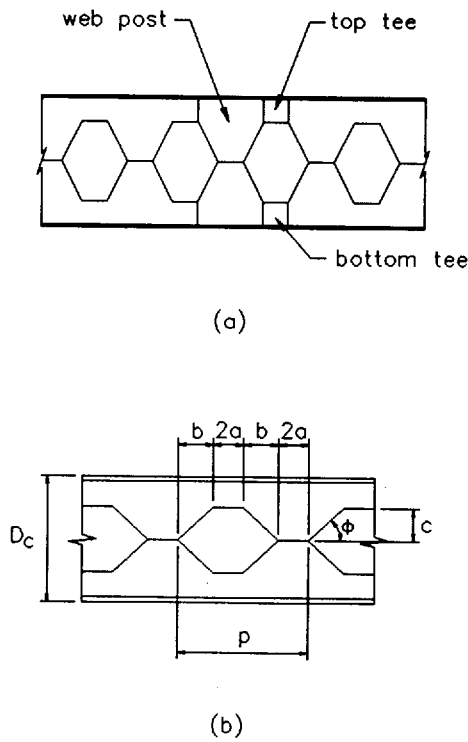


Fig. 16.18 Castellated beam: (a) basic concept, (b) details of normal UK module geometry

available.<sup>14</sup> This uses the concept of an analysis for girder stresses and deflections that neglects the effects of the holes, coupled with checking against suitably modified limiting values. The full list of design checks considered in Reference 14 is:

- (1) web shear due to overall bending acting on the reduced web area
- (2) web shear due to local Vierendeel bending at the hole
- (3) primary bending stresses (little effect since overall bending is resisted principally by the girder flanges)
- (4) local bending due to Vierendeel action
- (5) local buckling of the tee formed by the compression flange and the web adjoining the web hole
- (6) local buckling of the stem of the compression tee due to secondary bending
- (7) web crippling under concentrated loads or reactions near a web hole; as a simple guide, Reference 14 suggests that for loads which act at least  $(d/2)$  from the edge of a hole this effect may be neglected
- (8) shear buckling of the web between holes; as a simple guide, Reference 14 suggests that for a clear distance between holes that exceeds the hole length this effect may be neglected
- (9) vertical deflections; as a rough guide, secondary effects in castellated beams may be expected to add about 30% to the deflections calculated for a plain web beam of the same depth  $(1.5D)$ . Beams with circular holes of diameter  $(D/2)$  may be expected to behave similarly, while beams with comparable rectangular holes may be expected to deflect rather more.

As an alternative to the use of elastic methods, significant progress has been made in recent years in devising limit states approaches based on ultimate strength conditions. A CIRIA/SCI design guide<sup>15</sup> dealing with the topic principally from the point of composite beams is now available. If some of the steps in the 24-point design check of Reference 15 are omitted, the method may be applied to non-composite beams, including composite beams under construction. Much of the basis for Reference 15 may be traced back to the work of Redwood and Choo,<sup>16</sup> and the following treatment of bare steel beams is taken from Reference 16.

The governing condition for a stocky web in the vicinity of a hole is taken as excessive plastic deformation near the opening corners and in the web above and below the opening as illustrated in Fig. 16.19. A conservative estimate of web strength may then be obtained from a moment–shear interaction diagram of the type shown as Fig. 16.20. Values of  $M_0$  and  $V_1$  in terms of the plastic moment capacity and plastic shear capacity of the unperforated web are given in Reference 14 for both plain and reinforced holes;  $M_1$  may also be determined in this way. Solution of these equations is tedious, but some rearrangement and simplification are possible so that an explicit solution for the required area of reinforcement may be obtained. However, the whole approach is best programmed for a microcomputer and a program based on the full method of Reference 15 is available from the SCI.

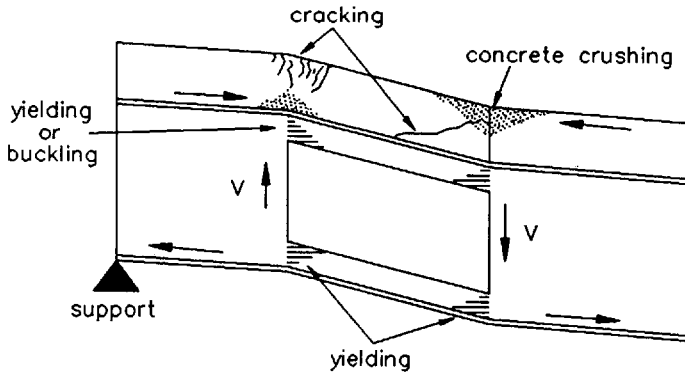


Fig. 16.19 Hole-induced failure

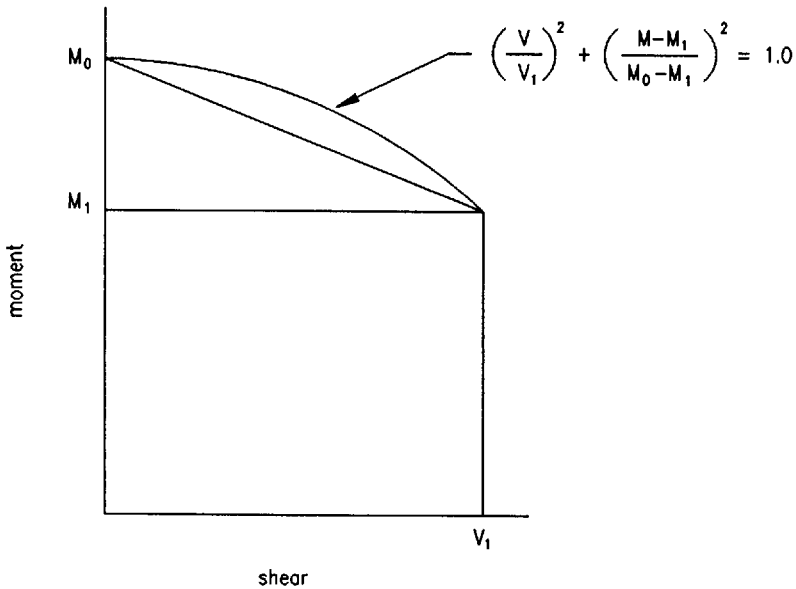


Fig. 16.20 Moment–shear interaction for a stocky web in the vicinity of a hole


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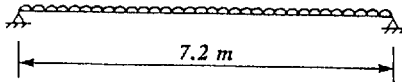
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A series of worked examples follows which are relevant to Chapter 16.

|   |  |   |                           |
|---|--|---|---------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>BEAM EXAMPLE 1<br/>                 LATERALLY RESTRAINED<br/>                 UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>16</b> |
|   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>        |

**Problem**

Select a suitable UB section to function as a simply supported beam carrying a 140 mm thick solid concrete slab together with an imposed load of 7.0 kN/m<sup>2</sup>. Beam span is 7.2 m and beams are spaced at 3.6 m intervals. The slab may be assumed capable of providing continuous lateral restraint to the beam's top flange.



Due to restraint from slab there is no possibility of lateral-torsional buckling, so design beam for:

- i) *Moment capacity*
- ii) *Shear capacity*
- iii) *Deflection limit*

**Loading**

*D.L.* =  $(2.4 \times 9.81 \times 0.14)$  = 3.3 kN/m<sup>2</sup>

*I.L.* = 7.0 kN/m<sup>2</sup>

*Total serviceability loading* = 10.3 kN/m<sup>2</sup>


*Table 2*


*Total load for ultimate limit state*


=  $1.4 \times 3.3 + 1.6 \times 7.0$  = 15.8 kN/m<sup>2</sup>

*Design ultimate moment* =  $(15.8 \times 3.6) \times 7.2^2/8$   
 = 369 kNm

*Design ultimate shear* =  $(15.8 \times 3.6) \times 7.2/2$   
 = 205 kN

|  |  |   |  |
|--|--|---|--|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>                                        | <p>Subject<br/><b>BEAM EXAMPLE 1<br/>LATERALLY RESTRAINED<br/>UNIVERSAL BEAM</b></p> |   | <p>Chapter ref.<br/><b>16</b></p>          |
|  | <p>Design code<br/><b>BS5950: Part 1</b></p>   | <p>Made by <b>DAN</b><br/>Checked by <b>GWO</b></p> | <p>Sheet no. <b>2</b></p>                  |
| <p>Assuming use of Grade 43 steel and no material greater than 16 mm thick,</p>  |  |   | <p><b>Table 6</b></p>                      |
| <p>take <math>p_y = 275 \text{ N/mm}^2</math></p>  |  |   |  |
| <p>Required <math>S_x = 369 \times 10^6 / 275</math><br/><math>= 1.34 \times 10^6 \text{ mm}^3 = 1340 \text{ cm}^3</math></p>  |  |   |  |
| <p>A 457 × 152 × 67 UB has a value of <math>S_x</math> of 1440 cm<sup>3</sup></p>  |  |   | <p><b>Steelwork Design Guide Vol 1</b></p> |
| <p><math>T = 15.0 &lt; 16.0 \text{ mm}</math></p>  |  |   |  |
| <p>∴ <math>p_y = 275 \text{ N/mm}^2</math></p>   |  |   |  |
| <p>Check section classification</p>  |  |   | <p><b>3.5.2</b></p>                        |
| <p>Actual <math>b/T = 5.06</math>                      <math>d/t = 44.7</math></p>   |  |   |  |
| <p><math>\epsilon = (275/p_y)^{1/2} = 1</math></p>   |  |   | <p><b>Table 7</b></p>                      |
| <p>Limit on <math>b/T</math> for plastic section = 8.5 &gt; 5.06</p>   |  |   |  |
| <p>Limit on <math>d/t</math> for shear = 63 &gt; 44.7</p>  |  |   |  |
| <p>∴ <u>Section is plastic</u></p>   |  |   |  |
| <p>Actual <math>M_c = 275 \times 1440 \times 10^3</math><br/><math>= 396 \times 10^6 \text{ Nmm}</math><br/><math>= \underline{396 \text{ kNm}} &gt; \underline{369 \text{ kNm}} \text{ OK}</math></p> |  |   | <p><b>4.2.5</b></p>                        |
| <p>Vertical shear capacity</p>   |  |   |  |
| <p><math>P_v = 0.6 p_y A_v</math></p>  |  |   | <p><b>4.2.3</b></p>                        |
| <p>where <math>A_v = t D</math></p>  |  |   |  |
| <p>∴ <math>P_v = 0.6 \times 275 \times 9.1 \times 457.2 = 686 \times 10^3 \text{ N}</math><br/><math>= \underline{686 \text{ kN}} &gt; \underline{205 \text{ kN}} \text{ OK}</math></p>                |  |   |  |

|  |  |   |                           |
|--|--|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>BEAM EXAMPLE 1<br/>         LATERALLY RESTRAINED<br/>         UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>16</b> |
|  | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>        |
| <b>Check serviceability deflections under imposed load</b>   |  |   | <b>2.5.1</b>              |
| $\delta = \frac{5 \times (7.0 \times 3.6) \times 7200^4}{384 \times 205000 \times 32400 \times 10^4}$ $= 13.3 \text{ mm} = \text{span}/541$                        |  |   |                           |
| From Table 5, limit is span/360 $\therefore \delta$ OK   |  |   |                           |
| $\therefore$ Use <u>457 × 152 × 67 UB Grade 43</u>   |  |   |                           |

|   |  |   |                           |
|---|--|---|---------------------------|
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|   | Design code<br><b>BSS950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>I</b>        |

**Problem**

For the same loading and support conditions of example 1 select a suitable UB assuming that the member must be designed as laterally unrestrained.

It is not now possible to arrange the calculations in such a way that a direct choice is possible; a guess and check approach must be adopted.

Try **610 × 229 × 125 UB**

$u = 0.873$                        $r_y = 4.98 \text{ cm}$                       *Steelwork Design Guide Vol 1*

$x = 34.0$                        $S_x = 3680 \text{ cm}^3$                       *4.3.7.5*

$\lambda = L_E / r_y = 7200 / 49.8 = 145$

$\lambda / x = 145 / 34 = 4.26$

$v = 0.85$                       *Table 14*


$\lambda_{LT} = n u v \lambda$

For simplicity make a safe approximation of  $n = 1.0$

$\therefore \lambda_{LT} = 1.0 \times 0.873 \times 0.85 \times 145 = 108$

$p_b = 116 \text{ N/mm}^2$                       *Table 11*

$M_b = S_x p_b = 3680 \times 10^3 \times 116 = 427 \times 10^6 \text{ Nmm} = 427 \text{ kNm} > 369 \text{ kNm OK}$                       *4.3.7.3*

|  |  |   |                           |
|--|--|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>BEAM EXAMPLE 2<br/>         LATERALLY UNRESTRAINED<br/>         UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>16</b> |
|  | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |

*Since section is larger than before,  $P_v$  and  $\delta$  will also be satisfactory*

*$\therefore$  Adopt 610 × 229 × 125 UB*

*However for a UDL,  $n = 0.94$  when determining  $\lambda_{LT}$*

*Table 16*

*Refer to member capacities section for values of  $M_b$  directly, noting grade 43 material.*

*Steelwork  
Design Guide  
Vol 1*


*Value of  $M_b$  required is 369 kNm; interpolating for  $n = 0.94$  &  $L_E = 7.2$  m suggests as possible sections:*

*533 × 210 × 122 UB  $M_b$  OK*

*610 × 229 × 113 UB  $M_b$  OK*

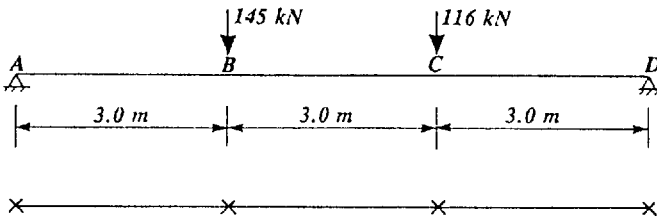
*Since both are larger than that checked for shear capacity and serviceability deflection in the previous example, either may be adopted.*

*$\therefore$  Adopt 533 × 210 × 122 UB or 610 × 229 × 113 UB Grade 43*

|   |   |  |
|---|---|--|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>BEAM EXAMPLE 3</b><br/><b>LATERALLY UNRESTRAINED</b><br/><b>UNIVERSAL BEAM</b></p> | <p>Chapter ref.</p> <p>16</p>                          |
|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p>   | <p>Made by <b>DAN</b></p> <p>Checked by <b>GWO</b></p> |

**Problem**

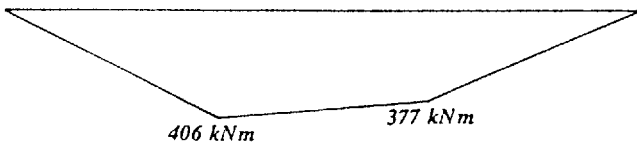
Select a suitable UB section in Grade 43 steel to carry the pair of point loads at the third points transferred by crossbeams as shown in the accompanying sketch. Design to BS 5950: Part 1.



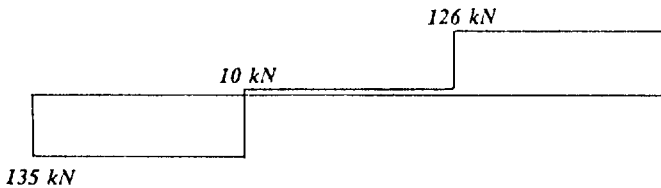
The crossbeams may reasonably be assumed to provide full lateral and torsional restraint at B and C; assume further that ends A and D are similarly restrained. Thus the actual level of transfer of load at B and C (relative to the main beam's centroid) will have no effect, the lateral-torsional buckling aspects of the design being one of considering the 3 segments AB, BC and CD separately.


From statics the BMD and SFD are

**BMD**




**SFD**



|   |  |   |                           |
|---|--|---|---------------------------|
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|   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |
| <p><i>For initial trial section select a UB with <math>M_{cx} &gt; 406</math> kNm.</i></p> <p><i>A 457 × 152 × 74 UB provides <math>M_{cx}</math> of 429 kNm. Now check lateral-torsional buckling strength for segments AB, BC &amp; CD.</i></p> <p><b>AB</b></p> <p><math>\beta = 0/406 = 0.0</math></p> <p><math>m = 0.57</math> <span style="float: right;"><i>Table 18</i></span></p> <p><math>\bar{M} = 0.57 \times 406 = 231.4</math> kNm</p> <p>For <math>L_E = 3.0</math> m, <math>M_b = 288</math> kNm <span style="float: right;"><i>Steelwork Design Guide Vol 1</i></span></p> <p><math>\therefore 288 &gt; 231.4</math> kNm <b>OK</b></p> <p><b>BC</b></p> <p><math>\beta = 377/406 = 0.93</math></p> <p><math>m = 0.97</math> <span style="float: right;"><i>Table 18</i></span></p> <p><math>\bar{M} = 0.97 \times 406 = 393.8</math> kNm</p> <p>But for <math>L_E = 3.0</math> m, <math>M_b = 288</math> kNm <u>Not</u> OK</p> <p>Try 457 × 191 × 82 UB</p> <p>this provides, <math>M_b</math> of 396 kNm &gt; 393.8 kNm <b>OK</b> <span style="float: right;"><i>Steelwork Design Guide Vol 1</i></span></p> <p><b>CD</b></p> <p><i>Satisfactory by inspection OK</i></p> <p><i>A 457 × 191 × 82 UB provides sufficient resistance to lateral-torsional buckling for each segment and thus for the beam as a whole.</i></p> |  |   |                           |



|  |  |   |  |
|--|--|---|--|
| <p>The Steel Construction Institute<br/> <br/>                 Silwood Park, Ascot, Berks SL5 7QN</p>   | Subject<br><b>BEAM EXAMPLE 3<br/>                 LATERALLY UNRESTRAINED<br/>                 UNIVERSAL BEAM</b> |   | Chapter ref.<br><b>16</b>  |
|  | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>   |
| <p><i>Check shear capacity; maximum shear at A is 135 kN</i></p> <p><math>P_v = 752 \text{ kN} &gt; 135 \text{ kN OK}</math></p> <p><i>Check bearing and buckling capacity of web at the supports - required capacity is 135 kN.</i></p> <p><i>Since <math>C_1</math> values exceed 135 kN in both cases, section is clearly adequate.</i></p> <p><i>For initial check on serviceability deflections assume an equivalent UDL and factor down all loads by 1.5 to obtain</i></p> $w = \frac{145 + 116}{1.5 \times 9} = 19.3 \text{ kN/m}$ $\delta = \frac{5 \times 19.3 \times 9000^4}{384 \times 205000 \times 37100 \times 10^4}$ $= 21.68 \text{ mm} = \text{span}/415$ <p><i>Limiting deflection is span/360 ∴ OK</i></p> <p><i>Beam is clearly satisfactory for deflection since these (approximate) calculations have used the full load and not just the imposed load.</i></p> <p><i>∴ Adopt <u>457 × 191 × 82 UB</u></i></p> |  |   |  |
|  |  |   | <p><b>Steelwork<br/>                 Design Guide<br/>                 Vol 1</b></p> <p><b>Table 5</b></p> |

# Chapter 17

## Plate girders

by RANGACHARI NARAYANAN

### 17.1 Introduction

Plate girders are employed to support heavy vertical loads over long spans; the resulting bending moments are larger than the moment capacity of available rolled sections. In its simplest form the plate girder is a built-up beam consisting of two flange plates, fillet welded to a web plate to form an I-section. The primary function of the top and bottom flange plates is to resist the axial compressive and tensile forces caused by the applied bending moments; the main function of the web is to resist the shear. Indeed this partition of structural action is used as the basis for design in some Codes of Practice.

For a given bending moment the required flange areas can be reduced by increasing the distance between them. Thus for an economical design, it is advantageous to increase the distance between flanges. To keep the self-weight of the girder to a minimum the web thickness should be reduced as the depth increases, but this leads to web buckling considerations being more significant in plate girders than in rolled beams.

Plate girders are sometimes used in buildings and are often used in small- to medium-span bridges. They are designed in accordance with the provisions contained in BS 5950: Part 1<sup>1</sup> and BS 5400: Part 3<sup>2</sup> respectively. This chapter explains current practice in designing plate girders for buildings and bridges; references to the relevant clauses in the Codes are made.

### 17.2 Advantages and disadvantages

The development of highly automated workshops in recent years has reduced the fabrication costs of plate girders very considerably; box girders and trusses still have to be fabricated manually, with consequently high fabrication costs. Optimum use of material is made compared with rolled sections as the girder is fabricated from plates and so the designer has greater freedom to vary the section to respond to a change in the applied forces. Thus variable depth plate girders have been increasingly designed in recent years. Plate girders are aesthetically more pleasing than trusses and are easier to transport and erect than box girders.

There are only a very few limitations in the use of plate girders. Compared with trusses, they are heavier, more difficult to transport and have larger wind resist-

**Table 17.1** Recommended span-to-depth ratios for plate girders used in buildings

| Applications   | Span-to-depth ratio |
|--|---------------------|
| (1) Constant-depth beams used in simply-supported composite girders, and for simply-supported non-composite girders, with concrete decking               | 12 to 20            |
| (2) Constant-depth beams used in continuous non-composite girders using concrete decking ( <i>NB</i> continuous composite girders are rare in buildings) | 15 to 20            |
| (3) For simply-supported crane girders (non-composite construction is usual)   | 10 to 15            |

ance. The provision of openings for services is also more difficult. The low torsional stiffness of plate girders makes them difficult to use on bridges having small plan radius. Plate girders can sometimes pose problems during erection because of concern for the stability of compression flanges.

## 17.3 Initial choice of cross-section in buildings

### 17.3.1 Span-to-depth ratios

Advances in fabrication methods allow the economic manufacture of plate girders of constant or variable depth. Traditionally, constant-depth girders were more common in buildings; however this may change as designers become more inclined to modify the steel structure to accommodate services.<sup>3</sup> Recommended span-to-depth ratios are given in Table 17.1.

### 17.3.2 Recommended plate thicknesses and proportions

The choice of the thickness of the web is related to the stiffening. Care should be exercised in ensuring that not too thin a web is chosen; some of the material saved has to be put back by way of stiffening and the extra workmanship required is expensive.

The minimum web thickness chosen for plate girders in buildings usually varies from 10 mm for girders up to 1200 mm deep to 20 mm for those 2500 mm deep.

Changes in flange size along the girder are not worthwhile in buildings. For non-composite girders the flange width chosen is usually within a range of 0.3–0.5 times the depth of the section (0.4 is most common). It is important to ensure that the flange size chosen is within the breadth-to-thickness limits for semi-compact sections in order to avoid local buckling of the flange. As a preliminary guide it is suggested that the *overall* flange width-to-thickness ratio be limited to 24. For simply-supported composite girders these rules can still be employed for the preliminary sizing of top flanges. The width of bottom (tension) flanges can be increased by 30%.

### 17.3.3 Stiffeners

Horizontal web stiffeners are not usually required for plate girders used in buildings. Vertical web stiffeners may be provided close to supports to enhance the resistance to shear near the supports. Intermediate stiffening at locations far away from supports will, in general, be unnecessary due to reduced shear.

The provision of vertical stiffeners enables the web to sustain shear stresses well in excess of its unstiffened elastic critical shear stress. Furthermore, additional strength is obtained as a consequence of *tension field action*, whereby the web panel between the stiffeners resists additional shear loads by developing diagonal tensile stresses.

Where vertical stiffeners are specified, they are spaced such that the panel aspect (width-to-depth) ratio is around 1.2 to 1.6. Where end panels are designed without utilizing the tension field action (see Fig. 17.6), the aspect ratio of the end panels is reduced to 0.6–1.0. Sometimes double stiffeners are employed as bearing stiffeners at the end (see Fig. 17.7). The overhang of the beam beyond the support is generally limited to a maximum of one-eighth of the depth of the girder.

## 17.4 Design of plate girders used in buildings to BS 5950: Part 1

### 17.4.1 General

Any cross section of a plate girder will normally be subjected to a combination of shear force and bending moment, present in varying proportions. BS 5950: Part 1 allows one of the following three methods to be used for the determination of capacity (see clause 4.4.4.2):

- (1) The moment may be assumed to be resisted by the flanges alone and the web designed for shear only

- (2) The moment may be assumed to be resisted by the whole section, the web being designed for combined shear and longitudinal stresses
- (3) A proportion of the loading may be assumed to be resisted by Method (1), the remainder being resisted by Method (2).

The separation of moment and shear effects in Method (1) leads to considerable simplification and a better physical appreciation of the load-carrying action. Although slightly conservative it is probably the most commonly used, and is the method described in the following sections.

### 17.4.2 Web thickness

The slenderness at which web plates become prone to buckling is defined as  $63\varepsilon$  in BS 5950: Part 1, where  $\varepsilon = (275/p_y)^{1/2}$  (see clause 4.4.4.2). When  $d/t \leq 63\varepsilon$  (see Fig. 17.1), webs will not buckle and the design principles for plate girders are similar to those for universal beams. For economy, plate girders are designed with thin webs ( $d/t > 63\varepsilon$ ), hence shear buckling *must* be taken into account.

The buckling capacity of slender webs can be increased by the provision of web stiffeners. In general, plate girder webs used in buildings are unstiffened or have transverse stiffeners only.

Minimum web thickness requirements (clause 4.4.2 of BS 5950: Part 1) are largely fixed by serviceability considerations such as adequate stiffness to prevent unsightly buckles developing during normal handling and erection, 'breathing of the web' during loading and unloading in service, etc. The following minimum thickness values are prescribed in BS 5950: Part 1 (see Fig. 17.1):

- (1) For unstiffened webs,  $t \geq \frac{d}{250}$

(where  $t$  = thickness of the web, and  $d$  = depth of the web)

- (2) For transversely stiffened webs,

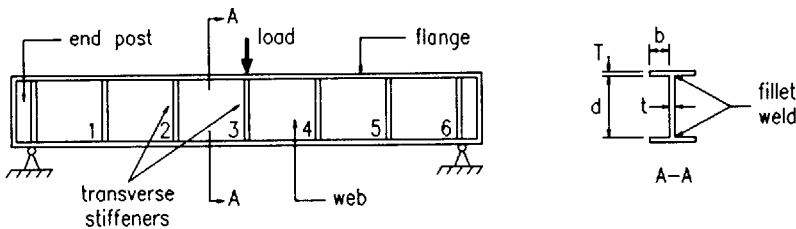


Fig. 17.1 Elevation of a typical plate girder

with stiffener spacing  $a > d$ ,  $t \geq \frac{d}{250}$

with stiffener spacing  $a \leq d$ ,  $t \geq \frac{d}{250} \left(\frac{a}{d}\right)^{\frac{1}{2}}$ .

To prevent the flange buckling into the web, the Code specifies:

(1) For unstiffened webs,  $t \geq \frac{d}{250} \frac{p_{yf}}{345}$

(where  $p_{yf}$  is the design stress of the flange material)

(2) For transversely stiffened webs,

with stiffener spacing  $a > 1.5d$ ,  $t \geq \frac{d}{250} \left(\frac{p_{yf}}{345}\right)^{\frac{1}{2}}$

with stiffener spacing  $a \leq 1.5d$ ,  $t \geq \frac{d}{250} \left(\frac{p_{yf}}{455}\right)^{\frac{1}{2}}$ .

### 17.4.3 Flange thickness

Local buckling of the compression flange may also occur if the flange plate is of slender proportions, i.e. if  $b/T > 13\epsilon$ . However, flanges of such slender proportions are rare in buildings since there would seldom appear to be a good reason to exceed the specified outstand width in normal design.

#### 17.4.3.1 Moment capacity

Following Method (1), the overall moment capacity,  $M_c$ , is calculated from the plastic capacity of the flange plates only:

$$M_c = p_{yf} S_{xf}$$

where  $p_{yf}$  is the design stress of the flange material and  $S_{xf}$  is the plastic modulus of the flanges only about the section axis.

#### 17.4.4 Shear capacity

Following Method (1), the shear capacity is determined as that of the web plate only, assuming the web to be unaffected by the bending moment.

Thin webs may be designed with or without transverse stiffeners; the procedures are considered individually.

**17.4.4.1 Webs without intermediate stiffeners**

(clause 4.4.5.3 of BS 5950: Part 1)

The shear capacity of unstiffened webs is limited to their shear buckling resistance,

$$V_{cr} = q_{cr}dt$$

where  $q_{cr}$  is the critical shear stress.

Based on the elastic buckling theory, the Code gives the following values for  $q_{cr}$ :

(1) When  $\lambda_w \leq 0.8$ ,

$$q_{cr} = 0.6p_{yw}$$

(2) When  $0.8 < \lambda_w < 1.25$ ,

$$q_{cr} = 0.6p_{yw} [1 - 0.8(\lambda_w - 0.8)]$$

(3) When  $\lambda_w \geq 1.25$ ,

$$q_{cr} = q_c$$

where  $\lambda_w$  is the equivalent slenderness of the web and equals  $(0.6p_{yw}/q_c)^{1/2}$ ;  $q_c$  is the elastic critical shear strength of the panel (in  $N/mm^2$ ) given by:

(a) when  $a/d \leq 1$ , 
$$q_c = \left[ 0.75 + \frac{1}{(a/d)^2} \right] \left( \frac{1000}{dt} \right)^2$$

(b) when  $a/d > 1$ , 
$$q_c = \left[ 1 + \frac{0.75}{(a/d)^2} \right] \left( \frac{1000}{dt} \right)^2$$

where  $a$  is the spacing of transverse stiffeners;  $d$  is the depth of the web;  $t$  is the thickness of the web;  $p_{yw}$  is the design strength of the web.

Values of  $q_{cr}$  are tabulated in the Code.

**17.4.4.2 Webs with intermediate transverse stiffeners**

(clause 4.4.5.4 of BS 5950: Part 1)

Webs with intermittent stiffeners are illustrated in Fig. 17.2. BS 5950: Part 1 allows such webs to be designed by limiting their shear capacity to the shear buckling resistance of the panels in a similar way to section 17.4.4.1. Values of  $q_{cr}$  are tabulated in the Code for different stiffener spacing-to-web depth ratios,  $a/d$ .

However, this approach is very conservative since the introduction of transverse stiffeners increases the shear capacity in two ways.<sup>4</sup> As has already been noted, the buckling resistance  $V_{cr}$  is increased as a consequence of reduced  $a/d$  values and the development of post-critical strength; secondly, the stiffeners enable the girder to withstand loads considerably in excess of the conventional elastic critical

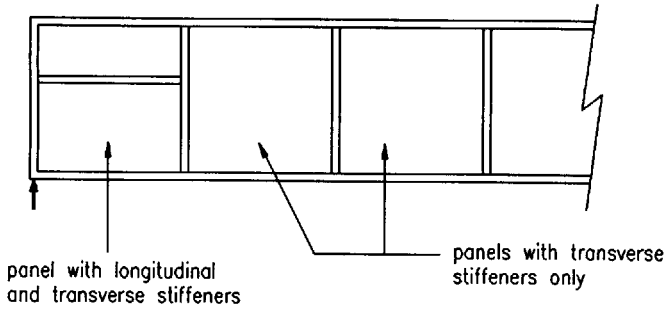


Fig. 17.2 Different stiffener arrangements

strength of the web in shear, because of the development of tension field action. Advantage should be taken of the tension field action to achieve an effective design; the Code permits the designer to do so, should he so wish.

Figure 17.3(a) shows the development of a tension field in a typical girder. Once a web panel has buckled, its capacity to carry additional diagonal compressive stresses is ignored and it is assumed that a new load-carrying mechanism is developed, whereby any additional shear load is carried by an inclined tensile membrane stress field. This tensile force anchors against the top and bottom flanges and against the transverse stiffener on either side of the web panel, as shown. The load-carrying action of the plate girder then becomes similar to that

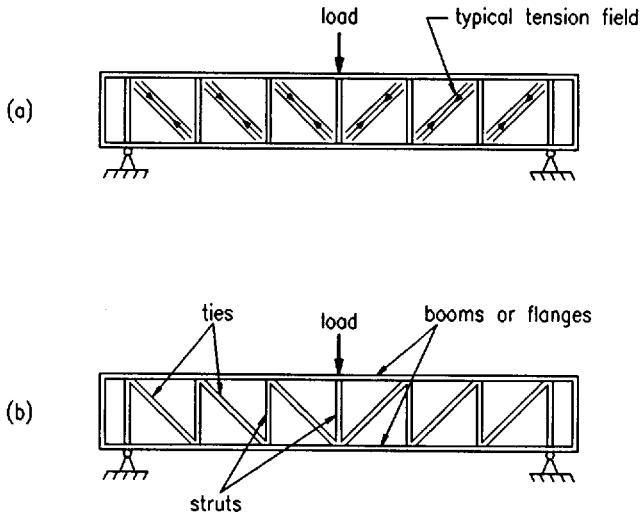


Fig. 17.3 Tension field action (a) in individual sub-panels as a result of transverse stiffeners. (b) Typical N-truss for comparison



of the N-truss in Fig. 17.3(b). The resistance offered by the web plates is analogous to that of the diagonal tie bars in the truss.

The behaviour of a girder under an increasing shear load may thus be divided into the three phases shown in Fig. 17.4. Figure 17.4(a) shows the situation prior to buckling when equal tensile and compressive principal stresses are developed in the plate. Figure 17.4(b) shows the development of a tension field in the post-buckling phase, and Fig. 17.4(c) shows the situation at collapse. As indicated, failure occurs when the web yields and four plastic hinges form in the flanges to allow the development of a sway collapse mechanism.

In the Code the full shear buckling resistance,  $V_b$ , is expressed as:

$$V_b = [q_b + q_t (K_t)^{\frac{1}{2}}] dt \quad \text{but } \leq 0.6p_y dt$$

In this expression  $q_b$  represents the *basic* shear strength of the web. It combines the buckling strength  $q_{cr}$  and the post-buckling strength derived from that part of the web tension field supported by the transverse stiffeners. Values of the basic shear strength,  $q_b$ , are tabulated in the Code for different stiffener spacing ratios ( $a/d$ ) and web slenderness ratios ( $d/t$ ), but may be calculated by formulae given below.

The basic shear strength of the web panel,  $q_b$ , is given by:

$$q_b = q_{cr} + \frac{y_b}{2\{a/d + [1 + (a/d)^2]^{\frac{1}{2}}\}}$$

where  $q_{cr}$  is the elastic critical stress in shear of the web panel ( $a \times d$ ) calculated from elastic buckling theory;  $y_b$  is the basic tension field strength given by:

$$y_b = (p_{yw}^2 - 3q_{cr}^2 + \phi_t^2)^{\frac{1}{2}} - \phi_t$$

in which  $\phi_t = \frac{1.5q_{cr}}{[1 + (a/d)^2]^{\frac{1}{2}}}$

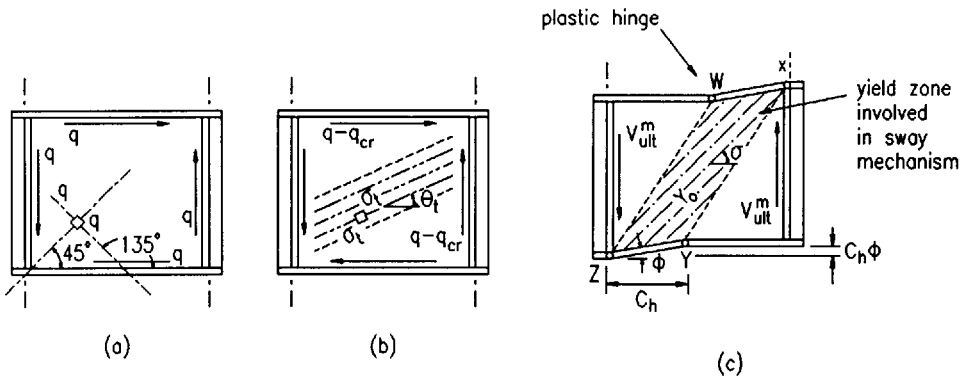


Fig. 17.4 Phases in behaviour up to collapse of a typical panel in shear: (a) unbuckled, (b) post-buckled, (c) collapsed

$a$  is the spacing of transverse stiffeners;  $d$  is the depth of the web;  $t$  is the thickness of the web;  $p_{yw}$  is the design strength of the web.

*NB* If  $q_b$  is greater than  $0.57p_{yw}$ , it may be taken as equal to but not greater than  $0.6p_{yw}$ .

The second term in the equation for  $V_b$  (i.e.  $q_f (K_f)^{\frac{1}{2}}$ ) represents the contribution made by the flanges to the post-buckling strength. The flanges support that part of the web tension field that pulls against them, as in Fig. 17.4(b), and they finally develop plastic hinges at collapse.

The term  $q_f$  helps to evaluate the flange-dependent shear strength, which is again tabulated in the Code for different  $a/d$  and  $d/t$  ratios. The term  $K_f$  is a non-dimensional parameter relating the plastic moment capacity of the flange,  $M_{pf}$ , to that of the web,  $M_{pw}$ .

The flange-dependent shear strength,  $q_f$ , is given by:

$$q_f = \left[ 4\sqrt{3} \sin \left( \frac{\theta}{2} \right) \left( \frac{y_b}{p_{yw}} \right)^{\frac{1}{2}} \right] \times 0.6p_{yw}$$

where  $\theta = \tan^{-1} \left( \frac{d}{a} \right)$ .

If the girder is subjected to shear forces only, then  $M_{pf}$  is taken as the full plastic moment capacity of the flange:

$$M_{pf} = \frac{2b}{4} T^2 p_{yf}$$

When a girder is subjected to a bending moment as well as shear then the flanges have to carry the axial forces arising from the bending action in addition to the lateral pull exerted by the tension field. These axial forces will reduce the plastic moment capacity of the flange plates, the reduced value  $M_{pf}$  being obtained from plasticity theory as:

$$M_{pf} = M_{pf} \left( 1 - \frac{f}{p_{yf}} \right)$$

where  $f$  is the mean axial stress developed in the flange as a result of bending.

Thus, at sections of high moment, where the mean stress  $f$  may approach the flange design strength  $p_{yf}$ , the flange will make little contribution to the shear buckling resistance,  $V_b$ .

The plastic moment of resistance of the web,  $M_{pw}$ , is given by:

$$M_{pw} = \frac{1}{4} d^2 t p_{yw}$$

and

$$K_f = \frac{M_{pf}}{4M_{pw}}$$

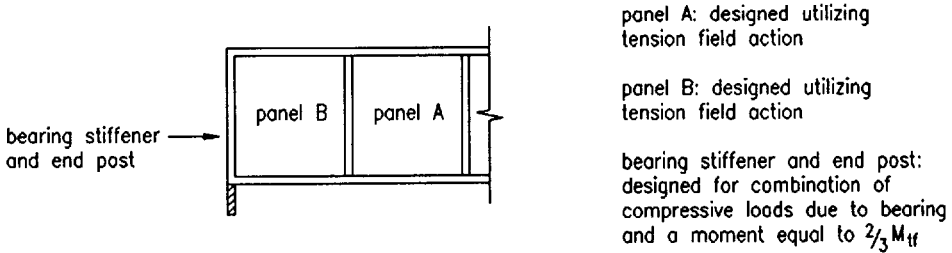


Fig. 17.5 End panel designed using tension field action (single stiffener)

**17.4.4.3 Special consideration for end panels**  
(clause 4.4.5.4.3 of BS 5950: Part 1)

Tension field forces can only develop when an adequate anchorage is provided by the members bounding the panel. This is a particular problem at the ends of a girder where the anchorage has to be provided by the end stiffener alone.

The Code suggests that the anchor force  $H_q$  arising from tension field action be calculated as:

$$H_q = 0.75dt p_y \left( 1 - \frac{q_{cr}}{0.6p_y} \right)^{\frac{1}{2}}$$

The Code then offers two possible approaches to end panel design. In the first (Fig. 17.5), the capacity of the end panel B may be limited to its shear buckling resistance,  $V_{cr}$ , so that no tension field develops within it. Panel B and its bounding transverse stiffeners then act as a beam, spanning vertically between the girder flanges to resist the shear and bending moment arising from the tension field pull,  $H_q$ , of panel A.

This first approach is conservative and results in a substantial end member. It has the disadvantage of omitting the additional shear capacity that could be derived from tension field action in the end panel, and this in the region close to the support where applied shear forces could well be a maximum. To prevent the calculated shear capacity of panel B being much lower than that of panel A, the intermediate stiffener would have to be positioned close to the support to make B a narrow panel.

To overcome this disadvantage, the second approach offered by the Code (Fig. 17.6) does allow the development of a tension field in the end panel, i.e. panel B is designed in the same way as the internal panels. The disadvantage now is that the single end stiffener by itself, spanning vertically between the flanges, has to resist the tension field pull of panel B. This represents a significant demand on the capacity of the single stiffener.

To overcome this, a double stiffener may be used as in Fig. 17.7 to form a rigid end post in which the two stiffeners and the portion of the web projecting beyond the support now form the vertically spanning beam. The disadvantage in this case

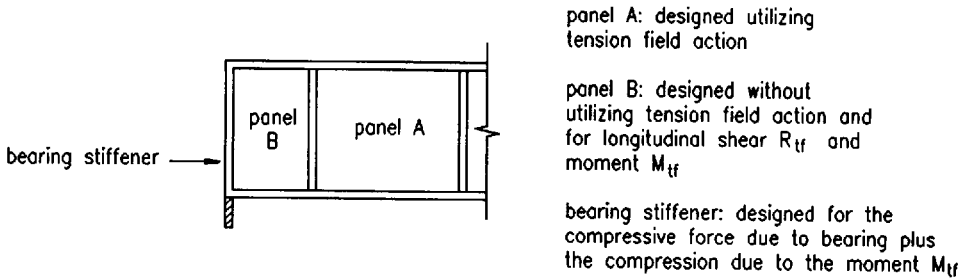


Fig. 17.6 End panel designed without using tension field action

is that adequate space must be available to allow the girder to project beyond its support.

Thus, each of the three alternatives shown in Figs 17.5, 17.6 and 17.7 has certain disadvantages. However, their inclusion in the Code enables the most appropriate to be chosen for each particular design situation. In most cases, the double stiffener solution results in economy, assuming the site conditions permit the girder to project beyond the support.

**17.4.4.4 Special considerations for webs with openings**

Web openings frequently have to be provided in girders used on building construction for service ducts, etc. When any dimension of such an opening exceeds 10% of the minimum dimensions of the panel in which it is placed, then the Code limits the shear capacity of the panel to its shear buckling resistance,  $V_{cr}$ . Any tension field capacity of a perforated web is thus conservatively ignored to avoid design complexity. Also, the panels immediately adjacent to that containing the large openings are designed as end panels according to the special considerations outlined above.

Guidance on design of plate girders with openings is provided in Reference 5.

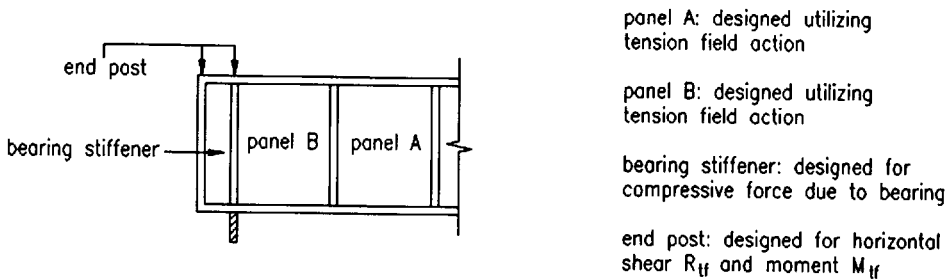


Fig. 17.7 End panel designed using tension field action (double stiffener)

### **17.4.5 Design of web stiffeners**

The provision of adequate transverse stiffeners is essential to the satisfactory performance of the web panels of girders. The three most important types of stiffeners are:

- (1) load-carrying
- (2) bearing
- (3) intermediate transverse.

Stiffeners of each of these types are subjected to compression and should be checked for local buckling.

#### ***17.4.5.1 Load-carrying stiffeners***

These are provided to prevent local buckling of the web due to concentrated loads or reactions applied through the flange. The Code requires that the stiffeners should be positioned wherever such actions occur, if the buckling resistance of the unstiffened web would otherwise be exceeded.

Load-carrying stiffeners must be checked for both buckling and bearing. When checking for buckling an effective web width of  $20t$  on either side of the centreline of the stiffener is considered to act with it to form a cruciform section. The resulting stiffener strut is then assumed to have an effective length of 0.7 times its actual length if the flange is restrained against rotation in the plane of the stiffener. If the flange is not so restrained, the actual length is taken. The buckling resistance of the stiffener strut is then determined as for a normal compression member.

When checking the stiffener for bearing, only that area of the stiffener in contact with the flange is taken into account.

Sometimes it is not possible to provide stiffeners immediately under the externally applied vertical loading, e.g. in the case of a travelling load on a gantry girder or during launching of a girder in construction. In such cases of patch loading (loads applied between the stiffeners), an additional check is required to ensure that the specified compressive strength of the web for edge loading is not exceeded.

#### ***17.4.5.2 Bearing stiffeners***

These are provided to prevent local crushing of the web due to concentrated loads or reactions applied through the flange. Should such actions not exceed the buckling resistance of the web, then the load-carrying stiffeners of section 17.4.5.1 are not needed but the local bearing resistance can still be exceeded. If so, then bearing stiffeners are introduced designed to provide a sufficient bearing area to resist the loading.

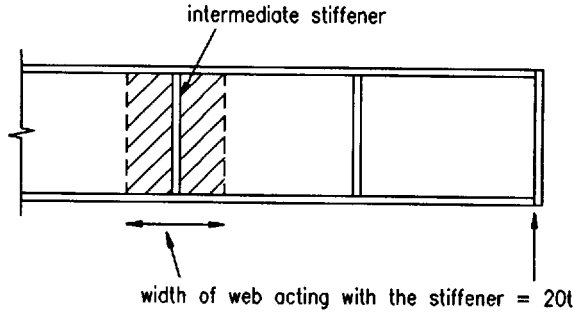


Fig. 17.8 Web acting with stiffener

**17.4.5.3 Intermediate transverse stiffeners**

The need for intermediate transverse stiffeners and their required spacing is dictated by the rules for shear web design discussed in section 17.4.4.2 (webs with intermediate transverse stiffeners).

The Code requires the stiffeners alone to have a specified minimum second moment of area about the centreline of the web. This ensures that the stiffener is able to remain straight and prevent out-of-plane buckling of the web at the stiffener position.

Designing for tension field action imposes additional loading on the transverse stiffeners. Because of the additional compressive forces induced, the stiffener must be designed as a strut and checked for buckling. As discussed later in section 17.5.1 for load-carrying stiffeners, an effective portion of the web, of width  $20t$  on each side of the centreline of the stiffener, is considered to act with the stiffener to form a cruciform section (Fig. 17.8). The buckling resistance,  $P_q$ , of the stiffener strut, calculated as for a normal compression member, is then required to be in excess of the stiffener loading,  $F_q$ , calculated as:

$$F_q = V - V_s$$

where  $V$  is the maximum shear force in the panels adjacent to the stiffener, and  $V_s$  is the shear buckling resistance of the web panel designed without using tension field action, i.e. smaller values of  $V_{cr}$  for the panels on either side of the stiffener.

**17.4.5.4 Combined loads on stiffeners**

Stiffeners may, of course, be required to perform more than one of the above functions. For example, an intermediate stiffener may also be subjected to an

external load, in which case it should also satisfy the requirements for a load-carrying stiffener.

#### **17.4.6 Gantry girders**

Plate girders used to support cranes are specifically excluded from utilizing the extra load capacity provided by tension field action. Apart from this limitation, gantry girders are designed using procedures outlined above.

### **17.5 Initial choice of cross-section for plate girders used in bridges** (see also Chapter 4)

#### **17.5.1 Choice of span**

Plate girders are frequently employed to support railway and highway loadings on account of their economic advantages and ease of fabrication and are considered suitable for spans in the region of 25–100 m. Plate girders are considered when rolled sections are not big enough to carry the loads over the chosen span.

Spans are usually fixed by site restrictions and clearances. If there is freedom for the designer, simply-supported spans within the range of 25–45 m will be found to be appropriate; the optimum for continuous spans is about 45 m, as 27 m long *span* girders can be spliced with *pier* girders 18 m long. However, plate girders can be employed for spans of up to about 100 m in continuous construction.

#### **17.5.2 Span-to-depth ratios**

For supporting highways, a composite concrete decking, having a concrete thickness in the region of 250 mm is commonly employed. A span-to-depth ratio of 20 for simply-supported spans serves as an initial choice for such girders; where continuous spans are employed, the depth of the girder can be reduced at least by one-third, compared with a simply-supported span.

Through girders of constant depth are rarely employed in continuous construction. For simply-supported plate girders designed for highway loading, a span-to-depth ratio of 20 can serve as an initial choice; for through girders supporting railway loading, larger depths are required, hence a (span-to-depth) ratio of 15 is more appropriate. Variable depth plate girders are more appropriate when spans in excess of 30 m are required.

For continuous girders in composite construction, a (span-to-depth) ratio of 25 at the pier and 40 at mid-span is suitable. For highway bridges provided with an orthotropic deck, the corresponding values are increased to 30 and 60 respectively.

**Table 17.2** Guide for selection of deck thickness

| Transverse girder spacing (m) | Deck   | Thickness (mm)               |
|-------------------------------|--|------------------------------|
| 2.5–3.8                       | Reinforced concrete slab on permanent formwork | Constant 225–275             |
| 3.3–5.5                       | Haunched slab                                  | Min. 250 up to 350 at haunch |
| 5.0–7                         | Stringer                                       | Constant 225–275             |
| 6.5+                          | Cross girders                                  | Typically 250                |

### 17.5.3 Initial sizing of flange proportions

It is important to keep the flanges as wide as possible consistent with outstand limitations. The outstand should not ordinarily be wider than 12 times its thickness if the flange is fully stressed in compression, or 16 times its thickness if the flange is not fully stressed or is in tension. This ensures that the flange is stable during erection with the minimum number of bracings. For practical reasons, e.g. to accommodate detailing for certain types of permanent formwork, it is desirable to use a minimum flange width of 400 mm. A maximum flange thickness of 65 mm is recommended to avoid heavy welds and the consequent distortion.

Changes in the width of the top flange can be incorporated easily in composite decks to suit design requirements and these do not invite criticism on appearance grounds. On the other hand, changes in widths of bottom flanges are less acceptable visually. In any case it is desirable not to change flange sizes frequently lest the economy achieved by saving in material should be offset by expensive butt welding.

For composite girders having concrete decks it is usually necessary to allow for at least two rows of shear connectors on top flanges of beams; for longer spans three rows may be required at piers where high shear transfer takes place.

The cross sections chosen affect deck thickness and overall structural form. The guide in Table 17.2 is useful for initial selection of deck thickness.

### 17.5.4 Initial sizing of the webs

The thickness of web chosen for initial sizing is related to stiffening. There is no special advantage in using too slender a web, as the material saved will have to be replaced by stiffening; moreover, the workmanship with a thicker web plate is often superior. Probably the biggest single problem when determining the girder layout for a concrete decked plate girder road bridge is to achieve a solution with



**Table 17.3** Initial values of web thickness

| Beam depth (mm) | Web thickness (mm) |
|-----------------|--------------------|
| Up to 1200      | 10                 |
| 1200–1800       | 12                 |
| 1800–2250       | 15                 |
| 2250–3000       | 20                 |

Consideration should also be given to the economy of providing thicker webs, without any intermediate stiffening.

optimum transverse deck spans and minimum cost of web steel, as this involves the balancing of weight against workmanship.

The following advice is intended as general guidance:

- (1) Two or three vertical stiffeners should be provided at, say, 1 m centres close to the bearings; thereafter, their spacing should be increased to  $1.5 \times$  girder depth.
- (2) Generally speaking, horizontal stiffeners should be avoided. In long-span continuous plate girders they may be necessary in locations close to the piers.
- (3) It is desirable to provide vertical stiffeners on one side and horizontal stiffeners on the other side, where possible.
- (4) The initial values for web thickness are suggested in Table 17.3, if it is intended to provide web stiffening. Consideration should also be given to the economy of providing thicker webs, without any intermediate stiffening.
- (5) Compact girders are more economical for most simply-supported spans and shorter continuous spans; economical plate girders for longer continuous spans will be non-compact.

## 17.6 Design of steel bridges to BS 5400: Part 3

The Code requires that the global analysis of the structure should be carried out elastically to determine the load effects (i.e. bending moments, shear forces, etc.). The section properties to be used will generally be those of the gross section. (See clauses 7.1 and 7.2 of the Code.<sup>2</sup>)

Plastic analysis of the structure (i.e. redistribution of moments due to plastic hinge formation) is *not* allowed under BS 5400: Part 3.

Analysis should be carried out for individual and unfactored load cases. Summation of the load effects in different combinations and with different load factors can then be carried out in tabular form, as required by the design process.

### 17.6.1 Design of beams at the ultimate limit state

In the design of beam cross sections at the ultimate limit state the following need to be considered:

- (1) Material strength
- (2) Limitations on shape on account of local buckling of individual elements (i.e. webs and flanges)
- (3) Effective section (reductions for compression buckling and holes)
- (4) Lateral torsional buckling
- (5) Web buckling (governed by depth-to-thickness ratio of web and panel size)
- (6) Combined effects of bending and shear

#### 17.6.1.1 *Material strength* (clause 4.3)

The nominal material strength is the yield stress of steel. The partial factor on strength,  $\gamma_m$ , depends on the structural component and behaviour; generally it is 1.05 at the ultimate limit state, but higher values are specified in the Code for compressive stress in bending or buckling.

#### 17.6.1.2 *Shape limitations* (clause 9.3)

The capacity of a section can be limited by local buckling if the flange outstand-to-thickness ratio is large. The Code limits this ratio so that local buckling will not govern (Chapter 13 discusses local buckling in detail). Similarly, limits are given for outstands in tension to limit local shear-lag effects.

Where the compression region of a web without stiffeners has a very large depth-to-thickness ratio (i.e.  $> 68$ ) the bending capacity of the section is modified by the requirement that webs are effectively reduced to take account of local buckling. Webs with longitudinal stiffeners are not so reduced.

When calculating the bending resistance of beams, it is important to recognize the contribution made by the webs and make appropriate provision for it in computing the modulus of the 'effective section'. Slender webs without horizontal stiffeners buckle in the compression zone, when subjected to high bending stresses. Based on parametric studies, the bending resistance contributed by the web (associated with a flange) is assessed by reducing the thickness of the web using the formula:

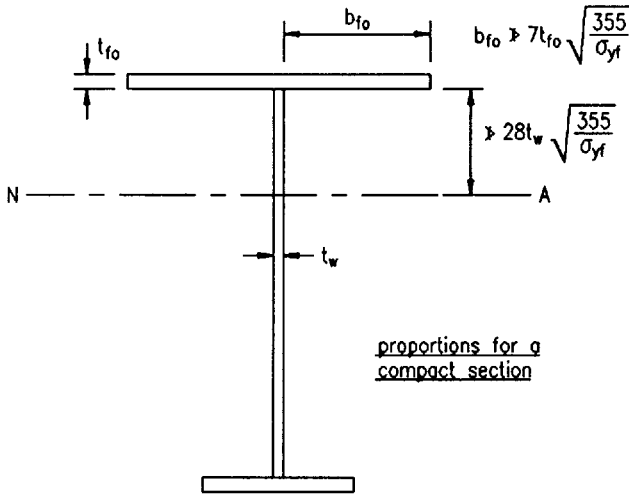


Fig. 17.9 Section classification

$$\frac{t_{we}}{t_w} = 1 \quad \text{if } \frac{y_c}{t_w} \left( \frac{\sigma_{yw}}{355} \right)^{\frac{1}{2}} \leq 68$$

$$\frac{t_{we}}{t_w} = \left[ 1.425 - 0.00625 \frac{y_c}{t_w} \left( \frac{\sigma_{yw}}{355} \right)^{\frac{1}{2}} \right] \quad \text{if } 68 < \frac{y_c}{t_w} \left( \frac{\sigma_{yw}}{355} \right)^{\frac{1}{2}} < 228$$

$$\frac{t_{we}}{t_w} = 0 \quad \text{if } \frac{y_c}{t_w} \left( \frac{\sigma_{yw}}{355} \right)^{\frac{1}{2}} \geq 228$$

where  $y_c$  is the depth of the web measured in its plane from the elastic neutral axis of the gross section of the beam to the compressive edge of the web.

The Code further defines cross sections as *compact* or *non-compact* and a different design approach is required for each classification.<sup>6</sup>

The classification of a section depends on the width-to-thickness ratio of the elements of the cross section considered, as shown in Fig. 17.9 for a compact plate girder.

A compact cross section can develop the full plastic moment capacity of the section (i.e. a rectangular stress block) and *local buckling of the individual elements of the cross section will not occur before this stage is reached* (see Fig. 17.10).

In a non-compact section, however, *local buckling of elements of the cross section may occur before the full moment capacity is reached* and hence the design of such sections is limited to first yield on the extreme fibre (i.e. triangular stress block) (see Fig. 17.11).

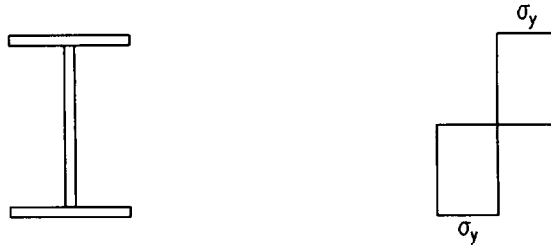


Fig. 17.10 Design stresses for compact sections



Fig. 17.11 Design stresses for non-compact sections

These classifications can best be illustrated by considering a beam in fully restrained bending. This gives the idealized moment capacity of the cross sections as:

$$\begin{array}{ll} \text{compact sections} & M_1 = Z_{pe} \sigma_y / \gamma_m \gamma_f \\ \text{non-compact sections} & M_1 = Z \sigma_y / \gamma_m \gamma_f \end{array}$$

where  $\sigma_y$  is the yield stress;  $Z_{pe}$  is the plastic modulus;  $Z$  is the elastic modulus;  $\gamma_m$  is the partial factor on strength; and  $\gamma_f$  is the partial factor on loads, reflecting uncertainty of loads.

The use of the plastic modulus for compact sections does not imply that plastic analysis can be employed. In fact, it is specifically excluded by BS 5400: Part 3. The achievement of a rectangular stress block does not necessarily mean that there has been redistribution of moments along the member.

### 17.6.1.3 Lateral torsional buckling (clause 9.6)

Where a member has portions of its length with unrestrained elements in compression, lateral torsional buckling may occur (see Fig. 17.12 and section 16.3.6).

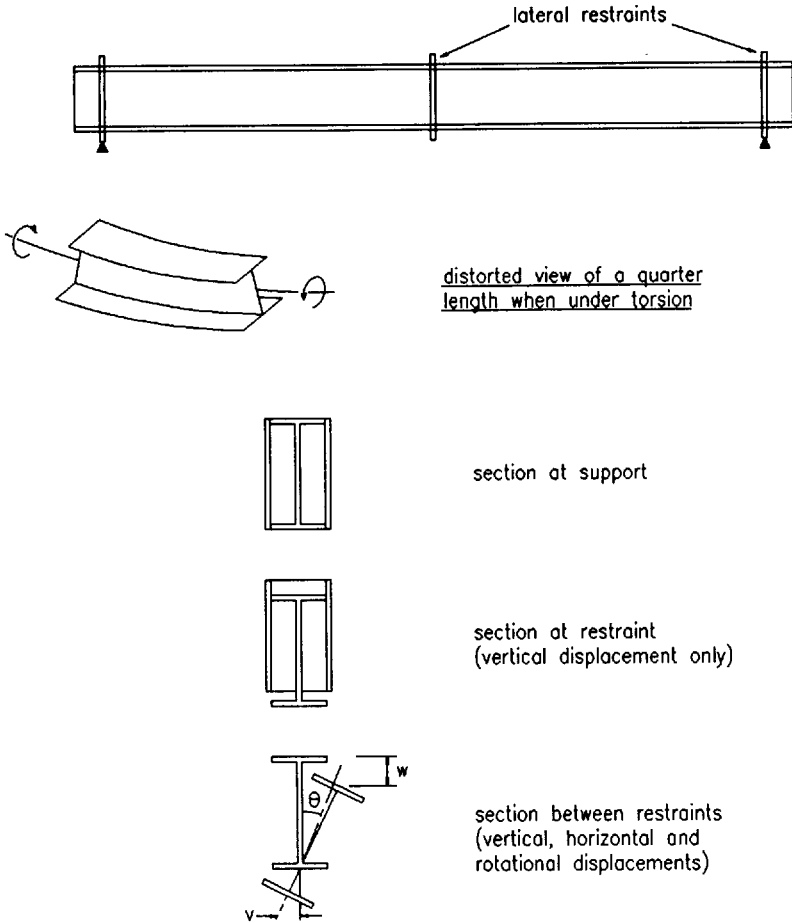


Fig. 17.12 Lateral torsional buckling

The Code deals with these effects by the use of a slenderness parameter  $\lambda_{LT}$  which is a modified form of the ratio  $L_c/r_y$ .

$$\lambda_{LT} = \frac{L_c}{r_y} K_4 \eta \nu$$

where  $L_c$  is the effective length for lateral torsional buckling;  $r_y$  is the radius of gyration of the whole beam about its  $yy$  axis;  $K_4$  is a torsion factor (taken as 0.9 for rolled I or channel sections or 1.0 for all other sections);  $\eta$  is a factor that takes account of moment gradient, i.e. shape of moment diagram; it takes account of the fact that a uniform moment over the unrestrained length will cause buckling more readily than a non-uniform moment; and  $\nu$  is a torsion factor dependent on the shape of the beam.

The process of calculating the value of the limiting compressive stress,  $\sigma_c$ , from the value  $\lambda_{LT}$  is described in the Code.

Portions of beams between restraints can deflect downwards and sideways and rotate. Failure may then occur before the full moment capacity of the section is reached. The possibility of this type of failure is dictated by the unrestrained length of the compression flange, the cross section geometry of the beam and the moment gradient.

#### 17.6.1.4 *Shear buckling* (clause 9.9.2)

This phenomenon becomes significant in webs with depth-to-thickness ratios greater than about 80.

The actual shear strength of a web panel is dependent on

- (1) Yield stress (suitably factored)
- (2) Depth-to-thickness ratio of web
- (3) Spacing of stiffeners
- (4) Conditions of restraint provided by flanges.

The web of a plate girder between stiffeners acts similarly to the diagonal of a Pratt truss (this phenomenon known as tension field action has already been described in section 17.4.4.2). The theory stipulates that the web will resist the applied loading in *three* successively occurring stages (see Fig. 17.4):

Stage 1 A pure shear field

Stage 2 A diagonal tension field

Stage 3 A collapse mechanism due to the formation of hinges in the flanges.

In BS 5400: Part 3, the theory explained in section 17.4.4.2 is slightly modified for the design of steel bridges. In slender web panels, the limit of stage 1, i.e. the pure shear field, is reached when the applied shear stress reaches the elastic critical stress,  $\tau_c$ . To allow for the effects of residual stresses and initial imperfections in stocky plates, a limiting value,  $\tau_1$ , is taken less than  $\tau_c$  when  $\tau_c$  is greater than 0.8 times the yield stress in shear ( $\tau_y$ ), and equal to  $\tau_y$  when  $\tau_c$  exceeds 1.5 times  $\tau_y$ .

The elastic critical stress for a plate loaded in shear,  $\tau_c$ , is given by:

$$\tau_c = K \frac{\pi^2 E}{12 (1 - \mu^2)} \left( \frac{t_w}{d_{we}} \right)^2$$

where

$$K = 5.34 + \frac{4}{\phi^2} \quad \text{when } \phi \geq 1$$

$$\text{and } K = 4 + \frac{5.34}{\phi^2} \quad \text{when } \phi < 1$$

$$\phi = \text{aspect ratio} = \frac{a}{d_{we}}$$

The criteria outlined previously have been incorporated in computing the value of  $\tau_c$ :

$$\begin{aligned} \frac{\tau_c}{\tau_y} &= \frac{904}{\beta^2} && \text{when } \beta \geq 33.62 \\ &= 1 && \text{when } \beta \leq 24.55 \\ &= 1.54 - 0.022\beta && \text{when } 24.55 < \beta < 33.62 \end{aligned}$$

where  $\beta = \frac{\lambda}{K^{\frac{1}{2}}}$

$$\text{and } \lambda = \frac{d_{we}}{t_w} \left( \frac{\sigma_{yw}}{355} \right)^{\frac{1}{2}}$$

In stage 2, a tensile membrane stress field develops in the panel, the direction of which does not necessarily coincide with the diagonal of the panel. The maximum shear capacity is reached in stage 3, when the pure shear stress,  $\tau_1$ , of stage 1 and the membrane stress,  $\sigma_t$ , of stage 2 cause yielding of the panel according to the von Mises yield criterion *and* plastic hinges are formed in the flanges.

The magnitude of the membrane tensile stress,  $\sigma_t$ , in terms of its *assumed* direction  $\theta$  and the first stage limiting stress,  $\tau_1$ , is given by:

$$\frac{\sigma_t}{\tau_y} = \left[ 3 + (2.25 \sin^2 2\theta - 3) \left( \frac{\tau_c}{\tau_y} \right)^2 \right]^{\frac{1}{2}} - 1.5 \frac{\tau_c}{\tau_y} \sin 2\theta$$

Adding the resistance in the three stages, the ultimate shear capacity is obtained as:

$$\frac{\tau_u}{\tau_y} = \left[ \frac{\tau_c}{\tau_y} + 5.264 \sin \theta \left( m_{tw} \frac{\sigma_t}{\tau_y} \right)^{\frac{1}{2}} + \frac{\sigma_t}{\tau_y} (\cot \theta - \phi) \sin^2 \theta \right]$$

$$\text{when } m_{tw} \leq \frac{\phi^2}{4\sqrt{3}} \frac{\sigma_t}{\tau_y} \sin^2 \theta$$

$$\frac{\tau_u}{\tau_y} = \left[ \frac{4\sqrt{3} m_{tw}}{\phi} + \frac{\sigma_t}{2\tau_y} \sin^2 \theta + \frac{\tau_c}{\tau_y} \right]$$

$$\text{when } m_{tw} > \frac{\phi^2}{4\sqrt{3}} \frac{\sigma_t}{\tau_y} \sin^2 \theta$$

To provide an added measure of safety in respect of slender webs, the above values are multiplied by a varying correction factor,  $f$ , to obtain the limiting shear stress.

$$\begin{aligned}
 f &= 1 && \text{when } \lambda \leq 56 \\
 f &= \frac{1.15}{1.35} && \text{when } 56 < \lambda < 156 \\
 f &= \frac{1.15}{1.15 + 0.002(\lambda - 56)} && \text{when } \lambda \geq 156
 \end{aligned}$$

The value of  $\frac{\tau_1}{\tau_y}$  is taken as the lower of  $\left(\frac{\tau_u}{\tau_y}\right)$ , computed as given above, and 1.0.

The term  $m_{fw}$  in the above equations is a non-dimensional representation of plastic moment of resistance of the flange (taking the smaller value at the top and bottom flanges, ignoring any concrete).

$$\begin{aligned}
 m_{fw} &= \frac{M_p}{d_{wc}^2 t_w \sigma_{yw}} \\
 &= \frac{\sigma_{yf} b_{fe} t_f^2}{2d_{wc}^2 t_w \sigma_{yw}}
 \end{aligned}$$

Values of  $\left(\frac{\tau_1}{\tau_y}\right)$  versus  $\lambda$  are plotted in Figures 11–17 of the Code corresponding to various values of  $m_{fw}$  and  $\phi$ . These can be used directly by designers.

The term  $b_{fe}$  is the width of flange associated with the web and is limited to

$$10t_f \left(\frac{355}{\sigma_{yf}}\right)^{\frac{1}{2}}$$

Where two flanges are unequal, the value of  $m_{fw}$  is conservatively taken as that corresponding to the weaker flange; moreover only a section symmetric about the mid-plane is taken as effective and any portion of the flange plate outside this plane of symmetry is ignored so that complexities due to the torsion of the flange are eliminated.

The above procedure has to be repeated for several values of  $\theta$  and the highest value of  $\tau_u/\tau_y$  is to be used. From parametric studies it has been established that  $\theta$  is never less than  $(1/3) \cot^{-1} \phi$  or more than  $(4/3) \cot^{-1} \phi$ .

When tension field action is used, consideration must be given to the anchorage of the tension field forces created in the end panels and special procedures must be adopted for designing the end stiffener.

### 17.6.1.5 *Combined bending and shear* (clause 9.9.3)

The Code has simplified the procedure for girders *without* longitudinal stiffeners by allowing shear and bending capacities to be calculated independently and then combined by employing an interaction relationship on the basis given below:



- (1) The bending capacity of the whole section is determined with and without contribution from the web ( $M_1$  and  $M_R$  respectively).
- (2) The shear capacity using the tension field theory discussed above is determined with and without contribution from the flanges ( $V_D$  and  $V_R$  respectively).
- (3) The bending and shear capacities without any contribution from the web and flanges respectively ( $M_R$  and  $V_R$ ) can be mobilized simultaneously.
- (4) The pure bending capacity of the whole section,  $M_D$ , can be obtained even when there is a coincident shear on the section provided the latter is less than  $\frac{1}{2}V_R$ . Similarly the theoretical design shear capacity,  $V_D$ , of the whole beam section is attained even if the coexisting bending moment is not greater than  $\frac{1}{2}M_R$ .

The interaction relationship is linear between this set of values of shear force and bending moment and is shown graphically in Fig. 17.13. In this figure,  $V_D$  and  $M_D$  represent capacity in shear and bending;  $V_R$  is the shear capacity ignoring flange contribution; and  $M_R$  is the bending capacity ignoring web contribution, i.e. flange capacity  $\times$  depth.

The important feature from the designer's point of view is that full values of calculated bending capacity can be utilized in the presence of a moderate magnitude of shear.

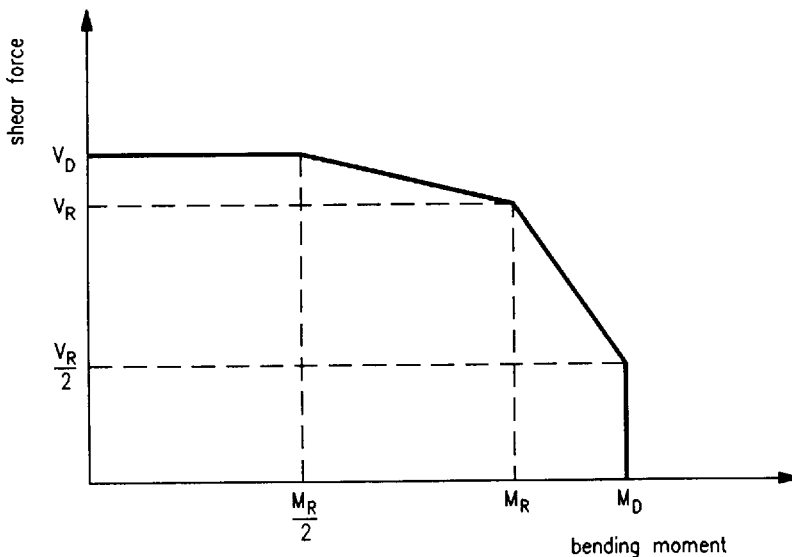


Fig. 17.13 Interaction between shear and bending resistances

For girders with longitudinal stiffeners, account is taken of the combined effects of bending and shear by the comparison of the stresses in the web panels with the relevant critical buckling strength of the panel. The buckling coefficients are based upon large-deflection elastic-plastic finite element studies. An interaction expression is then used which is based on an equivalent stress check. This makes suitable allowance for webs with longitudinal stiffeners and having large depth-to-thickness ratios: no reduction need be made to account for local buckling.

#### **17.6.1.6 Bearing stiffeners** (clause 9.14)

BS 5400: Part 3 requires such stiffeners to be provided at supports. The design forces to be applied to the stiffener include the direct reaction from the bearing (less the force component in the flange if the beam soffit is haunched), a force to account for the de-stabilizing effect of the web, forces from any local cross bracing (including forces from restraint system) and a force due to tension field. The derivation of these is far more precise and lengthy than BS 5950: Part 1 requires, largely because plate girders in bridges are usually part of a much more complex structural system than in buildings.

Bearing stiffeners are almost always placed symmetrically about the web centre-line. Stiffeners that are symmetrical about the axis perpendicular to the web, i.e. flats or tees rather than angles, are preferred.

#### **17.6.1.7 Intermediate stiffeners** (clause 9.13)

Intermediate stiffeners are usually placed on one side of the web only. Standard flat sizes should be used. BS 5400: Part 3 does not prescribe stiffness criteria for intermediate stiffeners (which have an associated length of web), but it does prescribe design forces for which these stiffeners are designed similar to those outlined for bearing stiffeners.

### **17.6.2 Design of beams at the serviceability limit state**

In practice, due to the proportions of partial safety factors at the ultimate and serviceability limits, the serviceability check on the steel section is automatically satisfied if designs are satisfactory at the ultimate stage.

The design of beams is carried out using an elastic distribution throughout the cross section in a manner generally similar to that used at the ultimate limit but with different partial safety factors, i.e. different values of  $\gamma_{FL}$ ,  $\gamma_m$  and  $\gamma_F$ . The determination of effective section must take account of shear lag, where appropriate.

Stresses should be checked at critical points in the steel member to ensure that no permanent deformation due to yielding takes place.<sup>7,8,9</sup> Plastic moment capacity is not considered at the serviceability limit state.

In composite construction, crack widths of concrete deck may often govern the design at serviceability limit state. For non-compact sections, because the analysis at the ultimate limit state has been carried out using a triangular stress distribution (i.e. an elastic distribution), the serviceability limit check is always satisfied for bending analysis, as these factors are less than the ultimate limit state. The Code lists the clauses which require checking at both limit states.

### **17.6.3 Fatigue**

Fatigue should be checked with reference to BS 5400: Part 10. Generally it is only bracing connections, stiffeners and shear connectors and their welding to the girders that have to be checked for fatigue. The details of the connection have a significant effect on the fatigue life and by careful detailing fatigue may be 'designed out' of the bridge.

### **17.6.4 Design format**

One of the significant features of BS 5400: Part 3 is that plastic redistribution across the section is now permitted in certain circumstances prior to the attainment of the ultimate limit state. Such redistributions are, of course, much less than those permitted in simple plastic design for buildings, but they can give a considerable enhancement in strength.

For example, design bending strength is based on plastic section modulus for compact sections, and the basic shear strength is based on rules which take account of tension field action, which only develops in the presence of considerable plasticity.

In addition, the interaction between shear strength and bending strength of a cross section is empirically based and also implicitly assumes that plastic strains may occur prior to the attainment of design strength.

Finally, the design strength of compact sections that are built in stages assumes that a redistribution of stresses may take place within the cross-section; thus the ultimate limit state check for the completed structure is simply to ensure that the bending resistance (given by the limiting stress times the plastic section modulus divided by partial factors) is greater than the maximum design moment (obtained by summing all the moments due to the various design loads).

This recognition of the reserve strength beyond first yield is limited to situations where plasticity may be permitted safely. The principal limitations are as follows:

- (1) Plastic section moduli may only be used for compact sections, i.e. those that can sustain local compressive yielding without any local buckling.
- (2) Where the structure is built in stages and is non-compact, plasticity is permitted implicitly only in considering the interaction between bending and shear strength.
- (3) Where longitudinal stiffeners are present, neither plastic section modulus nor plastic bending/shear interaction may be used.
- (4) If flanges are curved in elevation, similar restrictions to (3) apply.


### References to Chapter 17

1. British Standards Institution (1990) *Structural use of steelwork in building. Part 1: Code of practice for design in simple and continuous construction: hot rolled sections*. BS 5950, BSI, London.
2. British Standards Institution (1982) *Steel, concrete and composite bridges. Part 3: Code of practice for the design of steel bridges*. BS 5400, BSI, London.
3. Owens, G.W. (1989) *Design of Fabricated Composite Beams in Buildings*. The Steel Construction Institute, Ascot, Berks.
4. Evans H.R. (1988) Design of plate girders. In *Introduction to Steelwork Design to BS 5950: Part 1*, pp. 12.1–12.10. The Steel Construction Institute, Ascot, Berks.
5. Lawson R.M., Rackham J.W. (1989) *Design for Openings in Webs of Composite Beams*. The Steel Construction Institute, Ascot, Berks.
6. Chatterjee S. (1981) Design of webs and stiffeners in plate and box girders. In *The Design of Steel Bridges* (Ed. by K.C. Rockey & H.R. Evans), Chapter 11. Granada.
7. Iles D.C. (1989) *Design Guide for Continuous Composite Bridges 1: Compact Sections*. SCI Publication 065, The Steel Construction Institute, Ascot, Berks.
8. Iles D.C. (1989) *Design Guide for Continuous Composite Bridges 2: Non-Compact Sections*. SCI Publication 066, The Steel Construction Institute, Ascot, Berks.
9. Iles D.C. (1991) *Design Guide for Simply Supported Composite Bridges*. The Steel Construction Institute, Ascot, Berks.

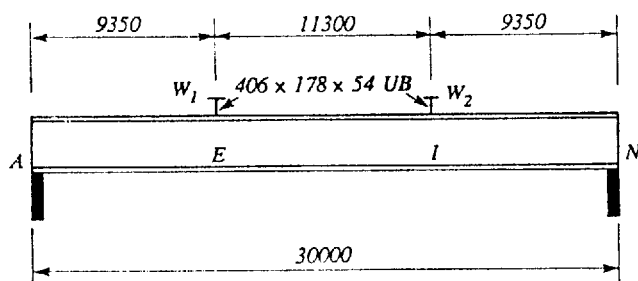
### Further reading for Chapter 17

References 3, 4, 7, 8 and 9 are recommended wider reading.

A worked example follows which is relevant to Chapter 17.

|   |                                      |  |                           |
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The girder shown is fully restrained throughout its length. For the loading shown design a stiffened plate girder in Grade 43 steel. Girder depth is unrestricted.



$$w = w_d + w_i$$

$$W_1 = W_{1d} + W_{1i}$$

$$W_2 = W_{2d} + W_{2i}$$

**Loading**

*Dead loads:*

UDL  $w_d = 20 \text{ kN/m}$

Point load  $W_{1d} = 200 \text{ kN}$


Point load  $W_{2d} = 200 \text{ kN}$

*Imposed loads:*

UDL  $w_i = 40 \text{ kN/m}$

Point load  $W_{1i} = 300 \text{ kN}$

Point load  $W_{2i} = 300 \text{ kN}$

|   |                                      |  |                           |
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**Load factors**

**Dead load factor**       $\gamma_{fd} = 1.4$

**2.4.1.1  
Table 2**

**Imposed load factor**       $\gamma_{fi} = 1.6$

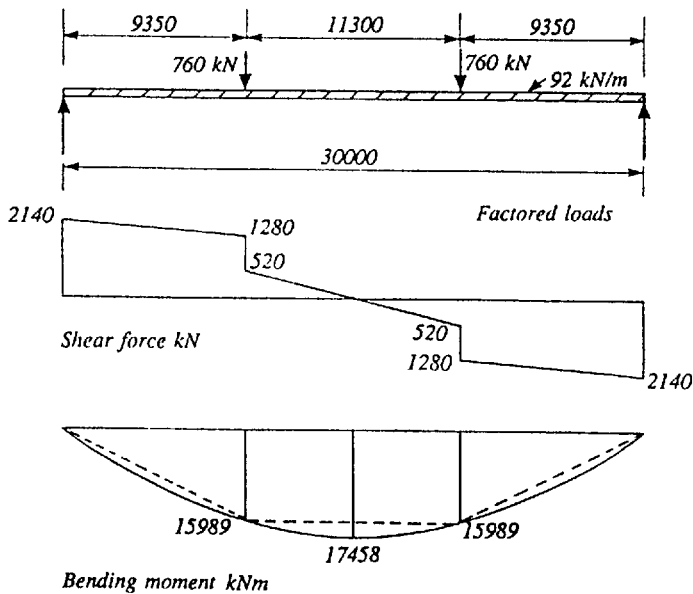
**Factored loads**


$$w' = w_d \times \gamma_{fd} + w_i \times \gamma_{fi} = 20 \times 1.4 + 40 \times 1.6 = 92 \text{ kN/m}$$

$$W_1' = W_{1d} \times \gamma_{fd} + W_{1i} \times \gamma_{fi} = 200 \times 1.4 + 300 \times 1.6 = 760 \text{ kN}$$

$$W_2' = W_{2d} \times \gamma_{fd} + W_{2i} \times \gamma_{fi} = 200 \times 1.4 + 300 \times 1.6 = 760 \text{ kN}$$

*The design shear forces and moments are shown below:*



|   |                                       |  |                           |
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Initial sizing of plate girder

The recommended span/depth ratio for simply supported non-composite girders varies between 12 for short span girders and 20 for long span girders. Here the depth will be assumed to be one-fifteenth of the span.

$$\text{Depth, } D \approx \frac{\text{span}}{15} = \frac{30000}{15} = 2000 \text{ mm}$$

Single flange area, (assuming  $p_y = 255 \text{ N/mm}^2$ , see Table 6)

$$A_f \approx \frac{M_{\max}}{D p_y} = \frac{17458}{2000 \times 255} \times 10^6 \quad 4.4.4.2(a)$$

$$\therefore A_f \approx 34232 \text{ mm}^2$$

For non-composite girders, the flange width chosen is usually within a range of 0.3 to 0.5 of the depth of the section (0.4 is more common). Suggest  $700 \times 50 = 35000 \text{ mm}^2$ .

Minimum web thickness for plate girders in buildings usually varies between 10 mm for girders up to 1200 mm deep to 20 mm for those of 2500 mm deep. Here the web thickness  $t$ , will be chosen as 14 mm.

Try girder with flanges of 700 mm × 50 mm thick and web 2000 mm × 14 mm thick


Section classification

Flange

For  $T = 50 \text{ mm}$  Table 6

$$p_y = p_{yf} \quad p_{yf} = 255 \text{ N/mm}^2$$

$$\epsilon = \left[ \frac{275}{p_y} \right]^{1/2} \quad \epsilon = \left[ \frac{275}{255} \right]^{1/2} = 1.04 \quad \text{Table 7 Note 3}$$

|  |                                      |  |                           |
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*Outstand,  $b = \frac{B - t}{2} = \frac{700 - 14}{2} = 343 \text{ mm}$*  *Fig 3*

$\frac{b}{T} = \frac{343}{50} = 6.86$

*Compact limiting value of  $b/T$  for outstand of welded section is  $8.5 \epsilon$*  *Table 7*

$8.5 \epsilon = 8.5 \times 1.04 = 8.84$

$6.86 < 8.84$

$\therefore$  *Flange is compact*

Web

*For  $t = 14 \text{ mm}$*  *Table 6*

$p_y = p_{yw} \quad p_{yw} = 275 \text{ N/mm}^2$

$\epsilon = \left[ \frac{275}{p_y} \right]^{1/2} \quad \epsilon = \left[ \frac{275}{275} \right]^{1/2} = 1.00$  *Table 7*  
*Note 3*

$\frac{d}{t} = \frac{2000}{14} = 142.8$

$120 \epsilon = 120$


$142.8 > 120$  *Table 7*


$\therefore$  *the web is slender*

*since  $\frac{d}{t} > 63\epsilon \quad 142.8 > 63$*  *Table 7*  
*Note 2*

*the web must be checked for shear buckling as given in 4.4.4.2*



|  |   |   |                                      |
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| <p><u>Dimension of webs and flanges</u></p>  |   |   | <p><b>4.4.2</b></p>                  |
| <p>Assuming stiffener spacing, <math>a &gt; d</math></p>   |   |   | <p><b>4.4.2.2</b></p>                |
| $t \geq \frac{d}{250} \quad \frac{d}{250} = \frac{2000}{250} = 8.0 \text{ mm}$   |   |   | <p><b>4.4.2.2(b)(1)</b></p>          |
| <p>since <math>t &gt; \frac{d}{250} \quad 14 &gt; 8.0</math></p>   |   |   |                                      |
| <p>web is adequate for serviceability</p>  |   |   |                                      |
| <p>Assuming stiffener spacing, <math>a &gt; 1.5d</math></p>  |   |   | <p><b>4.4.2.3</b></p>                |
| $t \geq \frac{d}{250} \times \frac{p_{yf}}{345} = 8.0 \times \frac{255}{345} = 5.9 \text{ mm}$   |   |   | <p><b>4.4.2.3(b)(1)</b></p>          |
| <p>since <math>t = 14 \text{ mm} &gt; 5.9 \text{ mm}</math></p>  |   |   |                                      |
| <p>the web is adequate to avoid flange buckling into web</p>   |   |   |                                      |
| <p>For sections with slender webs (and flanges which are not slender) three methods of design are given. Method (2) will be used in this example. The moment is assumed to be resisted by the flanges alone and the web designed for shear only.</p> |   |   | <p><b>4.4.4.2</b></p>                |
| <p><u>Moment capacity of the section ignoring the web</u></p>  |   |   |                                      |
| $M_c = p_{yf} \times A_f \times h_s$   |   |   |                                      |
| $p_{yf} = 255 \text{ N/mm}^2$  |   |   |                                      |
| $h_s = \text{distance between centroid of flanges}$  |   |   |                                      |
| $h_s = d + T = 2000 + 50 = 2050 \text{ mm}$  |   |   |                                      |
| $A_f = B \times T = 700 \times 50 = 35000 \text{ mm}^2$  |   |   |                                      |

|  |   |                                      |  |
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$$\therefore M_c = 255 \times 35000 \times 2050 \times 10^{-6}$$

$$M_c = 18296 \text{ kNm}$$

Maximum design moment,  $M = 18296 \text{ kNm}$

Since  $M_c > \text{Moment at G}$   $18296 > 17458 \text{ kNm}$

section is adequate for carrying the moment

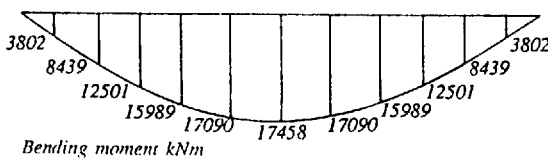
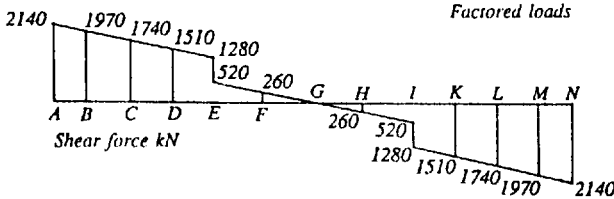
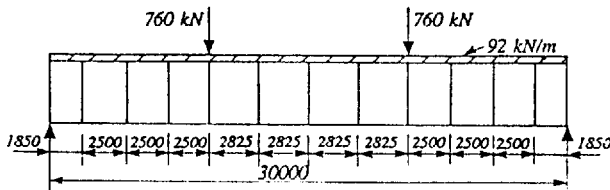
Web design for shear only


4.4.5


Webs with intermediate stiffeners may be designed according to 4.4.5.3 or 4.4.5.4.

Although the Code allows three alternative methods for providing stiffeners (see Clauses 4.4.5.4.2 and 4.4.5.4.3), the most commonly employed method consists of designing end panels without accounting for tension field action (Clause 4.4.5.4.2). This method is illustrated in this worked example.

Try the stiffener spacing shown below:



|  |                                      |  |                           |
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| <p><u>Consider end panel AB</u> <span style="float: right;">4.4.5.4.2</span></p> <p><math>d = 2000 \text{ mm}</math></p> <p><math>t = 14 \text{ mm}</math></p> <p>Maximum shear stress in the panel</p> $f_v = \frac{F_{v,A}}{dt}$ $f_v = \frac{2140 \times 10^3}{2000 \times 14} = 76.43 \text{ N/mm}^2$ $\frac{a}{d} = \frac{1850}{2000} = 0.925$ $\frac{d}{t} = \frac{2000}{14} = 142.8$ $p_y = 275 \text{ N/mm}^2$ <p>Critical shear strength, <math>q_{cr} = 94.22 \text{ N/mm}^2</math> <span style="float: right;">Table 21b</span></p> <p>Since <math>f_v &lt; q_{cr}</math> <span style="margin-left: 100px;"><math>76.43 &lt; 94.22</math></span></p> <p><math>\therefore</math> <u>Tension field action need not be utilized for design.</u></p> <p>End panel AB should also be checked as a beam spanning between the flanges of the girder capable of resisting a shear force <math>R_{lf}</math> and a moment <math>M_{lf}</math> due to anchor forces. <span style="float: right;">Fig 5</span></p> $R_{lf} = \frac{H_q}{2}$ <span style="float: right;">4.4.5.4.4</span> $M_{lf} = \frac{H_q d}{10}$ |                                      |  |                           |

|  |                                      |  |                           |
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$$H_q = 0.75 d t p_y \left[ 1 - \frac{q_{cr}}{0.6 p_y} \right]^{1/2}$$

$$q_{cr} = 94.22 \text{ N/mm}^2$$

$$H_q = 0.75 \times 2000 \times 14 \times 275 \times \left[ 1 - \frac{94.22}{0.6 \times 275} \right]^{1/2} \times 10^{-3}$$

$$H_q = 3782.4 \text{ kN}$$

$$R_{cf} = \frac{3782.4}{2} = 1891.2 \text{ kN}$$

*Although panel AB and its bounding transverse stiffeners act as a beam, spanning vertically between the girder flanges to resist the shear and bending moment arising from the tension field pull of panel BC, the effect of the bounding transverse stiffeners will be disregarded in the following calculations. In cases where the moment  $M_{cf}$  arising from the anchor forces is higher than the moment capacity of the web alone, the moment resistance of the bounding stiffeners should be included in the design.*

Shear capacity of the end panel AB

$$P_v = 0.6 p_{yw} A_v \quad 4.2.3$$


$$A_v = t a$$

*'a' is the distance between the transverse stiffeners making up the end panel*

$$a = 1850 \text{ mm}$$

$$P_v = 0.6 \times 275 \times 14 \times 1850 \times 10^{-3}$$

$$P_v = 4273.5 \text{ kN}$$

|  |                                      |  |                           |
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$$\text{Since } R_{yf} < P_y \quad 1891.2 < 4273.5$$

*the end panel is capable of carrying the shear force*

$$M_{yf} = \frac{H_q d}{10}$$

$$M_{yf} = \frac{3782.4 \times 2000}{10} \times 10^{-3} = 756.5 \text{ kNm}$$

Moment capacity of the end panel AB,  $M_q$

$$M_q = \frac{I}{y} p_y$$

$$I = \frac{1}{12} t a^3 \quad (\text{Stiffeners not included)}$$

$$y = \frac{a}{2} = 925 \quad a = 1850 \text{ mm}$$

$$I = \frac{1}{12} \times 14 \times 1850^3$$

$$I = 738689.6 \times 10^4 \text{ mm}^4$$


$$y = \frac{1850}{2} = 925 \text{ mm}$$

$$M_q = \frac{738689.6 \times 10^4}{925} \times 275 \times 10^{-6}$$

$$M_q = 2196 \text{ kNm}$$

$$\text{Since } M_{yf} < M_q \quad 756.5 < 2196$$

*the end panel is capable of carrying the bending moment.*

|  |                                      |  |                           |
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***Consider panel BC***

***Panel BC will be designed utilizing tension field action*** **Fig 5**

$d = 2000 \text{ mm}$

$t = 14 \text{ mm}$

***Maximum shear stress in the panel***

$$f_v = \frac{F_{v,B}}{dt}$$

$$f_v = \frac{1970}{2000 \times 14} \times 10^3 = 70.36 \text{ N/mm}^2$$

$$\frac{a}{d} = \frac{2500}{2000} = 1.25$$

$$\frac{d}{t} = \frac{2000}{14} = 142.8$$

$$p_y = 275 \text{ N/mm}^2$$

$$q_b = 105.65 \text{ N/mm}^2$$

**Table 22b**

Since  $q_b > f_v$        $105.65 > 70.36$

***panel BC is safe against shear buckling***


***Load bearing stiffener at A*** **Fig 5**

***Design should be made for a compression force due to bearing plus the compression force due to the moment  $M_{lf}$ .*** **4.4.5.4.2**

Design force due to bearing,       $F_b = 2140 \text{ kN}$

Force due to moment  $M_{lf}$ ,  $F_m$

$$F_m = \frac{M_{lf}}{a} = \frac{756.5}{1850} \times 10^3 = 409 \text{ kN}$$

|  |                                      |  |                           |
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*Total compression force,  $F_x = F_b + F_m$*

$F_x = 2140 + 409 = 2549 \text{ kN}$

*Area of stiffener in contact with the flange* 4.5.4.2

$$A > \frac{0.8 F_x}{p_{ys}}$$

$$\frac{0.8 F_x}{p_{ys}} = \frac{0.8 \times 2549}{265} \times 10^3 = 7695 \text{ mm}^2$$

*Try stiffeners consisting of 2 flats 240 mm × 22 mm thick*

For  $t_s = 22 \text{ mm} < 40 \text{ mm}$        $p_{ys} = 265 \text{ N/mm}^2$  Table 6

*Allow 15 mm to cope for the web/flange weld*

$A = 225 \times 22 \times 2 = 9900 \text{ mm}^2 > 7695 \text{ mm}^2$

$\therefore$  *Bearing check is OK*

Check outstands 4.5.1.2


*Outstands from the face of the web should not be greater than  $19 t_s \epsilon$*

$$\epsilon = \left[ \frac{275}{p_y} \right]^{1/2} = \left[ \frac{275}{265} \right]^{1/2} = 1.02$$
 Table 8

*Outstand,  $b_s = 240 \text{ mm}$*

$19 t_s \epsilon = 19 \times 22 \times 1.02 = 425 \text{ mm}$

$b_s < 19 t_s \epsilon$        $240 < 425$       **OK**

|  |   |                                      |  |                           |
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|  |   | Design code<br><b>BSS950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. <b>12</b>       |

Check if  $b_s < 13 t_s \epsilon$

$$13 t_s \epsilon = 13 \times 22 \times 1.02 = 291 \text{ mm}$$

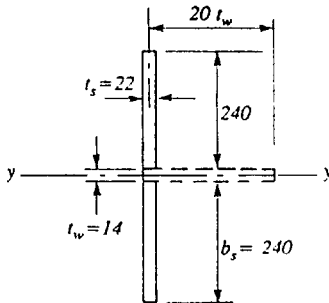
$$b_s < 13 t_s \epsilon \quad 240 < 291 \therefore \text{Satisfactory}$$

Check stiffener for buckling

4.5.1.5

Although the effective section from 4.5.1.5 may be used for providing buckling resistance of stiffeners, here the buckling resistance due to the web will be disregarded. Thus, no moment will occur on the stiffener coming from the eccentricity in the load due to an unsymmetric effective section. But if the required stiffener cross section using this method comes out to be very massive, the effective section should be regarded as a T section and the stiffener designed accordingly.

The effective section of the stiffener is shown below




In the above figure:

\_\_\_\_\_ shows the effective section that will be used in this example.

----- shows the additional area contributed by the web. That section will be disregarded here for simplicity.



|  |                                      |  |                           |
|--|--------------------------------------|--|---------------------------|
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$$I_y = \frac{22 \times 494^3}{12} - \frac{22 \times 14^3}{12}$$

$$I_y = 22101 \times 10^4 \text{ mm}^4$$

$A_E$ : effective area of the stiffener

$$A_E = 240 \times 22 \times 2$$

$$A_E = 10560 \text{ mm}^2$$

$$r_y = \left[ \frac{I}{A} \right]^{1/2}$$

$$r_y = \left[ \frac{22101 \times 10^4}{10560} \right]^{1/2}$$

$$r_y = 144.7 \text{ mm}$$

Flange is restrained against rotation in the plane of the stiffener 4.5.1.5(a)

$$\therefore L_E = 0.7 L = 0.7 \times 2000 = 1400 \text{ mm}$$

$$\lambda = \frac{L_E}{r_y} = \frac{1400}{144.7} = 9.68$$

$$p_y = 265 - 20 = 245 \text{ N/mm}^2 \text{ when using Table 27} \quad 4.7.5$$

for  $p_y = 245, \quad \lambda = 9.68$


$$p_c = 245 \text{ N/mm}^2 \quad \text{Table 27c}$$


$\therefore$  Buckling resistance of the stiffener

$$P_x = p_c A_E = 245 \times 10560 = 2587.2 \text{ kN}$$

Since  $F_x < P_x \quad 2549 < 2587.2$

stiffener is adequate to resist buckling

|   |                                      |  |                           |
|---|--------------------------------------|--|---------------------------|
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|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. <b>14</b>       |
| <b><u>Check stiffener at A as a bearing stiffener</u></b>   |                                      |  | <b>4.5.5</b>              |
| <i>Local capacity of the web</i>  |                                      |  |                           |
| Assume stiff bearing length $b_1 = 0$   |                                      |  |                           |
| $P_{crip} = (b_1 + n_2) t p_{yw}$   |                                      |  | <b>4.5.3</b>              |
| $n_2 = 2.5 \times 50 \times 2 = 250 \text{ mm}$   |                                      |  |                           |
| $P_{crip} = (0 + 250) \times 14 \times 275 \times 10^{-3} = 962.5 \text{ kN}$   |                                      |  |                           |
| Bearing stiffener should be designed for a force, $F_A$   |                                      |  |                           |
| $F_A = F_x - P_{crip} = 2549 - 962.5 = 1586.5 \text{ kN}$   |                                      |  | <b>4.5.5</b>              |
| <i>Bearing capacity of the stiffener alone</i>  |                                      |  |                           |
| $P_A = p_{ys} \times A = 265 \times 9900 = 2623.5 \text{ kN}$   |                                      |  |                           |
| Since $F_A < P_A$ $1586.5 < 2623.5$   |                                      |  |                           |
| Stiffener is OK for bearing.  |                                      |  |                           |
| <b><u>Stiffener at A: Adopt 2 flats 240 mm × 22 mm thick, Grade 43 Steel</u></b>  |                                      |  |                           |
| <b><u>Intermediate stiffeners at B,C,D,F &amp; G</u></b>  |                                      |  | <b>4.4.6</b>              |
| Stiffener at B is the most critical one and will be the design criterion  |                                      |  |                           |
| Minimum stiffness   |                                      |  | <b>4.4.6.4</b>            |
| $I_s \geq 0.75 dt^3 \quad \text{for } a \geq d\sqrt{2}$   |                                      |  |                           |
| $I_s \geq \frac{1.5 d^3 t^3}{a^2} \quad \text{for } a < d\sqrt{2}$  |                                      |  |                           |

|  |                                      |  |                           |
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$$d\sqrt{2} = \sqrt{2} \times 2000 = 2828 \text{ mm}$$

$$\therefore a < d\sqrt{2} \quad 2825 < 2828 \text{ (maximum 'a')}$$

*Note: Conservatively 't' will be taken as the actual web thickness*

$$\frac{1.5d^3t^3}{a^2} = \frac{1.5 \times 2000^3 \times 14^3}{2500^2} = 526.8 \times 10^4 \text{ mm}^4$$

*(conservatively minimum 'a' is used above)*

*Try intermediate stiffener 2 flats 80 mm × 13 mm*

*Note: 13 mm is not a standard thickness but is available*

$$I_s = \frac{13 \times 174^3}{12} - \frac{13 \times 14^3}{12} = 570.4 \times 10^4 \text{ mm}^4 \text{ OK}$$

*Outstand of the stiffener  $\leq 13 t_s \epsilon$  4.5.1.2*

$$13 t_s \epsilon = 13 \times 13 \times 1 = 169 \text{ mm}$$

*Outstand = 80 mm 80 < 169 OK*

*Buckling check on intermediate stiffeners at B, C, D, F & G 4.4.6.6*


*Design force on the stiffener*

$$F_q = V - V_s \quad V = 1970 \text{ kN}$$

$$V_s = V_{cr}$$

$$V_{cr} = q_{cr} d t$$

$$\frac{a}{d} = \frac{2825}{2000} = 1.41 \quad (\text{'a' is conservatively taken as the maximum})$$

|  |   |                                      |  |                           |
|--|---|--------------------------------------|--|---------------------------|
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|  |   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. <b>16</b>       |

$$\frac{d}{t} = \frac{2000}{14} = 142.8$$

$$p_y = 275 \text{ N/mm}^2$$

$$q_{cr} = 67.89 \text{ N/mm}^2$$

*Table 21b*

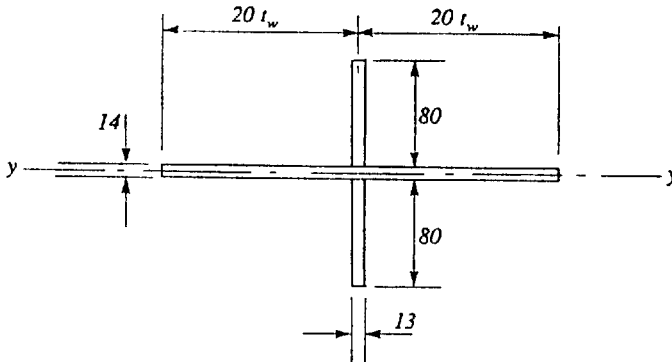
$$V_{cr} = 67.89 \times 2000 \times 14 \times 10^{-3}$$

$$V_{cr} = 1900 \text{ kN}$$

$$F_q = 1970 - 1900 = 70 \text{ kN}$$

**Buckling resistance of the intermediate stiffener at B,  $P_q$**

The effective section is shown below





$$20 t_w = 20 \times 14 = 280 \text{ mm}$$


$$I_y = \frac{13 \times 174^3}{12} + \frac{560 \times 14^3}{12} - \frac{13 \times 14^3}{12} = 583.2 \times 10^4 \text{ mm}^4$$

$$A = 160 \times 13 + 560 \times 14 = 9920 \text{ mm}^2$$

$$r_y = \left[ \frac{583.2 \times 10^4}{9920} \right]^{1/2} = 24.25 \text{ mm}$$

|   |                                      |  |                    |
|---|--------------------------------------|--|--------------------|
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|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. 17       |
| <p> <math>L_E = 0.7 \times 2000 = 1400 \text{ mm}</math> </p> <p> <math>\lambda = \frac{L_E}{r_y} = \frac{1400}{24.25} = 57.7</math> </p> <p>                 for <math>p_y = 255 \text{ N/mm}^2</math>, <math>\lambda = 57.7</math> <span style="float: right;">4.7.5</span> </p> <p> <math>p_c = 192.6 \text{ N/mm}^2</math> <span style="float: right;">Table 27c</span> </p> <p>                 Buckling resistance, <math>P_q = p_c A</math> </p> <p> <math>P_q = 192.6 \times 9920 \times 10^{-3} = 1910.6 \text{ kN}</math> </p> <p>                 Since <math>F_q &lt; P_q</math> <span style="margin-left: 100px;"><math>70 \text{ kN} &lt; 1910.6 \text{ kN}</math></span> </p> <p> <i>intermediate stiffener at B is safe against buckling.</i> </p> <p> <u>Intermediate Stiffener at B, C, D, F &amp; G</u><br/> <u>Adopt 2 flats 80 mm × 13 mm thick, Grade 43 Steel</u> </p> <p> <u>Stiffener at E</u> </p> <p> <i>Intermediate stiffener subject to external load</i> </p> <p>                 Minimum stiffness calculations: <span style="float: right;">4.4.6.5</span> </p> <p> <math>a = 2825 &lt; d\sqrt{2} = 2828</math> </p> <p> <math>\therefore I_s \geq \frac{1.5 d^3 t^3}{a^2} = 526.8 \times 10^4 \text{ as calculated for stiffener at B}</math> </p> <p>                 Try intermediate stiffeners 2 flats 80 mm × 13 mm thick             </p> <p> <math>I_s = 570.4 \times 10^4 \text{ mm}^4 \text{ (from stiffener design at B)}</math> </p> <p> <math>\therefore</math> Satisfactory             </p> |                                      |  |                    |

|  |                                      |  |                           |
|--|--------------------------------------|--|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>PLATE GIRDERS</b>      |  | Chapter ref.<br><b>17</b> |
|  | Design code<br><b>BS5950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. <b>18</b>       |
| <b>Intermediate stiffener subject to external load</b>   |                                      |  | <b>4.4.6.6</b>            |
| $\frac{F_q - F_x}{P_q} + \frac{F_x}{P_x} + \frac{M_s}{M_{ys}} \leq 1$  |                                      |  |                           |
| $F_q = V - V_s \qquad V = 1280 \text{ kN}$   |                                      |  |                           |
| $V_s = V_{cr}$   |                                      |  |                           |
| $V_{cr} = q_{cr} d t$  |                                      |  |                           |
| $\frac{a}{d} = \frac{2825}{2000} = 1.41$   |                                      |  |                           |
| $\frac{d}{t} = \frac{2000}{14} = 142.8$  |                                      |  |                           |
| $p_y = 275 \text{ N/mm}^2$   |                                      |  |                           |
| $q_{cr} = 67.89$   |                                      |  |                           |
| <i>Table 21b</i>   |                                      |  |                           |
| $V_{cr} = 67.89 \times 2000 \times 14 \times 10^{-3}$  |                                      |  |                           |
| $V_{cr} = 1900 \text{ kN}$   |                                      |  |                           |
| $F_q = 1280 - 1900 < 0$  |                                      |  |                           |
| $F_q$ is negative  |                                      |  |                           |
| <i>so no tension field action occurs</i>   |                                      |  |                           |
| $\therefore F_q - F_x = 0$   |                                      |  |                           |
| <b>4.4.6.6</b>   |                                      |  |                           |
| $M_s = 0$  |                                      |  |                           |
| $F_x = 760 \text{ kN}$   |                                      |  |                           |

|   |                                      |  |                           |
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|   | Design code<br><b>BSS950: Part 1</b> | Made by <b>RN</b><br>Checked by <b>GWO</b> | Sheet no. <b>19</b>       |

**Buckling resistance of load carrying stiffener at E,  $P_x$**  **4.5.1.5**

$P_x = P_q$  as calculated for stiffener at B

$P_x = 1910.6 \text{ kN}$

Since  $F_x < P_x$   $760 < 1910.6$

stiffener at E is OK for buckling

Stiffener at E: Adopt flats 80 mm × 13 mm thick, Grade 43 Steel

**Web check between stiffeners** **4.5.2.2**

$f_{ed} \leq P_{ed}$

$f_{ed} = w'/t = 92/14 = 6.57 \text{ N/mm}^2$

When the compression flange is restrained against rotation relative to the web


$$P_{ed} = \left[ 2.75 + \frac{2}{(a/d)^2} \right] \frac{E}{(d/t)^2}$$

$$P_{ed} = \left[ 2.75 + \frac{2}{\left( \frac{2825}{2000} \right)^2} \right] \frac{205000}{\left( \frac{2000}{14} \right)^2} \text{ (check the largest panel only)}$$

$P_{ed} = 37.7 \text{ N/mm}^2$

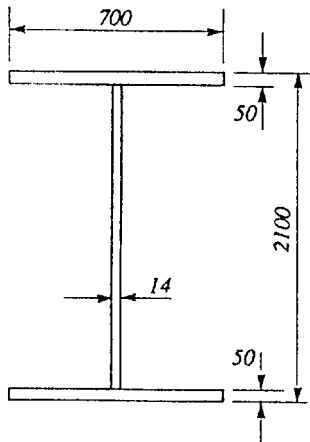
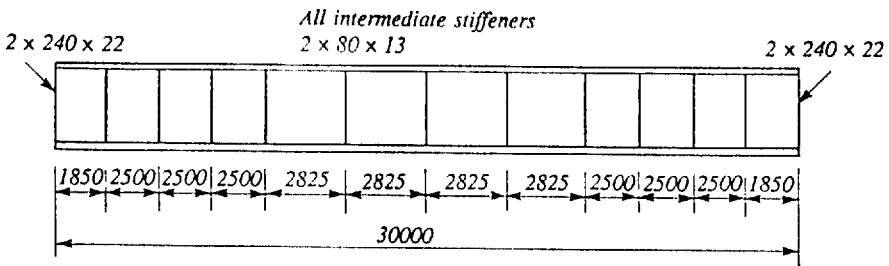
Since  $f_{ed} < P_{ed}$   $6.57 < 37.7$

the web is OK for all panels.

|   |   |   |                                      |
|---|---|---|--------------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>PLATE GIRDERS</b></p>      |   | <p>Chapter ref.</p> <p><b>17</b></p> |
|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p> | <p>Made by <b>RN</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>20</b></p>           |

***FINAL GIRDER***

***All Grade 43 Steel***





# Chapter 18

## Members with compression and moments

by DAVID NETHERCOT

### 18.1 Occurrence of combined loading

Chapters 15 and 16 deal respectively with the design of members subject to compression and bending when these loadings act in isolation. However, in practice a combination of the two effects is frequently present. Figure 18.1 illustrates a number of common examples.

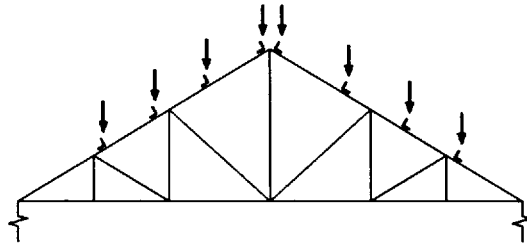
The balance between compression and bending, which may be induced about one or both principal axes, depends on a number of factors, the most important ones being the type of structure, the form of the applied loading, the member's location in the structure and the way in which the connections between the members function.

For building frames designed according to the principles of simple construction, it is customary to regard column moments as being produced only by beam reactions acting through notional eccentricities as illustrated in Fig. 18.2. Thus, column axial load is accumulated down the building but column moments are only ever generated by the floor levels under consideration with the result that they typically contain increasing ratios of compression to moment. Many columns are therefore designed for high axial loads but rather low moments. Corner columns suffer bending about both axes, but may well carry less axial load; edge columns are subject to bending about at least one axis; and internal columns may, if both the beam framing arrangements and the loading are balanced, be designed for axial load only.

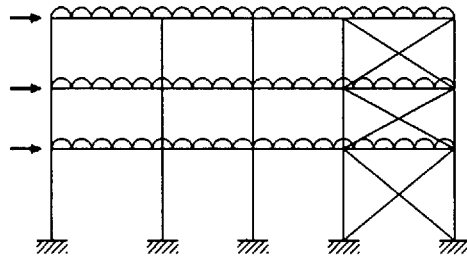
Conversely the columns of portal frames are required to carry high moments in the plane of the frame but relatively low axial loads, unless directly supporting cranes. Rafters also attract some small axial load, particularly when wind loading is being considered. Portals employ rigid connections between members permitting the transfer of moments around the frame. Similarly, multi-storey frames designed on the basis of rigid beam-to-column connections are likely to contain columns with large moments.

Members required to carry combined compression and moments are not restricted to rectangular building frames. Although trusses are often designed on the basis that member centrelines intersect at the joints, this is not always possible and the resulting eccentricities induce some moments in the predominantly axially loaded members. Sometimes the transfer of loads from secondary members into the main

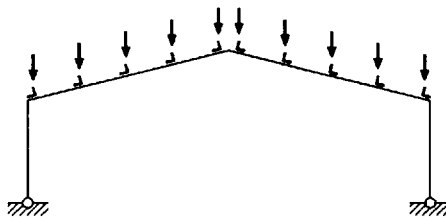
booms of trusses is arranged so that they do not coincide with joints, leading to beam action between joints being superimposed on the compression produced by overall bending.



(a)



(b)



(c)

*Fig. 18.1* Occurrence of beam-columns in different types of steel frames. (a) Roof truss – top chord members subject to bending from purlin loads and compression due to overall bending. (b) Simple framing – columns subject to bending from eccentric beam reactions and compression due to gravity loading. (c) Portal frame – rafters and columns subject to bending and compression due to frame action

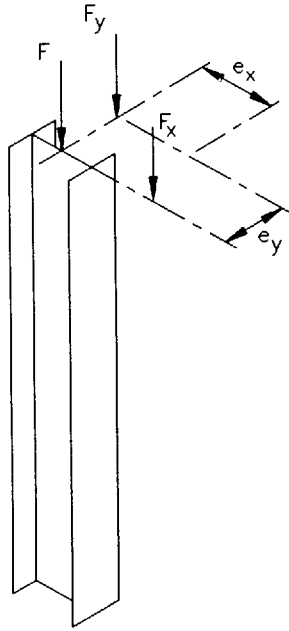
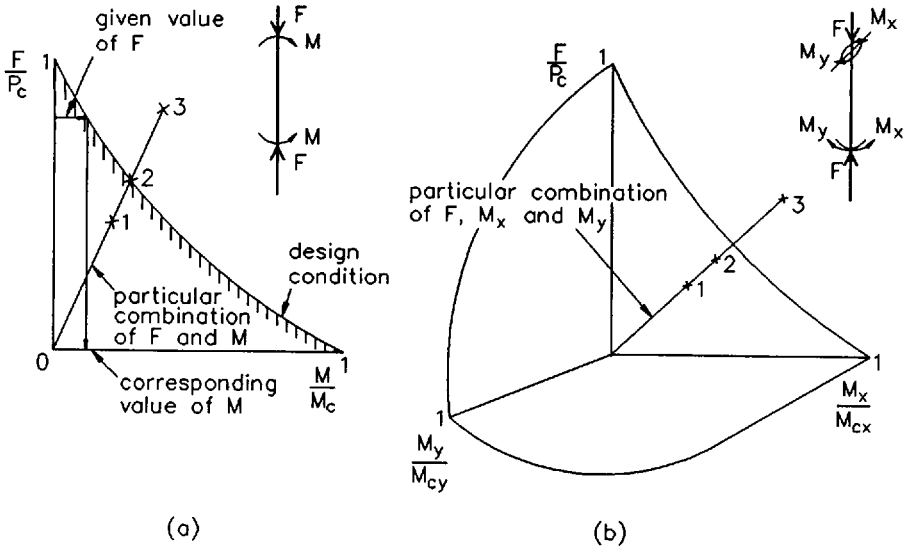


Fig. 18.2 Loading on a beam-column in a 'simply-designed' frame

## 18.2 Types of response – interaction

It is customary in many parts of the world, but not in the UK, to designate members subject to combined compression and bending as 'beam-columns'. The term is helpful in appreciating member response because the combination of loads produces a combination of effects incorporating aspects of the behaviour of the two extreme examples: a beam carrying only bending loads and a column carrying only compressive load. This then leads naturally to the concept of interaction as the basis for design, an approach in which the proportions of the member's resistance to each component load type are combined using diagrams or formulae. Figure 18.3 illustrates the concept in general terms for cases of two and three separate load components. Any combination is represented by a point on the diagram and an increasing set of loads with fixed ratios between the components corresponds to a straight line starting from the origin. Points that fall inside the boundary given by the design condition are safe, those that fall on the boundary just meet the design condition and those that lie outside the boundary represent an unsafe load combination. For the two load component case if one load type is fixed and the maximum safe value of the other is required, the vertical co-ordinate corresponding to the specified load is first located; projecting horizontally to meet the design boundary the horizontal co-ordinate can be read off.



- point 1 - safe
- point 2 - design condition just satisfied
- point 3 - unsafe

Fig. 18.3 Concept of interaction diagrams for combined loading: (a) two-dimensional, (b) three-dimensional

The exact version of Fig. 18.3 appropriate for a design basis depends upon several factors which include the form of the applied loading, the type of response that is possible, the member slenderness and the cross-sectional shape. Design methods for beam-columns must therefore seek to balance the conflicting requirements of rigour, which would try to adjust the form of the design boundary of Fig. 18.3 to reflect the influence of each of these factors, and simplicity. However, some appreciation of the role of each factor is necessary if even the simplest design approach is to be properly appreciated and applied.

The importance of member slenderness may be appreciated readily with reference to the two-dimensional example illustrated in Fig. 18.4. The member is loaded by compression plus equal and opposite end moments and is assumed to respond simply by deflecting in the plane of the applied loading. Under the action of the applied moments bending occurs leading to a lateral deflection  $v$ . The moment at any point within the length comprises two components: a constant primary moment  $M$  due to the applied end moments plus a secondary moment  $Fv$  due to the axial load  $F$  acting through the lateral deflection  $v$ . Summing the effects of compression and bending gives

$$F/P_c + M_{\max}/M_c = 1.0 \tag{18.1}$$

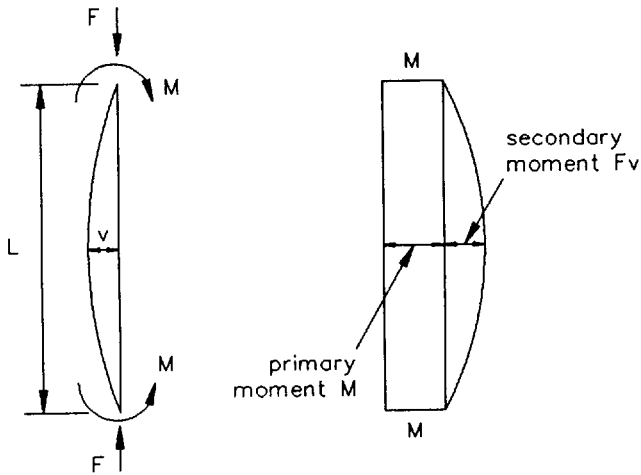


Fig. 18.4 In-plane behaviour of beam-columns

in which  $P_c$  and  $M_c$  are the resistance as a strut and a beam respectively and  $M_{\max}$  is the total moment.

Analysis of beam-column problems shows that  $M_{\max}$  may be closely approximated by

$$M_{\max} = M/(1 - F/P_{cr}) \quad (18.2)$$

in which  $P_{cr} = \pi^2 EI/L^2$  is the elastic critical load.

Combining these two expressions gives

$$F/P_c + M/(1 - F/P_{cr})M_c = 1.0 \quad (18.3)$$

Figure 18.5 shows how this expression plots in an increasingly concave fashion as member slenderness increases and the amplification of the primary moments  $M$  becomes more significant due to reductions in  $P_{cr}$ . Clearly if secondary moments are neglected, and the member is designed on the basis of summing the effects of  $F$  and  $M$  without allowing for their interaction, then an unsafe result is obtained.

If the member can respond only by deforming in the plane of the applied bending, the foregoing is an adequate representation of that response and so can be used as the basis for design. However, more complex forms of response are also possible. Figure 18.6 illustrates an I-section column subject to compression and bending about its major axis. Reference to Chapters 15 and 16 on columns and beams indicates that either the compression or the bending if acting alone would induce failure about the minor axis, in the first case by simple flexural buckling at a load  $P_{cy}$  and in the second by lateral-torsional buckling at a load  $M_b$ . Both tests and rigorous analysis confirm that the combination of loads will

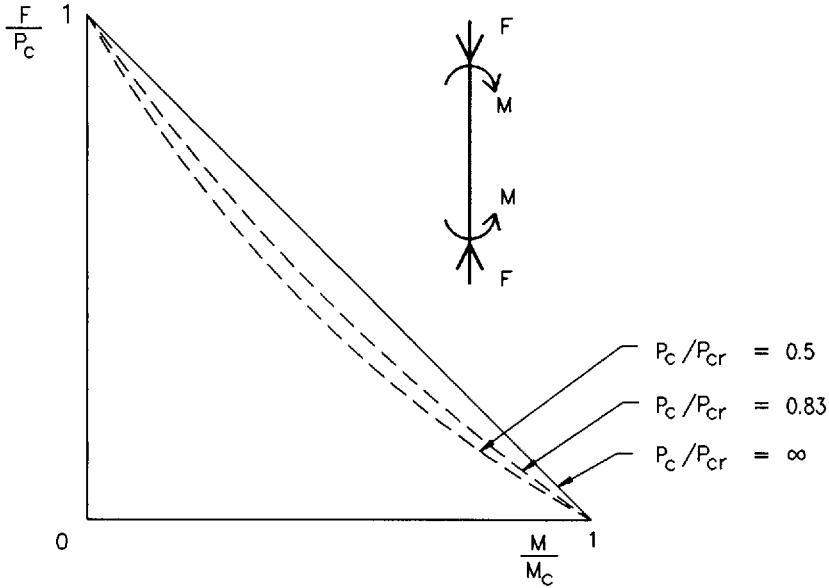


Fig. 18.5 Effect of slenderness on form of interaction according to Equation (18.3)

also produce a minor axis failure. Noting the presence of the amplification effect of the axial load acting through the bending deflections in the plane of the web and not the out-of-plane deformations associated with the eventual failure mode, leads therefore to a modified form of Equation (18.3) as an interaction equation that might form a suitable basis for design

$$F/P_{cy} + M/(1 - F/P_{crx})M_b = 1.0 \tag{18.4}$$

Note that both resistances  $P_{cy}$  and  $M_b$  relate to out-of-plane failure but that the amplification depends upon the in-plane Euler load. Consideration of the term  $F/P_{crx}$ , given that  $F$  is limited to  $P_{cy}$  which is less than  $P_{cx}$  and which is, in turn, less than  $P_{crx}$ , suggests that amplification effects are less significant than for the purely in-plane case.

Applied moments are not necessarily restricted to a single plane. For the most general case illustrated in Fig. 18.7, in which compression is accompanied by moments about both principal axes, the member's response is a three-dimensional one involving bending about both axes combined with twisting. This leads to a complex analytical problem which cannot really be solved in such a way that it provides a direct indication of the type of interaction formulae that might be used as a basis for design. A practical view of the problem, however, suggests that some form of combination of the two previous cases might be suitable, providing any proposal were properly checked against data obtained from tests and reliable analyses. This leads to two possibilities: combining the acceptable moments  $M_x$

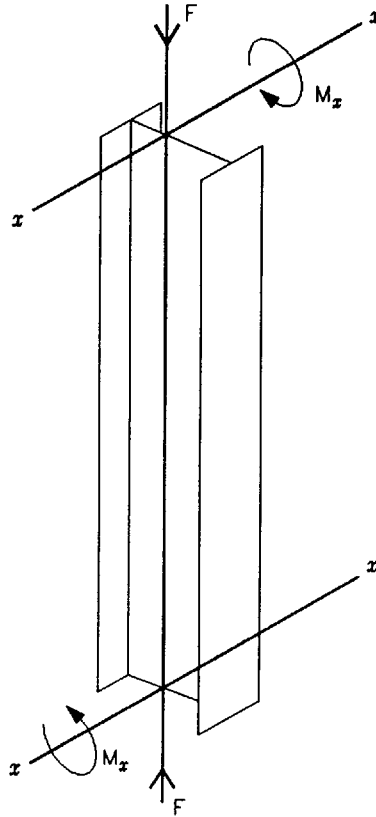


Fig. 18.6 Compression plus major axis bending for an I-section column

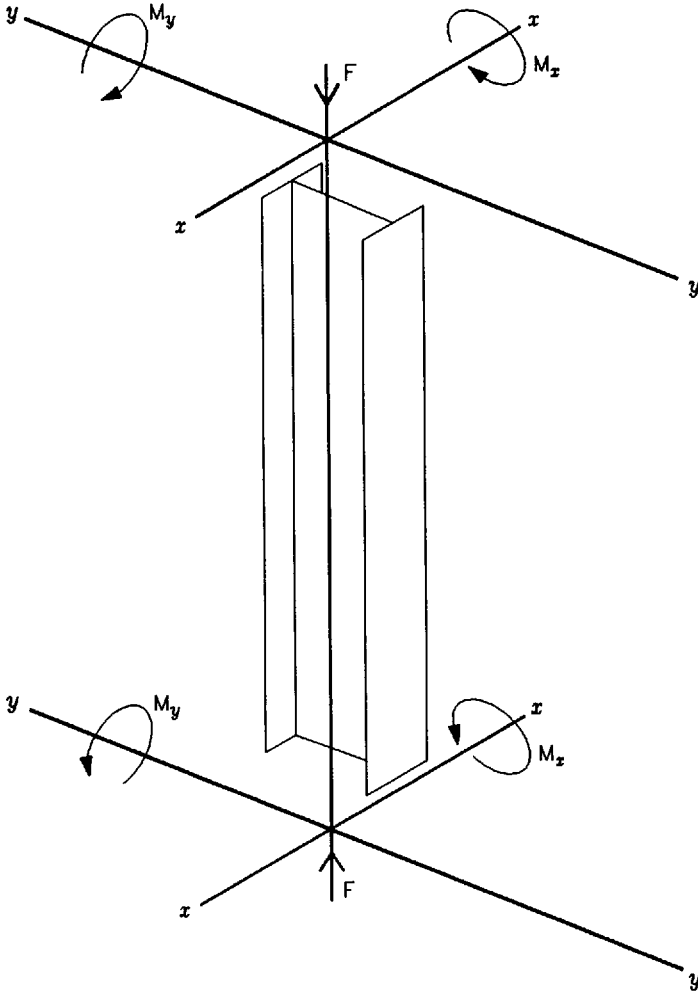
and  $M_y$  that can safely be combined separately with the axial load  $F$  obtained by solving Equations (18.3) and (18.4) to give

$$M_x/M_{ax} + M_y/M_{cy} = 1.0 \quad (18.5)$$

in which  $M_{ax}$  and  $M_{ay}$  are the solutions of Equations (18.3) and (18.4); or simply adding the minor axis bending effect to Equation (18.4) as

$$F/P_{cy} + M_x/(1 - F/P_{crx})M_b + M_y/(1 - F/P_{cry})M_{cy} = 1.0 \quad (18.6)$$

Although the first of these two approaches does not lead to such a seemingly straightforward end result as the second, it has the advantage that interaction about both axes may be treated separately, and so leads to a more logical treatment of cases for which major axis bending does not lead to a minor axis failure as for a rectangular tube in which  $M_b = M_{cr}$ , and  $P_{crx}$  and  $P_{cry}$  are likely to be much closer than is the case for a UB. Similarly for members with different effective lengths for the two planes, for example, due to intermediate bracing



*Fig. 18.7* Compression plus major and minor axis bending for an I-section column

acting in the weaker plane only, the ability to treat in-plane and out-of-plane response separately and to combine the weaker with minor axis bending leads to a more rational result.

The foregoing discussion has deliberately been conducted in rather general terms, the main intention being to illustrate those principles on which beam-column design should be based. Collecting them together:

- (1) interaction between different load components must be recognized; merely summing the separate components can lead to unsafe results
- (2) interaction tends to be more pronounced as member slenderness increases



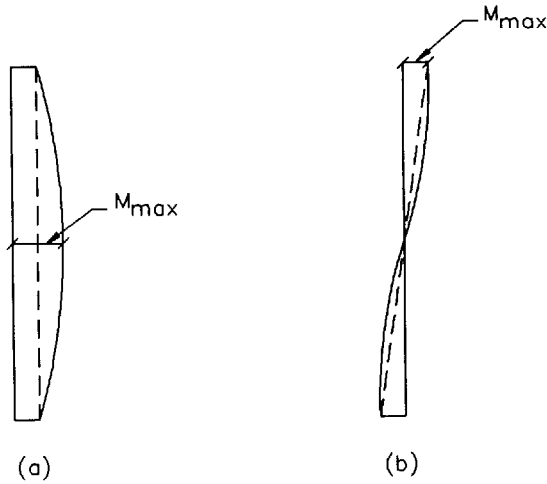


Fig. 18.8 Primary and secondary moments 1: (a) single curvature, (b) double curvature

(3) different forms of response are possible depending on the form of the applied loading.

Having identified these three principles it is comparatively easy to recognize their inclusion in the design procedures of BS 5950 and BS 5400.

### 18.3 Effect of moment gradient loading

Returning to the comparatively simple in-plane case, Fig. 18.8 illustrates the patterns of primary and secondary moments in a pair of members subject to unequal end moments that produce either single- or double-curvature bending. For the first case, the point of maximum combined moment occurs near mid-height where secondary bending effects are greatest. On the other hand, for double-curvature bending the two individual maxima occur at quite different locations and for the case illustrated, in which the secondary moments have deliberately been shown as small, the point of absolute maximum moment is at the top. Had larger secondary moments been shown, as is the case in Fig. 18.9, then the point of maximum moment moves down slightly but is still far from that of the single-curvature case.

Theoretical and experimental studies of steel beam-columns constrained to respond in-plane and subject to different moment gradients, as represented by the factor of the ratio of the numerically smaller end moment to the numerically larger end moment ( $\beta$ ), show clearly that, when all other parameters are held constant, failure loads tend to increase as  $\beta$  is varied from +1 (uniform single-curvature bending) to -1 (uniform double-curvature bending). Figure 18.10 illus-

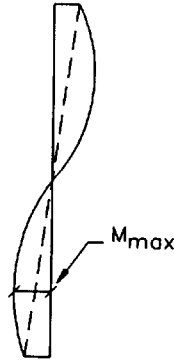


Fig. 18.9 Primary and secondary moments 2

trates the point in the form of a set of interaction curves. Clearly if all beam-column designs were to be based upon the  $\beta = +1$  case, safe but rather conservative designs would result.

Figure 18.10 also shows how for high moments the curves for  $\beta \neq +1$  tend to merge into a single line corresponding to the condition in which the more heavily stressed end of the member controls design. Reference to Figs 18.8 and 18.9 illustrates the point. The left-hand and lower parts of Fig. 18.10 correspond to situations in which Fig. 18.9 controls, while the right-hand and upper parts represent failure at one end. The two cases are sometimes referred to as 'stability' and 'strength' failure respectively. While this may offend the purists, for in both cases the limiting condition is one of exhausting the cross-sectional capacity, but at different locations within the member length, it does, nonetheless, serve to draw attention to the principal difference. Also shown in Fig. 18.10 is a line corresponding to the cross-sectional interaction; the combinations of  $F$  and  $M$  corresponding to the full strength of the cross-section. This is the 'strength' limit, representing the case where the primary moment acting in conjunction with the axial load accounts for all the cross-section's capacity.

The substance of Fig. 18.10 can be incorporated within the type of interaction formula approach of section 18.2 through the concept of 'equivalent uniform moment' presented in Chapter 16 in the context of the lateral-torsional buckling of beams; its meaning and use for beam-columns is virtually identical. For moment gradient loading member stability is checked using an equivalent moment  $\bar{M} = mM$ , as shown in Fig. 18.11. Coincidentally, suitable values of  $m$ , based on both test data and rigorous ultimate strength analyses, for the in-plane beam-column case are almost the same as those for laterally unrestrained beams (see section 16.3.6);  $m$  may conveniently be represented simply in terms of the moment gradient parameter  $\beta$ .

The situation corresponding to the upper boundary or strength failure of Fig. 18.10 must be checked separately using an appropriate means of determining cross-sectional capacity under  $F$  and  $M$ . The strength check is superfluous for  $\beta = +1$  as

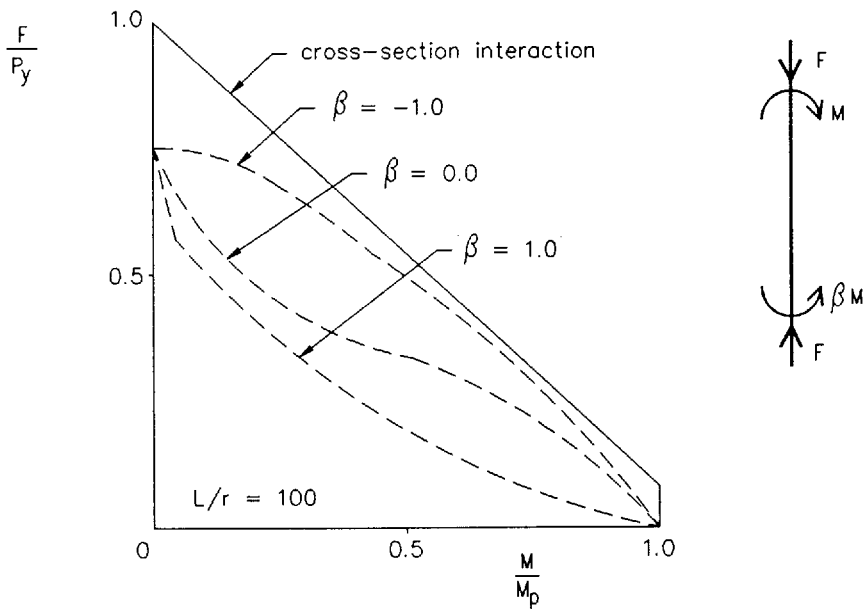
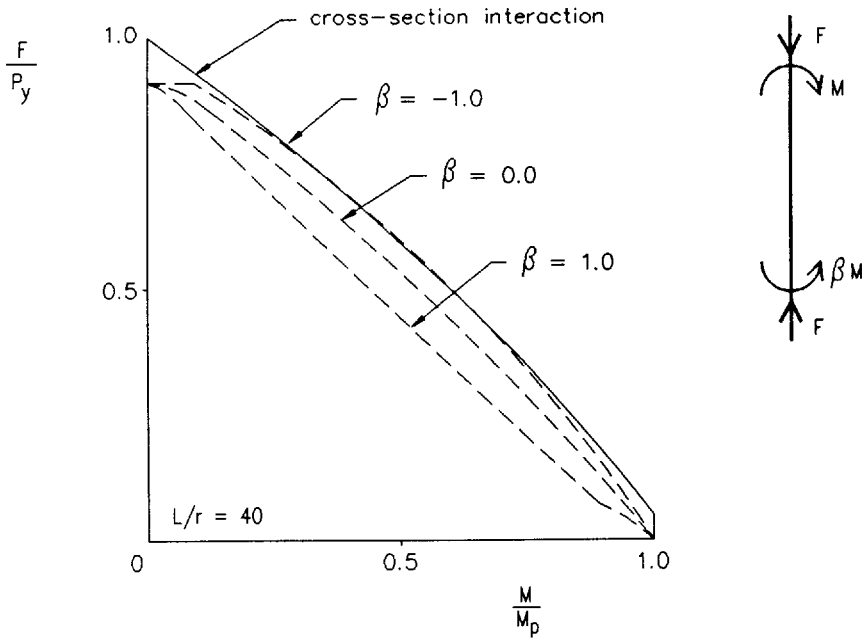


Fig. 18.10 Effect of moment gradient on interaction

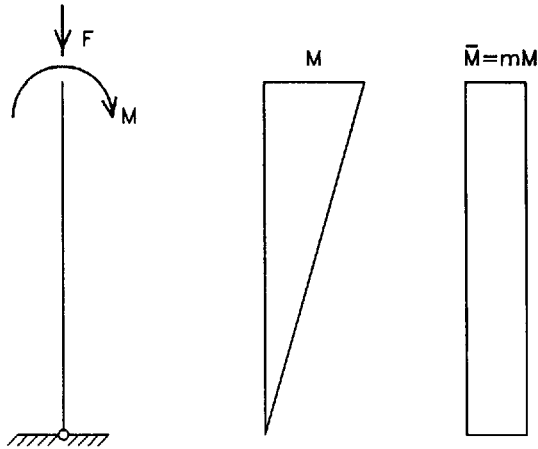


Fig. 18.11 Concept of equivalent uniform moment applied to primary moments on a beam-column

it can never control, while as  $\beta \rightarrow -1$  and  $M \rightarrow M_c$  it becomes increasingly likely that the strength check will govern. The procedure is:

- (1) check stability using an interaction formula in terms of buckling resistance  $P_c$  and moment capacity  $M_c$  with axial load  $F$  and equivalent moment  $\bar{M}$ ,
- (2) check strength using an interaction procedure in terms of axial capacity  $P_s$  and moment capacity  $M_c$  with coincident values of axial load  $F$  and maximum applied end moment  $M_1$  (this check is unnecessary if  $m = 1.0$ ;  $\bar{M} = M_1$  is used in the stability check).

Consideration of other cases involving out-of-plane failure or moments about both axes shows that the equivalent uniform moment concept may also be applied. For simplicity the same  $m$  values are normally used in design, although minor variations for the different cases can be justified. For biaxial bending, two different values,  $m_x$  and  $m_y$ , for bending about the two principal axes may be appropriate. An exception occurs for a column considered pinned at one end about both axes for which  $\beta_x = \beta_y = 0.0$ , whatever the sizes of the moments at the top.

## 18.4 Selection of type of cross-section

Several different design cases and types of response for beam-columns are outlined in section 18.2 of this chapter. Selection of a suitable member for use as

a beam-column must take account of the differing requirements of these various factors. In addition to the purely structural aspects, practical requirements such as the need to connect the member to adjacent parts of the structure in a simple and efficient fashion must also be borne in mind. A tubular member may appear to be the best solution for a given set of structural conditions of compressive load, end moments, length, etc., but if site connections are required, very careful thought is necessary to ensure that they can be made simply and economically. On the other hand, if the member is one of a set of similar web members for a truss that can be fabricated entirely in the shop and transported to site as a unit, then simple welded connections should be possible and the best structural solution is probably the best overall solution too.

Generally speaking when site connections, which will normally be bolted, are required, open sections which facilitate the ready use of, for example, cleats or endplates are to be preferred. UCs are designed principally to resist axial load but are also capable of carrying significant moments about both axes. Although buckling in the plane of the flanges, rather than the plane of the web, always controls the pure axial load case, the comparatively wide flanges ensure that the strong-axis moment capacity  $M_{cx}$  is not reduced very much by lateral-torsional buckling effects for most practical arrangements. Indeed the condition  $M_b = M_{cx}$  will often be satisfied.

In building frames designed according to the principles of simple construction, the columns are unlikely to be required to carry large moments. This arises from the design process by which compressive loads are accumulated down the building but the moments affecting the design of a particular column lift are only those from the floors at the top and bottom of the storey height under consideration. In such cases preliminary member selection may conveniently be made by adding a small percentage to the actual axial load to allow for the presence of the relatively small moments and then choosing an appropriate trial size from the tables of compressive resistance given in Reference 1. For moments about both axes, as in corner columns, a larger percentage to allow for biaxial bending is normally appropriate, while for internal columns in a regular grid with no consideration of pattern loading, the design condition may actually be one of pure axial load.

The natural and most economic way to resist moments in columns is to frame the major beams into the column flanges since even for UCs,  $M_{cx}$  will always be comfortably larger than  $M_{cy}$ . For structures designed as a series of two-dimensional frames in which the columns are required to carry quite high moments about one axis but relatively low compressive loads, UBs may well be an appropriate choice of member. The example of this arrangement usually quoted is the single-storey portal building, although here the presence of cranes, producing much higher axial loads, the height, leading to large column slenderness, or a combination of the two, may result in UCs being a more suitable choice. UBs used as columns also suffer from the fact that the  $d/t$  values for the webs of many sections are non-compact when the applied loading leads to a set of web stresses that have a mean compressive component of more than about 70–100 N/mm<sup>2</sup>.

## 18.5 Basic design procedure

When the distribution of moments and forces throughout the structure has been determined, for example, from a frame analysis in the case of continuous construction or by statics for simple construction, the design of a member subject to compression and bending consists of checking that a trial member satisfies the design conditions being used by ensuring that it falls within the design boundary defined by the type of diagram shown as Fig. 18.3. BS 5950 and BS 5400 therefore contain sets of interaction formulae which approximate such boundaries, use of which will automatically involve the equivalent procedures for the component load cases of strut design and beam design, to define the end points. Where these procedures permit the use of equivalent uniform moments for the stability check, they also require a separate strength check.

BS 5950: Part 1 requires that stability be checked using

$$\frac{F}{A_g p_c} + \frac{\bar{M}_x}{M_b} + \frac{\bar{M}_y}{p_y Z_y} \leq 1 \quad (18.7)$$

In Equation (18.7) the use of  $p_y Z_y$ , rather than  $M_{cy}$ , makes some allowance in the case of plastic and compact sections for the effects of secondary moments as described in section 18.2. For non-compact sections, for which  $M_{cy} = p_y Z_y$ , no such allowance is made and an unconservative effect is therefore present. Evaluation of Equation (18.7) may be effected quite rapidly if the tabulated values of  $P_{cy}$ ,  $P_{cx}$ ,  $M_b$  and  $p_y Z_y$  given in Reference 1 for all UB, UC, RSJ and SHS are used. In the cases where  $\bar{M}$  values are being used and  $M_x$  and  $M_y$  are not taken as the full values of the maximum moments about the two principal axes, it is essential to check that the most highly stressed cross section is capable of sustaining the coincident compression and moment(s). BS 5950: Part 1 covers this with the expression:

$$\frac{F}{A_g p_{yu}} + \frac{M_x}{M_{cx}} + \frac{M_y}{M_{cy}} \not\leq 1 \quad (18.8)$$

Clearly when both  $M_{cx}$  and  $M_b$  values are the same Equation (18.7) is always a more severe check, or in the limit is identical, and only Equation (18.7) need be used. Values of  $A_g p_y$ ,  $M_{cx}$  and  $M_{cy}$  are also tabulated in Reference 1.

As an alternative to the use of Equations (18.7) and (18.8), BS 5950: Part 1 does, for plastic or compact sections only, permit the use of an alternative pair of interaction formulae. These are both presented in the same form as:

$$\left( \frac{\bar{M}_x}{M_{ax}} \right) + \left( \frac{\bar{M}_y}{M_{ay}} \right) \not\leq 1 \quad (18.9)$$

$$\left( \frac{M_x}{M_{rx}} \right)^{2.1} + \left( \frac{M_y}{M_{ry}} \right)^{2.5} \not\leq 1 \quad (18.10)$$

The first controls overall buckling, the second local capacity and in both cases the denominators in the two terms ( $M_a$  and  $M_r$ ) are a measure of the moment that

can be carried in the presence of the axial load  $F$ . If bending is present about one axis only both checks reduce to a single term on the left-hand side, which corresponds to ensuring that

$$M \nless M_a \quad \text{for overall buckling}$$

$$M \nless M_r \quad \text{for local capacity}$$

Evaluation of  $M_{ax}$  and  $M_{ay}$  is explained in the code, while  $M_{rx}$  and  $M_{ry}$  may be obtained either from the formulae given in the first part of Reference 1, or, much more conveniently using the tabulated values given in the later parts of that handbook. For fabricated sections, the principles of plastic theory may be applied first to locate the plastic neutral axis for a given combination of  $F$ ,  $M_x$  and  $M_y$  and then to calculate  $M_{rx}$  and  $M_{ry}$ . This is manageable for uniaxial bending –  $F$  and  $M_x$  or  $F$  and  $M_y$  – but it is tedious for the full three-dimensional case and some use of approximate results <sup>1</sup> may well be preferable.

## 18.6 Cross-section classification under compression and bending

It is assumed in the discussion of the use of the BS 5950: Part 1 procedure that the designer has conducted the necessary section classification checks so as to ensure that the appropriate values of  $M_{cx}$ ,  $M_{cy}$ , etc. are used. When the tabulated data of Reference 1 are being employed, any allowances for non-compactness are included in the listed values of  $M_{cx}$  and  $M_{cy}$  but only if  $P_{cx}$  and  $P_{cy}$  have been taken from the strut tables rather than the beam-column tables will these contain any reduction. The reason is that for pure compression the stress pattern is known, whereas under combined loading the requirement may be to sustain only a very small axial load; to reduce  $P_{cx}$  and  $P_{cy}$  on the basis of uniform compression in each plate element of the section is much too severe. For simplicity, section classification may initially be conducted under the most severe conditions of pure axial load; if the result is either plastic or compact nothing is to be gained by conducting additional calculations with the actual pattern of stresses. However, if the result is a non-compact section, possibly when checking the web of a UB, then it is normally advisable for economy of both design time and actual material use to repeat the classification calculations more precisely, as illustrated in the following.

### 18.6.1 Compactness check under combined loading

When checking a web subject to combined compression and bending for compactness according to BS 5950: Part 1, careful ordering of the calculations will simplify what may well at first sight appear to be a complex process. Rearrangement of the limits of Table 7 of the code into the five categories of Table 18.1<sup>2</sup> is

**Table 18.1** Check for compact web under combined loading

| Category | $d/t$ limit    | $F$ limit                    | Result/action                   |
|----------|----------------|------------------------------|---------------------------------|
| 1        | $39\epsilon$   | Any                          | Compact                         |
| 2        | $49\epsilon$   | $tdp_y$                      | Compact                         |
| 3        | $> 49\epsilon$ | $t^2p_y(98\epsilon - d/t)$   | Compact                         |
| 4        | $> 49\epsilon$ | $> t^2p_y(98\epsilon - d/t)$ | App. H3.2<br>of BS 5950: Part 1 |
| 5        | $> 39\epsilon$ | $> tdp_y$                    | App. H3.2<br>of BS 5950: Part 1 |

the first step. In drawing up this table the limitations on axial load  $F$  are a measure of the proportion of axial load  $F$  to moment  $M$ ; since the check is being conducted at the compact/semi-compact boundary, the use of plastic (rectangular) stress blocks is appropriate. It is therefore necessary that the compression flange is at least compact.

Since all webs satisfying  $d/t < 39\epsilon$  are compact even if the whole section is under uniform compression, as shown in Fig. 18.12(a), it follows that such webs subject to combined loading are also compact whatever the value of  $F$ .

The upper limits for the second category are illustrated in Fig. 18.12(b), which shows the case of a web subject to uniform compression throughout ( $y_c = d$ ,  $\alpha = 2$ ). The flanges are resisting all the moment, leading to a maximum value for  $F$  of  $tdp_y$ , and, using the condition from Table 7 for 'web generally', a compact limit of

$$\begin{aligned} d/t &\leq 98\epsilon/\alpha \\ &\leq 98\epsilon/2 \\ &\leq 49\epsilon \end{aligned}$$

Increasing the moment so that part of it must be resisted by a portion of the web leads to the condition of Fig. 18.12(c), in which equilibrium requires that:

$$C = T$$

$$F = C'$$

$C$  and  $T$  together resist  $M$

Block  $C'$  must be symmetrical about the geometrical axis, and so  $y_c$  may be obtained as:

$$y_c = d/2 + \frac{1}{2}(F/tp_y)$$

and since  $\alpha = 2y_c/d$ , it follows that

$$\begin{aligned} \alpha &= 2/d[d/2 + \frac{1}{2}(F/tp_y)] \\ &= 1 + F/tdp_y \end{aligned}$$

From Table 7 for 'web generally', a compact limit is

$$\begin{aligned} d/t &\leq 98\epsilon/\alpha \\ &\leq 98\epsilon/(1 + F/tdp_y) \end{aligned}$$



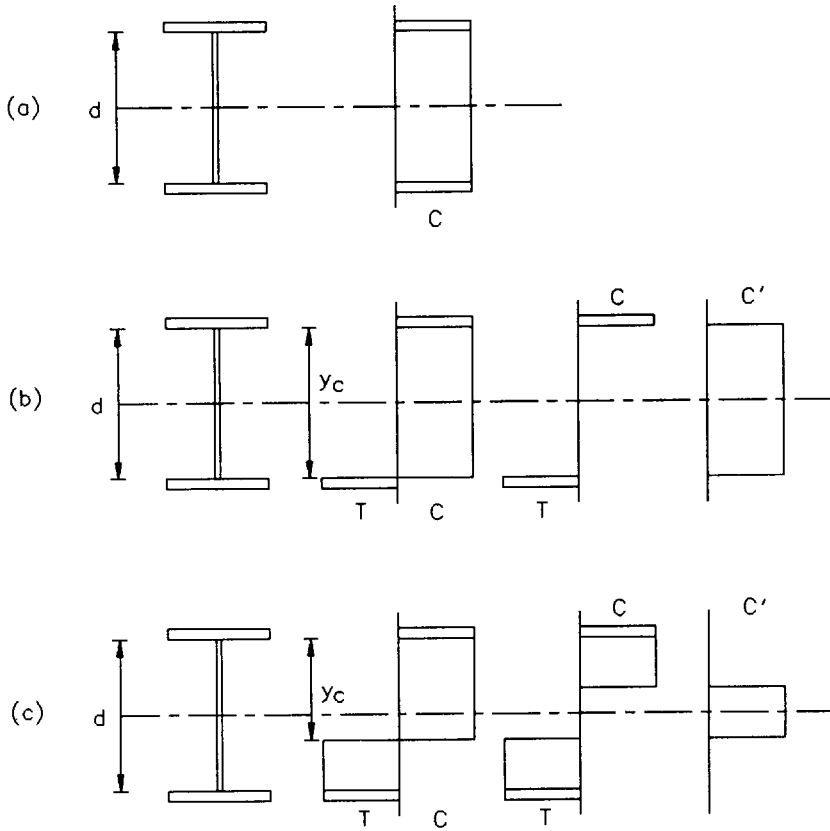


Fig. 18.12 Compactness checks for webs under combined compression and bending: (a) category 1, (b) category 2, (c) category 3

$$\begin{aligned} \therefore d/t (1 + F/tdp_y) &\leq 98\epsilon \\ d/t + d/t(F/tdp_y) &\leq 98\epsilon \\ \text{and } (F/tdp_y)d/t &\leq 98\epsilon - d/t \\ \text{or } F/t^2p_y &\leq 98\epsilon - d/t \\ F &\leq (98\epsilon - d/t) t^2p_y \end{aligned}$$

If  $F$  is limited to this value, and  $d/t$  does not exceed the absolute limit of  $98\epsilon$ , the position of the neutral axis means that the ‘web generally’ limit will be met.

If the value of  $F$  exceeds this limit (and  $d/t > 49\epsilon$ ), the web may still be compact if it satisfies the more extensive procedure of Appendix H3.2 of the code, use of which is best demonstrated by means of an example.

Take a  $406 \times 140 \times 39$  UB (the UB with the highest  $d/t$ ) with  $\epsilon = 1$  and  $F = 450$  kN and  $M = 150$  kN m.

$$\begin{aligned} \text{Plastic resistance, } dtp_y &= 359.7 \times 6.3 \times 275/10^3 \\ &= 623 \text{ kN} \end{aligned}$$

$F = 450 \text{ kN} < 623$  and plastic neutral axis is in web

$$\begin{aligned} \text{Reduced plastic moment, } M_{pr} &= M_p - \frac{F^2}{4tp_y} \\ &= 721 \times 275/10^3 - 450^2/4 \times 6.3 \times 275 \\ &= 198.3 - 29.2 \\ &= 169.1 \text{ kN m} \end{aligned}$$

$M = 150 \text{ kN} < 169.1$  so plastic resistance okay.

Compactness,  $d/t = 57.1 > 49$

$$\begin{aligned} \text{Check whether } F > (98\epsilon - d/t)t^2p_y \\ > (98 - 57.1)6.3^2 \times 275/10^3 \\ &= 446.4 \text{ kN} \end{aligned}$$

$F = 450 \text{ kN} > 446.4$  so use Appendix H3.2

Local buckling

$$\begin{aligned} M_p \text{ of web} &= 6.3 \times 359.7^2 \times 275/4 \times 10^3 \times 10^3 \\ &= 56.0 \text{ kN m} \end{aligned}$$

$$\begin{aligned} M_p \text{ of flanges} &= 198.3 - 56.0 \\ &= 142.3 \text{ kN m} \end{aligned}$$

$$\begin{aligned} M_w &= 150 - 142.3 \\ &= 7.7 \text{ kN m} \end{aligned}$$

$$\begin{aligned} p_{b.cr} &= (1630/57.1)^2 \\ &= 814.9 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} M_{cr} &= 6.3 \times 359.7^2 \times 814.9/4 \times 10^3 \times 10^3 \\ &= 166.1 \text{ kN m} \end{aligned}$$

$$\begin{aligned} p_{c.cr} &= (815/57.1)^2 \\ &= 203.7 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} P_{c.cr} &= dtp_{c.cr} \\ &= 359.7 \times 6.3 \times 203.7/10^3 \\ &= 461.6 \text{ kN} \end{aligned}$$

$$\begin{aligned} \frac{F_c}{P_{c.cr}} + \left(\frac{M_w}{M_{cr}}\right)^2 &= \frac{450}{461.6} + \left(\frac{7.7}{166.1}\right)^2 \\ &= 0.975 + 0.002 \\ &= 0.977 < 1 \quad \text{okay} \end{aligned}$$

Despite the limits on  $d/t$  and  $F$  given by Table 7 being exceeded, the more rigorous check shows the web to be just safe against buckling under a fully plastic stress distribution and so compact. Were  $F$  to be increased to the level of  $P_{c.cr}$  then the corresponding value of  $M_w$  would fall to zero; alternatively if  $F$  is taken as the limiting value  $(98 - d/t)t^2p_y$ :

$$\begin{aligned} M_{pr} &= 198.3 - 446.4^2/4 \times 6.3 \times 275 \\ &= 198.3 - 23.8 \\ &= 169.5 \text{ kN m} \end{aligned}$$

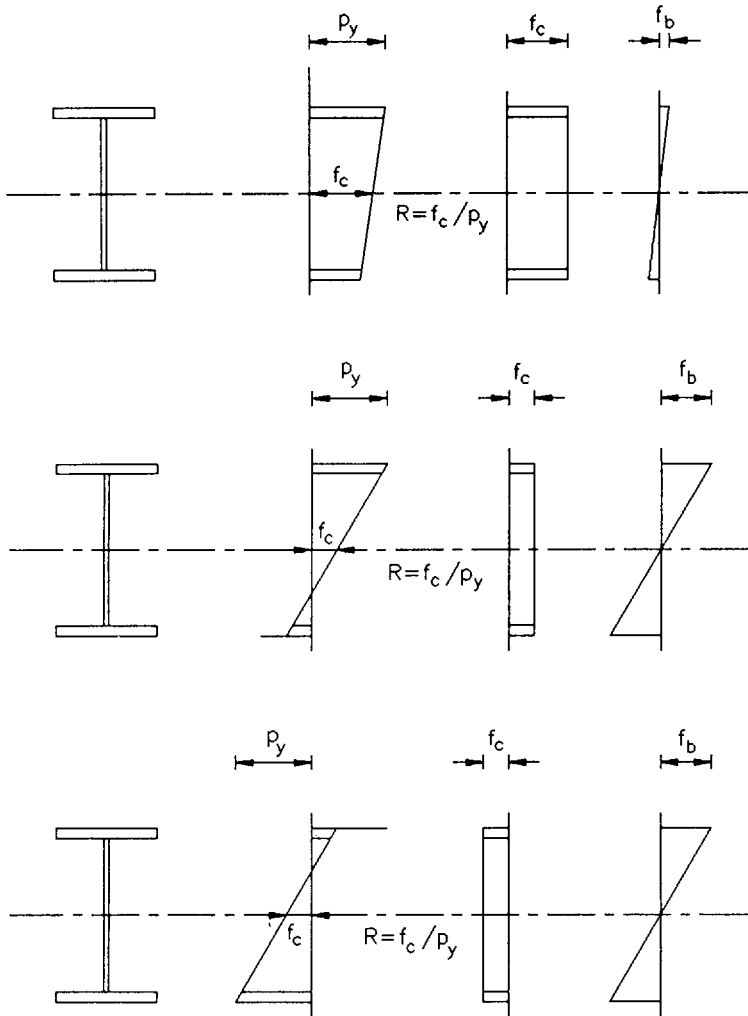


Fig. 18.13 Definition of  $R$  when checking semi-compact webs under compression and bending – symmetrical sections

$$M_w = 169.5 - 142.3$$

$$= 27.2 \text{ kN m}$$

$$\frac{F_c}{P_{c,cr}} + \left(\frac{M_w}{M_{cr}}\right)^2 = \frac{446.4}{461.6} + \left(\frac{27.2}{166.1}\right)^2$$

$$= 0.967 + 0.027$$

$$= 0.994 \approx 1$$

which shows that Appendix H3.2 leads to higher results with the web resisting some of the moment. If the compression exceeds the web capacity and the web

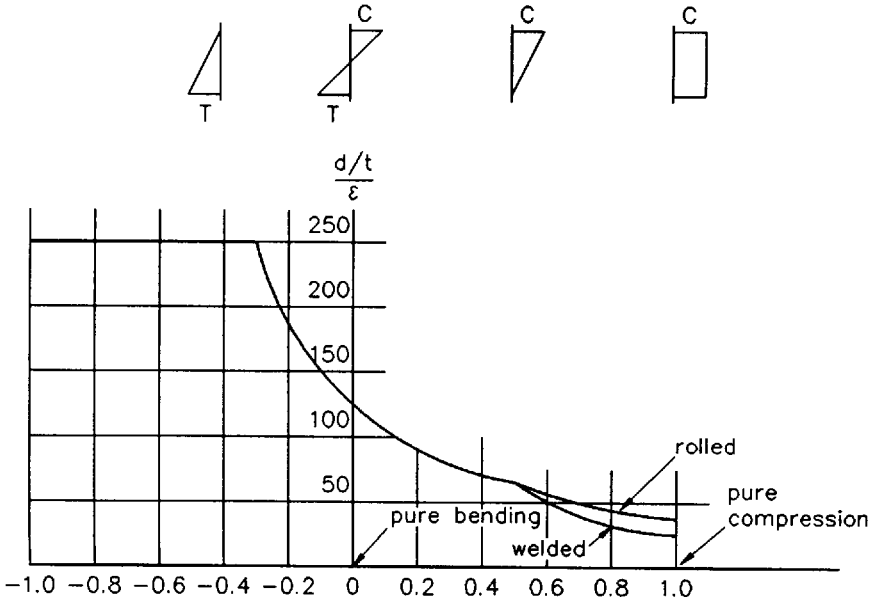


Fig. 18.14 Semi-compact limits for webs subject to compression and bending

**Table 18.2** Semi-compact limits of webs subject to compression and bending

| Range of values for $R$ | $d/t$ limits                    |                                 |
|-------------------------|---------------------------------|---------------------------------|
|                         | Rolled sections                 | Welded sections                 |
| $R < -0.307$            | $250\epsilon$                   | $250\epsilon$                   |
| $0 \geq R \geq -0.307$  | $\frac{120\epsilon}{(1 + R)^2}$ | $\frac{120\epsilon}{(1 + R)^2}$ |
| $0.504 \geq R \geq 0$   | —                               | $\frac{120\epsilon}{1 + 1.5R}$  |
| $R > 0.504$             | —                               | $(41/R - 13)\epsilon$           |
| $0.656 \geq R \geq 0$   | $\frac{120\epsilon}{1 + 1.5R}$  | —                               |
| $R > 0.656$             | $(41/R - 2)\epsilon$            | —                               |

slenderness exceeds the limit for ‘web subject to compression throughout’ i.e.  $F > tdp_y$  and  $d/t > 39\epsilon$ , Appendix H3.2 should be used since the plastic neutral axis is located in the flange.

Appendix H3.2 may also be used if  $F$  exceeds the web capacity ( $F > tdp_y$ ) and  $d/t$  exceeds the ‘uniform compression throughout the section’ limit of  $39\epsilon$ , although in such cases the plastic neutral axis is located part way through the flange.

Web elements which are non-compact should be checked against the semi-compact limit since meeting this will require no reductions in  $P_c$  and the simple limitation of  $M_c$  (or  $M_b$ ) to  $p_y Z$ . BS 5950: Part 1 uses a set of formulae expressed in terms of a property  $R$  which is the ratio of the mean longitudinal stress in the web to  $p_y$ . From Fig. 18.13 it is clear that for symmetrical sections,  $R$  is equal to  $F/Ap_y$ . The formulae ensure a smooth transition between the Table 7 values for compression throughout to pure bending as  $R$  reduces from unity to zero as shown in Fig. 18.14. Table 18.2 defines the range of  $R$ -values for which each formula is applicable.

Taking the UB with the most slender web (a  $406 \times 140 \times 39$  UB with  $d/t = 57.1$ ) gives limits on  $R$  of 0.66 and 0.52 for grade 43 and 50 material respectively, up to which levels of compression the section will not be slender. Higher figures are appropriate for other UBs; no UC has a sufficiently high  $d/t$  value to be other than compact even under pure compression ( $d/t \leq 39\epsilon$ ).

## 18.7 Special design methods for members in portal frames

### 18.7.1 Design requirements

Both the columns and the rafters in the typical pitched roof portal frame represent particular examples of members subject to combined bending and compression. Providing such frames are designed elastically, the methods already described for assessing local cross-sectional capacity and overall buckling resistance may be employed. However, these general approaches fail to take account of some of the special features present in normal portal frame construction, some of which can, when properly allowed for, be shown to enhance buckling resistance significantly.

When plastic design is being employed, the requirements for member stability change somewhat. It is no longer sufficient simply to ensure that members can safely resist the applied moments and thrust; rather for members required to participate in plastic hinge action, the ability to sustain the required moment in the presence of compression during the large rotations necessary for the development of the frame's collapse mechanism is essential. This requirement is essentially the same as that for a 'plastic' cross-section discussed in Chapter 13. The performance requirement for those members in a plastically designed frame actually required to take part in plastic hinge action is therefore equivalent to the most onerous type of response shown in Fig. 13.4. If they cannot achieve this level of performance, for example, because of premature unloading caused by local buckling, then they will prevent the formation of the plastic collapse mechanism assumed as the basis for the design, with the result that the desired load factor will not be attained. Put simply the requirement for member stability in plastically-designed structures is to impose limits on slenderness and axial load level, for example, that ensure stable behaviour while the member is carrying a moment

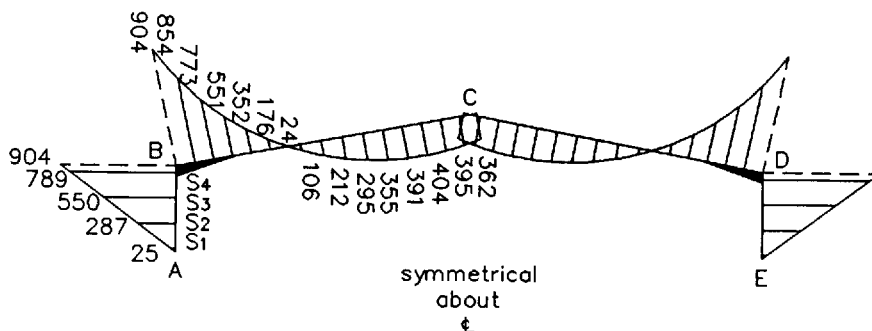


Fig. 18.15 Moment distribution for dead plus imposed load condition

equal to its plastic moment capacity suitably reduced so as to allow for the presence of axial load. For portal frames, advantage may be taken of the special forms of restraint inherent in that form of construction by, for example, purlins and sheeting rails attached to the outside flanges of the rafters and columns respectively.

Figure 18.15 illustrates a typical collapse moment diagram for a single-bay pin-base portal subject to gravity load only (dead load + imposed load), this being the usual governing load case in the UK. The frame is assumed to be typical of UK practice with columns of somewhat heavier section than the rafters and haunches of approximately 10% of the clear span and twice the rafter depth at the eaves. It is further assumed that the purlins and siderails which support the cladding and are attached to the outer flanges of the columns and rafters provide positional restraint to the frame, i.e. prevent lateral movement of the flange, at these points. Four regions in which member stability must be ensured may be identified.

- (1) full column height AB
- (2) haunch, which should remain elastic throughout its length
- (3) eaves region of rafter for which the lower unbraced flange is in compression due to the moments, from end of haunch
- (4) apex region of the rafter between top compression flange restraints.

### 18.7.2 Column stability

Figure 18.16 provides a more detailed view of the column AB, including both the bracing provided by the siderails and the distribution of moment over the column height. Assuming the presence of a plastic hinge immediately below the haunch, the design requirement is to ensure stability up to the formation of the collapse mechanism.

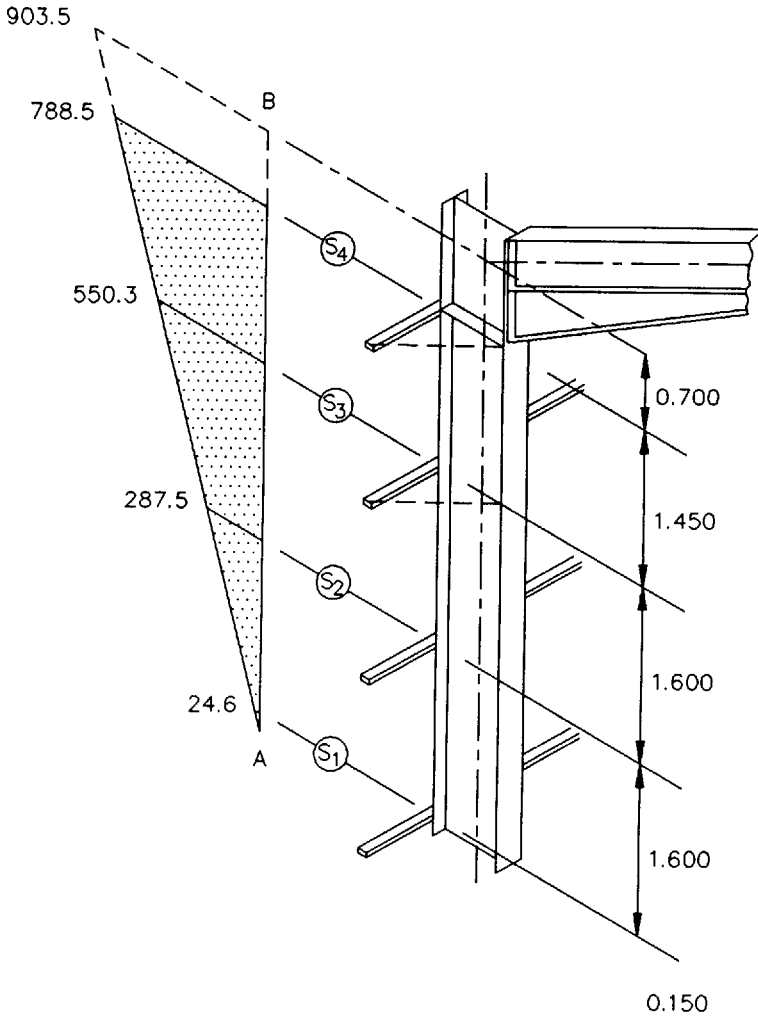


Fig. 18.16 Member stability – column

According to clause 5.3.5 of BS 5950: Part 1, torsional restraint must be provided no more than  $D/2$ , where  $D$  is the overall column depth, measured along the column axis, from the underside of the haunch. This may conveniently be achieved by means of the knee brace arrangement of Fig. 18.17. The simplest means of ensuring adequate stability for the region adjacent to this braced point is to provide another torsional restraint within a distance of not more than  $L_m$ , where  $L_m$  is obtained from clause 5.3.5 as

$$L_m \leq \frac{38r_y}{[f_c/130 + (p_y/275)^2(x/36)^2]^{\frac{1}{2}}} \tag{18.11}$$

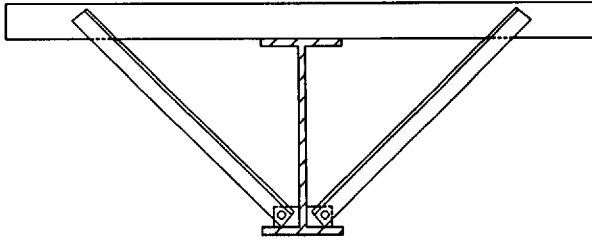


Fig. 18.17 Effective torsional restraints

Noting that the mean axial stress in the column  $f_c$  is normally small, that  $p_y$  is around  $275 \text{ N/mm}^2$  for grade 43 steel and that  $x$  has values between about 20 and 45 for UBs, gives a range of values for  $L_m/r_y$  of between 30 and 68. Placing a second torsional restraint at this distance from the first therefore ensures the stability of the upper part of the column.

Below this region the distribution of moment in the column normally ensures that the remainder of the length is elastic. Its stability may therefore be checked using the procedures of section 18.5. Frequently no additional intermediate restraints are necessary, the elastic stability condition being much less onerous than the plastic one.

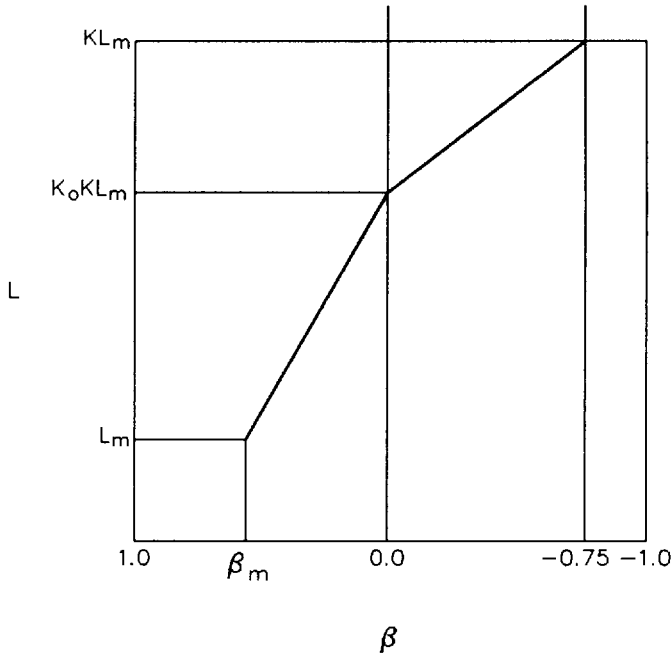
Equation (18.11) is effectively a fit to the limiting slenderness boundary of the column design charts<sup>3</sup> that were in regular use until the advent of BS 5950: Part 1, based on the work of Horne,<sup>4</sup> which recognized that for lengths of members between torsional restraints subject to moment gradient, longer unbraced lengths could be permitted than for the basic case of uniform moment. Equation (18.11) may therefore be modified to recognize this by means of the coefficients proposed by Brown.<sup>5</sup> Figure 18.18 illustrates the concept and gives the relevant additional formulae. For a  $533 \times 210 \text{ UB82}$  of grade 43 steel for which  $x = 41.6$  and assuming  $f_c = 15 \text{ N/mm}^2$ , the key values become:

$$\begin{aligned} L_m &= 31.55r_y \\ KL_m &= 122.7r_y \\ K_0KL_m &= 90.6r_y \\ \beta_m &= 0.519 \end{aligned}$$

When checking a length for which the appropriate value of  $\beta$  is significantly less than +1.0, use of this modification permits a more relaxed approach to the provision of bracing. Some element of trial and error is involved since the exact value of  $\beta$  to be used is itself dependent upon the location of the restraints.

Neither the elastic nor the plastic stability checks described above take account of the potentially beneficial effect of the tension flange restraint provided by the sheeting rails. This topic has been extensively researched,<sup>6</sup> with many of the findings being distilled into the design procedures of Appendix G of BS 5950: Part 1. Separate procedures are given for both elastic and plastic stability checks. Although significantly more complex than the use of Equation (18.11) or the





$$\begin{aligned}
 20 < x \leq 30 \quad K &= 2.3 + 0.03x - x f_c / 3000 \\
 30 < x < 50 \quad K &= 0.8 + 0.08x - (x - 10)f_c / 2000 \\
 K_0 &= (180 + x) / 300 \\
 \text{Grade 43 steel } \beta_m &= 0.44 + x / 270 - f_c / 200 \\
 \text{Grade 50 steel } \beta_m &= 0.47 + x / 270 - f_c / 250
 \end{aligned}$$

Fig. 18.18 Modification to Equation (18.11) to allow for moment gradient

methods of section 18.5, their use is likely to lead to significantly increased allowable unbraced lengths, particularly for the plastic region.

### 18.7.3 Rafter stability

Stability of the eaves region of the rafter may most easily be ensured by satisfying the conditions of clause 5.5.3.5. If tension flange restraint is not present between

points of compression flange restraint i.e. widely spaced purlins and a short unbraced length requirement, this simply requires the use of Equation (18.11). However, when the restraint is present in the form illustrated in Fig. 18.19, the distance between compression flange restraints for grade 43 steel and a haunch that doubles the rafter depth may be taken as  $L_s$ , given by

$$L_s = \frac{495 r_y x}{(72x^2 - 10^4)^{\frac{1}{2}}} \tag{18.12}$$

Variants of this expression are given in the code for changes in the grade of steel or haunch depth. Certain other limitations must also be observed:

- (1) the rafter must be a UB
- (2) the haunch flange must not be smaller than the rafter flange
- (3) the distance between tension flange restraints must be stable when checked as a beam using the procedure of section 16.3.6.

Equation (18.12) is less sensitive than Equation (18.11) to changes in  $x$  with the result that it gives an average value for  $L_s/r_y$  of about 65. It is often regarded as good practice to provide bracing at the toe of the haunch since this region corresponds to major changes in the pattern of force transfer due to the change in the line of action of the compression in the bottom flange. In cases where the use of clause 5.5.3.5 does not give a stable haunch because the length from eaves to

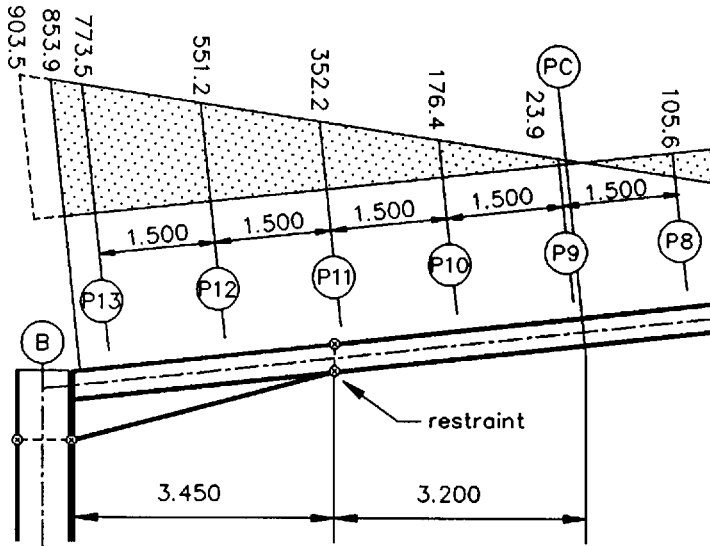


Fig. 18.19 Member stability in haunched rafter region

toe exceeds  $L_s$ , Appendix G may be used to obtain a larger value of  $L_s$ . If this is still less than the haunch length, then additional compression flange restraints are required.<sup>6</sup>

#### 18.7.4 Bracing

The general requirements of lateral bracing systems have already been referred to in Chapter 16 – sections 16.3, 16.4 and 16.5 in particular. When purlins or siderails are attached directly to a rafter or column compression flange it is usual to assume that adequate bracing stiffness and strength are available without conducting specific calculations. In cases of doubt the ability of the purlin to act as a strut carrying the design bracing force may readily be checked. Definitive guidance on the appropriate magnitude to take for such a force is noticeably lacking in codes of practice. A recent suggestion for members in plastically-designed frames<sup>7</sup> is 2% of the squash load of the compression flange of the column or rafter;  $0.02p_yBT$  at every restraint. In order that bracing members possess sufficient stiffness a second requirement that their slenderness be not more than 100 has also been proposed.<sup>7</sup> Both suggestions are largely based on test data. For elastic design the provisions of BS 5950: Part 1 may be followed.

When purlins or siderails are attached to the main member's tension flange, any positional restraint to the compression flange must be transferred through both the bracing to main member interconnection and the webs of the main member. Both effects are allowed for in the work on which the special provisions in BS 5950: Part 1 for tension flange restraint are based.<sup>8</sup> When full torsional restraint is required so that interbrace buckling may be assumed, the arrangement of Fig. 18.17 is often used. The stays may be angles, tubes (providing simple end connections can be arranged) or flats (which are much less effective in compression than in tension). In theory a single member of sufficient size would be adequate but practical considerations such as hole clearance<sup>6</sup> normally dictate the use of pairs of stays. It should also be noted that for angles to the horizontal of more than  $45^\circ$  the effectiveness of the stay is significantly reduced.

Reference 9 discusses several practical means of bracing or otherwise restraining beam-columns.

#### References to Chapter 18


1. The Steel Construction Institute (SCI) (1991) *Steelwork Design Guide to BS 5950: Part 1: 1990, Vol. 1, Section Properties, Member Capacities*, 3rd edn. SCI, Ascot, Berks.
2. Advisory Desk (1988) *Steel Construction Today*, 2, Apr., 61–2.
3. Morris L.J. & Randall A.L. (1979) *Plastic Design*. Constrado. (See also *Plastic Design (Supplement)*, Constrado, 1979.)

4. Horne M.R. (1964) Safe loads on I-section columns in structures designed by plastic theory. *Proc. Instn Civ. Engrs*, **29**, Sept., 137–50 and *Discussion*, **32**, Sept. 1965, 125–34.
5. Brown B.A. (1988) The requirements for restraint in plastic design to BS 5950. *Steel Construction Today*, **2**, 184–96.
6. Morris L.J. (1981 & 1983) A commentary on portal frame design. *The Structural Engineer*, **59A**, No. 12, 394–404 and **61A**, No. 6, 181–9.
7. Morris L.J. & Plum D.R. (1988) *Structural Steelwork Design to BS 5950*. Longman, Harlow, Essex.
8. Horne M.R. & Ajmani J.L. (1972) Failure of columns laterally supported on one flange. *The Structural Engineer*, **50**, No. 9, Sept., 355–66.
9. Nethercot D.A. & Lawson R.M. (1992) *Lateral stability of steel beams and columns – common cases of restraint*. SCI publication 093, The Steel Construction Institute.

### **Further reading for Chapter 18**

- Chen W.F. & Atsuta T. (1977) *Theory of Beam-Columns, Vols 1 and 2*. McGraw-Hill, New York.
- Galambos T.V. (1988) *Guide to Stability Design Criteria for Metal Structures*, 4th edn. Wiley, New York.
- Horne M.R. (1979) *Plastic Theory of Structures*, 2nd edn. Pergamon, Oxford.
- Horne M.R., Shakir-Khalil H. & Akhtar S. (1967) The stability of tapered and haunched beams. *Proc. Instn Civ. Engrs*, **67**, No. 9, 677–94.
- Morris L.J. & Nakane K. (1983) Experimental behaviour of haunched members. In *Instability and Plastic Collapse of Steel Structures* (Ed. by L.J. Morris), pp. 547–59. Granada.

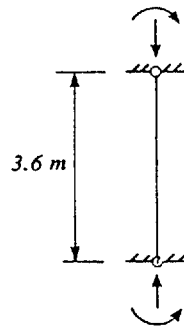
A series of worked examples follows which are relevant to Chapter 18.

|   |   |  |
|---|---|--|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>BEAM-COLUMN EXAMPLE 1</b><br/><b>ROLLED UNIVERSAL COLUMN</b></p> | <p>Chapter ref.</p> <p><b>18</b></p>                   |
|   | <p>Design code</p> <p><b>BSS950: Part 1</b></p>                                       | <p>Made by <b>DAN</b></p> <p>Checked by <b>GWO</b></p> |

**Problem**

Select a suitable UC in grade 43 steel to carry safely a combination of 940 kN in direct compression and a moment about the minor axis of 16 kNm over an unsupported height of 3.6 m.

Problem is one of uniaxial bending producing failure by buckling about the minor axis. Since no information is given on distribution of applied moments make conservative (& simple) assumption of uniform moment ( $\beta = 1.0$ ).



Try 203 × 203 × 60 UC - member capacities suggest  $P_{cy}$  of approximately 1400 kN will provide correct sort of margin to carry the moment

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$$r_y = 5.19 \text{ cm} \qquad Z_y = 199 \text{ cm}^3$$

$$A = 75.8 \text{ cm}^2 \qquad S_y = 303 \text{ cm}^3$$

$$\lambda_y = 3600/51.9 = 69.4 \qquad \text{4.7.3}$$

Use Table 27c for  $p_c$  Table 25

$$\text{For } p_y = 275 \text{ N/mm}^2 \text{ and } \lambda = 69.4$$

$$\text{value of } p_c = 183 \text{ N/mm}^2$$


$$P_{cy} = 183 \times 7580 = 1387 \times 10^3 \text{ N} \qquad \text{4.7.4}$$

$$= 1387 \text{ kN}$$

$$\frac{940}{1387} + \frac{16}{275 \times 199000 \times 10^{-6}} = 0.68 + 0.29 \qquad \text{4.8.3.3.1}$$

$$= 0.97$$

∴ Adopt 203 × 203 × 60 UC

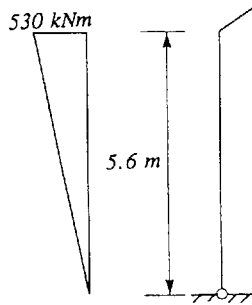
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|   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |
| <p><i>The determination of <math>P_{cy}</math> assumed that the section is not slender; similarly the use of Clause 4.8.3.3.1 in the present form presumes that the section is not slender. The actual stress distribution in the flanges will vary linearly due to the minor axis moment component of the load. Since the actual case cannot be more severe than uniform compression, check classification for pure compression.</i></p> |  |   | 3.5                       |
| <p><i>Flange limiting <math>b/T</math> = 15</i></p>   |  |   | <i>Table 7</i>            |
| <p><i>Web limiting <math>d/t</math> = 39</i></p>  |  |   |                           |
| <p><i>Actual <math>b/T</math> = 7.23</i></p>  |  |   |                           |
| <p><i>Actual <math>d/t</math> = 17.3</i></p>  |  |   |                           |
| <p><i>∴ <u>section is not slender</u></i></p>   |  |   |                           |

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**Problem**

Check the suitability of a 533 × 210 × 82 UB in grade 50 steel for use as the column in a portal frame of clear height 5.6 m if the axial compression is 160 kN, the moment at the top of the column is 530 kNm and the base is pinned. The ends of the column are adequately restrained against lateral displacement (i.e. out of the plane) and rotation.

Loading corresponds to compression and major axis moment distributed as shown. Check initially over full height.



|                |   |                       |     |                           |       |                              |
|----------------|---|-----------------------|-----|---------------------------|-------|------------------------------|
| $r_y$          | = | 4.38 cm               | $u$ | =                         | 0.865 | Steelwork Design Guide Vol 1 |
| $S_x$          | = | 2060 cm <sup>3</sup>  | $x$ | =                         | 41.6  |                              |
| $A$            | = | 104 cm <sup>2</sup>   |     |                           |       |                              |
| $p_y$          | = | 355 N/mm <sup>2</sup> |     |                           |       | Table 6                      |
| $\lambda_y$    | = | 5600/43.8             | =   | 128                       |       | 4.7.3                        |
| $\lambda/x$    | = | 128/41.6              | =   | 3.08                      |       |                              |
| $v$            | = | 0.91                  |     |                           |       | Table 14                     |
| $\lambda_{LT}$ | = | 0.865 × 0.91 × 128    | =   | 101                       |       | 4.3.7.5                      |
| $p_b$          | = | 139 N/mm <sup>2</sup> |     |                           |       | Table 11                     |
| $M_b$          | = | 139 × 2060000         | =   | 286 × 10 <sup>6</sup> Nmm |       | 4.3.7.3                      |
|                |   |                       | =   | 286 kNm                   |       |                              |

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|  | Design code<br><b>BSS5950: Part 1</b>                                      | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |
| <p><i>Use Table 27b for <math>p_c</math></i> <span style="float: right;"><i>Table 25</i></span></p> <p>for <math>\lambda_y = 128</math>    <math>p_c = 103 \text{ N/mm}^2</math> <span style="float: right;"><i>Table 27b</i></span></p> <p><math>P_{cy} = 103 \times 10400 = 1071 \times 10^3 \text{ N} = 1071 \text{ kN}</math> <span style="float: right;"><i>4.7.4</i></span></p> <p>For <math>\beta = 0/530 = 0</math>    take <math>m = 0.57</math> <span style="float: right;"><i>Table 18</i></span></p> <p><math>\frac{\overline{M}}{M_b} = \frac{0.57 \times 530}{286} = 1.06</math></p> <p><i>∴ member has insufficient buckling resistance moment. Check moment capacity</i></p> <p><math>M_{cx} = 355 \times 2060000 = 731 \times 10^6 \text{ Nmm}</math><br/> <math>= 731 \text{ kNm}</math></p> <p><i>∴ section capacity OK so increase stability by inserting a brace from a suitable side rail to the compression flange. Estimate suitable location as 1.6 m below top.</i></p> <p><i>For upper part of column</i></p> <p><math>\lambda_y = 1600/43.8 = 37</math> <span style="float: right;"><i>4.7.3</i></span></p> <p><math>\lambda/x = 37/41.6 = 0.9</math></p> <p><math>v = 0.99</math> <span style="float: right;"><i>Table 14</i></span></p> <p><math>\lambda_{LT} = 0.865 \times 0.99 \times 37 = 32</math> <span style="float: right;"><i>4.7.3.5</i></span></p> <p><math>p_b = 350 \text{ N/mm}^2</math> <span style="float: right;"><i>Table 11</i></span></p> <p><math>M_b = 350 \times 2060000 = 721 \times 10^6 \text{ Nmm}</math><br/> <math>= 721 \text{ kNm}</math> <span style="float: right;"><i>4.3.7.3</i></span></p> <p><math>p_c = 320 \text{ N/mm}^2</math> <span style="float: right;"><i>Table 27b</i></span></p> <p><math>P_{cy} = 320 \times 10400 = 3328 \times 10^3 \text{ N}</math><br/> <math>= 3328 \text{ kN}</math> <span style="float: right;"><i>4.7.4</i></span></p> |  |   |                           |




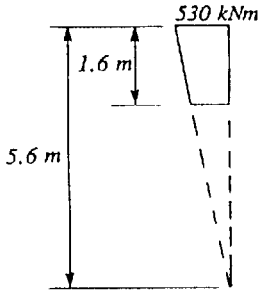
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|   | <p>Design code</p> <p><b>BS5950; Part 1</b></p>                                     | <p>Made by <b>DAN</b></p> <p>Checked by <b>GWO</b></p> |

Table 18



$$\beta = \frac{(5.6 - 1.6)}{5.6} = 0.72$$

$$m = 0.85$$

$$\frac{\overline{M}}{M_b} = \frac{0.85 \times 530}{721} = 0.62$$

$$\frac{P}{P_c} = \frac{160}{3328} = 0.05$$

$$0.05 + 0.62 = 0.67 \text{ OK} \quad 4.8.3.3.1$$

Check lower part of column for moment of

$$0.72 \times 530 = 382 \text{ kNm}$$

$$\lambda_y = 4000/43.8 = 91 \quad 4.7.3$$


$$\lambda/x = 91/41.6 = 2.2$$


$$v = 0.96 \quad \text{Table 14}$$

$$\lambda_{LT} = 0.865 \times 0.96 \times 91 = 76 \quad 4.7.3.5$$

$$p_b = 202 \text{ N/mm}^2$$

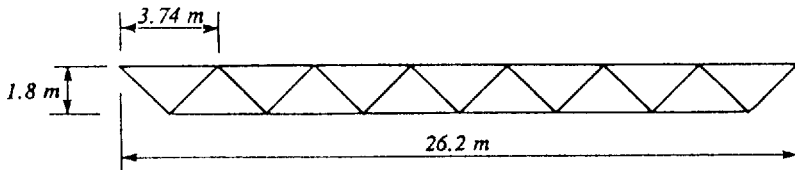
$$M_b = 416 \text{ kNm} \quad 4.7.3.3$$

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|  | Design code<br><b>BS5950: Part 1</b>                                       | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>        |
| <p> <math>P_c = 178 \text{ N/mm}^2</math> <span style="float: right;"><i>Table 27b</i></span> </p> <p> <math>P_{cy} = 1851 \text{ kN}</math> <span style="float: right;"><i>4.7.4</i></span> </p> <p> <math>\frac{\bar{M}}{M_b} = \frac{0.57 \times 382}{416} = 0.52</math> </p> <p> <math>\frac{P}{P_{cy}} = \frac{160}{1851} = 0.09</math> </p> <p> <math>0.09 + 0.52 = 0.61 \text{ OK}</math> <span style="margin-left: 20px;"><i>Use 1 brace</i></span> <span style="float: right;"><i>4.8.3.3.1</i></span> </p> <p> <i>Capacity of cross-section under compression and bending should also be checked at point of maximum coincident values. However, since <math>M_{cx} = 355 \times 2060000 \times 10^{-6} = 731 \text{ kNm}</math> and compression is small by inspection, capacity is OK.</i> </p> <p> <i>As before, use of <math>M_b</math> presumes section is at least compact.</i> </p> <p> <math>b/T \text{ limit} = 9.5\epsilon</math> <span style="float: right;"><i>Table 7</i></span> </p> <p> <math>d/t \text{ limit (pure compression)} = 39\epsilon</math> </p> <p> <i>Since <math>\epsilon = (275/355)^{1/2} = 0.88</math> these are:</i> </p> <p> <i>8.4 and 34.3</i> </p> <p> <i>Actual <math>b/T = 5.98</math></i> </p> <p> <i>Actual <math>d/t = 41.2</math></i> </p> <p> <i><math>\therefore d/t</math> greater than limit for pure compression. However, actual loading is principally bending for which limit is <math>98\epsilon = 86</math></i> </p> <p> <i><math>\therefore</math> without performing a rigorous check (by locating plastic neutral axis position etc.) it is clear that section will meet the limit for principally bending.</i> </p> <p> <i>Section compact</i> </p> <p> <i><math>\therefore</math> <u>Adopt <math>533 \times 210 \times 82 \text{ UC}</math></u></i> </p> |  |   |                           |

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|  |   | Design code<br><b>BS5950: Part 1</b>  | Made by <b>DAN</b><br>Checked by <b>GWO</b> |

**Problem**

Select a suitable RHS in grade 50 material for the top chord of the 26.2 m span truss shown below.



Trusses are spaced at 6 m intervals with purlins at 1.87 m intervals; these may be assumed to prevent lateral deflection of the top chord at these points. Under the action of the applied loading the chord loads in the most severely loaded bay are:

- compression            664 kN
- vertical moment        24.4 kNm
- horizontal moment    19.6 kNm

It is necessary to consider a length between nodes, allowing for the lateral restraint at mid-length under the action of compression plus biaxial bending.


Take  $L_{Ex}$  as distance between nodes and  $L_{Ey}$  as distance between purlins


$L_{Ex} = 3.74 \text{ m}$   
 $L_{Ey} = 1.87 \text{ m}$

Try 150 × 150 × 10 RHS

For  $L_{Ex} = 3.74 \text{ m}$      $P_{cx} = 1560 \text{ kN}$   
 For  $L_{Ey} = 1.87 \text{ m}$      $P_{cy} = 1900 \text{ kN}$   
 $P_z = 1970 \text{ kN}$          $M_{cx} = M_{cy} = 102 \text{ kNm}$

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|   | Design code<br><b>BS5950: Part 1</b>  | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>  |
| <p><i>Check local capacity using "more exact" method for plastic section</i> <span style="float: right;">4.8.3.2(b)</span></p> $\left[ \frac{M_x}{M_{rx}} \right]^{5/3} + \left[ \frac{M_y}{M_{ry}} \right]^{5/3} \leq 1$ <p> <math>F/P_z = 664/1970 = 0.337</math><br/> <math>M_{rx} = M_{ry} = 87 \text{ kNm}</math> </p> $\left[ \frac{24.4}{87} \right]^{5/3} + \left[ \frac{19.6}{87} \right]^{5/3} = 0.120 + 0.083$ $= 0.203 < 1 \text{ local capacity OK}$   |   |   | <i>Steelwork<br/>         Design Guide<br/>         Vol 1</i> |
| <p><i>Check overall buckling using "more exact" method</i> <span style="float: right;">4.8.3.3.2</span></p> $\left[ \frac{m M_x}{M_{ax}} \right] + \left[ \frac{m M_y}{M_{ay}} \right] \leq 1$ <p> <i>Take <math>m = 1.0</math> for both axes since exact moment distributions not given; this will be conservative</i> </p> $M_{ax} = M_{cx} \frac{(1 - F/P_{cx})}{(1 + 1/2 \times F/P_{cx})}$ $= 102 \frac{(1 - 664/1560)}{(1 + 1/2 \times 664/1560)} = 48.3 \text{ kNm}$ <p> <i>For RHS, in-plane case will govern for <math>M_{ay}</math></i> </p> $M_{ay} = M_{cy} \frac{(1 - F/P_{cy})}{(1 + 1/2 \times F/P_{cy})}$ $= 102 \frac{(1 - 664/1900)}{(1 + 1/2 \times 664/1900)} = 56.5 \text{ kNm}$ |   |   |   |

|   |   |   |                           |
|---|---|---|---------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>BEAM-COLUMN EXAMPLE 3<br/>         RHS IN BIAXIAL BENDING</b> |   | Chapter ref.<br><b>18</b> |
|   | Design code<br><b>BS5950: Part 1</b>  | Made by <b>DAN</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>        |

$$\left[ \frac{24.4}{48.3} \right] + \left[ \frac{19.6}{56.5} \right] = 0.505 + 0.347$$

$$= 0.852 < 1 \text{ overall buckling OK}$$

∴ Adopt 150 × 150 × 10 RHS

Care is needed if the simplified approach of Clause 4.8.3.3.1 is used since this presumes that  $F$  and  $M_x$  would produce a lateral-torsional buckling failure. Since  $M_b = M_{cx}$  for RHS this will not be the case. One possibility would be to approximate the in-plane interactions for  $M_x$  &  $M_y$  in the same way using

$$\frac{F}{A_g p_c} + \frac{m M_x}{p_y Z_x} + \frac{m M_y}{p_y Z_y} \leq 1$$

$$\frac{664}{1560} + \frac{24.4}{85} + \frac{19.6}{85} = 0.426 + 0.287 + 0.231$$

$$= 0.944 \leq 1 \text{ OK}$$

For this example since  $m = 1.0$  has been used throughout overall buckling will always control.

# Chapter 19

## Trusses

by PAUL TASOU

### 19.1 Common types of trusses

#### 19.1.1 Buildings

The most common use of trusses in buildings is to provide support to roofs, floors and such internal loading as services and suspended ceilings. There are many types and forms of trusses; some of the most widely used are shown in Fig. 19.1. The type of truss adopted in design is governed by architectural and client requirements, varied in detail by dimensional and economic factors.

The Pratt truss, Fig. 19.1(a) and (e), has diagonals in tension under normal vertical loading so that the shorter vertical web members are in compression and the longer diagonal web members are in tension. This advantage is partially offset by the fact that the compression chord is more heavily loaded than the tension chord at mid-span under normal vertical loading. It should be noted, however, that for a light-pitched Pratt roof truss wind loads may cause a reversal of load thus putting the longer web members into compression.

The converse of the Pratt truss is the Howe truss (or English truss), Fig. 19.1(b). The Howe truss can be advantageous for very lightly loaded roofs in which reversal of load due to wind will occur. In addition the tension chord is more heavily loaded than the compression chord at mid-span under normal vertical loading. The Fink truss, Fig. 19.1(c), offers greater economy in terms of steel weight for long-span high-pitched roofs as the members are subdivided into shorter elements. There are many ways of arranging and subdividing the chords and web members under the control of the designer.

The mansard truss, Fig. 19.1(d), is a variation of the Fink truss which has the advantage of reducing unusable roof space and so reducing the running costs of the building. The main disadvantage of the mansard truss is that the forces in the top and bottom chords are increased due to the smaller span-to-depth ratio.

However, it must not escape the designer's mind that any savings achieved in steel weight by introducing a greater number of smaller members may, as is often the case, substantially increase fabrication and maintenance costs.

The Warren truss, Fig. 19.1(f), has equal length compression and tension web members, resulting in a net saving in steel weight for smaller spans. The added advantage of the Warren truss is that it avoids the use of web members of differing length and thus reduces fabrication costs. For larger spans the modified

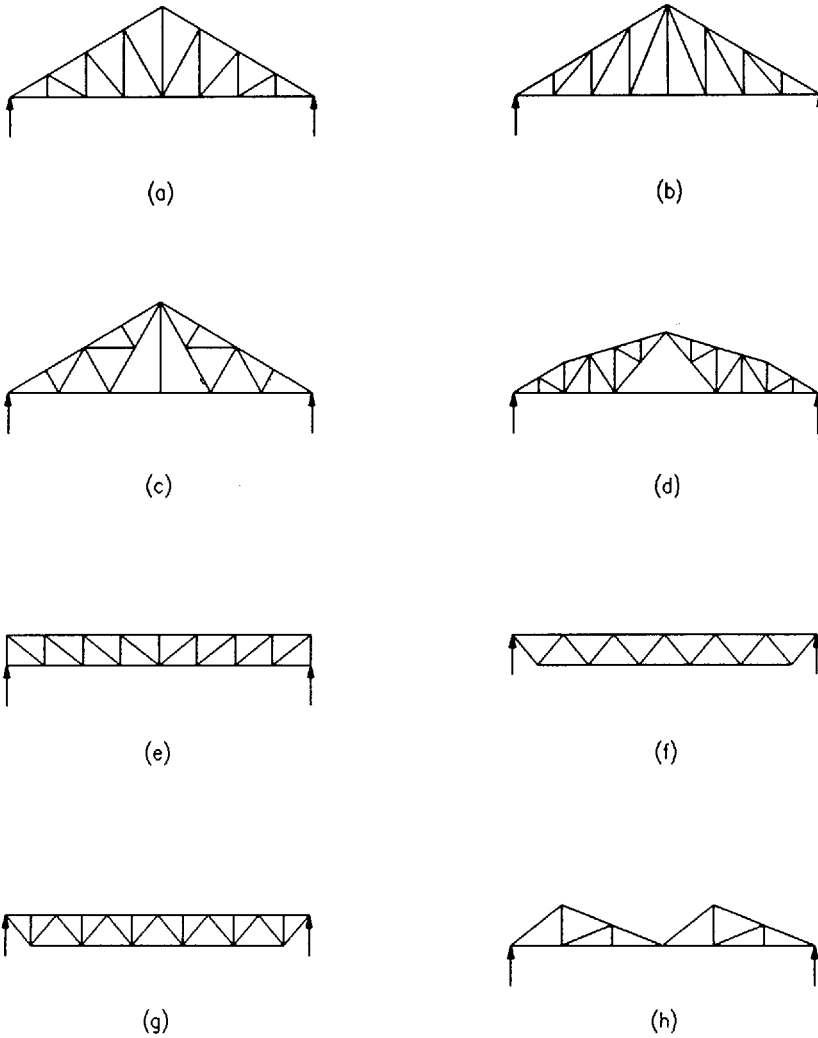


Fig. 19.1 Common types of roof trusses: (a) Pratt – pitched, (b) Howe, (c) Fink, (d) mansard, (e) Pratt – flat, (f) Warren, (g) modified Warren, (h) saw-tooth

Warren truss, Fig. 19.1(g), may be adopted where additional restraint to the chords is required (this also reduces secondary stresses). The modified Warren truss requires more material than the parallel-chord Pratt truss, but this is offset by its symmetry and pleasing appearance. The saw-tooth or butterfly truss, Fig. 19.1(h), is just one of many examples of trusses used in multi-bay buildings, although the other types described above are equally suitable.

### 19.1.2 Bridges

Trusses are now infrequently used for road bridges in the UK because of high fabrication and maintenance costs. However, the recent award-winning Brinnington railway bridge (Fig. 19.2) demonstrates that they can still be used to create efficient and attractive railway structures. In many parts of the world, particularly the Third World countries where labour costs are low and material costs are high, trusses are often adopted for their economy in steel. Their structural form also lends itself to transportation in small components and piece-small erection, which may be suitable for remote locations.



*Fig. 19.2* Brinnington Railway Bridge



Some of the most commonly used trusses suitable for both road and rail bridges are illustrated in Fig. 19.3. Pratt, Howe and Warren trusses, Fig. 19.3(a), (b) and (c), which are discussed in section 19.2.1, are more suitable for short to medium spans. The economic span range of the Pratt and Howe trusses may be extended by subdividing the diagonals and the deck support chord as shown for the Petit truss, Fig. 19.3(h), although this often gives rise to high secondary stresses for short to medium spans. In the case of the Warren truss the unsupported length of the chords may be too great for the economic span and depth range, in such a case the modified Warren truss, Fig. 19.3(d), is more appropriate.

The variable depth type truss such as the Parker, Fig. 19.3(e), offers an aesthetically pleasing structure. With this type of truss its structural function is emphasized and the material is economically distributed at the cost of having expensive fabrication due to the variable length and variable inclination of the web and top chord members.

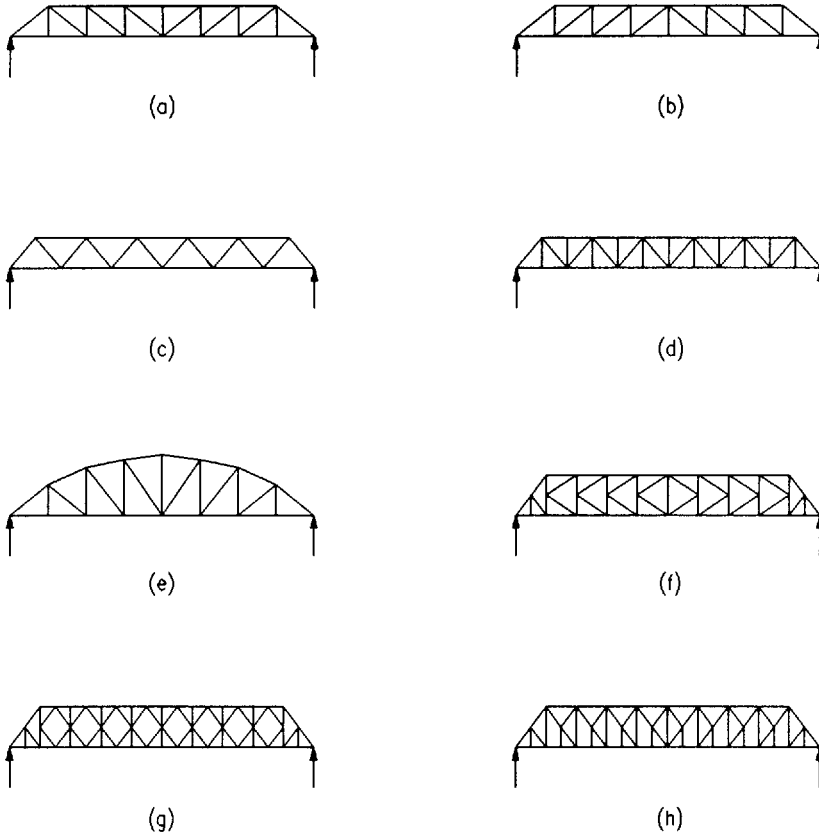


Fig. 19.3 Common types of bridge trusses: (a) Pratt, (b) Howe, (c) Warren, (d) modified Warren, (e) Parker, (f) K, (g) diamond, (h) Petit

For economy the truss depth is ideally set at a fixed proportion of the span. As the span increases the truss depth and bay width increase accordingly. The bay width is usually fixed by providing truss nodes on the centrelines of the deck cross-beams, thus avoiding high local bending stress in the deck chord. For large-span bridges with an economical spacing for the deck cross-beams, the height of the truss may be as much as four times the bay width. In such a case a subdivided form of truss will be required to avoid very long uneconomical compression web members, or tensile members subjected to load reversal due to moving live loads. The diamond, Petit and K-trusses, Fig. 19.3(g), (h) and (f), are just three types which can be used.

The diamond and Petit trusses have the advantage of having shorter diagonals than the K-truss. The main disadvantage of trusses such as the diamond or Petit, which have intermediate bracing members connected to the chords away from the main joints, is that they give rise to high secondary stresses for short to medium spans due to differential joint deformations caused by moving live loads. The K-truss is far superior in this respect.

## 19.2 Guidance on overall concept

### 19.2.1 Buildings

For pitched-roof trusses such as the Pratt, Howe or Fink, Fig. 19.1(a), (b) and (c), the most economical span-to-depth ratio (at apex) is between 4 and 5, with a span range of 6 m to 12 m, the Fink truss being the most economical at the higher end of the span range. Spans of up to 15 m are possible but the unusable roof space becomes excessive and increases the running costs of the building. In such circumstances the span-to-depth ratio may be increased to about 6 to 7, the additional steel weight (increase in initial capital expenditure) being offset by the long-term savings in the running costs. For spans of between 15 m and 30 m, the mansard truss, Fig. 19.1(d), reduces the unusable roof space but retains the pitched appearance and offers an economic structure at span-to-depth ratios of about 7 to 8.

The parallel (or near parallel) chord trusses (also known as lattice girders) such as the Pratt or Warren, Fig. 19.1(e) and (f), have an economic span range of between 6 m and 50 m, with a span-to-depth ratio of between 15 and 25 depending on the intensity of the applied loads. For the top end of the span range the bay width should be such that the web members are inclined at approximately  $50^\circ$  or slightly steeper. For long, deep trusses the bay widths become too large and are often subdivided with secondary web members.

For roof trusses the web member intersection points with the chords should ideally coincide with the secondary transverse roof members (purlins). In practice this is not often the case for economic truss member arrangements, thus resulting in the supporting chord being subject to local bending stresses.

The most economical spacing for roof trusses is a function of the span and load intensity and to a lesser extent the span and spacing of the purlins, but as a general rule the spacing should be between  $\frac{1}{4}$  and  $\frac{1}{5}$  of the span, which results in a spacing of between 4 m and 10 m for the economic range of truss spans.

For short-span roof trusses between 6 m and 15 m the minimum spacing should be limited to 3–4 m.

### 19.2.2 Bridges

Road and railway truss bridges can either be underslung (deck at top chord level), through (deck at bottom chord level) or semi-through.

Limits on headroom, navigation height and construction depth will determine whether an underslung or through truss will be the most appropriate. For large-span bridges the through type is often adopted as ample headroom will be available to permit direct lateral restraint to the top compression chord using cross bracing. For short-span bridges however, the underslung type is most appropriate provided the navigation height or construction depth limits are satisfied. Underslung trusses are usually more economical than either through or semi-through trusses as the deck structure performs the dual function of directly supporting the traffic loads and providing lateral restraint to the compression chords. In the case of short-span through trusses the span-to-depth ratio may be uneconomically low if the top chord is restrained by cross-beams, as sufficient traffic headroom must be provided. In such a situation it is more economical to brace the top compression chords by U-frame action.

A span-to-depth ratio of between 6 and 8 for railway bridges and between 10 and 12 for road bridges offers the most economical design. In general terms the proportions should be such that the chords and web members have approximately an equal weight.

The bay widths should be proportioned so that the diagonal members are inclined at approximately  $50^\circ$  or slightly steeper. For large-span trusses subdivision of the bays is necessary to avoid having excessively long web members.

The Pratt, Howe and Warren trusses, Fig. 19.3(a)–(c), have an economic span range of between 40 m and 100 m for railway bridges and up to 150 m for road bridges. For the shorter spans of the range the Warren truss requires less material than either the Pratt or the Howe trusses. For medium spans of the range the Pratt or Howe trusses are both more favourable and by far the most common types. For large spans the modified Warren truss and subdivided Parker (inclined chord) truss are the most economical.

For spans of between 100 m and 250 m the depth of the truss may be up to four times the economic bay width, and in such a case the K-, diamond or Petit (subdivided Pratt or Howe) trusses are more appropriate. For the shorter spans of the range the diamond or Petit trusses, by their nature, are subject to very high secondary stresses. In such a case the K-truss, with primary truss members at all

nodes, is more appropriate as joint deflections are uniform, greatly reducing the secondary stresses.

For spans greater than 150 m variable depth trusses are normally adopted for economy.

The spacing of bridge trusses depends on the width of the carriageway for road bridges and the required number of tracks for railway bridges, in addition to considerations regarding lateral strength and rigidity. However, in general the spacing should be limited to between  $\frac{1}{18}$  and  $\frac{1}{20}$  of the span, with a minimum of 4 m to 5 m for through trusses and approximately  $\frac{1}{15}$  of the span, with a minimum of 3 m to 4 m, for underslung trusses.

### 19.3 Effects of load reversal

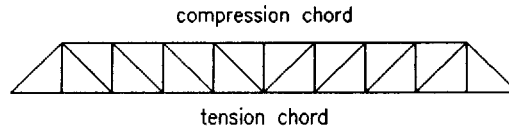
For buildings with light pitched roofs, load reversal is often caused by wind suction and internal pressure. Load reversal caused by wind load is of particular importance as light sections normally acting as ties under dead and imposed loads may be severely overstressed or even fail by buckling when required to act as struts. For heavy pitched or flat roofs load reversal is rarely a problem because the dead load usually exceeds the wind uplift forces.

For bridge trusses, load reversal in the component elements may be caused by the erection technique adopted or by moving live loads, particularly in continuous bridges. During the detailed design stage, consideration should be given to the method of erection to ensure stability and adequacy of any member likely to experience load reversal. For short-span simply-supported trusses erected whole, load reversal in the chords and web members is attained if the crane pick-up points during erection are at or near mid-span, Fig. 19.4(a) and (b). For large-span bridges, erection by the cantilever method causes load reversal in the chords and web members. Load reversal caused by moving loads is usually more significant in continuous trusses. A convenient way of overcoming the problem of load reversal in web elements which are likely to buckle is to provide either temporary or permanent counter bracing, Fig. 19.4(c). This will ensure that the web elements are always in tension under all load conditions and avoids the use of heavy compression elements.

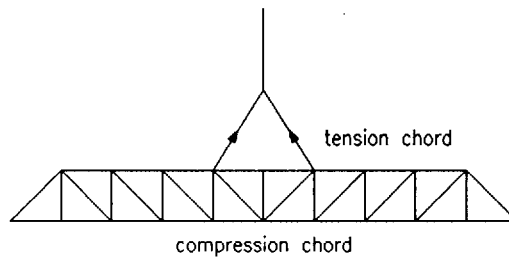
## 19.4 Selection of elements and connections

### 19.4.1 Elements

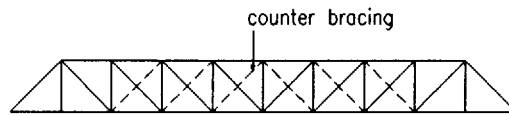
For light roof trusses in buildings the individual members are normally chosen from rolled sections for economy; these are illustrated in Fig. 19.5(a). Structural hollow sections are becoming more popular due to their efficiency in compression



(a)



(b)

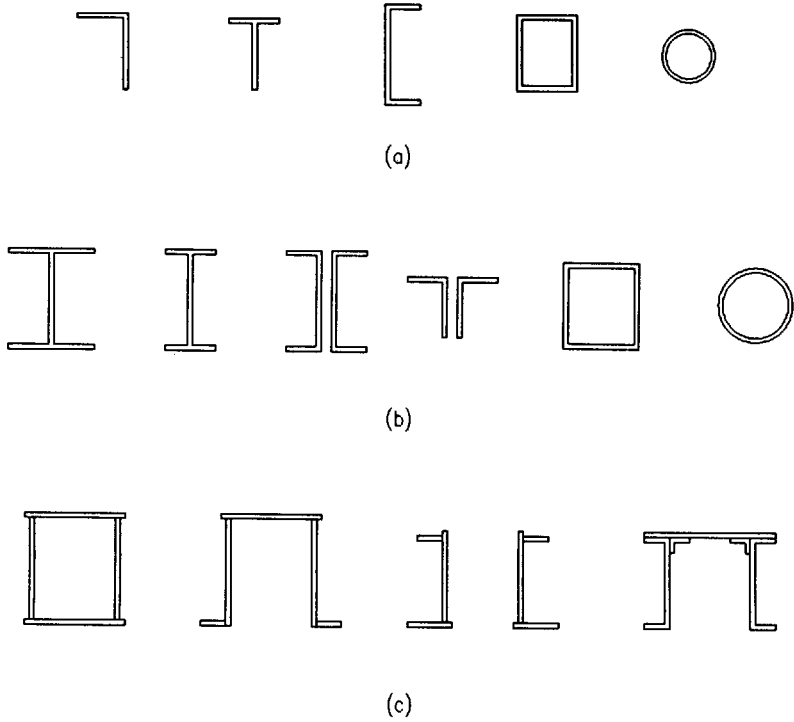


(c)

Fig. 19.4 Effects of load reversal. (a) Normal loading; (b) reversal during erection; (c) counter bracing

and their neat and pleasing appearance in the case of exposed trusses. Structural hollow sections, however, have higher fabrication costs and are only suited to welded construction. For larger-span heavily-loaded roof trusses and small span bridge trusses it often becomes necessary to use heavier sections such as rolled universal beams and columns and multiples of the smaller rolled sections such as back-to-back angles and channels, Fig. 19.5(b).

For large-span bridge trusses, compound or fabricated sections are normally necessary, particularly for the chords and the compression web members. Figure 19.5(c) illustrates some typical arrangements often used, although the choice available to the designer is very wide. For heavily-loaded bridge trusses, fabricated box sections offer economy in material due to their high efficiency in compression.



*Fig. 19.5* Typical element cross sections. (a) Light building trusses; (b) heavy building trusses and light, small-span bridges; (c) road and railway bridges

The open sections shown assist the connections to the web members of the truss but require lacing or battening and are prone to distortion during fabrication.

Providing suitable access to all members and surfaces for inspection, cleaning and painting should be a primary consideration in deciding on the sections and details to be incorporated in the design. Laced sections are disadvantageous in this respect as access can be severely restricted. In highly corrosive environments welded closed box or circular hollow sections with welded connections are usually used in order to reduce maintenance costs as all exposed surfaces are readily accessible.

**19.4.2 Connections**

There are basically three types of connections used for connecting truss elements to each other, that is, welding, bolting and riveting. Riveting is rarely used in the UK due to the very high labour costs involved, although it is still widely used in

Third World countries where labour costs are low. Small-span trusses which can be transported whole from the fabrication shop to the site can be entirely welded. In the case of large-span roof trusses which cannot be transported whole, welded sub-components are delivered to site and are either bolted or welded together on site. Generally in steelwork construction bolted site splices are much preferred to welded splices for economy and speed of erection. In light-building roof trusses entirely bolted connections are less favoured than welded connections due to the increased fabrication costs, and usually bolted connections require cumbersome and obtrusive gusset plates. However, bolted connections are more widely used in bridge trusses, particularly medium- to large-span road bridges and railway bridges, due to their improved performance under fatigue loading. In addition, bolted connections may sometimes permit site erection of the individual elements without the need for expensive heavy craneage. Gusset plates are often associated with bolted bridge trusses, their size being dependent on the size of the incoming members and the space available for bolting.

Gusset plates also enable the incoming members to be positioned in such a way that their centroidal axes meet at a single point thus avoiding load eccentricities. Ideally for all types of trusses the connections should be arranged so that the centres of gravity of all incoming members meeting at the joint coincide. If this is not possible the out-of-balance moments caused by the eccentricities must be taken into account in the design.

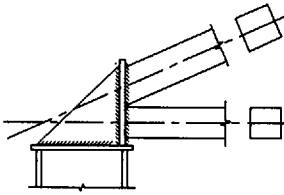
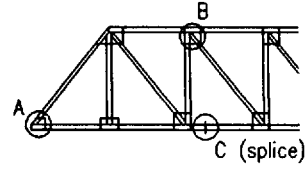
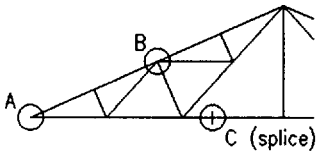
Some typical joint details are illustrated in Fig. 19.6.

## 19.5 Guidance on methods of analysis

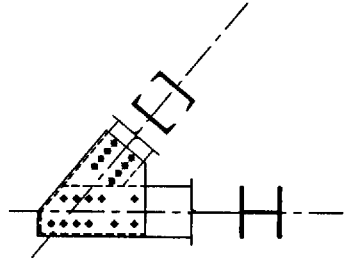
Loads are generally assumed to be applied at the intersection points of the members, so that they are principally subjected to direct stresses. To simplify the analysis the weights of the truss members are assumed to be apportioned to the top and bottom chord panel points and the truss members are assumed to be pinned at their ends, even though this is usually not the case. Normally chords are continuous and the connections are either welded or contain multiple bolts; such joints tend to restrict relative rotations of the members at the nodes and end moments develop.

Generally, in light building trusses secondary stresses are negligible and are often ignored. Guidance on whether or not to consider secondary stresses in light building trusses is given in BS 5950: Part 1. In accordance with clause 4.10, secondary stresses may be neglected provided that:

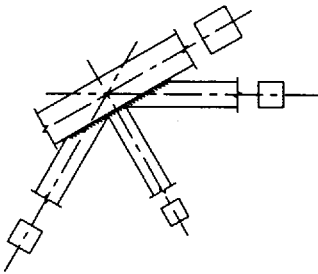
- the slenderness of the chord members in the plane of the truss is greater than 50, and
- the slenderness of most of the web members, about the same axis, is greater than 100.



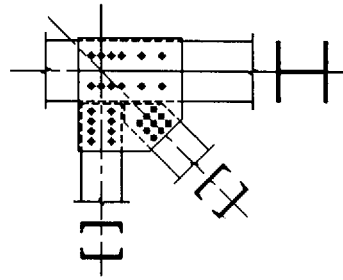
connection A



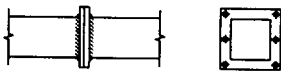
connection A



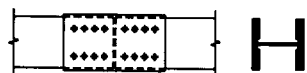
connection B



connection B



connection C



connection C

(a)

(b)

*Fig. 19.6* Typical joints in trusses. (a) Welded RHS building roof truss; (b) bolted bridge truss



However in bridge trusses, the secondary stresses can be a significant proportion of the primary stresses and must be taken into account. The British Standard for the design of steel bridges, BS 5400: Part 3, 1982, requires the fixity of the joints to be taken into account although axial deformation of the members may be ignored for the ultimate limit state.

The magnitude of the secondary stresses depends on a number of factors including member layout, joint rigidity, the relative stiffness of the incoming members at the joints and lack of fit.

Manual methods of analysis are often adopted to analyse the stresses, particularly in simple trusses. For simple, statically-determinate trusses, methods of analysis include joint resolution, graphical analysis (Bow's notation or Maxwell diagram) and the method of sections. The last method is particularly useful as the designer can limit the analysis to the critical sections.

Statically-indeterminate trusses are more laborious to analyse manually; methods available include virtual work, least work and the reciprocal theorem with influence lines. For a full discussion on these methods of analysis the reader should refer to textbooks on structural analysis.

Computers are nowadays readily available to designers and provide a useful means of analyzing the most complex of trusses. In addition, joint and member rigidities can easily be incorporated in the modelling thus avoiding laborious hand calculations in determining out-of-balance moments caused by joint deformations. Local stresses caused by loads not applied at the panel points, joint eccentricities and axial deformation should generally be calculated and superimposed on the direct stresses. However, stresses due to axial deformation are normally neglected except for bridge trusses and trusses of major importance.

Careful consideration must be given to the out-of-plane stability of a truss and resistance to lateral loads such as wind loads or eccentric loads causing torsion about their longitudinal axis. An individual truss is very inefficient and generally sufficient bracing must be provided between trusses to prevent instability. In bridges, plan bracing is normally provided between trusses at the chord levels in addition to stiff end portals to prevent lateral instability.

## **19.6 Detailed design considerations for elements**

### **19.6.1 Design loads**

The current British Standards for steel structures in buildings and bridges are both limit-state codes. The magnitude of the partial load factors to be applied is dependent on the load type, the load combination and the limit state (ultimate or serviceability) under consideration.

The following approach may be adopted in deriving the critical load combinations for each truss member:

- (1) The member forces and moments are calculated for each, unfactored, load type (dead, superimposed dead, imposed, wind, etc.) using an appropriate method of analysis.
- (2) Load combinations are identified and the appropriate load factors for each combination applied for both serviceability and ultimate limit states.
- (3) The critical loads in each element and joint are extracted for both limit states.

The above process is long-winded but with experience the designer can often take short cuts in determining the critical load combinations for each element.

In the analysis the member forces and moments due to joint fixity should be calculated and superimposed on the global member forces. For trusses in buildings to BS 5950: Part 1: 1985, the secondary effects due to joint fixity may be ignored provided the slenderness, in the plane of the truss, is greater than 50 for the chord elements and 100 for most of the web members. If this condition is satisfied the members are assumed to be pin jointed in the analysis. Secondary effects due to axial deformations are usually ignored in building trusses. Local effects due to joint eccentricities and where loads are not applied at nodes should be taken into account.

For bridge trusses to BS 5400: Part 3: 1982, the effects of joint rigidity are required to be taken into account. Secondary stresses due to axial deformations may be ignored at the ultimate limit state but should be considered at the serviceability limit state and for fatigue checks. As for building trusses, the local effects due to joint eccentricities and cases where loads are not applied at nodes must be considered in bridge trusses.

### **19.6.2 Effective length of compression members**

For building trusses the fixity of the joints and the rigidity of adjacent members may be taken into account for the purpose of calculating the effective length of compression members. BS 5950: Part 1: 1985 limits the maximum slenderness permissible in struts to the following:

- 180 for members resisting loads other than wind loads
- 250 for members resisting self-weight and wind loads
- 350 for members normally acting as a tie but subject to load reversal under wind action.

In addition, members whose slenderness exceeds 180 must be checked for self-weight deflection. If this exceeds  $(\text{length}/1000)$  the effect of bending should be taken into account.

The designer should be careful to ensure that he identifies the critical slenderness. For chords, out-of-plane unrestrained lengths do not necessarily relate to the truss nodes and effective length factors are usually unity; in-plane effective length

factors may be demonstrated to be less than unity if the restraining actions of tension members and non-critical compression members are mobilized at the ends of the member. Single angle elements, both for the webs and chord, have minimum radii of gyration that do not lie either in, or normal to, the plane of the truss.

For compression members in bridge trusses the effective lengths may either be obtained from Table 11 of BS 5400: Part 3: 1982 or be determined by an elastic critical buckling analysis of the truss.

In the case of simply supported underslung trusses the top compression chord will be effectively restrained laterally throughout its length provided the connection between the chord and the deck is capable of resisting a uniformly distributed lateral force of 2.5% of the maximum force in the chord. The effective length in such a case is taken as zero where friction provides the restraint, or as equal to the spacing of discrete connections where these are provided.

The economic advantages of underslung trusses over through or semi-through trusses is obvious in this respect, due to the dual function of the deck structure.

In the case of unbraced compression chords, that is, chords with no lateral restraints, the provision of U-frames is necessary. The effective length of the compression chord is a function of the stiffness of the chord and the spacing and stiffness of the U-frame members. Clause 12.5 of BS 5400: Part 3: 1982 gives guidance on the calculation of the effective length of compression chords restrained by U-frames.

### **19.6.3 Detailed design**

For building trusses to BS 5950 the members need only be designed at the ultimate limit state for strength, stability and fatigue where applicable, and at the serviceability limit state for deflection and durability.

Compression members in bridge trusses to BS 5400 are designed at both the ultimate and serviceability limit states. Certain compression members, however, are exempt from the serviceability limit state check as defined in clause 12.2.3 of BS 5400: Part 3. Tension members need only be designed at the ultimate limit state.

For guidance on the detailed design of axially loaded members the reader should refer to Chapters 14 and 15, and to Chapter 18 for members subject to combined axial load and bending.

## **19.7 Factors dictating the economy of trusses**

Some of the general factors dictating the economy of trusses relating to truss type, spacing, span-to-depth ratios, pitch, etc. have already been discussed earlier. However, factors such as the location of the structure, contractors' experience

and material availability, may have a significant effect on the choice of truss type and details adopted. When designing trusses for overseas locations, particularly the Third World countries or for remote areas with difficult access, the designer should consider the following:

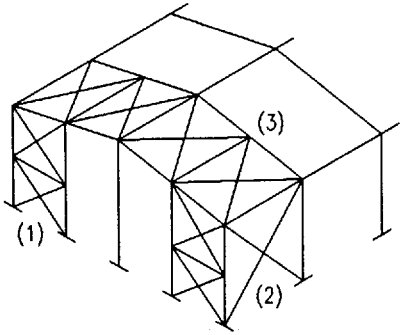
- Material available locally, i.e. weldable or unweldable steel
- Preferred connections, i.e. welded, bolted or riveted
- Maximum size of elements that can be transported to site
- Method of erection, capacity and type of plant available
- Use of rolled, compound or fabricated sections
- Redundancy of structure in case of overloading and lack of maintenance
- Experience of local contractors
- Simple design with maximum repetition.

The designer should always try to maximize the use of local materials, labour and expertise so as to avoid expensive importation of materials and trained manpower. In addition, the relative costs between materials and labour should be reflected in the design. For Third World countries material costs are often high and labour costs are very low, whereas the reverse is true for developed countries.

## 19.8 Other applications of trusses

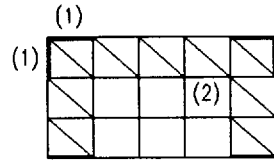
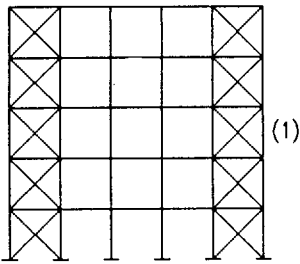
Trusses are often used as secondary structures in buildings and bridges in the form of triangulated bracing. Bracing is generally required to resist horizontal loading in buildings or bridges or to prevent deformations and provide torsional rigidity to stiffening girders or box girders.

In buildings, bracing is often required for stability and to transmit horizontal wind loads or crane surges down to foundation level. To avoid the use of heavy compression bracing members, the members are usually arranged so that they always act in tension. Although this requires a high degree of redundancy it is normally more economical than providing compression members. Some examples of wind bracing to single-storey building are illustrated in Fig. 19.7(a). For multi-storey buildings with 'simple' connections, vertical bracing is required on all elevations to stabilize the building. Normally the floor slabs act as horizontal bracing which transmits the lateral wind loads to the vertical bracing. If the steel frame to the building is erected before the floors are constructed, temporary horizontal bracing must be supplied which can be removed once the floors are in place. Bracing at floor levels may be required if the slabs are discontinuous. Although horizontal bracing in buildings can often be hidden within the depth of the floor, vertical bracing can be obtrusive and undesirable, particularly if the building is clad in glass. In such an instance rigidly-jointed frames are adopted in which the wind loading is resisted by bending in the beams and stanchions. However, if the joints to such frames are made with friction-grip bolts, then



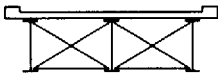
- (1) transverse vertical bracing
- (2) longitudinal vertical bracing
- (3) plan bracing

(a)

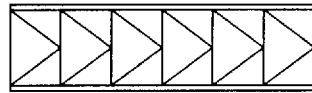


- (1) vertical bracing
- (2) plan bracing

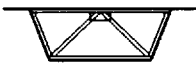
(b)



vertical bracing to plate girders

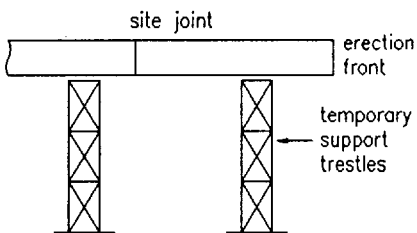


plan bracing between trusses



internal bracing to box girder

(c)



(d)

Fig. 19.7 Other applications of trusses. (a) Bracing to single-storey building; (b) bracing to multi-storey building; (c) typical bracing to bridges; (d) other uses

temporary bracing may be required for stability prior to the joints being completed. Figure 19.7(b) illustrates some typical bracing systems to multi-storey buildings.

In bridges, secondary truss or bracing frames are often required for stability and to resist lateral loads due to wind in addition to loads due to road and railway loading such as centrifugal or braking forces. Depending on the type of structure the bracing may be temporary or permanent, usually placed in both horizontal and vertical planes. For trusses, permanent plan bracing is provided at both chord levels for underslung bridges and at deck level for through or semi-through bridges. Where headroom permits, plan bracing is also provided at the top chord level for through trusses thus conveniently providing restraint to the top compression chord and avoiding the need for stiff U-frames. In addition, vertical bracing is also provided between trusses to reduce differential loading and therefore distortion between trusses and to provide added restraint to the compression chord.

In composite steel plate girder and concrete slab decks temporary vertical bracing may be required when the concrete is poured to provide lateral restraint to the plate girder compression flanges. It may be removed once the concrete has gained sufficient strength to act compositely with the steelwork. In stiffening girders or box girders bracing is often provided in place of plated diaphragms to avoid torsional distortion and to maintain the shape of the cross section under service loads. Figure 19.7(c) illustrates some uses of trusses in bridgeworks. Other uses of trusses in bridgeworks include trestling, i.e. triangulated temporary support frames normally used to support medium- to large-span bridges over land during erection, see Fig. 19.7(d).

## **19.9 Rigid-jointed Vierendeel girders**

### **19.9.1 Use of Vierendeel girders**

Vierendeel girders, unlike trusses or lattice girders, are rigidly-jointed open-web girders having only vertical members between the top and bottom chords. The chords are normally parallel or near parallel; some typical forms are shown in Fig. 19.8(a).

The elements in Vierendeel girders are subjected to bending, axial and shear stress, unlike conventional trusses with diagonal web members where the members are primarily design for axial loads. Vierendeel girders are usually more expensive than conventional trusses and their use is limited to instances where diagonal web members are either obtrusive or undesirable. Vierendeel girders in bridges are rare; they are more commonly used in buildings where access for circulation or a large number of services is required within the depth of the girder.

The economic proportions and span lengths are similar to those of the parallel chord trusses already discussed in section 19.2.

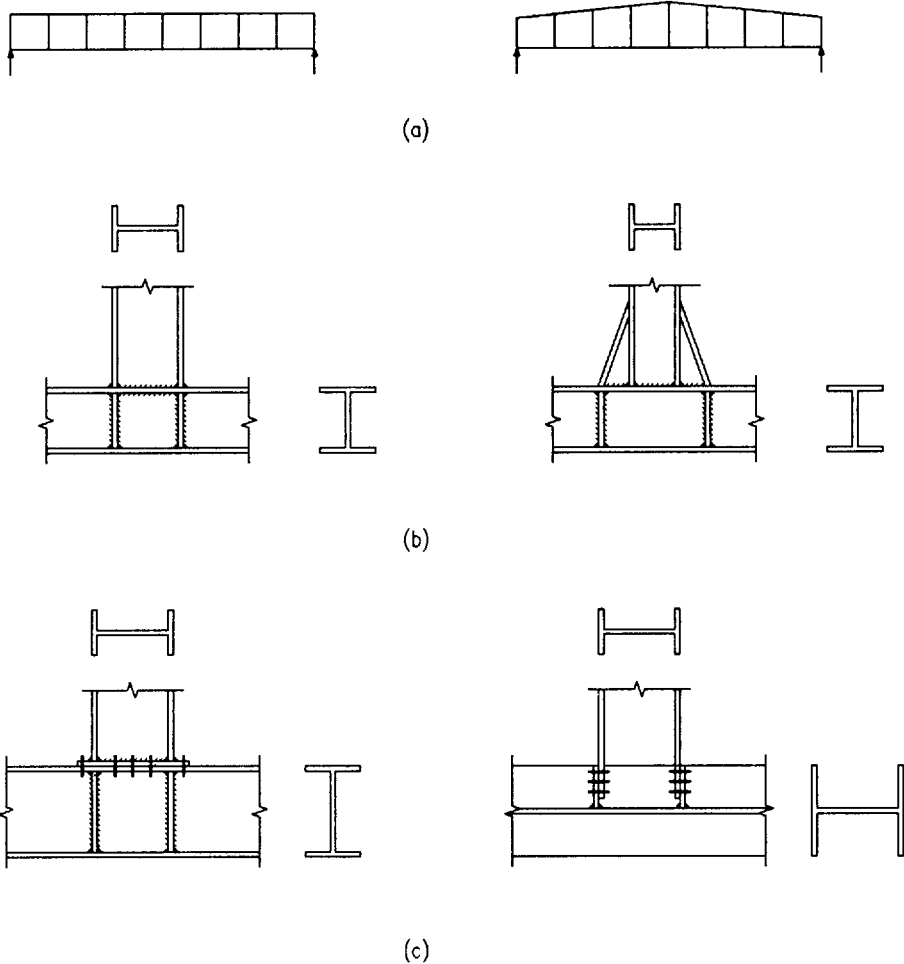


Fig. 19.8 Typical details of Vierendeel girders: (a) typical forms, (b) welded connections, (c) bolted connections

### 19.9.2 Analysis

Vierendeel girders are statically indeterminate structures but various manual methods of analysis have been developed. The statically determinate method assumes pin joints at the mid-points of the verticals and chords of each panel. The method, however, is only suitable for girders with parallel chords of constant stiffness and when the loads are applied at the node points. Various modified moment distribution methods have been developed for the analysis of Vierendeel

girders which allow for inclined chords, chords of different stiffness in the panels and member widening at the node positions.

The use of computers offers the most accurate and efficient way of analyzing Vierendeel girders, particularly those with inclined chords, chords of varying stiffness and when the loading is not applied at the node positions. A further advantage of computer analysis is that joint rotations and deflections are easily calculated.

Plastic theory may be applied to the design of Vierendeel girders in a similar way to its application to other rigid frames such as portal frames. Failure of the structure, as a whole, generally results from local failure of a small number of its members to form a mechanism. Once the failure mode is established the chords and verticals are designed against failure. Computer programs are available for the plastic analysis of plane frameworks including Vierendeel arrangements.


### **19.9.3 Connections**

Vierendeel girders have rigid joints with full fixity and so the connections must be of the type which prevents rotation or slip of the incoming members, such as welded or friction-grip bolted connections. Welded connections are usually the most efficient and compact although undesirable if the connections are required to be made on site. Normally site splices are bolted for economy. For very large Vierendeel girders delivered and erected piecemeal, fully bolted connections are normally used. For member and joint efficiency the ends of the verticals are often splayed. This is of advantage in heavily-loaded girders as the high concentrated local stresses are reduced thus avoiding the need for heavy stiffening.

Some typical joint examples are illustrated in Fig. 19.8(b) and (c).

A series of worked examples follows which are relevant to Chapter 19.



|   |   |   |                                      |
|---|---|---|--------------------------------------|
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|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p> | <p>Made by <b>RT</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>1</b></p>            |

**Problem**

*Design the roof trusses for an industrial building with two 25 m spans, 120 m long. The roofing is insulated metal sheeting with purlins at node positions. The building is 9 m to the eaves, basic wind speed is 42 m/s and ground roughness is category 3c.*

**Structural form:**

*For 25 m span a pitched roof will not be economical as the height at the apex would be in the order of 5.5 m.*

*Ideal solutions would either be a Mansard truss or a parallel chord Pratt, Howe or Warren truss.*

*For the purpose of this design example a Mansard truss will be adopted.*

*Economical span to depth ratio between 7 and 8*


$$\begin{aligned}
 \text{For 3.5 m depth } \frac{\text{span}}{\text{depth}} &= \frac{25}{3.5} \\
 &= 7.14 \text{ acceptable}
 \end{aligned}$$

*Truss spacing should be in the region of 1/4 to 1/5th of the span*

*For 6 m truss centres*

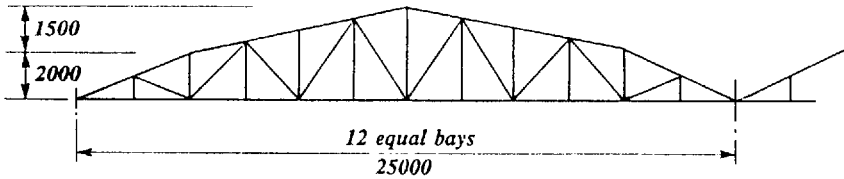
$$\text{spacing/span} = 6/25 = 1/4.17 \text{ acceptable}$$

*A truss spacing of 6 m conveniently suits the length of the building.*

|  |   |                                      |  |
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*Number of bays* =  $120/6 = 20$  No.

**Truss dimensioning:**



| <u>Loading:</u>                          | <i>kN/m<sup>2</sup></i>        | <b>BS: 648</b> |
|--|--------------------------------|----------------|
| <i>Dead load</i> - <i>Steel sheeting</i> | = 0.075                        |                |
| <i>Insulation</i>                        | = 0.020                        |                |
| <i>Fixings</i>                           | = 0.025                        |                |
| <i>Services etc</i>                      | = 0.100                        |                |
| <i>Total</i>                             | = <u>0.22 kN/m<sup>2</sup></u> |                |

*for 6 m bays*


*Roof dead load* =  $0.22 \times 25 \times 6 = 33.0$  kN

*Allow for purlins* = 11.8 kN

*Allow for own weight* = 30.0 kN

*Total load* = 74.8 kN

*nodal load* =  $\frac{74.8}{12} = 6.2$  kN

|  |   |  |
|--|---|--|
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|  | Design code<br><p style="text-align: center;"><b>BS5950: Part 1</b></p> | Made by <b>RT</b><br>Checked by <b>GWO</b>                   |

**Imposed load:**

No access to roof,  $\therefore$  snow load =  $0.75 \text{ kN/m}^2$

nodal load =  $0.75 \times 6 \times 25/12 = 9.4 \text{ kN}$

**Wind loading:**

Basic wind speed =  $42 \text{ m/s}$

Design wind speed  $V_s = V S_1 S_2 S_3$

Topography factor  $S_1 = 1.0$

Statistical factor  $S_3 = 1.0$

Ground roughness category =  $3 \text{ c}$

Roof elevation between 9 m & 12.5 m

**BS: 6399**

**CP3:  
Chapter V:  
P2**

$\therefore S_2 = 0.74$

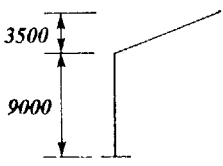
$V_s = 42 \times 1 \times 0.74 \times 1 = 31.1 \text{ m/s}$

Dynamic pressure  $q = k V_s^2$

where  $k = 0.613$

$q = 0.613 \times 31.1^2 \times 10^{-3}$

$= 0.593 \text{ kN/m}^2$




**CP3:  
Chapter V:  
P2 Table 3**

**External pressure coefficients,  $C_{pe}$**

Roof slopes approximately  $26^\circ$  at ends

&  $10^\circ$  at C (see diagram, sheet 5)

|  |                                      |  |
|--|--------------------------------------|--|
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|  | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> |

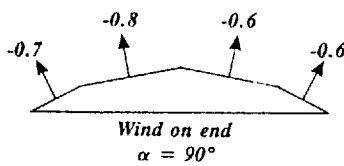
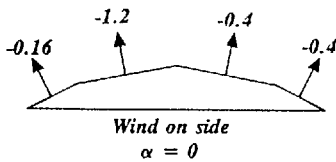
**Building Dimensions**

$w = 28 \text{ m}$  ( $b/N = 0.32$ )

$l = 120 \text{ m}$

$h = 9 \text{ m}$

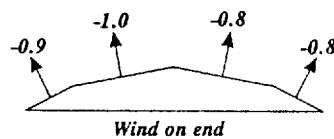
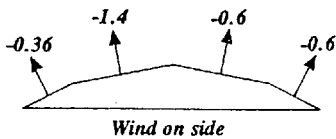
**CP3:**  
**Chapter V:**  
**P2 Table 8**



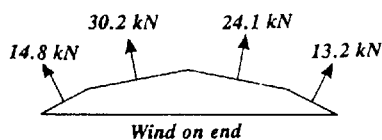
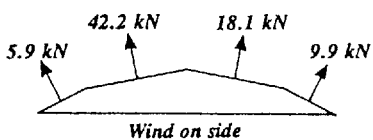
**Internal pressure coefficients**  $C_{pi} = +0.2 \text{ or } -0.3$


**Wind force** =  $q A (C_{pe} - C_{pi})$

**Maximum ( $C_{pe} - C_{pi}$ )**

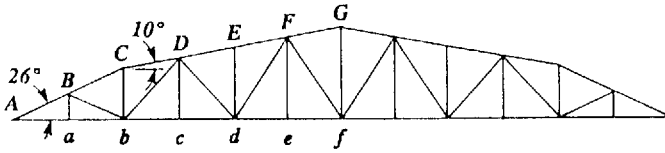


**Wind forces:**




|   |                                      |  |                           |
|---|--------------------------------------|--|---------------------------|
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|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> | Steel no. <b>5</b>        |

**Member forces (unfactored)**



| Member | Dead Load<br>kN | Imposed Load<br>kN | Wind on Side<br>kN | Wind on End<br>kN |
|--------|-----------------|--------------------|--------------------|-------------------|
| A-B    | -78.8           | -118.2             | 104.0              | 91.0              |
| B-C    | -72.7           | -109.1             | 101.7              | 85.2              |
| C-D    | -67.0           | -100.5             | 96.2               | 81.5              |
| D-E    | -76.8           | -115.2             | 110.6              | 87.4              |
| E-F    | -76.8           | -115.2             | 113.2              | 89.2              |
| F-G    | -66.6           | -99.9              | 102.0              | 79.1              |
| A-a    | 72.5            | 108.8              | -106.9             | -97.2             |
| a-b    | 72.5            | 108.8              | -106.9             | -97.2             |
| b-c    | 74.3            | 111.5              | -115.3             | -94.4             |
| c-d    | 74.3            | 111.5              | -115.3             | -94.4             |
| d-e    | 71.9            | 107.9              | -105.9             | -82.8             |
| e-f    | 71.9            | 107.9              | -105.9             | -82.8             |
| B-a    | 0               | 0                  | 0                  | 0                 |
| C-b    | 12.7            | 19.1               | -15.1              | -11.8             |
| D-c    | 0               | 0                  | 0                  | 0                 |
| E-d    | -6.2            | -9.3               | 11.9               | 8.5               |
| F-e    | 0               | 0                  | 0                  | 0                 |
| G-f    | 18.6            | 27.9               | -37.4              | -29.4             |
| B-b    | -7.4            | -11.1              | 6.3                | 9.5               |
| b-D    | -12.8           | -19.2              | 17.8               | 8.8               |
| D-d    | 1.7             | 2.6                | -1.9               | -2.8              |
| d-F    | 6.2             | 9.3                | -14.9              | -12.8             |
| F-f    | -11.5           | -17.3              | 22.4               | 17.8              |

The above forces have been calculated assuming pin joints

|  |                                      |  |                           |
|--|--------------------------------------|--|---------------------------|
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|  | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>6</b>        |

**Load factors & combinations:**

**For Dead + Imposed**  
 $1.4 \times DL + 1.6 \times IL$

**For Dead + Wind**  
 $1.0 \times DL + 1.4 \times WL$


**For Dead + Imposed + Wind**

*not critical as wind loads act in opposite direction to Dead and Imposed loads*

**Member forces (factored)**

| Member | Dead + Imposed<br>kN | Dead + Wind<br>kN |
|--------|----------------------|-------------------|
| A-B    | -299.4               | 66.8              |
| B-C    | -276.3               | 69.7              |
| C-D    | -254.6               | 67.7              |
| D-E    | -291.8               | 78.0              |
| E-F    | -291.8               | 81.7              |
| F-G    | -253.1               | 76.2              |
| A-a    | 275.6                | -77.2             |
| a-b    | 275.6                | -77.2             |
| b-c    | 282.4                | -87.1             |
| c-d    | 282.4                | -87.1             |
| d-e    | 273.3                | -76.4             |
| e-f    | 273.3                | -76.4             |
| B-a    | 0                    | 0                 |
| C-b    | 48.3                 | -8.4              |
| D-c    | 0                    | 0                 |
| E-d    | -23.6                | 10.5              |
| F-e    | 0                    | 0                 |
| G-f    | 70.7                 | -33.8             |
| B-b    | -28.1                | 5.9               |
| b-D    | -48.6                | 12.1              |
| D-d    | 6.5                  | -2.2              |
| d-F    | 23.6                 | -14.7             |
| F-f    | -43.8                | 19.9              |

**BS 5950:  
Part 1  
Table 2**

|   |                                      |  |                           |
|---|--------------------------------------|--|---------------------------|
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|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>7</b>        |

**Secondary stresses:**

**BS 5950:  
Part 1  
4.10**

*Provided the slenderness of the chords and (most) web members are greater than 50 and 100 respectively, secondary stresses may be ignored (slenderness in the plane of the truss). This condition is to be checked after preliminary sizing of the members.*

**Member Design:**

(A) Top Chord - member A-B

Maximum compressive force = 299.4 kN

Effective length  $L_E$  = 1.0L = 2311 mm Table 24

Try 90 × 90 × 5 RHS Grade 43

$$\lambda = \frac{L_E}{r_y} = \frac{2311}{34.6} = 66.8 \quad (> 50 \text{ ignore secondary stresses}) \quad 4.10$$

Maximum slenderness ratio  $\lambda$  = 180 OK 4.7.3.2

$$p_y = 275 \text{ N/mm}^2$$

$$p_c = 228 \text{ N/mm}^2 \quad \text{Table 27(a)}$$

Allowable compressive force  $P_c = A_g p_c$  4.7.4

$$A_g = 16.9 \text{ cm}^2$$


$$P_c = 16.9 \times 10^2 \times 228 \times 10^{-3} = 385 \text{ kN} > 299.4 \text{ kN OK}$$

∴ Use 90 × 90 × 5 RHS Grade 43

(B) Bottom Chord - Member b-c

Maximum tensile force = 282.4 kN

Maximum compressive force = 87.1 kN

|  |                                      |  |                           |
|--|--------------------------------------|--|---------------------------|
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|  | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>8</b>        |

*For welded connections allowable tensile force,  $P_t$*  **4.6.1**

$$P_t = A_e p_y \quad A_e = \text{gross area in this case}$$

*Assume the same size section as the top chord*

*∴ Try 90 × 90 × 5 RHS Grade 43*

$$\begin{aligned} \text{Allowable tensile force} &= 16.9 \times 10^2 \times 275 \times 10^{-3} \\ &= 464.8 \text{ kN} > 282.4 \text{ kN OK} \end{aligned}$$

*Under Wind + Dead load the bottom chord goes into compression.*

*By inspection, the bottom chord will require longitudinal ties. Assume that these ties are at quarter positions i.e. 6.25 m spacing.*

$$\therefore L_E = 6.25 \times 1.0$$

$$\lambda = 6.25 \times 10^3 / 34.6 = 181 < 350 \quad \text{4.7.3.2}$$

$$\therefore p_c = 56 \text{ N/mm}^2 \quad \text{Table 27(a)}$$

$$\begin{aligned} p_c &= 16.9 \times 10^2 \times 56 \times 10^{-3} \\ &= 94.6 \text{ kN} > 87.1 \text{ kN OK} \end{aligned}$$

*∴ Use 90 × 90 × 5 RHS Grade 43 with longitudinal ties at 6.25 m intervals.*

**(C) Web members - member G - f**


$$\text{Maximum tensile force} = 70.7 \text{ kN}$$


$$\text{Maximum compressive force} = 33.8 \text{ kN}$$

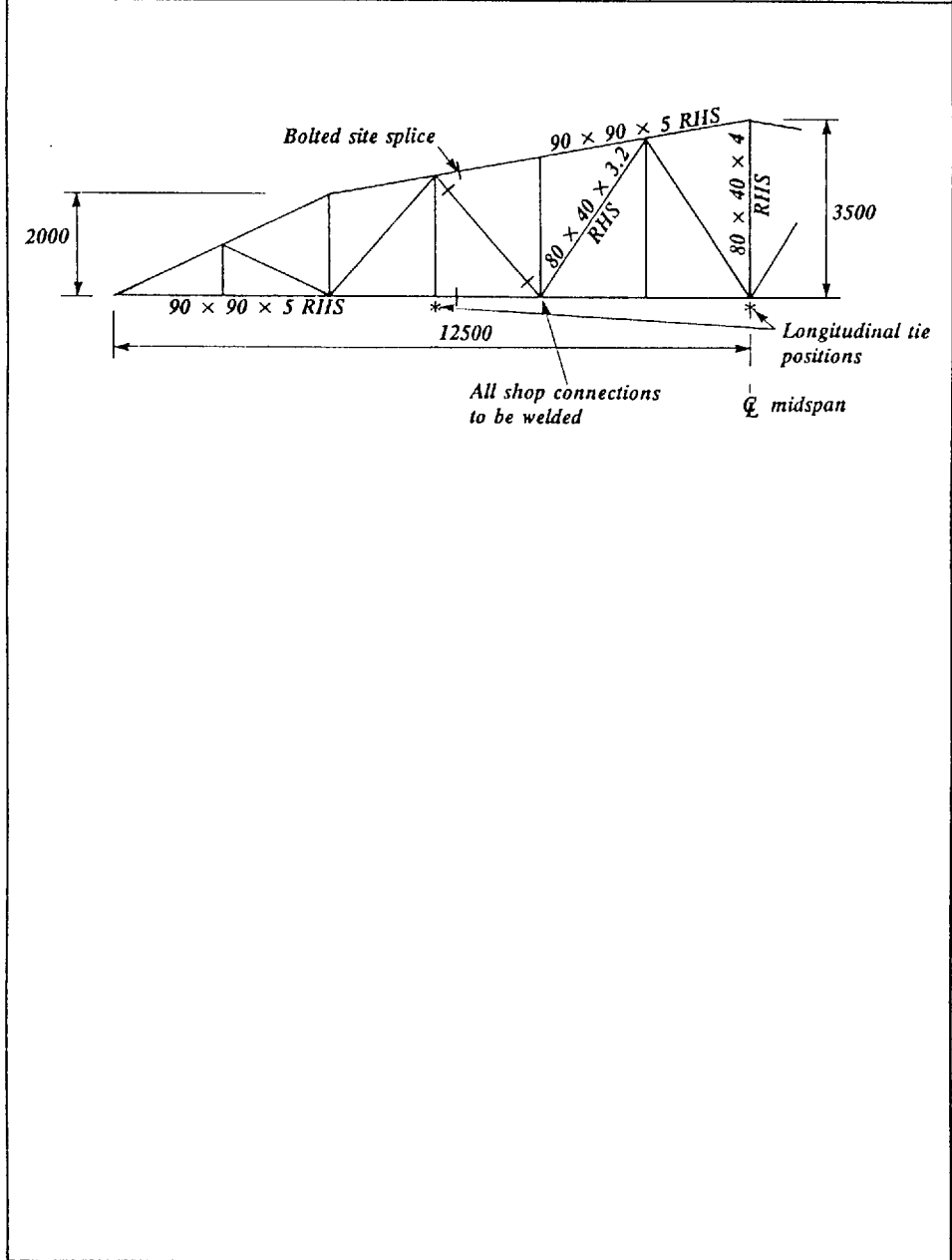
*Try using 40 × 40 × 3.2 RHS*


$$\begin{aligned} \text{Allowable tensile force } P_t &= 466 \times 275 \times 10^{-3} & \text{4.6.1} \\ &= 128.2 \text{ kN} > 70.7 \text{ kN} \therefore \text{OK} \end{aligned}$$



|   |                                      |  |                           |
|---|--------------------------------------|--|---------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p>   | Subject<br><b>ROOF TRUSS</b>         |  | Chapter ref.<br><b>19</b> |
|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>9</b>        |
| <p>Effective length <math>L_E = 1.0 L</math> <span style="float: right;">Table 24</span></p> <p>Slenderness <math>\lambda = \frac{L_E}{r_y} = \frac{3500}{15.0} = 233.3</math> <span style="float: right;">4.7.3.1<br/>4.10</span></p> <p>( &gt; 100 ∴ ignore secondary stresses)</p> <p>Max allowable slenderness <math>\lambda = 350 &gt; 233.3</math> ∴ OK <span style="float: right;">4.7.3.2</span></p> <p>(in compression due to wind loads)</p> <p><math>p_c = 35 \text{ N/mm}^2</math> <span style="float: right;">Table 27(a)</span></p> <p>Allowable compressive force <math>P_c = 466 \times 35 \times 10^{-3}</math><br/> <math>P_c = 16.3 \text{ kN} &lt; 33.8 \text{ kN}</math></p> <p>section is overstressed due to wind load reversal</p> <p>Try using <math>80 \times 40 \times 4</math> RIIS</p> <p><math>\lambda = \frac{3500}{15.9} = 220</math></p> <p>∴ <math>p_c = 39 \text{ N/mm}^2</math> <span style="float: right;">Table 27(a)</span></p> <p>Allowable compressive force <math>P_c = 39 \times 888 \times 10^{-3}</math><br/> <math>= 34.6 \text{ kN} &gt; 33.8 \text{ kN OK}</math></p> <p><u>Use <math>80 \times 40 \times 4</math> RIIS</u></p> <p>For guidance on the design of connections the reader should refer to Chapter 26.</p> |                                      |  |                           |

|  |   |   |                                      |
|--|---|---|--------------------------------------|
| <p><b>The Steel Construction Institute</b></p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>ROOF TRUSS</b></p>         |   | <p>Chapter ref.</p> <p><b>19</b></p> |
|  | <p>Design code</p> <p><b>BS5950: Part 1</b></p> | <p>Made by <b>RT</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>10</b></p>           |



|   |  |  |  |
|---|--|--|--|
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|   | Design code<br><p style="text-align: center;"><b>BS5400</b></p>  | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>   |

**Problem**

*Design the principal structure for a bridge span of 70 m, carrying a 2 lane carriageway 7.5 m wide with 2 footways 1.5 m wide. The loading is to be H1A plus 37.5 units of H1B. Construction depth below the road level is limited to 2.5 m maximum.*

**Structural form:**

*For road bridge span to depth ratio ~ 10 to 12*

*Try using 6.5 m depth*

$$\text{span/depth} = \frac{70}{6.5} = 10.8 \text{ adequate}$$

*Bay width say 5 m*


$$\begin{aligned} \text{angle of diagonals} &= \text{arc tan } \frac{6.5}{5} \\ &= 52.4^\circ \end{aligned}$$

*> 50° adequate*

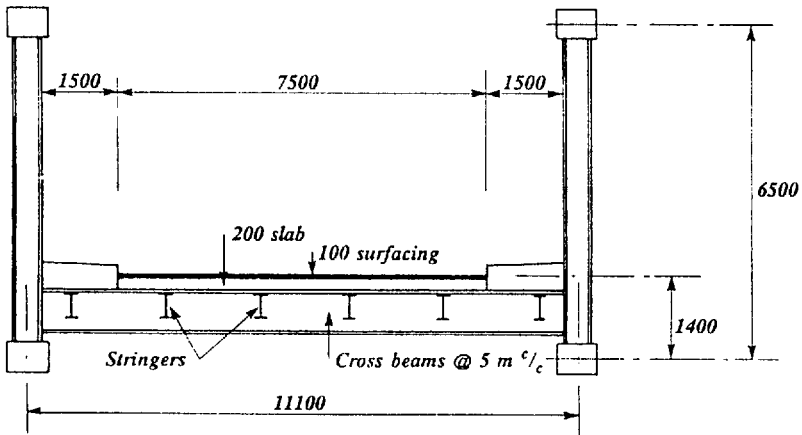
*Cross beams to be provided at each panel point.*

*From the limitations imposed on the construction depth below road level an undershung truss will not be appropriate. A through truss will be adopted with an unbraced compression chord to meet the unlimited headroom requirement. Restraint to the compression chord to be provided by U-frame action.*

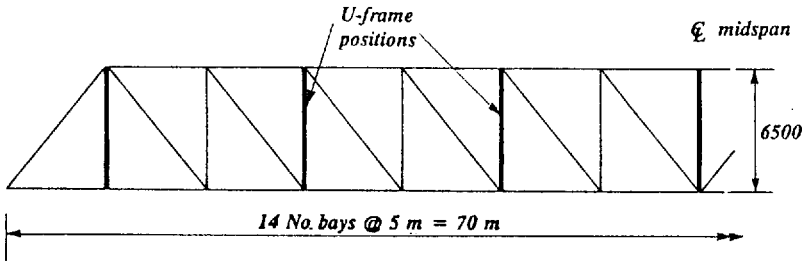
*A Pratt truss will be appropriate for a span of 70 m although a Warren or Howe truss could also be adopted.*

|   |  |   |
|---|--|---|
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|   | <p>Design code</p> <p><b>BS5400</b></p>  | <p>Made by <b>RT</b></p> <p>Checked by <b>GWO</b></p> |

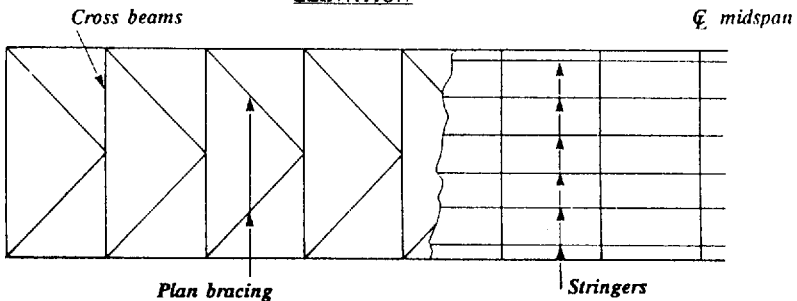
**Proposed arrangement:**




**SECTION**



**ELEVATION**



**PLAN**

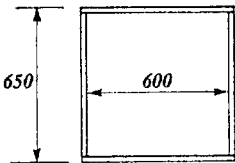
|   |                               |  |
|---|-------------------------------|--|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | Subject<br><b>ROAD BRIDGE</b> | Chapter ref.<br><b>19</b>                  |
|   | Design code<br><b>BS5400</b>  | Made by <b>RT</b><br>Checked by <b>GWO</b> |

**Sections:**

The truss is analysed using a plane frame stress analysis program. The members are estimated using hand analysis.

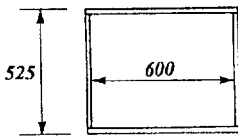
Try using the following sections:

**Top chord**



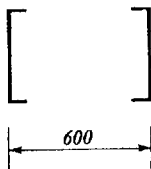
- 650 × 25 top plate
- 600 × 25 webs
- 650 × 25 bottom plate

**Bottom chord**



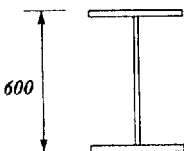
- 640 × 20 top plate
- 485 × 20 webs
- 640 × 20 bottom plate

**Diagonal webs**




- 2 No. 381 × 102 C's

**Vertical webs**



- 400 × 25 flange
- 15 web
- 400 × 25 flange

|  |                    |            |              |
|--|--------------------|------------|--------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject            |            | Chapter ref. |
|  | <b>ROAD BRIDGE</b> |            | <b>19</b>    |
|  |                    |            |              |
| <b>BS5400</b>  | <b>RT</b>          | <b>GWO</b> |              |

Section properties:

| Member              | Area<br>mm <sup>2</sup> | $\bar{y}$<br>mm | <i>I</i><br>In Plane<br>mm <sup>4</sup> | <i>I</i><br>Out of Plane<br>mm <sup>4</sup> | wt/m<br>kN/m |
|---------------------|-------------------------|-----------------|---|---|--------------|
| <i>Top chord</i>    | 62500                   | 325             | 4.074 E9                                | 4.074 E9                                    | 4.95         |
| <i>Bottom chord</i> | 45000                   | 263             | 2.012 E9                                | 2.738 E9                                    | 3.53         |
| <i>Diagonals</i>    | 14038                   |                 | 0.298 E9                                | 1.072 E9                                    | 1.10         |
| <i>Verticals</i>    | 28250                   |                 | 0.267 E9                                | 1.861 E9                                    | 2.16         |

For the purpose of this example the members will be kept constant throughout the span.

Loading

Loads calculated for each truss at each cross beam location.


- (i) Surfacing =  $0.1 \times 7.5 \times 5 \times 0.5 \times 22 = 41.3 \text{ kN}$
- (ii) Parapets =  $5 \times 1.0 = 5.0 \text{ kN}$
- (iii) Slab =  $0.2 \times 10.5 \times 5 \times 0.5 \times 24 = 126.0 \text{ kN}$
- (iv) Footways =  $0.2 \times 1.5 \times 5 \times 24 = 36.0 \text{ kN}$
- (v) Deck ~~steelwork~~ & bracing =  $24 \text{ kN}$
- (vi) Own wt. =  $(4.95 + 3.53) \times 5 + 1.1 \times 8.2 + 2.16 \times 6.5$   
                   =  $65.5 + 10\% \text{ (extras)} = 72 \text{ kN}$

(vii) HA UDL

No. of notional lanes 2

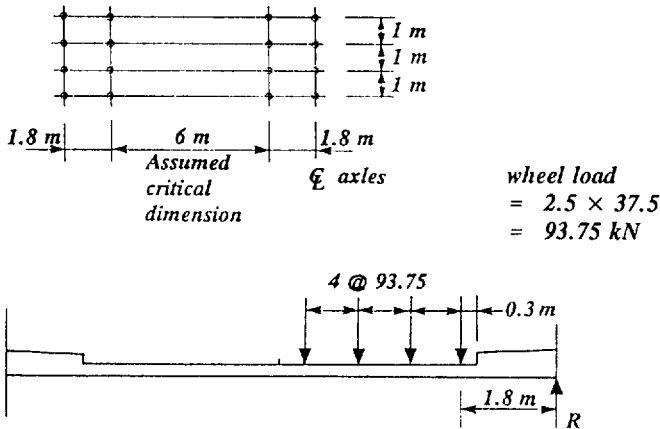
Part 2,  
3.2.9.3



|  |   |                              |  |
|--|---|------------------------------|--|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject                      | Chapter ref.                               |
|  |   | Design code<br><b>BS5400</b> | Made by <b>RT</b><br>Checked by <b>GWO</b> |
|  |   | Sheet no.                    | <b>6</b>                                   |

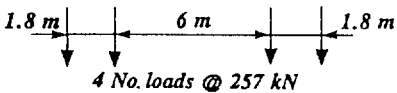
(x) *HB load (37.5 units):*

*Part 2, 6.3*



$$\begin{aligned}
 \text{Reaction } R &= \frac{93.75}{10.5} \times (8.7 + 7.7 + 6.7 + 5.7) \\
 &= 257 \text{ kN}
 \end{aligned}$$

*Travelling load to be applied*



(xi) *Footway loading:*


*Part 2, 7.1.1*

$$= 5 \times \left[ \frac{22.5}{30} \right] \times 1.5 \times 5 = 28.2 \text{ kN}$$

*For the purpose of this example the following loads shall be ignored, but would normally be considered in a similar way to the primary loading ie.*

*Wind; Temperature; Erection; Braking, traction; etc.*



|  |   |                               |  |
|--|---|-------------------------------|--|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>ROAD BRIDGE</b> | Chapter ref.<br><b>19</b>                  |
|  |   | Design code<br><b>BS5400</b>  | Made by <b>RT</b><br>Checked by <b>GWO</b> |

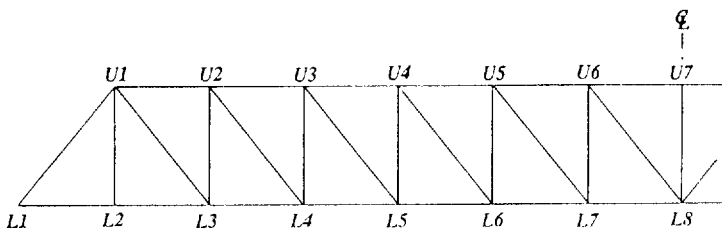
**Design for load combination**

**Part 2, 4.4**

**Load cases:**


- (a) **Steel Dead Load - top nodal points** =  $72/2$  = **36 kN**  
**Steel Dead Load - bottom nodal points** =  $36 + 24$  = **60 kN**
- (b) **Concrete dead load - bottom nodal points** =  $126 + 36$  = **162.0 kN**
- (c) **Superimposed dead - bottom nodal points** =  $41.3 + 5$  = **46.3 kN**
- (d) **HA UDL + KEL - bottom nodal points** = **112.5 kN**  
**& Travelling load** = **120 kN**
- (e) **HB + Associated HA UDL - bottom nodal points** = **36.2 kN**  
**& 4 No. Travelling loads @ 257 kN**
- (f) **Footway loading - bottom nodal points** = **28.2 kN**

**Nodal points notation:**



**The design will be limited to the following members**

- U6 - U7** Top chord
- L7 - L8** Bottom chord
- U1 - L3** Diagonal
- U2 - L3** Vertical

|   |                               |                       |                           |
|---|-------------------------------|-----------------------|---------------------------|
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|   | Design code<br><b>BSS400</b>  | Made by <b>RT</b>     | Steel no. <b>8</b>        |
|   |                               | Checked by <b>GWO</b> |                           |

*From the computer output,*

| <i>Member</i>       | <i>Dead Steel kN</i> | <i>Dead Concrete kN</i> | <i>Super Dead kN</i> | <i>HA kN</i> | <i>HB kN</i> | <i>FTWY kN</i> |
|---------------------|----------------------|-------------------------|----------------------|--------------|--------------|----------------|
| <i>U6 - U7</i>      | - 1695               | - 3041                  | - 869                | - 2428       | - 3113       | - 530          |
| <i>L7 - L8</i>      | 1658                 | 2974                    | 850                  | 2342         | 3244         | 518            |
| <i>U1 - L3</i>      | 580                  | 1039                    | 297                  | 836          | 1157         | 181            |
| <i>U2 - L3</i>      | - 419                | - 812                   | - 232                | - 648        | - 843        | - 141          |
| <i>(U6 - U7) U6</i> | 32.5                 | 58.3                    | 16.7                 | 60.1         | 145.8        | 10.1           |
| <i>U7</i>           | 34.1                 | 60.4                    | 17.5                 | 62.1         | 87.0         | 10.7           |
| <i>(L7 - L8) L7</i> | 15.2                 | 27.2                    | 7.8                  | 33.3         | 95.8         | 4.7            |
| <i>L8</i>           | 16.2                 | 28.9                    | 8.3                  | 32.7         | 34.0         | 5.1            |
| <i>(U1 - L3) U1</i> | 25.3                 | 45.4                    | 13.0                 | 36.7         | 48.5         | 7.9            |
| <i>L3</i>           | - 24.4               | - 43.8                  | - 12.5               | - 35.3       | - 50.0       | - 7.6          |
| <i>(U2 - L3) U2</i> | 22.1                 | 39.7                    | 11.4                 | 32.2         | 44.4         | 6.9            |
| <i>L3</i>           | - 20.5               | - 36.6                  | - 10.5               | - 29.9       | - 41.5       | - 6.4          |

*Unfactored axial loads*

*Unfactored bending moments kNm*

*for load combination 1*

*Part 2, 4.4*

*load combination 1a*

*Part 2, T1*


*at SLS* **1.0DS + 1.0DC + 1.25DL + 1.2HA + 1.0FTWY**

*at ULS* **1.05DS + 1.2DC + 1.75SDL + 1.5HA + 1.0FTWY**

*load combination 1b*

*at SLS* **1.0DS + 1.0DC + 1.25DL + 1.1HB + 1.0FTWY**

*at ULS* **1.0DS + 1.2DC + 1.75SDL + 1.3HB + 1.5FTWY**

|  |                               |  |                           |
|--|-------------------------------|--|---------------------------|
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|  | Design code<br><b>BS5400</b>  | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>9</b>        |

**Factored Axial loads & Bending Moments**

| Member              | Load Combination 1a |      |       |      | Load Combination 1b |      |       |      |
|---------------------|---------------------|------|-------|------|---------------------|------|-------|------|
|                     | ULS                 |      | SLS   |      | ULS                 |      | SLS   |      |
|                     | AXIAL               | BM   | AXIAL | BM   | AXIAL               | BM   | AXIAL | BM   |
|                     | kN                  | kNm  | kN    | kNm  | kN                  | kNm  | kN    | kNm  |
| (U6-U7)<br>U6<br>U7 | -11387              | 239  | -9222 | 193  | -11792              | 338  | -9733 | 281  |
|                     |                     | 248  |       | 201  |                     | 268  |       | 222  |
| (L7-L8)<br>L7<br>L8 | 11087               | 119  | 8980  | 96   | 11791               | 194  | 9738  | 162  |
|                     |                     | 123  |       | 99   |                     | 118  |       | 98   |
| (U1-L3)<br>U1<br>L3 | 3901                | 171  | 3160  | 138  | 4151                | 179  | 3429  | 148  |
|                     |                     | -164 |       | -133 |                     | -177 |       | -146 |
| (U2-L3)<br>U2<br>L3 | -3004               | 149  | -2428 | 121  | -3128               | 159  | -2578 | 131  |
|                     |                     | -138 |       | -112 |                     | -147 |       | -122 |

Load combination (1b) critical for members selected.

The tensile members are designed at the ULS only.

Part 3,  
12.2.3

The compression members are designed at the ULS and the SLS to meet the requirements of Clause 12.2.3(a) and (b).

Compression chord effective length:

U-frame restraints are 10 m centres

$$\text{Effective length } l_e = 2.5 k_3 (EI_c a \delta)^{0.25}$$


Ignoring the contribution of stiffness from the concrete slab

$$I_c = 4.074 \times 10^9 \text{ mm}^4$$

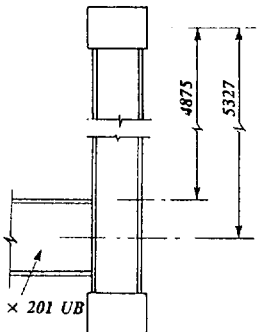
$$a = 10000 \text{ mm}$$

$$E = 205000 \text{ N/mm}^2$$

$$k_3 = 1.0$$

|  |                               |  |                           |
|--|-------------------------------|--|---------------------------|
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|  | Design code<br><b>BS5400</b>  | Made by <b>RT</b><br>Checked by <b>GWO</b> | Sheet no. <b>10</b>       |



*914 × 305 × 201 UB*

$d_1 = 4875 \text{ mm}$

$d_2 = 5327 \text{ mm}$

$I_1 = 1.861 \times 10^9 \text{ mm}^4$

$I_2 = 3.255 \times 10^9 \text{ mm}^4$

$U = 0.5$

$S = 11100 \text{ mm}$

$f = 0.1 \times 10^{-10}$

$$\delta = \frac{d_1^3}{3 EI_1} + \frac{US d_2^2}{EI_2} + f d_2^2$$

$$\delta = \frac{4875^3}{3 \times 2.05 \times 10^5 \times 1.861 \times 10^9} + \frac{0.5 \times 11100 \times 5327^2}{2.05 \times 10^5 \times 3.255 \times 10^9} + 0.1 \times 10^{-10} \times 5327^2$$

$$\delta = 6.21 \times 10^{-4}$$

$\therefore$  effective length  $l_e = 2.5 \times 1.0 \times (2.05 \times 10^5 \times 4.074 \times 10^9 \times 10000 \times 6.21 \times 10^{-4})^{0.25}$


$l_e = 21216 \text{ mm}$

*Effective length of vertical web members:*

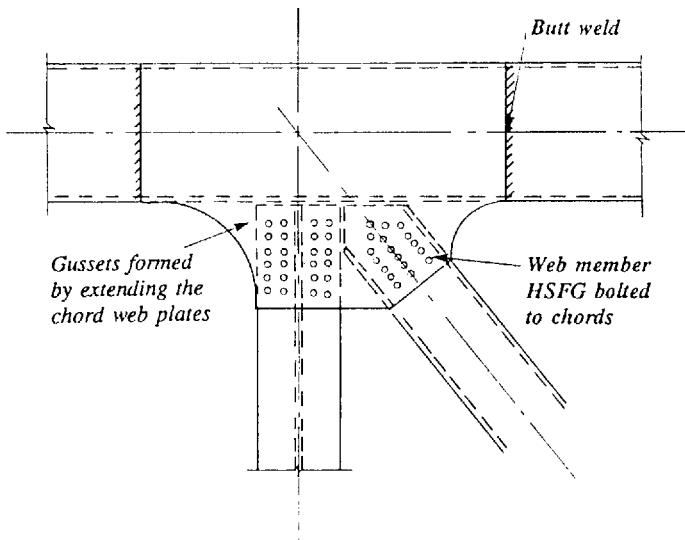
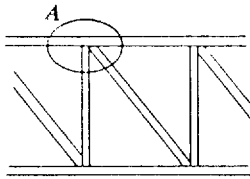
|                                    |               |                    |
|------------------------------------|---------------|--------------------|
| For buckling in plane of truss     | $l_e = 0.7 l$ | <i>Part 3, T11</i> |
| For buckling out of plane of truss | $l_e = 1.0 l$ |                    |

*Member design:*

*The individual members may now be designed. For guidance on the design of axially loaded members with bending, reference should be made to Chapters 14, 15 and 18. Further analysis may be required if the chosen members are found to be over or understressed.*

|   |  |   |                                      |
|---|--|---|--------------------------------------|
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|   | <p>Design code</p> <p><b>BS5400</b></p>  | <p>Made by <b>RT</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>11</b></p>           |

*Typical connection detail:*



*Enlarged Detail A*

*For guidance on the detailed design of connections the reader should refer to Chapter 26.*

# Chapter 20

## Composite deck slabs

by MARK LAWSON and PETER WICKENS

### 20.1 Introduction

#### 20.1.1 Form of construction

'Composite floor' is the general term used to denote the composite action of steel beams and concrete or composite slabs that form a structural floor. 'Composite deck slabs', in this context, comprise profiled steel decking (or sheeting) as the permanent formwork to the underside of a concrete slab spanning between support beams. The decking acts compositely with the concrete under service loading. It also supports the loads applied to it before the concrete has gained adequate strength. A light mesh reinforcement is placed in the concrete. A cross-section through a typical composite slab is shown in Fig. 20.1. Shear-connectors are used to develop composite action between the concrete slab and steel beams (see also Chapter 21).

The decking has a number of roles. It

- (1) supports the loads during construction
- (2) acts as a working platform
- (3) develops adequate composite action with the concrete

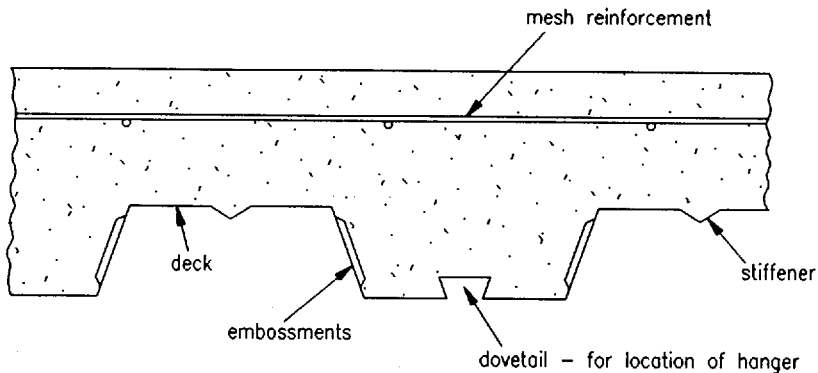


Fig. 20.1 Section through a typical composite deck slab

- (4) transfers in-plane loads by diaphragm action to vertical bracing or walls (in conjunction with the concrete topping)
- (5) stabilizes the beams against lateral buckling
- (6) acts as transverse reinforcement to the composite beams
- (7) distributes shrinkage strains preventing serious cracking.

In addition it has a number of advantages over precast or in situ concrete alternatives:

- (1) construction periods are reduced
- (2) decking is easily handled
- (3) attachments (e.g. ceiling hangers) can be made easily
- (4) openings can be formed
- (5) shear-connectors can be welded through the decking
- (6) decking can be cut to length and is less prone to tolerance problems.

The main economy sought in buildings is speed of construction and for this reason slabs and beams are generally designed to be unpropped during the construction stage. Spans of the order of 3 m to 3.6 m between support beams are most common, but can be increased to over 4 m if propping is used. Design of composite slabs is covered by BS 5950: Part 4.<sup>1</sup>

## 20.2 Deck types

Deck profiles are usually in the range of 38–75 mm height and 150–300 mm trough spacing with sheet thicknesses between 0.8 mm and 1.5 mm, use of the lower thickness being limited by local buckling and the upper thickness by difficulties in rolling. A summary of the different decking profiles marketed for use in composite slabs is shown in Fig. 20.2. There are two well-known generic types: the dovetail profile and the trapezoidal profile with web indentations.

The shape of the profile is controlled by a number of criteria:

- (1) the need to maximize the efficiency of the cross-section in bending (both positive and negative moments)
- (2) the need to develop adequate composite action with the concrete by use of embossments or indentations or by the shape of the profile itself
- (3) the efficient transfer of shear from the beam into the concrete slab (a similar problem to the haunch design in reinforced concrete slabs).

Deeper, thicker profiles are used where there is a need to maximize spans in unpropped construction. Practice in North America has been to use profiles with a trough pitch typically 300 mm and 50 mm height based on a 3 m span.<sup>2</sup> In the UK there is a tendency to design for longer spans with slightly deeper profiles, of typically 60 mm.

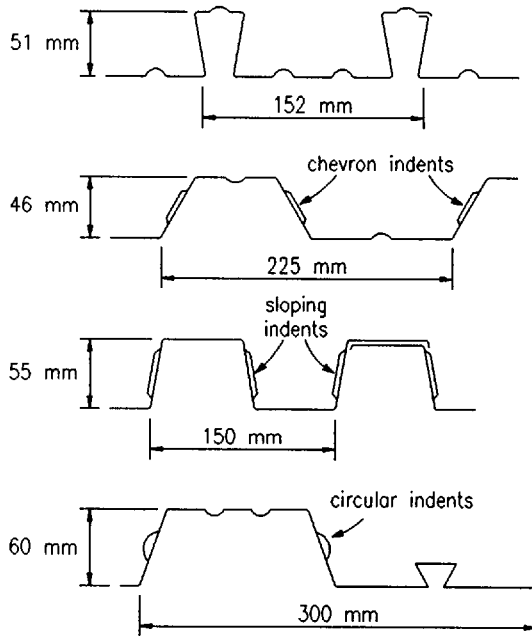


Fig. 20.2 Examples of composite deck profiles

Steel grades are generally Z25 or Z28 (250 N/mm<sup>2</sup> and 280 N/mm<sup>2</sup> yield strength respectively). There is normally no benefit in using higher grade steel because serviceability criteria often control the design of the deck (see section 20.5.5).

Steel decking is usually galvanized to a standard of 275 g/m<sup>2</sup> (roughly 0.04 mm per face) which gives adequate protection for internal use. In North America, unprotected decks have been used but one problem lies in the specification of steel decks for car parks because of potential salt attack through cracks in the concrete.

### 20.3 Normal and lightweight concretes

One of the principal advantages of steel decking is that it acts as a working platform. The loads that it supports arise mainly during the concreting operation. Lightweight concrete (LWC), therefore, has advantages in terms of its reduced self-weight in comparison to normal-weight concrete (NWC). In the UK the main form of LWC comprises Lytag and sand with a dry density range of 1750–1900



kg/m<sup>3</sup>. The compressive strength of Lytag LWC is similar to NWC, although there is a slight reduction in shear strength.

Concrete is usually placed by pump, mainly for reasons of speed, but also because it is difficult to 'skip' the concrete with the decking in place above. Indeed, it is usual practice to deck-out a number of floors ahead of the concreting operation. The decking is attached to its supports by shot-fired pins or screws and later by welded shear-connectors.

Unlike traditional reinforced concrete, there is no need to restrict bay sizes during construction because the decking serves to distribute early age and shrinkage strains, thereby eliminating the formation of wide cracks. Typical pumped pours are 500–1000 m<sup>2</sup>. LWC also has a higher tensile strain capacity than NWC, reducing the tendency for cracking. The mesh reinforcement is of a nominal size to control cracking at supports, and to act as 'fire reinforcement'. A142 or A193 are the common sizes specified.

The concrete grade (cube strength in N/mm<sup>2</sup>) is normally specified as 30 to 40. Pumped concrete also contains additives to aid lubrication. For this reason the slump test is not a good measure of workability and so the 'flow-meter' method is often used. The concrete is usually tamped level by fixing the tamping rails to the support beams. As these beams deflect, the slab level adopts that of the support beams. In propped construction, the slab level deflects further on removal of the props.

## 20.4 Selection of floor system

Slab depths are normally in the range of 110–150 mm. Clearly, the minimum depth for structural adequacy is usually selected, but the slab depth is affected by insulation requirements in a fire (see section 20.6.3) and serviceability criteria as influenced by the ratio of slab span to depth. As a general rule, span:depth ratios (considering the overall slab depth) of continuous composite slabs should be less than 30 for LWC and 35 for NWC. Longer spans may suffer from excessive deflections.

In designing the composite slab it is difficult to develop the full flexural capacity of the slab determined by the area of the deck acting as effective tensile reinforcement. Failure is normally one of shear-bond rupture resulting in slip between the deck and the concrete. Nevertheless, load capacities of composite slabs with the above proportions are normally adequate for most imposed loads up to 10 kN/m<sup>2</sup>. The shear-bond capacity of composite slabs is determined from tests (see section 20.5.3); this capacity may be enhanced by end-anchorage provided by shear-connectors attached to the support beams.

The concrete slab also acts as the principal compressive element in the design of the composite beams (see Chapter 21). This interaction between the flexural behaviour of the slab and the beams is only important where both the slab and beam span in the same direction.

## 20.5 Basic design

### 20.5.1 Construction condition

The decking supports the weight of concrete in the finished slab, excess weight from concrete placement and ponding, the weight of operatives and any impact loads during construction. There is a variety of recommendations for this temporary construction load to be considered in the design of the decking; these are expressed in terms of either a uniformly-distributed load or a single line load transverse to the span being checked. In BS 5950: Part 4,<sup>1</sup> the standard used in the design of the decking and composite slab, these construction loads are specified as 1.5 kN/m<sup>2</sup> or a transverse line load of 2 kN/m<sup>2</sup> (for spans up to 3 m) respectively. Self-weight and construction loads are multiplied by a load factor of 1.4.<sup>1</sup>

However, significant loads can be developed before concreting due to storage of equipment and materials. To avoid premature failure of the deck these loads applied before concreting should not exceed 3 kN/m<sup>2</sup>. Similarly, loads applied to the composite slab before it has gained adequate strength for fully composite action should not exceed 1.5 kN/m<sup>2</sup>. The definition of 'adequate strength' is considered to be a cube strength of 75% of the specified value, which is often achieved in 5–7 days after concreting.

The design of single-span decking is usually controlled by deflection and ponding of concrete. Continuous decking is generally designed on strength rather than deflection criteria and longer unpropped spans are permissible. The construction load is applied in design as a pattern load even though only one span is likely to be loaded to this extent, in view of the progressive nature of concreting.

In BS 5950<sup>1</sup> a limit on the residual deflection of the soffit of the slab after concreting of the smaller of (span/180) or (slab depth/10) is specified, increased to (span/130) if the effects of ponding are included. Greater deflections are likely to be experienced during concreting.

The design of the decking in bending is dependent on the properties of the profile, and particularly the thin plate elements in compression. Where profiles are stiffened by one or two folds in the compression plate, the section is more efficient in bending (Fig. 20.3).

The design of continuous decking is based, according to code requirements, on an elastic distribution of moment, as a safe lower bound to the collapse strength. Elastic moments are normally greatest at internal supports. For the two equal span case this negative (hogging) moment is equal to that of the positive (sagging) moment of single-span decking. Many profiles with wide troughs are weaker under negative moment than positive, and the effect of the localized reaction at the internal support is to reduce further the negative moment capacity. In design to code requirements, therefore, continuous decking may appear to be weaker than simply-supported decking even though in reality it must be considerably stronger.

In general the capacity of the decking is obtained from tests. However, it is possible to calculate strength conservatively using the following approach.

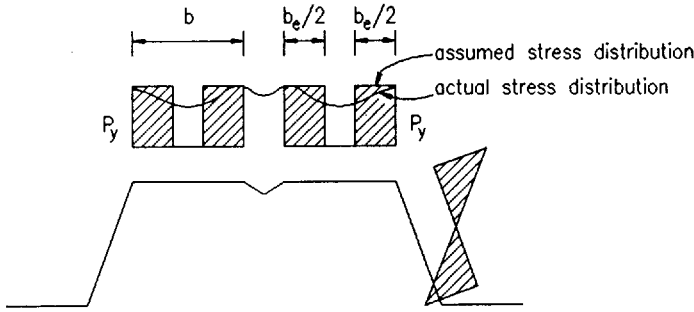


Fig. 20.3 Behaviour of stiffened plate in compression

The compressive strength of a thin plate is presented in terms of an effective width of plate acting at its full yield strength. This effective width  $b_e$  is based on a semi-empirical formula<sup>1</sup> considering the post-buckling strength of the plate, and is given by:

$$b_e = \frac{857t}{\sqrt{p_y}} \left( 1 - \frac{187t}{b\sqrt{p_y}} \right) \quad \text{but } \nless b \tag{20.1}$$

where  $t$  is the plate thickness,  $b$  is the plate width, both in mm, and  $p_y$  is the design strength of the steel in  $\text{N/mm}^2$ .

Where a stiffener is introduced, then the dimension  $b$  is based on the flat plate width between the stiffener and the web (see Fig. 20.3). However, there is a limiting size of stiffener below which it does not contribute to the increased capacity of the unstiffened plate. In most practical cases the web of the profile is fully effective.

The moment capacity of the section is evaluated using this effective width. In the calculations the design strength of the steel is taken as 0.93 times the specified yield strength. Under positive moment the top plate is in compression, whereas under negative moment the bottom plate is in compression. This suggests that the most efficient profiles are symmetric in shape. For serviceability calculations, the actual stress replaces the design stress in Equation (20.1). For most serviceability calculations, this stress may be taken as 65% of the design stress.

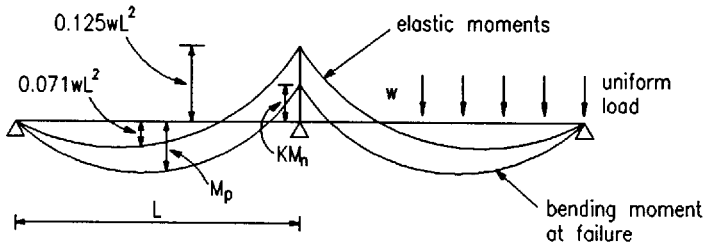
The construction condition generally determines the permissible spans of the slabs; this is the case which has the greatest influence on the economy of the method of construction. Design based on elastic moments in continuous decking is very conservative because at failure there is a significant redistribution of moment from the most highly stressed areas at the supports to the mid-span area, initially as a result of elastic effects because the stiffness of the section changes with applied moment. Beyond the point at which yield takes place, plate collapse and some 'plastic' deformation occurs with increasing deformation.

If the decking were able to deform in an ideal plastic manner, as in Fig. 20.4(a), then the 'plastic' failure load of an end-span would be approximately:

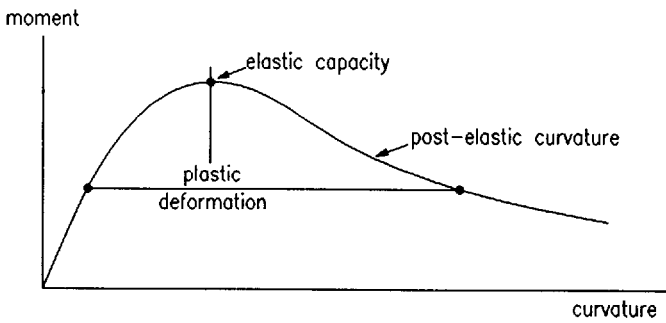
$$w = \frac{8}{L^2} (M_p + 0.46KM_n)$$

where  $M_p$  and  $M_n$  are the elastic moment capacities of the profile under positive and negative moment respectively. The factor  $K$  (less than unity) is introduced because only a proportion of  $M_n$  can be developed at failure. The key to this is the post-elastic behaviour of the section illustrated in Fig. 20.4(b).

From tests on different profile shapes it can be shown that the value of  $K$  has a lower bound over the normal range of sheet thicknesses and spans. Typically, the reduction in  $M_n$  (as reflected in the  $K$  value) corresponding to a support rotation of  $2-3^\circ$  to develop  $M_p$  is 50%. This method of design is covered in more detail in CIRIA Technical Note 116.<sup>3</sup>



(a)



(b)

Fig. 20.4 Ultimate behaviour of continuous decking: (a) moment on two-span decking, (b) typical moment-curvature relationship of decking

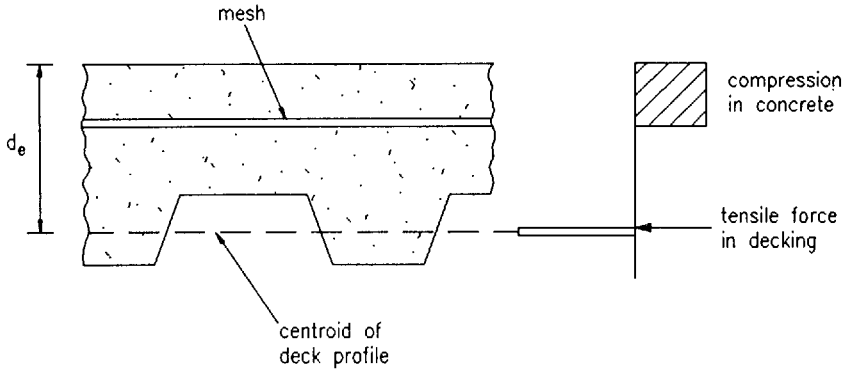


Fig. 20.5 Behaviour of composite deck slab as an equivalent reinforced concrete section

Spans 10% to 15% in excess of those predicted by elastic design are possible while maintaining an adequate factor of safety against failure, and satisfactory performance at working load. It is for this reason that manufacturers often present load–span tables on the basis of tests rather than the elastic method specified in BS 5950: Part 4.<sup>1</sup>

### 20.5.2 Composite condition

The cross-sectional area of the decking  $A_p$  acts as conventional reinforcement at a lever arm determined by the centroid of the profile, as shown in Fig. 20.5. The tensile forces in the decking are developed as a result of the bond between the decking and the concrete, enhanced by some form of mechanical connection, such as by indenting the profile.

If the shear-connectors used to develop composite action between the slab and the steel beam are also included in the design, then the full flexural capacity of the slab can usually be mobilized because of the end anchorage provided. If not, failure is usually by slip between the decking and the concrete, known as incomplete shear connection as indicated in Fig. 20.6. This means that the full flexural capacity of the slab is not developed. Nevertheless, the degree of composite action is sufficiently good that, for all but very heavy imposed loads, permissible spans are controlled by the construction condition. Vertical shear rarely influences the design.

Composite slabs are usually designed as simply-supported elements with no account taken of continuity provided by the reinforcement in the concrete at internal beams, reflecting the behaviour of an end-bay slab. However, internal bays will not fail by incomplete shear connection provided the decking is laid continuously over the supports, an observation which also applies to end anchorage which need only be developed at the edge beams or at sheet discontinuities in a continuous composite slab.

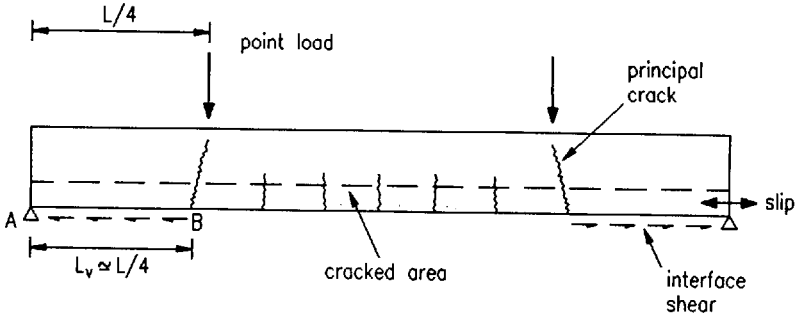


Fig. 20.6 Failure of composite slab by incomplete shear connection

The ultimate capacity of composite slabs, in the absence of end anchorage, is controlled by a combination of friction and chemical bond, followed by mechanical interlock after initial slippage. As a result, the performance of a particular decking system can only be readily assessed by testing. A typical slab under test is shown in Fig. 20.7.

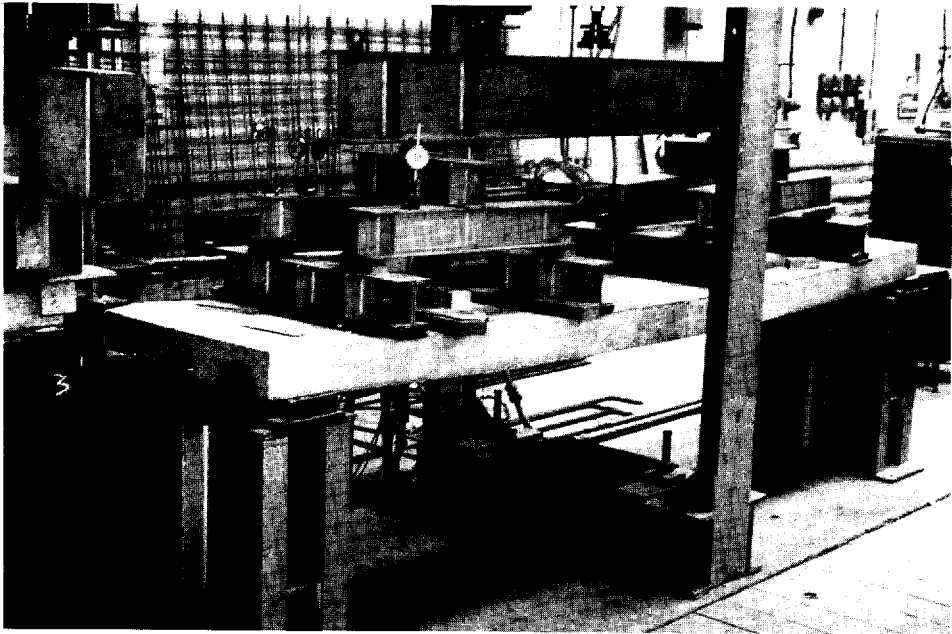


Fig. 20.7 Testing of composite slab to establish composite action

Mechanical interlock is partly dependent on the local plate stiffness and so indentations are best situated close to the more rigid sections of the profile, such as corners or narrow plate elements. Slippage is associated with separation; some profiles, such as the dovetail section, achieve good shear-bond capacity by preventing separation. Different trapezoidal profiles incorporate a wide variety of indent and embossment shapes, as illustrated in Fig. 20.2, which have varying degrees of effectiveness.

If design were to be carried out on elastic principles, permissible bond strengths between the deck profile and the concrete would be of the order of  $0.05 \text{ N/mm}^2$  for plain profiles rising to about  $0.2 \text{ N/mm}^2$  for some indented profiles. First slip and flexural failure of plain trapezoidal profiles are coincident, whereas there is often a considerable reserve following initial slip in properly designed composite slabs.

If failure of a composite slab that is propped during construction occurs by incomplete shear connection, then the applied load to be considered in the analysis of its shear bond strength is the imposed load plus self-weight loads on depropping. If the slab is not propped, then only the imposed load contributes to the shear bond mode of failure. If flexure governs strength, as in an equivalent reinforced concrete section, then the ultimate strength of the section is independent of the sequence of loading, and therefore the total load is to be considered in both propped and unpropped construction.

### 20.5.3 Requirements of BS 5950

The method of determining the ultimate shear bond capacity of composite slabs with a particular deck profile is based on load tests. A simply-supported slab of the appropriate proportions is subject to 2 or 4 point loads to simulate a uniformly distributed load (see Fig. 20.7). Crack inducers are cast into the slab so that a pre-determined length of the outer portion of the slab can slip under load relative to the deck, without developing the tensile reserve of the concrete. These crack inducers are placed at the desired position for the form of loading (normally quarter span points).

Testing to BS 5950: Part 4<sup>1</sup> requires that a minimum of six composite slabs are tested covering a range of design parameters. The slabs are first subject to a dynamic loading between 50% and 150% of the desired working load, and then the load is increased statically to failure. The objective of the dynamic part of the test is to identify those cases where there is inherent fragility in the concrete-deck connection. The ultimate load is then recorded.

The problem remains of how to use the test information in design, where the parameters may be different from those tested. This is achieved by using an empirical design formula in terms of experimentally derived constants.<sup>4</sup>

The ultimate vertical shear strength (per unit width) of a composite slab is given by the formula:

$$V_u = 0.8A_c (m_d p d_e/L_v + k_d \sqrt{f_{cu}}) \quad (20.2)$$

where  $p$  is the ratio of the cross-sectional area of the profile to that of the concrete  $A_c$  per unit width of slab;  $f_{cu}$  is the cube strength of the concrete;  $d_e$  is the effective slab depth to the centroid of the profile; and  $L_v$  is the shear span length, taken as one quarter of the slab span  $L$ .

The empirical constants  $m_d$  and  $k_d$  are calculated from the slope and intercept, respectively, of the reduced regression line of Fig. 20.8. Tests are carried out at the extremes of the regression line (such as low and high  $L$ ). The regression line is to be reduced by 15% if fewer than eight slab tests are performed over the range of spans. Extrapolation outside the limits of the tests is not permitted. The constant of 0.8 represents 1 (material factor) and takes account of the potential variability of this form of failure. The slab capacity is then compared to the applied shear forces using the load factors in Part 1 of BS 5950.

Physically,  $m_d$  is a broad measure of the effect of mechanical interlock and  $k_d$  broadly represents the friction bond. Despite this,  $k_d$  can be negative. In reality, it is unlikely that interlock is linearly dependent on profile area but Equation (20.2) may be considered to be reasonably accurate for small variations from the test parameters  $p$ ,  $d_e$ ,  $L_v$  and  $f_{cu}$ .

#### 20.5.4 Design tables

Manufacturers normally present design information in terms of load–span tables for the different decks that are marketed. A typical load–span table for a composite slab is shown in Table 20.1. It can be seen that the permissible spans of unpropped slabs are largely unaffected by imposed load because spans are controlled by the construction condition and the composite capacity of slabs of these spans exceeds the tabulated imposed loads. Conversely, permissible spans of propped slabs are considerably greater because design is now based on the composite condition. However, some of these designs may be controlled by deflection (see the span-to-depth ratios in section 20.4).

#### 20.5.5 Serviceability

The two key serviceability aspects relating to the design of composite slabs are avoidance of premature slip and control of deflections. It is not normally considered necessary to control cracking in concrete in heated buildings. Nevertheless, standard mesh reinforcement of area greater than 0.1% of the cross-sectional area of the concrete is placed at about 25 mm from the slab surface. This reinforcement also acts as ‘fire-reinforcement’ (see section 20.6). However, this minimum amount of



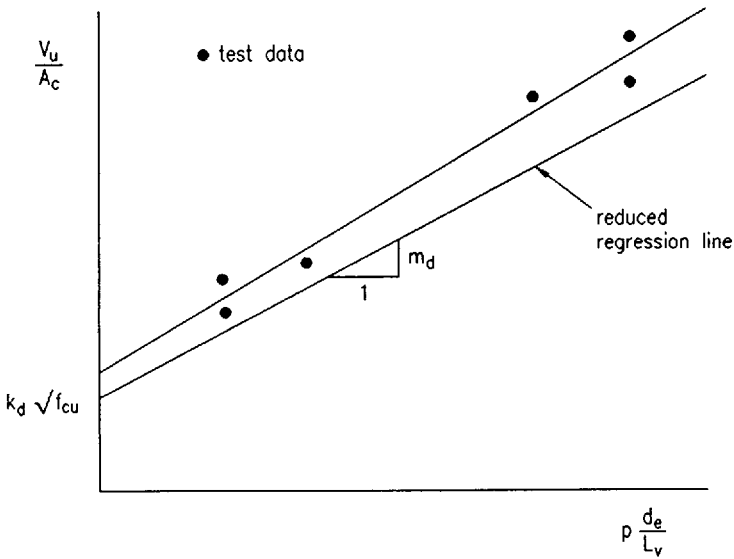
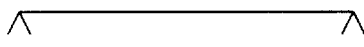
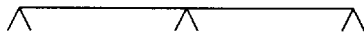



Fig. 20.8 Regression line for design of composite slabs

**Table 20.1** Permissible spans (m) according to BS 5950: Part 4 for typical 50 mm deep deck of thickness, *t*

| Support condition   | Slab depth (mm) | <i>t</i> = 0.9 mm                    |     | <i>t</i> = 1.2 mm |     |     |     |
|---|-----------------|--------------------------------------|-----|-------------------|-----|-----|-----|
|   |                 | Imposed loading (kN/m <sup>2</sup> ) |     |                   |     |     |     |
|   |                 | 2.5                                  | 5.0 | 7.5               | 2.5 | 5.0 | 7.5 |
| <br>Single span – no props | 100             | 2.6                                  | 2.6 | 2.6               | 3.1 | 3.1 | 3.1 |
|   | 150             | 2.2                                  | 2.2 | 2.2               | 2.7 | 2.7 | 2.7 |
| <br>Multiple span          | 100             | 2.7                                  | 2.7 | 2.7               | 3.2 | 3.2 | 3.1 |
|   | 150             | 2.3                                  | 2.3 | 2.3               | 2.8 | 2.8 | 2.8 |
| <br>Single span – one prop | 100             | 3.5                                  | 3.3 | 2.8               | 3.5 | 3.5 | 3.1 |
|   | 150             | 4.6                                  | 4.1 | 3.5               | 5.2 | 4.5 | 3.8 |

Maximum span-to-depth ratio limited to 35 for normal weight concrete slab

reinforcement would in theory be insufficient to control cracking at the supports of continuous slabs.

A typical load–deflection relationship of a composite slab is shown in Fig. 20.9. Initial slip occurs well before the ultimate load is reached in a well-designed slab. Nevertheless, it would be inadvisable if first slip occurred at below half of the ultimate load, because this might suggest poor serviceability performance.

The deflection of a composite slab is usually calculated on the assumption that it behaves as a reinforced concrete element with the deck area acting as an equivalent reinforcing bar. The section is assumed to be cracked in mid-span. The neutral axis depth below the upper slab surface is determined from:

$$x_c = d_c \{ \sqrt{[(\alpha_c p)^2 + 2\alpha_c p]} - \alpha_c p \} \quad (20.3)$$

where  $\alpha_c$  is the ratio of the elastic moduli of steel to concrete. The selection of an appropriate modular ratio is discussed in Chapter 21 (section 21.7.2). The values  $p$  and  $d_c$  are defined in section 20.5.3 and Fig. 20.5 respectively.

The cracked second moment of area (in steel units) is therefore given by:

$$I_c = x_c^3 / (3\alpha_c) + p d_c (d_c - x_c)^2 + I_s \quad (20.4)$$

where  $I_s$  is the second moment of area of the deck profile per unit width.

In determining deflections it is common practice to use the average value of the cracked and uncracked second moments of area of the section reflecting the fact that only part of the slab is cracked. Shrinkage-induced deflection of slabs is usually ignored.

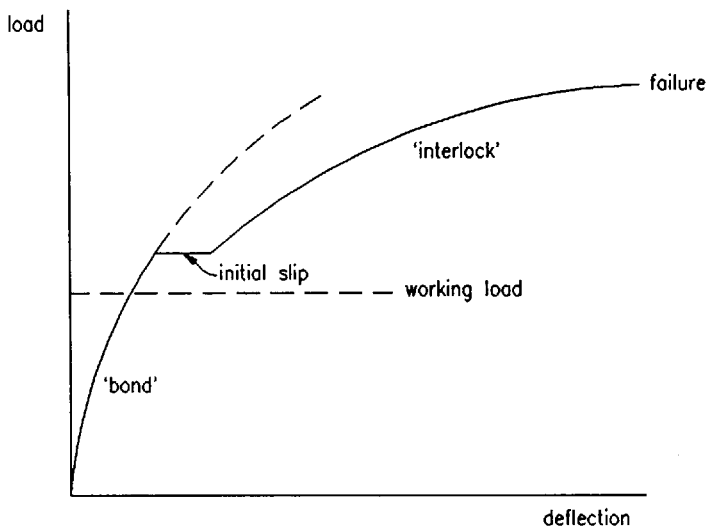


Fig. 20.9 Typical load–deflection behaviour of composite deck slabs

Although deflections are usually calculated assuming that the slab is simply-supported, the effect of continuity of negative (hogging) reinforcement may be estimated by reducing the deflection  $\delta_0$  of the simply-supported slab according to:

$$\delta_c = \delta_0 [1 - 0.6 (M_1 + M_2)/M_0] \quad (20.5)$$

where  $M_1$  and  $M_2$  are the negative moments at each support (not more than the moment capacity of the reinforced slab) and  $M_0$  is the simply-supported moment for the same loading conditions.

## 20.6 Fire resistance

### 20.6.1 Fire tests

Three criteria are imposed by the standard fire-resistance test on floors to BS 476: Part 20.<sup>5</sup> These are:

- (1) strength or stability under load
- (2) integrity to the passage of smoke or flame
- (3) insulation, so that the rise of temperature on the upper surface of the slab is not excessive.

Failure of a floor or beam is deemed to occur when the maximum deflection exceeds (span/20) or when the rate of deflection exceeds a specified amount.<sup>5</sup> To satisfy the insulation criterion the temperature on the upper surface of the slab should not exceed a maximum of 185°C or an average of 140°C above ambient.

In principle, the minimum depth of composite slabs is based on an insulation criterion, and the amount of reinforcement needed in a fire is based on a strength criterion. It would be reasonable to assume that most of the tensile capacity of the deck would be lost in a severe fire and therefore the load-carrying capacity derives mainly from the reinforcement.

There are a number of beneficial factors which make fires in real buildings generally less onerous than in a standard fire test. From a structural point of view, the most important factor to be modelled in a fire test is the effect of structural continuity. Membrane action (or in-plane restraint) is generally ignored because of its indeterminate magnitude. Until recently, few fire tests had included the effect of continuity of the slab and its reinforcement.

Simply-supported composite slabs with nominal reinforcement rarely exceed a fire-resistance period of 30 minutes whereas tests on continuous slabs with the same reinforcement can achieve over 60 minutes fire resistance. Indeed, a series of ten fire tests carried out in the UK showed that 90 minutes fire resistance can be achieved for slabs with standard mesh reinforcement and subject to imposed loads of up to 6.7 kN/m<sup>2</sup>. These imposed load and fire resistance requirements are typical of those specified currently for most commercial buildings.

### 20.6.2 Fire engineering method

The phrase 'fire engineering method' (FEM) is the term given to the means of calculating the amount of emergency reinforcement needed for a certain fire resistance period. This is described fully in a Steel Construction Institute publication.<sup>6</sup> In principle, the moment of resistance of the section is calculated taking into account the temperatures in the section and the reduced strength of the various elements at elevated temperatures. Temperatures are determined from tables or indicative tests. The plastic capacity of continuous members can be evaluated and compared to the applied moment with load factors of unity. In some areas, BS 5950: Part 8<sup>7</sup> permits a further 20% reduction in imposed load in a fire. Typically, therefore, the applied moment in a fire would be 50–60% of the ultimate design moment.

The critical element determining the moment of resistance of the section is the reinforcement. Mesh reinforcement is normally well-insulated from the effects of the fire and contributes significantly to the fire resistance of the slab. Where fire resistance periods greater than 90 minutes are required (see below) then additional reinforcing bars or heavier mesh can be introduced. In such cases it may be economic to design the slab as a reinforced concrete ribbed slab to BS 8110,<sup>8</sup> and treat the decking as permanent formwork. Bars of diameter 10 mm or 12 mm are normally placed singly in the troughs at the appropriate cover.

### 20.6.3 Design recommendations

Simple design tables covering common design cases are given in Reference 9. A minimum slab depth and mesh size are given for different profile types. Data for only two spans (i.e. 3 m and 3.6 m) and one imposed load (6.7 kN/m<sup>2</sup>) are presented, but these may be converted to other cases by using the same equivalent moment as the tabulated cases. The data are reproduced in Table 20.2.

## 20.7 Diaphragm action

The decking serves to transfer lateral loads to vertical bracing of concrete walls. It is normally attached on all four sides to support beams at spacings of not less than 600 mm. However deck–deck seam fasteners are not normally installed. The shear stiffness of the 'diaphragm' is very high and the strength is normally determined by the capacity of the fixings. Typical ultimate strengths of the standard screws or pins are 6 kN/mm sheet thickness. Where through-deck welding of shear-connectors is used the ultimate shear strength of the decking is considerably enhanced.

**Table 20.2** Simplified rules for fire resistance of composite deck slabs<sup>9</sup>

| (a) Trapezoidal profiles (depth not exceeding 60 mm) |                 |                      |                 |     |           |
|--|-----------------|----------------------|-----------------|-----|-----------|
| Minimum dimensions                                   |                 |                      |                 |     |           |
| Max. span (m)  | Fire rating (h) | Sheet thickness (mm) | Slab depth (mm) |     | Mesh size |
|  |                 |                      | NWC             | LWC |           |
| 2.7  | 1               | 0.8                  | 130             | 120 | A142      |
| 3.0  | 1               | 0.9                  | 130             | 120 | A142      |
|  | 1½              | 0.9                  | 140             | 130 | A142      |
| 3.6  | 1               | 1.0                  | 130             | 120 | A193      |
|  | 1½              | 1.0                  | 140             | 130 | A193      |

| (b) Dovetail profiles (depth not exceeding 50 mm) |                 |                      |                 |     |           |
|---|-----------------|----------------------|-----------------|-----|-----------|
| Minimum dimensions                                |                 |                      |                 |     |           |
| Max. span (m)                                     | Fire rating (h) | Sheet thickness (mm) | Slab depth (mm) |     | Mesh size |
|   |                 |                      | NWC             | LWC |           |
| 2.5   | 1               | 0.8                  | 100             | 100 | A142      |
|   | 1½              | 0.8                  | 110             | 105 | A142      |
| 3.0   | 1               | 0.9                  | 120             | 110 | A142      |
|   | 1½              | 0.9                  | 130             | 120 | A142      |
| 3.6   | 1               | 1.0                  | 125             | 120 | A193      |
|   | 1½              | 1.2                  | 135             | 125 | A193      |

The steel beams are laterally supported in simple bending by the decking, provided the decking crosses the beams and is attached to them by shear-connectors or pins at spacings not exceeding 600 mm. However, beams running parallel to the decking are laterally supported only at transverse beam connections. All beams are laterally supported under positive moment in their composite state.

## 20.8 Other constructional features

In the role of the decking as formwork, shuttering at the edge of the slab and at large openings is usually in the form of light cold-formed channels which are attached by pins or screws to the decking. Small openings can be formed by leaving 'boxed out' voids in the slab and the decking cut away once the concrete

has gained adequate strength. Additional reinforcement should be placed to redistribute the loads that would otherwise have been resisted by the composite slabs in this zone.

Propping of composite slabs is rarely used, but if so, it is important to ensure that the slab beneath can resist the self-weight and construction load of the slab being cast. This may be critical if the support slab has not gained its full strength for composite action. Timber spreaders should be used to avoid damage to the deck.

## References to Chapter 20

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9. Construction Industry Research and Information Association (CIRIA) (1986) *Data Sheet: Fire Resistance of Composite Slabs with Steel Decking*. CIRIA Special Publication 42.

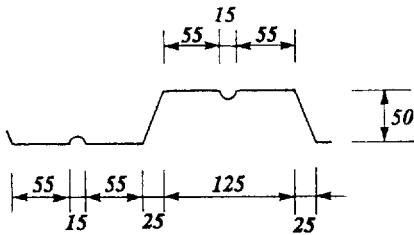
A worked example follows which is relevant to Chapter 20.

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**Problem**

Check the design of a composite slab 125 mm deep, spanning 3 m and using the deck shown below. (Note: this design is carried out to BS 5950: Part 4: 1982 which is currently under review.)

Deck shape :



Steel thickness  $t = 1.2 \text{ mm}$  (bare thickness of steel)

Steel grade  $p_y = 280 \text{ N/mm}^2$

Trough spacing = 300 mm

**Loads**

Imposed load = 5.0 kN/m<sup>2</sup>

Partitions (imposed load) = 1.0 kN/m<sup>2</sup>

Ceiling = 0.5 kN/m<sup>2</sup>

Self weight (slab) = 2.0 kN/m<sup>2</sup> - see later


Construction load (temporary) = 1.5 kN/m<sup>2</sup>

**Concrete**

Cube strength  $f_{cu} = 30 \text{ N/mm}^2$

Density (dry) = 1800 kg/m<sup>3</sup> (lightweight)

Density (wet) = 1900 kg/m<sup>3</sup> (lightweight)

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**Construction condition**

*Self weight of slab*

$$w_d = 1900 \times 9.81 \times 10^{-6} (75 + 50/2) = 1.86 \text{ kN/m}^2$$

$$\text{Self weight of deck} = 0.12 \text{ kN/m}^2$$

$$\text{Total self weight} \approx 2.0 \text{ kN/m}^2$$

*Design moment in construction condition*

$$M_u = (2.0 + 1.5) \times 1.4 \times \frac{3.0^2}{8}$$

$$= 5.51 \text{ kNm}$$

**Moment resistance of deck in sagging (positive bending)**

*Assume in the worst case that the deck is laid simply supported. The moment resistance derives from the positive (sagging) elastic moment resistance of the section.*

*Effective breadth of flat compression plate*

*Equation  
20.1*

$$b_e = \frac{857 t}{\sqrt{p_y}} \left[ 1 - \frac{187 t}{b \sqrt{p_y}} \right] \leq b$$


*where  $b = 55 \text{ mm}$*

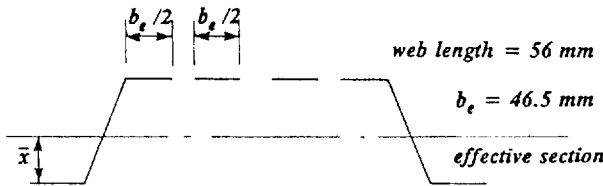
$$b_e = \frac{857 \times 1.2}{\sqrt{280}} \left[ 1 - \frac{187 \times 1.2}{55 \sqrt{280}} \right]$$

$$= 46.5 \text{ mm} < b$$

*According to BS5950: Part 4 the stiffener area is ignored when calculating the compressive resistance of the plate.*



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Neutral axis position

$$\bar{x} = \frac{(46.5 \times 2 + 56) \times 50}{(125 + 2 \times 56 + 2 \times 46.5)} = 22.5 \text{ mm}$$

Second moment of area

$$\begin{aligned} I &= 1.2 [46.5 \times 2 \times (48.8 - 22.5)^2 + 125 \times 22.5^2 \\ &\quad + 2 \times 56 \times \frac{50^2}{12} + 2 \times 56 \times (24.4 - 22.5)^2] \\ &= 1.2 (64.3 + 63.3 + 23.3 + 0.4) \times 10^3 \\ &= 181.6 \times 10^3 \text{ mm}^4 / \text{trough} \\ &= 605 \times 10^3 \text{ mm}^4 / \text{m width} \end{aligned}$$

Depth of web in compression = 26.3 mm

$$d/t = 21.9 \quad - \text{it is not necessary to check for local buckling of web}$$


Elastic section modulus

$$Z_e = \frac{605 \times 10^3}{(49.4 - 22.5)} = 22.5 \times 10^3 \text{ mm}^3 / \text{m}$$

Elastic moment resistance of section (sagging moment)

$$\begin{aligned} M_c &= Z_e \times 0.93 p_y = 22.4 \times 10^3 \times 0.93 \times 280 \times 10^{-6} \\ &= 5.8 \text{ kNm} > M_u \end{aligned}$$

(using a design strength of 0.93 p<sub>y</sub> as in BS 5950: Part 4)

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**Check deflection of slab after construction**

***Bending moment on deck after construction***

$$= 2.0 \times 3.0^2 / 8 = 2.25 \text{ kNm}$$

***Equivalent stress in compression plate***

$$\sigma \approx \frac{2.25}{6.3} \times 280 = 100 \text{ N/mm}^2$$

***Repeating the calculation of second moment of area using this stress (rather than  $p_y$ ) in equation 20.1 gives:***

$$I = 649 \times 10^3 \text{ mm}^4 / \text{m width}$$

***Deflection of soffit of deck (simply supported)***

$$\delta_2 = \frac{5 \times 2.0 \times 3000^4}{384 \times 205 \times 10^3 \times 649 \times 10^3}$$

$$= 15.9 \text{ mm (span/188)}$$

***This is less than the limit of span/180 in BS 5950: Part 4. If this limit had been exceeded it would be necessary to include for the effects of ponding of concrete at greater deflections.***

**Composite condition**

***Check moment resistance of the composite section as a reinforced concrete slab, assuming full shear connection.***


***Area of deck*** =  $(125 + 56) \times 2 \times 1.2$

$$= 434 \text{ mm}^2 / \text{trough}$$

$$A_p = 1448 \text{ mm}^2 / \text{m}$$

***Tensile resistance*** =  $0.93 \times 280 \times 1448 \times 10^{-3}$

$$= 377 \text{ kN}$$

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*Neutral axis depth into concrete*

$$x_c = \frac{377 \times 10^3}{0.4 \times f_{cu} \times 10^3} = 31.4 \text{ mm}$$

*Plastic moment resistance of composite section*

$$M_p = 377 \times (125 - 25 - 31.4/2) \times 10^{-3}$$

$$= 31.8 \text{ kNm}$$

*Applied moment in composite condition*

$$M_u = [1.6(5.0 + 1.0) + 1.4(2.0 + 0.5)] \times 3.0^2/8$$

$$= 14.7 \text{ kNm}$$

*Therefore, the plastic moment resistance of the section is more than adequate.*

*Check for incomplete shear connection*

*Equation 20.2*

$$V_u = 0.8 A_c \left( m_d \times p \times \frac{d_e}{L_v} + k_d \sqrt{f_{cu}} \right)$$


$$\text{where } p = \frac{A_p}{A_c} = \frac{1448}{100 \times 1000} = 0.0145$$

$$d_e = 100 \text{ mm}$$

$$L_v = 3000/4 = 750 \text{ mm}$$

*Typical values of empirical constants are:*

$$m_d = 130 \quad \text{and} \quad k_d = 0.004$$

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$$\begin{aligned}
 V_u &= 0.8 \times 100 \times \times \left( 130 \times 0.0145 \times \frac{100}{750} + 0.004\sqrt{30} \right) \\
 &= 80 (0.251 + 0.022) \\
 &= 21.8 \text{ kN}
 \end{aligned}$$

*Applied ultimate shear force*

$$V = 4 M_u / L = 4 \times 14.7 / 3.0 = 19.6 \text{ kN}$$

*The slab can resist the applied loads adequately without failure by incomplete shear connection.*

*Check shear stress on concrete*

$$v_c = \frac{19.6 \times 10^3}{100 \times 10^3} = 0.20 \text{ N/mm}^2$$


*This is relatively small according to BS8110.*

*Check deflection of composite slab*

*Properties of cracked section:*

*Neutral axis depth below upper surface of slab*

$$\begin{aligned}
 x_e &= d_e \left( \sqrt{(\alpha_e p)^2 + 2 \alpha_e p} - \alpha_e p \right) && \text{Equation 20.3} \\
 \alpha_e &= \text{modular ratio} = 15 \text{ for LWC} \\
 \alpha_e p &= 0.0145 \times 15 = 0.218 \\
 x_e &= 100 \left( \sqrt{0.218^2 + 2 \times 0.218} - 0.218 \right) \\
 &= 51.5 \text{ mm}
 \end{aligned}$$

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Second moment of area of cracked section

Equation  
20.4

$$\begin{aligned}
 I_c &= \frac{51.5^3}{3 \times 15} + 0.0145 \times 100 \times (100 - 51.5)^2 + 649 \\
 &= 3035 + 3411 + 649 \\
 &= 7095 \text{ mm}^4 / \text{mm width (in steel units)}
 \end{aligned}$$

Service load on composite slab

$$w_s = 5.0 + 1.0 + 0.5 = 6.5 \text{ kN/m}^2$$

Deflection under service load

$$\begin{aligned}
 \delta &= \frac{5 \times 6.5 \times 3000^4 \times 10^{-3}}{384 \times 205 \times 10^3 \times 7095} \\
 &= 4.7 \text{ mm (or span/638)}
 \end{aligned}$$

This is satisfactory.

Note:

Mesh reinforcement is required for crack control and fire resistance requirements.

# Chapter 21

## Composite beams

by MARK LAWSON and PETER WICKENS

### 21.1 Applications of composite beams

In buildings and bridges steel beams often support concrete slabs. Under load each component acts independently with relative movement or slip occurring at the interface. If the components are connected so that slip is eliminated, or considerably reduced, then the slab and steel beam act together as a composite unit (Fig. 21.1). There is a consequent increase in the strength and stiffness of the composite beam relative to the sum of the components.

The slab may be solid in situ concrete or the composite deck slab considered in Chapter 20. It may also comprise precast concrete units with an in situ concrete topping. In buildings, steel beams are usually of standard UB section, but UC sections are sometimes used where there is need to minimize the beam depth. A typical building under construction is shown in Fig. 21.2. Welded fabricated sections are often used for long-span beams in buildings and bridges.

Design of composite beams in buildings is now covered by BS 5950: Part 3,<sup>1</sup> although guidance was formerly available in an SCI publication.<sup>2</sup> The design of composite beams incorporating composite slabs is affected by the shape and orientation of the decking, as indicated in Fig. 21.3.

One of the advantages of composite construction is smaller construction depths. Services can usually be passed beneath, but there are circumstances where the

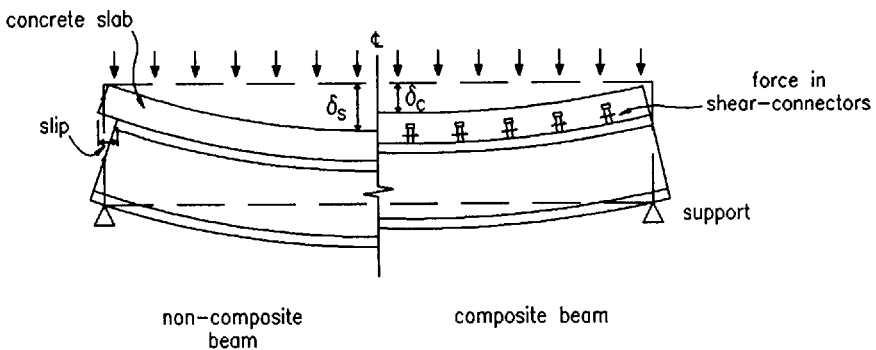


Fig. 21.1 Behaviour of composite and non-composite beams



Fig. 21.2 Composite building under construction showing decking and shear-connectors

beam depth is such that services can be passed through the structure, either by forming large openings, or by special design of the structural system. A good example of this is the stub-girder.<sup>3</sup> The bottom chord is a steel section and the upper chord is the concrete slab. Short steel sections or 'stubs' are introduced to transfer the forces between the chords.

Openings through the beam webs can be provided for services. Typically, these can be up to 70% of the beam depth and can be rectangular or circular in shape. Guidance on the design of composite beams with web openings is given in Reference 4. Examples of the above methods of introducing services within the structure are shown in Fig. 21.4.

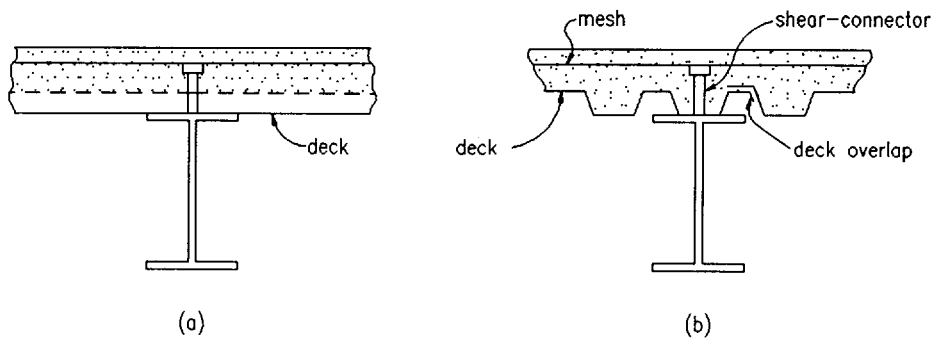


Fig. 21.3 Composite beams incorporating composite deck slabs: (a) deck perpendicular to beam, (b) deck parallel to beam

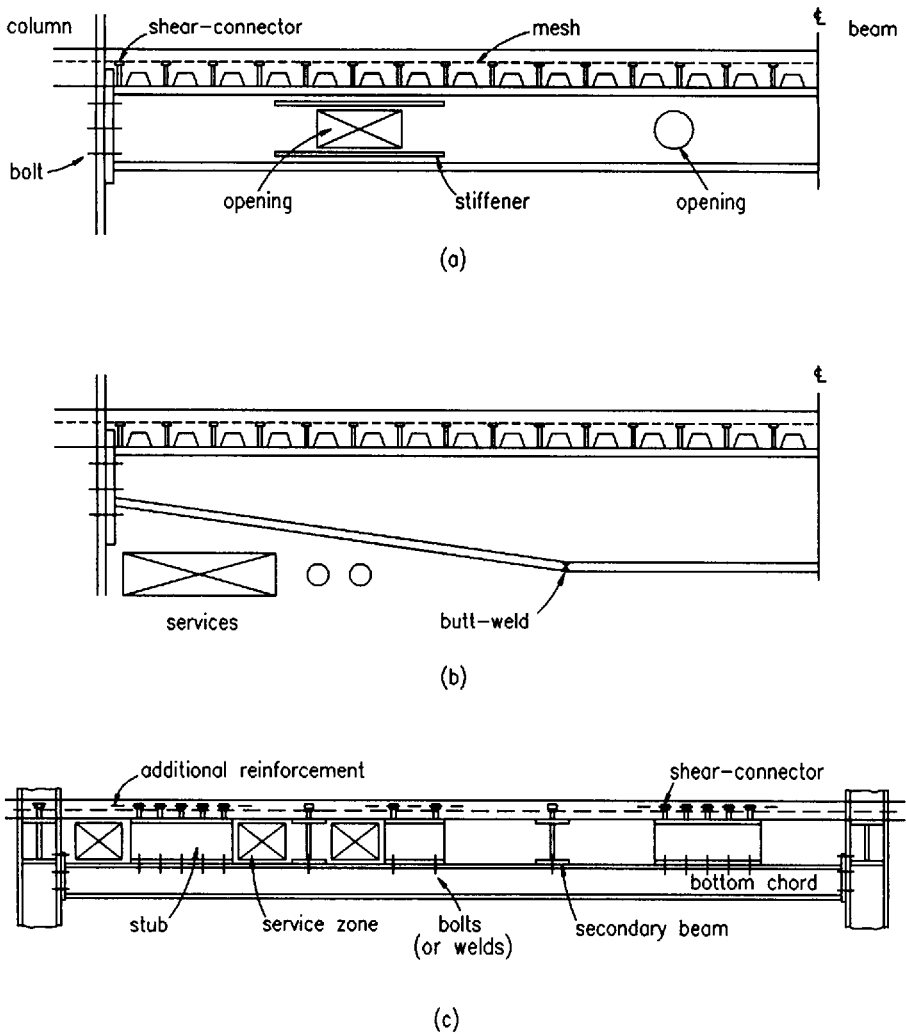


Fig. 21.4 Different methods of incorporating services within the structural depth

## 21.2 Economy

Composite beam construction has a number of advantages over non-composite construction:

- (1) savings in steel weight are typically 30% to 50% over non-composite beams.
- (2) the greater stiffness of the system means that beams can be shallower for the same span, leading to lower storey heights and savings in cladding, etc.



It also shares the advantage of rapid construction.

The main disadvantage is the need to provide shear-connectors at the interface between the steel and concrete. There may also be an apparent increase in complexity of design. However, design tables have been presented to aid selection of member sizes.<sup>2</sup>

The normal method of designing simply-supported beams for strength is by plastic analysis of the cross-section. Full shear connection means that sufficient shear-connectors are provided to develop the full plastic capacity of the section. Beams designed for full shear connection result in the lightest beam size. Where fewer shear-connectors are provided (known as partial shear connection) the beam size is heavier, but the overall design may be more economic.

Partial shear connection is most attractive where the number of shear-connectors is placed in a standard pattern; such as one per deck trough or one per alternate trough where profiled decking is used. In such cases, the resistance of the shear-connectors is a fixed quantity irrespective of the size of the beam or slab.

Conventional elastic design of the section results in heavier beams than with plastic design because it is not possible to develop the full tensile capacity of the steel section. Designs based on elastic principles are to be used where the compressive elements of the section are non-compact or slender, as defined in BS 5950 Part 1. This mainly affects the design of continuous beams (see section 21.6.3).

### 21.3 Guidance on span-to-depth ratios

Beams are frequently designed to be unpropped during construction. Therefore, the steel beam is sized first to support the self-weight of the slab before the concrete has gained adequate strength for composite action. Beams are assumed to be laterally restrained by the decking in cases where the decking crosses the beams and is directly attached to them. These beams can develop their full flexural capacity.

Where simply-supported unpropped composite beams are sized on the basis of their plastic capacity it is normally found that span-to-depth ratios can be in the range of 18 to 22 before serviceability criteria influence the design. The 'depth' in these cases is defined as the overall depth of the beam and slab. Grade 50 steel is often specified in preference to grade 43 in composite beam design because the stiffness of a composite beam is often three to four times that of the non-composite beam, justifying the use of higher working stresses.

The span-to-depth ratios of continuous composite beams are usually in the range of 22 to 25 for end spans and 25 to 30 for internal spans before serviceability criteria influence the design. Many continuous bridges are designed to satisfy the serviceability limit state.

## 21.4 Types of shear connection

The modern form of shear-connector is the welded headed stud ranging in diameter from 13–25 mm and from 65–125 mm in height. The most popular size is 19 mm diameter and 100 mm height. When used with steel decking, studs are often welded through the decking using a hand tool connected via a control unit to a power generator. Each stud takes only a few seconds to weld in place. Alternatively, the studs can be welded directly to the steel beams in the factory and the decking butted up to or slotted over the studs.

There are, however, some limitations to through-deck welding: the top flange of the beam must not be painted, the galvanized steel should be less than around 1.25 mm thick and the deck should be clean and free of moisture. The power generator needs 415 V electrical supply, and the maximum cable length between the weld gun and the power control units should be limited to around 70 m to avoid loss of power.

Where precast concrete planks are used, the positions of the shear-connectors are usually such that they project through holes in the slab which are later filled with concrete. Alternatively, a gap is left between the ends of the units sitting on the top flange of the beam on to which the shear connectors are fixed. Reinforcement (usually in the form of looped bars) is provided around the shear-connectors.

There is a range of other forms of welded shear-connector, but most lack practical applications. The ‘bar and hoop’ and ‘channel’ welded shear-connectors have been used in bridge construction.<sup>5</sup> Shot-fired shear-connectors are marketed for use in smaller building projects where site power might be a problem. All shear-connectors should be capable of resisting uplift forces; hence the use of headed rather than plain studs.

The number of shear-connectors placed along the beam is usually sufficient to develop the full flexural capacity of the member. However it is possible to reduce the number of shear-connectors in cases where the moment capacity exceeds the applied moment and the shear-connectors have adequate ductility. This is known as ‘partial shear connection’ and is covered in section 21.7.4.

## 21.5 Span conditions

In buildings, composite beams are usually designed to be simply-supported, mainly to simplify the design process, to reduce the complexity of the beam-to-column connections, and to minimize the amount of slab reinforcement and shear-connectors that are needed to develop continuity at the ultimate limit state.

However, there are ways in which continuity can be readily introduced, in order to improve the stiffness of composite beams. Figure 21.5 shows how a typical connection detail at an internal column can be modified to develop continuity. The stub girder system also utilizes continuity of the secondary members (see Fig. 21.4(c)). Other methods of continuous design are presented in References 3 and 6.

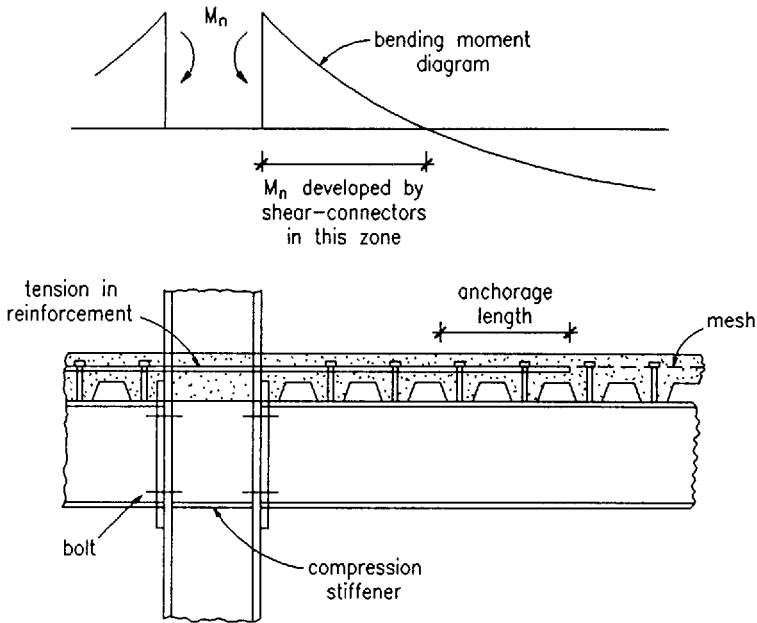


Fig. 21.5 Representation of conditions at internal column of continuous beam

Continuous composite beams may be more economic than simply-supported beams where plastic hinge analysis of the continuous member is carried out, provided the section is plastic according to BS 5950: Part 1. However, where the lower flange or web of the beam is non-compact or slender in the negative (hogging) moment region, then elastic design must be used, both in terms of the distribution of moment along the beam, and also for analysis of the section. Lateral instability of the lower flange is an important design condition, although torsional restraint is developed by the web of the section and the concrete slab.<sup>6</sup>

In bridges, continuity is often desirable for serviceability reasons, both to reduce deflections, and to minimize cracking of the concrete slab, finishes and wearing surface in road bridges. Special features of composite construction appropriate to bridge design are covered in the publication by Johnson and Buckby<sup>7</sup> based on BS 5400: Part 5.<sup>5</sup>

## 21.6 Analysis of composite section

### 21.6.1 Elastic analysis

Elastic analysis is employed in establishing the serviceability performance of composite beams, or the strength of beams subject to the effect of instability, for

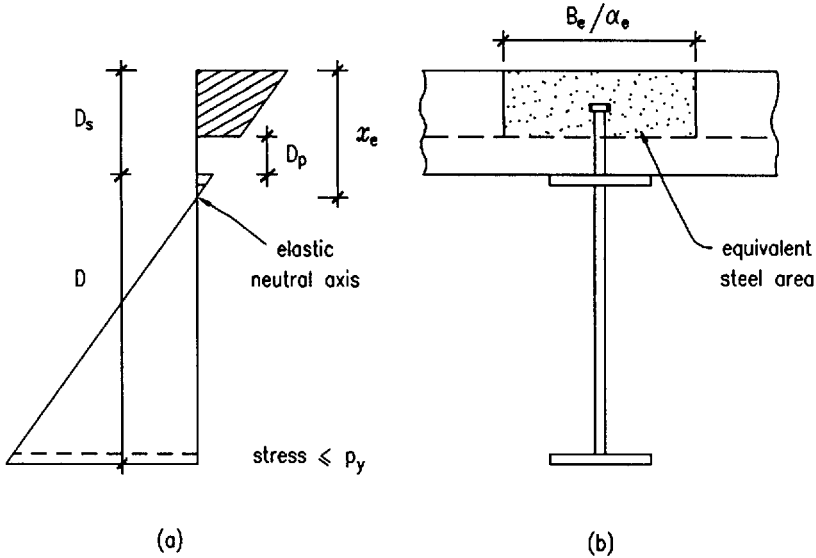


Fig. 21.6 Elastic behaviour of composite beam. (a) Elastic stress distribution. (b) Transformed section

example, in continuous construction, or in beams where the ductility of the shear connection is not adequate.

The important properties of the section are the section modulus and the second moment of area. First it is necessary to determine the centroid (elastic neutral axis) of the transformed section by expressing the area of concrete in steel units by dividing the concrete area within the effective breadth of the slab,  $B_e$ , by an appropriate modular ratio (ratio of the elastic modulus of steel to concrete).

In unpropped construction, account is taken of the stresses induced in the non-composite section as well as the stresses in the composite section. In elastic analysis, therefore, the order of loading is important. For elastic conditions to hold, extreme fibre stresses are kept below their design values, and slip at the interface between the concrete and steel should be negligible.

The elastic section properties are evaluated from the transformed section as in Fig. 21.6. The term  $\alpha_e$  is the modular ratio. The area of concrete within the profile depth is ignored (this is conservative where the decking troughs lie parallel to the beam). The concrete can usually be assumed to be uncracked under positive moment.

The elastic neutral axis depth,  $x_e$ , below the upper surface of the slab is determined from the formula:

$$x_e = \frac{\frac{D_s - D_p}{2} + \alpha_e r \left( \frac{D}{2} + D_s \right)}{1 + \alpha_e r} \tag{21.1}$$

where  $r = A/[(D_s - D_p)B_e]$ ,  $D_s$  is the slab depth,  $D_p$  is profile height (see Fig. 21.6) and  $A$  is the cross-sectional area of the beam of depth  $D$ .

The second moment of area of the uncracked composite section is:

$$I_c = \frac{A(D + D_s + D_p)^2}{4(1 + \alpha_e r)} + \frac{B_e(D_s - D_p)^3}{12\alpha_e} + I \quad (21.2)$$

where  $I$  is the second moment of area of the steel section. The section modulus for the steel in tension is:

$$Z_t = I_c / (D + D_s - x_c) \quad (21.3)$$

and for concrete in compression is:

$$Z_c = I_c \alpha_e / x_c \quad (21.4)$$

The composite stiffness can be 3 to 5 times, and the section modulus 1.5 to 2.5 times that of the I-section alone.

### 21.6.2 Plastic analysis

The ultimate strength of a composite section is determined from its plastic capacity. It is assumed that the strains across the section are sufficiently great that the steel stresses are at yield throughout the section and that the concrete stresses are at their design strength. The plastic stress blocks are therefore rectangular, as opposed to linear in elastic design.

The plastic capacity of the section is independent of the order of loading (i.e. propped or unpropped construction). The plastic capacity is compared to the moment resulting from the total factored loading using the load factors in BS 5950: Part 1.

The plastic neutral axis of the composite section is evaluated assuming stresses of  $p_y$  in the steel and  $0.45f_{cu}$  in the concrete. The tensile capacity of the steel is therefore  $R_s = p_y A$ , where  $A$  is the cross-sectional area of the beam. The compressive capacity of the concrete slab depends on the orientation of the decking. Where the decking crosses the beams the depth of concrete contributing to the compressive capacity is  $D_s - D_p$  (Fig. 21.6(a)). Clearly,  $D_p$  is zero in a solid slab. Where the decking runs parallel to the beams (Fig. 21.6(b)), then the total cross-sectional area of the concrete is used. Taking the first case:

$$R_c = 0.45f_{cu} (D_s - D_p)B_e \quad (21.5)$$

where  $B_e$  is the effective breadth of the slab considered in section 21.7.1.

Three cases of plastic neutral axis depth  $x_p$  (measured from the upper surface of the slab) exist. These are presented in Fig. 21.7. It is not necessary to calculate  $x_p$  explicitly if the following formulae for the plastic capacity of I-section beams subject to positive (sagging) moment are used. The value  $R_w$  is the axial capacity of the web and  $R_f$  is the axial capacity of one steel flange (the section is assumed

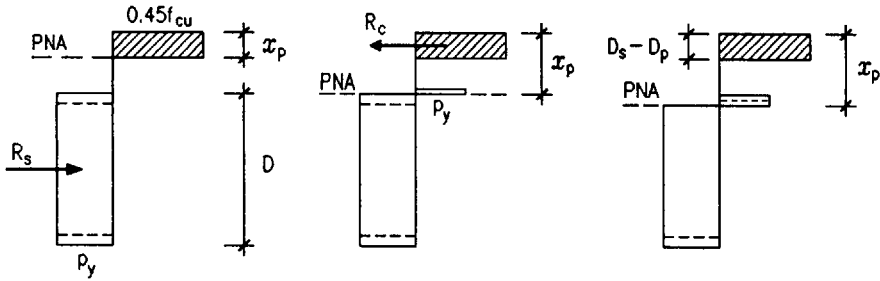


Fig. 21.7 Plastic analysis of composite section under positive moment (PNA: plastic neutral axis)

to be symmetrical). The top flange is considered to be fully restrained by the concrete slab.

The moment capacity,  $M_{pc}$ , of the composite beam is given by:

Case 1:  $R_c > R_s$  (plastic neutral axis lies in concrete slab):

$$M_{pc} = R_s \left[ \frac{D}{2} + D_s - \frac{R_s}{R_c} \left( \frac{D_s - D_p}{2} \right) \right] \tag{21.6}$$

Case 2:  $R_s > R_c > R_w$  (plastic neutral axis lies in steel flange):

$$M_{pc} = R_s \frac{D}{2} + R_c \left( \frac{D_s + D_p}{2} \right) - \frac{(R_s - R_c)^2 T}{R_f 4} \tag{21.7}$$

NB the last term in this expression is generally small ( $T$  is the flange thickness).

Case 3:  $R_c < R_w$  (plastic neutral axis lies in web):

$$M_{pc} = M_s + R_c \left( \frac{D_s + D_p + D}{2} \right) - \frac{R_c^2 D}{R_w 4} \tag{21.8}$$

where  $M_s$  is the plastic moment capacity of the steel section alone. This formula assumes that the web is compact i.e. not subject to the effects of local buckling. For this to be true the depth of the web in compression should not exceed  $78t\epsilon$ , where  $t$  is the web thickness ( $\epsilon$  is defined in BS 5950: Part 1). If the web is non-compact, a method of determining the moment capacity of the section is given in BS 5950: Part 3, Appendix B.<sup>1</sup>

### 21.6.3 Continuous beams

Bending moments in continuous composite beams can be evaluated from elastic global analysis. However, these result in an overestimate of moments at the supports because cracking of the concrete reduces the stiffness of the section and permits a relaxation of bending moment. A simplified approach is to redistribute

**Table 21.1** Maximum redistribution of support moment based on elastic design of continuous beams at the ultimate limit state

| Assumed section properties at supports | Classification of compression flange at supports |              |         |           |   |
|--|--|--------------|---------|-----------|---|
|  | Slender  | Semi-compact | Compact | Plastic   |   |
|  |  |              |         | Generally | Beams (with nominal slab reinforcement) |
| Gross uncracked                        | 10%  | 20%          | 30%     | 40%       | 50%                                     |
| Cracked                                | 0%   | 10%          | 20%     | 30%       | 30%                                     |

the support moment based on gross (uncracked) section properties by the amounts given in Table 21.1. Alternatively, moments can be determined using the appropriate cracked and uncracked stiffnesses in a frame analysis. In this case, the permitted redistribution of moment is less.

The section classification is expressed in terms of the proportions of the compression (lower) flange at internal supports. This determines the permitted redistribution of moment. A special category of plastic section is introduced where the section is of uniform shape throughout and nominal reinforcement is placed in the slab which does not contribute to the flexural capacity of the beam. In this case the maximum redistribution of moment under uniform loading is increased to 50%. A simplified elastic approach is to use the design moments in Table 21.2 assuming that:

- (1) the unfactored imposed load does not exceed twice the unfactored dead load;
- (2) the load is uniformly distributed;
- (3) end spans do not exceed 115% of the length of the adjacent span;
- (4) adjacent spans do not differ in length by more than 25% of the longer span.

An alternative to the elastic approach is plastic hinge analysis of plastic sections. Conditions on the use of plastic hinge analysis are presented in BS 5950: Part 3,<sup>1</sup> and Eurocode 4 (draft).<sup>8</sup> However, large redistributions of moment may adversely affect serviceability behaviour (see section 21.7.8).

The ultimate capacity of a continuous beam under positive moment is determined as for a simply-supported beam. The effective breadth of the slab is based on the effective span of the beam under positive moment (see section 21.7.1). The number of shear-connectors contributing to the positive moment capacity is ascertained knowing the point of contraflexure.

The negative (hogging) moment capacity of a continuous beam or cantilever should be based on the steel section together with any properly anchored tension reinforcement within the effective breadth of the slab. This poses problems at edge columns, where it may be prudent to neglect the effect of the reinforcement unless particular measures are taken to provide this anchorage. The behaviour of a continuous beam is represented in Fig. 21.5.

**Table 21.2** Moment coefficients (multiplied by free moment of  $WL/8$ ) for elastic design of continuous beams

| Location                         |                 | Classification of compression flange at supports |              |         |           |   |
|----------------------------------|-----------------|--|--------------|---------|-----------|---|
|                                  |                 | Slender  | Semi-compact | Compact | Plastic   |   |
|                                  |                 |  |              |         | Generally | Beams (with nominal slab reinforcement) |
| Middle of end span               | 2 spans         | 0.71   | 0.71         | 0.71    | 0.75      | 0.79                                    |
|                                  | 3 or more spans | 0.80   | 0.80         | 0.80    | 0.80      | 0.82                                    |
| First internal support           | 2 spans         | 0.91   | 0.81         | 0.71    | 0.61      | 0.50                                    |
|                                  | 3 or more spans | 0.86   | 0.76         | 0.67    | 0.57      | 0.48                                    |
| Middle of internal spans         |                 | 0.65   | 0.65         | 0.65    | 0.65      | 0.67                                    |
| Internal supports (except first) |                 | 0.75   | 0.67         | 0.58    | 0.50      | 0.42                                    |
| Redistribution                   |                 | 10%  | 20%          | 30%     | 40%       | 50%                                     |

The negative moment capacity is evaluated from plastic analysis of the section:

*Case 1:*  $R_r < R_w$  (plastic neutral axis lies in web):

$$M_{nc} = M_s + R_s \left( \frac{D}{2} + D_r \right) - \frac{R_q^2 D}{R_w 4} \quad (21.9)$$

where  $R_r$  is the tensile capacity of the reinforcement over width  $B_c$ ,  $R_q$  is the capacity of the shear-connectors between the point of contraflexure and the point of maximum negative moment (see section 21.7.3).  $D_r$  is the height of the reinforcement above the top of the beam.

*Case 2:*  $R_r > R_w$  (plastic neutral axis lies in flange):

$$M_{nc} = R_s \frac{D}{2} + R_r D_r - \frac{(R_s - R_r)^2 T}{R_f 4} \quad (21.10)$$

*NB* the last term in this expression is generally small.

The formulae assume that the web and lower flange are compact i.e. not subject to the effects of local buckling. The limiting depth of the web in compression is  $78t\varepsilon$  (where  $\varepsilon$  is defined in Chapter 2) and the limiting breadth : thickness ratio of the flange is defined in Table 7 of BS 5950: Part 1.

If these limiting slendernesses are exceeded then the section is designed elastically; often the situation in bridge design. The appropriate effective breadth of slab



is used because of the sensitivity of the position of the elastic neutral axis and hence the zone of the web in compression to the tensile force transferred by the reinforcement. The elastic section properties are determined on the assumption that the concrete is cracked and does not contribute to the resistance of the section.

## 21.7 Basic design

### 21.7.1 Effective breadths

The structural system of a composite floor or bridge deck is essentially a series of parallel T beams with wide thin flanges. In such a system the contribution of the concrete flange in compression is limited because of the influence of 'shear lag'. The change in longitudinal stress is associated with in-plane shear strains in the flanges.

The ratio of the effective breadth of the slab to the actual breadth ( $B_e/B$ ) is a function of the type of loading, the support conditions and the cross-section under consideration as illustrated in Fig. 21.8. The effective breadth of slab is therefore not a precise figure but approximations are justified. A common approach in plastic design is to consider the effective breadth as a proportion (typically 20% – 33%) of the beam span. This is because the conditions at failure are different from the elastic conditions used in determining the data in Fig. 21.8, and the plastic bending capacity of a composite section is relatively insensitive to the precise value of effective breadth used.

Eurocode 4 (in draft)<sup>8</sup> and BS 5950: Part 3<sup>1</sup> define the effective breadth as (span/4) (half on each side of the beam) but not exceeding the actual slab breadth

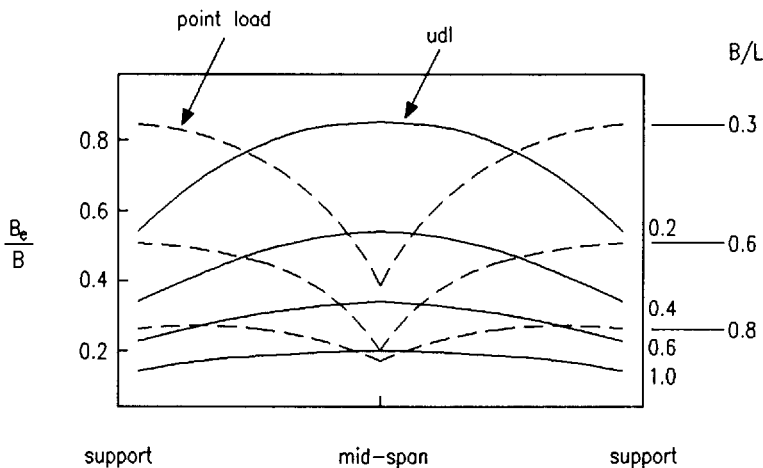


Fig. 21.8 Variation of effective breadth along beam and with loading

considered to act with each beam. Where profiled decking spans in the same direction as the beams, as in Fig. 21.3(b), allowance is made for the combined flexural action of the composite slab and the composite beam by limiting the effective breadth to 80% of the actual breadth.

In building design, the same effective breadth is used for section analysis at both the ultimate and serviceability limit states. In bridge design to BS 5400: Part 5,<sup>5</sup> tabular data of effective breadths are given for elastic design at the serviceability limit state. If plastic design is appropriate, the effective breadth is modified to  $(\text{span}/3)$ .<sup>5</sup>

In the design of continuous beams, the effective breadth of the slab may be based conservatively on the effective span of the beam subject to positive or negative moment. For positive moment, the effective breadth is 0.25 times 0.7 span, and for negative moment, the effective breadth is 0.25 times 0.25 times the sum of the adjacent spans. These effective breadths reduce to 0.175 span and 0.125 span respectively for positive and negative moment regions of equal-span beams.

### 21.7.2 Modular ratio

The modular ratio is the ratio of the elastic modulus of steel to the creep-modified modulus of concrete which depends on the duration of the load. The short- and long-term modular ratios given in Table 21.3 may be used for all grades of concrete. The effective modular ratio used in design should be related to the proportions of the loading that are considered to be of short- and long-term duration. Typical values used for office buildings are 10 for normal weight and 15 for lightweight concrete.

### 21.7.3 Shear connection

The shear strength of shear-connectors is established by the push-out test, a standard test using a solid slab. A typical load–slip curve for a welded stud is

**Table 21.3** Modular ratios ( $\alpha_e$ ) of steel to concrete

| Type of concrete                                   | Duration of loading |           |                  |
|--|---------------------|-----------|------------------|
|  | Short-term          | Long-term | 'Office' loading |
| Normal weight                                      | 6                   | 18        | 10               |
| Lightweight<br>(density > 1750 kg/m <sup>3</sup> ) | 10                  | 25        | 15               |

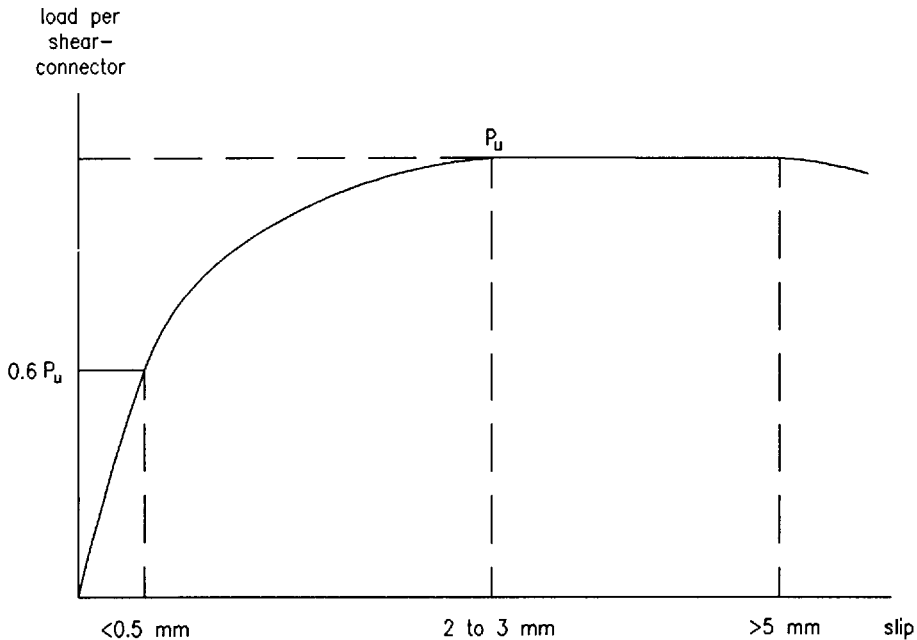


Fig. 21.9 Load-slip relationship for ductile welded shear-connector

shown in Fig. 21.9. The loading portion can be assumed to follow an empirical curve.<sup>9</sup> The strength plateau is reached at a slip of 2–3 mm.

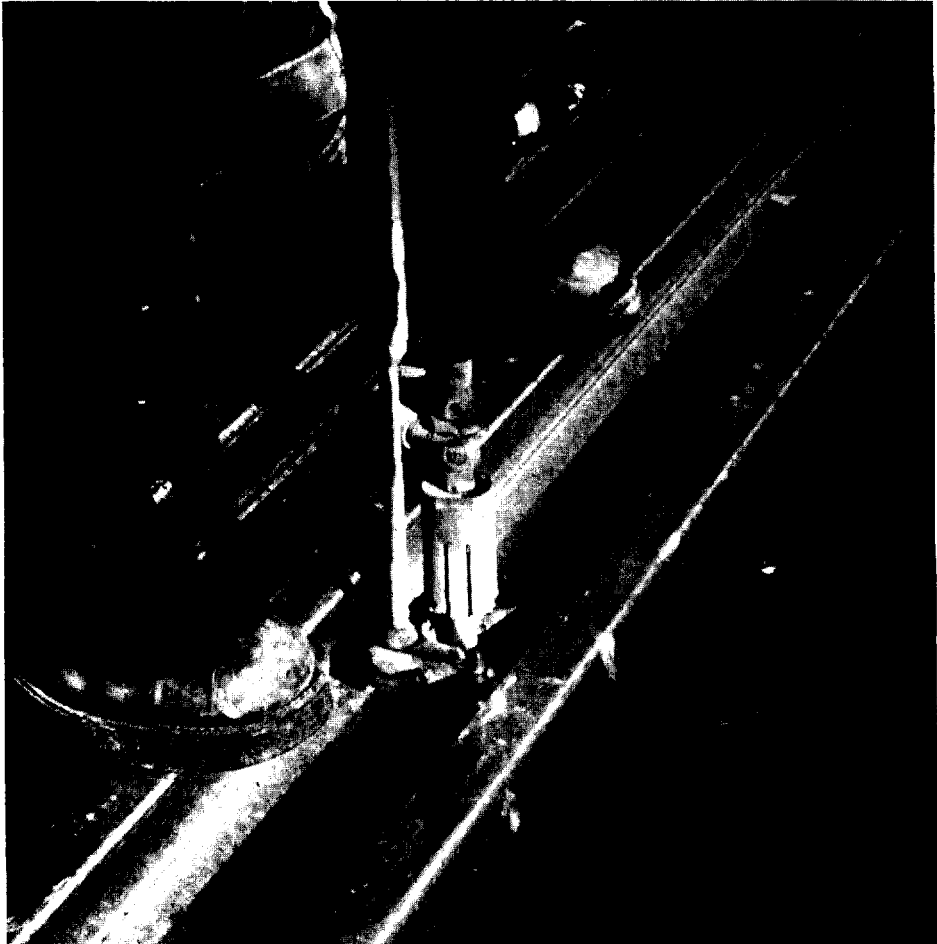
The shear strength of shear-connectors is a function of the concrete strength, connector type and the weld, related to the diameter of the connector. The purpose of the head of the stud is to prevent uplift. The common diameter of stud which can be welded easily on site is 19 mm, supplied in 75 mm, 100 mm or 125 mm heights. The material properties, before forming, are typically:

|                           |                       |
|---------------------------|-----------------------|
| Ultimate tensile strength | 450 N/mm <sup>2</sup> |
| Elongation at failure     | 15%                   |

Higher tensile strengths (495 N/mm<sup>2</sup>) are required in bridge design.<sup>5</sup> Nevertheless, the 'push-out' strength of the shear-connectors is relatively insensitive to the strength of the steel because failure is usually one of the concrete crushing for concrete grades less than 40. Also the weld collar around the base of the shear-connector contributes to increased shear resistance.

The modern method of attaching studs in composite buildings is by through-deck welding. An example of this is shown in Fig. 21.10. The common in situ method of checking the adequacy of the weld is the bend-test, a reasonably easy method of quality control which should be carried out on a proportion of studs (say 1 in 50) and the first 2 to 3 after start up.

Other forms of shear-connector such as the shot-fired connector have been developed (Fig. 21.11). The strength of these types is controlled by the size of the



*Fig. 21.10* Welding of shear-connector through steel decking to a beam

pins used. Typical strengths are 30%–40% of the strengths of welded shear-connectors, but they demonstrate greater ductility.

The static strength data for stud shear-connectors are given in Table 21.4 taken from BS 5400: Part 5 and also incorporated in BS 5950: Part 3. As-welded heights are some 5 mm less than the nominal heights. The strengths of shear-connectors in structural lightweight concrete (density  $> 1750 \text{ kg/m}^2$ ) are taken as 90% of these values.

In Eurocode 4,<sup>8</sup> the approach is slightly different. Empirical formulae are given based on two failure modes; failure of the concrete and failure of the steel. The upper bound strength is given by shear failure of the shank and therefore there is apparently little advantage in using high-strength concrete.

In BS 5950: Part 3 and Eurocode 4, the design capacity of the shear-connectors



Fig. 21.11 Shot-fired shear-connector

**Table 21.4** Characteristic strengths of headed stud shear-connectors in normal weight concrete

| Diameter | Dimensions of stud shear-connectors (mm) |                  | Characteristic strength of concrete ( $\text{N}/\text{mm}^2$ ) |     |     |     |
|----------|--|------------------|--|-----|-----|-----|
|          | Nominal height                           | As-welded height | 25   | 30  | 35  | 40  |
| 25       | 100                                      | 95               | 146  | 154 | 161 | 168 |
| 22       | 100                                      | 95               | 119  | 126 | 132 | 139 |
| 19       | 100                                      | 95               | 95   | 100 | 104 | 109 |
| 19       | 75                                       | 70               | 82   | 87  | 91  | 96  |
| 16       | 75                                       | 70               | 70   | 74  | 78  | 82  |
| 13       | 65                                       | 60               | 44   | 47  | 49  | 52  |

For concrete of characteristic strength greater than  $40 \text{ N}/\text{mm}^2$  use the values for  $40 \text{ N}/\text{mm}^2$

For connectors of heights greater than tabulated use the values for the greatest height tabulated

is taken as 80% of the nominal static strength. Although this may broadly be considered to be a material factor applied to the material strength, it is, more correctly, a factor to ensure that the criteria for plastic design are met (see below). The design capacity of shear-connectors in negative moment regions is taken as 60% of the nominal strength. In BS 5400: Part 5, an additional material factor of 1.1 is introduced to further reduce the design capacity of the shear connectors.

In plastic design, it is important to ensure that the shear-connectors display adequate ductility. It may be expected that shear-connectors maintain their ultimate capacity at displacements of up to 5 mm. A possible exception is where concrete strengths exceed grade 40 as the form of failure may be more brittle.

For beams subject to uniform load, the degree of shear connection that is provided by uniformly-spaced shear-connectors (defined in section 21.7.4) reduces more rapidly than the applied moment away from the point of maximum moment. To ensure that the shear connection is adequate at all points along the beam, the design strength of the shear-connectors is taken as 80% of their static strength. This also partly ensures that flexural failure will occur before shear failure. For beams subject to point loads, it is necessary to design for the appropriate shear connection at each major load point.

In a simple composite beam subject to uniform load the elastic shear flow defining the shear transfer between the slab and the beam is linear, increasing to a maximum at the ends of the beam. Beyond the elastic limit of the connectors there is a transfer of force among the shear-connectors, such that, at failure, each of the shear-connectors is assumed to be subject to equal force, as shown in Fig. 21.12. This is consistent with a relatively high slip between the concrete and the

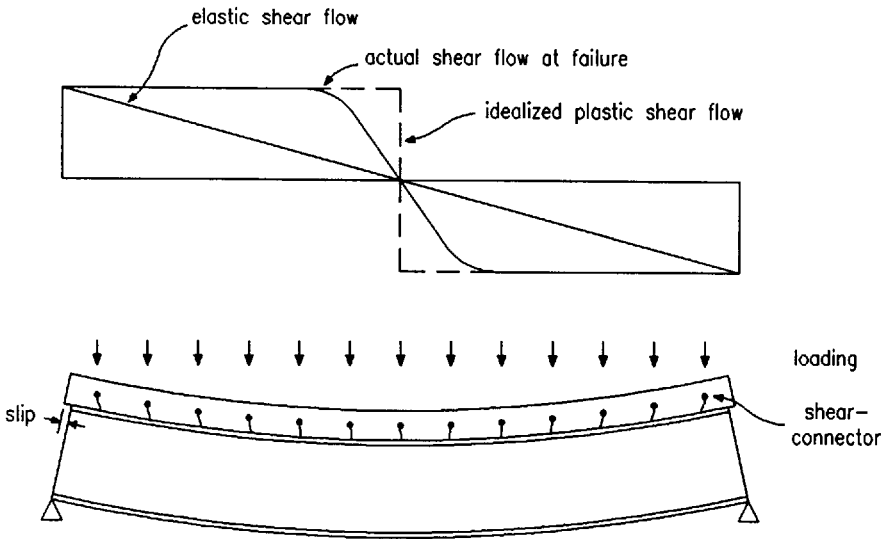


Fig. 21.12 Idealization of forces transferred between concrete and steel

steel. The slip increases as the beam span increases and the degree of shear connection reduces. For this reason BS 5400: Part 5<sup>5</sup> requires that shear-connectors in bridges are spaced in accordance with elastic theory. In building design, shear-connectors are usually spaced uniformly along the beam when the beam is subject to uniform load.

No serviceability limit is put on the force in the shear-connectors, despite the fact that consideration of the elastic shear flow suggests that such forces can be high at working load. This is reflected in the effect of slip on deflections in cases where partial shear connection is used. When designing bridges<sup>5</sup> or structures subject to fatigue loading, a limit of 55% of the design capacity of the shear connectors is appropriate for design at the serviceability limit state.

#### 21.7.4 Partial shear connection

In plastic design of composite beams the longitudinal shear force to be transferred between the concrete and the steel is the lesser of  $R_c$  and  $R_s$ . The number of shear-connectors placed along the beam between the points of zero and maximum positive moment should be sufficient to transfer this force.

In cases where fewer shear-connectors than the number required for full shear connection are provided it is not possible to develop  $M_{pc}$ . If the total capacity of the shear-connectors between the points of zero and maximum moment is  $R_q$  (less than the smaller of  $R_s$  and  $R_c$ ), then the stress block method in section 21.6.2 is modified as follows, to determine the moment capacity,  $M_c$ :

Case 4:  $R_q > R_w$  (plastic neutral axis lies in flange):

$$M_c = R_s \frac{D}{2} + R_q \left[ D_s - \frac{R_q}{R_c} \left( \frac{D_s - D_p}{2} \right) \right] - \frac{(R_s - R_q)^2 T}{R_f 4} \quad (21.11)$$

NB the last term in this expression is generally small.

Case 5:  $R_q < R_w$  (plastic neutral axis lies in web):

$$M_c = M_s + R_q \left[ \frac{D}{2} + D_s - \frac{R_q}{R_c} \left( \frac{D_s - D_p}{2} \right) \right] - \frac{R_q^2 D}{R_w 4} \quad (21.12)$$

The formulae are obtained by replacing  $R_c$  by  $R_q$  and re-evaluating the neutral axis position. The method is similar to that used in the American method of plastic design<sup>10</sup> which predicts a non-linear increase of moment capacity with degree of shear connection  $K$  defined as:

$$K = R_q/R_s \quad \text{for } R_s < R_c \\ \text{or } K = R_q/R_c \quad \text{for } R_c < R_s$$

An alternative approach, which has proved attractive, is to define the moment capacity in terms of a linear interaction of:

$$M_c = M_s + K (M_{pc} - M_s) \quad (21.13)$$

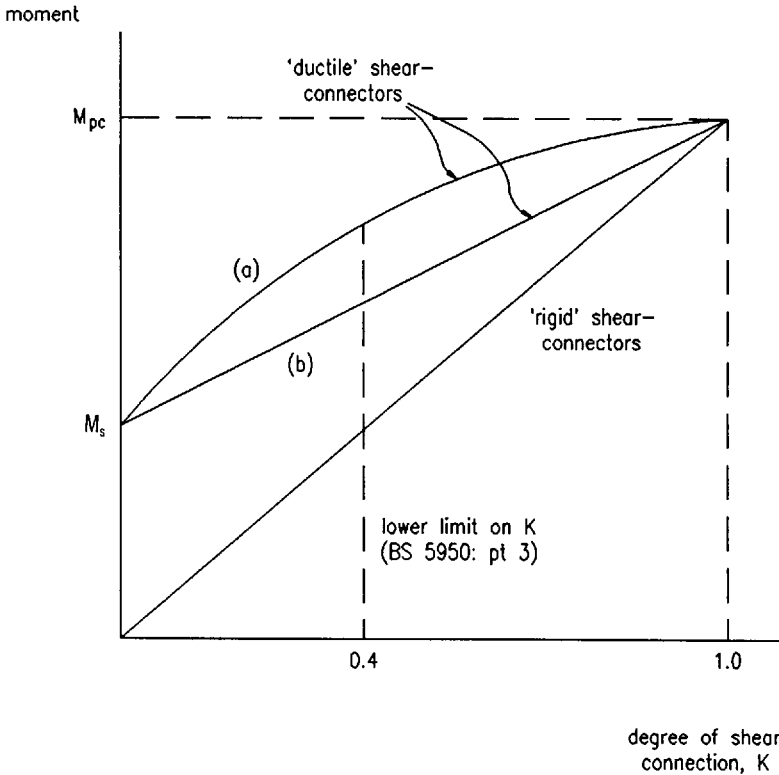


Fig. 21.13 Interaction between moment capacity and degree of shear connection. (a) Stress block method. (b) Linear interaction method

The ‘stress block’ and ‘linear interaction’ methods are presented in Fig. 21.13 for a typical beam. It can be seen that there is a significant benefit in the stress block method in the important range of  $K = 0.5$  to  $0.7$ .

In using methods based on partial shear connection a lower limit for  $K$  of  $0.5$  is specified in Eurocode 4 (draft).<sup>8</sup> This is to overcome any adverse effects arising from the limited deformation capacity of the shear connectors.

In BS 5950: Part 3, the limiting degree of shear connection increases with span ( $L$  in metres) such that:

$$K \leq (L - 6)/10 \geq 0.4 \tag{21.14}$$

This formula means that beams longer than 16 m span should be designed for full shear connection, and beams of up to 10 m span designed for not less than 40% shear connection, with a linear transition between the two cases. Partial shear connection is also not permitted for beams subject to heavy off-centre point loads.

A further requirement is that the degree of shear connection should be adequate at all points along the beam length. For a beam subject to point loads, it follows that



**Table 21.5** Comparison of designs of simply-supported composite beams

| Beam data  | Elastic design                    | Plastic design                     |                              |                          |
|--|-----------------------------------|------------------------------------|------------------------------|--------------------------|
|  |                                   | No connectors<br>(BS 5950: Part 1) | Partial<br>connection        | Full shear<br>connection |
| Full depth (mm)                                  | 536                               | 536                                | 435                          | 435                      |
| Beam size (mm)                                   | 406 × 140                         | 406 × 140                          | 305 × 102                    | 305 × 102                |
| Beam weight (kg/m)                               | 39                                | 46                                 | 33                           | 28                       |
| Number of 19 mm<br>diameter shear-<br>connectors | 50<br>(every trough)              | 0                                  | 25<br>(alternate<br>troughs) | 50<br>(every trough)     |
| Deflection (mm)<br>imposed load                  | 7                                 | 19                                 | 14                           | 13                       |
| Deflection (mm)<br>self-weight                   | 14                                | 11                                 | 25                           | 30                       |
| Beam span:                                       | 7.5 m (unpropped)                 |                                    |                              |                          |
| Beam spacing:                                    | 3.0 m                             |                                    |                              |                          |
| Slab depth:                                      | 130 mm                            |                                    |                              |                          |
| Deck height:                                     | 50 mm                             |                                    |                              |                          |
| Steel grade:                                     | 50 ( $p_y = 355 \text{ N/mm}^2$ ) |                                    |                              |                          |
| Concrete grade:                                  | 30 (normal weight)                |                                    |                              |                          |
| Imposed load:                                    | 5 kN/m <sup>2</sup>               |                                    |                              |                          |

the shear-connectors should be distributed in accordance with the shear force diagram.

Comparison of the method of partial shear connection with other methods of design is presented in Table 21.5. Partial shear connection can result in overall economy by reducing the number of shear-connectors at the expense of a slightly heavier beam than that needed for full shear connection. Elastic design is relatively conservative and necessitates the placing of shear-connectors in accordance with the elastic shear flow. Deflections are calculated using the guidance in section 21.7.8.

### 21.7.5 Influence of deck shape on shear connection

The efficiency of the shear connection between the composite slab and the composite beam may be reduced because of the shape of the deck profile. This is analogous to the design of haunched slabs where the strength of the shear-connectors is strongly dependent on the area of concrete around them. Typically, there should be a 45° projection from the base of the connector to the core of the solid slab to transfer shear smoothly in the concrete without local cracking.

The model for the action of a shear-connector placed in the trough of a deck profile is shown in Fig. 21.14. For comparison also shown is the behaviour of a connector in a solid slab. Effectively, the centre of resistance in the former case moves towards the head of the stud and the couple created is partly resisted by bending of the stud but also by tensile and compressive forces in the concrete, encouraging concrete cracking and consequently the strength of the stud is reduced.

A number of tests on different stud heights and profile shapes have been performed. The following formula has been adopted by most standards worldwide. The strength reduction factor (relative to a solid slab) for the case where the decking crosses the beams is:

$$r_p = \frac{0.85 b_a}{\sqrt{n} D_p} \left( \frac{h - D_p}{D_p} \right) \leq 1.0 \quad \text{for } n = 1$$

$$\leq 0.8 \quad \text{for } n = 2 \quad (21.15)$$

where  $b_a$  is the average width of the trough,  $h$  is the stud height, and  $n$  is the number of studs per trough ( $n < 3$ ). The limit for pairs of studs is given in BS 5950 Part 3 and takes account of less ductile behaviour when  $n > 1$ . This formula does not apply in cases where the shear-connector does not project at

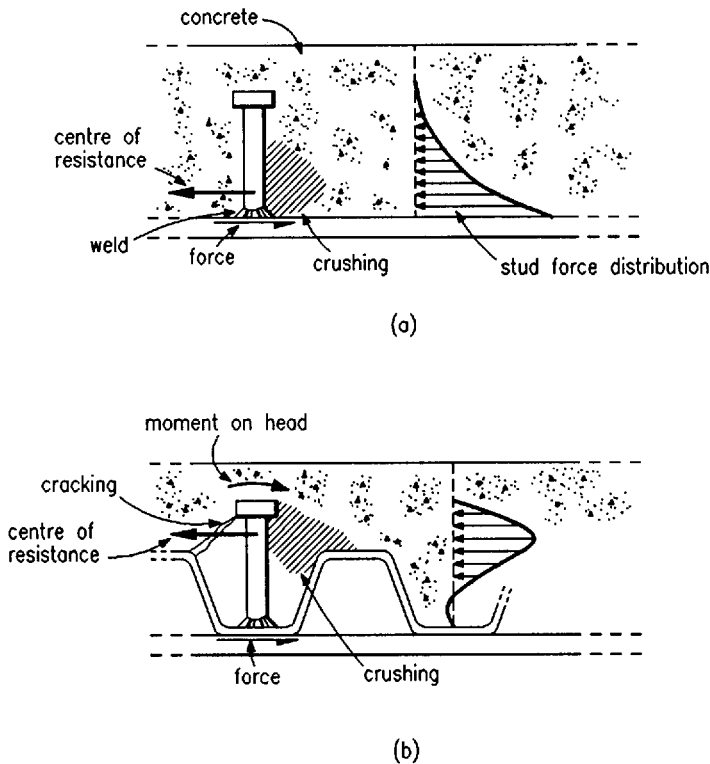


Fig. 21.14 Model of behaviour of shear-connector. (a) Shear-connector in plain slab. (b) Shear-connector fixed through profile sheeting

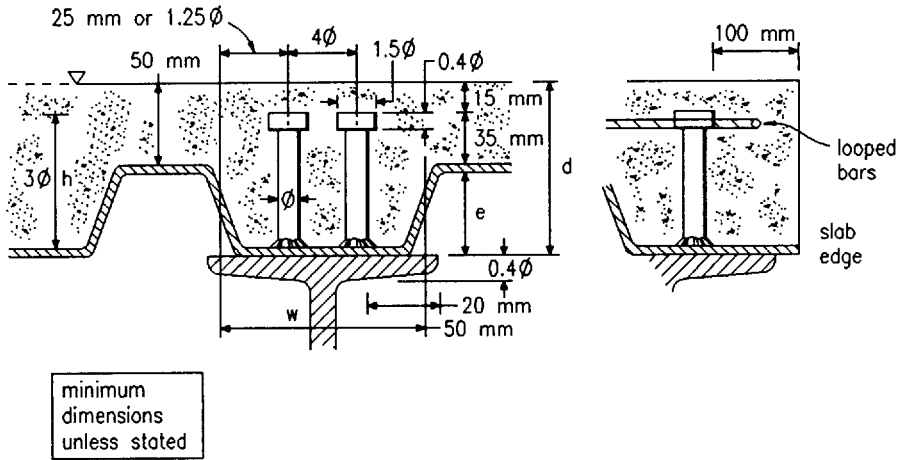


Fig. 21.15 Geometric limits on location of shear-connectors

least 35 mm above the top of the deck. A further limit is that  $h \nlessgtr 2D_p$  in evaluating  $r_p$ .

Where the decking is placed parallel to the beams no reduction is made for the number of connectors but the constant in Equation (21.15) is reduced to 0.6 (instead of 0.85). No reduction is made in the second case when  $b_a/D_p > 1.5$ .

Further geometric limits on the placing of the shear-connectors are presented in Fig. 21.15. The longitudinal spacing of the shear-connectors is limited to a maximum of 600 mm and a minimum of 100 mm.

### 21.7.6 Longitudinal shear transfer

In order to transfer the thrust from the shear-connectors into the slab, without splitting, the strength of the slab in longitudinal shear should be checked. The strength is further influenced by the presence of pre-existing cracks along the beam as a result of the bending of the slab over the beam support.

The design recommendations used to check the resistance of the slab to longitudinal shear are based on research into the behaviour of reinforced concrete slabs. The design shear stress which can be transferred is taken as  $0.9 \text{ N/mm}^2$  for normal weight and  $0.7 \text{ N/mm}^2$  for lightweight concrete; this strength is relatively insensitive to the grade of concrete.<sup>11</sup>

It is first necessary to establish potential planes of longitudinal shear failure around the shear-connectors. Typical cases are shown in Fig. 21.16. The top reinforcement is assumed to develop its full tensile capacity, resisted by an equal and opposite compressive force close to the base of the connector. Both top and bottom reinforcement play an important role in preventing splitting of the concrete.

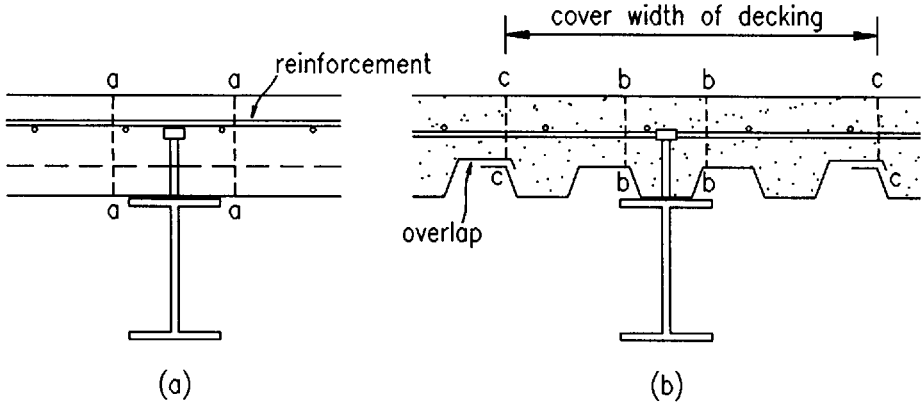


Fig. 21.16 Potential failure planes through slab in longitudinal shear

The shear resistance per unit length of the beam which is equated to the shear force transferred through each shear plane (in the case of normal weight concrete) is:

$$V = 0.9L_s + 0.7A_r f_y \leq 0.15 L_s f_{cu} \tag{21.16}$$

where  $L_s$  is the length of each shear plane considered on a typical cross-section, which may be taken as the mean slab depth in Fig. 21.16(a) or the minimum depth in Fig. 21.16(b). The total area of reinforcement (per unit length) crossing the shear plane is  $A_r$ . For an internal beam, the slab shear resistance is therefore  $2V$ .

The effect of the decking in resisting longitudinal shear is considerable. Where the decking is continuous over the beams, as in Fig. 21.3(a), or rigidly attached by shear-connectors, there is no test evidence of the splitting mode of failure. It is assumed, therefore, that the deck is able to provide an important role as transverse reinforcement. The term  $A_r f_y$  may be enhanced to include the contribution of the decking, although it is necessary to ensure that the ends of the deck (butt joints) are properly welded by shear-connectors. In this case, the anchorage provided by each weld may be taken as  $4\phi t_s p_y$ , where  $\phi$  is the stud diameter,  $t_s$  is the sheet thickness, and  $p_y$  is the strength of the sheet steel. Dividing by the stud spacing gives the equivalent shear resistance per unit length provided by the decking.

Where the decking is laid parallel to the beams, longitudinal shear failure can occur through the sheet-to-sheet overlap close to the line of studs. Failure is assessed assuming the shear force transferred diminishes linearly across the slab to zero at a distance of  $B_c/2$ . Therefore, the effective shear force that is transferred across the longitudinal overlaps is  $(1 - \text{cover width of decking}/\text{effective breadth}) \times \text{shear force}$ . The shear resistance at these points excludes the effect of the decking.

To prevent splitting of the slab at edge beams, the distance between the line of shear-connectors and the edge of the slab should not be less than 100 mm. When this distance is between 100 mm and 300 mm, additional reinforcement in the form of U bars located below the head of the shear-connectors is to be provided.<sup>12</sup> No additional reinforcement (other than that for transverse reinforcement) need be provided where the edge of the slab is more than 300 mm from the shear-connectors.

### 21.7.7 Interaction of shear and moment in composite beams

Vertical shear can cause a reduction in the plastic capacity of a composite beam where high moment and shear co-exist at the same position along the beam (i.e. the beam is subject to one or two point loads). Where the shear force  $F_v$  exceeds  $0.5P_v$  (where  $P_v$  is the lesser of the shear capacity and the shear buckling capacity, determined from Part 1 of BS 5950), the reduced moment capacity is determined from:

$$M_{cv} = M_c - (M_c - M_f) (2F_v/P_v - 1)^2 \quad (21.17)$$

where  $M_c$  is the plastic capacity of the composite section, and  $M_f$  is the plastic capacity of the composite section having deducted the shear area (i.e. the web of the section).

The interaction is presented diagrammatically in Fig. 21.17. A quadratic relationship has been used, as opposed to the linear relationship in BS 5950: Part 1, because of its better agreement with test data, and because of the need for greater economy in composite sections which are often more highly stressed in shear than non-composite beams.

### 21.7.8 Deflections

Deflection limits for beams are specified in BS 5950: Part 1. Composite beams are, by their nature, shallower than non-composite beams and often are used in structures where long spans would otherwise be uneconomic. As spans increase, so traditional deflection limits based on a proportion of the beam span may not be appropriate. The absolute deflection may also be important and pre-cambering may need to be considered for beams longer than 10 m.

Elastic section properties, as described in section 21.6.1, are used in establishing the deflection of composite beams. Uncracked section properties are considered to be appropriate for deflection calculations. The appropriate modular ratio is used, but it is usually found that the section properties are relatively insensitive to the precise value of modular ratio. The effective breadth of the slab is the same as that used in evaluating ultimate strength.

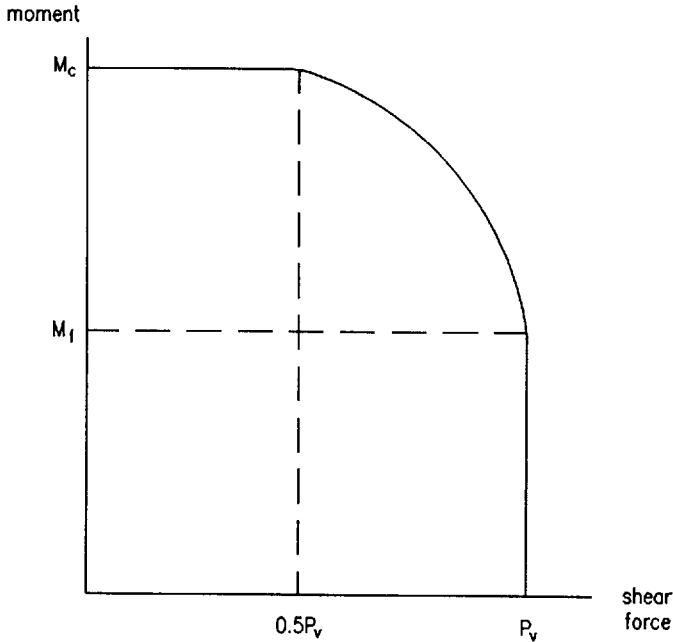


Fig. 21.17 Interaction between moment and shear

The deflection of a simple composite beam at working load, where partial shear connection is used, can be calculated from:<sup>13</sup>

$$\left. \begin{aligned} \delta'_c &= \delta_c + 0.5 (1 - K) (\delta_s - \delta_c) \quad \text{for propped beams} \\ \delta'_c &= \delta_c + 0.3 (1 - K) (\delta_s - \delta_c) \quad \text{for unpropped beams} \end{aligned} \right\} \quad (21.18)$$

where  $\delta_c$  and  $\delta_s$  are the deflections of the composite and steel beam respectively at the appropriate serviceability load;  $K$  is the degree of shear connection used in the determining of the plastic strength of the beam (section 21.7.4). The difference between the coefficients in these two formulae arises from the different shear-connector forces and hence slip at serviceability loads in the two cases. These formulae are conservative with respect to other guidance.<sup>10</sup>

The effect of continuity in composite beams may be considered as follows. The imposed load deflection at mid-span of a continuous beam under uniform load or symmetric point loads may be determined from the approximate formula:

$$\delta_{cc} = \delta'_c (1 - 0.6 (M_1 + M_2)/M_0) \quad (21.19)$$

where  $\delta'_c$  is the deflection of the simply-supported composite beam for the same loading conditions;  $M_0$  is the maximum moment in a simply-supported beam subject to the same loads;  $M_1$  and  $M_2$  are the end moments at the adjacent supports of the span of the continuous beam under consideration.

To determine appropriate values of  $M_1$  and  $M_2$ , an elastic global analysis is carried out using the flexural stiffness of the uncracked section.

For buildings of normal usage, these support moments are reduced to take into account the effect of pattern loading and concrete cracking. The redistribution of support moment under imposed load should be taken as the same as that used at the ultimate limit state (see Table 21.1), but not less than 30%.

For buildings subject to semi-permanent or variable loads (e.g. warehouses), there is a possibility of alternating plasticity under repeated loading leading to greater imposed load deflections. This also affects the design of continuous beams designed by plastic hinge analysis, where the effective redistribution of support moment exceeds 50%. In such cases a more detailed analysis should be carried out considering these effects (commonly referred to as 'shakedown') as follows:

- (1) evaluate the support moments based on elastic analysis of the continuous beam under a first loading cycle of dead load and 80% imposed load (or 100% for semi-permanent load);
- (2) evaluate the excess moment where the above support moment exceeds the plastic capacity of the section under negative moment;
- (3) the net support moments based on elastic analysis of the continuous beam under imposed load are to be reduced by 30% (or 50% for semi-permanent loads) and further reduced by the above excess moment;
- (4) these support moments are input into Equation (21.19) to determine the imposed load deflection.

### 21.7.9 Vibration

Shallower beams imply greater flexibility and although the in-service performance of composite beams and floors in existing buildings is good, the designer may be concerned about the susceptibility of the structure to vibration-induced oscillations. The parameter commonly associated with this effect is the natural frequency of the floor or beams. The damping of the vibration by a bare steel-composite structure is often low. However, when the building is occupied, damping increases considerably.

The lower the natural frequency, the more the structure may respond dynamically to occupant-induced vibration. A limit of 4 Hz (cycles per second) is a commonly accepted lower bound to the natural frequency of each element of the structure. Clearly, vibrating machinery or external vibration effects pose particular problems and in such cases it is often necessary to isolate the source of the vibration.

In practice, the mass of the structure is normally such that the exciting force is very small in comparison leading to the conclusion that long-span structures may respond less than light short-span structures. Guidance is given in Reference 14 and Chapter 12.

### 21.7.10 Shrinkage, cracking and temperature

It is not normally necessary to check crack widths in composite floors in heated buildings, even where the beams are designed as simply-supported, provided that the slab is reinforced as recommended in BS 5950: Part 4 or BS 8110 as appropriate. In such cases crack widths may be outside the limits given in BS 8110, but experience shows that no durability problems arise.

In other cases additional reinforcement over the beam supports may be required to control cracking and the relevant clauses in BS 8110: Part 2<sup>15</sup> and BS 5400: Part 5<sup>5</sup> should be followed. This is particularly important where hard finishes are used.

Questions of long-term shrinkage and temperature-induced effects often arise in long-span continuous composite beams, as they cause additional negative (hogging) moments and deflections. In buildings these effects are generally neglected, but in bridges they can be important.<sup>5,7</sup>

The curvature of a composite section resulting from a free shrinkage (or temperature induced) strain  $\varepsilon_s$  in the slab is:

$$K_s = \frac{\varepsilon_s (D + D_s + D_p) A}{2 (1 + \alpha_c r) I_c} \quad (21.20)$$

where  $I_c$  and  $r$  are defined in section 21.6.1 and  $\alpha_c$  is the appropriate modular ratio for the duration of the action considered. The free shrinkage strain may be taken to vary between  $100 \times 10^{-6}$  in external applications and  $300 \times 10^{-6}$  in dry heated buildings. A creep reduction factor is used in BS 5400: Part 5<sup>5</sup> when considering shrinkage strains. This can reduce the effective strain by up to 50%. The central deflection of a simply-supported beam resulting from shrinkage strain is then  $0.125K_s L^2$ .


### References to Chapter 21

1. British Standards Institution (1990) *Structural use of steelwork in building*. Part 3, Section 3.1: *Code of practice for design of composite beams*. BS 5950, BSI, London.
2. The Steel Construction Institute (SCI) (1989) *Design of Composite Slabs and Beams with Steel Decking*. SCI, Ascot, Berks.
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6. Brett P.R., Nethercot D.A. & Owens G.W. (1987) Continuous construction in steel for roofs and composite floors. *The Structural Engineer*, **65A**, No. 10, Oct.
7. Johnson R.P. & Buckby R.J. (1986) *Composite Structures of Steel and Concrete, Vol. 2: Bridges*, 2nd edn. Collins.
8. Commission of the European Communities (1985) *Eurocode 4: Common unified rules for composite steel and concrete structures*. Report EUR 9886 EN.
9. Yam L.C.P. & Chapman J.C. (1968) The inelastic behaviour of simply supported composite beams of steel and concrete. *Proc. Instn Civ. Engrs*, **41**, Dec., 651–83.
10. American Institute of Steel Construction (1986) *Manual of Steel Construction: Load and Resistance Factor Design*. AISC, Chicago.
11. Johnson R.P. (1975 & 1986) *Composite Structures of Steel and Concrete. Vol. 1: Beams. Vol. 2: Bridges*, 2nd edn. Granada.
12. Johnson R.P. & Oehlers D.J. (1982) Design for longitudinal shear in composite L beams. *Proc. Instn Civ. Engrs*, **73**, Part 2, March, 147–70.
13. Johnson R.P. & May I.M. (1975) Partial interaction design of composite beams. *The Structural Engineer*, **53**, No. 8, Aug., 305–11.
14. Wyatt T.A. (1989) *Design Guide on the Vibration of Floors*. The Steel Construction Institute (SCI)/CIRIA.
15. British Standards Institution (1985) *Structural use of concrete. Part 2: Code of practice for special circumstances*. BS 8110, BSI, London.

A series of worked examples follows which are relevant to Chapter 21.

|   |   |   |                           |
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**Problem**

*Design a composite floor with beams at 3 m centres spanning 12 m. The composite slab is 130 mm deep. The floor is to resist an imposed load of 5.0 kN/m<sup>2</sup>, partition loading of 1.0 kN/m<sup>2</sup> and a ceiling load of 0.5 kN/m<sup>2</sup>. The floor is to be unpropped during construction.*

**Deck:**

- Profile height  $D_p$  = 50 mm*
- Trough spacing = 300 mm*
- Trough width (average) = 150 mm*

**Shear connectors:**

- 19 mm diameter*
- 95 mm as-welded length*


**Concrete:**

- Compressive strength  $f_{cu}$  = 30 N/mm<sup>2</sup>*
- Density (lightweight concrete) is 1800 kg/m<sup>3</sup> (dry)*
- (no extra allowance is made for wet weight - assumed to be included in construction load)*

**Loads:**

- Imposed load = 5.0 kN/m<sup>2</sup>*
- Partitions (imposed load) = 1.0 kN/m<sup>2</sup>*
- Ceiling = 0.5 kN/m<sup>2</sup>*
- Self weight (slab) = 2.00 kN/m<sup>2</sup> }*
- Self weight (beam) = 0.67 kN/m } see later*
- Construction load (temporary) = 0.5 kN/m<sup>2</sup>*

*Finishes and other loads are neglected.*

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Initial selection of beam size

Choose beam depth so that ratio of span/overall depth is about 20

Choose 457 × 191 × 67 kg/m beam steel grade 50

$p_y = 355 \text{ N/mm}^2$  as flange thickness is less than 16 mm

Alternatively, use "Design of Composite Slabs and Beams with Steel Decking".

SCI  
Publication

Construction condition

Self weight of slab (symmetric deck)

$$\text{Self weight} = 105 \times 1800 \times 9.81 \times 10^{-6} = 1.85 \text{ kN/m}^2$$

Self weight of deck is taken as 0.14 kN/m<sup>2</sup>

Total slab weight is 2.0 kN/m<sup>2</sup>

Design load in construction condition

$$= (1.6 \times 0.5 + 1.4 \times 2.0) \times 3.0 + 0.67 \times 1.4$$

$$= 11.74 \text{ kN/m}$$

Design moment in construction condition

$$= 11.74 \times 12.0^2/8 = 211.0 \text{ kNm}$$

Moment resistance of steel section

$$M_s = 1470 \times 10^3 \times 355 \times 10^{-6}$$

$$= 521.9 \text{ kNm} > 211.0 \text{ kNm}$$

(the beam is assumed to be laterally restrained by the decking)

Check stress due to self weight


$$\text{Moment} = (2.0 \times 3.0 + 0.67) \times 12^2/8$$

$$= 120.1 \text{ kNm}$$

$$\text{Bending stress} = \frac{120.1 \times 10^6}{1300 \times 10^3} = 92 \text{ N/mm}^2$$

Deflection of soffit of beam after construction

$$\delta = \frac{5}{384} \times \frac{(2.0 \times 3.0 + 0.67) \times 12000^4}{205 \times 10^3 \times 29400 \times 10^4}$$

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***Composite condition - ultimate load***

***Factored load on composite beam***

$$\begin{aligned}
 w_u &= (5.0 \times 1.6 + 1.0 \times 1.6 + 0.5 \times 1.4 + 2.0 \times 1.4) \times 3.0 + 0.67 \times 1.4 \\
 &= 40.2 \text{ kN/m}
 \end{aligned}$$

***Design moment on composite beam***

$$M_u = \frac{40.2 \times 12^2}{8} = 723.6 \text{ kNm}$$

***Effective breadth of slab***

$$B_e = 12000/4 = 3000 \text{ mm} \quad \neq b = 3000 \text{ mm}$$

***Resistance of slab in compression***

$$\begin{aligned}
 R_c &= 0.45 f_{cu} B_e (D_s - D_p) \\
 &= 0.45 \times 30 \times 3000 \times (130 - 50) \times 10^{-3} \\
 &= 3240 \text{ kN}
 \end{aligned}$$


***Resistance of steel section in tension***

$$\begin{aligned}
 R_s &= A p_y \\
 &= 8540 \times 355 \times 10^{-3} \\
 &= 3032 \text{ kN}
 \end{aligned}$$

As  $R_c > R_s$  plastic neutral axis lies in concrete.

***Moment resistance of composite beam (equation 21.6) for full shear connection is:***

$$\begin{aligned}
 M_{pc} &= R_s \left[ \frac{D}{2} + D_s - \frac{R_s}{R_c} \frac{(D_s - D_p)}{2} \right] \quad \text{for } R_s \leq R_c \\
 &= 3032 \left\{ \frac{453.6}{2} + 130 - \frac{3032}{3240} \times \frac{80}{2} \right\} \times 10^{-3} \\
 &= 968.3 \text{ kNm} > M_u
 \end{aligned}$$

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**Degree of shear connection**

Use two shear connectors per trough  
(i.e. 2 per 300 mm spacing)

$$\text{Number of shear connectors in half span} = \frac{6000}{150} = 40$$

Resistance of shear connector:

From Table 21.4, characteristic strength = 100 kN

Design strength =  $0.8 \times 100 = 80$  kN

For lightweight concrete multiply by 0.9

Design strength (LWC) =  $0.9 \times 80 = 72$  kN

Reduction factor for profile shape (equation 21.15)

$$r = \frac{0.85}{\sqrt{2}} \times \frac{150}{50} \times \frac{(95 - 50)}{50} = 1.62 > 0.8$$


Therefore use  $r = 0.8$  for pairs of shear connectors as required in BS 5950: Part 3 Clause 5.4.7.2.

Total resistance of shear connectors

$$R_q = 0.8 \times 72 \times 40 = 2304 \text{ kN}$$

As  $R_q < R_s$  and  $R_q < R_c$

redesign beam for partial shear connection.

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**Moment resistance of composite beam with partial shear connection (equation 21.11)**

**Tensile resistance of web**

$$R_w = 8.5 \times (453.6 - 2 \times 12.7) \times 355 \times 10^{-3}$$

$$= 1292 \text{ kN}$$

As  $R_q > R_w$ , plastic neutral axis lies in steel flange

$$M_c = R_s \frac{D}{2} + R_q \left[ D_s - \frac{R_q}{R_c} \frac{(D_s - D_p)}{2} \right] - \frac{(R_s - R_q)^2}{R_f} \frac{T}{4}$$

(normally the final term can be ignored)

$$M_c = 3032 \times \frac{453.6}{2} \times 10^{-3} + 2304 \times \left[ 130 - \frac{2304}{3240} \times \frac{80}{2} \right] \times 10^{-3}$$

$$- \frac{(3032 - 2304)^2}{(3032 - 1292) \times 0.5} \times \frac{12.7}{4} \times 10^{-3}$$

$$= 687.6 + 234.0 - 1.9 = 919.7 \text{ kNm} > 723.6 \text{ kNm}$$

**Degree of shear connection provided**

$$K = R_q / R_s = 2304 / 3032 = 0.76$$


**Check possibility of providing fewer shear connectors. Limit on degree of shear connection is:**

$$K \geq \frac{L - 6}{10}; \quad \text{but } K \geq 0.4$$

For  $L = 12 \text{ m}$                        $K \geq 0.6$

One shear connector every trough (i.e. 300 mm spacing) corresponds to  $K = 0.47 < 0.6$

which does not provide adequate shear connection.

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Composite condition - service load

Determine elastic section properties

Modular ratio  $\alpha_e = 15$  for LWC (see Table 21.3)

Elastic neutral axis depth (equation 21.1):

$$x_e = \frac{\frac{D_s - D_p}{2} + \alpha_e r \left[ \frac{D}{2} + D_s \right]}{(1 + \alpha_e r)}$$

where  $r = \frac{A}{(D_s - D_p) B_e} = \frac{8540}{80 \times 3000} = 0.0355$

$$x_e = \frac{\frac{80}{2} + 0.0355 \times 15 \times \left[ \frac{453.6}{2} + 130 \right]}{(1 + 0.0355 \times 15)}$$

= 150.1 mm below top of slab

Second moment of area (equation 21.2):

$$I_c = \frac{A (D + D_s + D_p)^2}{4 (1 + \alpha_e r)} + \frac{B_e (D_s - D_p)^3}{12 \alpha_e} + I_s$$

$$= \frac{8540 (453.6 + 130 + 50)^2}{4 (1 + 0.0355 \times 15)} + \frac{3000 \times 80^3}{12 \times 15} + 294 \times 10^6$$


=  $861.8 \times 10^6 \text{ mm}^4$

Elastic section modulus - steel flange (equation 21.3)

$$Z_t = \frac{861.8 \times 10^6}{(453.6 + 130 - 150.1)} = 1.98 \times 10^6 \text{ mm}^3$$

Elastic section modulus - concrete (equation 21.4)

$$Z_c = \frac{861.8 \times 10^6}{150.1} \times 15 = 86.1 \times 10^6 \text{ mm}^3$$

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**Service load on composite section**

$$= (5.0 + 1.0 + 0.5) \times 3.0 = 19.5 \text{ kN/m}$$

**Service moment**

$$= 19.5 \times 12^2/8 = 351 \text{ kNm}$$

**Stress in steel**

$$= \frac{351 \times 10^6}{1.98 \times 10^6} = 177 \text{ N/mm}^2$$

**Additional stress on non-composite section**

$$= 92 \text{ N/mm}^2$$

**Total serviceability stress**

$$= 177 + 92 = 269 \text{ N/mm}^2 < p_y$$

**Stress in concrete**

$$= \frac{351 \times 10^6}{86.1 \times 10^6} = 4.1 \text{ N/mm}^2 < 0.5 f_{cu}$$

**Deflection - imposed load**

**Imposed load**

$$= (5.0 + 1.0) \times 3.0 = 18.0 \text{ kN/m}$$

**Deflection**  $\delta_c$

$$= \frac{5}{384} \times \frac{18.0 \times 12000^4 \times 10^{-3}}{205 \times 10^3 \times 861.8 \times 10^6}$$

$$\delta_c = 27.5 \text{ mm}$$

**Additional deflection from partial shear-connection (equation 21.18)**

$$\delta_s = \frac{861.8}{294.0} \times 27.5 = 80.6 \text{ mm}$$

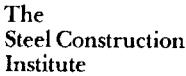
$$\delta_c^I = \delta_c + 0.3 (1 - K) (\delta_s - \delta_c)$$

$$= 27.5 + 0.3 (1 - 0.76) (80.6 - 27.5)$$

$$= 31.3 \text{ mm (span/383)}$$

**Deflection is the limiting criterion.**  
 It would be possible to show that the imposed load could be increased to 6 kN/m<sup>2</sup> for the same beam size.



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Check natural frequency of beam

Consider weight of floor in dynamic calculations to include: self weight of slab and beam + 10% imposed load + ceiling load but excluding partitions

$$= (2.0 + 0.1 \times 5.0 + 0.5) \times 3.0 + 0.67 = 9.67 \text{ kN/m}$$

Accurate calculations show that the ratio of the dynamic to static stiffness of a composite beam used in deflection calculations is 1.1 to 1.15. Consider deflection reduction of 1.1 for the same section properties as calculated under imposed load.

Deflection of composite beam, when subject to instantaneously applied self weight (as above)


$$\delta_{sw} = \frac{5 \times 9.67 \times 12^4 \times 10^3}{384 \times 205 \times 10^6 \times 1.1 \times 861.8 \times 10^{-6}}$$

$$= 13.4 \text{ mm}$$

Natural frequency of beam

$$f \approx 18 / \sqrt{\delta_{sw}} = 18 / \sqrt{13.4} = 4.91 \text{ Hz Satisfactory}$$

(A detailed check to Reference 21.14 demonstrates that this floor is satisfactory for general office use).

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Use same design data as for simply - supported composite beams.

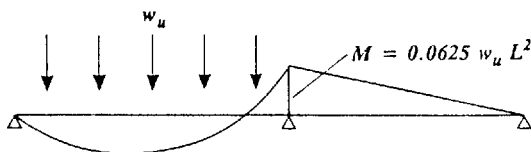
Choose  $406 \times 178 \times 60$  kg/m UB grade 50 - N.B. Section is plastic.  
(span/depth ratio = 22, and 12% weight saving).

Construction condition

Design load in construction condition

$$w_u = (1.6 \times 0.5 + 1.4 \times 2.0) \times 3.0 + 0.60 \times 1.4 = 11.6 \text{ kN/m}$$

Check stability of bottom flange under worst combination of loading



$$M = 0.0625 \times 11.6 \times 12^2 = 104.4 \text{ kNm}$$

Consider effective length as  $0.85 L = 0.85 \times 12000 = 10200$  mm

$$\text{Slenderness } \lambda = 10200/39.7 = 257$$

Slenderness correction factor for shape of bending moment diagram (linear) is obtained from Table 20 of BS 5950: Part 1.

From SCI publication 'Steelwork Design: Guide to BS 5950: Part 1: Volume 1' (page 29)


$$u = 0.882 \quad x = 33.9$$

Assume top flange is laterally restrained by the decking. Use design formula for effective slenderness in BS 5950: Part 1 (Appendix G3.3).

$$\lambda_{LT} = n u v_t \lambda \quad \text{where } v_t = \left[ \frac{\frac{4a}{d}}{1 + \left[ \frac{2a}{d} \right]^2 + \frac{1}{20} \left[ \frac{\lambda}{x} \right]^2} \right]^{0.5}$$

and  $a$  = distance of restraint above shear centre of beam (=  $d/2$  in this case)

$d$  = clear web depth

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Hence:

$$v_t = \left[ \frac{1}{1 + \frac{1}{40} \left( \frac{\lambda}{x} \right)^2} \right]^{0.5} = \left[ \frac{1}{1 + \frac{1}{40} \left( \frac{257}{33.9} \right)^2} \right]^{0.5} = 0.64$$

$$\lambda_{LT} = 0.77 \times 0.882 \times 0.64 \times 257 = 112$$

From Table 11 of BS 5950: Part 1, bending strength

$$p_b = 122 \text{ N/mm}^2$$

Buckling resistance moment

$$\begin{aligned} M_b &= 122 \times 1194 \times 10^3 \times 10^{-6} \\ &= 145.6 \text{ kNm} > 104.4 \text{ kNm i.e. stable during construction} \end{aligned}$$

Maximum negative (hogging) moment

$$= 0.125 w_u L^2 = 208.8 \text{ kNm}$$

Plastic moment resistance of steel section

$$\begin{aligned} &= 355 \times 1194 \times 10^3 \times 10^{-6} \\ &= 423.9 \text{ kNm} > 208.8 \text{ kNm} \end{aligned}$$

Hence, the steel beam can support the loads during construction.

Moment in mid-span of two span beam after construction


$$= 0.0703 \times (2.0 \times 3.0 + 0.6) \times 12^2 = 66.8 \text{ kNm}$$

Bending stress (elastic)

$$= \frac{66.8 \times 10^6}{1058 \times 10^3} = 63 \text{ N/mm}^2$$

Deflection of underside of beam after construction

$$\begin{aligned} \delta_o &= \frac{2.1 \times (2.0 \times 3.0 + 0.6) \times 12000^4}{384 \times 205 \times 10^3 \times 21508 \times 10^4} \\ &= 17.0 \text{ mm (span/706)} \end{aligned}$$

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***Composite condition - ultimate loading***

***Factored loading on composite beam***

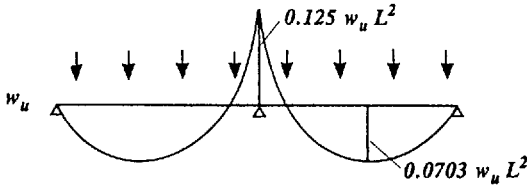
$$\begin{aligned}
 w_u &= [(5.0 + 1.0) \times 1.6 + (0.5 + 2.0) \times 1.4] \times 3.0 + 0.6 \times 1.4 \\
 &= 40.1 \text{ kN/m}
 \end{aligned}$$

***Design moment on composite beam***

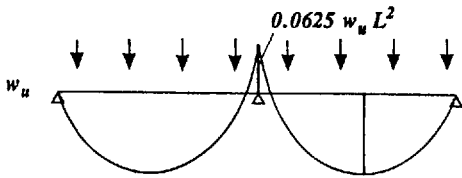
***Ratio of imposed load: dead load***

$$= \frac{5.0 + 1.0}{2.0 + 0.5 + 0.6/3.0} = 2.22 > 2$$

*Therefore, the use of Table 21.2 is not permitted. However, calculate moments from pattern load cases as follows:*

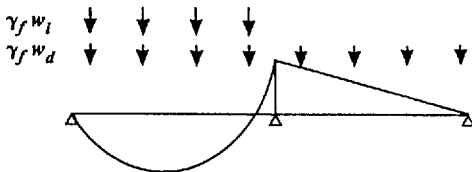


*No redistribution*




*50% redistribution*

$$\begin{aligned}
 &(0.0703 + 0.032) w_u L^2 \\
 &= 0.103 w_u L^2 \\
 &\text{(accurate value} = 0.096 w_u L^2)
 \end{aligned}$$



*Imposed load on one span; dead load on both spans*

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*The section is 'plastic' when grade 50 steel is used. According to Table 21.1, 50% redistribution of the negative (hogging) moment can be made provided the slab has nominal reinforcement.*

**Negative moment** =  $0.0625 \times 40.1 \times 12^2$   
= 360.9 kNm

**Positive moment** =  $0.096 \times 40.1 \times 12^2$   
= 554.3 kNm (50% redistribution)

*Alternatively, single span loading gives:*

**Positive (sagging) moment**

$$= \{0.096 \times 1.6 \times (5.0 + 1.0) \times 3.0 + 0.070 \times 1.4 \times [(2.0 + 0.5) \times 3.0 + 0.6]\} \times 12^2$$

= 512.4 kNm

**Plastic moment resistance of steel section**

$$= 355 \times 1194 \times 10^3 \times 10^{-6}$$

= 423.9 kNm > 360.9 kNm


*This exceeds the design moment. It may be shown that 42% redistribution of moment is adequate. Check moment resistance of composite section.*

**Moment resistance of composite section**

**Effective breadth of slab (for internal span)**

$$B_e = 0.7 \times 12000/4 = 2100 \text{ mm } \nlessdot \text{ beam spacing}$$

*(note 0.7 has been used for internal span, rather than 0.8 for external span)*

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*Resistance of slab in compression*

$$\begin{aligned}
 R_c &= 0.45 f_{cu} B_e (D_s - D_p) \\
 &= 0.45 \times 30 \times 2100 \times (130 - 50) \times 10^{-3} \\
 &= 2268 \text{ kN}
 \end{aligned}$$

*Resistance of steel section in tension*

$$\begin{aligned}
 R_s &= A p_y = 7600 \times 355 \times 10^{-3} \\
 &= 2698 \text{ kN}
 \end{aligned}$$

As  $R_s > R_c$ , plastic neutral axis lies in steel flange

*Plastic moment resistance of composite section*

$$M_{pc} = R_s \frac{D}{2} + R_c \frac{(D_s + D_p)}{2} - \left[ \frac{(R_s - R_c)^2}{R_f} \times \frac{T}{4} \right]$$


where  $R_f = 12.8 \times 177.8 \times 355 \times 10^{-3}$

$$\begin{aligned}
 &= 808 \text{ kN}
 \end{aligned}$$

*The final term is small and may be neglected*

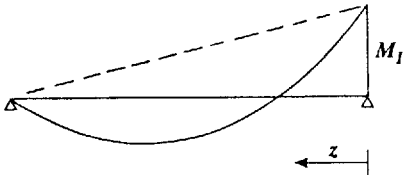
$$\begin{aligned}
 M_{pc} &= \left[ 2698 \times \frac{406.4}{2} + 2268 \times \frac{(130 + 50)}{2} - \frac{(2698 - 2268)^2}{808} \times \frac{12.8}{4} \right] \times 10^{-3} \\
 &= 548.2 + 204.1 - 0.7 \\
 &= 751.6 \text{ kNm} > 554.3 \text{ kNm}
 \end{aligned}$$

As there is sufficient reserve in the composite section, consider reducing the amount of shear connectors.

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**Partial shear connection**

**Zone of beam subject to positive (sagging) moment**



$$M = 0; \text{ when } z = L \left[ \frac{2 M_1}{w_u L^2} \right]$$

If  $M_1 = 0.0625 w_u L^2$  (after redistribution)

$z = L/8$

**Zone of beam from point of zero to max. positive moment = 0.43 L**

**Use two shear connectors every 300 mm**

$$\text{Number of shear connectors} = \frac{0.43 \times 12000 \times 2}{300} = 34$$

**Resistance of one shear connector in LWC**

(see simple beam calculations) = 72 kN


$$R_q = 0.8 \times 72 \times 34 = 1958 \text{ kN}$$

**Degree of shear connection ( $R_c < R_s$ )**

$$K = 1958/2268 = 0.86$$

**Minimum shear connection**

$$K > \frac{L - 6}{10} = 0.6 < 0.86 \quad \text{OK}$$

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| BS5950: Parts 1 & 3  |   | Checked by                                 | GWO |              |

As  $R_q > R_w$ ; plastic neutral axis lies in steel flange

*Plastic moment resistance of section*

$$M_c = R_s \frac{D}{2} + R_q \left[ D_s - \frac{R_q}{R_c} \frac{(D_s - D_p)}{2} \right]$$

$$\begin{aligned}
 M_c &= \left\{ 2698 \times \frac{406.4}{2} + 1958 \left[ 130 - \frac{1958}{2268} \frac{(130 - 50)}{2} \right] \right\} \times 10^{-3} \\
 &= 548.2 + 186.9 \\
 &= 735.1 \text{ kNm} > 554.3 \text{ kNm}
 \end{aligned}$$

Vertical shear resistance

*Shear resistance (to BS 5950: Part 1, Clause 4.2.6)*

$$\begin{aligned}
 P_v &= 0.6 \times 355 \times 406.4 \times 7.8 \times 10^{-3} \\
 &= 675.2 \text{ kN}
 \end{aligned}$$


*Applied shear force at internal support*

$$\begin{aligned}
 F_v &= w_u \frac{L}{2} + \frac{M_I}{L} \\
 &= 1.25 \left[ \frac{w_u L}{2} \right] \\
 &= 1.25 \times 40.1 \times 12/2 = 300.7 \text{ kN}
 \end{aligned}$$

$$F_v = 0.45 P_v < 0.5 P_v$$

*So no reduction in moment resistance is necessary.*



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Composite condition - service loading

Determine elastic section properties under positive moment

Elastic neutral axis depth

$$x_e = \frac{\frac{D_s - D_p}{2} + \alpha_e r \left[ \frac{D}{2} + D_s \right]}{1 + \alpha_e r}$$

Take  $\alpha_e = 15$  for LWC

$$r = \frac{A}{(D_s - D_p) B_e} + \frac{7600}{(130 - 50) 2100} = 0.045$$

$$x_e = \frac{\left[ \frac{80}{2} + 0.045 \times 15 \times \left[ \frac{406.4}{2} + 130 \right] \right]}{(1 + 0.045 \times 15)}$$

$$= 158.1 \text{ mm}$$

Second moment of area of section (equation 21.2)

$$I_c = \frac{A(D + D_s + D_p)^2}{4 (1 + \alpha_e r)} + \frac{B_e (D_s - D_p)^3}{12 \alpha_e} + I_x$$

$$= \left[ \frac{7600 (406.4 + 130 + 50)^2}{4 (1 + 0.045 \times 15)} + \frac{2100 \times (130 - 50)^3}{12 \times 15} + 215.1 \right] \times 10^6$$


$$= (390.0 + 6.0 + 215.1) \times 10^6$$

$$= 611.1 \times 10^6 \text{ mm}^4$$

Elastic section modulus - steel flange (equation 21.3)

$$Z_t = \frac{611.1 \times 10^6}{(406.4 + 130 - 158.1)}$$

$$= 1.62 \times 10^6 \text{ mm}^3$$

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*Service load on composite section*

$$= (5.0 + 1.0 + 0.5) \times 3 = 19.5 \text{ kN/m}$$

*Mid span moment for serviceability conditions should take into account 'shakedown effects' as degree of moment redistribution at ultimate loads exceeds 30%.*

*Shakedown load = Dead load + 80% Imposed load*

$$\begin{aligned} w_s &= [2.0 + 0.5 + 0.8 \times (5.0 + 1.0)] \times 3 + 0.6 \\ &= 22.5 \text{ kN/m} \end{aligned}$$

*Shakedown moment (elastic negative (hogging) moment)*

$$\begin{aligned} &= 0.125 w_s L^2 = 0.125 \times 22.5 \times 12^2 \\ &= 405 \text{ kNm} \end{aligned}$$

*This is less than the plastic moment resistance of the beam (= 423.9 kNm), so no plastification occurs at working load.*

*Service moment under imposed loading on all spans (allowing for 30% redistribution of negative moment)*

$$\begin{aligned} &= (0.0703 + 0.15 \times 0.125) \times 19.5 \times 12^2 \\ &= 250.0 \text{ kNm} \end{aligned}$$

*Steel stress (lower flange)*

$$= \frac{250.0 \times 10^6}{1.62 \times 10^6} = 154 \text{ N/mm}^2$$


*Additional stress in steel beam arising from self weight of floor*

$$= 63 \text{ N/mm}^2$$

$$\text{Total stress} = 63 + 154 = 217 \text{ N/mm}^2 < p_y$$

*Concrete stress*

$$= \frac{250 \times 10^6}{611.1 \times 10^6} \times \frac{158.1}{15} = 4.3 \text{ N/mm}^2 < 0.5 f_{cu}$$

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**Deflection - imposed loading**

*Imposed loading*  $w_i = (5.0 + 1.0) \times 3 = 18.0 \text{ kN/m}$

*Free moment*  $M_o = w_i L^2/8 = 18.0 \times 12^2/8 = 324 \text{ kNm}$

*Negative (hogging) moment* = 324 kNm for a two span beam

According to section 21.7.8, reduce negative moment by 30% to represent the effects of pattern loading

$M_1 = 0.7 \times 324 = 226.8 \text{ kNm}$

$M_2 = 0$

*Deflection of simply supported beam*

$$\delta_o = \frac{5 \times 18.0 \times 12^4 \times 10^3}{384 \times 205 \times 10^6 \times 611.1 \times 10^{-6}} = 38.8 \text{ mm}$$


Allowing for partial shear connection  $K = 0.86$

*Deflection of steel beam*  $\delta_s = \frac{611.1}{215.1} \times 38.8 = 110.2 \text{ mm}$

*Modified deflection*  $\delta_o' = \delta_o + 0.3 (1 - K) \delta_s = 38.8 + 0.3 \times (1 - 0.86) \times 110.2 = 43.4 \text{ mm}$

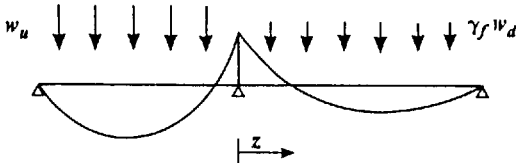
*Deflection of continuous beam*

$$\delta_c = \delta_o \left[ 1 - 0.6 \frac{(M_1 + M_2)}{M_o} \right] = 43.4 \left[ 1 - 0.6 \times \frac{226.8}{324} \right] = 25.2 \text{ mm} \quad (\text{span}/476) \text{ Satisfactory}$$

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### Stability of bottom flange

Check the stability of the bottom flange in the negative (hogging) moment region. The worst case for instability is when only one span is loaded:



$$\text{Negative moment} = 0.0625 (w_u + \gamma_f w_d) L^2$$

$$\gamma_f w_d = 1.4 [ (2.0 + 0.5)3 + 0.6 ] = 11.3 \text{ kN/m}$$

$$w_u = 40.1 \text{ kN/m}$$

$$\begin{aligned} \text{Negative moment} &= 0.0625 (40.1 + 11.3) 12^2 \\ &= 462.6 \text{ kNm} \end{aligned}$$


This exceeds the plastic resistance moment of the beam,  
 $M_p = 423.9 \text{ kNm}$

Use this moment  $M_p$  at the support

$$M = 0 \quad \text{when } z = L \left[ \frac{2 \times M_p}{\gamma_f w_d L^2} \right]$$

$$z = 12 \left[ \frac{2 \times 423.9}{11.3 \times 12^2} \right] = 6.3 \text{ m}$$

It is necessary to introduce an additional lateral restraint close to the support such that  $\lambda_{LT} < 30$  for grade 50 steel.

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The distortional restraint provided by the web has been neglected. However, it is reasonable to take:

$$n = 0.95; \quad u = 0.88; \quad v_t = 0.9$$

$$\text{such that } \lambda_{max} = \frac{30}{0.95 \times 0.88 \times 0.9} = 39.9$$

$$\text{and } L_{max} = 39.9 \times 39.7 = 1582 \text{ mm}$$

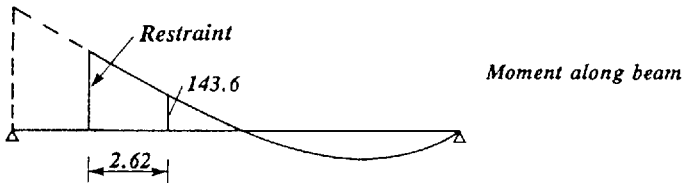
(say 1500 mm)

Check the stability of the remaining portion of the beam

Moment at the above position

$$\approx \frac{(6.2 - 1.5)}{6.2} \times 423.9 = 321.3 \text{ kNm}$$

From Appendix G3.6, it is possible to evaluate an effective value of  $n$  as follows:




$$n = \left[ \frac{1}{12} \left( \frac{321.3}{423.0} + 3 \times \frac{143.6}{423.9} \right) \right]^{0.5} = 0.38$$

BS 5950:  
Part 1  
G.3.6.1.

$$\lambda = \frac{10500}{39.7} = 264$$

$$v_t = \frac{1}{\left[ 1 + \frac{1}{40} \left( \frac{\lambda}{x} \right)^2 \right]^{0.5}}$$

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$$v_t = \left[ 1 + \frac{1}{40} \left( \frac{264}{33.9} \right)^2 \right]^{-0.5} = 0.63$$

$$\lambda_{LT} = 0.38 \times 0.88 \times 0.63 \times 264 = 56$$

*Buckling resistance moment* **BS 5950:  
Part 1  
4.3.7.3**

$$M_b = 271 \times 1194 \times 10^3 \times 10^{-6} = 323.6 \text{ kNm} > 321.3 \text{ kNm}$$

*So adequate restraint is provided by a single lateral restraint 1.5 m from the internal support. This is done by introducing a web stiffener at this point.*

Check natural frequency of beam


*To calculate the natural frequency of a continuous beam it is necessary to consider the mode shape of vibration. Because of the influence of the asymmetric inertial forces, the natural frequency is taken as the same as for a simply supported beam.*

*Considering the same loads as previously:*

$$\delta_{sw} = \frac{5 \times 9.67 \times 12^4 \times 10^3}{384 \times 205 \times 10^6 \times 1.1 \times 611.1 \times 10^{-6}} = 18.9 \text{ mm}$$

$$\text{Natural frequency} = 18/\sqrt{\delta_{sw}} = 18/\sqrt{18.9} = 4.1 \text{ Hz}$$

*However, when carrying out the full Response Factor analysis of Reference (21.14), account can be taken of the effective mass of both spans, thus reducing the amplitude of the vibration from a given excitation. This reduces the sensitivity of the floor to vibration.*

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|  | <p>Design code</p> <p><b>BSS950: Parts 1 &amp; 3</b></p>         | <p>Made by <b>RML</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>14</b></p>           |

**Conclusion:**

*The design using a 406 × 178 × 60 kg/m UB is adequate. However, reducing the section to 406 × 178 × 54 kg/m would not result in an acceptable design because this section is 'compact' in grade 50 steel. Consequently, only 40% redistribution of support moment is permitted and design is limited by the moment resistance of the steel section at the supports.*

## Chapter 22

# Composite columns

by MARK LAWSON and PETER WICKENS

### 22.1 Introduction

#### 22.1.1 Form of construction

Composite columns comprise steel sections with a concrete encasement or core. Encased columns usually consist of standard I-beam or column sections with a rectangular or square concrete section cast around them to form a solid composite section. Additional reinforcement is placed in the concrete cover around the steel section in order to prevent spalling under axial stress.

Concrete-filled columns consist of circular, square or rectangular hollow sections filled with concrete. Additional reinforcement is not normally required except in columns of large section. Examples of these different types of composite columns are shown in Fig. 22.1.

The steel structure is normally constructed in advance of the formation of the composite section. The minimum size of the steel element is therefore controlled by the construction condition. For practical reasons it is normally necessary to fill the tubular sections shortly after their erection but I-sections can be encased much later. However, there are practical problems in concreting around a column with the floors in place. Alternatively, columns can be pre-encased in the factory and in situ concrete used to fill the zone around the beam-column connections.

#### 22.1.2 Advantages of composite columns

In many cases of design, concrete or some other protective material is needed around steel columns for reasons of fire-resistance and durability. It would seem appropriate, therefore, to develop composite action between the steel and concrete, thereby taking advantage of the inherent compressive strength of the concrete, increasing the capacity of the section and leading to considerable savings in the cost of the steelwork. Even ignoring this composite action, the slenderness of the steel column in lateral buckling is reduced, thereby increasing the compressive stress that can be resisted by the steel section.

Much research has gone into the behaviour of concrete-filled tubular sections. Architecturally, tubular columns have many attractive features; concrete filling



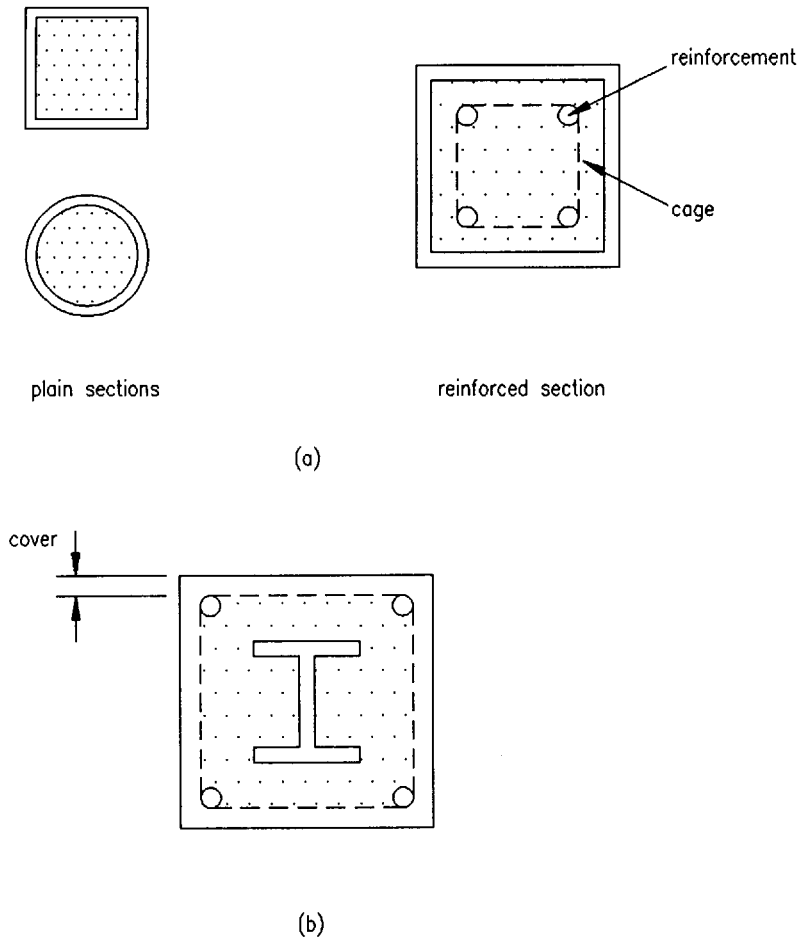


Fig. 22.1 Examples of composite columns: (a) RHS and CHS concrete-filled section, (b) concrete-encased section

has no visual effect on their appeal. The advantages from a structural point of view are, first, the triaxial confinement of the concrete within the section, and second, the fire-resistance of the column which largely depends on the residual capacity of the concrete core.

### 22.1.3 Principles of design

The axial load capacity of a stocky column, defined as a column that is not subject to the effects of instability, is determined by adding the ultimate compressive

strengths of the steel and concrete components. In traditional reinforced concrete design a 'short' column is defined as one whose effective height to least cross-sectional dimension is less than 12, and a nominal allowance is made for eccentricity of axial load.

The axial capacity of concrete-filled sections is greater because the concrete is not able to expand laterally (Poisson's ratio effect) under load and triaxial stresses are developed in the concrete. This causes an increase in the compressive strength of the concrete by an amount dependent on the proportions of the cross-section. The hoop tensions created in the steel have a small adverse affect on its strength.

The effect of eccentricity of axial load is to develop a bending moment in the section. The moment resistance of the section (in the absence of axial load) can be calculated considering plastic stress blocks (see Fig. 22.2). Formulae are given in BS 5400: Part 5, Appendix C.<sup>1</sup> The interaction between axial load and bending moment can be considered in terms of a simplified interaction formula (section 22.2.2).

Slender columns require a more refined treatment. The effective slenderness of a column is determined from the proportions of the composite section. The second moment of area is obtained by adding the second moments of area of the steel and concrete (divided by an appropriate modular ratio). This represents a considerable increase over the properties of steel alone. The axial stress that the section can resist is then determined from the column buckling curves for the steel section under consideration. The resulting axial stress, relative to the yield stress of the steel, is effectively a capacity reduction factor to be applied to the 'stocky column' capacity.

It should be noted that the above approach assumes that loads are not applied laterally over the column length. Concentric and eccentric axial loads cause

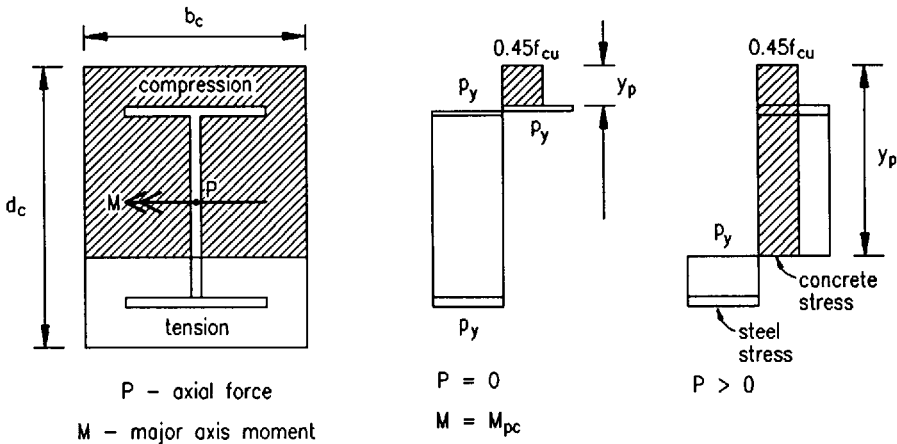


Fig. 22.2 Plastic stress blocks acting on cross section of composite column subject to moment and axial force

relatively low interface shear stresses between the steel and the concrete. Lateral loads cause greater shear stresses and may necessitate the introduction of shear-connectors (as for composite beams – see Chapter 21, section 21.4).

### 22.1.4 Cased strut method

The traditional method of designing cased columns, presented in BS 449: 1969,<sup>2</sup> can be very conservative but is readily accepted as a method of simple design.

The minimum width of the concrete casing, according to BS 449, should be the flange width  $b$  of the steel section plus 100 mm. At least four reinforcing bars are to be located in the concrete at a cover not exceeding 50 mm, to which 5 mm diameter steel stirrups are attached at spacings not exceeding 200 mm. The normal aggregate size is 10 mm and the minimum concrete grade is 21 N/mm<sup>2</sup>.

To establish the axial capacity of the cased column (or strut), the radius of gyration of the solid section is taken as 0.2 ( $b + 100$ ) mm, or alternatively that of the major axis of the steel section. The cross section excludes any concrete cover in excess of 75 mm from the overall dimension of the steel section. The net area of concrete is replaced by an equivalent area of steel by dividing by a modular ratio of 30.

Therefore, knowing the permissible axial stress, as a function of the effective slenderness of the cased column, and the equivalent area of steel, the axial capacity of the section can be easily calculated. However, an onerous limit on the use of this method is that axial load on the cased column should not exceed twice that permitted on the uncased section.

## 22.2 Design of encased composite columns

### 22.2.1 Axial load capacity

The design of composite columns is described in BS 5400: Part 5<sup>1</sup> and in Eurocode 4 (draft).<sup>3</sup> It is based on the method developed by Basu and Sommerville<sup>4</sup> and modified by Viridi and Dowling.<sup>5</sup> The maximum compressive strength (squash load) of a stocky column is:

$$P_u = 0.45f_{cu}A_c + A_s p_y + 0.87A_r f_y \quad (22.1)$$

where  $A_c$  is the cross-sectional area of concrete

$A_s$  is the cross-sectional area of the steel section

$A_r$  is the cross-sectional area of the reinforcement

$f_{cu}$  is the cube strength of concrete

$p_y$  is the design strength of the steel

$f_y$  is the yield strength of the reinforcement.

In BS 5400: Part 5 a factor of 0.91 (corresponding to a material factor of 1.1) is used to modify the term  $A_s p_y$ . This formula is restricted to concrete contribution factors, defined as  $0.45 f_{cu} A_c / P_u$ , between 0.15 and 0.8. In order for any reinforcement to contribute to the axial load capacity of the column, shear links of not less than 5 mm diameter should be provided at not more than 150 mm spacing. The value of  $A_r$  should not exceed  $0.03 A_c$ .

Limits on the proportion of the cross section<sup>3</sup> are that the concrete casing should provide a minimum cover to the steel section of 40 mm, and that the dimensions of the concrete section used in determining  $P_u$  should not exceed  $1.8 \times b$  or  $1.6 \times D$  (where  $b$  is the flange width, and  $D$  is the depth of the steel section.)

The relative slenderness of a composite column of length  $L$  is defined by the slenderness factor:

$$\bar{\lambda} = \frac{L}{\pi} \sqrt{\left( \frac{P_u}{E_s \Sigma I} \right)} \quad (22.2)$$

where  $\Sigma I$  is the combined second moments of area of the concrete, steel section and reinforcement expressed in steel units. To do this the second moment of area of the concrete is divided by the modular ratio  $E_s / (450 f_{cu})$ , where  $E_s$  is the elastic modulus of steel in  $\text{N/mm}^2$ .

The slenderness factor  $\bar{\lambda}$ , converted to an effective slenderness  $\lambda$  by multiplying  $\bar{\lambda}$  by  $\pi \sqrt{(E_s / p_y)}$ , can then be used to determine the axial stress that may be resisted by the steel section. The selection of the appropriate column design curve in BS 5950: Part 1 depends on the steel section used (i.e. Tables 27(a)–(d) in BS 5950: Part 1).

The column design stress  $p_c$ , as determined from  $\lambda$ , divided by  $p_y$  is then used as a capacity reduction factor  $K_1$  to be applied to all the components of  $P_u$  in Equation (22.1). Hence, this method can be used to determine the axial capacity of a composite column  $K_1 P_u$  in the absence of applied moment. This method can be used for slenderness factors  $\bar{\lambda}$  less than 2.0, as proposed in Eurocode 4;<sup>3</sup> for greater slendernesses second order effects are underestimated. Columns of slenderness factor less than 0.2 may be taken as 'stocky' (i.e.  $K_1 = 1.0$ ).

In BS 5400: Part 5,<sup>1</sup> short columns are defined as those where the ratio of the length  $L$  to the least lateral dimension  $b_c$  of the composite column does not exceed 12. Where short columns are not designed to be subject to significant applied moment, the axial capacity may be taken as  $0.85 K_1 P_u$  to allow for slight eccentricity of load.

Slender columns are those where  $L/b_c$  exceeds 12. In design to BS 5400: Part 5,<sup>1</sup> the analysis of the member should consider a minimum additional moment given by the axial load times an eccentricity of  $0.03 b_c$ . This, together with any further applied moments, may be treated as in the following section.

### 22.2.2 Combined axial load and bending moments

The moment resistance of a composite column may be determined by establishing plastic stress blocks defining the strengths of the portions of the section under tension and compression. The plastic neutral axis depth  $y_p$  is defined as below the extreme edge of the concrete in compression. Three cases of neutral axis position exist: in the concrete, through the steel flange, and in the web of the section. The position depends on the relative proportions of steel and concrete (see Fig. 22.2). Commonly,  $y_p$  lies within the steel flange (i.e.  $y_p \approx (d_c - D)/2$ ) for major axis bending of a composite section. In this case:

$$A_s p_y \geq \left( \frac{d_c - D}{2} \right) \times (0.45 f_{cu} b_c) \geq A_w p_y + A_f (0.45 f_{cu}) \quad (22.3)$$

The moment capacity of the composite section is then given by:

$$M_{pc} = 0.5 A_s p_y (d_c - y_p) + 0.5 A_r (0.87 f_y) (d_c - 2d_r) \quad (22.4)$$

where  $d_c$  is the depth and  $b_c$  is the breadth of the concrete section,  $d_r$  is the cover to the reinforcement,  $D$  is the depth of the steel section,  $A_w$  is the cross-sectional area of the web,  $A_f$  is the cross-sectional area of the flange, and  $A_r$  is the cross-sectional area of any additional reinforcement.

Other cases are defined in BS 5400: Part 5, Appendix C.<sup>1</sup>

Because the plastic stress block method slightly overestimates the strength of the section, the moment resistance  $M_{pc}$  is to be multiplied by 0.9 for design purposes.

In the presence of axial load the plastic neutral axis depth increases. For small to medium axial loads the plastic neutral axis remains within the steel web, but for higher axial loads most of the section is in compression. A typical interaction diagram representing the variation of moment capacity with axial load is shown in Fig. 22.3. An interesting phenomenon is that there is a slight increase in moment resistance with increasing axial load (compression), and there is a certain axial load where the moment resistance of the section equals that in the absence of axial load (i.e.  $M_{pc}$  from Equation (22.4)).

For simple design, the possibility exists of defining the interaction between moment and axial force in terms of three intercepts A, B and C on the moment and axial load axes, and also point D which corresponds to the axial load at which the moment capacity remains unchanged. Therefore, a trilinear relationship AD, DC, CB closely models the real interaction diagram. It is normal practice to ignore the beneficial effect of axial load as it cannot always be assumed to be coincident with the applied moment. The curvature of the interaction diagram at higher axial loads can also be ignored without much loss of economy. The method developed by Basu and Sommerville<sup>4</sup> empirically follows the shape of the interaction diagram using coefficients  $K_1$ ,  $K_2$  and  $K_3$  (see Fig. 22.3).

The value of axial load  $P$  at which the moment resistance remains unchanged (point D) may be evaluated as follows.

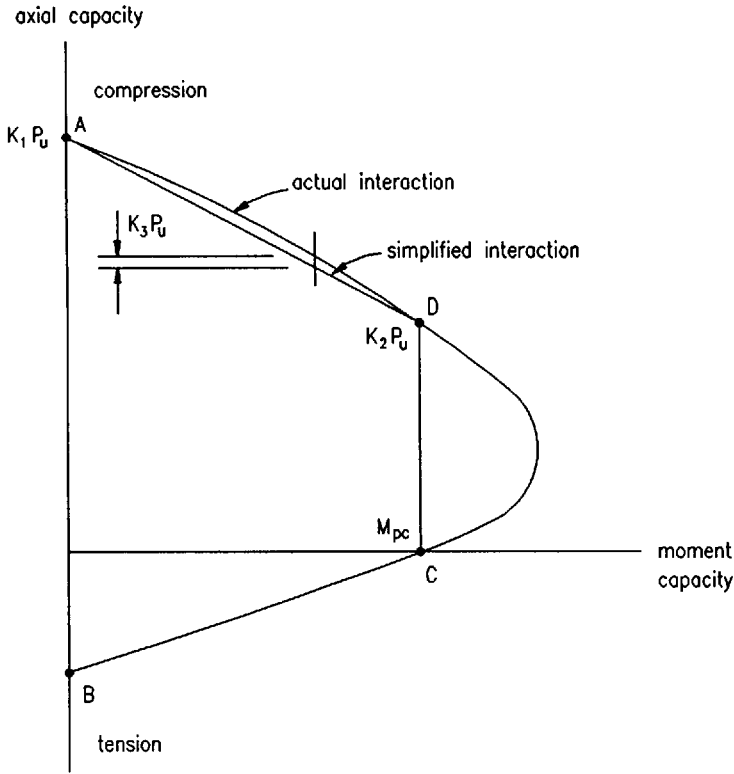


Fig. 22.3 Interaction between moment and axial force

Determine the neutral axis depth  $y_p$  for  $P$  of zero, corresponding to equal tension and compression forces across the composite section. Redefine a neutral axis depth,  $y'_p = d_c - y_p$ , which corresponds to an axis symmetrically placed with respect to  $y_p$  around the centre of the section. The net axial resistance of the section with neutral axis  $y'_p$  corresponds to no change in moment capacity because the net moment effect of the section contained between depths  $y_p$  and  $y'_p$  is zero as illustrated in Fig. 22.2.

It may be shown that the axial resistance of the section (termed  $P_0$ ), corresponding to depth  $y'_p$ , is, in fact, the axial resistance of the concrete section ignoring the contribution of the steel member and the reinforcement. Hence,

$$P_0 = 0.45f_{cu}d_c b_c \tag{22.5}$$

Dividing by  $P_u$  from Equation (22.1) gives a non-dimensional ordinate on the moment/axial-force diagram, corresponding to the moment resistance of the composite section. This ordinate is also equivalent to the concrete contribution factor for major axis bending, and can also be used for minor axis bending. For

stocky columns it also corresponds to the appropriate value of  $K_2$  in the Basu and Sommerville approach.<sup>4</sup>

For slender columns account is to be taken of the moments arising from eccentricity of axial load in addition to the applied moments. The Basu and Sommerville method<sup>4</sup> has been codified in BS 5400: Part 5.<sup>1</sup> Because the method uses empirical formulae for  $K_1$ ,  $K_2$  and  $K_3$  as a function of the slenderness of the column, it appears to be relatively complicated, but it may be simplified by taking  $K_3$  as zero so that the moment resistance at any value of axial load is given by:

$$M = \left( \frac{K_1 - P/P_u}{K_1 - K_2} \right) M_{pc} \leq 0.9M_{pc} \quad (22.6)$$

In design to BS 5400: Part 5,<sup>1</sup> slender columns subject to major axis moment are treated as subject to biaxial moment by including an additional minor axis moment of  $0.03Pb_c$ , where  $P$  is the axial load on the column. An interaction formula given for combining major and minor axis effects is not considered further here.

Provision should be made for the smooth transfer of force between the concrete and steel in cases where the section is subject to high moment. No mechanical shear connection need be provided where the shear stress at the interface between the concrete and the steel is less than  $0.6 \text{ N/mm}^2$  for encased columns.

### 22.2.3 Method of Eurocode 4

The method proposed in Eurocode 4 differs in the treatment of slender columns subject to moment. The moment/axial-force diagram may be determined for a stocky column as above, and a straight line drawn from the origin to intersect the point on the diagram corresponding to an axial force of  $K_1P_u$ . The assumption is made that the moments to the left of this line are utilized as second-order effects under axial load, and moments to the right are available to resist the applied moment. These second-order effects only apply to columns with moments about their major axis.

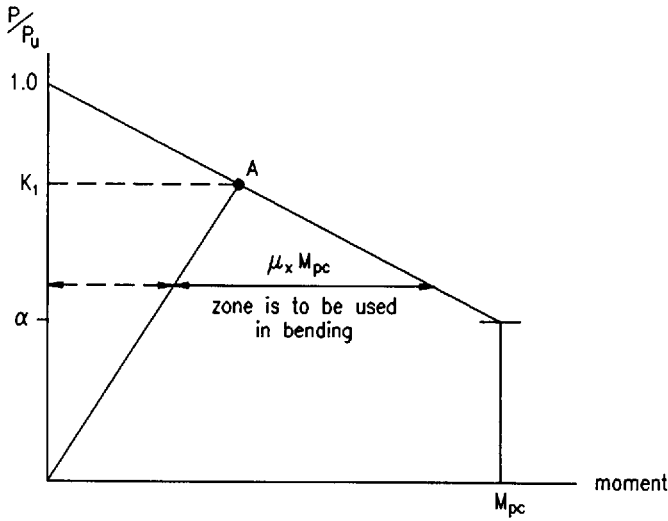
The simple bilinear interaction diagram may therefore be modified by subtracting the moment to the left of this line (see Fig. 22.4(a)). The method also permits treatment of columns subject to non-uniform moment, but it is conservative to ignore this beneficial effect and to design for the maximum moment.

This approach may be followed independently for major and minor axis bending. A simple method of combining these effects is by a linear interaction of the two directions of bending such that:

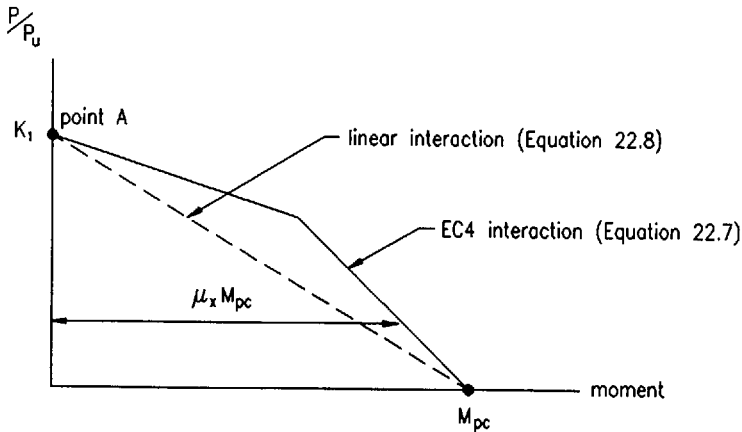
$$\frac{M_x}{\mu_x M_{pc,x}} + \frac{M_y}{\mu_y M_{pc,y}} \leq 1.0 \quad \text{for } P \leq K_1 P_u \quad (22.7)$$

and  $M_x \leq 0.9M_{pc,x}$  and  $M_y \leq 0.9M_{pc,y}$ , where the subscripts  $x$  and  $y$  represent the bending actions in the two directions. The values  $\mu_x$  and  $\mu_y$  represent the reduction

axial force ratio



(a)



(b)

Fig. 22.4 Simplified treatment of slender composite columns in Eurocode 4: (a) moment/axial-force interaction for stocky column, (b) moment/axial-force interaction for slender column

factors on moment resistance considering the effect of axial load. Imperfections are only considered in the weak direction of the column when determining  $K_1$ . The values  $\mu_x$  and  $\mu_y$  for slender columns may be determined from relationships of the form of Fig. 22.4(b) (taking  $K_1$  as unity when determining  $\mu_y$ ).



For low values of concrete contribution factor, a simple linear interaction formula of the following form may be used for slender columns:

$$\frac{P}{K_1 P_u} + \frac{M_x}{M_{pc,x}} + \frac{M_y}{M_{pc,y}} \leq 1.0 \tag{22.8}$$

This is very conservative, but at least overcomes the need to determine interaction charts and can be used for scheme design.

## 22.3 Design of concrete-filled tubes

### 22.3.1 Axial load capacity

The axial capacity of a concrete-filled rectangular or circular section is enhanced by the confining effect of the steel section on the concrete which depends in magnitude on the shape of the section and the length of the column. Buckling tends to reduce the benefit of confinement on the squash load as the column slenderness increases. To account for this, modification factors are introduced. In circular sections it is possible to develop the cylinder strength ( $0.83f_{cu}$ ) of the concrete.

The ‘squash’ load capacity of a circular concrete-filled column is:

$$P_u = C_1 p_y A_s + 0.87 f_y A_r + (0.83 f_{cu} / \gamma_{mc}) A_c \{1 + C_2 (t/\phi) [p_y / (0.83 f_{cu})]\} \tag{22.9}$$

where  $t$  is the thickness and  $\phi$  is the diameter of the tubular section, and  $\gamma_{mc}$  is the material factor for concrete ( $= 1.5$ ). The terms  $C_1$  and  $C_2$  are coefficients which are a function of the slenderness factor  $\bar{\lambda}$  of the column, defined in Equation (22.2);  $C_1$  is less than unity because of the effect of hoop tensions created in the steel. The values of  $C_1$  and  $C_2$  are presented in Table 22.1.

The method derives from research<sup>6,7</sup> carried out by CIDECT and CIRIA and has been incorporated into Eurocode 4.<sup>3</sup> Limits to the use of the method are that the term  $A_s p_y$  should represent between 20% and 90% of  $P_u$ , and to avoid local buckling,  $\phi \leq 85t\epsilon$  (where  $\epsilon$  is  $\sqrt{(275/p_y)}$ ).

The effect of slenderness on the axial strength of a concrete-filled column may be treated as in section 22.2.1. The slenderness factor  $\bar{\lambda}$  may be determined from Equation (22.2) as a function of  $P_u$ . This involves iteration as  $P_u$  is partly dependent on  $\bar{\lambda}$ . As a reasonable approximation,  $\bar{\lambda}$  may be determined assuming

**Table 22.1** Values of  $C_1$  and  $C_2$  defining the behaviour of concrete-filled circular hollow sections

| $\bar{\lambda}$ | 0    | 0.1  | 0.2  | 0.3  | 0.4  | $\geq 0.5$ |
|-----------------|------|------|------|------|------|------------|
| $C_1$           | 0.75 | 0.80 | 0.85 | 0.90 | 0.95 | 1.00       |
| $C_2$           | 4.90 | 3.22 | 1.88 | 0.88 | 0.22 | 0.00       |

that  $C_1 = 1.0$  and  $C_2 = 0.0$ . Having evaluated  $\bar{\lambda}$ , the strength modification factor  $K_1$  can be determined from the column buckling curve given in Table 27(a) of BS 5950: Part 1.

No design formulae are readily available for the axial strength of rectangular filled sections in section 22.2.1. A limit on the proportions of rectangular sections is that  $b \leq 52t\epsilon$  and  $d \leq 52t\epsilon$ .

### 22.3.2 Combined axial load and bending moment

The effect of eccentric axial load or applied moment may be treated conservatively by evaluating the moment capacity of the section taking the concrete strength as  $0.45f_{cu}$  and ignoring the benefits of confinement of the concrete (i.e.  $C_1 = 1.0$  and  $C_2 = 0.0$ ). Formulae for  $M_{pc}$  are given in Reference 7. The interface shear stress is limited to  $0.4 \text{ N/mm}^2$ .<sup>3</sup>

The reduced moment capacity of a concrete-filled section subject to axial load may be determined from the method in section 22.2.2. Design tables for both circular and rectangular hollow sections are given in Reference 7 and are based on the Basu and Sommerville approach.<sup>4</sup>

### 22.3.3 Fire-resistant design

The fire-resistance of encased composite columns may be treated in the same way as reinforced concrete columns. The steel is insulated by an appropriate concrete cover, as given in BS 8110: Part 2.<sup>8</sup> To preserve the cover in the event of a fire, light reinforcement to the steel section is required. In such cases, two-hour fire-resistance can usually be achieved.

The fire-resistance of concrete-filled columns has been the subject of extensive research.<sup>9</sup> During a fire, sufficient redistribution of stress occurs between the hot steel section and the relatively cool concrete cover, such that a minimum of 30 minutes fire-resistance can be achieved.

The fire-resistance of a concrete-filled hollow section may be defined by redefining the load ratio in fire conditions as:<sup>10</sup>

$$\eta = \frac{P_f}{K_1 P_u} \quad (22.10)$$

$$\text{where } P_u = 0.83f_{cu}A_c + f_yA_r \quad (22.11)$$

The axial load  $P_f$  is determined for load factors of unity. The concrete strength of  $0.83f_{cu}$  is the cylinder strength of concrete which can be developed in both circular and rectangular sections in fire. The material factors for concrete and for reinforcement are taken as 1.0 in this formula.

**Table 22.2** Fire-resistance of concrete-filled hollow sections as a function of load ratio<sup>10</sup>

| Fire-resistance<br>(min) | Load ratio, $\eta$ |                      |
|--------------------------|--------------------|----------------------|
|                          | Plain<br>concrete  | 5% fibre<br>concrete |
| 30                       | —                  | —                    |
| 60                       | 0.51               | 0.67                 |
| 90                       | 0.40               | 0.53                 |
| 120                      | 0.36               | 0.49                 |

The term  $K_1$  is determined as in section 22.2.1 or as in Table 10 of BS 5950 Part 8.<sup>10</sup> It excludes the contribution of the steel hollow section and includes the enhanced strength of the concrete. The reinforcing bars are assumed to be fully effective, provided they are located at the appropriate cover.<sup>8</sup> A method of including the effect of applied moment is given in BS 5950: Part 8.<sup>10</sup>

Fire-resistance periods that can be achieved for plain (or bar-reinforced) or fibre-reinforced concrete-filled hollow sections are presented in Table 22.2.

Where enhanced periods of fire-resistance or greater load-carrying capacity are required, external fire protection may be provided. Normally, the effect of concrete filling offers a considerable reduction in the thickness of fire protection material that would be required for an unfilled hollow section.<sup>9</sup>


An important practical requirement for the use of concrete-filled sections is the provision of vent holes at the top and bottom of each column. These are to prevent dangerous build-up of steam pressure inside the columns in the event of a fire. They also permit seepage of any excess moisture in the concrete after construction. Two 12 mm diameter holes placed diametrically opposite each other at the top and bottom of each storey height have been used in testing and proved to be adequate.

## References to Chapter 22

1. British Standards Institution (1979) *Steel, concrete and composite bridges. Part 5: Code of practice for design of composite bridges*. BS 5400, BSI, London.
2. British Standards Institution (1969) *Specification for the use of structural steelwork in building*. BS 449, BSI, London.
3. Commission of the European Communities (1985) *Eurocode 4: Common unified rules for composite steel and concrete structures*. Report EUR 9886 EN.

4. Basu A.K. & Sommerville W. (1969) Derivation of formulae for the design of rectangular composite columns. *Proc. Instn Civ. Engrs*, supplementary volume, Paper 7206S, 233–80.
5. Virdi K.S. & Dowling P.J. (1973) The ultimate strength of composite columns in biaxial bending. *Proc. Instn Civ. Engrs*, **55**, Part 2, March, 251–72.
6. Sen H.K. & Chapman J.C. (1970) *Ultimate Load Tables for Concrete-Filled Tubular Steel Columns*. Construction Industry Research and Information Association (CIRIA), Technical Note 13.
7. British Steel plc (1986) *Design Manual SHS Concrete Filled Columns*. BS Tubes Division, Corby.
8. British Standards Institution (1985) *Structural use of concrete. Part 2: Code of practice for special circumstances*. BS 8110, BSI, London.
9. British Steel plc (1985) *Recent developments in the assessment of the fire-resistance of structural hollow sections*. BS Tubes Division, Corby.
10. British Standards Institution (1990) *Structural use of steelwork in building. Part 8: Code of practice for fire-resistant design*. BS 5950, BSI, London.

A worked example follows which is relevant to Chapter 22.

|  |   |   |                           |
|--|---|---|---------------------------|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>  | Subject<br><b>DESIGN OF COMPOSITE COLUMN</b>  |   | Chapter ref.<br><b>22</b> |
|  | Design code<br><b>EUROCODE 4 (1990 DRAFT)</b> | Made by <b>RML</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>        |

**Problem**

Determine the envelope of design resistance to axial load, major axis moment and minor axis moment of the composite column shown below. Its effective length is 4 m.

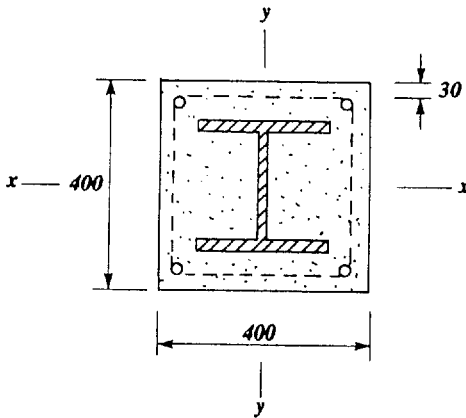
Column size 400 mm square

Steel section 254 × 254 × 89 kg/m UC

Grade 50 steel  $p_y = 355 \text{ N/mm}^2$


Concrete grade  $f_{cu} = 30 \text{ N/mm}^2$  (normal weight)

Reinforcement 4 No. T12 bars  
 $f_y = 460 \text{ N/mm}^2$



Cross-section through column

Note: EC3 does not limit the design strength for steel for  $t \leq 40 \text{ mm}$ .

|  |   |   |   |
|--|---|---|---|
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|  |   | Design code<br><b>EUROCODE 4 (1990 DRAFT)</b> | Made by <b>RML</b><br>Checked by <b>GWO</b> |

Column section properties

Area of section  $A_s = 11400 \text{ mm}^2$

Area of reinforcement  $A_r = 4 \times \pi \times \frac{12^2}{4} = 452 \text{ mm}^2$

Area of concrete  $A_c = 400^2 - 11400 - 452 = 148.1 \times 10^3 \text{ mm}^2$

*Squash load (compressive resistance) of stocky column - equation 22.1*

$$\begin{aligned}
 P_u &= A_s p_y + A_r \times 0.87 f_y + A_c \times 0.45 f_{cu} \\
 &= (11.4 \times 10^3 \times 355 + 452 \times 0.87 \times 460 + 148.1 \times 10^3 \times 0.45 \times 30) \times 10^{-3} \\
 &= 6228 \text{ kN}
 \end{aligned}$$

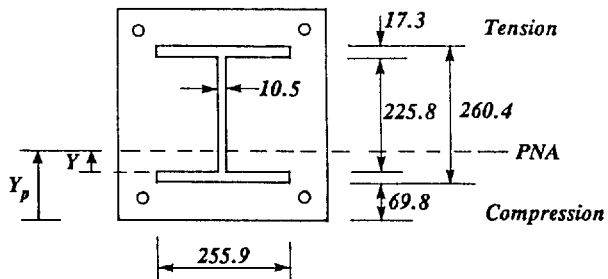
*Tensile resistance of column*


$$\begin{aligned}
 P_t &= A_s p_y + A_r \times 0.87 f_y \\
 &= (11.4 \times 10^3 \times 355 + 452 \times 0.87 \times 460) \times 10^{-3} \\
 &= 4228 \text{ kN}
 \end{aligned}$$

Moment resistance of column - major axis

*Determine position of plastic neutral axis (PNA) parallel to x-x axis of column. Assume that PNA lies at a distance Y into the web of the steel section. Concrete tensile strength is neglected.*

*Equating tension and compression, it follows that the forces in flanges and reinforcement cancel out.*



|   |   |   |                    |
|---|---|---|--------------------|
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|   | Design code<br><b>EUROCODE 4 (1990 DRAFT)</b> | Made by <b>RML</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b> |

**Therefore**

*tensile force in web depth (225.8 - 2Y) = compressive force in concrete*

$$(225.8 - 2Y) \times 10.5 \times 355 = \left[ (Y + 69.8 + 17.3) \times 400 - \frac{452}{2} - 17.3 \right] \times 225.9 - Y \times 10.5 \times 0.45 \times 30$$

$$841.7 \times 10^3 - 7.46 \times 10^3 Y = 5.4 \times 10^3 Y + 470.3 \times 10^3 - 3.05 \times 10^3 - 52.7 \times 10^3 - 0.14 \times 10^3 Y$$

or  $(5.4 + 7.46 - 0.14) Y = 841.7 - 470.3 + 3.05 + 52.7$

$\therefore Y = 33.6 \text{ mm}$

*Hence plastic neutral axis depth from edge of slab is*

$$Y_p = 33.6 + 69.8 + 17.3 = 120.7 \text{ mm}$$

*Plastic moment of resistance about x-x axis:*

*Take moments about PNA at depth  $Y_p$*

$$M_{px} = 17.3 \times 255.9 \times 355 \times 10^{-6} \times (260.4 - 17.3) + \frac{452}{2} \times 0.87 \times 460 \times 10^{-6} \times (400 - 30 \times 2 - 12) + 10.5 \times \frac{Y^2}{2} \times 355 \times 10^{-6} + 10.5 \times \frac{(225.8 - Y)^2}{2} \times 355 \times 10^{-6} + (5.4 Y + 470.3 - 3.05 - 52.7 - 0.14 Y) \times 10^{-3} \times Y_p / 2$$

$$M_{px} = 382.0 + 29.7 + 2.1 + 68.8 + 35.7 \text{ for } Y = 33.6 \text{ mm}$$


$$M_{px} = 518.3 \text{ kNm}$$

$$0.9 M_{px} = 466.5 \text{ kNm}$$

*Compressive resistance of column with co-existing moment (equation 22.5)*

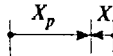
*This is equivalent to the resistance of the concrete in compression (see text)*

$$P_{o,x} = 148.1 \times 10^3 \times 0.45 \times 30 \times 10^{-3} = 1999 \text{ kN}$$

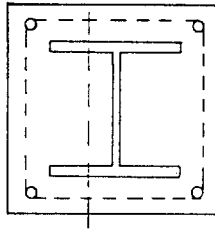
|  |   |                                   |              |
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| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject                           | Chapter ref. |
|  |   | <b>DESIGN OF COMPOSITE COLUMN</b> |              |
| Design code  |   | Made by                           | Sheet no. 4  |
| EUROCODE 4<br>(1990 DRAFT)   |   | RML<br>Checked by GWO             |              |

***Moment resistance of column - minor axis***

Assume PNA at distance  $X$  from edge of web.



Equating tensile and compressive forces.



If  $A_w p_y > 0.45 f_{cu} ( b^2 - A_f - \frac{A_r}{2} )$

then PNA lies in web

$$10.5 \times 225.8 \times 355 \times 10^{-3} > 0.45 \times 30 \times (400^2 / 2 - 17.3 \times 255.9 - 452 / 2)$$

$$841.7 < 1017.2$$

So PNA lies just outside web

Therefore distance  $X$  is obtained from:

$$(2X + 10.5) \times 2 \times 17.3 \times 355 \times 10^{-3} + 10.5 \times 225.8 \times 355 \times 10^{-3}$$

$$= 0.45 \times 30 \times [ (200 - \frac{10.5}{2} - X) \times 400 - \frac{452}{2} - [ \frac{255.9}{2} - \frac{10.5}{2} - X ] \times 17.3 ]$$


$$24.6X + 129.0 + 841.7 = 1051.6 - 5.4X - 3.1 - 28.7 + 0.2X$$

$$X (24.6 + 5.4 - 0.2) = 1051.6 - 841.7 - 129.0 - 3.1 - 28.7$$

$$X = 1.7 \text{ mm}$$

$$\text{Therefore } X_p = 200 - 10.5/2 - 1.7 = 193.0 \text{ mm}$$



|   |   |   |                    |
|---|---|---|--------------------|
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*Plastic moment resistance about y-y axis*

*Take moments about  $X_p$*


$$\begin{aligned}
 M_{py} = & \frac{452}{2} \times 0.87 \times 460 \times 10^{-6} \times (400 - 30 \times 2 - 12) \\
 & + 10.5 \times 225.8 \times \left(X + \frac{10.5}{2}\right) \times 355 \times 10^{-6} \\
 & + \left[ \left[ \frac{255.9}{2} - X - \frac{10.5}{2} \right]^2 + \left[ \frac{255.9}{2} + X + \frac{10.5}{2} \right]^2 \right] \times 17.3 \times 355 \times 10^{-6} \\
 & + (1051.6 - 5.4X - 3.1 - 28.7 + 0.2X) \frac{X_p}{2} \times 10^{-3}
 \end{aligned}$$

$$\begin{aligned}
 M_{py} &= 29.7 + 5.8 + 201.6 + 97.6 \\
 &= 334.7 \text{ kNm}
 \end{aligned}$$

$$0.9 M_{py} = 301.2 \text{ kNm}$$

*Compressive resistance of column subject to co-existing moment of  $M_{py}$*

$$P_{o,y} = P_{o,x} = 1999 \text{ kN}$$

|  |   |   |                           |
|--|---|---|---------------------------|
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***Effect of column slenderness***

$$\text{Modular ratio } \alpha_e = \frac{E_s}{450 f_{cu}} = \frac{205 \times 10^3}{450 \times 30} = 15.2$$

***Second moment of area of column - major axis bending***

$$I_{xx} \approx \left[ I_{xs} + \frac{452}{4} \times (400 - 60 - 12)^2 \right] \left[ 1 - \frac{1}{\alpha_e} \right] + \frac{400^4}{12} \times \frac{1}{\alpha_e}$$

$$I_{xs} = 143.0 \times 10^6 \text{ mm}^4$$

$$I_{xx} = 285.3 \times 10^6 \text{ mm}^4$$

***Second moment of area of column - minor axis bending***

$$I_{yy} = \left[ I_{ys} + \frac{452}{4} \times (400 - 60 - 12)^2 \right] \left[ 1 - \frac{1}{\alpha_e} \right] + \frac{400^4}{12} \times \frac{1}{\alpha_e}$$

$$I_{ys} = 48.5 \times 10^6 \text{ mm}^4$$

$$I_{yy} = 197.0 \times 10^6 \text{ mm}^4$$

$$P_u = 6228 \text{ kN squash load - see calculation sheet no.2}$$

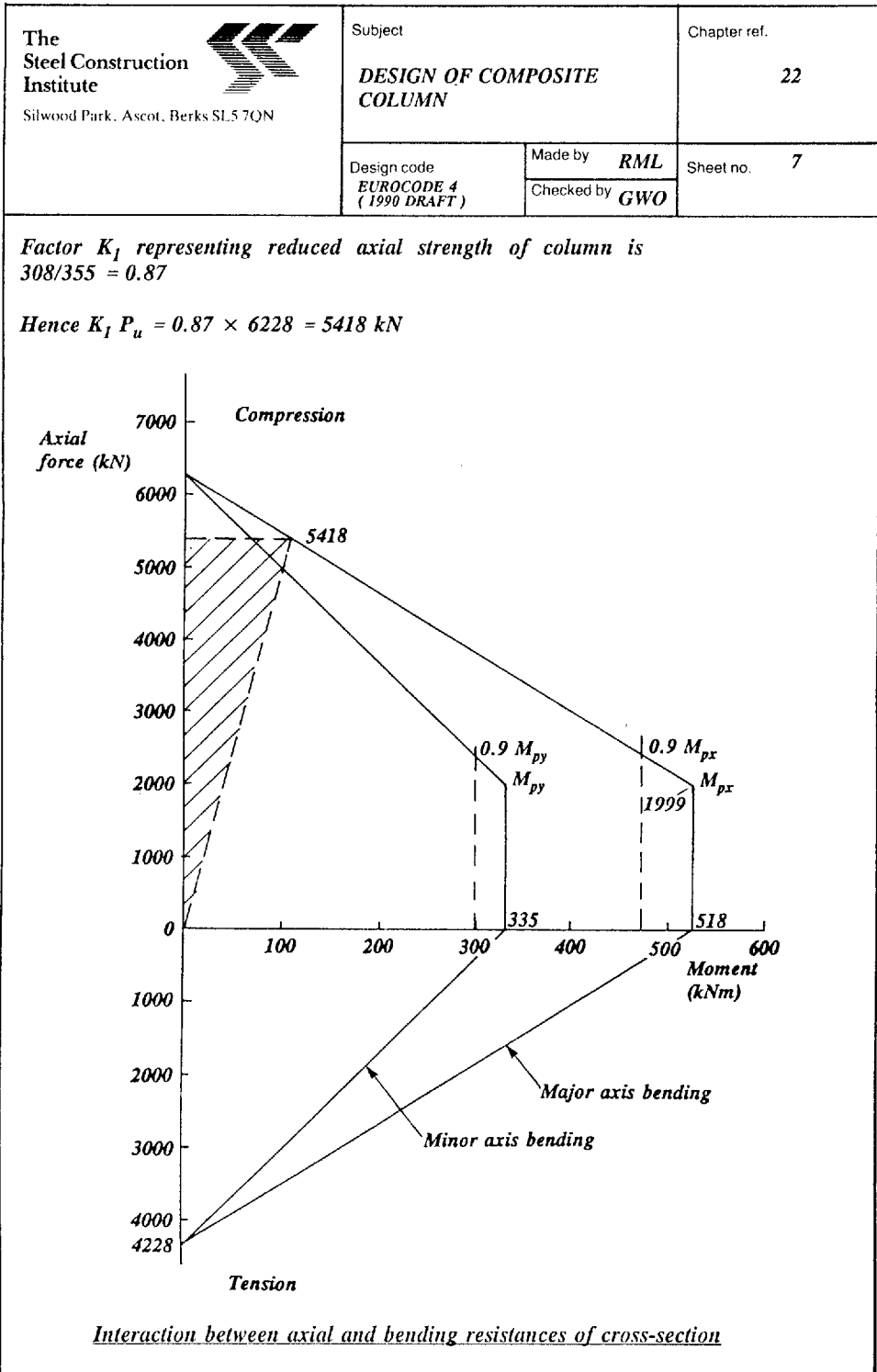
***Slenderness factor***


$$\begin{aligned} \bar{\lambda} &= \frac{L}{\pi} \left[ \frac{P_u}{E_s \Sigma I_{yy}} \right]^{0.5} \\ &= \frac{4000}{\pi} \left[ \frac{6228 \times 10^3}{205 \times 10^3 \times 197.0 \times 10^6} \right]^{0.5} = 0.5 \end{aligned}$$

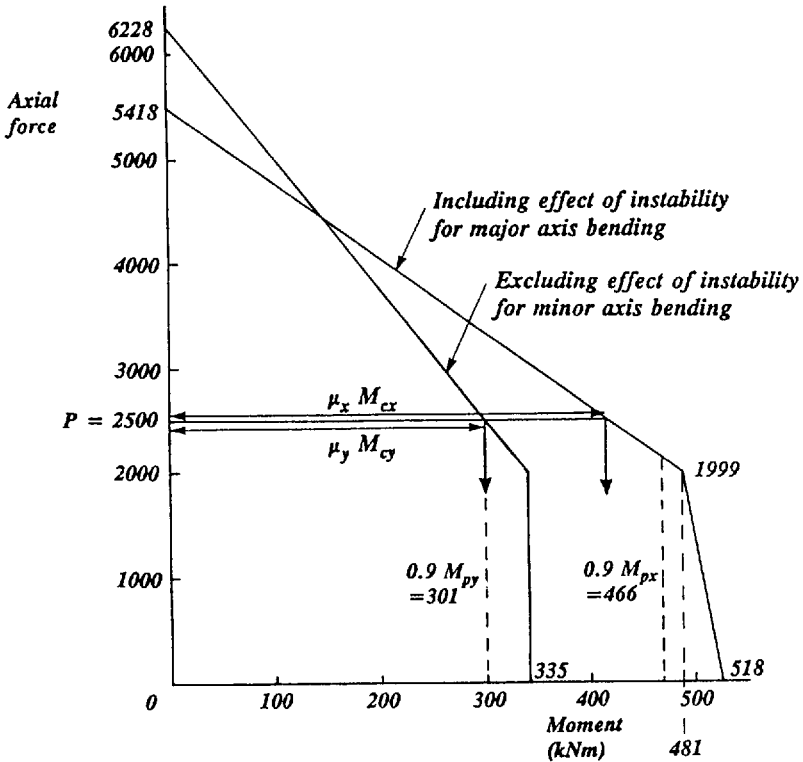
$$\lambda_{eff} = \bar{\lambda} \pi (E_s / p_y)^{0.5} = 0.5 \pi (205 \times 10^3 / 355)^{0.5} = 38$$

From BS 5950: Part 1 Table 27(c)

$$\text{Axial strength } p_c = 308 \text{ N/mm}^2$$



|   |   |   |
|---|---|---|
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|   | Design code<br><b>EUROCODE 4 (1990 DRAFT)</b> | Made by <b>RML</b><br>Checked by <b>GWO</b> |



Reduced interaction of axial force and moment in slender column

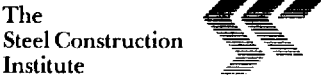
Example of use of interaction diagram

Assume the following design loads

Axial force  $P = 2500$  kN

Bending moment about major axis = 150 kNm

Bending moment about minor axis = 75 kNm

|  |   |   |                           |
|--|---|---|---------------------------|
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|  | Design code<br><b>EUROCODE 4 (1990 DRAFT)</b> | Made by <b>RML</b><br>Checked by <b>GWO</b> | Sheet no. <b>9</b>        |

*Additional moment arising from potential eccentricity of vertical load. Take eccentricity as 0.03 b<sub>c</sub>.*

$$\begin{aligned} \text{Moment } M_x &= 150 + 2500 \times 0.03 \times 0.4 = 180 \text{ kNm} \\ M_y &= 75 + 2500 \times 0.03 \times 0.4 = 105 \text{ kNm} \end{aligned}$$

*Simple interaction (equation 22.8)*

$$\frac{P}{K_1 P_u} + \frac{M_x}{M_{px}} + \frac{M_y}{M_{py}} \leq 1.0$$

$$\frac{2500}{5418} + \frac{180}{518.3} + \frac{105}{334.7} = 1.12 > 1.0$$

*Consider EC4 interaction (equation 22.7)*

*Major axis bending*

At  $P = 2500 \text{ kN}$ , resistance moment =  $\mu_y M_{px}$

$$\mu_y M_{px} = \frac{5418 - 2500}{5418 - 1999} \times 488 = 416 \text{ kNm}$$

*Minor axis bending =  $\mu_y M_{py}$*

$$\mu_y M_{py} = \frac{6228 - 2500}{6228 - 1999} \times 335 = 295 \text{ kNm}$$

$$\frac{M_x}{\mu_y M_{px}} + \frac{M_y}{\mu_y M_{py}} = \frac{180}{416} + \frac{105}{295} = 0.79 < 1.0$$

*Therefore, the design is satisfactory for biaxial bending.*

# Chapter 23

## Bolts

by HUBERT BARBER

### 23.1 Types of bolt

#### 23.1.1 Grade 4.6 and 8.8 bolts

The most frequently used bolts in structural connections are grade 4.6 black bolts and 8.8 high-strength bolts, the manufacture of which is governed by British Standards as follows:

BS 4190: *Specification for ISO metric black hexagon bolts, screws and nuts*<sup>1</sup>  
BS 3692: *Specification for ISO metric precision hexagon bolts, screws and nuts*.<sup>2</sup>

In practice many bolts are supplied that are made from BS 3692 material to the sizes and tolerances of BS 4190.

Bolts of other strength grades are also available: for example, grade 4.6, 4.8, 6.9 to BS 4190, and grade 4.6 through to 14.9 to BS 3692.

The strength grade designation, which is in accordance with ISO/R 898/1, is defined in both these British Standards. The system consists of two figures: the first is one-tenth of the minimum tensile strength in kilograms force per square millimetre and the second is one-tenth of the ratio between the minimum yield and minimum tensile strength expressed as a percentage. The two figures are separated by a decimal point.

In the case of higher strength bolts which have a less easily defined yield strength the stress at permanent set limit  $R_{0.2}$  is used.

From this it can be seen that the minimum ultimate strength of a grade 4.6 bolt is  $40 \text{ kgf/mm}^2$  ( $392 \text{ N/mm}^2$ ) and that its minimum yield stress is  $0.6 \times 40 = 24 \text{ kgf/mm}^2$  ( $235 \text{ N/mm}^2$ ). With higher grade bolts the permanent set limit will occur at 80% or 90%, depending on the classification.

There is a similar designation system for nuts. This is a single figure being one-tenth of the ultimate strength of the steel. Hence a grade 8 nut has an ultimate strength of  $80 \text{ kgf/mm}^2$  ( $785 \text{ N/mm}^2$ ) and would normally be used with a grade 8.8 bolt. It is permissible however to use a nut of higher grade than the bolt to minimize the risk of thread stripping.

### 23.1.2 High-strength friction-grip bolts

High-strength friction-grip bolts are manufactured to the requirements of BS 4395.<sup>3</sup> This British Standard covers three distinctly different types of fastener.

Part 1 – General grade. The most commonly used type in general structural steelwork. The strength grade is about that of 8.8 bolts up to 24 mm diameter. For larger sizes the minimum ultimate strength is reduced to approximately 73 kgf/mm<sup>2</sup> (715 N/mm<sup>2</sup>) and the yield to approximately 77% of that figure. Their use is governed by BS 4604: Part 1<sup>5</sup>.

Part 2 – Higher grade. These are made from 10.9 grade and although a higher tensile load can be applied to them there is a much reduced margin between the yield load and the ultimate strength. It is therefore not permissible to use them for connections in which there is applied tension. The ‘part turn’ method of tightening is not permitted by BS 4604: Part 2 which requires in Table 2 of that Standard that the prestressing is within strictly controlled limits; given as from 0.85 to 1.15 of the proof load.

Part 3 – Higher grade (waisted shank). These are made from higher grade steel quality as for Part 2 bolts, that is 10.9 grade, but as a consequence of the reduced diameter of the waisted shank the ultimate strengths are somewhat less than those of general grade bolts, except for diameters of 27 mm and over, which are higher than those of Part 1 bolts, for the reasons given in the paragraph ‘Part 1 – General grade’. As the area of the waisted shank is less than that of the threaded portion the combined torsional and tensile stresses during tightening do not become critical. The ‘part turn’ method of tightening, or any method utilizing direct measurement of the shank tension, is therefore allowed. BS 4604: Part 3 however expressly proscribes the torque control method for waisted shank bolts.

## 23.2 Methods of tightening and their application

The usual methods of tightening of friction-grip bolts are outlined in section 33.7.5. Further details are given in References 6 and 7.

## 23.3 Geometric considerations

### 23.3.1 Hole sizes

Ordinary bolts should be used in holes having a suitable clearance in order to facilitate insertion. For bolts up to and including diameters of 24 mm the clearance should be 2 mm, and above 24 mm should be 3 mm.

Normal clearance holes as given for ordinary bolts are usually used for HSFG fasteners but it is permissible to use oversize, short or long slotted holes provided standard hardened washers are used over the holes in the outer plies.

Oversize and short slotted holes may be used in all plies but long slotted holes may only be used in one single ply in any connection. If a long slotted hole occurs in an outer ply it should be covered with a washer plate longer than the slot and at least 8 mm thick.

Maximum dimensions of holes are given in Table 35 of BS 5950 and in the Appendix *Connection design: table of hole sizes*.

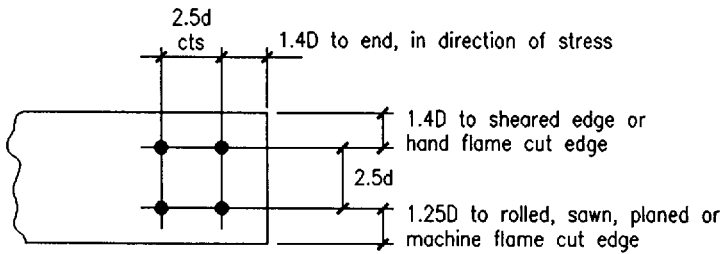
The assessment of the slip resistance is affected when oversize or slotted holes are used. The constant  $K_s$  (clause 6.4.2.1 of BS 5950), which is 1.0 for bolts in clearance holes, is reduced to 0.85 and 0.6 as given in paragraph 23.5.2.

**23.3.2 Spacing of fasteners, end and edge distances**

Spacing is covered fully in Section 6.2 of BS 5950, summarized as follows:

*Minimum requirements* (see Fig. 23.1)

|   |          |
|---|----------|
| Centres of fasteners                              | $2.5d$   |
| Edge distances                                    |          |
| to rolled, sawn, planed or machine flame cut edge | $1.25D$  |
| to sheared or hand flame cut edge                 | $1.4D$   |
| End distances                                     |          |
| in all cases                                      | $1.4D^a$ |



where  $d$  = fastener diameter  
 $D$  = hole diameter

Fig. 23.1 Minimum dimensions (see Table in Appendix)



<sup>a</sup> The full bearing value of a bolt through a connected part cannot be developed if the end distance is less than  $2D$ . For end distances between  $1.4D$  and  $2D$  the bearing value is proportionally reduced. The minimum end distance for the full bearing value in the case of parallel shank HSFG bolts is  $3d$  (see below).

*Maximum requirements* (see Fig. 23.2)

Centres of fasteners in the direction of stress  $14t$

where  $t$  is the thickness of the thinner element.

*Edge distances*

Distance to the nearest line of fasteners from the edge of an unstiffened part  $11t\epsilon$

*In corrosive environments*

Centres of fasteners in any direction  $16t$  or  $200$  mm

Edge distances  $4t + 40$  mm

$d$  = fastener diameter

$D$  = hole diameter

$t$  = thickness of the thinner outside ply

$\epsilon = \left[ \frac{275}{p_y} \right]^{\frac{1}{2}}$  where  $p_y$  is the design strength of the element concerned.

In the case of high-strength parallel-shank friction-grip bolts the slip resistance is a serviceability criterion and the connection could slip into bearing between working and failure load. It is necessary therefore to check the bearing strength of the joint. The end distance to attain the full bearing strength is increased to  $3d$ .

This does not apply to waisted shank fasteners, which cannot act satisfactorily in bearing. Accordingly the allowable slip resistance is reduced so that slip becomes the failure condition.

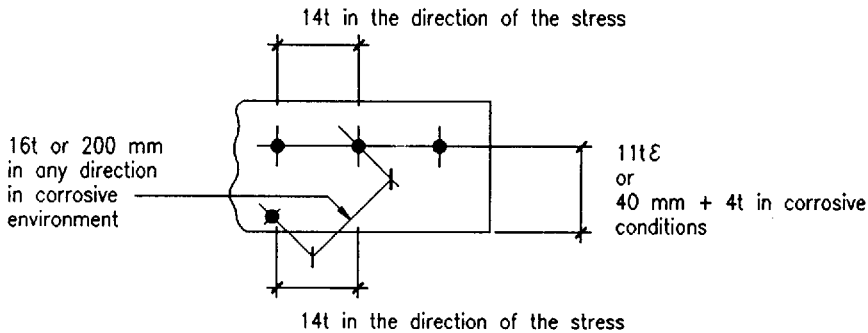


Fig. 23.2 Maximum dimensions (see Table in Appendix)

### 23.3.3 Back marks and cross centres

The back mark is the distance from the back of an angle or channel web to the centre of a hole through the leg or flange. This dimension is determined so as to allow the tightening of a bolt with a standard podger spanner, to be as near as possible to the centroidal axis and to allow the required edge distance. Recommended back marks and diameters are given in the tables for channels and for angles (*Appendix Connection design: Back marks in channel flanges and Back marks in angles*).

The distances between centres of holes (cross centres) in the flanges of joists, universal beams and universal columns are similarly determined after consideration of accessibility and edge distances.

Recommended cross centres and diameters are given in the *Appendix Connection design: Cross centres through flanges*.

## 23.4 Methods of analysis of bolt groups

### 23.4.1 Introduction

Any group of bolts may be required to resist an applied load acting through the centroid of the group either in or out of plane producing shear or tension respectively. The load may also be applied eccentrically producing additionally torsional shear or bending tension. Examples are given in Fig. 23.3.

### 23.4.2 Bolt groups loaded in shear

British and Australian practice is to distribute the torsional shear due to eccentricity elastically in proportion to the distance of each bolt from the centroid of the group. This is referred to as the polar inertia method.

(In some countries, notably Canada and in some cases the USA, the instantaneous centre method is used. This is a redistribution system, developed by Crawford and Kulak,<sup>4</sup> in which the assumed centre of rotation is continually adjusted until the three basic equations of equilibrium are satisfied. The method is a limit-state concept and has been shown to be less conservative than the traditional elastic methods.)

Consider first a single line of bolts subject to a torsional moment, Fig. 23.4(a). If the area of each bolt is  $a$ , the second moment of area of a typical bolt is  $ay^2$  and the total is  $\Sigma ay^2 = a\Sigma y^2$ . The stress in the extreme bolt due to the eccentricity then becomes:

$$\frac{My_1}{I} = \frac{My_1}{a\Sigma y^2}$$

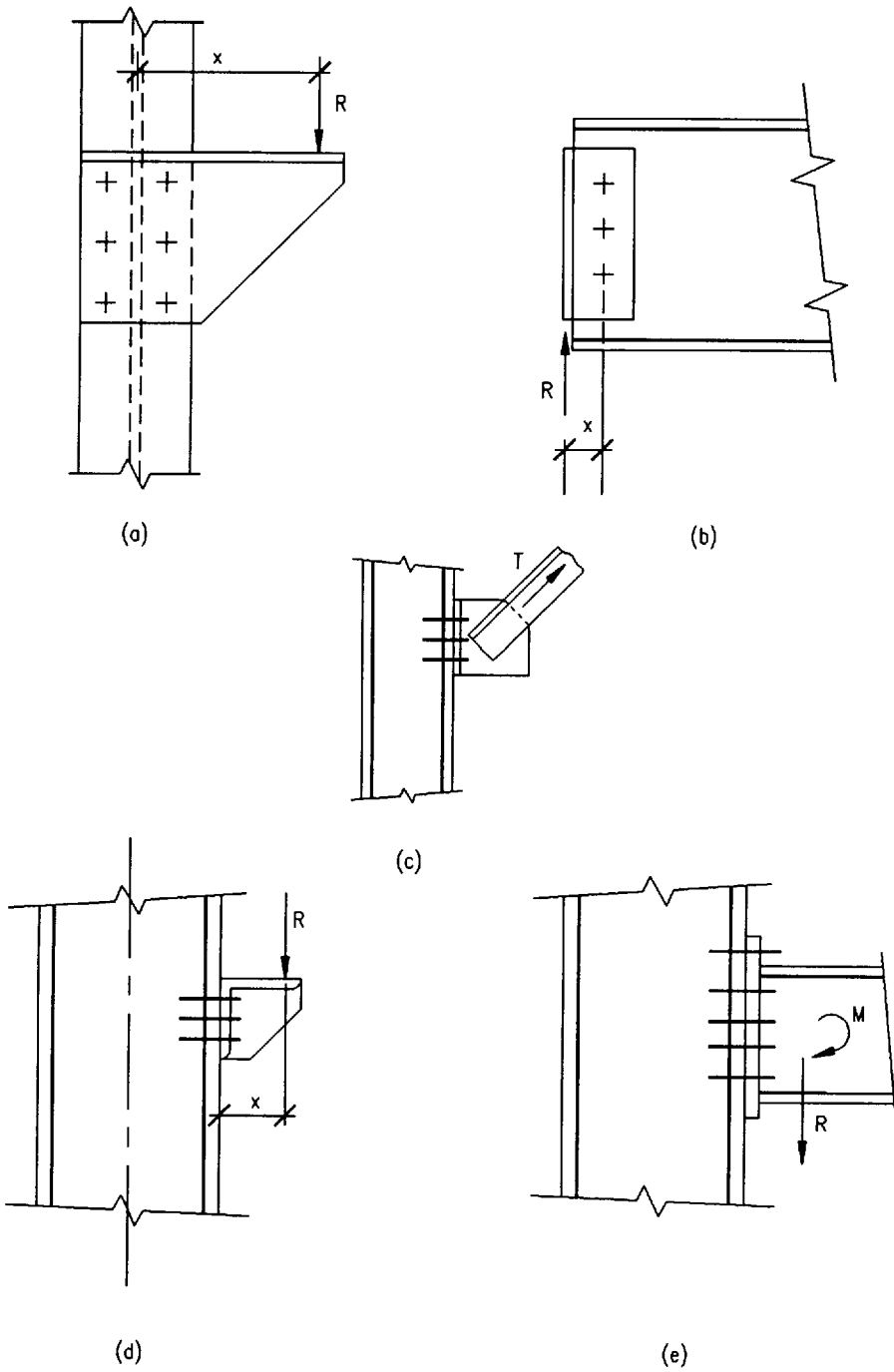


Fig. 23.3 Bolt groups

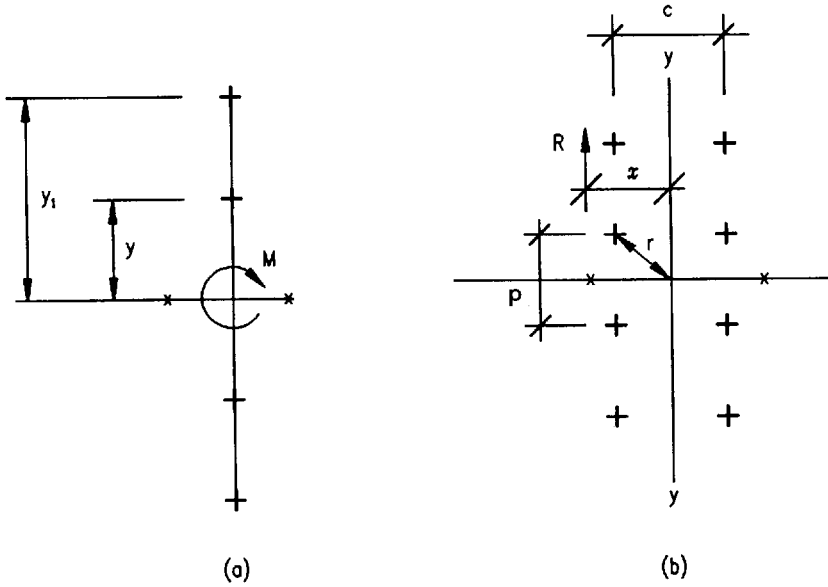


Fig. 23.4 Bolt group analysis

and the force per bolt

$$\frac{May_1}{a\Sigma y^2} = \frac{My_1}{\Sigma y^2}$$

The polar inertia about the centroid for any single line group containing  $n$  bolts with constant pitch  $p$  is

$$I_0 = \sum_{J=0}^{J=(n-1)} \left[ \frac{(n-1-2J)}{2} p \right]^2$$

Consider next a double line of bolts subject to a load  $R$  with eccentricity  $x$  (Fig. 23.4(b)). The radius to the nearest bolt is given by

$$r = \sqrt{\left[ \left( \frac{p}{2} \right)^2 + \left( \frac{c}{2} \right)^2 \right]}$$

$$r^2 = \left( \frac{p}{2} \right)^2 + \left( \frac{c}{2} \right)^2$$

$I_0$  for a typical bolt is then  $ar^2$  and it follows that  $I_0$  for the whole group becomes  $I_{xx} + I_{yy}$  which, if there are  $m$  vertical rows and  $n$  horizontal rows, is

$$I_{00} = m \sum_{J=0}^{J=(n-1)} \left[ \frac{(n-1-2J)}{2} p \right]^2 + n \sum_{J=0}^{J=(m-1)} \left[ \frac{(m-1-2J)}{2} c \right]^2$$

where  $c$  is the cross centres between the vertical lines. The distance to the extreme bolt is

$$r = \sqrt{\left\{ \left[ \frac{(n-1)}{2} p \right]^2 + \left[ \frac{(m-1)}{2} c \right]^2 \right\}}$$

The force in the extreme bolt due to the moment is

$$f_m = \frac{R_x r}{I_{00}}$$

The force in each bolt due to the shear (assumed equally divided between all bolts) is

$$f_v = \frac{R}{mn}$$

The combined force per bolt is the resultant of these two, see Fig. 23.5.

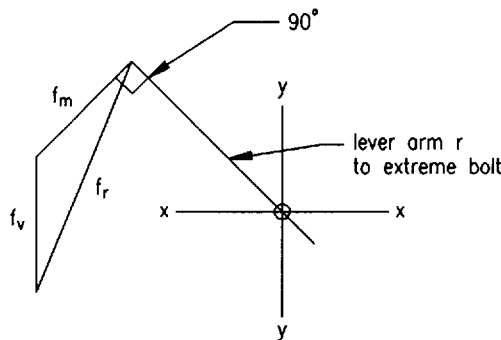


Fig. 23.5 Resultant force

The resultant bolt force is then checked against the bolt strength in single shear, double shear or bearing as is appropriate. In the case of bearing, however, it should be remembered that the full strength cannot be achieved if the end distance measured along the line of the resultant is less than twice the diameter of the bolt. In this case the bearing strength is reduced in proportion.

### 23.4.3 Bolt groups loaded in tension and out of plane moment

The connection types illustrated in Fig. 23.3(c), (d) and (e) are dealt with in Chapter 26.

## 23.5 Design strengths

### 23.5.1 General

Ordinary bolts have to resist forces in shear and bearing or tension or combinations of these. HSFG bolts resist shear by developing friction between the plies; they may also resist external tension. The load capacity of a joint may be affected if it is excessively long, has a large grip length or is subjected to prying action.

### 23.5.2 Shear

When bolts are loaded in shear some of the threads of the bolt may lie within the shear plane. The shear strength is then assessed on the tensile area of the bolt. If however it is known with certainty that no part of the threaded section of the bolt will fall within the shear plane the full shank area may be used in determining the strength.

Until an HSFG bolted shear connection slips shear force is resisted by friction. The slip resistance,  $P_{sL}$ , is given by

$$P_{sL} = 1.1 K_s \mu P_0$$

where  $K_s = 1.0$  for clearance holes;

= 0.85 for oversized holes, short slotted holes or long slotted holes loaded perpendicular to the slot direction;

= 0.6 for long slotted holes loaded parallel to the slot direction

$\mu$  = slip factor, determined from tests in accordance with BS 4604, must not exceed 0.55; but for BS 4395: Part 1 fasteners in connections with untreated surfaces in contact in accordance with BS 4604,  $\mu$  may be taken as 0.45 without further tests

$P_0$  = the minimum shank tension.

This expression gives the value for  $P_{sL}$  for bolts to BS 4395: Part 1 (general grade) taking  $\mu$ , the slip factor, as 0.45, the permitted value for untreated surfaces meeting the requirements of BS 4604: Part 1.<sup>5</sup>

In the case of higher grade parallel and waisted shank fasteners it is inappropriate to use the value 0.45 for  $\mu$  that is given for general grade bolts in BS 5950. The actual value of the slip factor,  $\mu$ , should always be established by tests in accordance with BS 4604: Part 2 or Part 3<sup>5</sup> as appropriate. BS 5950 however specifies in upper limit of 0.55. For waisted shank fasteners  $P_{sL} = 0.9K_s\mu P_0$ , where  $K_s$ ,  $\mu$  and  $P_0$  are as previously defined for parallel shank fasteners.

It is also required by BS 4604: Part 2<sup>5</sup> that the shank tension should be between 0.85 and 1.15 of the proof load so as to avoid distress in the threads during tightening. The minimum shank tension  $P_0$  then becomes 0.85 proof load.

### 23.5.3 Bearing

#### *Ordinary bolts*

In cases where the strength is assessed from the bearing of the bolt on one of the connected parts it is necessary to limit the bearing strength in accordance with the end distance requirements.

For end distances between the minimum ( $1.4D$ ) and the minimum value for full bearing ( $2.0D$ ) the bearing value is proportional to the end distance.

#### *HSFG bolts*

After slip has occurred a parallel shank HSFG bolt acts in shear or bearing.

When the end distance is at least three times the nominal diameter of the bolt the bearing strengths,  $p_{bg}$ , for steel to BS 4360 are as follows:

- Grade 43 – 825 N/mm<sup>2</sup>
- Grade 50 – 1065 N/mm<sup>2</sup>
- Grade 55 – 1210 N/mm<sup>2</sup>

This is a condition which can only apply after joint slip has occurred, and the joint is beyond the serviceability limit.

### 23.5.4 Tension

When bolts are loaded in tension additional axial forces are sometimes induced due to prying action. The strength values given in Table 32 of BS 5950 have been reduced to make allowance for these forces. Further discussion of prying action is given in Chapter 26.

It is permissible to subject HSFG bolts complying with Part 1 or Part 3 of BS 4395 to externally applied tension. Fasteners to Part 2 of that standard however should not be required to carry external tension.

The maximum tension,  $P_t$ , which may be applied to Part 1 and Part 3 fasteners is  $0.9P_0$ , where  $P_0$  is the minimum shank tension given in the Appendix and specified in BS 4604.

The values of  $P_t$  are given in the Appendix *Connection design: Bolt capacities in tension*.

### 23.5.5 Combined shear and tension

Ordinary bolts which are subject to both tension and shear should satisfy the relationship

$$\frac{F_s}{P_s} + \frac{F_t}{P_t} \leq 1.4$$

where  $F_s$  is the applied shear,  $F_t$  is the applied tension,  $P_s$  is the shear capacity, and  $P_t$  is the tensile capacity, in addition to the other specified requirements of section 6.3 of BS 5950. The shear capacity,  $P_s$ , may be based on the tension stress area or on the full shank area as appropriate (see section 23.5.2).

This expression allows that when either the shear or tensile capacity is fully taken up (i.e.  $F_s/P_s$  or  $F_t/P_t = 1.0$ ), the other may be stressed to 40% of its capacity.

HSFG bolts complying with Part 1 or Part 3 of BS 4395, subject to both shear and externally applied tension, should satisfy the relationship

$$\frac{F_s}{P_{sL}} + 0.8 \frac{F_t}{P_t} \leq 1$$

where  $F_s$  is the applied shear,  $F_t$  is the applied external tension,  $P_t$  is the tension capacity given in the Appendix *Connection design: Bolts to BS 4395, long joints*, and  $P_{sL}$  is the lesser appropriate slip resistance.

### 23.5.6 Long joints and large grips

When the joint length in a splice or end connection,  $L_j$ , defined as the distance between the first and last bolt on either side of the joint is greater than 500 mm, the strength of the joint is reduced by the factor  $(5500 - L_j)/5000$ , where  $L_j$  is the joint length as defined above (see Fig. 23.6). Similarly when the grip length,  $T_g$ , the total thickness of the connected plies, is greater than five times the nominal diameter of the bolts, the strength of the joint is reduced by the factor  $8d/(3d + T_g)$ , where  $d$  is the nominal bolt diameter and  $T_g$  is as defined above (see Fig. 23.7).

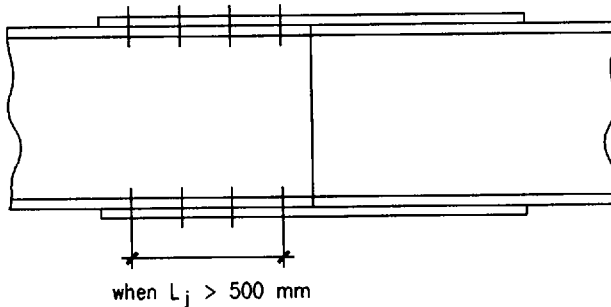


Fig. 23.6 Long joint



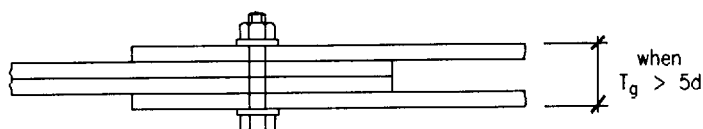


Fig. 23.7 Large grip

In cases when both the above conditions apply it is only necessary to apply the factor producing the greater reduction.

The large grip reduction does not apply to HSFG bolts except when parallel shank bolts are being used in bearing for considerations beyond serviceability.

'Long joint' connections, in the case of parallel shank HSFG bolted joints, are defined by the same criterion and the joint capacity due to slip is reduced by the same factor,  $(5500 - L_j)/5000$ .

$$P_{sL} = 0.6P_0 \frac{(5500 - L_j)}{5000}$$

as given in clause 6.4.2.3 of BS 5950.

## 23.6 Tables of strengths

### 23.6.1 Bolt strengths

Tables 32 and 33 of BS 5950 give respectively the strength of bolts in clearance holes and the bearing strength of connected parts to BS 4360 for ordinary bolts in clearance holes. The values are given in the Appendix *Connection design: Bolt strengths* for connected parts of steel to BS 4360.

### 23.6.2 Bolt capacities

Tables of bolt capacities for various grades and applications are given in the Appendix *Connection design*.

## References to Chapter 23

1. British Standards Institution (1967) *Specification for ISO metric black hexagon bolts, screws and nuts*. BS 4190, BSI, London.

2. British Standards Institution (1967) *Specification for ISO metric precision hexagon bolts, screws and nuts. Metric units.* BS 3692, BSI, London.
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### **Further reading for Chapter 23**

- British Constructional Steelwork Association (1979) *Metric Practice for Structural Steelwork.* BCSA Publication No. 5
- Douty R.T. & McGuire W. (1965) High strength bolted moment connections. *J. Struct. Div., ASCE*, **91**, ST2, April.
- Kulak G.L., Fisher J.W. & Struik J.H.A. (1987) *Design Criteria for Bolted and Riveted Joints*, 2nd edn. John Wiley & Sons.

# Chapter 24

## Welds

by HUBERT BARBER

### 24.1 Full penetration and partial penetration welds

#### 24.1.1 Butt welds

Butt welds are defined as those which join parts together essentially within the thickness of the parent metal. When the parts connected are thin it may be possible to achieve full penetration without preparation, depending on the welding process used. For thicker joints, edge preparation is undertaken in almost all butt-welded joints. In lightly-loaded joints partial penetration welds, nevertheless involving some preparation, are often adequate.

#### *Partial penetration butt welds*

In partial penetration butt joints welded from one or both sides the throat thickness should be taken as the design depth of penetration. In the case of V or bevel butt welds the depth of penetration should be taken as the depth of preparation minus 3 mm. Except when it can be shown that greater penetration can be consistently achieved, the depth of penetration on one side of a J or U weld should be taken as the depth of preparation.

The specified preparation should not be less than  $2\sqrt{t}$ , where  $t$  is the thickness in millimetres of the thinner part joined.

In the design of partial penetration butt joints the eccentricity of the joints should be allowed for in calculating the stress, and the joint should be suitably restrained against rotation where appropriate.

The above paragraphs summarize the requirements of clauses 6.6.6.2 and 6.6.6.3 of BS 5950.

Incomplete penetration butt welds welded from one side only should not be subjected to bending so as to put the root in tension. The use of such welds to resist repeating or alternating forces should also be avoided. If it is unavoidable, the design strengths should be suitably adjusted. Reference should be made to BS 5400: Part 10.

#### *Full penetration butt welds*

Provided that the weld is made with suitable welding consumables, the strength of a full penetration butt weld is equal to that of the parent metal.

### *Butt weld preparation*

The importance of the choice of the most appropriate form of preparation cannot be overemphasized as it often influences the integrity of the weld, the control of cracking and the control of distortion. The shape of the weld preparation in relation to the metal thickness also has an important influence on accessibility for the electrode. These matters are discussed in detail in Appendix B of BS 5135.<sup>1</sup> Table 15 of that British Standard gives full profiles of some commonly used preparation, of which thirteen are tabulated together with limiting dimensions and tolerances in Fig. 24.1.

When parts of unequal cross section are butt jointed with the centroidal axes out of line with each other, local bending will result and must be taken into account in assessing the strength of the joint. If it becomes desirable to taper the thicker member, the slope should not exceed one in four.

#### **24.1.2 Fillet welds**

Fillet welds may be made between surfaces where the fusion faces form an angle of between  $120^\circ$  and  $60^\circ$ . It is acceptable for the two legs to be of unequal lengths but the throat thickness should be appropriately calculated.

When fillet welds are used through holes or slots in one or more of the connected parts (plug welds) the holes should be of adequate size to allow welding access. The appropriate dimensions are given in Appendix A of BS 5135 and are summarized in the following paragraph.

The diameter of the hole to be not less than  $3 \times$  (thickness of part connected) or 25 mm. The ends of the slots should be radiused at  $1.5 \times$  (thickness of the plate) or 12 mm. The distance between the edge of the part and the edge of the slot should be not less than twice the plate thickness or 25 mm. Holes and slots should not be completely filled with weld metal in a single operation as there is a risk of cracking during cooling. If it is specifically required that the hole be filled it should be done as a separate pass after the slag has been removed from the first weld and it has been inspected.

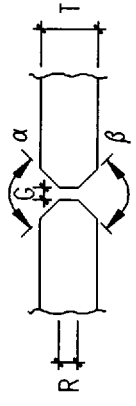
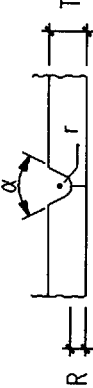
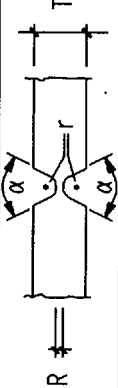
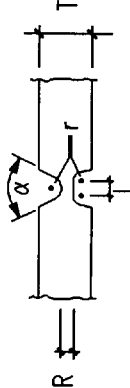
## **24.2 Geometric considerations**

### **24.2.1 Effective throats**

The throat thickness of fillet welds is given in Table 24.1. The factors given in the table are approximately equal to the cosine of the half angle between the fusion faces for welds of equal leg length, and when multiplied by the leg length will give the perpendicular distance between the root and a line joining the intersections of

| Weld type  | Shape of preparation | Dimensions in mm            |          |              |        |                          |   |  |
|--|----------------------|-----------------------------|----------|--------------|--------|--------------------------|---|--|
|  |                      | T                           | $\alpha$ | G            | R      | r                        | L |  |
| Open square butt<br>(without backing)                            |                      | 3 to 6                      |          | 3            |        |                          |   |  |
| Open square butt<br>(with backing)                               |                      | 3 to 5<br>5 to 8<br>8 to 16 |          | 6<br>8<br>10 |        |                          |   |  |
| Single V<br>(without backing)<br>Weld from one<br>side or both   |                      | 5 to 12<br>over 12          | 60<br>60 | 2<br>2       | 1<br>2 |                          |   |  |
| Single V<br>(with backing;<br>backing temporary<br>or permanent) |                      | >10<br>>10                  | 45<br>20 | 6<br>10      | 0<br>0 | Single run<br>Double run |   |  |
| Double V welded<br>from both sides                               |                      | >12                         | 60       | 3            | 2      |                          |   |  |

Fig. 24.1 Butt weld preparation from BS 5153, Table 5

| Weld type  | Shape of preparation   | Dimensions in mm |                               |   |   |   |   |
|--|--|------------------|-------------------------------|---|---|---|---|
|  |  | T                | $\alpha$                      | G | R | r | L |
| Double V<br>asymmetric,<br>welded from<br>both sides |  | >12              | $\alpha = 60$<br>$\beta = 60$ | 3 | 2 |   |   |
| Single U   |  | >20              | 20                            | 0 | 5 | 5 |   |
| Double U   |  | >40              | 20                            | 0 | 5 | 5 |   |
| Double U<br>Asymmetric                               |  | >30              | 20                            | 0 | 5 | 5 | 6 |

| Weld type                              | Shape of preparation | Dimensions in mm |          |   |   |   |   |  |
|--|----------------------|------------------|----------|---|---|---|---|--|
|  |                      | T                | $\alpha$ | G | R | r | L |  |
| Single J,<br>welded both<br>sides      |                      | >20              | 20       | 0 | 5 | 5 | 5 |  |
| Double J,<br>welded from<br>both sides |                      | >40              | 20       | 0 | 5 | 5 | 5 |  |
| Single bevel<br>welded both<br>sides   |                      | 5 to 12          | 45       | 3 | 1 |   |   |  |
| Double bevel<br>welded both<br>sides   |                      | >12              | 45       | 3 | 2 |   |   |  |

Fig. 24.1 Continued

**Table 24.1** Throat thickness of fillet welds (from BS 5135, Table 14)

| Angle between fusion faces (degrees) | Factor (to be applied to the leg lengths) |
|--------------------------------------|---|
| 60 to 90                             | 0.7                                       |
| 91 to 100                            | 0.65                                      |
| 101 to 106                           | 0.6                                       |
| 107 to 113                           | 0.55                                      |
| 114 to 120                           | 0.5                                       |

the weld with the fusion faces. This by definition is the throat thickness. For welds with an angle less than 90° between the fusion faces, for which the defined distance would be greater than that for a right angle weld, there is an upper limit to the factor of 0.7. Similarly in the case of welds of unequal leg lengths the assumed throat thickness is not to exceed 0.7 multiplied by the shorter of the two legs (Fig. 24.2).

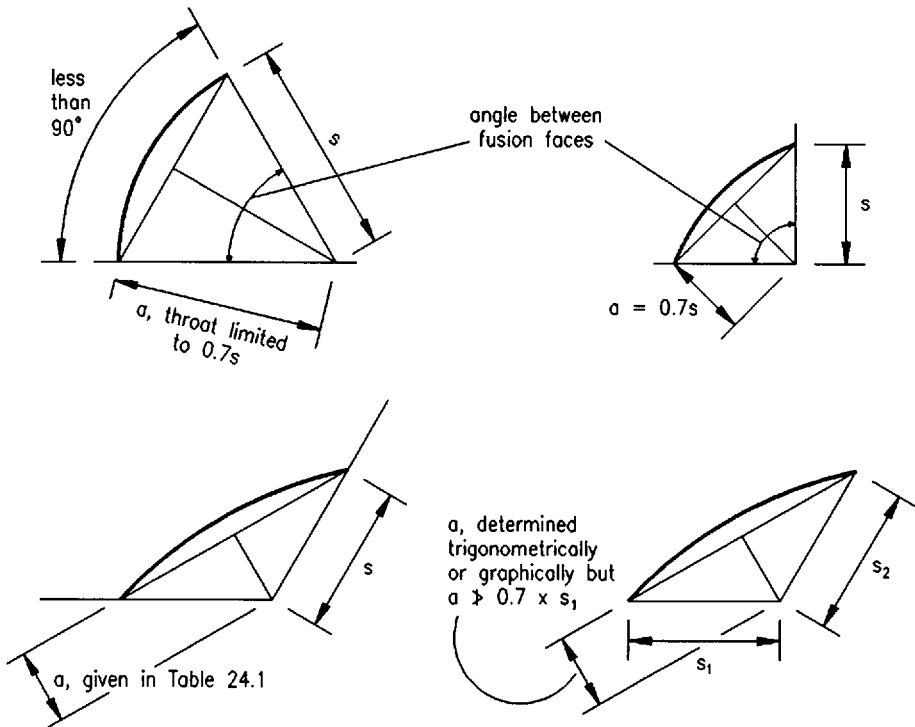


Fig. 24.2 Throat thickness of fillet welds



### **24.2.2 Effective lengths**

The effective length of a fillet weld is the actual length less twice the leg length to allow for the starting and stopping of the weld. It should not be less than four times the leg length. When a fillet weld terminates at the end or edge of a plate it should be returned continuously round the corner for a distance of twice the leg length.

Intermittent fillet welds are laid in short lengths with gaps between. They should not be used in fatigue situations or where capillary action could lead to the formation of rust pockets. The effective length of each run within a length is calculated in accordance with the general requirements for fillet welds.

### **24.2.3 Spacing limitations**

The longitudinal spacing between effective lengths of weld along any edge of an element should not exceed 300 mm or  $16t$  for compression elements, where  $t$  is the thickness of the thinner part joined.

## **24.3 Methods of analysis of weld groups**

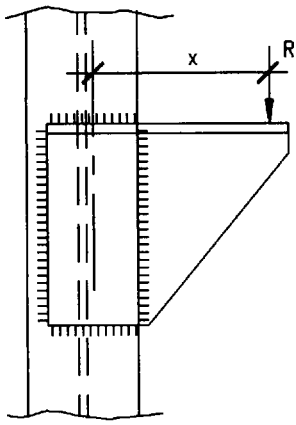
### **24.3.1 Introduction**

Any weld group may be required to resist an applied load acting through the centroid of the group either in or out of plane producing shear or tension respectively. The load may also be applied eccentrically producing in addition bending tension or torsional shear. Examples are given in Fig. 24.3.

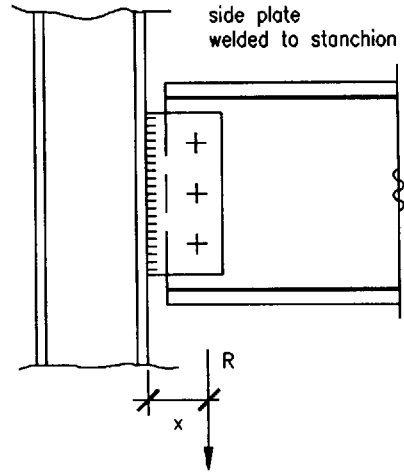
### **24.3.2 Weld groups loaded in shear**

British and Australian practice is to distribute the torsional shear due to eccentricity elastically in proportion to the distance of each element of the weld from the centroid of the group. This is referred to as the polar inertia method.

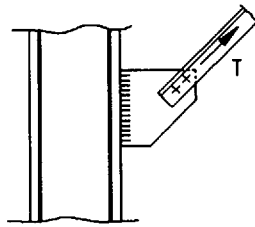
In some countries, notably Canada and in some cases the USA, the instantaneous centre method, referred to in Chapter 23 for bolt groups, is also used for weld groups.



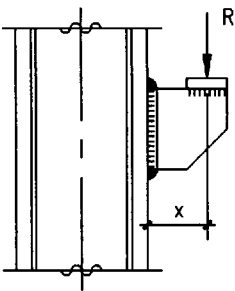
(a)



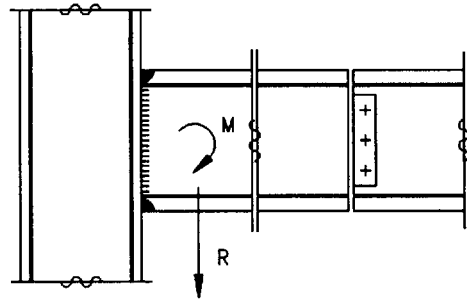
(b)



(c)



(d)



(e)

Fig. 24.3 Weld groups loaded eccentrically

*The polar inertia method*

Consider the four-sided weld group shown in Fig. 24.4(a). Assume the throat thickness is unity.

$$I_{xx} = \frac{2b^3}{12} + 2a \left(\frac{b}{2}\right)^2$$

$$I_{yy} = \frac{2a^3}{12} + 2b \left(\frac{a}{2}\right)^2$$

$$I_{00} = I_{xx} + I_{yy}$$

$$I_{00} = \frac{b^3 + 3ab^2 + 3ba^2 + a^3}{6}$$

Distance  $r$  to extreme fibre Fig. 24.4(b)

$$r = \frac{1}{2} \sqrt{(a^2 + b^2)}$$

$$Z_{00} = \frac{b^3 + 3ab^2 + 3ba^2 + a^3}{3 \sqrt{(a^2 + b^2)}}$$

By similar reasoning to that given in Chapter 23 for bolts,  $f_m$ , the force vector per unit length from the moment, is

$$f_m = \frac{Rxr}{Z_{00}}$$

$f_v$ , the shear, is assumed uniformly distributed around the weld group

$$f_v = \frac{R}{2a + 2b}$$

The resultant force vector per unit length,  $f_r$ , may be determined as shown in Fig. 24.4(c) either graphically or trigonometrically

$$\tan \alpha = b/a$$

$$f_r = \sqrt{[(f_m \cos \alpha + f_v)^2 + (f_m \sin \alpha)^2]}$$

The value  $f_r$  can then be compared with the strength of the weld proposed from the three tables in the Appendix *Capacities of fillet welds* as appropriate.

**24.3.3 Weld groups loaded in shear and tension/compression**

Weld groups loaded in shear and bending (tension/compression), such as crane brackets or portal knee joints, are dealt with in Chapter 26.

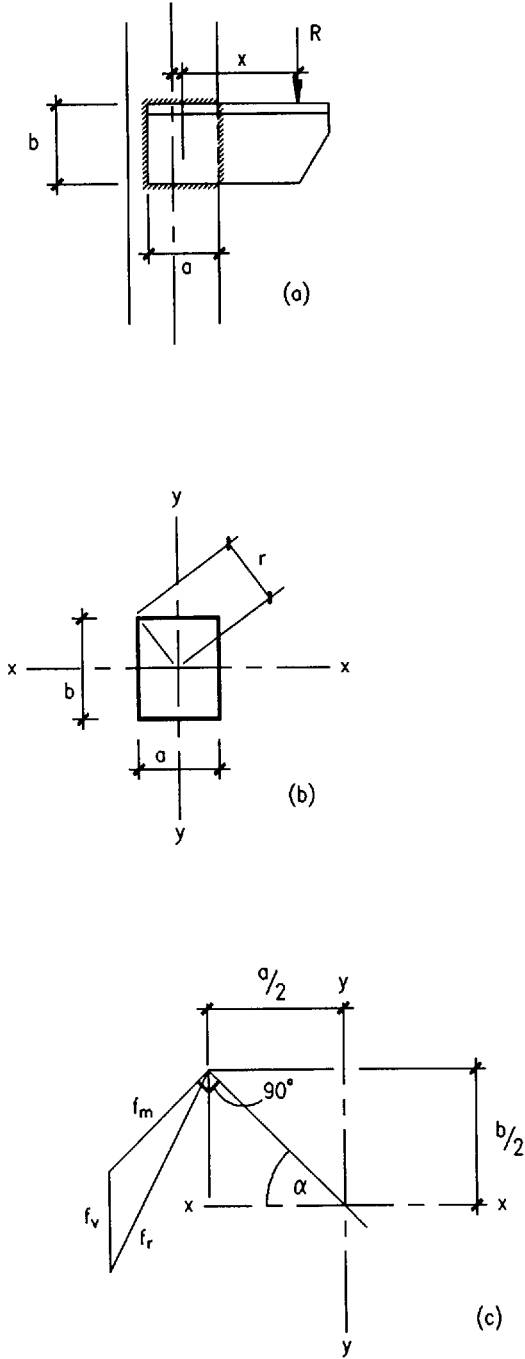


Fig. 24.4 Weld groups loaded in shear

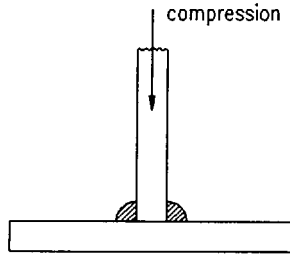


Fig. 24.5 Weld in compression

## 24.4 Design strengths

### 24.4.1 General

In fillet-welded joints which are subject to compression forces as shown in Fig. 24.5, it should not be assumed, unless provision is made to ensure this, that the parent metal surfaces are in bearing contact. In such cases the fillet weld should be designed to carry the whole of the load.

Single-sided fillet welds should not be used in cases where there is a moment about the longitudinal axis: see Fig. 24.6 and clause 6.6.2.4 of BS 5950. Ideally they should not be used to transmit tension.

A further limitation for fillet welds with unequal leg lengths, deep penetration fillet welds or partial penetration butt welds with superimposed fillet welds, is that the shear and tension on the fusion line should not exceed  $0.7p_y$  and  $1.0p_y$  respectively (clause 6.6.5.5 of BS 5950).

### 24.4.2 Strength

The design strengths of fillet welds when electrodes complying with BS 639<sup>2</sup> have been used and the parent metal complies with BS EN 10025 are given in Table 24.2 which is reproduced from BS 5950.

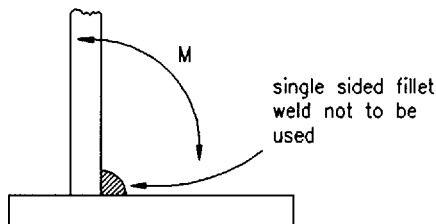


Fig. 24.6 Weld with moment

**Table 24.2** Design strength of fillet welds

| Grade steel to BS 4360 | Design strength, $P_w$       |                             |  | Other types <sup>b</sup><br>(N/mm <sup>2</sup> ) |
|------------------------|------------------------------|-----------------------------|--|--|
|                        | Electrode strength to BS 639 |                             |  |  |
|                        | E43<br>(N/mm <sup>2</sup> )  | E51<br>(N/mm <sup>2</sup> ) | E51 <sup>a</sup><br>(N/mm <sup>2</sup> ) |  |
| 40 or 43               | 215                          | 215                         | —  | 0.5 $U_e$ but<br>$\leq 0.54U_s$                  |
| WR50 and 50            | 215                          | 255                         | —  |  |
| 55                     | —                            | 255                         | 275                                      |  |

<sup>a</sup> Only applies to electrodes having minimum tensile strength of 550 N/mm<sup>2</sup> and a minimum yield strength of 450 N/mm<sup>2</sup>

<sup>b</sup>  $U_e$  = minimum tensile strength of electrode based on all weld tensile tests to BS 709<sup>4</sup>  
 $U_s$  = minimum ultimate tensile strength of the steel

Three tables in the Appendix *Capacities of fillet welds* show fillet weld capacities using appropriate strengths of 215 N/mm<sup>2</sup>, 255 N/mm<sup>2</sup> and 275 N/mm<sup>2</sup> respectively.

**References to Chapter 24**

1. British Standards Institution (1984) *Specification for arc welding of carbon and carbon manganese steels*. BS 5135, BSI, London.
2. British Standards Institution (1986) *Specification for covered carbon and carbon manganese steel electrodes for manual metal arc welding*. BS 639, BSI, London.
3. British Standards Institution (1990) *Specification for weldable structural steels*. BS EN 10025, BSI, London.
4. British Standards Institution (1983) *Methods of destructive testing of fusion welded joints and weld metal in steel*. BS 709, BSI, London.

**Further reading for Chapter 24**

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Owens G.W. & Cheal B.D. (1989) *Structural Steelwork Connections*. Butterworths, London.

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## Chapter 25

# Plate and stiffener elements in connections

by BRIAN CHEAL

### 25.1 Dispersion of load through plates and flanges

Where loads (or reactions) are applied to the flanges of beams, columns or girders the web adjacent to the flange must be checked for its local bearing capacity. The effective length of web to be used for checking the bearing capacity is obtained by assuming a dispersion of the load through the plates and flanges. Generally the dispersion to find the *stiff bearing length* is taken at an angle of  $45^\circ$  through solid material as shown in Fig. 25.1(a) and (b).<sup>1</sup> The dispersion depends upon the local bending resistance of the plate and so the dispersion can only occur when there is some restraint to balance the bending moment. For example, in Fig. 25.1(c) where the loose pack is not symmetrical about the point of application of the load, the  $45^\circ$  dispersion should not be taken through the pack.

In the case of a flange which is integral with or is connected to the web a greater angle of dispersion at a slope of 1:2.5 to the plane of the flange is allowed.<sup>1</sup> The dispersion of 1:2.5, taken to the web-to-flange connection, has been verified by tests with loads applied to columns, remote from the column ends. It can also be established by calculation, assuming that at failure the web

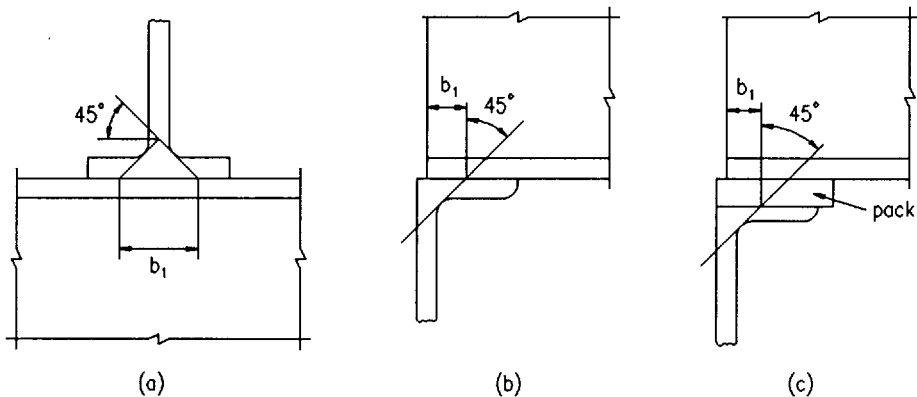


Fig. 25.1 Dispersion of load,  $b_1$  = stiff bearing length

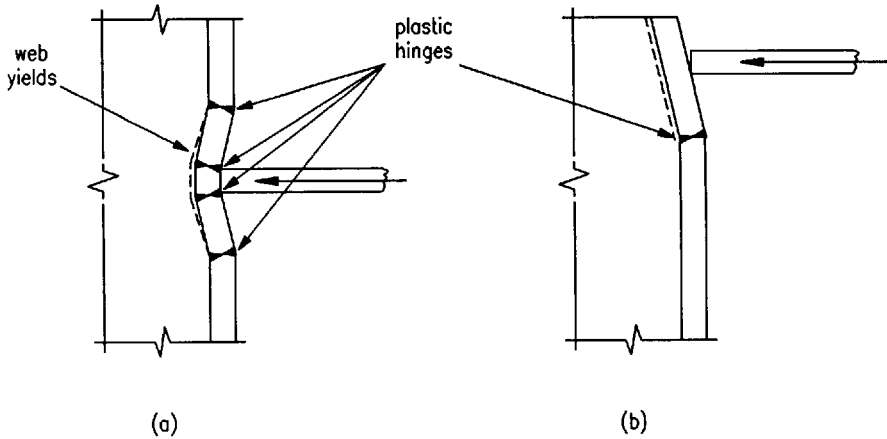


Fig. 25.2 Failure mechanism of flange

crushes and four plastic hinges form in the flange (Fig. 25.2(a)). The theoretical formula that is obtained is given in the draft Eurocode 3:<sup>2</sup>

$$P = (b_1 + n)t p_{yw} / \gamma_{M1}$$

in which the length due to dispersion ( $n$ ) is given as (Fig. 25.3):

$$n = 2T(B/t)^{\frac{1}{2}} (p_{yf}/p_{yw})^{\frac{1}{2}} [1 - (f_a/p_{yf})^2]^{\frac{1}{2}}$$

where  $P$  = crushing resistance of the web,

$b_1$  = length of stiff bearing,

$t$  = thickness of web,

$B$  = width of flange, but not greater than  $25T$ ,

$T$  = thickness of flange,

$p_{yf}$  = yield stress of flange,

$p_{yw}$  = yield stress of web,

$f_a$  = longitudinal stress in the flange,

$\gamma_{M1}$  = partial safety factor.

Conventionally for rolled sections dispersion has been taken to the K-line, i.e. through a distance equal to the flange thickness ( $T$ ) plus the flange to web root radius ( $r$ ). To adjust the formula to this practice the minimum value of  $T(B/t)^{\frac{1}{2}}$  in terms of  $(T + r)$  for rolled sections is substituted in the equation, i.e.  $T(B/t)^{\frac{1}{2}} = 2.5(T + r)$ , hence the 1:2.5 dispersion.

If the load is applied near the end of a beam or column (Fig. 25.2(b)) only one plastic hinge can be assumed to form in the flange, compared to the two hinges each side of the load in the columns tested; the allowable dispersion will be less than 1:2.5 and until further research is carried out the standard dispersion of 45° should be taken.



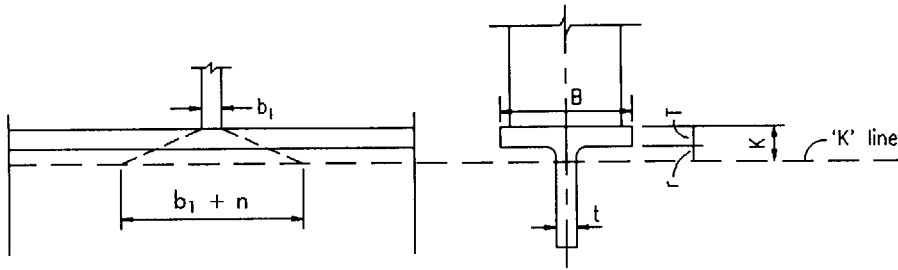


Fig. 25.3 Dispersion of load through flange

Compared with British and American sections European sections have a relatively larger root radius and the simplification of a 1:2.5 dispersion does not apply.

Where there are axial stresses in a flat plate the plastic bending moment capacity is reduced. As the dispersion depends upon the bending capacity of the flange, when there are relatively high longitudinal stresses in the flange caused by axial load and bending moments the angle of dispersion will be significantly reduced. To allow for this effect the 1:2.5 spread should be modified to  $1:2.5\sqrt{\mu}$ , where  $\mu = 1 - (f_a/p_y)^2$  and  $f_a$  = average longitudinal stress in the flange. This modification is included in the formula in the draft Eurocode 3.<sup>2</sup>

## 25.2 Stiffeners

### 25.2.1 General

At connections to beams and columns web stiffeners are provided where compressive forces applied through a flange by loads or reactions exceed the buckling resistance of the unstiffened web, or where the compressive or tensile forces applied through the flange exceed the local capacity of the web at its connection with the flange. They may also be provided to stiffen the flange where it is inadequate in bending, e.g. in a bolted tension connection.

### 25.2.2 Outstand of stiffeners

For flat stiffeners the outstand from the face of the web should not exceed  $19t_s\varepsilon$ , where  $t_s$  is the thickness of stiffener and  $\varepsilon = (275/p_y)^{1/2}$ ; but a maximum of  $13t_s\varepsilon$  should be used for the design of the stiffeners. The limit of  $13t_s\varepsilon$  corresponds to a semi-compact section in Table 7 of BS 5950: Part 1.

### 25.2.3 Buckling resistance

The buckling resistance of a stiffener should be based on the compressive strength of a strut using Table 27(c) in BS 5950: Part 1, the radius of gyration being taken about the axis parallel to the web. The effective section is the area of the stiffener together with an effective length of web on each side of the centreline of the stiffener limited to 20 times the web thickness. The effective length of the strut is taken as  $0.7L$  (where  $L$  is the length of the stiffener) provided that the flange is restrained against rotation in the plane of the stiffener and that the stiffener is fitted or welded to the flange so that the restraint is in fact applied to the stiffener. Where the stiffener is not so restrained the effective length is taken as  $L$ . These effective lengths assume that the flange through which the load or reaction is applied is effectively restrained against lateral movement relative to the other flange. If this is not so the stiffener should be designed as part of the compression member applying the load, and the design of the connection should include the moments due to strut action (see BS 5950: Part 1, clause 6.1.7.2 and Appendix C.3).

### 25.2.4 Local bearing

Web stiffeners are often *sniped* (the internal corners are cut) to clear the root radius or the web-to-flange welds. Since this reduces the effective bearing area of the stiffeners, it is necessary to check the local bearing capacity.

For the design of stiffeners where the web alone would be inadequate in bearing, and for the design of tension stiffeners, BS 5950: Part 1 allows the stiffeners to be designed to carry the applied load or reaction less the load capacity of the web without stiffeners.

In a compression detail, when stiffeners are used, a greater proportion of the load is initially carried by the stiffeners and it may well be advisable to limit the dispersion to  $45^\circ$  when calculating the portion of load carried by the web. This reservation follows from the stiffener outstand limitation being for a semi-compact section which by definition has limited ductility. Alternatively, the full 1:2.5 dispersion can be used with the compact criteria limitation  $b \nlessgtr 8.5t_s \epsilon$  applied to the stiffener outstand. In the case of a tensile load the potential problem is that the fillet welds attaching the stiffeners to the flange have limited ductility. To overcome this problem, for a pair of symmetrical fillet welds, the leg length of the fillet welds should be not less than  $0.85t_s$  for grade 43 steel and  $1.0t_s$  for grade 50 steel, or the welds can be designed for a net load based on the  $45^\circ$  dispersion. BS 5950: Part 1 also requires that the area of the stiffener in contact with the flange should be greater than  $0.8F_x/p_{ys}$ , where  $F_x$  is the external load or reaction and  $p_{ys}$  is the design strength of the stiffener.

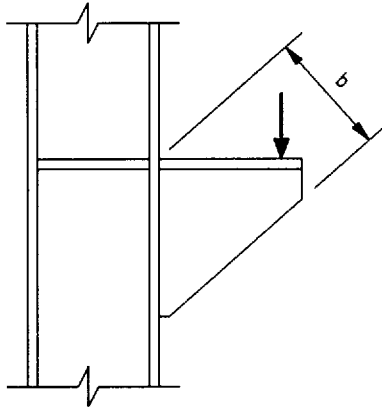


Fig. 25.4 Column bracket

### 25.2.5 Bracket stiffeners

The outside edge of the welded column bracket, shown in Fig. 25.4, is in compression and provided that a reasonably conservative approach is used in calculating the extreme fibre stress, semi-compact criteria for the outstand are appropriate (i.e.  $b \gtrsim 13t_s \epsilon$ ). With relatively light loads, this may require an unnecessarily thick stiffener. To overcome the problem, the simple design approach of substituting  $f_a$  for  $p_y$  in the formula for  $\epsilon$ , so that  $b \gtrsim 13t_s (275/f_a)^{1/2}$ , where  $f_a = 1.5 \times$  the extreme fibre compressive stress (at factored loading), can be used.

## 25.3 Plates loaded perpendicular to their plane

### 25.3.1 Prying forces

Where bolts are used to carry tensile forces they almost invariably connect together plates or flanges which flex in bending and are as a result subject to prying action. This prying action is best illustrated by considering a tee-connection (Fig. 25.5). When the flange of the tee is relatively flexible it bends under the applied load and the flanges outside the bolts are pressed against the supporting plate. The reactions generated at the points of contact are referred to as prying forces. For equilibrium, the total force in the bolts must equal the applied force plus the prying forces. Only when the flange is very stiff, with no plastic deformation so that its flexural deformation is small relative to the elongation of the bolts, will the prying forces be insignificant.

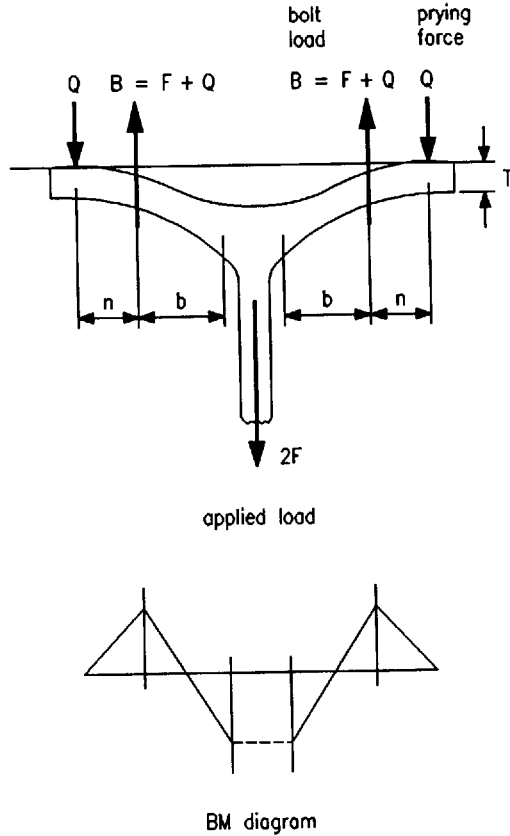


Fig. 25.5 Tee-connection prying forces

A number of semi-empirical formulae for calculating the prying forces have been published. A study of these formulae showed that although for a particular narrow range of connections they gave similar values for the prying forces, for other proportions of connection they gave very different values. Nowadays, the design procedure generally used assumes that a plastic hinge forms at the root and if required at the bolt line allowing the designer to select any suitable value for the prying forces. This design procedure is adopted in CIRIA Technical Note 98, BS 5400: Part 3 and the draft Eurocode 3.<sup>3,4,2</sup>

With this simple design procedure, due to the ductility of the plate in bending, the design will be adequate as far as strength is concerned. However, the ductility of the bolts may be limited, or plastic strain of the bolts may lead to an unacceptable loss of preload in the case of HSFGB bolts or to a loose nut with ordinary bolts. A limitation is placed on the distance  $n$  from the centreline of the bolt to the point at which the prying force,  $Q$ , is assumed to act, so that the bolt will not be required to stretch by an unacceptable amount to

accommodate the elastic curvature of the plate. The following rule has been proposed for determining the distance  $n$ :<sup>5</sup>

$n$  = distance from the centreline of the bolt to the edge of the plate or supporting plate if this is less

$$\text{but } \nless 1.1T \sqrt{\left(\frac{\beta p_0}{p_y}\right)}$$

where  $p_0$  = minimum proof stress of bolt,

$p_y$  = yield stress of steel in the plate,

$\beta$  = 1.0 for preloaded bolts

2.0 for non-preloaded bolts,

$T$  = thickness of flange of tee.

For practical design, where HSFG (or grade 8.8) bolts are used, with grade 43 or grade 50 plate, the limitation on  $n$  may be taken as  $n \nless 1.5T$  for preloaded bolts and  $n \nless 2.0T$  for non-preloaded bolts.

It is sometimes convenient for the designer to increase the plate thickness, so that the moment at the root can be increased with a corresponding decrease in the moment at the bolt line and a reduction in the prying force. This is another situation where it is possible that the bolt could be required to stretch by an unacceptable amount to accommodate the plate flexure assumed in the design. To safeguard against the possibility it has been suggested that the prying force,  $Q$ , should not be taken as less than that calculated from the following formula:<sup>5</sup>

$$Q = \frac{b}{2n} \left( F - \frac{\beta \gamma p_0 w T^4}{27nb^2} \right)$$

where  $b$  = distance from centreline of bolt to toe of fillet weld (or weld reinforcement) for a welded tee, or to half the root radius for a rolled section,

$n$  = distance from centreline of bolt to point where the prying force is assumed to act (as defined above),

$w$  = effective length of flange per bolt,

$T$  = thickness of flange of tee,

$F$  = applied load per bolt,

$p_0$  = minimum proof stress of bolt,

$\beta$  = 1.0 for preloaded bolts

2.0 for non-preloaded bolts,

$\gamma$  = 1.0 for working load design

1.5 for limit state design (with factored loads).

When  $\frac{\beta \gamma p_0 w T^4}{27nb^2}$  is greater than  $F$ , the prying force derived by the above formula

should be taken as zero (i.e.  $Q = 0$ ). The units of  $\frac{\beta \gamma p_0 w T^4}{27nb^2}$  must be consistent with the units of  $F$ .

With minimum plate thickness design, when plastic hinges are assumed at the root and the bolt line, the above check for the minimum value of  $Q$  is not required since for equilibrium

$$Q = (b/2n) F.$$

In the formulae for prying force,  $Q$ , and the limitation of the distance  $n$ , preloaded bolts may be considered as 'non-preloaded' bolts if they are not required to contribute to the shear strength of the connection and fatigue, vibration and stiffness considerations do not apply.

BS 5950: Part 1 has two different rules for the design of bolts in tension.<sup>1</sup> If the bolts are used as ordinary bolts (i.e. they are not pretensioned to a specific preload) the allowable tensile strength, given in Table 32, is  $0.58U_f$  but  $\leq 0.83Y_f$  and in clause 6.3.6.2 it is specifically stated that prying action need not be taken into account. Ignoring the prying action is inconsistent with the general recommendations for the design of connections in clause 6.1.1 and can be shown to be unsafe as a general procedure. If the bolts are installed as 'friction grip fasteners' the allowable tensile capacity given in clause 6.4.4.2 is  $0.9P_0$  and the implication is that prying action should be included in determining the bolt load, although this is not specifically stated.

Because of the danger of an unsafe design, it is recommended that, when it can occur, prying action should always be taken into account. Since the bolt load is increased by the prying force it is reasonable to use a higher tension strength,  $p_t$ , than that in Table 32. A suitable approach is to use the formulae below from clause 14.5.3.3 of BS 5400: Part 3,<sup>4</sup> taking  $\gamma_m\gamma_{f3}$  equal to 1.1 instead of 1.32 to bring it into line with BS 5950.

$$p_t = \frac{\alpha_t}{\gamma_m\gamma_{f3}}$$

where  $\alpha_t$  is the lesser of  $0.7 \times$  minimum ultimate tensile stress, and either the yield stress or the stress at permanent set of 0.2% as appropriate.

That is,

$$p_t = 0.64U_f \quad \text{but} \leq 0.91Y_f$$

where  $Y_f$  is the specified minimum yield strength of the fastener, and  $U_f$  is the specified minimum ultimate tensile strength of the fastener.

It is generally considered that a higher safety factor should be used for bolts in tension than for members in tension. The reasons for this are, the importance of connections at the final collapse of a structure, the relatively lower ductility of the bolts and the fact that the actual distribution of loads in the bolts (in for example an end plate connection) will not be the same as the simplified distribution assumed for the design. In the above proposal the higher margin of safety is obtained by limiting  $\alpha_t$  to  $0.7U_f$  and taking  $\gamma_m\gamma_{f3}$  equal to 1.1.

For a grade 8.8 bolt, the tension capacity obtained by taking  $p_t = 0.64U_f$  is only 2% less than the tension capacity of  $0.9P_0$  which would apply if it were to be designed as a preloaded friction grip fastener in accordance with clause 6.4.4.2 of BS 5950: Part 1.

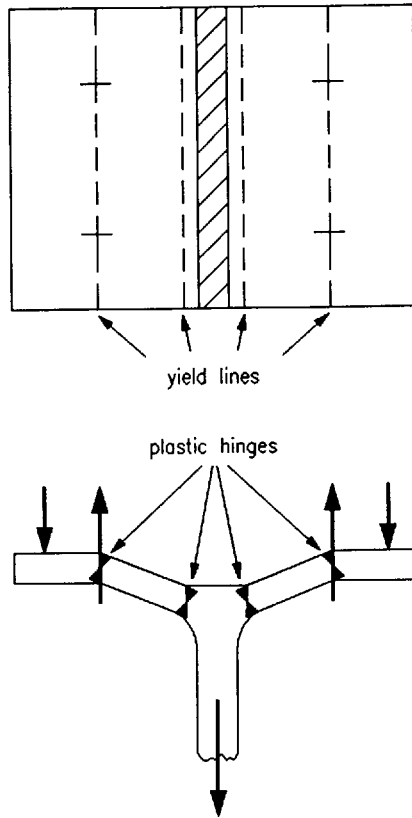


Fig. 25.6 Tee-connection yield lines

### 25.3.2 Short and long flanges

In a short tee-connection, provided that the capacity of the bolts is more than adequate, the maximum design capacity of the flange will be reached when parallel yield lines form at the connection of the flange to the supporting web and on the line of the bolts (Fig. 25.6). Alternatively, if the cross-section is considered, this can be stated in the terms used for plastic analysis, that the maximum design capacity will be reached when plastic hinges form at the flange-to-web connection and on the line of the bolts.

When the flange of the tee-connection is long (e.g. where it is part of the flange of a column and the detail is remote from the end of the column) the yield lines do not run to the end of the column but turn towards the edges of the flange (Fig. 25.7). The capacity of the flange can be assessed using yield line analysis. Five of the many possible yield line patterns are shown in Fig. 25.8. For a single bolt there is a mirror image of the yield line pattern on the right-hand side of the bolt; but if there is an adjacent bolt, there is a yield line linking the bolts with a parallel yield line adjacent to the web (Fig. 25.7).

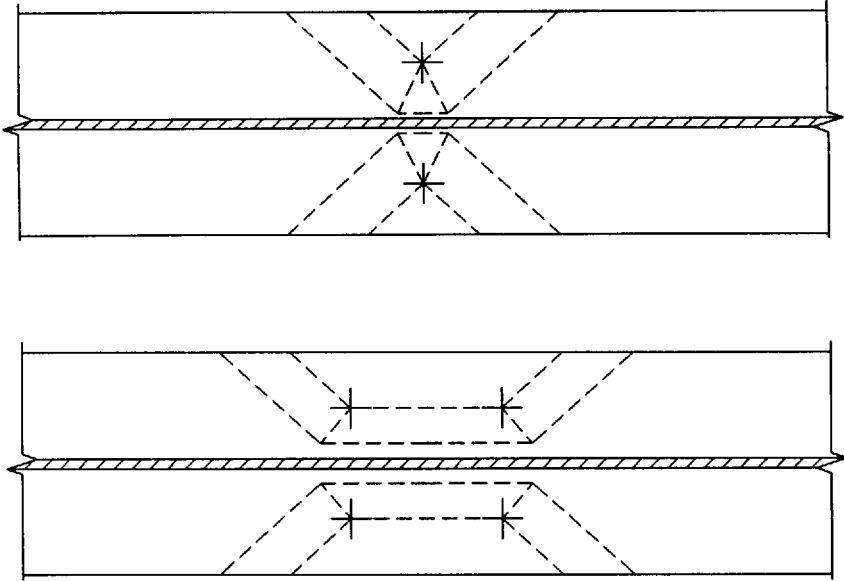


Fig. 25.7 Long flange yield lines

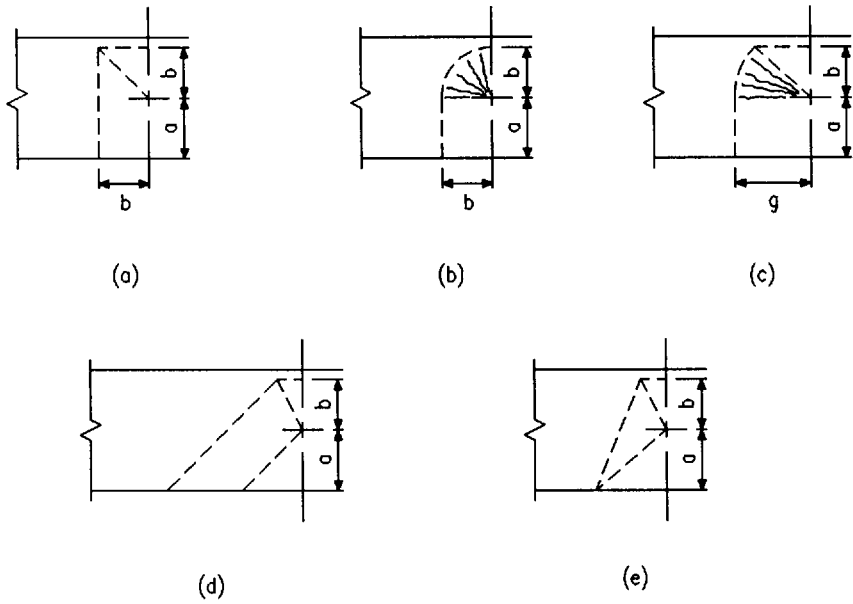


Fig. 25.8 Yield line patterns



Figure 25.8(a) shows a simple pattern with a 45° diagonal yield line; Fig. 25.8(b) is a modification of (a) with a fan yield line in the corner; Fig. 25.8(c) has a partial fan yield line at the corner (the dimension  $g$  being calculated to correspond to the minimum capacity of the pattern) and Fig. 25.8(d) and (e) are other patterns that have been proposed.<sup>5,6,7</sup>

The problem with the use of yield line analysis is that it is necessary to find the pattern which corresponds to, or is acceptably close to, the minimum capacity. It also requires a good working knowledge of the geometry of intersecting inclined planes (and cones where 'fan' yield lines are used). In view of this it is normal practice to use formulae based on yield line analysis. The most straightforward concept is to consider the formulae as giving the equivalent effective length of parallel yield lines so that the flange can be designed as an equivalent 'short flange' tee-connection. The equivalent lengths for the patterns in Fig. 25.8(a)–(e) are plotted in Fig. 25.9. The equivalent effective length derived from the yield line pattern in Fig. 25.8(d) is used for design since it corresponds to the minimum capacity for the practical range of values of  $a/b$ .

The equivalent length cannot be greater than  $\pi$  since this corresponds to another mode of failure which is a circular fan around the hole. If the effective value of  $a$  is limited to  $1.4b$ , in the formula corresponding to the pattern in

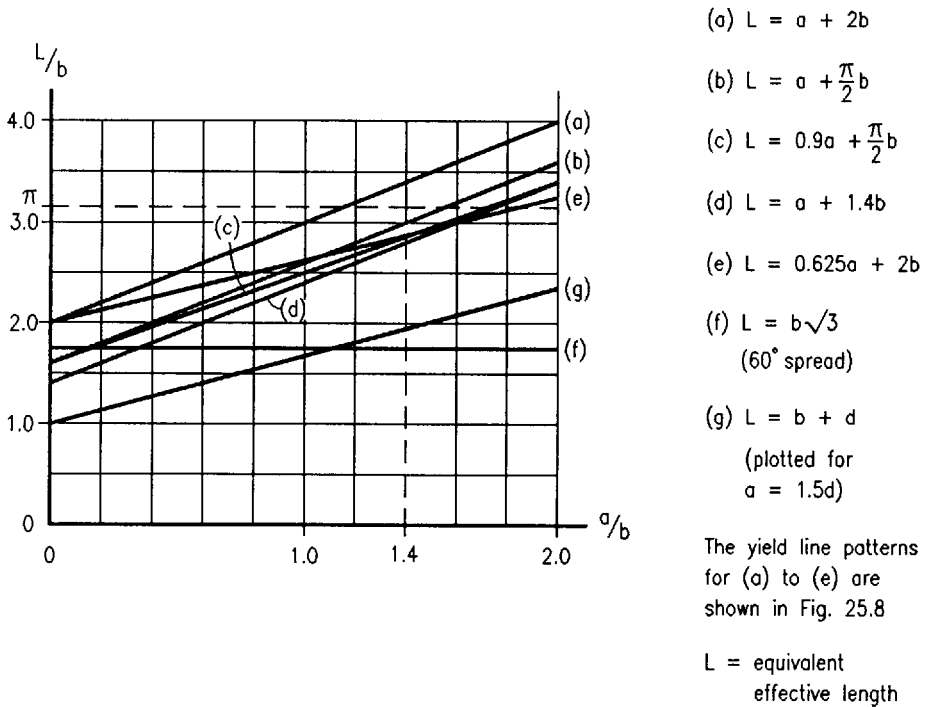


Fig. 25.9 Comparison of yield line patterns (graphs of  $L/b$  versus  $a/b$ )

Fig. 25.8(d), this covers the circular fan failure mode and also limits the deformation that can occur, before the full yield line pattern is formed, if large values of  $a$  relative to  $b$  are used in the formula.

The  $60^\circ$  maximum angle of spread used in BS 5400: Part 3 is shown as line (f) in Fig. 25.9. It can be seen that it is a good approximation for lower values of  $a/b$  (bearing in mind that  $a$  should not normally be less than  $b/3$ ) and although conservative for higher values it has the advantage of providing a relatively stiffer connection. The line for an effective length taken as the bolt diameter plus a  $45^\circ$  spread is shown as (g) in Fig. 25.9. This formula is used when formation of the full yield line pattern is not acceptable (e.g. when the connected tee or extended end plate is designed with yield lines at the bolt holes and for compatibility of the deformations and prying forces the column flange is designed as a short tee).

The prying forces, for a long flange tee calculated using the equivalent effective length, are higher than the theoretical values. However, as with many other instances in the design of structures where the theoretical analysis is simplified for practical design, it is considered that the advantages of a faster simpler approach to design outweigh the disadvantages. It is worth noting that one advantage of determining the prying force using the equivalent effective length is that it overcomes the difficult problem of determining how far the detail needs to be from the end of the column for the full 'long flange' pattern to develop.

### 25.3.3 Allowance for bolt holes

In some of the formulae and design procedures for the design of tee-connections and end plates, the holes are deducted when calculating the plastic moment of resistance; whereas in others the holes are ignored. In practice the bolt head (or nut) spreads the load from the bolt so that the bending moment diagram is modified. Some design procedures allow for this effect by moving the point of application of the bolt load to the edge of the hole, implying that there is bending in the bolt, which is not possible if the bolt is fully stressed in tension. A more straightforward approach is to use the extra capacity, due to the spreading of the load, to allow the bolt holes to be ignored in the design, while keeping the load applied on the centreline of the bolt. This is satisfactory provided that the effective length,  $w$ , of flange per bolt is greater than the distance,  $b$ , from the bolt line to the hinge at the root. When  $w < b/2$ , the hole should be deducted, with linear interpolation being used for intermediate cases.

### 25.3.4 Corner details

When the plate in a tension connection is supported on two adjacent sides, the yield line pattern for 'minimum capacity' incorporates fan yield lines (Fig. 25.10).

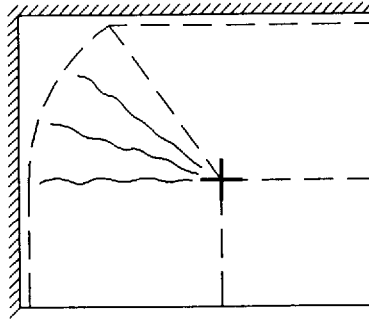


Fig. 25.10 Corner yield line pattern

A simple design approach, which allows for the various patterns that could occur in the corner, is to assume a yield line pattern with a diagonal line from the bolt to the corner; but to take only 70% of the lines in the corner as being effective (Fig. 25.11(a)). It can be shown that the diagonal yield line is equivalent to the projected yield lines on the perpendicular axes, so that the pattern with the diagonal line can be split into two parallel line patterns (Fig. 25.11(b)). This is convenient, because it not only simplifies the design of the flange plate, but it enables the bolt load to be divided between the supporting sides for the design of the supporting plates and welds.

For the collapse pattern associated with the yield lines, the load is divided between the supported sides in proportion to  $w/b$ . However, if the plate is thicker or its yield stress higher than the minimum required it can behave elastically and so change the distribution of the load. Normally, ductility takes care of this; but where fillet welds, which have limited ductility, transfer the load it is prudent to design them for the greater of the loads obtained by assuming that the distribution is proportional to  $w/b$  (plastic) or  $w/b^3$  (elastic).

It is a useful design point that if a simple pattern with a  $45^\circ$  diagonal yield line is assumed for the long flange case, with the corner yield lines only 70% effective, the equivalent effective length of  $a + 1.4b$  is obtained.

### 25.3.5 Summary

- (1) For minimum plate thickness assume plastic hinges (yield lines) at the web root and the bolt line (Fig. 25.6).
- (2) Where desired (to justify a smaller size of bolt), a smaller prying force can be assumed; but it is not advisable to assume a prying force,  $Q$ , less than that calculated using the formula in section 25.3.1.

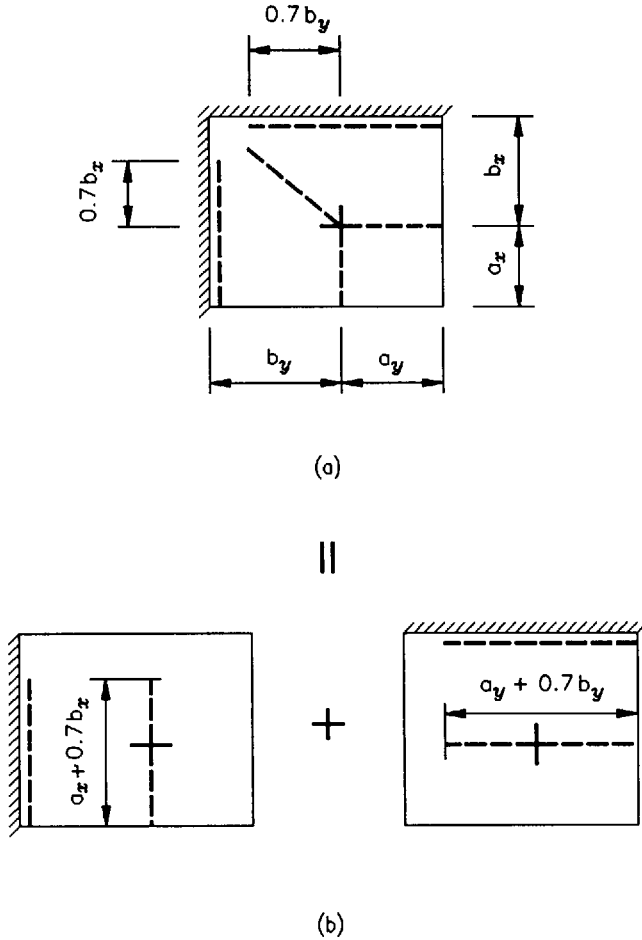


Fig. 25.11 Corner yield lines – equivalent pattern

- (3) Take the distance,  $n$ , from the centreline of the bolt to the point at which the prying force,  $Q$ , is assumed to act as the least of:
  - (a) the distance from the centreline of the bolt to the edge of the plate
  - (b) the distance from the centreline of the bolt to the edge of the supporting plate
  - (c)  $1.5T$  for preloaded bolts or  $2.0T$  for non-preloaded bolts (and preloaded bolts where some loss of preload would be acceptable); where  $T$  is the plate thickness.
- (4) Use the plastic modulus of the plate  $wT^2/4$ . The bolt holes may be ignored provided that the effective length,  $w$ , of flange per bolt is greater than the distance,  $b$ , from the bolt line to the hinge at the root.

(5) Calculate the effective length of plate associated with each bolt by taking, on each side of the bolt, the least of:

- (a) distance from the centreline of the bolt to the end of the plate
- (b)  $0.5 \times$  distance to the adjacent bolt
- (c)  $a + 1.4b$  (but  $\nless 2.8b$ )

where  $a$  = distance from centreline of bolt to edge of plate

$b$  = distance from centreline of bolt to toe of fillet weld (or weld reinforcement) for a welded detail, or half the root radius for a rolled section.

If stiffness is important, limit spread to  $60^\circ$  (i.e.  $1.73b$ ) instead of  $(a + 1.4b)$ .

For a fillet welded detail (which has limited ductility), when calculating the effective length of fillet weld, limit spread to  $d + b$ ; where  $d$  is the bolt diameter.

(6) For the purposes of design, when a plate is supported on two adjacent sides it may be considered as two independent 'cantilever' plates; but only 70% of the yield lines in the corner should be taken as being effective (see section 25.3.4).

For the design of the supporting 'plates' distribute the load in proportion to  $w/b$ .

For the design of fillet welds (which have limited ductility) design for the greater of the loads obtained by distribution in proportion to  $w/b$  or  $w/b^3$  and assume that the load is applied to the weld on the line of the bolt.

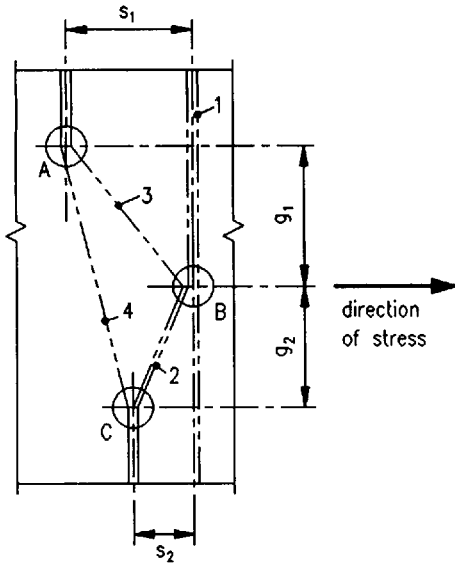
## 25.4 Plates loaded in-plane

### 25.4.1 Deductions for holes

Where holes are staggered the effective net section through the line of the holes is taken as the area of the gross cross section less a deduction of the area of the holes in any (zig-zag) section less  $s^2t/4g$  for each gauge space in the line of holes (Fig. 25.12);<sup>1</sup> where  $s$  is the bolt pitch in the direction of stress,  $t$  is the thickness of the material and  $g$  is the bolt gauge transverse to the pitch.

### 25.4.2 Gusset plates

The design of gusset plates can be carried out by developing separate rules for each of the possible modes of failure (e.g. in Fig. 25.13, failure on line A-F or failure by tearing out of the section G-C-D-H, etc.). A simpler procedure is normally adopted in which dispersion of the load is assumed and only transverse sections are checked in tension or compression (with the addition of bending



Deduction for holes equals greatest of:

- (1) Area of hole B
- (2) Area of holes B+C -  $\frac{s_2^2 t}{4g_2}$
- (3) Area of holes A+B+C -  $\frac{s_1^2 t}{4g_1} - \frac{s_2^2 t}{4g_2}$
- (4) Area of holes A+C -  $\frac{(s_1 - s_2)^2 t}{4(g_1 + g_2)}$

Fig. 25.12 Deduction factors

where appropriate). It is considered that 30° is a satisfactory maximum angle of dispersion.

The ratio of D-E to D-J is 0.577 (i.e.  $\tan 30^\circ$ ); if this is compared with the relationship between shear strength and tensile strength the reason why the check on B-E also covers the other modes of failure is apparent.

### 25.4.3 Notched beams

Although not absolutely clear in BS 5950: Part 1, it is normal practice to ignore bolt holes when checking the shear capacity of beams and channels. Other codes, such as the AISC specification, require a check allowing for the effect of the fastener holes.<sup>8</sup> In view of this, for a web without flanges (including beams and channels with one or both flanges notched) it is prudent to check against ultimate rupture of the detail:

$$\text{shear capacity, } P_v = 0.6p_y \times 0.9A_{ve}$$

where  $A_{ve} = K_e A_{vn}$  but  $\nless A_{vg}$

$A_{ve}$ ,  $A_{vn}$  and  $A_{vg}$  are the effective, net and gross areas and  $K_e$  is the factor defined in BS 5950: Part 1, clause 3.3.3.

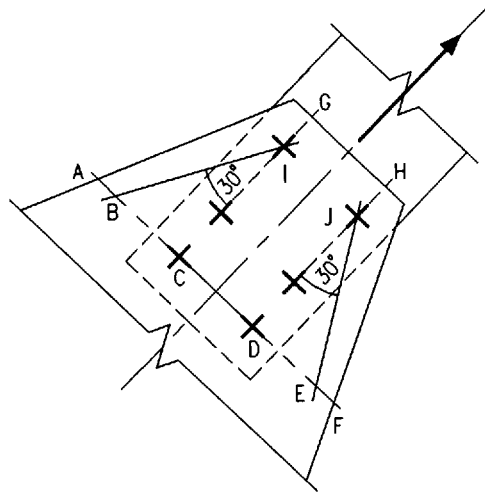


Fig. 25.13 Gusset plate load dispersion

Where, for example, the connection is concentrated toward the top of a notched beam a ‘block’ failure must also be considered; e.g. a tear-out failure along A–B–C in Fig. 25.14. In the light of test results, some allowance for the eccentricity of the reaction is made by taking a triangular stress distribution on B–C:<sup>9</sup>

$$\begin{aligned} \text{shear capacity, } P_v &= \text{shear capacity of A–B} + \text{tensile capacity of B–C} \\ &= 0.6p_y \times 0.9A_{vc(AB)} + 0.5p_yA_{vc(BC)} \end{aligned}$$

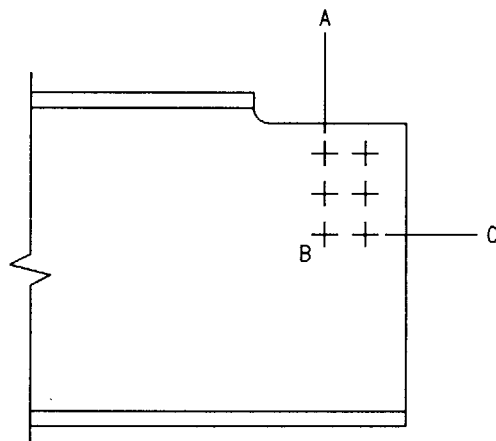


Fig. 25.14 Notched beam tear-out failure

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# Chapter 26

## Design of connections

by BRIAN CHEAL

### 26.1 Conceptual design of connections

#### 26.1.1 General

The design of the individual elements, the bolts, welds, plates and stiffeners, is described in Chapters 23, 24 and 25. For most connections the main problem to be dealt with is the determination of the distribution of forces, moments and stresses in the constituent elements. Other matters that need to be considered are the overall stiffness of the connection and the practical aspects of fabrication, erection and inspection.

#### 26.1.2 Load paths

In some simple details the distribution of forces in the elements of the connection is fairly obvious; but in more complex cases, such as the bolted end plates used for rigid beam-to-column connections, it is more difficult to ascertain the distribution of forces. The problem can be overcome by considering the load paths by which the applied moments and forces are carried through the connection. The principle is best illustrated by an example: the moment applied to the beam-to-column connection in Fig. 26.1 is replaced by a tensile force in the top flange and a compressive force in the bottom flange. The load paths taken by these forces through the various elements of the connection are illustrated in Fig. 26.2. The force in the tension flange is transmitted through

- (1) the flange to end plate fillet welds;
- (2) the end plate in bending;
- (3) the bolts in tension;
- (4) the column flange in bending;
- (5) the column flange to web fillet welds and the column web in tension and shear.

The force in the compression flange is transmitted through the end plate and column flange in bearing into the column stiffeners from whence it is transmitted by the fillet welds into the column web.

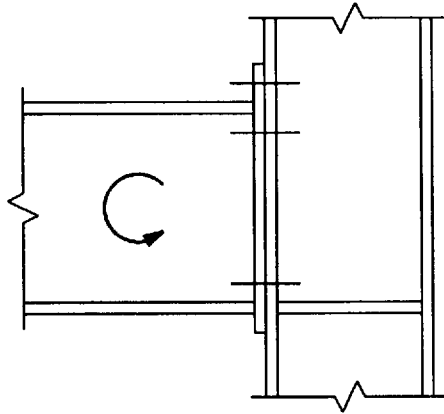


Fig. 26.1 Beam-to-column connection

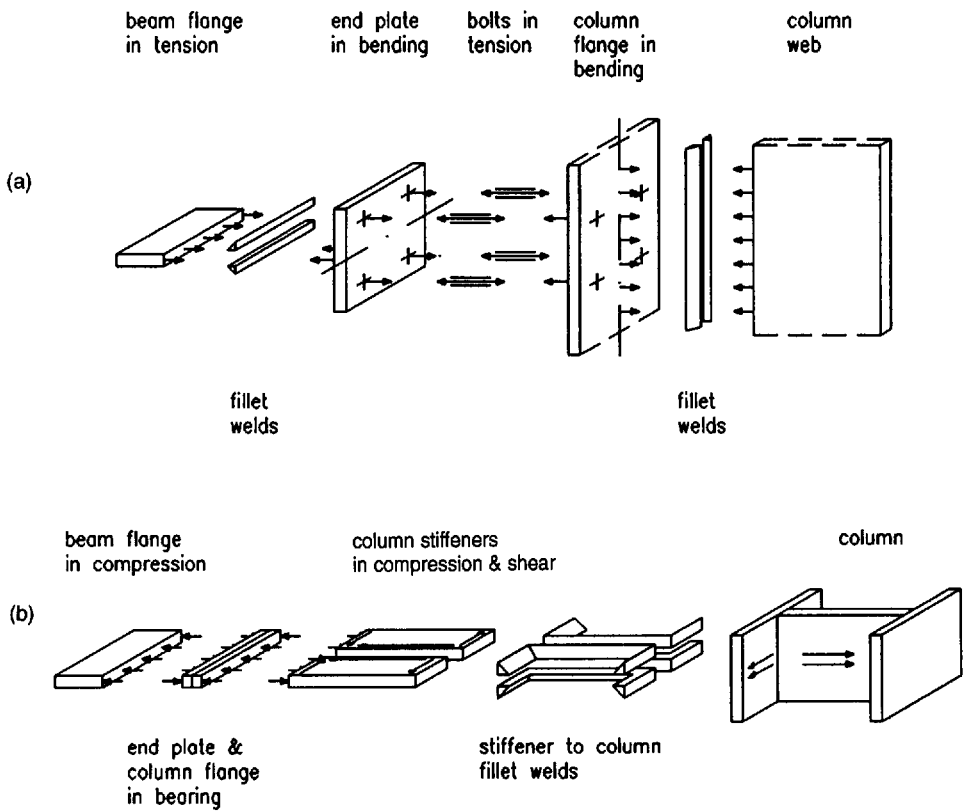


Fig. 26.2 Beam-to-column connection – load paths (a) at top flange, (b) at bottom flange

Every element in the chain that forms the load path must be adequate to carry the force being transmitted. In practice some of the elements in the load paths will be seen to be adequate by inspection and specific calculations will not be required. Nevertheless, the designer must be sure that there are no weak links in his detail.

### 26.1.3 Relative flexibility and hard spots

In the connection shown in Fig. 26.3(a), the applied moment is transmitted by compression in the lower part of the beam and by the bolts in tension in the upper part. The compression path is in direct bearing and is relatively much stiffer than the tension paths which include the end plate and the column flange in bending. Due to this difference in stiffness, the connection tends to rotate about the bottom flange; this assumption is usually made when choosing the load paths. At the stage of loading when the end plate and column flange are elastic they may be considered as springs. In practice the spring stiffnesses for the bolt positions vary with bolt spacing, are affected by the presence of the top flange (and column stiffeners if used) and by the partial formation of yield lines, and are further influenced by other variables such as lack of fit and variations in the preload of the bolts. For design these effects are generally ignored; the spring stiffnesses are assumed to be the same at each bolt and the tension in each bolt is then proportional to its distance from the point of rotation (Fig. 26.3(b)). There is one generally accepted modification to the distribution of bolt forces indicated in Fig. 26.3(b), which is used for the extended end plate detail where there is no

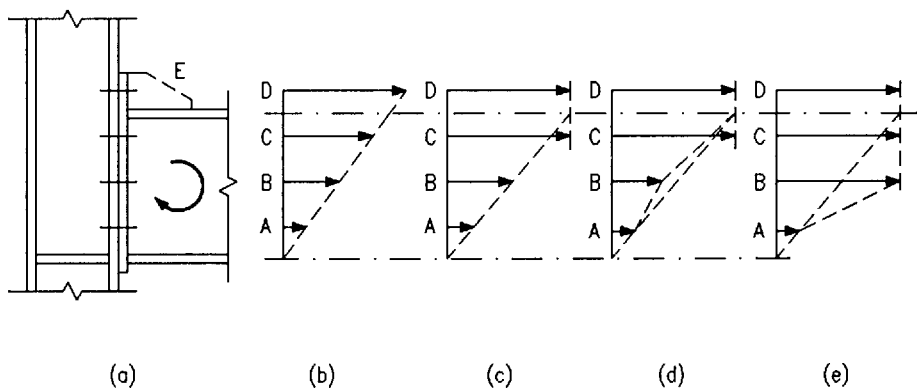


Fig. 26.3 Distribution of bolt loads

stiffener (E) above the tension flange (Fig. 26.3(a)). In this case equal forces are assumed in the bolts above and immediately below the flange as shown in Fig. 26.3(c). The reason for this modification is that the end plate below the flange (which is stiffened by the web of the beam) is stiffer than the cantilever portion of the end plate above the flange and tends to attract more load. The additional load due to stiffness is balanced against the effect of distance from the point of rotation.

Although the tension load paths are each associated with the pair of bolts at a given level, the strength of each load path is governed by the weakest link in the chain (i.e. bolts, welds, flange or end plate in bending or webs in tension). In some cases a small variation from the triangular distribution of forces may be reasonable. For example, if load path B is governed by the tension capacity of the web, the distribution in Fig. 26.3(d) can be used. The justification for this is that the web in tension has sufficient ductility to yield and allow the other load paths to reach their design capacity. On the other hand, if load path B is governed by the capacity of the fillet welds, the modification of the triangular distribution is not permissible because end fillet welds have very limited ductility. Compared with that shown in Fig. 26.3(d), the distribution shown in Fig. 26.3(e) is not generally acceptable because additional deformation at load paths C and D is required to allow the capacity assumed for load path B to be generated. This would reduce the overall stiffness of the connection.

#### 26.1.4 Ductility

It is clear that the stresses obtained by the load path analysis are unlikely to be the actual stresses that occur in the real connection. In fact, due to variables such as lack of fit, if two nominally identical connections are fabricated and tested the stresses are unlikely to be the same. What is required from the design of a connection is that the resulting detail will have adequate strength and stiffness or ductility. Stiffness is required for a fixed connection (and possibly ductility, although using a connection as a plastic hinge in the frame analysis is not recommended). Ductility is required for a simply-supported connection.

In a fixed connection, such as that shown in Fig. 26.3(a), provided that reasonable load paths are assumed, the ductility of the steel should accommodate any 'inaccuracy' in the load distribution used for analysis. For example, if one of the load paths is stiffer than implied by the triangular distribution, the load path will initially carry a greater proportion of load; but when the weakest element of the load path is fully stressed it will deform plastically and as the applied load is increased the distribution between the load paths will move towards that assumed in the design.

The elements in the load path will not have the same capacity for plastic deformation; this has to be kept in mind while carrying out the design. It is useful to consider the relative deformation capacities of the elements in the load path:

|  |  |
|--|--|
| Plates in bending  | Relatively large elastic deformation.<br>Large deformation capacity when plastic hinges form.            |
| Plates in tension (also plates in compression with 'plastic' cross-sections) | Small elastic deformation.<br>Reasonable plastic deformation.  |
| Butt welds   | Deformation occurs in plate adjacent to weld.  |
| Bolts  | Some plastic deformation (but deformation capacity dependent upon number of threads in the grip length). |
| Fillet welds   | End fillet welds have very little deformation capacity.  |

Due to the limited deformation capacity of end fillet welds care should be taken to avoid the possibility of their being subject to a load much greater than the design load. For example, in Fig. 26.1 the column flange could be designed as a long flange tee-connection using the full plastic collapse load. However, if the thickness of the flange is greater than the minimum required and/or the yield stress of the flange is greater than the minimum, the full yield line pattern will not form and there will be a higher load to be carried by the fillet welds near the bolts. To allow for this possibility it is reasonable to take a lesser spread of load when designing the fillet welds, for example, a maximum spread of the bolt diameter plus  $45^\circ$  from the centreline of the bolt.

### 26.1.5 Compatibility of design assumptions

Care is required to ensure that the assumptions made for the design of the various elements in the connection are compatible. For example, in a cover plate splice, sharing the load between ordinary bolts (in shear and bearing) and fillet welds is not acceptable. The reason for this is that the deformation characteristics of ordinary bolts and fillet welds are incompatible. The fillet welds are stiff compared with the bolts in clearance holes, and as the load is applied the welds will initially carry most of the load. Then, due to their limited ductility, the fillet welds will be liable to break before the bolts can take up their share of the load.

Another example of the need for compatibility is in the design of bolted tension connections where the two tees have their webs at right angles to each other. This is best understood by first of all considering the interaction of two short tees (Fig. 26.4). The shaded areas in Fig. 26.4(b) and (c) indicate where the two tees are in contact (ignoring elastic curvature) if they are attached to solid reaction plates and the crosses indicate where the prying forces required to generate the

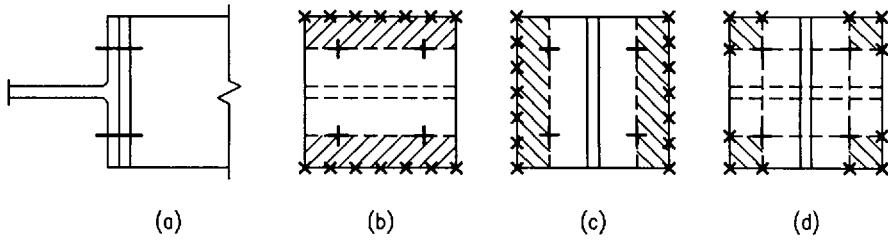


Fig. 26.4 Interaction of two short tees

yield lines through the bolts occur. Figure 26.4(d) shows the contact areas and the position of the prying forces for the two tees in Fig. 26.4(a), which is satisfactory. Now consider the interaction of a short tee with a long flange tee (Fig. 26.5). Using the same approach as for the two short tees, it can be seen that there are no common shaded areas and that, although prying forces can occur in suitable positions to generate the long flange yield line pattern, there are no prying forces to generate any yield lines through the bolt on the short tee. As shown in Fig. 26.5(e), the short tee is able to nest around the deformed shape of the long tee. The problem can be overcome either by designing the column flange as a long tee and the outstands of the short tee as simple cantilevers or by designing both parts as short tees. This is achieved by limiting the effective length of the tees, using a maximum spread of the bolt diameter plus  $45^\circ$ .

The above design provisions also apply to an extended end plate beam-to-column connection (Fig. 26.1), where the end plate at the top flange is in effect a short tee with its web (the beam flange) at right angles to the column web.

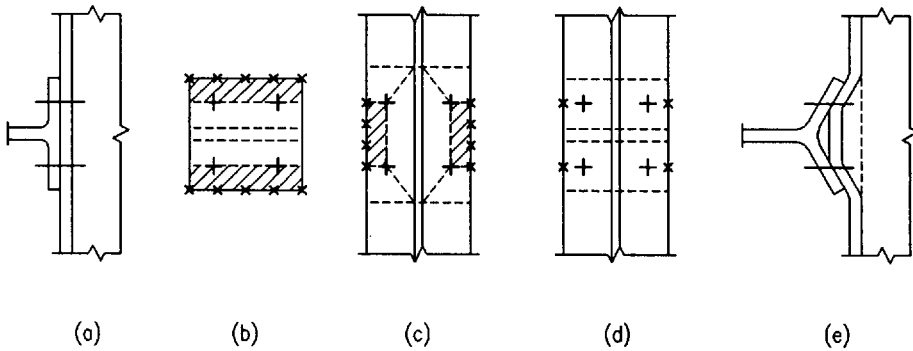


Fig. 26.5 Interaction of short and long tee

### **26.1.6 Stiffness**

One other aspect to be considered is the stiffness of the connection. This has to be acceptable with respect to the deflection of the structure, the overall and local stability, the analysis and the assumed distribution of forces and moments.

### **26.1.7 Summary**

Important points that must be kept in mind when designing connections are listed below:

- (1) The design of the connection should follow the assumptions made in the analysis of the frame or truss. Note that the forces and moments are related to the line diagram used in the analysis.
- (2) If fixed ended members are assumed in the analysis (e.g. in a lattice girder) the connections should be designed for the end moments as well as the axial forces. (Preferably analysis and design should assume pinned joints.)
- (3) Check whether any additional moment capacity is required to ensure stability (e.g. at a splice in the middle of a strut or beam).
- (4) Check that the load combinations taken in the analysis give the maximum forces for the connection design.
- (5) When choosing an analytical model of the connection, consider the effect of hard spots (in bearing) and the relatively more flexible plates (in bending) on the distribution of forces.
- (6) The load paths through the connection must be complete and in equilibrium and should be as direct as possible.
- (7) The elements in the connection must not only have adequate strength, but they must also have adequate ductility for the assumptions/simplifications made in the design to be satisfactory.
- (8) Wherever practicable, the centroidal axis of the splice material should coincide with the centroidal axis of the element joined.
- (9) Generally in lattice structures centroidal axes should intersect at the node points. Where they do not intersect the effect of the eccentricity should be allowed for in the design.
- (10) The load should not be shared between welds and fasteners of different stiffnesses.
- (11) The effects of lack of fit on the behaviour of the connection. Also the effect of the introduction of packs and shims. In particular beware of the effect of lack of fit on the fatigue life of the connection.
- (12) Avoid severe stress concentrations, particularly where fatigue could be a problem.
- (13) Consider the economics and ease of fabrication, erection and inspection. Allow adequate clearance for installation and tightening of fasteners (particularly HSFG bolts), welding, inspection and maintenance.

## 26.2 Types of connection

### 26.2.1 Column splices

#### 26.2.1.1 *General*

As well as providing continuity of strength, column splices are required to provide adequate continuity of stiffness about both axes. If a splice is near to a point of lateral restraint, and the strut is designed as pinned at that point, the splice is designed simply for the axial load and applied moments (if any). However, if the splice is away from a point of lateral restraint, or end fixity or continuity is assumed in calculating the effective length, the additional moments that can be induced by strut action must be taken into account. The procedure for calculating the additional moment is given in Appendix C.3 of BS 5950: Part 1.<sup>1</sup>

Where the web and flanges are spliced, the axial load can be shared between the web and the flanges in proportion to their areas. However, in bolted connections it is usual to assume that the bending moments are carried solely by the flanges.

#### 26.2.1.2 *Bolted cover plate splices*

The column ends are usually prepared for full contact, in which case compression forces may be transmitted in bearing. Alternatively the cover plates can be designed to carry all the loads and moments and full bearing need not be attained.

When the splice is near to the mid-point of the 'effective length' of the strut, the size of the flange cover plates should be not less than that of the associated flanges (of the lighter section where a change of section occurs) with respect to area and section modulus.

A typical splice is shown in Fig. 26.6(a). If the sections are of the same serial size but of different rolling weights, packs are required to make up the differences in flange thickness. If the two sections are of different serial size, some means, such as the division plate in Fig. 26.6(b), must be provided to transfer the bearing load between the flanges which are not in line.

#### 26.2.1.3 *Welded splices (primarily used for shop connections)*

Where the sections are of the same serial size, a full strength butt weld can be used (Fig. 26.7(a)). However, it is normally easier and cheaper to prepare the ends for full bearing and use partial penetration welds. Where the flanges do not line up, some provision must be made for transferring the flange forces (Fig. 26.7(b)).



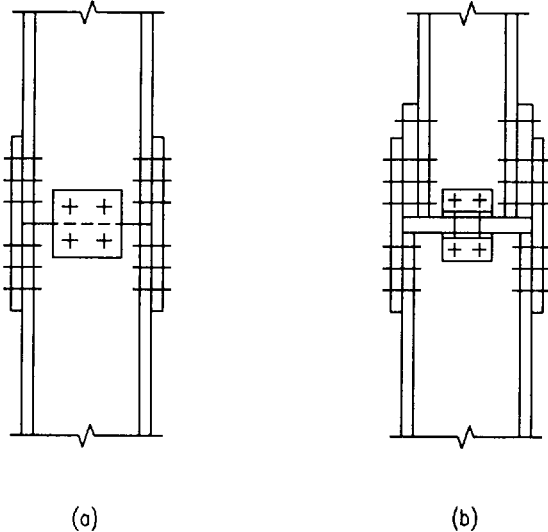


Fig. 26.6 Bolted column splices

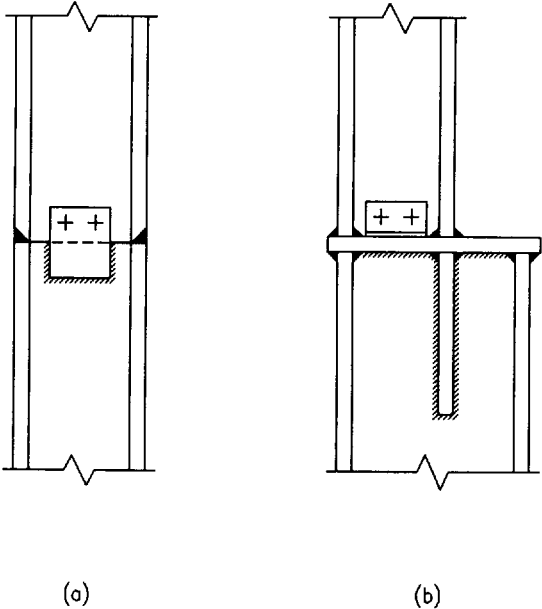


Fig. 26.7 Welded column splices

**26.2.2 Simple beam-to-column connections**

**26.2.2.1 Bolted seating cleats (Fig. 26.8(a))**

If the seating cleat is unstiffened, it is accepted practice to design the cleat-to-column connection for shear only. This assumes that there is a second cleat near the top flange of the beam and that the beam is connected to a column flange or to the web of a universal column. The detail is not suitable for the connection of a beam to a relatively flexible element such as the web of a plate girder or universal beam.

If the seating cleat is stiffened, the cleat-to-column connection should be designed for the eccentric moment as well as the shear. For a fully stiffened cleat, the load

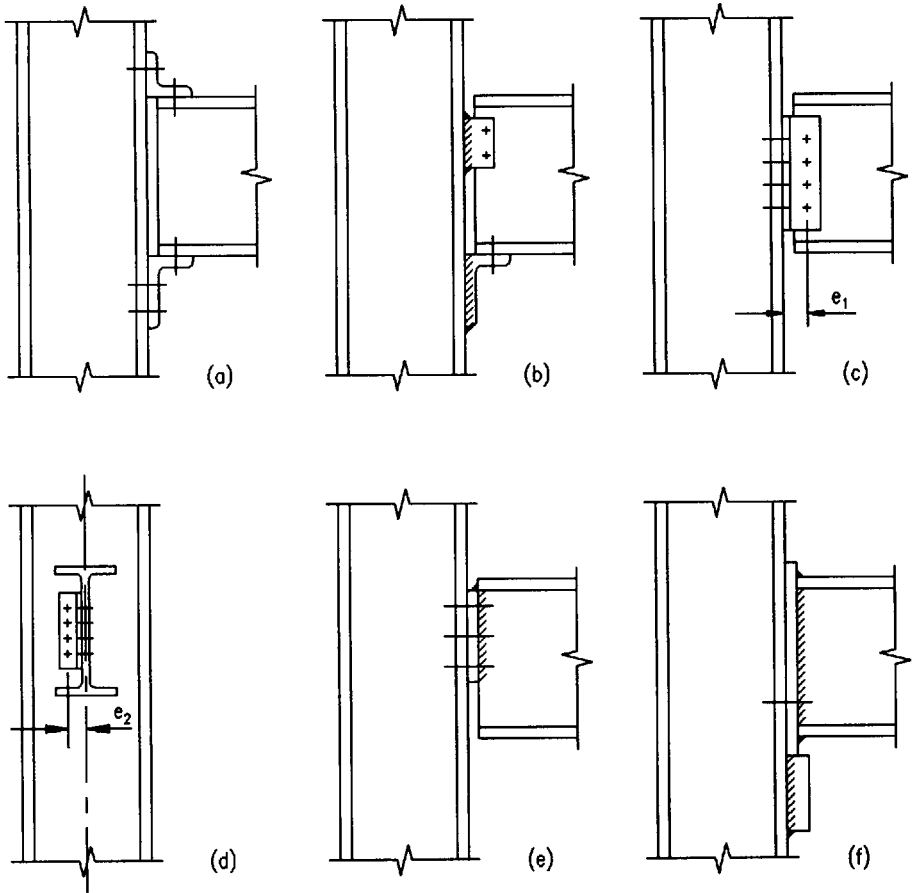


Fig. 26.8 Simple beam-to-column connections

is assumed to be applied at the toe of the horizontal leg. Since the horizontal leg of the top cleat is relatively flexible, the top cleat cannot be assumed to contribute to the shear resistance of the connection.

An alternative detail for the top cleat is to connect it to the top of the web. This alternative should be considered where the top flange cleat would interfere with the floor construction.

#### 26.2.2.2 Shop-welded seating cleats (Fig. 26.8(b))

This is a variation of the bolted detail where the cleats are shop-welded to the column and drilling of the column is avoided.

On the minor axis, where the seating cleat is connected to the column web, it is difficult to make sound welds if the edges of the angle cleat are close to the column flanges.

#### 26.2.2.3 Bolted web cleats (Fig. 26.8(c))

Normally the cleats are bolted and are in pairs. The bolt group connecting the cleats to the beam web should be designed for the eccentricity  $e_1$ . Conventionally, for a pair of cleats, the effects of eccentricity are ignored when designing the bolts connecting the cleats to the column flange. In practice, the cleat to column flange bolts are rarely critical, design is almost always governed by bolt bearing on the web of the beam.

If only one cleat is used, the eccentricity  $e_2$  must be taken into account when designing the bolts in the cleat-to-column connection (Fig. 26.8(d)). It is also prudent to use HSFGB bolts to limit the beam rotation.

#### 26.2.2.4 Welded web cleats and fin plates

A variation of the bolted web cleat detail is to weld the cleats to the beams, or where a single cleat is used, to weld the cleat to the column. A further variation is to use a flat (fin plate) shop-welded to the column and site-bolted to the beam. Care is required to ensure that the flat is welded on perpendicular to the web or flange. In the web the flat is 'protected' by the column flanges, but if a flat is used on the flange, extra care is required to avoid damage during transportation. For the connection to the column web, the flange of the minor axis beam usually has to be notched to allow the beam to be erected.

With cleats welded to the column, the designer has to ensure that the end connection is able to accommodate the end rotation of the simply-supported beam. To achieve this:

- (1) use ordinary (not preloaded HSFG) bolts and ensure that deformation of the plate in bearing occurs before shear deformation of the bolts, for example, with 8.8 bolts make the cleat (or beam web) thickness less than  $0.5d$  for grade 43 steel and  $0.4d$  for grade 50 steel, where  $d$  is the diameter of the bolt.
- (2) make the edge distance greater than twice the bolt diameter
- (3) ensure that the welds attaching the cleat to the column have a greater resistance than the moment that can be applied by the bolts; this is important because of the limited ductility of fillet welds. In the case of a welded flat this can be achieved by making (leg lengths of welds)  $> 0.8t$ , so that the deformation will take place in the flat rather than the welds.

#### 26.2.2.5 *Welded end plates* (Fig. 26.8(e))

Welded end plates are economical and widely utilised when welded fabrication is to be used for the beam rather than drilling and bolting. Care in detailing is required to ensure that there is sufficient ductility for the simply-supported beam to take up its end rotation without damage to the detail. To achieve this the bolts must be a sensible distance away from the web and flange of the beam and the end plate must not be too thick. Reference 3 gives more details on practical limits for end plate proportions which ensure that they have adequate deformation capacity.

The local shear capacity of the web of the beam must always be checked. Due to their lack of ductility, the welds attaching the end plate to the beam web must not be the weakest link. The rules in section 26.2.2.4 may be used to achieve this.

#### 26.2.2.6 *Shear plates* (Fig. 26.8(f))

When designing this type of connection, consideration should be given to the effect of tolerances and the possible use of packs, since the bearing (in the direction of the span of the beam) is relatively narrow.

Nominal bolts are used near the point of rotation but the requirements of lateral forces (wind/restraint/stability) must be considered.

If the shear plates are only welded on three sides, because welding along the top edge requires plate preparation and machining after welding, the possible distortion of the shear plates must be considered. Bolts or welding may be required to control this.

There will be a tendency for the structure to spread with this detail, due to the elongation of the bottom flanges of the beams. The effect should be considered for large structures; to overcome the problem the shear plate can be moved up to the neutral axis, but this introduces the complication of changing the thickness of the end plate where it sits on the shear plate.

Shear plates are normally only used for large end reactions. Their advantage is that the number of site bolts is reduced to those required to tie the structure together and the eccentricity on the column is less than with a stiffened bracket.

### 26.2.2.7 General

The choice between welded and bolted details will depend largely upon the availability of the appropriate equipment in the fabricating shop. For example, if the shop is equipped with numerically controlled cutting and drilling machines there will be a bias towards bolted shop details. In all the simple beam-to-column connections the site connection is bolted.

Another consideration in the choice of detail is that it is more economical if only shop drilling or shop welding is carried out on a particular beam or column.

Erection should always be considered and an advantage, particularly with heavier beams, of the seating cleat is that the beam can be lowered on to the cleat during erection.

## 26.2.3 Rigid beam-to-column connections

### 26.2.3.1 Site-welded connections (Fig. 26.9(a))

Site-welded connections are rarely used in this country but are frequently used in the USA and other countries.

The flange-to-column welds are usually down-hand welds using backing strips. Column stiffeners are usually required.

A variation of the site-welded connection is shown in Fig. 26.9(b). The web cleat, which is designed to carry the shear, is shop-welded to the column and site-bolted with HSFG bolts. The flanges are then site-welded.

### 26.2.3.2 Welded end plates site-bolted to the columns (Fig. 26.9(c)–(f))

The end plate can either be stopped at the level of the top flange of the beam or be extended beyond the flange to accommodate a row of bolts; the extended end plate is the most economic of the two alternatives. For beams subjected to only 70% or so of their yield moment capacity, the connection is usually idealized for design purposes as a tee-connection at the tension flange and a concentrated reaction at the compression flange. The detail without the extended end plate is only able to carry a relatively small proportion of the beam capacity (assuming that excessively thick end plates and large bolts are not being used).

This type of connection is used for the knee connections of portal frames. Normally it is haunched so that its moment capacity is equal to or greater than the beam capacity. Although end plates with all the tension bolts within the depth of the beam are frequently used, the extended end plate is really the better detail and is generally the more economic. However, it is important to check that the extended end plate and column can be fitted into the overall arrangement of the structure, with respect to such items as the purlins, eaves beams, gutters and curved sheeting at the eaves.

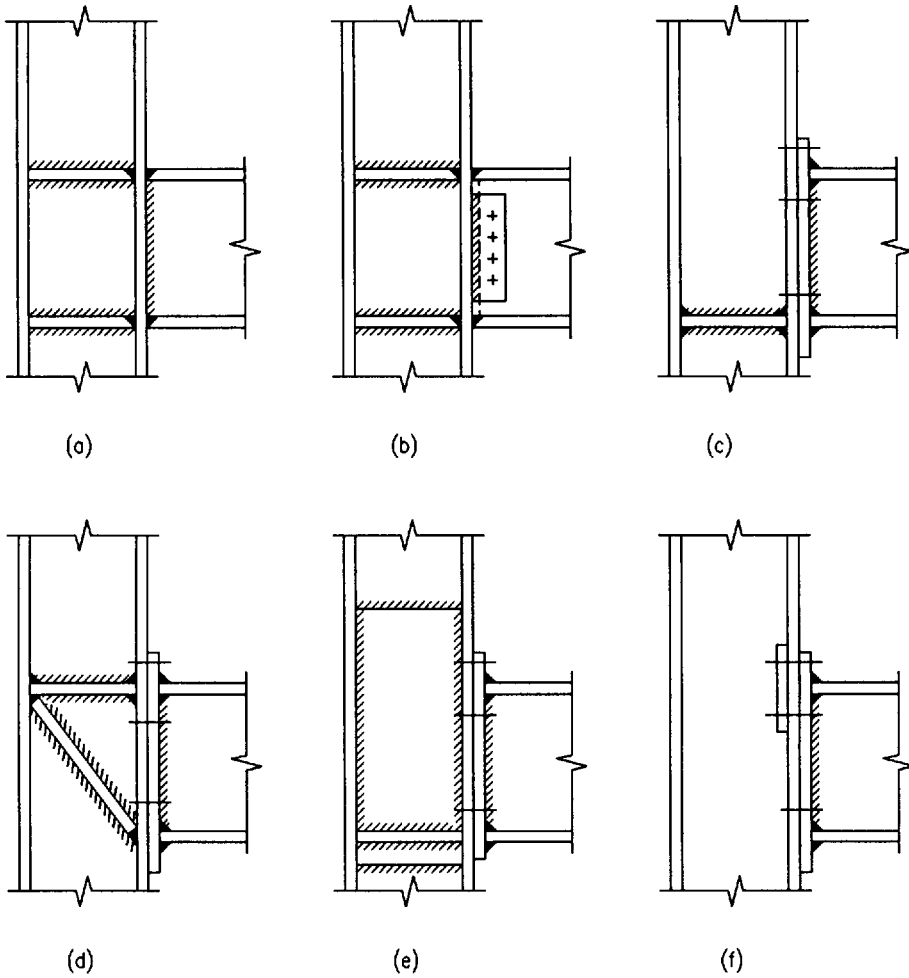


Fig. 26.9 Rigid beam-to-column connections

### 26.2.3.3 Column stiffening

Where rigid beam-to-column connections are used, some kind of column stiffening is normally required.

Horizontal stiffeners are used where the column web is overstressed by the concentrated load from the beam flanges (Fig. 26.9(a)).

There is often a high shear in the column over the depth of the beam and where this exceeds the shear capacity of the column web, stiffening is required. Normally diagonal stiffeners (Fig. 26.9(d)) are used but the web plate shown in Fig. 26.9(e) is another possibility.

The reason for the high shear in the external columns of rigid frames is illustrated in Fig. 26.10, where the bending moment diagram for the column is superimposed on a sketch of the column detail. The full line is the bending moment diagram obtained from a centreline analysis of the structure. The broken line shows how the diagram is modified locally by the application of the beam moment, which for simplicity is assumed to be applied by forces in the beam flanges. It can be seen that the shear in the column (which is the slope of the bending moment diagram) is much greater over the depth of the beam. The important point is that, whereas shear rarely governs the design of hot rolled section beams, the shear capacity can be critical at the joints in rigid frames.

Wherever possible the angle of diagonal stiffeners should be between  $30^\circ$  and  $60^\circ$ . If the column depth is considerably less than the beam depth, 'K' stiffening may be used.

If the web is adequate but the column flange at the tension connection is inadequate in bending it is possible that the use of horizontal stiffeners would

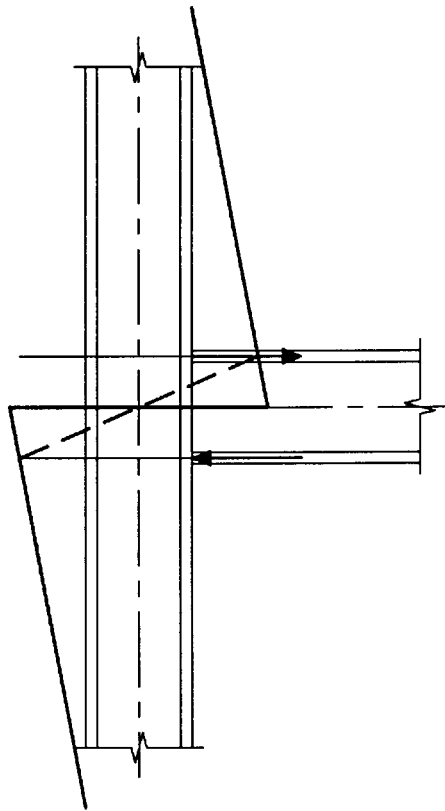


Fig. 26.10 Column bending moment diagram

enable the flange to be justified. Backing plates (Fig. 26.9(f)) are another method of strengthening the column flange to carry the bolt loads, but it should be noted that the use of backing plates increases the prying force on the bolts.

## **26.2.4 Beam and plate girder splices**

### **26.2.4.1 Butt-welded splices**

Connecting the flanges and web with full strength butt welds is the simplest beam splice from the point of view of design in that a full strength connection is obtained and no calculations are required. However, welded splices are of limited use due to the following considerations:

- (1) careful programming is necessary to avoid delays due to the time required for welding (which is more weather-dependent than bolting) and weld inspection
- (2) provision must be made for support and alignment while the welding is carried out
- (3) allowance has to be made for longitudinal shrinkage due to the welding and care is required in the welding sequence to avoid girder distortion and local buckling of the web.

### **26.2.4.2 Bolted cover plate splices**

For plate girders and the heavier beams, double cover plates are normally used so that the bolts are in double shear and the minimum number of bolts is required (Fig. 26.11(a)). It is also a preferred detail because the cover plates are balanced about the flange. However, for smaller beams with flanges less than 200 mm wide, single cover plates on the outside of the flanges are acceptable (Fig. 26.11(b)).

The splice should be situated away from the point of maximum bending moment and normally preloaded HSFGB bolts are used to avoid slip in the joint, which could lead to an unacceptable deflection of the beam.

For small beams it is normal practice to design the flanges to carry all of the bending moment. For larger beams and plate girders, the web splice should be designed to carry the portion of bending moment associated with the web as well as the shear.

### **26.2.4.3 End plate splices**

In pitched portal frames, end plate splices are normally used for the site joint at the apex (Fig. 26.12(a)). As the bending moment at this point is usually near to the capacity of the beam an extended end plate connection is required; usually



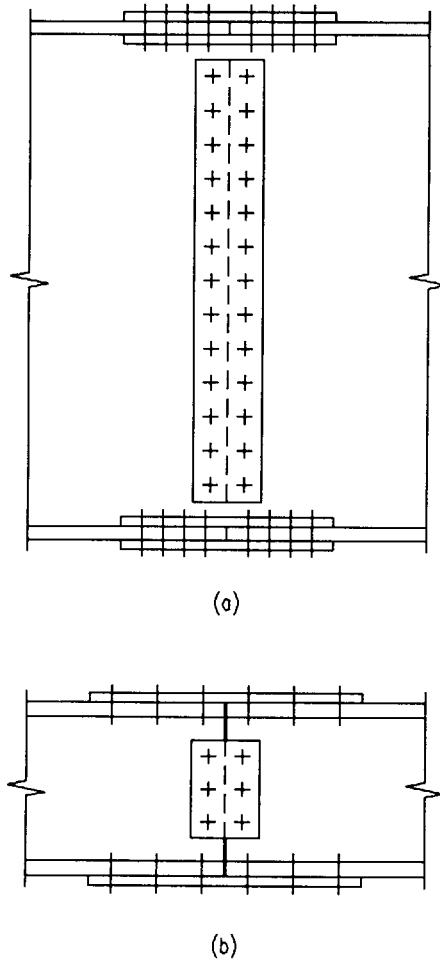
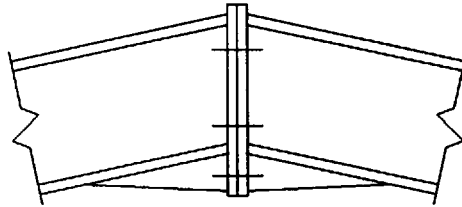


Fig. 26.11 Plate girder and beam splices

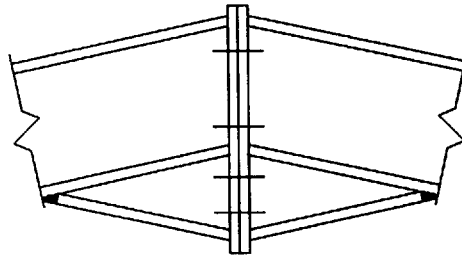
with the extended portion stiffened. Sometimes it is necessary to stiffen the extended portion with a beam cutting forming a mini-haunch detail (Fig. 26.12(b)).

### 26.2.5 Beam-to-beam connections

There are two general forms of beam-to-beam connection, bolted web cleats and welded end plates, and the comments in sections 26.2.2.3 and 26.2.2.5 on the similar beam-to-column connections will apply.



(a)



(b)

Fig. 26.12 Portal frame apex joints

Where the top flanges of the connected beams are at the same level, the flange of the supported beam is notched (Fig. 26.13(a)) and the web has to be checked allowing for the effect of the notch (see section 25.4.3).

The top of the web of the notch, which is in compression, has to be checked for local buckling of the unrestrained web. Provided the beam is laterally restrained (e.g. by a floor slab), to ensure that the web at the top of the notch does not buckle, it is recommended that the length of the notch should not exceed<sup>3</sup>

the depth of the beam ( $D$ ) for grade 43 and for grade 50 where  $D/t_w < 50$   
 half the depth of the beam for grade 50 where  $D/t_w > 50$

where  $t_w$  is the web thickness of the supported beam. For beams which are not laterally restrained a more detailed investigation is required (see Reference 3). If necessary the web is stiffened with horizontal stiffeners (Fig. 26.13 (b)).

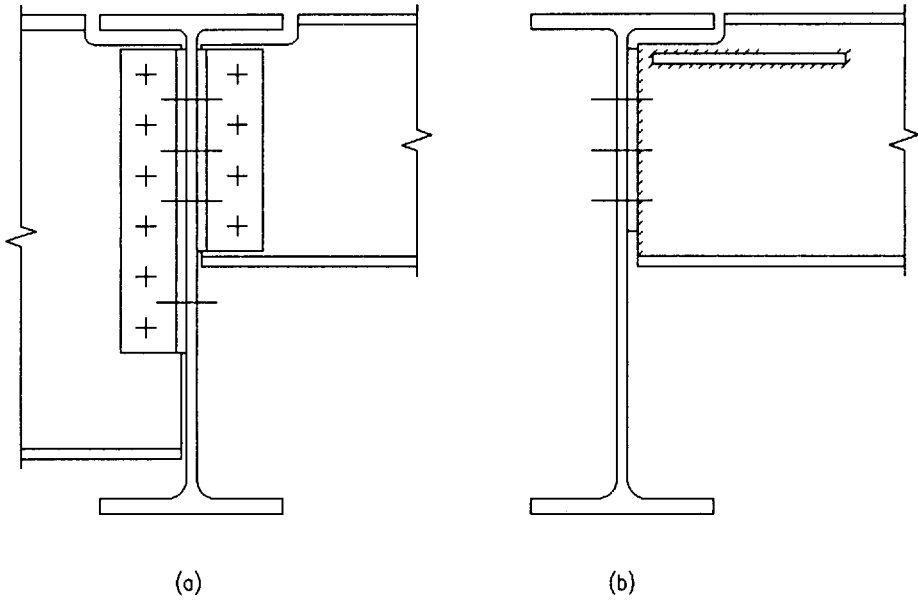


Fig. 26.13 Beam-to-beam connections


### References to Chapter 26

1. British Standards Institution (1990) *Structural use of steelwork in building. Part 1: Code of practice for design in simple and continuous construction: hot rolled sections*. BS 5950, BSI, London.
2. Anderson D. (1991) *Wind Moment Design for Unbraced Frames*. The Steel Construction Institute, Ascot, Berks.
3. The Steel Construction Institute/British Constructional Steelwork Association (1991) *Joints in Simple Construction. Vol. 1: Design Methods*. SCI/BCSA.

### Wider reading for Chapter 26

Owens G.W. & Cheal B.D. (1989) *Structural Steelwork Connections*. Butterworth, London.

A series of worked examples follows which are relevant to Chapter 26.

|  |  |   |                           |
|--|--|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>LIST OF DESIGN EXAMPLES</b>  |   | Chapter ref.<br><b>26</b> |
|  | Design code  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b>        |
|  |  |   | <i>Code</i>               |
| <b>1.</b>  | <b>Warren girder. Bolted gusset plate connection.</b>  |   | <b>BS 5950</b>            |
| <b>2.</b>  | <b>Pitched roof truss. Welded node connection.</b>   |   | <b>BS 5950</b>            |
| <b>3.</b>  | <b>N - girder. Welded node connection.</b>   |   | <b>BS 5950</b>            |
| <b>4.</b>  | <b>Universal column. Bolted cover plate splice. Splice near point of lateral restraint.</b>        |   | <b>BS 5950</b>            |
| <b>5.</b>  | <b>Universal column. Bolted cover plate splice. Splice remote from point of lateral restraint.</b> |   | <b>BS 5950</b>            |
| <b>6.</b>  | <b>Beam to column connection. Bolted web cleats.</b>   |   | <b>BS 5950</b>            |
| <b>7.</b>  | <b>Pitched portal frame. Extended end plate eaves connection.</b>                                  |   | <b>BS 5950</b>            |
| <b>8.</b>  | <b>Pitched portal frame. Apex connection.</b>  |   | <b>BS 5950</b>            |
| <b>9.</b>  | <b>Plate girder. Bolted cover plate splice.</b>  |   | <b>BS 5400</b>            |

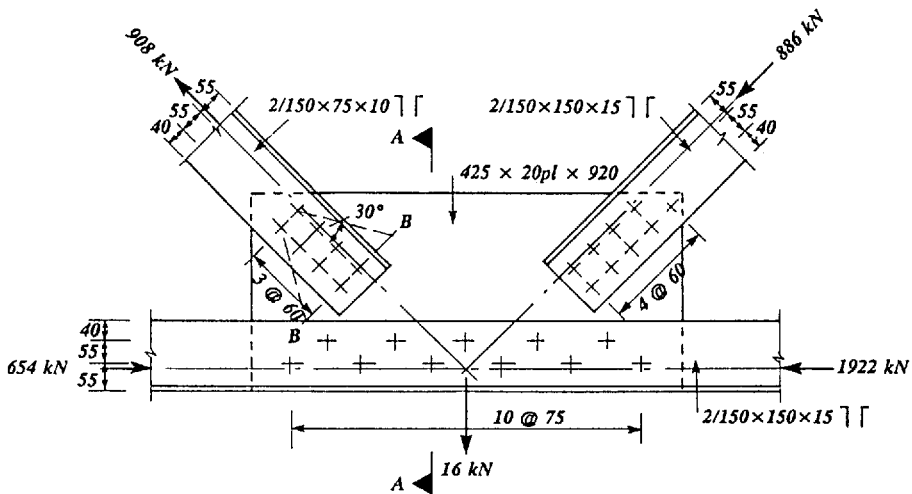
|  |   |   |                           |
|--|---|---|---------------------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>No.1 WARREN GIRDER.<br/>                 BOLTED GUSSET PLATE<br/>                 CONNECTION.</b> |   | Chapter ref.<br><b>26</b> |
|  | Design code<br><b>BSS950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>I</b>        |

The connection is for a node in the bottom boom of a Warren girder truss.

Forces are due to factored loads

All steel grade 43

M20 general grade HSFG bolts




**Bolts**

Use M20 general grade HSFG bolts in double "shear" ( $\mu = 0.45$ ) (see notes at end of example)

$$\begin{aligned}
 \text{Slip resistance per bolt} &= 2 \times 1.1 K_s \mu P_o && 6.4.2.1 \\
 &= 2 \times 1.1 \times 1.0 \times 0.45 \times 144 \\
 &= 142.6 \text{ kN}
 \end{aligned}$$

$$\text{Bearing capacity} = d t p_{bg} < \frac{1}{3} e t p_{bg} \quad 6.4.2.2$$

|  |   |   |   |
|--|---|---|---|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>No.1 WARREN GIRDER.<br/>         BOLTED GUSSET PLATE<br/>         CONNECTION.</b> | Chapter ref<br>26                           |
|  |   | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> |

**Minimum thickness of gusset plate**

$$= \frac{142.6 \times 10^3}{20 \times 825} = 8.6 \text{ mm}$$

**Try 20 mm thick gusset plate**

**Minimum end distance**

$$= \frac{142.6 \times 10^3 \times 3}{20 \times 825} = 25.9 \text{ mm}$$

Also, minimum end distance = 1.4 D

$$= 1.4 (20 + 2) = 30.8 \text{ mm}$$

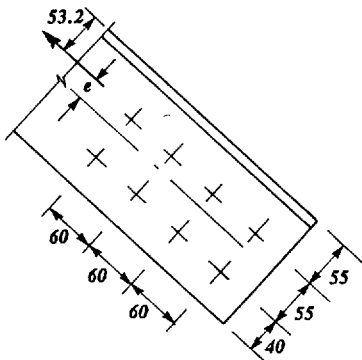
6.2.3  
Table 31

The 20 mm plate is necessary to ensure adequate local tension capacity (see later).

**Bearing thickness of angle members**


$$= 2 \times 10 = 20 > 8.6 \text{ mm OK}$$

**Tension diagonal (2/150 × 75 × 10 angles)**



$$\begin{aligned} \Sigma (x^2 + y^2) &= 8 \times 27.5^2 + 4 \times 30^2 + 4 \times 90^2 \\ &= 42050 \text{ mm}^2 \end{aligned}$$

[ 23.4.2 ]

|  |   |   |   |                    |
|--|---|---|---|--------------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>No.1 WARREN GIRDER.<br/>                 BOLTED GUSSET PLATE<br/>                 CONNECTION.</b> |   | Chapter ref.<br>26 |
|  |   | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. 3        |

$$\begin{aligned}
 \text{Moment} &= R e = 908 (55 + 27.5 - 53.2) \\
 &= 26604 \text{ Nm}
 \end{aligned}$$

(See notes at end of example for discussion of line of action of force)

Maximum resultant shear on bolt

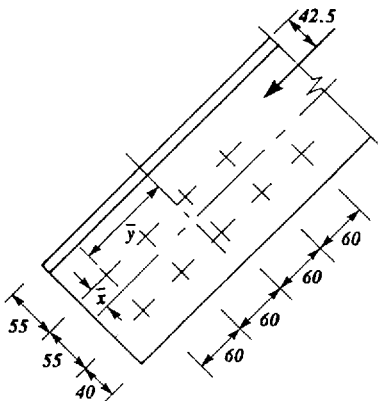
$$\begin{aligned}
 &= \left[ \left[ \frac{R}{n} + \frac{R e x_1}{\Sigma (x^2 + y^2)} \right]^2 + \left[ \frac{R e y_1}{\Sigma (x^2 + y^2)} \right]^2 \right]^{0.5} \\
 &= \left[ \left[ \frac{908}{8} + \frac{26604 \times 27.5}{42050} \right]^2 + \left[ \frac{26604 \times 90}{42050} \right]^2 \right]^{0.5} \\
 &= [ (113.5 + 17.4)^2 + (56.9)^2 ]^{0.5} \\
 &= 142.7 \text{ kN} = \text{slip resistance OK}
 \end{aligned}$$


Compression diagonal (2/150 × 150 × 15 angles)

Centroid is 42.5 mm from heel of angle.

By inspection 8 bolts are inadequate.

Try 9 bolts.



|   |   |   |   |
|---|---|---|---|
| <b>The Steel Construction Institute</b><br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>No.1 WARREN GIRDER.<br/>         BOLTED GUSSET PLATE<br/>         CONNECTION.</b> | Chapter ref.<br><b>26</b>                   |
|   |   | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> |

$$\bar{x} = \frac{5 \times 55}{9} = 30.6 \text{ mm}$$

$$\bar{y} = \frac{2 \times 60 + 2 \times 120 + 2 \times 180 + 1 \times 240}{9} = 106.7 \text{ mm}$$

$$\begin{aligned} \Sigma (x^2 + y^2) &= 5 \times 24.4^2 + 4 \times 30.6^2 + 2 \times 106.7^2 \\ &\quad + 2 \times 46.7^2 + 2 \times 13.3^2 + 2 \times 73.3^2 \\ &\quad + 1 \times 133.3^2 \\ &= 62722 \text{ mm}^2 \end{aligned}$$

$$\text{Moment} = 886 (55 + 30.6 - 42.5) = 38187 \text{ Nm}$$

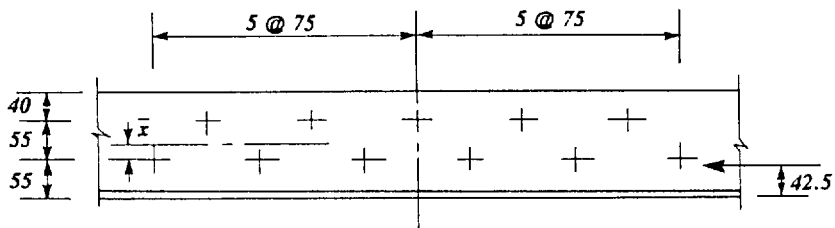
*Maximum resultant shear on bolt*

$$\begin{aligned} &= \left[ \left( \frac{886}{9} + \frac{38187 \times 30.6}{62722} \right)^2 + \left( \frac{38187 \times 133.3}{62722} \right)^2 \right]^{0.5} \\ &= [ (98.4 + 18.6)^2 + (81.2)^2 ]^{0.5} \\ &= 142.4 \text{ kN} < \text{slip resistance OK} \end{aligned}$$


**Bottom boom** (2/150 × 150 × 15 angles)

*Force to be transmitted to gusset plate*

$$= 1922 - 654 = 1268 \text{ kN}$$





|  |   |   |                           |
|--|---|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>No.1 WARREN GIRDER.<br/>         BOLTED GUSSET PLATE<br/>         CONNECTION.</b> |   | Chapter ref.<br><b>26</b> |
|  | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>5</b>        |

$$\bar{x} = \frac{5 \times 55}{11} = 25.0 \text{ mm}$$

$$\begin{aligned} \Sigma(x^2 + y^2) &= 6 \times 25.0^2 + 5 \times 30.0^2 + 2 \times 75^2 \\ &\quad + 2 \times 150^2 + 2 \times 225^2 + 2 \times 300^2 \\ &\quad + 2 \times 375^2 \\ &= 627000 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Moment} &= 1268 (55 + 25.0 - 42.5) \\ &= 47550 \text{ Nm} \end{aligned}$$

*Maximum resultant shear on bolt*


$$\begin{aligned} &= \left[ \left( \frac{1268}{11} + \frac{47550 \times 25.0}{627000} \right)^2 + \left( \frac{47550 \times 373}{627000} \right)^2 \right]^{0.5} \\ &= [ (115.3 + 1.9)^2 + (28.3)^2 ]^{0.5} \\ &= 120.6 \text{ kN} < \text{slip resistance OK} \end{aligned}$$


Gusset plate

*Check section A-A*

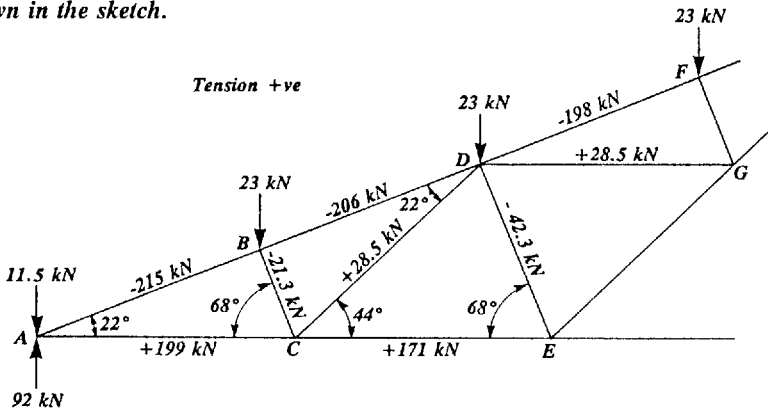
$$\text{Shear} = \frac{908}{\sqrt{2}} = 642 \text{ kN}$$

$$\begin{aligned} \text{Shear capacity} &= 0.6 p_y \times 0.9 t d && 4.2.3 \\ &= 0.6 \times 265 \times 0.9 \times 20 \times 425 \times 10^{-3} \\ &= 1216 \text{ kN} > 642 \text{ kN OK} \end{aligned}$$

|  |   |   |                    |
|--|---|---|--------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN  | Subject<br><b>No.1 WARREN GIRDER.<br/>         BOLTED GUSSET PLATE<br/>         CONNECTION.</b> |   | Chapter ref<br>26  |
|  | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>6</b> |
| <p><b>Check section B-B</b></p> <p><b>Take 30° spread from extreme bolts</b> <span style="float: right;"><b>[ 25.4.2 ]</b></span></p> <p><b>Effective width</b>      =    <math>2 \times 180 \tan 30^\circ + 55 - 2 \times 22</math></p> <p>                                 =    <b>219 mm</b></p> <p><b>Tension capacity</b>      <math>\dot{=} p_y t d</math> <span style="float: right;"><b>4.6.1</b></span></p> <p>                                 =    <math>265 \times 20 \times 219 \times 10^{-3}</math></p> <p>                                 =    <b>1161 kN</b></p> <p>                                 &gt;    <b>908 kN OK</b></p> <p><i>HSTG bolts have been used in this example and should be used in practice where the potential additional deflection of the truss due to slippage of the bolts is unacceptable. They should also be used if there is a possibility of vibration affecting the structure. If the effect of bolt slippage is acceptable, the use of ordinary bolts would lead to greater economy.</i></p> <p><i>In this example the centroidal axes of the members have been used for setting out the detail. In the case of bolted framing of angles and tees the code allows the setting out lines of the bolts to be used, instead of the centroidal axes, if this is desired. With 2 lines of bolts, the bolt line nearest the outstand leg of the angle or the flange of the tee should be used for the setting out.</i> <span style="float: right;"><b>6.1.2</b></span></p> <p><i>Note that it is necessary to allow for the bolt holes in the design of the tension member.</i> <span style="float: right;"><b>4.6.1</b></span></p> |   |   |                    |

|  |  |   |                                   |
|--|--|---|-----------------------------------|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>  | <p>Subject<br/><b>No.2 PITCHED ROOF TRUSS, WELDED NODE CONNECTION.</b></p> |   | <p>Chapter ref.<br/><b>26</b></p> |
|  | <p>Design code<br/><b>BS5950</b></p>                                       | <p>Made by <b>BDC</b><br/>Checked by <b>GWO</b></p> | <p>Sheet no. <b>I</b></p>         |

The connections are for nodes C and D of the roof truss shown in the sketch.



Forces are due to factored loads.

Member sizes (Grade 43)

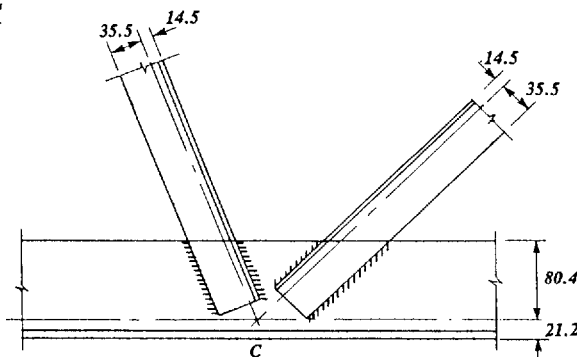
Member ABDF 146 × 127 × 22 Structural Tee


Member ACE 133 × 102 × 13 Structural Tee


Members BC, CD & DG 50 × 50 × 6 Angle

Member DE 60 × 60 × 6 Angle

Node C



|   |   |   |                           |
|---|---|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN  | Subject<br><b>No.2 PITCHED ROOF TRUSS.<br/>         WELDED NODE CONNECTION.</b> |   | Chapter ref.<br><b>26</b> |
|   | Design code<br><b>BSS950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>        |
| <p><i>Try 4 mm fillet welds. (Due to the radius on the toe of the angle, the leg of the fillet weld needs to be 2 mm less than the thickness of the angle. Therefore, 4 mm is the maximum reasonable size of fillet weld on a 6 mm thick angle.)</i></p> <p><b>Capacity of 4 mm fillet weld</b> <span style="float: right;">6.6.5</span></p> $= 4 \times 0.7 \times 215 \times 10^{-3} = 0.602 \text{ kN/mm}$ <p><b>Member CD</b></p> <p><i>Assume fillet welds to toe and heel of angle.<br/>         Line of action of load is on centroid of member; therefore, by moments about heel of angle:</i></p> <p><b>Load on fillet weld to toe</b></p> $= 28.5 \times \frac{14.5}{50} = 8.3 \text{ kN}$ <p><b>Effective length of weld required</b></p> $= \frac{8.3}{0.602} = 14 \text{ mm}$ <p><b>Length of weld required with end allowance</b> <span style="float: right;">6.6.5.2</span></p> $= 14 + 2 \times 4 = 22 \text{ mm}$ <p><b>Load on fillet weld to heel</b></p> $= 28.5 - 8.3 = 20.2 \text{ kN}$ <p><b>Total length of weld required</b></p> $= \frac{20.2}{0.602} + 2 \times 4 = 42 \text{ mm}$ <p><i>Available lengths of weld at toe and heel are adequate.</i></p> |   |   |                           |

|   |   |  |                               |
|---|---|--|-------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>No.2 PITCHED ROOF TRUSS. WELDED NODE CONNECTION.</b></p> |  | <p>Chapter ref.</p> <p>26</p> |
|   | <p>Design code</p> <p><b>BS5950</b></p>                                       | <p>Made by <b>BDC</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. 3</p>            |

**Member BC**

4 mm fillet welds to toe and heel of angle. OK by inspection.

**Member ACE**

Shear between inclined members

$$= 28.5 \sin 44^\circ = 19.8 \text{ kN}$$

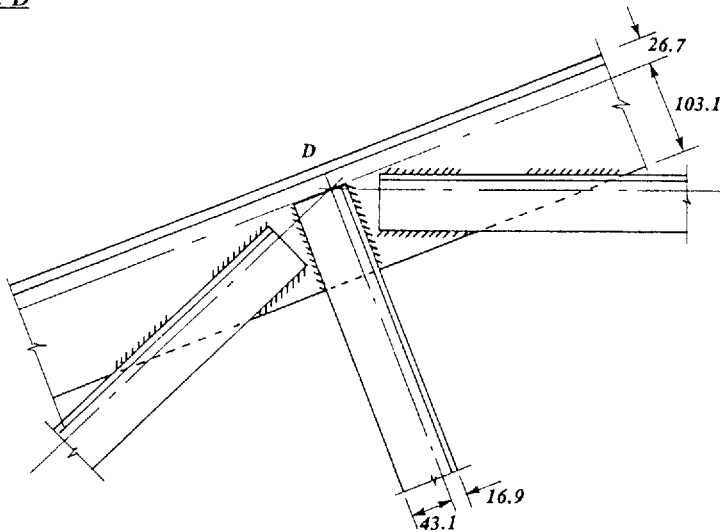
Shear capacity

4.2.3

$$= 0.6 p_y \times (0.9 d t) = 0.6 \times 275 \times 0.9 \times 101.6 \times 5.8 \times 10^{-3}$$


$$= 87.5 \text{ kN} > 19.8 \text{ kN OK}$$

**Node D**



**Members CD and DG**

From previous calculation for member CD at node C, use 4 mm fillet welds to toe and heel of angle (intermittent fillet welds would be adequate on the heel of the angle).

|  |   |   |                           |
|--|---|---|---------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>No.2 PITCHED ROOF TRUSS,<br/>         WELDED NODE CONNECTION.</b> |   | Chapter ref.<br><b>26</b> |
|  | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>        |

**Member DE**

Assume fillet welds to toe and heel of angle.

Load on fillet weld to heel

$$= 42.3 \times \frac{43.1}{60} = 30.4 \text{ kN}$$

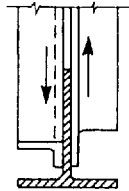
Length of 4 mm fillet weld required with end allowance

$$= \frac{30.4}{0.602} + 2 \times 4 = 58 \text{ mm} < \text{available length at heel OK}$$

Weld at toe, 4 mm fillet weld. OK by inspection.

By inspection, shear on BDF is not critical, being less than that calculated for ACE.


The single angles are all welded to the same face of the stalk of the tees, for ease of fabrication. This arrangement also has the advantage of reducing the torsional couple due to the eccentricity of the centroids. For example, at node C, if the angles were on opposite faces there would be an out-of-balance couple:



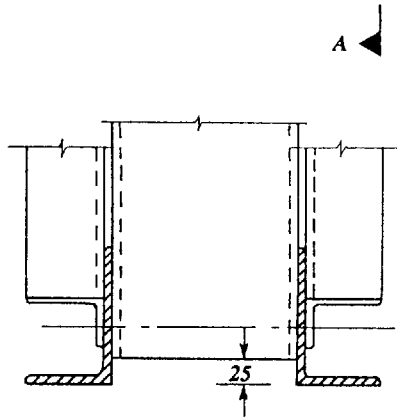
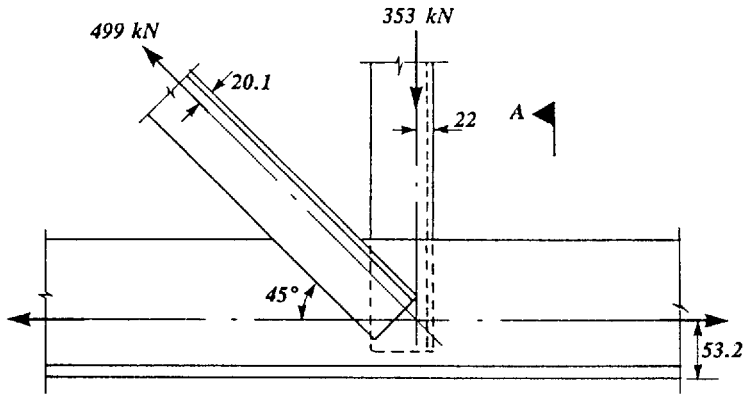
However, with the single sided arrangement, there is a higher out-of-balance moment on plan. In this example the forces are relatively small and the members should be able to accommodate the secondary stresses due to this out-of-balance moment.

The truss is detailed so that the member centroids intersect at the node point; therefore, there are no secondary moments to consider in the plane of the truss.

6.1.2

|  |   |   |                    |
|--|---|---|--------------------|
| <p>The Steel Construction Institute<br/> <br/>                 Silwood Park, Ascot, Berks SL5 7QN</p> | Subject<br><b>No.3 N - GIRDER.<br/>                 WELDED NODE CONNECTION.</b> |   | Chapter ref.<br>26 |
|  | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>1</b> |

The connection is for a node in the bottom boom of an N - girder truss.




Section A-A

Forces are due to factored loads.

**Member sizes**

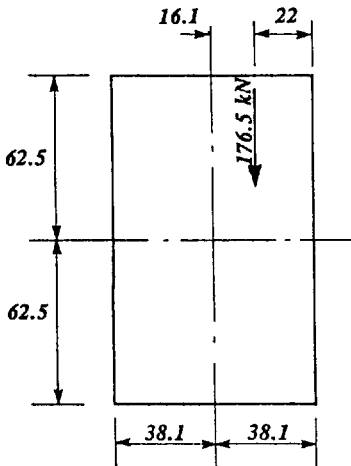
- Diagonal                    2 No 70 × 70 × 8 angles
- Vertical                    178 × 76 × 20.84 kg/m channel
- Bottom boom              2 No 150 × 75 × 10 angles

|  |   |   |              |
|--|---|---|--------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject                                     | Chapter ref. |
|  |   | No.3 N - GIRDER.<br>WELDED NODE CONNECTION. |              |
| Design code  |   | Made by                                     | Sheet no.    |
| BS5950   |   | BDC   | 2            |
|  |   | Checked by                                  |              |
|  |   | GWO   |              |

**Vertical member**

*Load is applied at centroid of channel.*

*Load for each weld group* =  $\frac{353}{2}$  = 176.5 kN



*Total length of weld*  
 = 2(125 + 76.2)  
 = 402.4 mm

$$I_{oo} = 2 \left[ \frac{125^3}{12} + 76.2 \times 62.5^2 + \frac{76.2^3}{12} + 125 \times 38.1^2 \right] \quad [ 24.3.2 ]$$


$$= 1.357 \times 10^6 \text{ mm}^3$$

*Maximum resultant shear on weld*

$$= \left[ \left[ \frac{R}{2(a+b)} + \frac{R_e \times \frac{a}{2}}{I_{oo}} \right]^2 + \left[ \frac{R_e \times \frac{b}{2}}{I_{oo}} \right]^2 \right]^{0.5}$$

$$= \left[ \left[ \frac{176.5}{2(76.2 + 125)} + \frac{176.5 \times 16.1 \times 38.1}{1.357 \times 10^6} \right]^2 + \left[ \frac{176.5 \times 16.1 \times 62.5}{1.357 \times 10^6} \right]^2 \right]^{0.5}$$



|   |   |  |                                      |
|---|---|--|--------------------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>No.3 N - GIRDER,<br/>WELDED NODE CONNECTION.</b></p> |  | <p>Chapter ref.</p> <p><b>26</b></p> |
|   | <p>Design code</p> <p><b>BS5950</b></p>                                   | <p>Made by <b>BDC</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>3</b></p>            |

$$= [ (0.439 + 0.080)^2 + (0.131)^2 ]^{0.5}$$

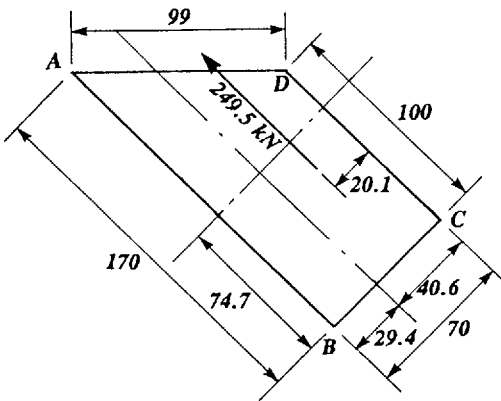
$$= 0.535 \text{ kN/mm}$$

Use 5 mm fillet welds (as required for diagonal member).

Diagonal member

Load is applied at centroid of angles.

Load for each weld group =  $\frac{499}{2} = 249.5 \text{ kN}$




Length of weld =  $170 + 70 + 100 + 99 = 439 \text{ mm}$

By moments about AB

$$\bar{x} = \frac{70 \times 35 + 100 \times 70 + 99 \times 35}{439} = 29.4 \text{ mm}$$

By moments about BC

$$\bar{y} = \frac{170 \times 85 + 99 \times 135 + 100 \times 50}{439} = 74.7 \text{ mm}$$

|   |  |   |                               |
|---|--|---|-------------------------------|
| The<br>Steel Construction<br>Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><br><b>No.3 N - GIRDER.<br/>WELDED NODE CONNECTION.</b> |   | Chapter ref.<br><br><b>26</b> |
|   | Design code<br><b>BS5950</b>                                       | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>            |

$$\begin{aligned}
 I_{oo} &= \frac{170^3}{12} + 170 \left[ \frac{170}{2} - 74.7 \right]^2 + 70 \times 74.7^2 \\
 &+ \frac{100^3}{12} + 100 \left[ 74.7 - \frac{100}{2} \right]^2 + 99 \times \frac{70^2}{12} \\
 &+ 99 (135 - 74.7)^2 + 170 \times 29.4^2 \\
 &+ \frac{70^3}{12} + 70 \left[ \frac{70}{2} - 29.4 \right]^2 + 100 \times 40.6^2 \\
 &+ 99 \times \frac{70^2}{12} + 99 \times \left[ \frac{70}{2} - 29.4 \right]^2 \\
 &= 1.749 \times 10^6 \text{ mm}^3
 \end{aligned}$$

$$\text{Eccentricity of load} = 40.6 - 20.1 = 20.5 \text{ mm}$$


*Maximum resultant shear on weld*

$$\begin{aligned}
 &= \left[ \left( \frac{249.5}{439} + \frac{249.5 \times 20.5 \times 40.6}{1.749 \times 10^6} \right)^2 + \left( \frac{249.5 \times 20.5 \times 74.7}{1.749 \times 10^6} \right)^2 \right]^{0.5} \\
 &= [ (0.568 + 0.119)^2 + (0.218)^2 ]^{0.5} \\
 &= 0.721 \text{ kN/mm}
 \end{aligned}$$

*Use 5 mm fillet welds.*

*Weld all round (angles & channels) with 5 mm fillet welds.*

$$\text{Capacity} = 5 \times 0.7 \times 215 \times 10^{-3} = 0.753 \text{ kN/mm} \quad 6.6.5$$

|  |   |   |                           |
|--|---|---|---------------------------|
| <p>The Steel Construction Institute<br/>Silwood Park, Ascot, Berks SL5 7QN</p>  | <p>Subject <b>No.4 UNIVERSAL COLUMN. BOLTED COVER PLATE SPLICE. SPLICE NEAR POINT OF LATERAL RESTRAINT.</b></p> |   | <p>Chapter ref. 26</p>    |
|  | <p>Design code <b>BS5950</b></p>  | <p>Made by <b>BDC</b><br/>Checked by <b>GWO</b></p> | <p>Sheet no. <b>1</b></p> |

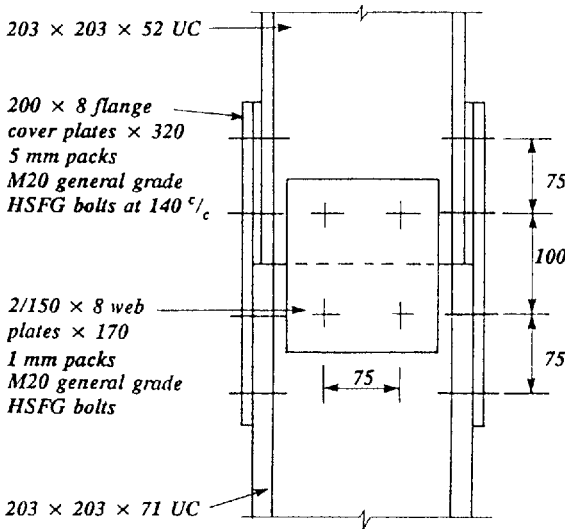
The splice is between a 203 × 203 × 52 UC upper column and a 203 × 203 × 71 UC lower column. Both sections are grade 43.

The splice is to carry a factored axial load of 653 kN.

The splice is near to a point of lateral restraint and moments due to strut action are not considered.

In this example it is assumed that all of the load is carried by the splice. If the ends of the members were prepared for full contact in bearing, only a nominal splice would be required for erection and continuity.

6.1.7.2  
[26.2.1.2]




Share the load between the web and the flanges in proportion to their areas.

[ 26.2.1.1 ]

$$\text{Area of } 203 \times 203 \times 52 \text{ UC} = 66.4 \text{ cm}^2$$

$$\begin{aligned} \text{Area of web} &= (206.2 - 2 \times 12.5) \times 8.0 \times 10^{-2} \\ &= 14.5 \text{ cm}^2 \end{aligned}$$

|  |  |   |                        |
|--|--|---|------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject <i>No.4 UNIVERSAL COLUMN. BOLTED COVER PLATE SPLICE. SPLICE NEAR POINT OF LATERAL RESTRAINT.</i> |   | Chapter ref. <b>26</b> |
|  | Design code<br><b>BS5950</b>   | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>     |

*Portion of load carried by web*

$$= 653 \times \frac{14.5}{66.4} = 142.6 \text{ kN}$$

*Portion of load carried by each flange*

$$= \frac{1}{2} (653 - 142.6) = 255.2 \text{ kN}$$

Try M20 general grade HSBG bolts.

Web splice

*Slip resistance per bolt (in double shear)* 6.4.2.1

$$= 2 \times 1.1 K_s \mu P_o = 2 \times 1.1 \times 1.0 \times 0.45 \times 144 = 142.6 \text{ kN}$$

*Bearing resistance per bolt* 6.4.2.2

$$= d t p_{bg} = 20 \times 8.0 \times 825 \times 10^{-3} = 132 \text{ kN}$$

*Bearing resistance governs.*


*Number of bolts required*  $= \frac{\text{web load}}{\text{resistance per bolt}}$

$$= \frac{142.6}{132} = 1.08$$

Use 2 No. M20 general grade HSBG bolts for web splice.

*Note that end failure check ( $P_{bg} \leq \frac{1}{2} e t p_{bg}$ ) is not required because bearing acts away from the end.* 6.4.2.2

But "edge" distance  $\nless 1.4 (20 + 2) = 30.8 \text{ mm}$  6.2.3  
 (could be  $\nless 1.25 D = 27.5 \text{ mm}$  if machine flame cut or sawn). Table 31

|   |  |   |                        |
|---|--|---|------------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject <i>No.4 UNIVERSAL COLUMN. BOLTED COVER PLATE SPLICE. SPLICE NEAR POINT OF LATERAL RESTRAINT.</i> |   | Chapter ref. <b>26</b> |
|   | Design code<br><b>BS5950</b>   | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b>     |

**Flange splices**

*Slip resistance per bolt (in single shear)* **6.4.2.1**

$$= 1.1 \times 1.0 \times 0.45 \times 144 = 71.3 \text{ kN}$$

*Bearing resistance per bolt on flange* **6.4.2.2**

$$= 20 \times 12.5 \times 825 \times 10^{-3}$$

$$= 206.3 \text{ kN}$$

*Slip resistance governs.*

*Number of bolts required*  $= \frac{255.2}{71.3} = 3.6$

*Use 4 No. M20 general grade HSFGB bolts for each flange splice.*

*Edge distance  $\leq 1.25 D$*   $= 1.25 (20 + 2) = 27.5 \text{ mm}$  **Table 31**

**Flange splice plates**


*Use 200 mm wide cover plates, bolts at 140 mm cross centres and 75 mm pitch (100 mm pitch across joint).*


*Minimum thickness of splice plate*

$$= \frac{255.2 \times 10^3}{275(200 - 140 + 2 \times 75 \tan 30^\circ)}$$

$$= 6.3 \text{ mm}$$

*(The effective width of plate is obtained by assuming a maximum dispersion angle of 30°. No deduction is made for holes since the plates are in compression.)* **[25.4.2]**  
**4.7.4**

|   |  |   |                        |
|---|--|---|------------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN  | Subject <i>No.4 UNIVERSAL COLUMN. BOLTED COVER PLATE SPLICE. SPLICE NEAR POINT OF LATERAL RESTRAINT.</i> |   | Chapter ref. <b>26</b> |
|   | Design code<br><i>BS5950</i>   | Made by <i>BDC</i><br>Checked by <i>GWO</i> | Sheet no. <b>4</b>     |
| <p>Also thickness <math>\nless \frac{\text{pitch}}{14} = \frac{100}{14} = 7.1 \text{ mm}</math> <span style="float: right;">6.2.2</span></p> <p><i>Use 8 mm thick <math>\times</math> 200 mm flange cover plates.</i></p> <p><i>(Bearing resistance on bolt OK by inspection)</i></p> <p><u><i>Web splice plates</i></u></p> <p><i>Use 150 mm <math>\times</math> 8 mm web cover plates.</i></p> <p><i>OK by inspection</i></p> <p><i>Packs will be required to make up the difference in size between the upper and lower column sections. The faying surfaces of the packs must provide a slip factor equal to or greater than that used in the design.</i></p> |  |   |                        |

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|   | <p>Design code <b>BS5950</b></p>   | <p>Made by <b>BDC</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>1</b></p>     |

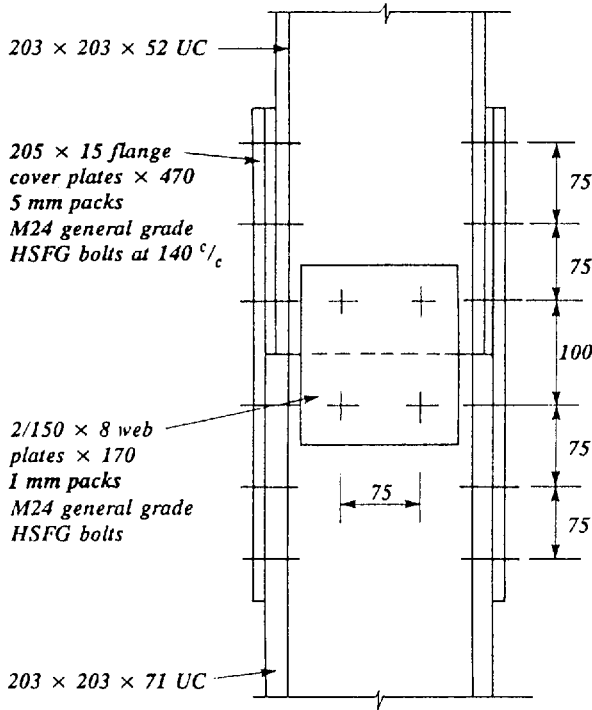
The splice is between a 203 × 203 × 52 UC upper column and a 203 × 203 × 71 UC lower column. Both sections are grade 43.


The splice is to carry a factored axial load of 653 kN.

The splice is assumed to be mid-way between points of lateral restraint and the moments due to strut action are considered in the design. (Effective length of strut = 6 m.)

As in the previous example all the load is assumed to be carried by the splice.

6.1.7.2



|  |   |   |                        |
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|  | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b>     |

*Moment at splice due to strut action* *Appendix C*  
*[26.2.1.1]*  
*C.2*

$$\lambda = \frac{600}{5.16} = 116.3$$

$$\lambda_o = 0.2 \left[ \frac{\pi^2 E}{P_y} \right]^{0.5} = 0.2 \left[ \frac{\pi^2 \times 205 \times 10^3}{275} \right]^{0.5} = 17.2$$

Use strut table 27(c) *Table 25*

$$\eta = 0.001 a (\lambda - \lambda_o) = 0.001 \times 5.5 (116.3 - 17.2) = 0.545 \quad \text{C.2}$$

$$P_E = \frac{\pi^2 E}{\lambda^2} = \frac{\pi^2 \times 205 \times 10^3}{116.3^2} = 149.6 \text{ N/mm}^2 \quad \text{C.1}$$

$$f_c = \frac{653 \times 10^3}{66.4 \times 10^2} = 98.3 \text{ N/mm}^2 \quad \text{C.3}$$

$$M_{max} = \frac{\eta f_c S}{\left[ 1 - \frac{f_c}{P_E} \right]} = \frac{0.545 \times 98.3 \times 264 \times 10^{-3}}{\left[ 1 - \frac{98.3}{149.6} \right]} = 41.2 \text{ kNm} \quad \text{C.3}$$


*Distribution of axial load*


*Share the axial load between the web and the flanges in proportion to their areas.* *[26.2.1.1]*


$$\text{Area of } 203 \times 203 \times 52 \text{ UC} = 66.4 \text{ cm}^2$$

$$\begin{aligned} \text{Area of web} &= (206.2 - 2 \times 12.5) \times 8.0 \times 10^{-2} \\ &= 14.5 \text{ cm}^2 \end{aligned}$$



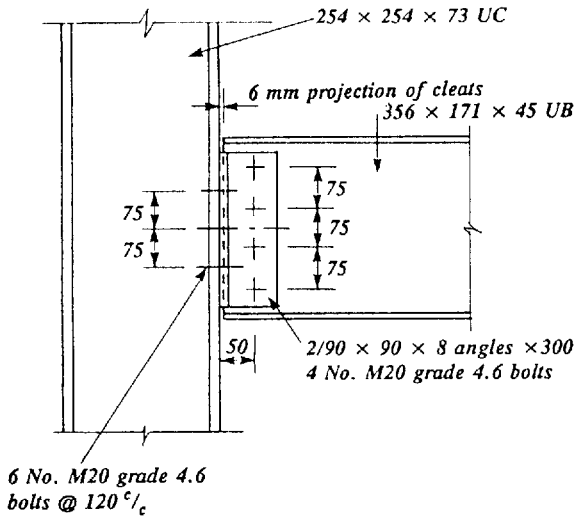
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|--|--|---|------------------------|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p>  | <p>Subject <i>No.5 UNIVERSAL COLUMN. BOLTED COVER PLATE SPLICE. SPLICE REMOTE FROM POINT OF LATERAL RESTRAINT.</i></p> |   | <p>Chapter ref. 26</p> |
|  | <p>Design code <i>BS5950</i></p>   | <p>Made by <i>BDC</i><br/>Checked by <i>GWO</i></p> | <p>Sheet no. 3</p>     |
| <p><i>Portion of load carried by web</i></p> $= 653 \times \frac{14.5}{66.4} = 142.6 \text{ kN}$ <p><i>Portion of load carried by each flange</i></p> $= \frac{1}{2} (653 - 142.6) = 255.2 \text{ kN}$ <p><i>Try M24 general grade HSFG bolts.</i></p> <p><u><i>Flange splices</i></u></p> <p><i>Slip resistance per bolt (in single shear)</i> <span style="float: right;">6.4.2.1</span></p> $= 1.1 k_s \mu P_o = 1.1 \times 1.0 \times 0.45 \times 207$ $= 102.5 \text{ kN}$ <p><i>Bearing resistance per bolt</i> <span style="float: right;">6.4.2.2</span></p> $= d t p_{bg} = 24 \times 12.5 \times 825 \times 10^{-3}$ $= 247.5 \text{ kN}$ <p><i>Slip resistance governs.</i></p> <p><i>Assume 2 lines of bolts at 140 mm cross centres in each flange.</i></p> <p><i>Axial load per line of bolts</i> <math>= \frac{255.2}{2}</math></p> $= 127.6 \text{ kN}$ <p><i>Load per line of bolts due to strut action moment</i> <span style="float: right;">[ 26.2.1.1 ]</span></p> $= \frac{41.2 \times 10^3}{2 \times 140} = 147.1 \text{ kN}$ |  |   |                        |

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| <p><i>Total load per line of bolts = 127.6 + 147.1</i></p> <p><i>= 274.7 kN</i></p> <p><i>Number of bolts required in each line</i></p> $= \frac{274.7}{102.5} = 2.7$ <p><i>Use 3 bolts in each line, 2 lines of 3 M24 general grade HSFSG bolts for each flange splice.</i></p> <p><i>Use 205 × 15 flange cover plates.</i></p> <p><i>Note that the size of the flange splice plates should not be less than that of the column flange in respect to area and modulus.</i> [26.2.1.2]</p> <p><u>Web splice</u></p> <p><i>By inspection use 2 / M24 general grade HSFSG bolts.</i></p> <p><i>Packs will be required to make up the difference in size between the upper and lower column sections. The faying surfaces of the packs must provide a slip factor equal to or greater than that used in the design.</i></p> |   |   |                        |

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|  | Design code<br><b>BS5950</b>   | Made by <b>BDC</b><br>Checked by <b>GWO</b> |

The connection is between a 356 × 171 × 45 UB (Grade 43) beam and a 254 × 254 × 73 UC (Grade 43) column.

The end reaction of the simply supported beam due to factored loads is 185 kN



Try 2/90 × 90 × 8 angle cleats × 300 mm and M20 Grade 4.6 bolts.

Connection of cleats to web of beam


Shear capacity of bolt in double shear 6.3.2

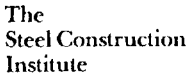
$$= 2 p_s A_t = 2 \times 160 \times 245 \times 10^{-3} = 78.4 \text{ kN}$$

Bearing capacity of bolt on web of beam 6.3.3

$$= p_{bb} d t = 460 \times 20 \times 6.9 \times 10^{-3} = 63.5 \text{ kN} \quad \text{Table 32 (Amd. 1)}$$

(bearing capacity on cleats is greater)

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|  | Design code<br><b>BS5950</b>   | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no.<br>2     |
| <p><i>Try 4 bolts at 75 mm vertical pitch and 50 mm from heel of cleats.</i></p> <p>Vertical shear force per bolt = <math>\frac{185}{4} = 46.3 \text{ kN}</math></p> <p>Moment due to eccentricity of reaction from centroid of bolt group [26.2.2.3]</p> <p><math>M_e = P e = 185 \times 50 = 9250 \text{ Nm}</math></p> <p>Horizontal shear due to eccentricity</p> <p>= <math>\frac{M_e r_i}{\Sigma (r_i^2)} = \frac{9250 \times 112.5}{2(37.5^2 + 112.5^2)}</math> [23.4.2]</p> <p>= 37.0 kN</p> <p>Resultant shear force = <math>\sqrt{(46.3)^2 + (37.0)^2}</math></p> <p>= 59.3 kN</p> <p>&lt; bolt capacity (= 63.5 kN) OK</p> <p><u>Connection of cleats to column flange</u></p> <p>Shear capacity of bolt in single shear 6.3.2</p> <p>= <math>p_s A_t = 160 \times 245 \times 10^{-3} = 39.2 \text{ kN}</math></p> <p>Bearing capacity of bolt on cleat 6.3.3</p> <p>= <math>p_{bb} d t = 460 \times 20 \times 8 \times 10^{-3} = 73.6 \text{ kN}</math> Table 32 (Amd. 1)</p> <p><i>Try 6 bolts in 2 columns at 75 mm vertical pitch and 120 mm cross centres.</i></p> <p>Vertical shear force per bolt = <math>\frac{185}{6} = 30.8 \text{ kN}</math></p> |  |   |                    |

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|  | Design code<br><b>BS5950</b>   | Made by<br><b>BDC</b><br>Checked by<br><b>GWO</b> | Sheet no.<br>3     |

Considering one cleat, horizontal shear force on bottom bolt due to eccentricity (assuming a centre of pressure 25 mm below the top of cleat) [26.2.2.3]

$$\begin{aligned}
 &= \frac{P}{2} \times e \times \frac{r_i}{\Sigma (r_i^2)} \\
 &= \frac{185}{2} \times \frac{1}{2} \times (120 - 6.9) \times \frac{200}{(50^2 + 125^2 + 200^2)} \\
 &= 18.0 \text{ kN}
 \end{aligned}$$


Resultant shear force =  $\sqrt{(30.8)^2 + (18.0)^2}$   
 = 35.7 kN  
 < bolt capacity (= 39.2 kN) OK

Use 2 / 90 × 90 × 8 angles × 300 long

4 No. M20 Grade 4.6 bolts

In the design of the bolts connecting the cleats to the column flange, the horizontal shear due to eccentricity has been included so that the "load path" check is complete. In traditional practice, the eccentricity effect is included in the design of bolts in the beam web, but (for a pair of cleats) is ignored in the design of the bolts in the column flange. Where there are 4 or more rows of bolts, this is reasonable since the effect of eccentricity is relatively small. For 3 rows and less it is probably advisable to check that the "load path" is complete. In this example, where grade 4.6 bolts are used, the horizontal shear could be ignored since the cleat can carry the 18.0 kN force in bending. [26.1.2]

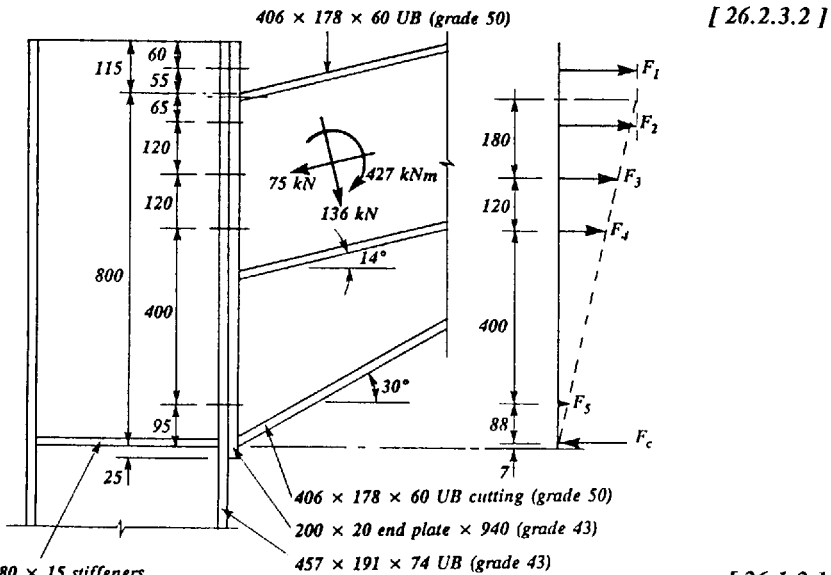
Note that if a similar detail is used for a beam to beam connection (and the top flange is notched) the beam web should be checked for "block shear" failure. [ 25.4.3 ]

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|  |   | Design code<br><b>BS5950</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> |

*The connection is between a haunched 406 × 178 × 60 UB rafter (Grade 50) 457 × 191 × 74 UB column (Grade 43)*

*The factored moment and forces at the end of the rafter are:*

*Bending moment            427 kNm*  
*Axial force                 75 kN (compression)*  
*Shear                         136 kN*




*2 No. 80 × 15 stiffeners*  
*M20 general grade HSFG bolts at 80 c/c (used as ordinary bolts)* [ 26.1.2 ]

*Distribution of applied loading*

*Assuming bolt loads as in the sketch.* [ 26.1.3 ]

*By moments about bottom flange*

$$427 \times 10^3 - (75 \cos 14^\circ - 136 \sin 14^\circ) \times \left[ 800 - \frac{406.4}{2 \cos 14^\circ} - \frac{12.8}{2 \cos 30^\circ} \right]$$

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$$= (2F_1 + 2F_2) \times 788 + 2F_3 \times 608 + 2F_4 \times 488 + 2F_5 \times 88$$

$$= \frac{2F_1}{788} [ 2 \times 788^2 + 608^2 + 488^2 + 88^2 ]$$

$$F_1 = F_2 = 85.6 \text{ kN}$$

$$F_3 = 66.1 \text{ kN}$$

$$F_4 = 53.0 \text{ kN}$$

$$F_5 = 9.6 \text{ kN}$$

*Reaction at bottom flange (of haunch)*

$$\begin{aligned}
 = F_c &= 2(85.6 + 85.6 + 66.1 + 53.0 + 9.6) \\
 &\quad + 75 \cos 14^\circ - 136 \sin 14^\circ \\
 &= 639.7 \text{ kN}
 \end{aligned}$$

Column flange

*Check capacity of flange in bending to resist bolt loads* [ 25.3.5 ]

*Distance from centreline of bolt to centreline of root fillet*

$$= b = \frac{80}{2} - \frac{9.1}{2} - \frac{10.2}{2} = 30.4 \text{ mm}$$


*Distance from centreline of bolt to prying force*

$$\begin{aligned}
 = n &= \text{edge distance but } \neq 2T && [25.3.1] \\
 &= 2 \times 14.5 = 29.0 \text{ mm}
 \end{aligned}$$

*Effective length of flange per bolt*

$$= w = 2(b + d) = 2(30.4 + 20) = 100.8 \text{ mm} \quad [ 25.3.2 ]$$

(assuming M20 bolts)

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$w > b$ , therefore bolt holes can be ignored. [ 25.3.3 ]

A maximum spread of  $(b + d)$  is used for checking the flange capacity so that a plastic hinge can be assumed at the bolt line for the design of the end plate. [ 25.3.2 ] [ 26.1.5 ]

Consider flange for maximum bolt load ( $F_1$ ) with equal moments at bolt line and root:

$$M = \frac{F_1 b}{2} = \frac{85.6 \times 30.4}{2} = 1301.1 \text{ Nm}$$

$$\begin{aligned} \text{Moment capacity} &= p_y \times \frac{w T^2}{4} \\ &= \frac{275 \times 100.8 \times 14.5^2 \times 10^{-3}}{4} \\ &= 1457 \text{ Nm} > M \text{ OK} \end{aligned}$$

$$\text{Prying force} = \frac{M}{n} = \frac{1301.1}{29.0} = 44.9 \text{ kN} \quad [25.3.1]$$

### Bolts


Tension capacity of M20 general grade HSF8 bolt, taken as  $0.64 U_f$  [25.3.1]

$$\begin{aligned} &= 0.64 \times 827 \times 245 \times 10^{-3} \\ &= 129.7 \text{ kN} \end{aligned}$$

### Bolt load

$$\begin{aligned} &= F_1 + \text{prying force} \\ &= 85.6 + 44.9 = 130.5 \text{ kN} > \text{bolt capacity} \end{aligned}$$



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Check with reduced prying force.

Maximum allowable prying force ( $Q_1$ )

$$= 129.7 - 85.6 = 44.1 \text{ kN}$$

'Serviceability check' for minimum prying force

$$\begin{aligned}
 Q &= \frac{b}{2n} \left[ F - \frac{\beta \gamma p_o w T^4}{27 n b^2} \right] && [25.3.1] \\
 &= \frac{30.4}{2 \times 29.0} \left[ 85.6 - \frac{2 \times 1.5 \times 0.587 \times 100.8 \times 14.5^4}{27 \times 29 \times 30.4^2} \right] \\
 &= 0.524 [ 85.6 - 10.8 ] = 39.2 \text{ kN} < 44.1 \text{ kN OK}
 \end{aligned}$$

Moment at root of flange, with reduced prying force


$$\begin{aligned}
 &= F_1 b - Q_1 n \\
 &= 85.6 \times 30.4 - 44.1 \times 29.0 \\
 &= 1323 \text{ Nm} < \text{moment capacity}
 \end{aligned}$$

M20 bolts are OK

Use M20 general grade HSFSG bolts (as ordinary bolts).

By inspection the bolt group is also satisfactory for shear load.

General grade HSFSG bolts are used as 'ordinary' bolts (i.e. they are not pre-tensioned to the proof load). They are 'black' bolts (defined by a British Standard) which are suitable for use in tension. Although it is not assumed in the design that they are pre-tensioned in accordance with BS 4604: Part 1, the bolts in the connection should be uniformly tightened to a reasonably high torque to provide the detail with adequate stiffness.

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*If the column flange (or the bolts) had not been adequate, a further check could have been made using a greater effective length (in this example,  $w = 120$  mm) based on the least of the end distance, half the bolt pitch and  $(a + 1.4 b)$  each side of the bolt. A thicker end plate would then be required based on a zero bending moment at the bolt line.*

**Column web (at upper bolts)**

*Tension capacity of 120 mm length of web*

$$\begin{aligned}
 &= 275 \times 120 \times 9.1 \times 10^{-3} && 4.6.1 \\
 &= 300.3 \text{ kN} > 2F_1 \text{ OK}
 \end{aligned}$$

**Column web (at bottom flange of haunch)**

[ 26.2.3.3 ]

*Assuming 20 mm thick end plate, local bearing capacity of web for reaction ( $F_c$ ) =  $(b_1 + n_2) t p_{yw}$*

[25.1]  
4.5.3

$$\begin{aligned}
 &= \frac{(12.8 + 2 \times 20 + 2 \times 2.5 \times (14.5 + 10.2)) \times 9.1 \times 275 \times 10^{-3}}{275 \times 10^{-3}} && 4.5.1.3 \\
 &= 441.2 \text{ kN} < F_c \text{ stiffeners required}
 \end{aligned}$$


**Stiffeners**

[25.2]

*Area required in contact with the flange*

$$\begin{aligned}
 &= \frac{0.8 F_c}{p_{ys}} = \frac{0.8 \times 639.7 \times 10^3}{275} && 4.5.4.2 \\
 &= 1861 \text{ mm}^2
 \end{aligned}$$

*Try 2 No. 80 × 15 stiffeners (with 15 mm snipes).*

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*Area in contact* =  $2(80 - 15) \times 15$   
 =  $1950 \text{ mm}^2$  OK

Use 2 No. 80 × 15 stiffeners.

**Buckling resistance** 4.5.1.5

*Area of effective section*

$$= 2 \times 80 \times 15 + 2 \times 20 \times 9.1^2 = 5712 \text{ mm}^2$$

$$I = \frac{15 \times 169.1^3}{12} = 6.04 \times 10^6 \text{ mm}^4$$

$$r = \left[ \frac{6.04 \times 10^6}{5712} \right]^{0.5} = 32.5 \text{ mm}$$

$$\frac{L}{r} = \frac{0.7 \times (457.2 - 2 \times 14.5)}{32.5} = 9.2$$

$p_c = 275 \text{ N/mm}^2$  Table 27(c)

*Buckling resistance* =  $5712 \times 275 \times 10^{-3}$   
 =  $1571 \text{ kN} > F_c$  OK

**Connection of stiffeners to column web**


*Effective length of weld*

$$= 457.2 - 2 \times (14.5 + 15 + 6)$$
6.6.5.2

$$= 386.2 \text{ mm}$$

*Load on welds* =  $\frac{639.7}{4 \times 386.2} = 0.414 \text{ kN/mm}$

Weld stiffeners to column with 6 mm fillet welds.

|  |   |   |                           |
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**Shear in column web** **[26.2.3.3]**

*Maximum shear in column web (immediately above bottom flange of haunch)*

$$= 2(85.6 + 85.6 + 66.1 + 53.0 + 9.6)$$

$$= 599.8 \text{ kN}$$

*Shear capacity* **4.2.3**

$$= 0.6 p_y t d$$

$$= 0.6 \times 275 \times 9.1 \times 457.2 \times 10^{-3}$$

$$= 686.5 \text{ kN} > 599.8 \text{ kN OK}$$

**End plate**

*By inspection, design will be governed by extended portion above the top flange.* **[ 25.3.5 ]**

*Try 200 mm wide plate × 20 mm thick.*

*(Assume 8 mm fillet welds to flange)*

*Distance from centreline of bolt to toe of fillet weld*

$$= b = 55 - 8 = 47 \text{ mm}$$

*Distance from centreline of bolt to prying force*


$$= n = \text{edge distance but } \nless 2T$$
**[ 25.3.1 ]**

$$= 2 \times 20 = 40 \text{ mm}$$

*Effective length of end plate per bolt* **[ 25.3.2 ]**

$$= w = \frac{1}{2} \times 200 = 100 \text{ mm}$$
**[ 25.3.3 ]**

*(In this case  $\frac{1}{2} \times$  flange width governs 'w')*

|   |   |   |
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*With equal moments at bolt line and root*

$$M = \frac{F_1 b}{2} = \frac{85.6 \times 47}{2} = 2012 \text{ Nm}$$

$$\text{Moment capacity} = p_y \times \frac{w T^2}{4}$$

$$\begin{aligned} \text{Minimum thickness} &= \left[ \frac{4 \times 2012 \times 10^3}{265 \times 100} \right]^{0.5} \\ &= 17.4 \text{ mm Use } 20 \text{ mm} \end{aligned}$$

$$\text{Prying force} = \frac{M}{n} = \frac{2012}{40} = 50.3 \text{ kN} \quad [25.3.1]$$

*As with the check on the column flange, applied load + prying force > bolt capacity*

*maximum allowable prying force ( $Q_1$ )*


$$= 129.7 - 85.6 = 44.1 \text{ kN}$$

*Serviceability check for minimum ( $Q$ )*

$$\begin{aligned} Q &= \frac{47.0}{2 \times 40.0} \left[ 85.6 - \frac{2 \times 1.5 \times 0.587 \times 100 \times 20^4}{27 \times 40.0 \times 47.0^2} \right] \quad [25.3.1] \\ &= 0.588 [85.6 - 11.8] = 43.4 \text{ kN} < 44.1 \text{ kN OK} \end{aligned}$$

*Check moment at root with reduced prying force*

$$\begin{aligned} &= F_1 b - Q_1 n \\ &= 85.6 \times 47 - 44.1 \times 40 \\ &= 2259 \text{ Nm} \end{aligned}$$

|  |   |   |                           |
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**Moment capacity of end plate**

$$= \frac{265 \times 100 \times 20^2 \times 10^{-3}}{4}$$

$$= 2650 \text{ Nm} > \text{moment at root OK}$$

Use 200 × 20 end plate × 940 Grade 43.

**Beam flanges**

Capacity of flange =  $p_y A$

$$= 355 \times 177.8 \times 12.8 \times 10^{-3}$$

$$= 807.9 \text{ kN}$$

Tension in top flange =  $\frac{2(F_1 + F_2)}{\cos 14^\circ}$

$$= \frac{4 \times 85.6}{\cos 14^\circ}$$

$$= 352.9 \text{ kN} < 807.9 \text{ kN OK}$$

Compression in bottom (haunch) flange

$$= \frac{F_c}{\cos 30^\circ}$$


$$= \frac{639.7}{\cos 30^\circ}$$

$$= 738.7 \text{ kN} < 807.9 \text{ kN OK}$$

**Welds**

**Top flange to end plate**

Load from bolts above flange =  $2F_1 = 2 \times 85.6 = 171.2 \text{ kN}$

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*Load on weld* =  $\frac{171.2}{177.8} = 0.963 \text{ kN/mm}$

*Capacity of 8 mm fillet weld* 6.6.5

=  $8 \times 0.7 \times 215 \times 10^{-3} = 1.20 \text{ kN/mm OK}$

$\therefore$  weld top flange to end plate with 8 mm fillet welds.

Web to end plate

*Bolt below top flange,  $F_2 = 85.6 \text{ kN}$*

*Centreline of bolt to toe of flange weld*

=  $b_x = 65 - 12.8 - 8 = 44.2 \text{ mm}$

*Centreline of bolt to toe of web weld*

=  $b_y = \frac{80}{2} - \frac{7.8}{2} - 6 = 30.1 \text{ mm}$

*Effective length of plate at flange*

=  $w_x = \frac{200 - 80}{2} + 0.7 \times 30.1 = 81.1 \text{ mm}$


*Effective length of plate at web*

=  $w_g = \frac{120}{2} + 0.7 \times 44.2 = 90.9 \text{ m}$


*Bolt load supported by web; plastic distribution of load* [25.3.4]

(proportional to  $\frac{w}{b}$ )

=  $\left[ \frac{\frac{90.9}{30.1}}{\frac{81.1}{44.2} + \frac{90.9}{30.1}} \right] \times 85.6 = 53.2 \text{ kN}$

|  |   |   |   |
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| <p><i>Bolt load supported by web; elastic distribution of load<br/>(proportional to <math>\frac{w}{b^3}</math>)</i></p> $= \left[ \frac{\frac{90.9}{30.1^3}}{\frac{81.1}{44.2^3} + \frac{90.9}{30.1^3}} \right] \times 85.6 = 66.8 \text{ kN}$ <p><i>Take higher load (66.8 kN) for design of weld.</i></p> <p><i>Take equal length of weld either side of bolt line, to avoid eccentricity calculations.</i></p> $\text{Load on weld} = \frac{66.8}{2 \times 44.2} = 0.756 \text{ kN/mm}$ <p><i>Use 6 mm fillet welds.</i></p> <p><i>Weld web (and middle flange) to end plate with 6 mm fillet welds.</i></p> <p><u><i>Bottom (haunch) flange to end plate</i></u></p> <p><i>Horizontal component of flange force</i></p> $= F_c = 639.7 \text{ kN}$ <p><i>Vertical component of flange force</i></p> $= F_c \tan 30^\circ = 639.7 \tan 30^\circ = 369.3 \text{ kN}$ <p><i>Fit end plate to flange and take horizontal component in direct compression and vertical component in shear on fillet welds</i></p> $\text{load on weld} = \frac{369.3}{2 \times 177.8} = 1.04 \text{ kN/mm}$ <p><i>Weld bottom (haunch) flange to end plate with 8 mm fillet welds on inside and 10 mm on outside to allow for 120° angle.</i></p> |   |   |   |
|  |   |   | <b>6.6.5.3</b><br><b>[ 24.2.1 ]</b>         |



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Web of rafter

*Load on web (at second row of bolts taking plastic distribution of load)*

$$= 2 \times 53.2 = 106.4 \text{ kN}$$


*Taking effective web as 'b<sub>x</sub>' each side of bolt line, capacity of web at second row of bolts = p<sub>y</sub> 2 b<sub>x</sub> t*

$$= 355 \times 2 \times 44.2 \times 7.8 \times 10^{-3}$$

$$= 244.8 \text{ kN}$$

$$> 106.4 \text{ kN OK}$$

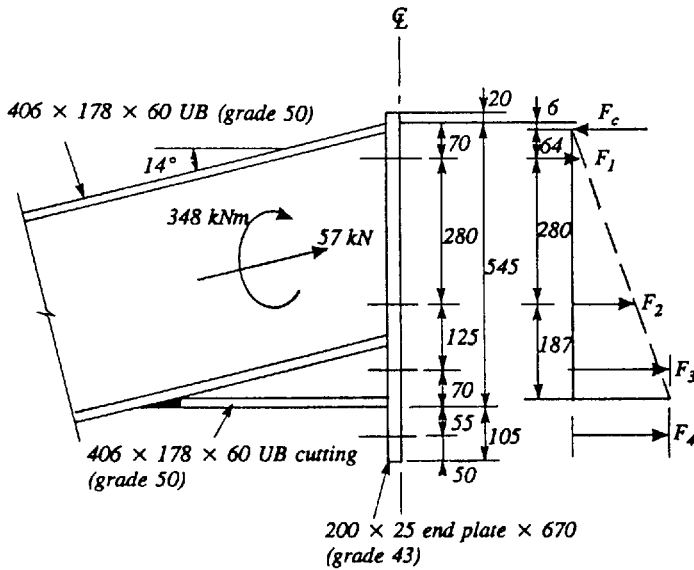
*The strengths of the other parts of the detail also have to be considered. For example, the shear capacity of the end plate to rafter weld and the adequacy of the column flange/end plate/welds/beam web to carry the loads in the third row of bolts. In this example, these are seen to be adequate by inspection (by comparison with the calculations for other parts of the detail) and no further calculations are required.*

|  |   |   |   |
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The bolted apex connection is for a 406 × 178 × 60 UB rafter (Grade 50).

The factored moment and axial force in the rafter are:

Bending moment 348 kNm  
 Axial force 57 kN




M24 general grade bolts at 100 c/c  
 (used as 'ordinary' bolts)

Distribution of applied loading [26.1.2]

By moments about top flange [26.1.3]

$$348 \times 10^3 - 57 \left[ \frac{406.4}{2} - \frac{12.8}{2} \right] = 2F_1 \times 64 + 2F_2 \times 344 + (2F_3 + 2F_4) \times 531$$

|   |   |  |                               |
|---|---|--|-------------------------------|
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|   | <p>Design code</p> <p><i>B55950</i></p>                                   | <p>Made by <i>BDC</i></p> <p>Checked by <i>GWO</i></p> | <p>Sheet no.</p> <p>2</p>     |

$$= \frac{2F_4}{531} [ 2 \times 531^2 + 344^2 + 64^2 ]$$

$$F_1 = 15.7 \text{ kN}$$

$$F_2 = 84.4 \text{ kN}$$

$$F_3 = F_4 = 130.3 \text{ kN}$$

*Reaction at top flange*

$$= F_c = 2 (15.7 + 84.4 + 130.3 + 130.3) + 57 \cos 14^\circ$$

$$= 776.7 \text{ kN}$$

*Beam flanges*

$$\text{Capacity of flange} = p_y A$$

$$= 355 \times 177.8 \times 12.8 \times 10^{-3}$$

$$= 807.9 \text{ kN}$$


*Compression in top flange*

$$= \frac{F_c}{\cos 14^\circ} = \frac{776.7}{\cos 14^\circ} = 800.5 \text{ kN} < 807.9 \text{ kN OK}$$

*Tension in bottom (haunch) flange*  $< 2 ( F_3 + F_4 )$

$$= 4 \times 130.3 = 521.2 \text{ kN} < 807.9 \text{ kN OK}$$

*(In practice part of  $F_3$  will be carried by the web and the middle flange.)*

|   |   |   |                    |
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***End plate*** [25.3.5]

*By inspection, design will be governed by extended portion at bottom of detail.*

*Try 200 mm wide plate.*

*(Assume 10 mm fillet welds to bottom flange)*

*Distance from centreline of bolt to toe of fillet weld*

$$= b = 55 - 10 = 45 \text{ mm}$$

*Effective length of end plate per bolt* [25.3.2]

$$= w = \frac{1}{2} \times 200 = 100 \text{ mm} \quad [25.3.3]$$

*(In this case  $\frac{1}{2} \times$  flange width governs 'w')*

*With equal moments at bolt line and root*

$$M = \frac{F_4 b}{2} = \frac{130.3 \times 45}{2} = 2932 \text{ Nm}$$


$$\text{Moment capacity} = p_y \times \frac{w T^2}{4}$$

$$\begin{aligned} \text{Minimum thickness} &= \left[ \frac{4 \times 2932 \times 10^3}{265 \times 100} \right]^{0.5} \\ &= 21.0 \text{ mm} \end{aligned}$$

*Use 200 × 25 end plate × 670 Grade 43.*

*Take advantage of 'excess' plate thickness to reduce prying force (and bolt size).*

$$\begin{aligned} \text{Moment capacity} &= 265 \times \frac{100 \times 25^2}{4 \times 10^3} \\ &= 4141 \text{ Nm} \end{aligned}$$

|   |   |   |                    |
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*Moment required at bolt line*

$$= M_b = F_d b - M_{root} = 130.3 \times 45 - 4141 = 1723 \text{ Nm}$$

*Distance from centreline of bolt to prying force* [25.3.1]

$$= n = \text{edge distance but } \neq 2T$$

$$= 50 \text{ mm}$$

$$\text{Prying force} = \frac{M_b}{n} = \frac{1723}{50} = 34.5 \text{ kN}$$

*'Serviceability' check for minimum prying force*

$$Q = \frac{b}{2n} \left[ F - \frac{\beta \gamma p_o w T^4}{27 n b^2} \right] \quad [25.3.1]$$

$$= \frac{45}{2 \times 50} \left[ 130.3 - \frac{2 \times 1.5 \times 0.587 \times 100 \times 25^4}{27 \times 50 \times 45^2} \right]$$

$$= 0.45 [ 130.3 - 25.2 ] = 47.3 \text{ kN} > 34.5 \text{ kN}$$

$$\text{Design bolt for } (F + Q) = 130.3 + 47.3$$

$$= 177.6 \text{ kN}$$


Bolts

*Tension capacity of M24 general grade HSF8 bolt, taken as* [25.3.1]  
*0.64 U<sub>f</sub>*

$$= 0.64 \times 827 \times 353 \times 10^{-3}$$

$$= 186.8 \text{ kN} > 177.6 \text{ kN OK}$$

*Use M24 general grade HSF8 bolts (as ordinary bolts).*

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WeldsBottom (haunch) flange to end plate

$$\begin{aligned} \text{Load from bolts below flange} &= 2F_4 \\ &= 2 \times 130.3 = 260.6 \text{ kN} \end{aligned}$$

$$\text{Load on weld} = \frac{260.6}{177.8} = 1.466 \text{ kN/mm}$$

Capacity of 10 mm fillet weld

$$= 10 \times 0.7 \times 215 \times 10^{-3} = 1.505 \text{ kN/mm OK}$$

*Weld bottom (haunch) flange to end plate with 10 mm fillet welds.*

Distribution of load ( $F_3$ ) from bolt between lower flange and haunch

*(Assume 6 mm fillet welds, except for 10 mm fillet weld to bottom haunch flange.)*

Centreline of bolt to toe of haunch flange weld

$$= b_x = 57 - 10 = 47 \text{ mm}$$

Centreline of bolt to toe of web weld


$$= b_y = \frac{100}{2} - \frac{7.8}{2} - 6 = 40 \text{ mm}$$

Centreline of bolt to toe of weld to 'middle' flange

$$= b_z = 56 - 6 = 50 \text{ mm}$$

Effective length of plate at haunch flange

$$= w_x = \frac{200 - 100}{2} + 0.7 \times 40 = 78 \text{ mm}$$

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|   | <p>Design code</p> <p><b>BS5950</b></p>                                  | <p>Made by</p> <p><b>BDC</b></p> <p>Checked by</p> <p><b>GWO</b></p> | <p>Sheet no.</p> <p>6</p>     |

*Effective length of plate at web*

$$= w_y = 0.7 \times 47 + 0.7 \times 50 = 68 \text{ mm}$$

*Effective length of plate at 'middle' flange*

$$= w_z = w_x = 78 \text{ mm}$$

(a) *Plastic distribution of load (proportional to  $\frac{w}{b}$ )* [25.3.4]

*Load supported by haunch flange*

$$= \left[ \frac{\frac{78}{47}}{\frac{78}{47} + \frac{68}{40} + \frac{78}{50}} \right] \times 130.3 = 44.0 \text{ kN}$$

*Load supported by web* = 45.0 kN

*Load supported by middle flange* = 41.3 kN


(b) *Elastic distribution of load (proportional to  $\frac{w}{b^3}$ )*

*Load supported by haunch flange*

$$= \left[ \frac{\frac{78}{47^3}}{\frac{78}{47^3} + \frac{68}{40^3} + \frac{78}{50^3}} \right] \times 130.3 = 40.2 \text{ kN}$$

*Load supported by web* = 56.8 kN

*Load supported by middle flange* = 33.4 kN

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**Welds** (taking higher of (a) and (b) above)

**End plate to web**

$$\begin{aligned}
 \text{Load on weld} &= \frac{56.8}{2 \times 47} \\
 &= 0.604 \text{ kN/mm}
 \end{aligned}$$

Use 6 mm fillet welds.

**End plate to middle flange**

Take equal lengths of weld either side of bolt line to avoid eccentricity calculations.

$$\begin{aligned}
 \text{Load on weld} &= \frac{41.3}{2 \times \frac{1}{2} (177.8 - 100)} \\
 &= 0.531 \text{ kN/mm}
 \end{aligned}$$

Use 6 mm fillet welds.

**Top flange to end plate**

*Horizontal component of flange force*

$$= F_c = 776.7 \text{ kN}$$

*Vertical component of flange force*


$$= F_c \tan 14^\circ = 776.7 \tan 14^\circ = 193.7 \text{ kN}$$

Fit end plate to flange and take horizontal component in direct compression and vertical component in shear on fillet welds.

$$\text{Load on weld} = \frac{193.7}{2 \times 177.8} = 0.545 \text{ kN/mm}$$

Weld end plate to rafter with 6 mm fillet welds (except for 10 mm fillet welds on bottom flange).



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|   | <p>Design code</p> <p><b>BSS950</b></p>                                  | <p>Made by</p> <p><b>BDC</b></p> <p>Checked by</p> <p><b>GWO</b></p> | <p>Sheet no.</p> <p>8</p>     |

Connection of haunch flange to rafter flange

Use full strength butt weld for flange connection.

If haunch flange were fully stressed at this point,

$$\text{flange force} = p_y A = 807.9 \text{ kN}$$

Component of force perpendicular to rafter

$$= 807.9 \sin 14^\circ = 195.4 \text{ kN}$$

Assume stiff bearing length = flange thickness and take 1 in 2.5 spread to one side only in consideration of the flange being fully stressed. [25.1]

Local "bearing" capacity of web 4.5.3


$$= [12.8 + 2.5 \times (12.8 + 10.2)] \times 7.8 \times 355 \times 10^{-3}$$

$$= 194.7 \text{ kN}$$

$$\approx 195.4 \text{ kN} \text{ Stiffeners not required}$$

Other parts of the detail (e.g. the web of the haunch) are satisfactory by inspection.

If the apex detail is part of the same frame as the eaves detail in example 9, it may be desirable to standardize the bolt size and design both details using M24 general grade IISFG bolts.

|  |   |   |                       |                    |
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|  |   | Design code<br><b>BS5400</b>  | Made by<br><b>BDC</b> | Sheet no. <b>I</b> |
|  |   | Checked by<br><b>GWO</b>  |                       |                    |

The connection is for a 1500 mm × 600 mm plate girder, with 40 mm thick flanges and a 15 mm thick web (Grade 43).

The factored loading for the ultimate limit state is:

Bending moment                      4783 kNm

Axial tensile load                    113 kN

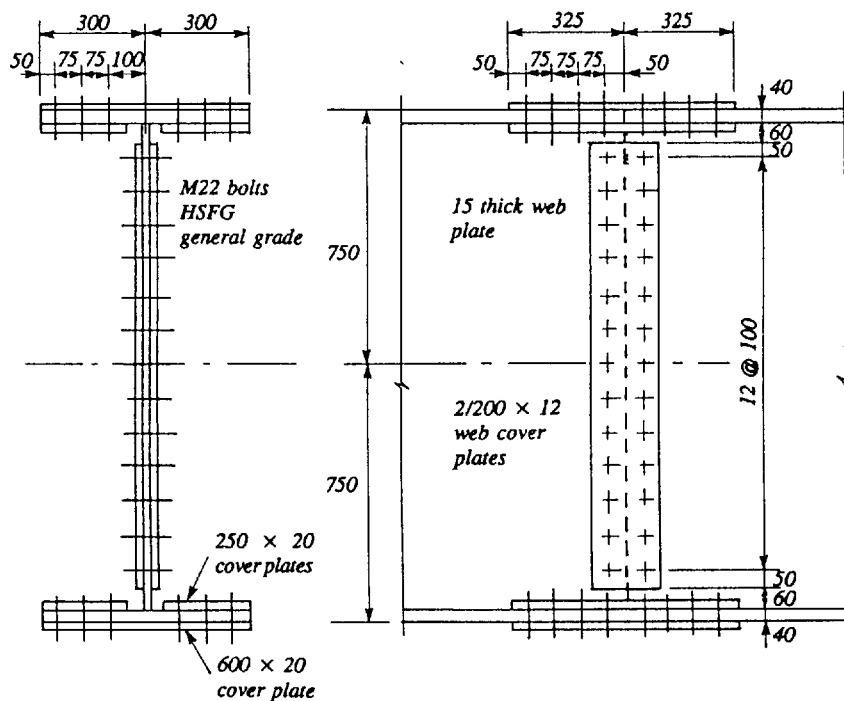
Shear                                    653 kN


The loading for the serviceability limit state is:

Bending moment                      3565 kNm

Axial tensile load                    85 kN

Shear                                    496 kN



|  |   |   |   |                    |
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|  |   | Design code<br><b>BS5400</b>  | Made by<br><b>BDC</b><br>Checked by<br><b>GWO</b> | Sheet no. 2        |

*Properties of plate girder*

$$\begin{aligned}
 I &= 2.916 \times 10^6 \text{ cm}^4 \\
 A &= 693 \text{ cm}^2
 \end{aligned}$$

Web splice

Try a single line of 13 bolts at 100 mm vertical pitch, 50 mm from centre of joint.

(a) Ultimate limit state

*Bending stress in web of girder at level of top and bottom bolts due to moment*

$$= f_b = \frac{M_y}{I} = \frac{4783 \times 10^6 \times 600}{2.916 \times 10^6 \times 10^4} = 98.4 \text{ N/mm}^2$$

*Horizontal shear force on bolt due to moment*

$$\begin{aligned}
 &= f_b \times \text{bolt pitch} \times t \\
 &= 98.4 \times 100 \times 15 \times 10^{-3} = 147.6 \text{ kN}
 \end{aligned}$$

*Average stress on girder due to axial load*


$$= f_a = \frac{F_a}{A} = \frac{113 \times 10^3}{693 \times 10^2} = 1.63 \text{ N/mm}^2$$


*Horizontal shear force on bolt due to axial load*

$$\begin{aligned}
 &= f_a \times \text{bolt pitch} \times t \\
 &= 1.63 \times 100 \times 15 \times 10^{-3} = 2.4 \text{ kN}
 \end{aligned}$$

*Vertical shear force on bolt due to shear*

$$= \frac{V}{n} = \frac{653}{13} = 50.2 \text{ kN}$$

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|---|---|---|--------------------|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN  | Subject<br><b>No.9 PLATE GIRDER.<br/>         BOLTED COVER PLATE<br/>         SPLICE.</b> |   | Chapter ref.<br>26 |
|   | Design code<br><b>BS5400</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>3</b> |
| <p><b>Horizontal shear force on bolt due to moment due to eccentricity</b> <span style="float: right;"><b>[23.4.2]</b></span></p> $= \frac{P \times e \times r_i}{\sum_n r_i^2}$ $= \frac{653 \times 50 \times 600}{2(100^2 + 200^2 + 300^2 + 400^2 + 500^2 + 600^2)}$ $= 10.8 \text{ kN}$ <p><b>Resultant shear force ( = vector sum of vertical and horizontal shear forces)</b></p> $= \sqrt{50.2^2 + (147.6 + 2.4 + 10.8)^2}$ $= 168.5 \text{ kN}$ <p><b>Try M22 general grade HSFG bolts in "double shear" with 12 mm thick cover plates.</b></p> <p><b>Friction capacity per bolt ( <math>\mu = 0.45</math> )</b> <span style="float: right;"><b>14.5.4.2</b></span></p> $= \frac{k_h F_v \mu N}{\gamma_m \gamma_{f_3}} = \frac{1.0 \times 177 \times 0.45 \times 2}{1.3 \times 1.1}$ $= 111.4 \text{ kN}$ <p><b>Shear capacity per bolt</b> <span style="float: right;"><b>14.5.3.4</b></span></p> $= \frac{\sigma_q n A_{eq}}{\gamma_m \gamma_{f_3} \sqrt{2}} = \frac{635 \times 10^{-3} \times 2 \times 303}{1.1 \times 1.1 \times \sqrt{2}}$ $= 224.9 \text{ kN}$ <p><b>Bearing capacity on web</b> <span style="float: right;"><b>14.5.3.6</b></span><br/>         (edge distance = 2 × hole diameter)</p> $= \frac{k_1 k_2 k_3 k_4 \sigma_y}{\gamma_m \gamma_{f_3}} \times d_{bolt} \times t$ |   |   |                    |

|  |   |   |                           |
|--|---|---|---------------------------|
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|  | Design code<br><b>BS5400</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>4</b>        |

$$= \frac{1.0 \times 1.97 \times 1.2 \times 1.5 \times 275 \times 10^{-3} \times 22 \times 15}{1.05 \times 1.1}$$

$$= 278.6 \text{ kN}$$

**Bearing capacity on cover plates** 14.5.3.6  
 (edge distance = 2.08 × hole diameter)

$$= \frac{1.0 \times 2.01 \times 0.95 \times 1.5 \times 275 \times 10^{-3} \times 2 \times 22 \times 12}{1.05 \times 1.1}$$

$$= 360.1 \text{ kN}$$

**Shear capacity governs design.** 14.5.4.1.1

**Bolt capacity > resultant force on bolt**  
 (224.9 kN) (168.5 kN)

but, since capacity is based on shear strength, serviceability check is required. Table 1  
14.5.4.1.2

**(b) Serviceability limit state**

Resultant shear force = 125.9 kN  
 (using the same procedure as for the ultimate limit state)

Friction capacity per bolt ( $\mu = 0.45$ ) 14.5.4.2


$$= \frac{k_h F_y \mu N}{\gamma_m \gamma_{f3}} = \frac{1.0 \times 177 \times 0.45 \times 2}{1.2 \times 1.0}$$

$$= 132.8 \text{ kN} > \text{resultant shear force OK}$$

Note that in this example the serviceability check governs the design.

**Flange splices**

Assume that the area of web associated with the web splice extends half a bolt pitch beyond the top and bottom bolts.

|  |   |   |                           |
|--|---|---|---------------------------|
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|  | Design code<br><b>BS5400</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>5</b>        |

*Second moment of area of portion of web where its share of the applied moment and axial load is carried by the web splice*

$$\begin{aligned}
 = I'_w &= \frac{t d^3}{12} = \frac{15 \times 1300^3}{12 \times 10^4} \\
 &= 0.275 \times 10^6 \text{ cm}^4
 \end{aligned}$$

*Area of the same portion of web*

$$\begin{aligned}
 = A'_w &= t d = 15 \times 1300 \times 10^{-2} \\
 &= 195 \text{ cm}^2
 \end{aligned}$$

*Proportion of applied moment carried by web splice*

$$= \frac{I'_w}{I_{girder}} = \frac{0.275 \times 10^6}{2.916 \times 10^6} = 0.094$$

*Proportion of axial load carried by web splice*

$$= \frac{A'_w}{A_{girder}} = \frac{195}{693} = 0.281$$


**(a) Ultimate limit state**

*Force to be carried by flange splice*

$$\begin{aligned}
 &= \frac{4783 \times 10^3}{(1500 - 40)} \times (1 - 0.094) + \frac{113}{2} (1 - 0.281) \\
 &= 2968 + 41 = 3009 \text{ kN}
 \end{aligned}$$

*Try M22 general grade HSFG bolts in "double shear" with 20 mm thick cover plates.*

*By inspection (from web splice design) shear capacity governs (224.9 kN per bolt).*

|  |   |   |                    |
|--|---|---|--------------------|
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|  | Design code<br><b>BS5400</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. <b>6</b> |

$$\text{No. of bolts required} = \frac{3009}{224.9} = 13.4$$

(b) Serviceability limit state

$$\text{Force to be carried by flange splice} = 2243 \text{ kN}$$

(using the same procedure as for the ultimate limit state)

$$\text{Friction capacity per bolt} = 132.8 \text{ kN}$$

$$\text{No. of bolts required} = \frac{2243}{132.8} = 16.9$$

As with the web connection, the serviceability check governs the design.

3 rows of 6 bolts would satisfy the design, but if there is any lack of fit the row of bolts next to the joint may be only partly effective as far as friction capacity is concerned. Therefore, since the slip (serviceability limit state) is critical, use 4 rows of 6 bolts each side of joint for flange splices M22 general grade HSFG bolts.

Splice plates


Effective area required for cover plates

$$\begin{aligned}
 &= \frac{P \gamma_m \gamma_{f_3}}{\sigma_y \times 0.8} = \frac{3009 \times 10^3 \times 1.05 \times 1.1}{275 \times 0.8} && 14.4.3.2 \\
 &= 15797 \text{ mm}^2
 \end{aligned}$$

Inner splice plates, try 2 No. 250 × 20 mm

$$\begin{aligned}
 \text{Effective area} &= k_1 k_2 A_t \quad (\text{but } \leq A) && 11.3.2 \\
 &= 2 \times 1.0 \times 1.2 (250 - 3 \times 24) \times 20 \\
 &= 8544 \text{ mm}^2 \\
 &> \frac{15797}{2} \text{ OK}
 \end{aligned}$$

Use 2 No. 250 × 20 mm

|   |   |   |                    |
|---|---|---|--------------------|
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|   | Design code<br><b>BSS400</b>  | Made by <b>BDC</b><br>Checked by <b>GWO</b> | Sheet no. 7        |

*Use 600 × 20 mm outer splice plates to flanges.*

**Flanges**

*Moment at end of splice*

$$= 4783 + 653 (3 \times 75 + 50) \times 10^{-3} = 4963 \text{ kNm}$$

*Average stress in tension flange*

$$= \frac{4963 \times 10^6 \times (1500 - 40) \times 0.5}{2.916 \times 10^6 \times 10^4} = 124.2 \text{ N/mm}^2$$

$$\text{Flange force} = 124.2 \times 600 \times 40 \times 10^{-3} = 2981 \text{ kN}$$

*Effective area of tension flange*

11.3.2

$$= k_1 k_2 A_t \text{ (but } \leq A)$$

$$= 1.0 \times 1.2 (600 - 6 \times 24) \times 40 = 21888 \text{ mm}^2$$

*Flange capacity*

$$= \frac{\sigma_y A_e}{\gamma_m \gamma_{f3}}$$

11.5.1

$$= \frac{275 \times 21888 \times 10^{-3}}{1.05 \times 1.1}$$

$$= 5211 \text{ kN} > \text{flange force OK}$$



## Chapter 27

# Foundations and holding-down systems

by HUBERT BARBER

### 27.1 Foundations

#### 27.1.1 Types of foundation

Pad foundations are used primarily to support the major structural elements in either sheds or multi-storey buildings. The pad foundations to major elements may be either mass concrete or reinforced concrete, the latter when either heavy loads or very poor ground conditions are present. They may be used in the context of cladding to support intermediate posts carrying sheeting rails, in which case the load is almost all from wind forces and is horizontal.

Strip foundations are used in steel-framed buildings to support external masonry or brickwork cladding and masonry internal partitions. In some cases the ground floor is thickened at these locations to provide a foundation but care should be taken with respect to the appropriate depth for clay or frost heave and for compatibility between such foundations and those of the main frame.

Piled foundations, either driven, bored or cast in place, are used on sites where ground conditions are poor or for buildings or structures in which differential settlement is critical. They may also be required in circumstances where heavy concentrations of load occur. In general when piled foundations are used the whole of the construction should be supported on piles. The ground floor slab, ground floor cladding and internal partitions should be carried by ground beams between the pile cap locations. If it is necessary for reasons of economy to support the ground floor independently, provision should be made for differential settlement by the inclusion of suitable movement joints.

Ground improvement techniques are appropriate for some types of poor ground. The most usual techniques are vibro-compaction or vibro-replacement but dynamic compaction can also be useful for improvement of large isolated sites. Ground improvement specialists or specialist consultants should be approached as economy will be the most important factor in the decision.

Typical foundation layouts are shown in Fig. 27.1.

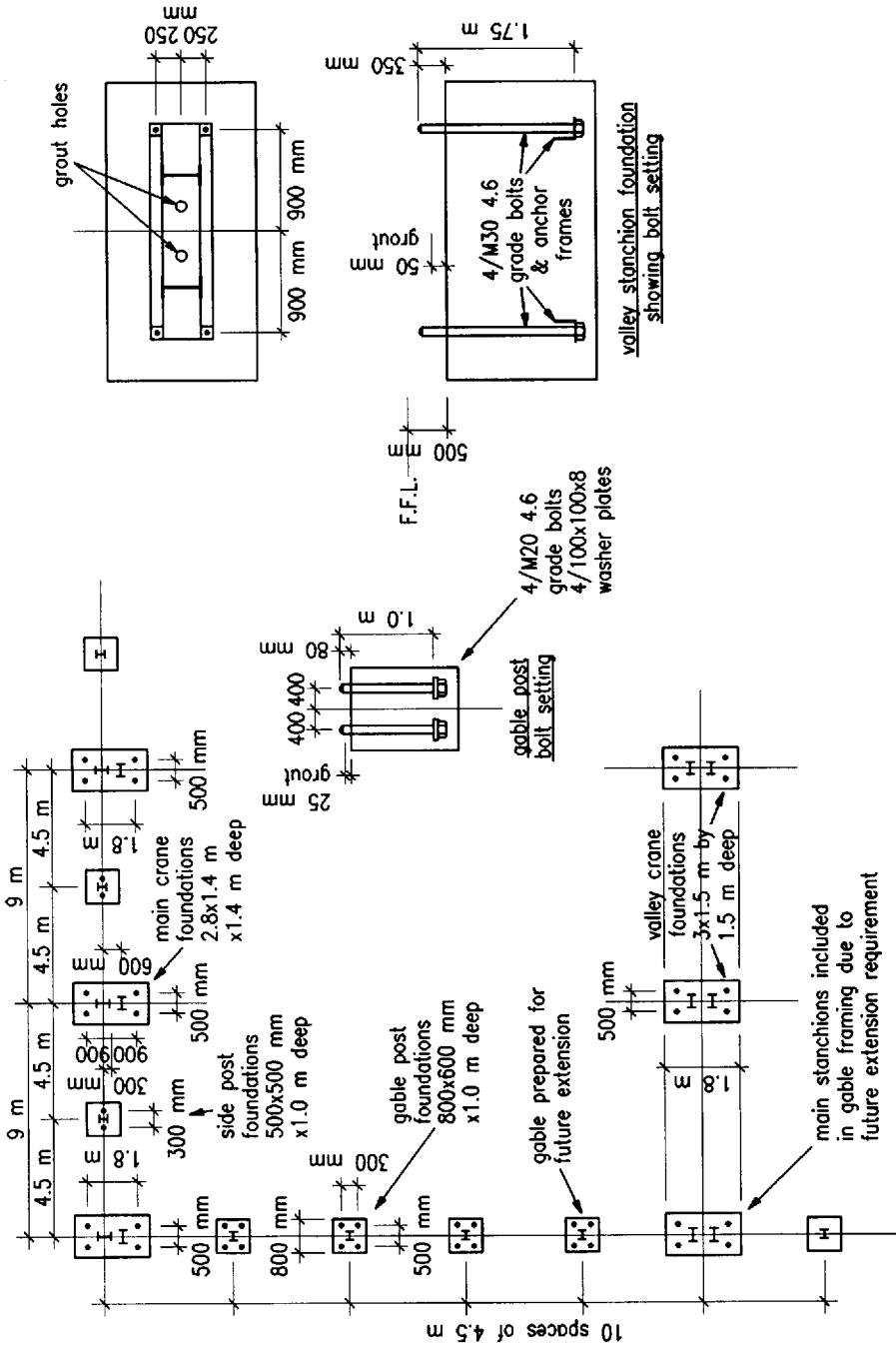


Fig. 27.1 Part plan of typical two-bay crane shed

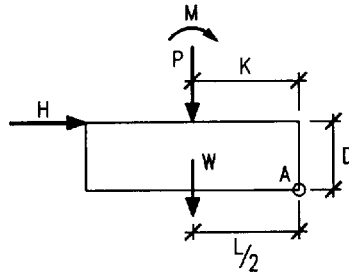


Fig. 27.2 Stability of foundation

### 27.1.2 Design of foundations

In order to assess the distribution of pressure under a foundation it is necessary to make a reasonable estimate of the weight of the foundation. In addition to distributing the forces to the ground the foundation block is also required to provide stability in cases where overturning moments are present.

Referring to Fig. 27.2, loads  $P$ ,  $H$  and  $M$  are factored as appropriate while  $W$ , the foundation mass, is factored by 1.0, being a restoring moment. Moments about A give

$$M + HD - PK - \frac{WL}{2} \leq 0$$

From this a minimum value of  $W$  for stability is produced.

The minimum value for  $D$  for a mass concrete foundation is established by 45° dispersal from the edge of the baseplate shown in Fig. 27.3. Shallower foundations can be used if they are suitably reinforced.

The distribution of pressure under the foundation is then assessed as follows.

#### Case 1

See Fig. 27.4(a):

$$f_g = \frac{P + W}{LB} \pm \frac{(M + DH)6}{BL^2}$$

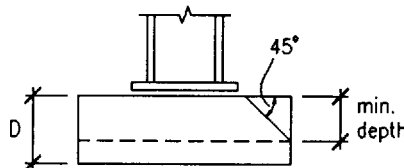


Fig. 27.3 Thickness of foundation

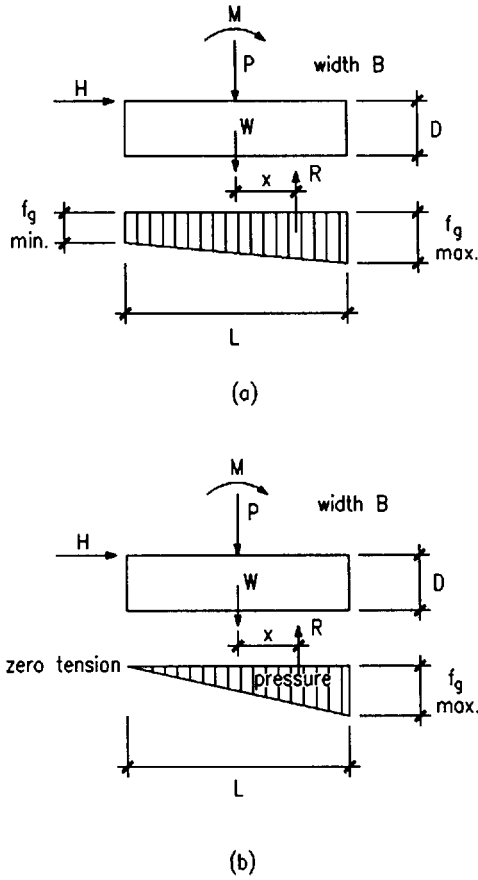


Fig. 27.4 Ground pressure – Case 1

It is necessary for  $f_{g \text{ max}}$  to be less than the stipulated ground bearing capacity for the foundation to be satisfactory.

For  $f_{g \text{ min}}$  to be zero (Fig. 27.4(b)):

$$\frac{P + W}{LB} - \frac{(M + DH)6}{BL^2} = 0$$

Replacing the forces by the resultant acting at eccentricity  $x$

$$\frac{R}{LB} - \frac{6Rx}{BL^2} = 0$$

from which

$$x = \frac{L}{6}$$

This is the limiting condition for the application of Case 1.

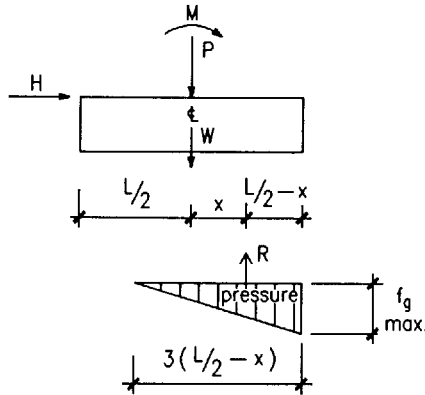


Fig. 27.5 Ground pressure – Case 2

Case 2

This occurs when  $f_{gmin}$  is negative. As no tension can exist between the soil and the underside of the concrete base a compressive stress wedge is formed at the compression side of the foundation. The summation of the stress under the block must equal the resultant of the applied loads. When  $x > L/6$ , the length of the triangular stress wedge is three times the edge distance  $(L/2 - x)$  in order that the resultant acts at the centroid of the wedge. The theory proposes that  $3(L/2 - x)$  is the length of surface contact between the foundation and the ground (Fig. 27.5).

$$\frac{f_{gmax}}{2} \left(\frac{L}{2} - x\right) 3B = P + W$$

$$f_{gmax} = \frac{2(P + W)}{3B \left(\frac{L}{2} - x\right)}$$

When  $f_{gmax}$  exceeds the stipulated ground bearing pressure, dimensions  $B$  or  $L$  or both may be increased within the limits of economy, after which piling or ground improvement techniques can be investigated.

27.1.3 Sub-soil bearing pressure

Foundation bearing pressure should always be determined on the basis of experimental results and field assessments taken during the soil investigation. Almost

all sites have considerable variation of strength and quality of the sub-strata and it is therefore necessary to undertake a comprehensive investigation producing a large number of test results in order to be satisfied that reasonable average values are obtained for the various parameters. A factor of safety of 3 is usually applied to the bearing strength to obtain the safe foundation bearing pressure.

### 27.1.3.1 Clayey soils – Terzaghi's method

(1) Foundation long in relation to width i.e. strip footing.

$$q = cN_c + \gamma zN_q + 0.5\gamma BN_\gamma$$

where  $q$  = bearing capacity (ultimate) (kN/m<sup>2</sup>)

$c$  = cohesion (kN/m<sup>2</sup>)

$\gamma$  = bulk density of the soil (kN/m<sup>3</sup>)

$z$  = depth of foundation (m)

$B$  = breadth of foundation (m)

and  $N_c$ ,  $N_q$  and  $N_\gamma$  are constants dependent upon the angle of cohesion. These constants are given in graph form in soil engineering references; Table 27.1 gives approximate values as guidance only.

**Table 27.1** Terzaghi's constants for clayey soils

| $\phi$ | $N_c$ | $N_q$ | $N_\gamma$ |
|--------|-------|-------|------------|
| 0      | 5.7   | 1.0   | 0          |
| 10     | 10    | 3.0   | 2.0        |
| 20     | 18    | 8.0   | 6.5        |
| 30     | 36    | 21.0  | 20         |
| 35     | 60    | 50.0  | 45.0       |

(2) Square and circular foundations to isolated piers or columns.

The bearing capacity of foundations rectangular, square or circular is higher than that of strip footings. Terzaghi's expression is adjusted as follows:

$$q = 1.3cN_c + \gamma zN_q + 0.3\gamma BN_\gamma$$

while Skempton applies a factor  $(1 + 0.2B/L)$  to the Terzaghi strip footing calculation where  $B$  is the breadth and  $L$  the length. In the case of a square the enhancement factor is then 1.2.

### 27.1.3.2 Sandy or cohesionless soils

The appropriate site test for cohesionless soils is the standard penetration test (SPT) in which the number of blows of a standard weight is recorded for unit

penetration of a standard cylindrical implement. According to Meyerhof the ultimate bearing capacity is given, in  $\text{kN/m}^2$ , by

$$q = 10.7 \times NB \left( 1 + \frac{z}{B} \right)$$

where  $N$  is the number of blows per metre and  $q$ ,  $z$  and  $B$  are as before.

Cohesionless soils subject to flooding will suffer a reduction of capacity at water table level:

$$\text{capacity when flooded} = K \times \text{unflooded capacity}$$

where  $K = (\gamma - 9.8)/\gamma$  and  $\gamma$  is the soil bulk density given for convenience in  $\text{kN/m}^3$ .

## 27.2 Connection of the steelwork

### 27.2.1 Fixed and pinned bases

The function of a column baseplate is to distribute the column forces to the concrete foundation. In general a plain or slab base is used for pinned conditions or when there is very little tension between the plate and the concrete. A gusseted base is used occasionally to spread very heavy loads but more generally for conditions of large moment in relation to the vertical applied loads, the principal function of the gusset being to allow the holding-down bolt lever arm to be increased to give maximum efficiency while keeping the baseplate thickness to an acceptable minimum. Gusseted or built-up bases give an ideal solution for compound or twin crane stanchions in industrial shed buildings.

Fixed bases are used primarily in low-rise construction either in portal buildings specifically designed as 'fixed base' or in industrial sheds in which the main columns cantilever from the foundations. They are also used, though less frequently, in multi-storey rigid-frame construction. In each of these cases it is assumed by definition that no angular rotation takes place and although this is unlikely to be achieved it is generally accepted that sufficient rigidity can be obtained to justify the assumption.

Pinned bases are those in which it is assumed that there is no restraint against angular rotation. Although this is also difficult to achieve it is accepted that sufficient flexibility can be introduced by minimizing the size of the foundation and similarly reducing the anchorage system. Pinned bases are used in portal and in multi-storey construction.

Typical pinned and fixed bases are shown in Fig. 27.6.

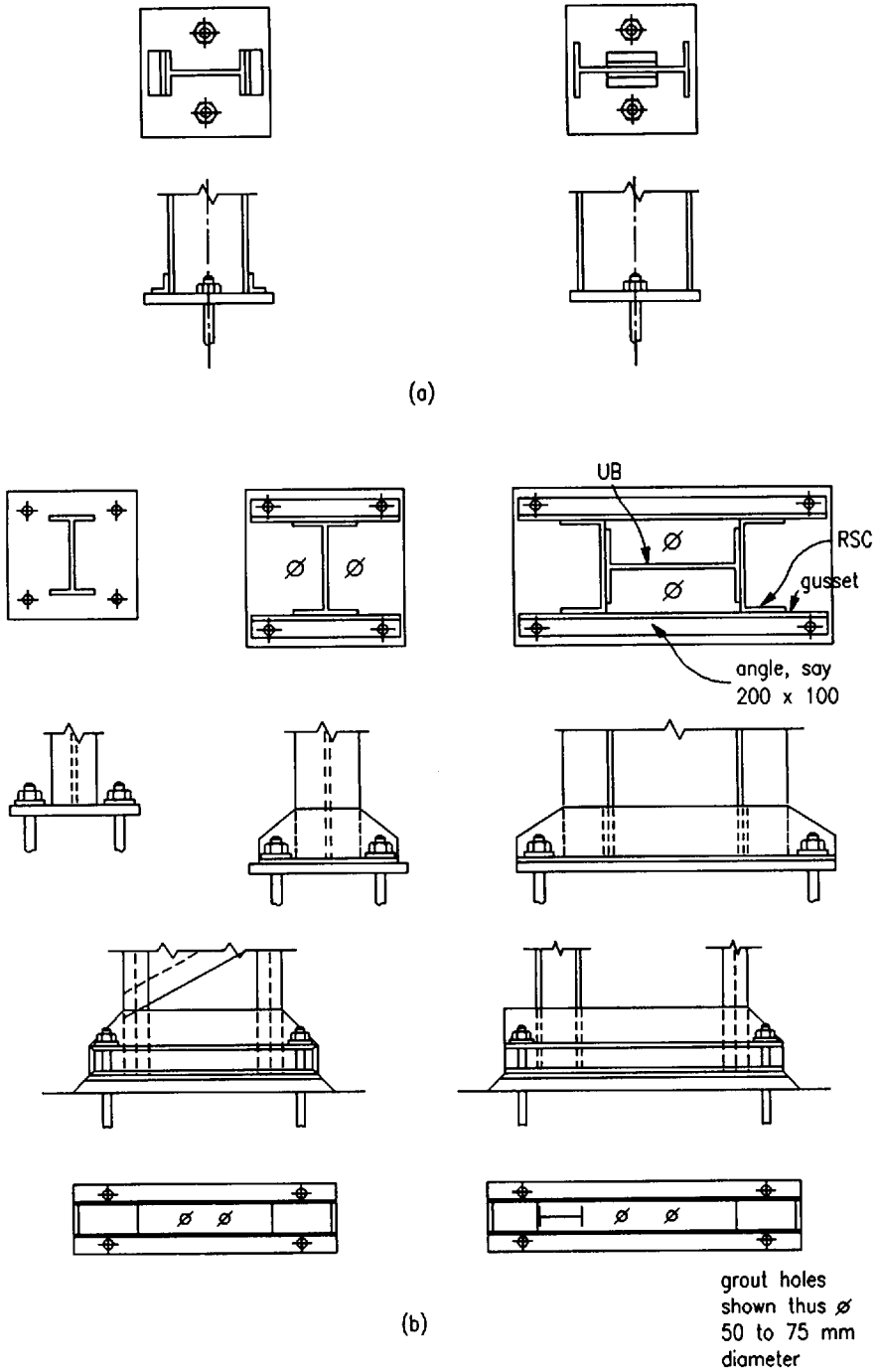


Fig. 27.6 Typical stanchion bases: (a) pinned bases, (b) gusseted and partially fixed bases



## 27.2.2 Baseplate design

### 27.2.2.1 Plain bases

#### (1) The effective area method

The empirical design method given in clause 4.13.2.2 of BS 5950 is to be used with caution in cases where the projections  $a$  and  $b$  are small and when the depth/width ratio of the column is high.

The effective area method given below will ensure adequacy in this respect. The plate thickness should never be less than the column flange thickness. The effective area method assumes that the whole of the axial load is spread on to an area of bedding material determined by dispersal through the plate to a boundary dimensioned  $K$  from the section profile as shown in Fig. 27.7(a). The resulting area is assumed to give an even distribution of pressure and the plate is assumed to cantilever the distance  $K$ .

The effective area is therefore given by

$$A_c = 2(B + 2K)(2K + T) + (D - 2T - 2K)(2K + t)$$

where  $B$  and  $D$  are the column dimensions,  $T$  is the flange thickness and  $t$  is the web thickness.

then  $\frac{W}{A_c} \nlessgtr$  the bearing strength of the bedding

The resulting quadratic is solved for  $K$  and the moment on the cantilever outstand,  $M$ , is given by

$$M = \frac{W}{A_c} \times \frac{K^2}{2}$$

then  $t_p = \left(\frac{6M}{p_{yp}}\right)^{\frac{1}{2}}$

where  $p_{yp} = 270 \text{ N/mm}^2$

(see the first worked example at the end of this chapter).

The method is also applied to tubular columns.

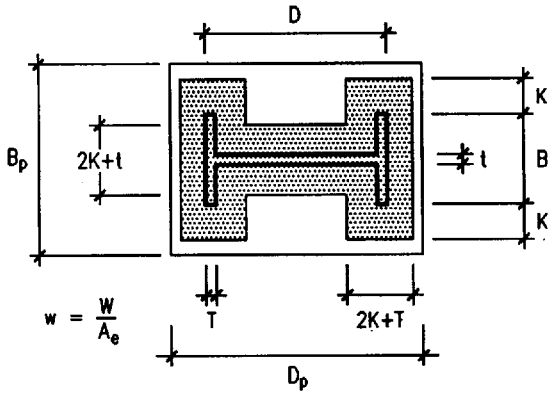
The dispersal dimension  $K$  taken radially on either side of the tube wall gives an annular contact area between the plate and the bedding material, as shown in Fig. 27.8(a). Then

$$A_c = (2K + t)(D - t)\pi$$

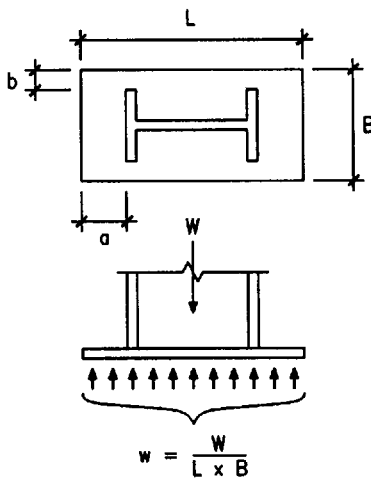
where  $D$  is the tube diameter and  $(W/A_c) \nlessgtr$  the bearing strength of the bedding.

After solving for  $K$ ,  $M$  and  $t$  are determined in the same way as for rolled sections (see the second worked example at the end of this chapter).

If  $K$  is greater than  $D/2$



(a)



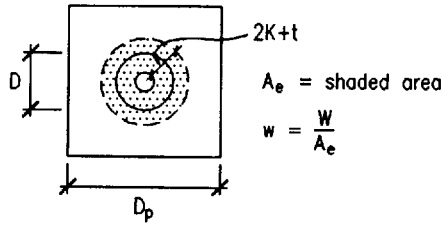
(b)

Fig. 27.7 Slab base design (a) the Effective Area Method (b) the Empirical Design Method (clause 4.13.2 or BS 5950)

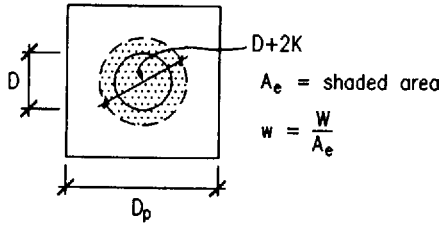
$$A_e = (D + 2K)^2 \frac{\pi}{4}$$

as shown in Fig. 27.8(b).

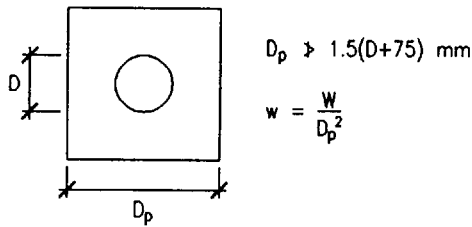
Similarly after solving for  $K$ ,  $M$  and  $t$  are obtained in the same way as for rolled sections (see the third worked example at the end of this chapter).



(a)



(b)



(c)

Fig. 27.8 Square base plate for CHS or solid column

(2) *The empirical design method*

In this method, given in clause 4.13.2 of BS 5950, it is assumed that the load from the column is evenly distributed at the underside of the plate. An empirical formula then defines the required baseplate thickness:

(a) for columns of I, H, channel, box or RHS (Fig. 27.7(b))

$$t = \left[ \frac{2.5w}{p_{yp}} (a^2 - 0.3b^2) \right]^{\frac{1}{2}}$$

(b) for circular solid or hollow columns (Fig. 27.8(c))

$$t = \left[ \frac{wD_p}{2.4p_{yp}} (D_p - 0.9D) \right]^{\frac{1}{2}}$$

where  $p_{yp}$  is the design strength of the plate,  $t$  is the required plate thickness,  $w$  is the pressure on the underside of the plate, assuming uniform distribution;  $a$  and  $b$  are the greater and lesser projections of the plates beyond the rolled section;  $D_p$  is the length of the side of the plate, or its diameter; and  $D$  is the diameter of the column.

NB  $D_p \leq 1.5 (D + 75)$  mm.

Typical solutions are included in the first and second worked examples at the end of this chapter.

In the event that the baseplate is oversized, that is, greater than is required for the bearing strength of the bedding material, in order to accommodate holding-down bolts, etc., the additional area may be taken as ineffective. The plate thickness may therefore be determined to suit the plate dimensions required for the bedding strength (see clause 4.13.2.1 of BS 5950).

In situations where the baseplate is of irregular shape or when the forces are eccentric giving non-uniform bearing pressures, the bending moments on the plate should be computed and the plate designed accordingly. The moment should not exceed  $1.2 p_{yp}Z_p$ , where  $Z_p$  is the elastic modulus and  $p_{yp} \geq 270$  N/mm<sup>2</sup> (Table 3.1.1 of BS 5950).

### 27.2.2.2 Gusseted bases

In a stiffened or gusseted base the moment in the gusset due to the bearing pressure under the effective area of the baseplate or due to the tensile forces in the holding-down bolts should not exceed  $p_{yg}Z_g$ , where  $Z_g$  is the elastic modulus of the gusset and  $p_{yg}$  is the design strength of the gusset ( $p_{yg} \geq 270$  N/mm<sup>2</sup>). When the effective area of the baseplate is less than its gross area, the connections of the gusset should be checked for the effects of a nominal distribution of bearing pressure on the gross area as well as for the distribution used in the design.

### 27.2.2.3 Beam bearing plates

Bearing plates at beam seatings are required to distribute the beam reaction to the masonry support at stress levels within the capacity of the masonry and to ensure that the web-crushing capacity of the beam is not exceeded. The distribution of bearing stresses under the plate is extremely complex although simplifying assumptions are usually made in appropriate cases.

The bending of the plate, shown in Fig. 27.9 in the direction transverse to the beam, will depend on the stiffness of the beam flange and the fixing of the flange

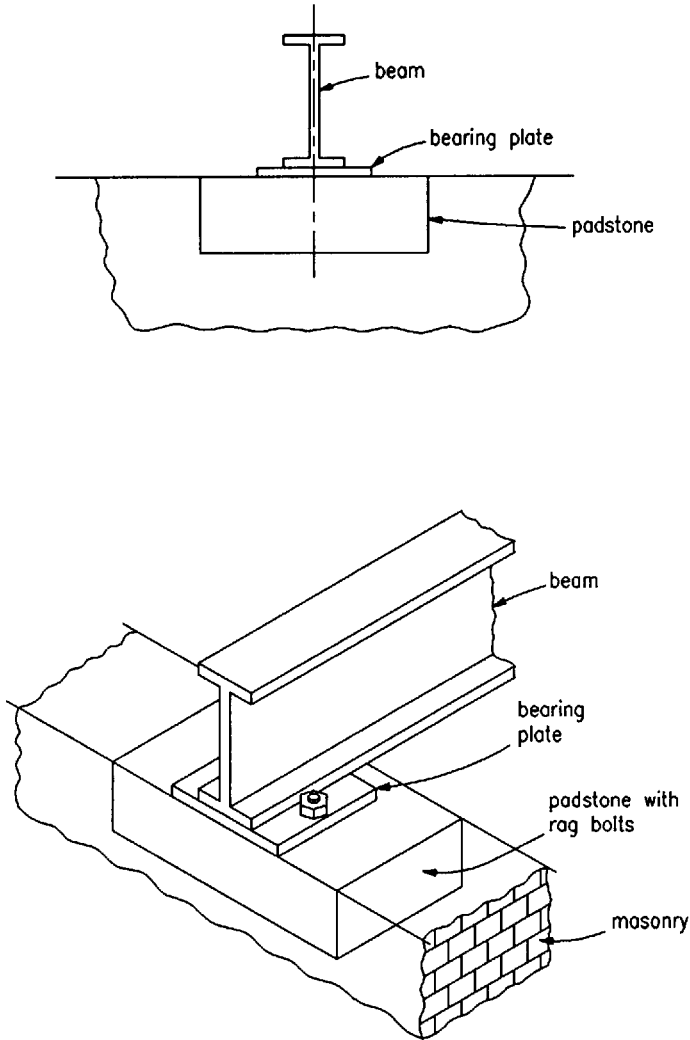


Fig. 27.9 Beam bearing

to the plate. It is usual to assume that the position of maximum bending is the outside edge of the root of the web and that the plate carries the whole of the bending.

In the longitudinal direction, shown in Fig. 27.10, the deflection and rotation of the beam due to its loading will cause a concentration of bearing at the front edge and, depending upon the load from above the bearing, a possible lifting of the back edge of the plate. It is often assumed, therefore, that the distribution will be either trapezoidal or triangular; possibly the triangle may not reach the back of

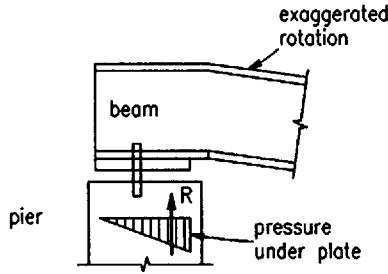


Fig. 27.10 Pressure under bearing plate (1)

the bearing. If it is expected that the front edge concentration will be high the plate is set back from the front of the pier as shown in Fig. 27.11. This is to reduce the possibility of spalling at the front of the pier but also has the advantage of applying the beam reaction more centrally to the masonry.

A method of assessing the rotation of the bearing has been proposed by Lothers. From this a more accurate estimate of the stress distribution can be made. The method, however, can only be applied in cases of isolated masonry piers and is dependent on the homogeneity of the masonry. It may be justified in cases of very heavy beam reactions provided the workmanship in constructing the pier can be reasonably guaranteed.

### 27.3 Analysis

#### 27.3.1 Bolt forces

The calculation of bolt forces, referring to Fig. 27.12, can be undertaken using the analogy of a reinforced concrete beam. Under elastic design principles a notional neutral axis is computed and from this the bolt lever arm established.

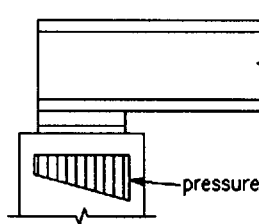
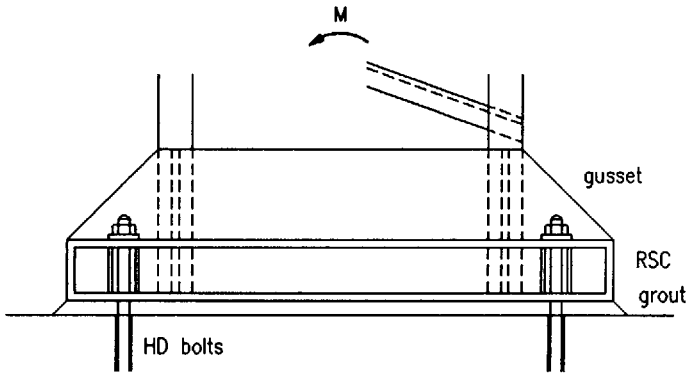
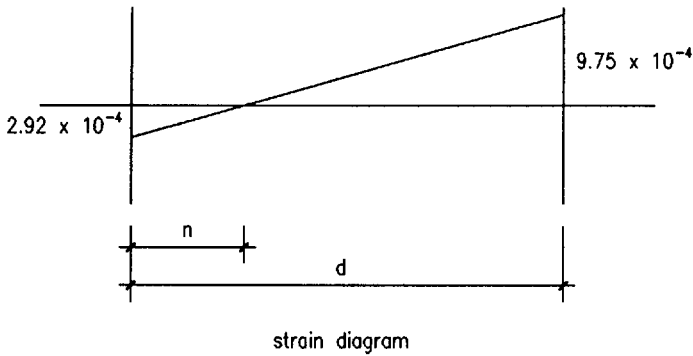


Fig. 27.11 Pressure under bearing plate (2)



(a)



(b)

Fig. 27.12 Reinforced concrete beam analogy

From Figure 2.1 of BS 8110:

$$\text{concrete strain at a stress of } 0.4f_{cu} = 0.8 \times 10^{-4} \left( \frac{f_{cu}}{\gamma_m} \right)^{\frac{1}{2}} = 2.92 \times 10^{-4}$$

Assuming  $f_{cu} = 20 \text{ N/mm}^2$  (grout) and  $\gamma_m = 1.5$ :

$$\text{steel strain} = \frac{195 \text{ N/mm}^2}{200 \text{ kN/mm}^2} = 9.75 \times 10^{-4}$$

taking the bolt strength as  $195 \text{ N/mm}^2$  (Table 32 of BS 5950) and  $E$ , the modulus of elasticity, as  $200 \text{ kN/mm}^2$ . Then

$$n = \frac{2.92 \times 10^{-4} d}{(2.92 + 9.75)10^{-4}} = 0.23d$$

(see Fig. 27.12 (b)).

However, the 'give' of the bolts over the distance of protrusion above the concrete or grout surface is greater than that which would occur internally in a concrete beam and the crushing of the grout is likely to be greater than that which would occur in a concrete beam.

These difficulties are overcome if the load factor principle is applied. The area required to transmit the compressive forces under the baseplate is calculated at the appropriate bearing strength of the concrete. The stress block may be assumed to be partly parabolic as shown in Figure 2.1 of BS 8110 or it may be approximated as a rectangle. The lever arm for the design of the bolts is then from the centroid of this stress block to the bolt position. The centroid of the stress block is often less than the edge distance from the compression edge of the plate to the holding-down bolt: it is therefore often assumed that the lever arm for the bolts is equal to the centres of the bolts. It is also very likely that the point of application of the compressive forces will be near to the holding-down bolts due to the extra stiffening that is often included in the vicinity of the bolts. This is illustrated in the typical design given as the fourth worked example at the end of this chapter.

### 27.3.2 Bolt anchorage

Anchorage of the holding-down bolts into the concrete foundation should be sufficient to cater for any uplift forces and to provide for any shears applied to the bolts. Attention is particularly directed to the last paragraph of clause 6.7 of BS 5950 which states that rag bolts and indented foundation bolts should not be used to resist uplift forces. The elastic elongation of indented screwed rods or bolts under tension causes the breakdown of the grout surrounding the bolt. This is even more critical in the case of resinous grouts.

The failure mode of bolts pulled from a concrete block is shown in Fig. 27.13(a); a reasonable approximation is shown in Fig. 27.13(b). The surface

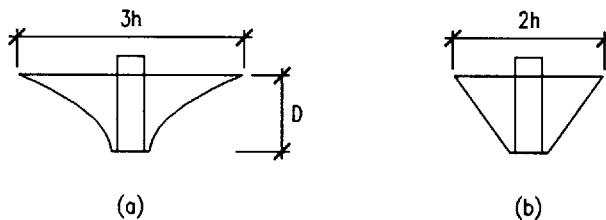


Fig. 27.13 Typical pull-out from concrete block



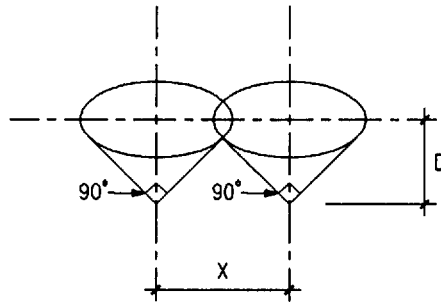


Fig. 27.14 Conical pull-out

area of the conical pull-out (Fig. 27.14) is  $4.44D^2$ , where  $D$  is the depth of embedment. The factored tensile capacity of an M20 (4.6) bolt is  $245 \times 195 \times 10^{-3} = 47.7$  kN. For an M20 HD bolt 450 mm long with an embedment of say 350 mm

the conical surface is  $4.44 \times 350^2 = 544 \times 10^3 \text{ mm}^2$

the surface stress is  $\frac{47.7 \text{ kN}}{544 \times 10^3} = 0.09 \text{ N/mm}^2$

As holding-down bolts usually act in pairs the conical pull-outs often overlap depending on the depth of embedment. The BCSA have tabulated the surface areas including those which overlap (Table 27.2).

## 27.4 Holding-down systems

### 27.4.1 Holding-down bolts

The most generally used holding-down bolts are of grade 4.6 although 8.8 grade are also available (see Table 27.3). They are usually supplied  $\square\square\times$ : square head, square shoulder, round shank, hexagon nut. Each bolt must be provided with an anchor washer (square hole to match the shoulder) or an appropriate anchor frame to embed in the concrete in circumstances of high uplift forces. In such cases the anchor frame may be composed of angles or channels. Typical frames are shown in Fig. 27.15. When long anchors are required a rod threaded at both ends may be used, and in exceptional circumstances when prestressing is required a high tensile rod (usually Macalloy bar) is adopted. In both these cases provision should be made to prevent rotation of the rod during tightening which may result in the embedded nut being slackened.

Corrosion of holding-down bolts to a significant extent has been reported in some instances. This usually occurs between the level of the concrete block and

**Table 27.2** Embedded lengths of holding-down bolts based on conical pull-out

| Depth, <i>D</i> (mm) | Distance between centres, <i>X</i> (mm) |        |       |       |       |       |       |       |       |       |       |
|----------------------|---|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                      | 75                                      | 100    | 125   | 150   | 200   | 225   | 300   | 450   | 600   | 750   | 1000  |
| 75                   | 402.1                                   | 445.1  | 479.9 | 499.8 | 499.8 | 499.8 | 499.8 | 499.8 | 499.8 | 499.8 | 499.8 |
| 100                  | 651.3                                   | 714.9  | 773.2 | 824.5 | 888.6 | 888.6 | 888.6 | 888.6 | 888.6 | 888.6 | 888.6 |
| 125                  | 955.3                                   | 1038.1 | 1117  | 1191  | 1316  | 1362  | 1388  | 1388  | 1388  | 1388  | 1388  |
| 150                  | 1315                                    | 1416   | 1514  | 1608  | 1780  | 1855  | 1999  | 1999  | 1999  | 1999  | 1999  |
| 200                  | 2199                                    | 2337   | 2473  | 2605  | 2859  | 2979  | 3298  | 3554  | 3554  | 3554  | 3554  |
| 225                  | 2724                                    | 2880   | 3034  | 3186  | 3479  | 3619  | 4006  | 4498  | 4498  | 4498  | 4498  |
| 300                  | 4633                                    | 4843   | 5052  | 5258  | 5664  | 5862  | 6434  | 7420  | 7997  | 7997  | 7997  |
| 450                  | 9950                                    | 10267  | 10583 | 10897 | 11521 | 11831 | 12743 | 14476 | 16022 | 17277 | 17994 |
| 600                  | 17266                                   | 17689  | 18112 | 18533 | 19373 | 19790 | 21032 | 23448 | 25735 | 27837 | 30715 |
| 750                  | 26581                                   | 27111  | 27640 | 28168 | 29221 | 29746 | 31312 | 34392 | 37371 | 40211 | 44507 |
| 1000                 | 46550                                   | 47256  | 47962 | 48667 | 50076 | 50779 | 52882 | 57048 | 61141 | 65134 | 71486 |

Effective conical surface area (allowing for overlap) (cm<sup>2</sup>)

Values to the right of the heavy zig-zag line are for two non-intersecting cones

**Table 27.3** Holding-down bolts; tension capacity per pair of bolts

| Nominal diameter (mm) | Tensile stress area (mm <sup>2</sup> ) <sup>b</sup> | Bolts grade 4.6@<br>195 N/mm <sup>2</sup><br>(kN) | Bolts grade 8.8@<br>450 N/mm <sup>2</sup><br>(kN) |
|-----------------------|---|---|---|
| M16                   | 314   | 61.22   | 141.30  |
| M20                   | 490   | 95.54   | 220.50  |
| M22 <sup>a</sup>      | 606   | 118.16  | 272.70  |
| M24                   | 706   | 137.66  | 317.70  |
| M27 <sup>a</sup>      | 918   | 179.00  | 413.10  |
| M30                   | 1122  | 218.78  | 504.90  |

<sup>a</sup> Non-preferred size

<sup>b</sup> Tensile stress areas are taken from BS 4190 and BS 3692

the underside of the steel baseplate, in aggressive chemical environments or at sites where moisture ingress to this level is recurrent. Fine concrete grout, well mixed, well placed and well compacted will provide the best protection against corrosion but in cases where this is not adequate for the prevailing conditions, an allowance may be made in the sizing of the bolts or by specifying a higher grade bolt which provides a larger factor of safety against tensile failure in the event that some corrosion does occur.

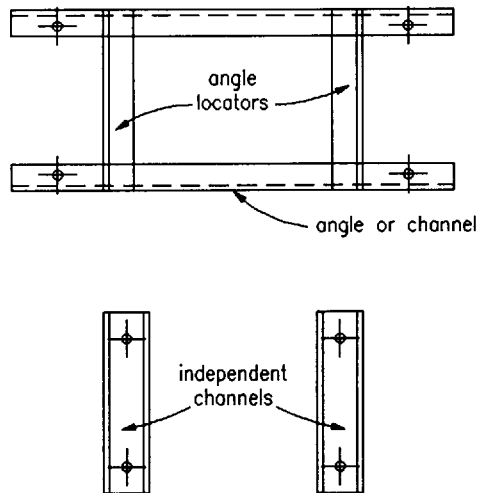


Fig. 27.15 Typical anchorages for holding-down bolts

### 27.4.2 Grouting

The casting-in of the holding-down bolts with adequate provision for adjustment requires that they are positioned in the concrete surrounded by a tube, conical or cylindrical, or a polystyrene former. After removal of the tube or former, which should be delayed until the last possible time before the erection of the columns, the available lateral movement of the bolts should be between three and four times the bolt diameter. In cases where open tubes are used they should be provided with a cap or cover to prevent the ingress of water, rubbish and mud. After erection, lining, levelling and plumbing of the frame the grout voids around the bolts should be cleaned out by compressed air immediately prior to grouting. The bolt grouting and baseplate filling should be done as two separate operations to allow shrinkage to take place. During the levelling and plumbing operations wedges and packings are driven into the grout space. Before final grouting these should be removed, otherwise, after shrinkage of the grout filling material, they will become hard spots, preventing the even distribution of the compressive forces to the concrete base.

### 27.4.3 Bedding

Bedding materials are required to perform a number of functions, one of which is the provision of the corrosion protection referred to earlier in section 27.4.1. In accordance with BS 5950, steel baseplates are designed for a compression under the plate of  $0.4f_{cu}$ , where  $f_{cu}$  is the cube strength of the filling. Design to BS 8110 and more recent design advice<sup>1</sup> recommend the use of a design strength of  $0.6 f_{cu}$ . The bedding material therefore transmits high vertical stresses including those resulting from the applied moment. The third function is to transmit the horizontal forces or shears resulting from wind or crane surge. It is clear therefore that the bedding material is a structural medium and should be specified, controlled and supervised accordingly.

For heavily-loaded columns or those carrying large moments resulting in high compressive forces the bedding should be fine concrete using a maximum aggregate of 10 mm size. The usual mix is  $1:1\frac{1}{4}:2$  with a water–cement ratio of between 0.4 and 0.45 (this is not suitable for filling the bolt tubes as it is too stiff; a pure cement water mix has suitable flow properties and is usually used). It also has high shrinkage properties and should be allowed to set fully before continuing with the bedding. A cement mortar mix is often used for moderately-loaded columns. A suitable mix would be  $1:2\frac{1}{2}$ . Weaker filling than this should only be used for lightly-loaded columns where the erection packs are left in position and transfer all the load to the foundation. In cases when erection packs are left in place it may be necessary to re-examine the baseplate design as load transference will be directly through the steel packs.

In order to facilitate the compaction of the bedding material, holes are cut in the baseplate of the order of 50 mm diameter or more, near to the centre of the plate in order to allow the escape of air pockets and to ensure that the bedding reaches to centre.


## References

1. The Steel Construction Institute/British Constructional Steelwork Association (1991) *Joints in Simple Construction*, Vol. 1. SCI/BCSA.

## Further reading for Chapter 27

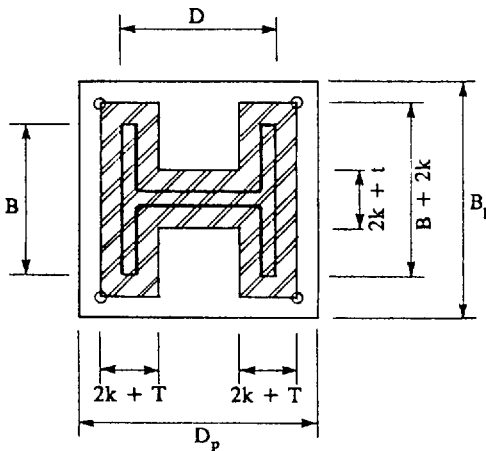
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A series of worked examples follows which are relevant to Chapter 27.

|  |  |  |
|--|--|--|
| <b>The Steel Construction Institute</b><br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>FOUNDATION<br/>EXAMPLE 1</b> | Chapter ref.<br><b>27</b>                  |
|  | Design code<br><b>BS5950: Part 1</b>       | Made by <b>HB</b><br>Checked by <b>GWO</b> |

**Problem**

Design a simple base plate for a  $254 \times 254 \times 73$  UC to carry a factored axial load of 1000 kN

**Design by the Effective Area Method using Reference 27.1**

$$\text{Bearing strength of concrete} = 0.6 f_{cu} - \text{take } f_{cu} \text{ as } 40 \text{ N/mm}^2$$

$$\text{Area required (in mm}^2\text{)} = \frac{1000 \times 10^3}{0.6 \times 40} = 41667 \text{ mm}^2$$


$$\text{Bearing area} = \text{hatched area}$$

$$= 2(B + 2k)(2k + T) + (D - 2T - 2k)(2k + t)$$

$$\therefore 2(254 + 2k)(2k + 14.2) + (254 - 28.4 - 2k)(2k + 8.6) = 41667$$

$$\therefore 4k^2 + 1506.8k - 32513 = 0$$

$$k = \frac{-1506.8 \pm \sqrt{1506.8^2 + 520208}}{8} = 20.46 \text{ mm}$$

|   |                                      |  |                    |
|---|--------------------------------------|--|--------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | <b>FOUNDATION<br/>EXAMPLE 1</b>      |  | 27                 |
|   | Design code<br><b>BS5950: Part 1</b> | Made by <b>HB</b><br>Checked by <b>GWO</b> | Sheet no. <b>2</b> |

$$t_p = \left[ \frac{6 \times 24 \times 20.46^2}{2 \times 270} \right]^{0.5} = 10.57$$

Use a base plate 300 × 300 × 15

Using the empirical method:

**Area required = 41667 i.e. 204 × 204 plate**

**Assume projection of 25 mm each dimension**


**Use 304 × 304 plate**

$$w = \frac{1000 \times 10^3}{304^2} = 10.82 \text{ N/mm}^2$$

$$t_p = \left[ 10.82 \times \frac{2.5}{270} (25^2 - 0.3 \times 25^2) \right]^{0.5}$$

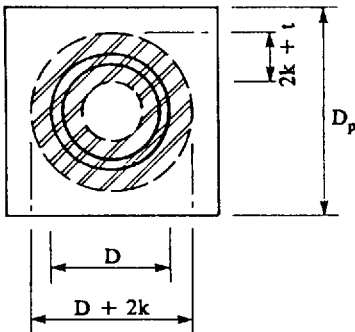
$$t_p = 6.62 \text{ mm}$$

***This is inadequate by the effective area method. This demonstrates the necessity for caution when the projections are small.***

|  |   |  |  |
|--|---|--|--|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject<br><b>FOUNDATION EXAMPLE 2</b> | Chapter ref.<br>27                         |
|  |   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>HB</b><br>Checked by <b>GWO</b> |

**Problem**

*Design a simple base plate for a 219 × 6.3 CHS to carry a factored axial load of 1010 kN*



219 × 6.3 CHS

Factored axial load = 1010 kN

Assumed bedding material  
 $f_{cu} = 40 \text{ N/mm}^2$

Design by the Effective Area Method using Reference 27.1

$$\text{Area required} = \frac{1010 \times 10^3}{0.6 \times 40} = 42083 \text{ mm}^2$$

$$\text{Area of shaded annulus} = (2k + t) (D - t) \pi = 42083$$

$$(2k + 6.3) (219 - 6.3) = 13395, \text{ hence } k = 28.3 \text{ mm}$$

$$t_p = \left[ \frac{6 \times 24 \times 28.3^2}{2 \times 270} \right]^{0.5} = 14.62 \text{ mm} \therefore \text{Use } 280 \times 280 \times 15 \text{ plate}$$


Using the empirical method:

$$w = \frac{1010 \times 10^3}{280^2} = 12.9 \text{ N/mm}^2$$

$$t = \left[ \frac{12.9}{2.4 \times 270} \times 280 (280 - 0.9 \times 219) \right]^{0.5} = 21.5 \text{ mm}$$

Attention is drawn to Clause 4.13.2.1 of BS 5950



|  |   |                         |             |
|--|---|-------------------------|-------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject                 | Chapter ref |
|  |   | FOUNDATION<br>EXAMPLE 3 | 27          |
| Design code  | Made by   | Sheet no.               |             |
| BS5950: Part 1   | HB  | I                       |             |
|  | Checked by  |                         |             |
|  | GWO   |                         |             |

**Problem**

Design a simple base plate for a 273 × 25 CHS to carry a factored axial load of 6340 kN

Strength of bedding material = 40 N/mm<sup>2</sup>

$$\text{Area required} = \frac{6340 \times 10^3}{0.6 \times 40} = 264167 \text{ mm}^2$$

Design by the Effective Area Method using Reference 27.1

$$(2k + 25)(273 - 25)\pi = 264167$$

from which  $k = 157 \text{ mm}$

$$\text{When } k > \frac{D - 2t}{2}$$

the bearing area is a circle of  $(D + 2k)$  diameter.

Then:

$$(D + 2k)^2 \frac{\pi}{4} = 264167$$

$$(273 + 2k)^2 = 336348$$

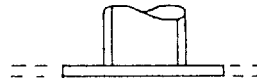
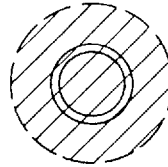
$$4k^2 + 1092k + 74529 = 336348$$


$$k = \frac{-1092 \pm [1092^2 - 16 \times (-261819)]^{0.5}}{8}$$

$$= 153$$

$$t_p = \left[ \frac{6 \times 24 \times 153^2}{2 \times 270} \right]^{0.5}$$

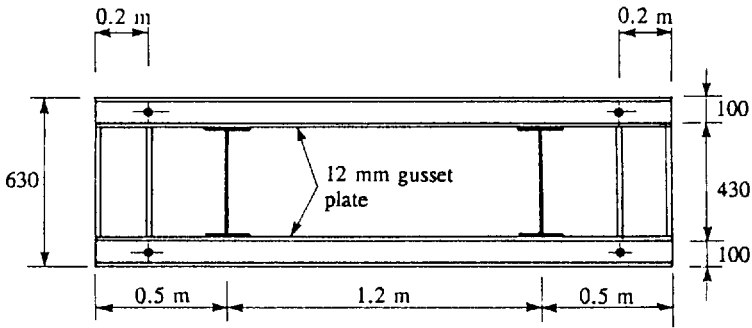
$$= 79 \text{ mm} \quad \therefore \text{Use } 600 \times 600 \times 80 \text{ plate}$$



|   |   |   |
|---|---|---|
| <p>The Steel Construction Institute</p>  <p>Silwood Park, Ascot, Berks SL5 7QN</p> | <p>Subject</p> <p><b>FOUNDATION EXAMPLE 4</b></p> | <p>Chapter ref.</p> <p><b>27</b></p>                  |
|   | <p>Design code</p> <p><b>BS5950: Part 1</b></p>   | <p>Made by <b>HB</b></p> <p>Checked by <b>GWO</b></p> |

**Problem**

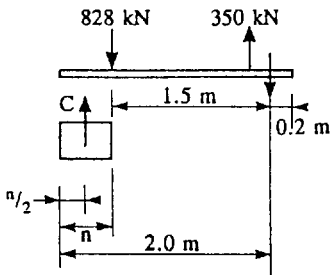
*Design a built-up base for the valley stanchion of a double bay crane shed that is shown below. The stanchion comprises twin 406 × 178 UB.*



*Taking moments about the tensile bolt, with  $n$ , the trial neutral axis as 0.4 m depth, and taking*


$$f_c = 0.4 f_{cu} = 8 \text{ N/mm}^2$$

**Loading**



$$828 \times 1.5 - 350 \times 0.3 = C (2.0 - 0.2)$$

$$C = \frac{828 \times 1.5 - 350 \times 0.3}{1.8} = 632 \text{ kN}$$

|   |  |  |                    |
|---|--|--|--------------------|
| The Steel Construction Institute<br><br>Silwood Park, Ascot, Berks SL5 7QN | Subject<br><b>FOUNDATION EXAMPLE 4</b> |  | Chapter ref.<br>27 |
|   | Design code<br><b>BS5950: Part 1</b>   | Made by <b>HB</b><br>Checked by <b>GWO</b> | Sheet no. 2        |

$$f_c = \frac{632 \times 10^3}{0.4 \times 0.6 \times 10^6} = 2.63 \text{ N/mm}^2$$

taking  $n$  as 0.2 m,  $C$  becomes 598 kN and  $f_c$  is 4.98 N/mm<sup>2</sup>

$$T \text{ is then: } 598 + 350 - 828 = 120 \text{ kN}$$

to check, take moments about  $C$

$$\frac{828 \times 0.4 - 350 \times 1.6}{1.9} = 120.4 \text{ kN}$$

The relative stiffness of the base plate and channels will determine the point of application of the compressive force. As an alternative therefore assume the lever arm to be equal to the bolt centres and the centre of compression at the bolt line with appropriate stiffening added at this point.

$$C = \frac{828 \times 1.5 - 350 \times 0.3}{1.7} = 669 \text{ kN}$$

$$T = 669 + 350 - 828 = 191 \text{ kN}$$

$$n = \frac{669 \times 10^3}{630 \times 8 \text{ N/mm}^2} = 133 \text{ mm}$$

This is the minimum value of  $n$  for concrete strength of 20 N/mm<sup>2</sup>.


Design of channels & gusset

$$M = 669 \times 300 / 10^3 = 200.7 \text{ kNm}$$

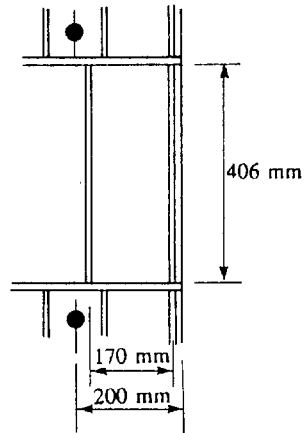
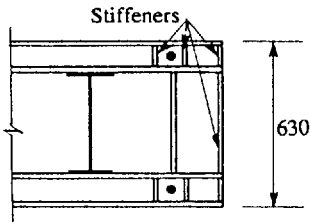
Use 2/ 229 × 89 × 32.76 RSCS,  $M_{cx} = 95 \text{ kNm}$

These are satisfactory by inspection since the gussets and base plate acting compositely would also make a contribution.

The internal stiffener and base plate would similarly be designed as a composite member taking the maximum outstand given in Table 7 of BS 5950.

|  |   |                         |             |
|--|---|-------------------------|-------------|
| The Steel Construction Institute<br>Silwood Park, Ascot, Berks SL5 7QN |  | Subject                 | Chapter ref |
|  |   | FOUNDATION<br>EXAMPLE 4 | 27          |
| Design code  | Made by <i>HB</i>   | Sheet no. 3             |             |
| <i>BS5950: Part 1</i>  | Checked by <i>GWO</i>   |                         |             |

*The base plate panel between the stiffeners should be checked using the Pounder expressions given in Chapter 30 as follows - the panel is shown below.*



Base plate

$$\frac{L}{B} = \frac{406}{170} = 2.38$$

$$K = \frac{2.38^4}{2.38^4 + 1} = 0.97$$

$K_{me}$ , the Pounder expression for moment, in the centre of the long edge, when all four edges are encastre, is given below:

$$K_{me} = K \left[ 1 + \frac{11}{35} (1 - k) + \frac{79}{141} (1 - k)^2 \right]$$

$$= 0.9796$$

$w_{me}$ , the ultimate load intensity is given by:

$$w_{me} = \frac{275 \times 12 \times 1.2 \times t^2}{6 \times 170^2 [K_{me}]}$$

$$f_c = \frac{669 \times 10^3}{600 \times 200} = 5.58 \text{ N/mm}^2, \text{ cf. } f_c = 4.98 \text{ N/mm}^2 \text{ for } n = 0.2 \text{ m}$$

*the plate thickness of 16 mm is therefore satisfactory.*

---

# Chapter 28

## Bearings and joints

by STEPHEN MATTHEWS

### 28.1 Introduction

#### 28.1.1 Movement

All structures move to some extent. Movements may be permanent and irreversible or short-term and possibly reversible. The effects can be significant in terms of the behaviour of the structure, its performance during its lifetime, and the continued integrity of the materials from which it is built.

Movements can arise from a variety of sources:

- (1) environmental: thermal, humidity, wind-induced.
- (2) material properties: creep, shrinkage.
- (3) loading: axial and flexural strains, impact, braking, traction, centrifugal forces.
- (4) external sources: tilt, settlement, subsidence, seismic loads.
- (5) use of the building: heating, cold storage.
- (6) others: requirements for moving or lifting bridges, allowances for jacking procedures, during or after construction.

In general it is necessary to consider the behaviour of the structure at each point in terms of its possible movement in each of three principal directions, together with any associated rotations. The movements of a structure are not in themselves detrimental; the problems arise where movements are restrained, either by the way in which the structure is connected to the ground, or by surrounding elements such as claddings, adjacent buildings, or other fixed or more rigid items. If provision is not made for such movements and associated forces it is possible that they will lead to, or contribute towards, deterioration in one or more elements. Deterioration in this context can range from, for example, cracking or disturbance of the finishes on a building to buckling or failure of primary structural elements due to large forces developed through inadvertent restraint.

#### 28.1.2 Design philosophies

In catering for movement of a structure, one of three methods can be adopted:

- (1) Design the structure to withstand all the forces developed by restraint of movement. This is possible with smaller structures (small-span bridges) or structures which are comparatively flexible (portal frames, in the plane of the frame). The method will avoid joints but may require the use of additional material in construction.
- (2) Subdivide the structure into smaller structurally stable units, each of which then becomes essentially a structure in its own right, able to move independently of the surrounding units. This principle is ideal for controlling those factors such as thermal movement which are related to the size of the overall structure. In many cases, the need for bearings as discrete elements can be eliminated. The disadvantage lies in the need to provide joints between the various units of the structure capable of accommodating all the anticipated relative movements between the units, while at the same time fulfilling all the other requirements, i.e. visual, practical, etc. It is, however, generally possible to achieve a balance by subdividing the structure so that the movements at the joints between units are kept relatively small, permitting the joints to be simple and economical (possibly at the expense of larger numbers of joints).
- (3) Subdivide the structure into fewer but larger sections, and make provision for a smaller number of joints, each with larger movement capacity, and thus possibly more complex than those that would be used at (2). Examples are to be found in bridges where use of the least number of road deck joints is preferable both in terms of riding quality, and also in the minimization of long-term maintenance requirements.

The need to restrict strains on elements and thus to protect finishes will lead to the adoption of the second of the above methods for design of building structures. Bridges, for reasons cited above, are more frequently designed adopting the third method.

## **28.2 Bearings**

### **28.2.1 Criteria for design and selection**

#### **28.2.1.1 Form of the unit**

Choice of form depends on several criteria:

- (1) *Physical size limitations.* The space available in the structure for the bearing. As bearings are subject to more wear than other parts of the structure they may have a shorter life and consequently this space should include allowance for access, inspection, maintenance and possible replacement.
- (2) *Bearing pressure.* The allowable bearing pressure on the materials above and below the bearing will dictate the minimum size of the top and bottom faces of the bearing unit.

- (3) *Loading*. The magnitude of the design load to be withstood by the bearing in each of the three principal directions will govern the form and type of the bearing. For each direction the maximum and minimum load should be considered at ultimate limit state, serviceability limit state or working load depending on the requirements of the design. In each case co-existent load and movement effects should be considered, together with a check for the existence of any load combinations which would act so as to separate the components of the bearing (e.g. uplift). For bearings carrying both horizontal and vertical loads it is common that the design of the bearing requires a *minimum* vertical load to be present to ensure satisfactory performance under horizontal loads.
- (4) *Rotations*. The magnitude of the maximum anticipated rotations in the three principal directions should be considered. For certain types of bearing (e.g. elastomeric bearings) there exists an interaction between maximum load-carrying capacity and rotation/translation capacity, so that it may be necessary to consider co-existent effects under loading (3) and movement (5).
- (5) *Movements*. Provision for maximum calculated movements can affect the size of the moving parts of the bearing and thus the overall size of the unit. As with rotations, the design of certain types of bearing is sensitive to the interaction of movement and loading requirements.
- (6) *Stiffness (vertical, rotational or translational)*. Certain structures may be sensitive to the deformation which occurs within the bearing during its support of the loads. The various types of bearing have different stiffness characteristics so that an appropriate form can be selected.
- (7) *Dynamic considerations*. Any particularly onerous dynamic loadings on the structure will have to be considered. Certain types of bearings (e.g. elastomeric bearings) have damping characteristics which may be desirable in particular instances, such as vibration of footbridges or machine foundations.
- (8) *Connections to structure*. The form of connection of the bearing to the structure requires careful consideration of the materials involved and the need for installation, maintenance and replacement of the bearing. In addition, bearings are frequently at a position in the structure where different forms of construction meet, perhaps constructed by different contractors. In this case, it is necessary to ensure that surrounding construction is properly detailed so that design requirements for load transfer are achieved.
- (9) *Use of proprietary bearings*. Many types of bearings are commercially available. These range from items which are available 'off the shelf' to more specialized units which may be designed and proven, but which are only produced to order. It is often appropriate for bearings to be individually designed to meet a particular need in situations where proprietary types may not be suitable. In these instances the engineer has the option of designing the units using available literature (see References to Chapter 28) and perhaps incorporating standard bearings from a manufacturer as components of a completed assembly or alternatively engaging a recognized manufacturer to design and produce the item as a special bearing. For straightforward

applications such as may be required on a short single-span bridge, it may be worthwhile investigating the relative costs of a simple fabricated bearing compared with the equivalent proprietary unit. Bearings (particularly 'special' bearings) can prove to be a large item of expenditure in a structure and an estimate of the costs involved should be made early in the design stage.

- (10) *Summary of design requirements.* Before selecting a particular bearing it is suggested that a summary of all relevant parameters is prepared. This can then be used if necessary for submission to the bearing manufacturers for examination and recommendations as to particular bearing types. A typical format for such a sheet is given in Table 9 of BS 5400: Section 9.1.<sup>1</sup>

### 28.2.1.2 *Materials*

Generally materials fall into three groups:

- (1) those able to withstand high localized contact pressures e.g. steel.
- (2) those able to withstand lower contact pressures but having a low coefficient of friction; these slide easily in a direction perpendicular to the direction of the pressure and thus accommodate translational movement, e.g. polytetrafluoroethylene (PTFE).
- (3) those able to withstand contact pressure and also to accommodate translational or rotational movements by deformation of the material (e.g. elastomers). Certain of these materials may be confined within a steel cylinder in order to increase their compressive resistance.

#### (a) *Mild or high-yield steel*

The coefficient of friction of steel on steel is of the order of 0.3 to 0.5, unless continuously lubricated; in order to provide for movement alternative arrangements are usually necessary. Traditionally this has been through the use of single or multiple rollers or knuckles. Rollers will permit translation in one direction and, if a single roller is used, rotation about an axis perpendicular to that direction. Knuckles permit rotation about one axis only. Rotation in two directions may be achieved using spherical-shaped bearing surfaces.

The allowable pressures between surfaces for steel on steel contact depend upon the radii of the two surfaces and the hardness and ultimate tensile strength of the material used. BS 5400: Section 9.1<sup>1</sup> gives expressions for design load effects in such cases. As load-carrying requirements increase, the use of steels with greater hardness is dictated. This can be achieved by use of high-grade alloy steels of various compositions. For design purposes, Table 2 of BS 5400: Section 9.1<sup>1</sup> gives indicative values of coefficients of friction of between 0.01 and 0.05 for steel roller bearings.



*(b) Stainless steel*

Stainless steel is frequently used in strip or plate form to provide a smooth path for sliding surfaces. It is important to utilize a material for the sliding surface which will not deteriorate and adversely affect the coefficient of friction assumed for design of the structure. A typical arrangement is a polished austenitic stainless steel surface sliding against dimpled PTFE.

*(c) Polytetrafluoroethylene (PTFE)*

PTFE has good chemical resistance and very low coefficients of static and dynamic friction. Unfortunately, pure PTFE has a low compressive strength, high thermal expansion and very low thermal conductivity. As a consequence it is frequently used in conjunction with 'filler' materials which improve these detrimental effects without significantly affecting the coefficient of friction.

The coefficient of friction varies with the bearing stress acting upon it. BS 5400: Section 9.1<sup>1</sup> gives the relationship shown in Fig. 28.1 for continuously lubricated pure PTFE sliding on stainless steel.

Lubrication of the pure PTFE is commonly achieved by means of silicone grease confined in dimples which are rolled on to the surface of the material. References 1 and 2 give further guidance on the restrictions on shape, thickness and containment on the PTFE and stainless steel components.

In preliminary design and assessment of forces on structures using PTFE sliding bearings, a figure of 0.06 is usually assumed for the coefficient of friction and the value checked later when the bearing selection is complete.

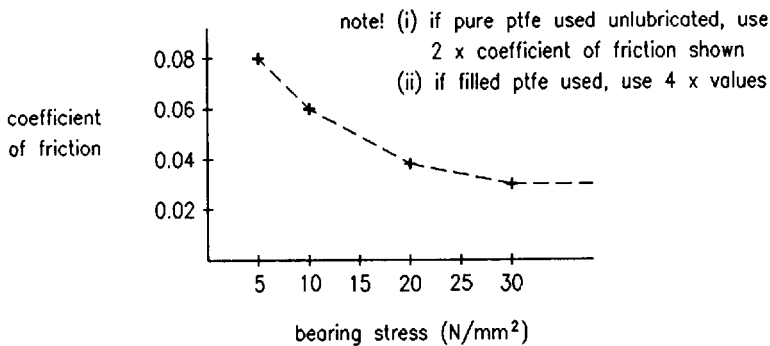


Fig. 28.1 Coefficient of friction for continuously lubricated pure PTFE

*(d) Phosphor bronze*

For particular applications, such as bearing guides, phosphor bronze may be used. BS 5400: Section 9.1 suggests a coefficient of friction of 0.35 for phosphor bronze sliding on steel or cast iron.

*(e) Elastomers*

An elastomer is either a natural rubber or a man-made material which has rubber-like characteristics. Elastomers are used frequently in bearings; they either constitute the bulk of the bearing itself or act as a medium for permitting rotation to take place (see sections 28.2.2.2 and 28.2.2.3(7)).

Elastomers are principally characterized by their hardness which is measured in several ways, the most common of which is the international rubber hardness (IRHD). This ranges on a scale from very soft at 0 to very hard at 100. Those elastomers used in bearings which are to comply with BS 5400: Part 9 have hardnesses in the range 45 IRHD to 75 IRHD.

The tensile capacity of most elastomers is considerable. As an illustration BS 5400: Part 9 specifies a minimum tensile elongation at failure of between 300% and 450% depending on IRHD.

When considering the behaviour of a block of elastomer under vertical compression it is assumed that the material is securely bonded to top and bottom loading plates. In this case (which is representative of most bearing situations) the vertical behaviour is related to the material's ability to bulge on the four non-loaded faces and is expressed in terms of the *shape factor* for the block, which is the ratio of the loaded area to the force free surface area (see Fig. 28.2).

$$S = \frac{LB}{2t(L + B)} \quad \text{for a rectangle}$$

$$S = \frac{D}{4t} \quad \text{for a circle}$$



Fig. 28.2 Elastomeric bearing dimensions for (a) a rectangular block, (b) a circular block

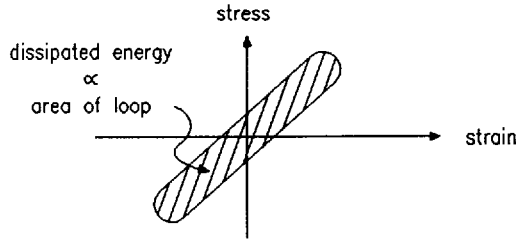


Fig. 28.3 Energy loss in elastomer

The vertical stiffness of the block is significantly reduced if the loaded faces can slip laterally.

The shear stiffness of a block of elastomer bonded to top and bottom plates is more or less linear and independent of shape factor. A detailed treatment of these effects is given in References 3 and 1.

An important property of elastomers is related to the fact that the strain in the material tends to lag behind the stress which causes it. As a consequence, some of the energy input during deformation is dissipated within the bearing as heat. A typical plot of stress versus strain for an elastomer is shown in Fig. 28.3. The energy lost as heat in one loading cycle is represented by the area of the loop.

This effect, known as 'hysteresis', has two implications:

- (1) it can result in a build-up of heat in the bearing under dynamic loading conditions,
- (2) if appropriately sized it can be used to act as a form of damping device to the structure.

The sensitivity of the elastomer to dynamic loading depends upon both the frequency of the applied stress and also temperature, as elastomers exhibit hardening at low temperatures.

Elastomers are prone to creep and are sensitive to attack by atmospheric oxygen and ozone, petrol and radiation from nuclear sources. They are not suitable for operation in temperatures above 120°C.

A more detailed discussion of these aspects is given by Long,<sup>4</sup> and limits are given for their control in practice by BS 5400.<sup>1</sup>

#### (f) Concrete

The concept of the use of a small, highly contained block of concrete as a hinge has been employed in the form of the Freysinnet hinge or the Mesnager hinge. Details of these are given in Reference 5.

## 28.2.2 Types of bearing

### 28.2.2.1 General

Structural bearings can be broadly divided into two types: elastomeric and mechanical. Elastomeric bearings comprise blocks of elastomeric material reinforced as necessary with other materials. They can be made to accommodate movement by shearing of the elastomer block. Mechanical bearings are generally formed from metal and employ sliding surfaces of PTFE to achieve any necessary movement capabilities. It should be noted that the above divisions are not exclusive as, for example, some bearings are commercially available which employ elastomer blocks with sliding surfaces which cater for larger movements than could be accommodated by shearing of the block, but which do not merit the larger expense of a mechanical bearing.

In the following sections the principal types of bearing are briefly described.

### 28.2.2.2 Elastomeric bearings

Elastomeric bearings rely for their operation on the interaction between vertical load, rotation and translation. As a consequence, design of most elastomeric bearings must be carefully checked. Large proprietary ranges are available and although load tables of the various capacities are published by manufacturers, it is prudent to ask the supplier to confirm that the selected bearing is suitable for the load/movement conditions under which it will be used. The basis of design of these bearings is related to controlling strains and stresses in the elastomer and any reinforcing material and ensuring that the bearing does not deform excessively, become unstable, lift off, or slip under the anticipated design effects. Further guidance on this subject is given in BS 5400: Part 9.1<sup>1</sup> and by Long.<sup>4</sup> The latter reference also gives a detailed discussion of the properties of elastomers.

Bearing types are:

- (1) *Rubber pad or strip bearings*. As the name implies, these bearings consist simply of a block or strip of elastomer. They have the advantage of being inexpensive and simple although their load-carrying and movement capability is limited.
- (2) *Fabric-reinforced bearings*. In order to increase the capabilities of the simple pad bearing, use is made of fabric (e.g. compressed cotton duck) to reinforce the elastomer. Movement in these bearings is usually provided by use of a PTFE surface bonded to the top of the block and sliding against a stainless steel plate attached to the underside of the superstructure. In this manner, the elastomer is used to provide rotational capability only, rather than rotation and movement as in the case of other elastomeric bearings.
- (3) *Elastomeric-laminated bearings*. This type of bearing consists of a block of elastomeric material reinforced with steel plates to which the elastomer is also

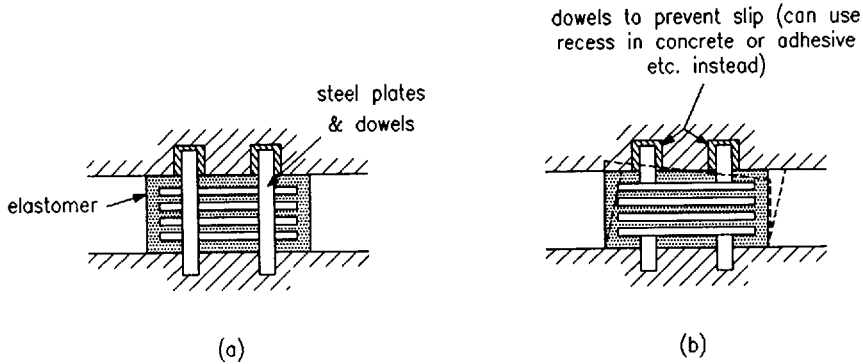


Fig. 28.4 Two types of elastomeric bearing: (a) fixed, (b) free

bonded. The characteristics of the bearings can be varied considerably by alteration of the size, shape and disposition of the layers as well as the usual parameters of bearing plan area and thickness. Generally, these bearings are either 'fixed' for translation by means of a steel dowel passing through the bearing layers (Fig. 28.4(a)) or 'free' bearings which permit translation and rotation by deformation of the bearing (see Fig. 28.4(b)). This type of bearing is capable of carrying quite substantial loadings and movements and has the benefit of being cheaper than mechanical bearings.

### 28.2.2.3 Mechanical bearings

- (1) *Roller* (Fig. 28.5(a)). The earlier and more traditional forms of bearing comprised single or multiple steel rollers sandwiched between upper and lower steel plates. Single rollers will allow for longitudinal movement and rotation about the axis of the roller, while at the same time carrying comparatively high vertical loads, but will not permit transverse rotation or movement. Bearings of very large capacity have been produced by use of special alloy steels to form the contact surfaces. Note that bearings which utilize multiple rollers will not allow rotation about an axis parallel to the axis of the rollers. Rollers are sometimes used enclosed in an oil bath or grease box to exclude deleterious matter. Other forms of bearing have, to a large extent, supplanted the use of rollers for the most common applications.
- (2) *Rocker* (Fig. 28.5(b)). Rocker bearings will not permit translational movement. The bearings may be cylindrical or spherical on one surface with the other surface flat or curved. In the cylindrical form there is no provision for transverse rotation which may have consequences for design of the structures above and below the unit. Rocker bearings usually incorporate a pin or shear key between the two surfaces to maintain relative position.

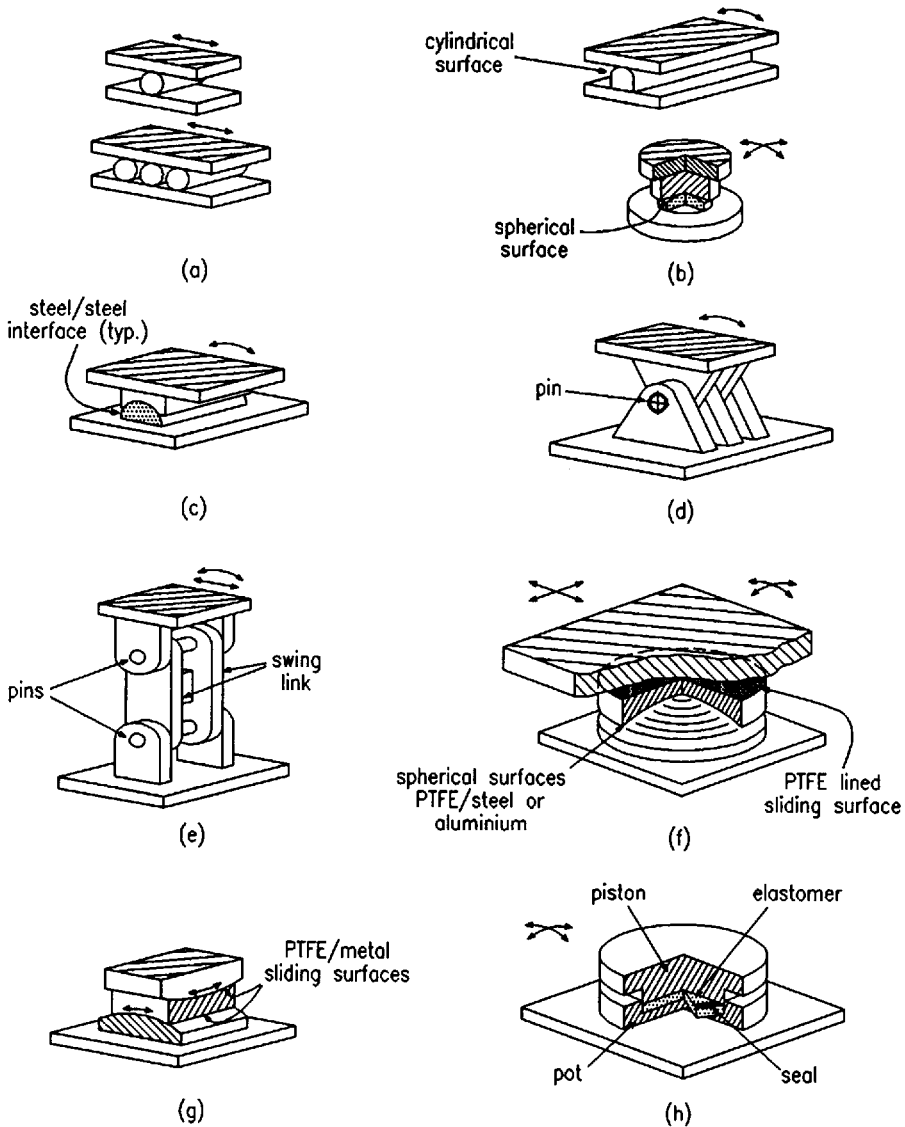


Fig. 28.5 Mechanical bearings: (a) single/multiple roller, (b) cylindrical/spherical rocker, (c) cylindrical knuckle, (d) knuckle leaf, (e) swing link, (f) spherical – with sliding top plate, (g) cylindrical PTFE bearings combined to form ‘anticlastic’ bearing, (h) ‘pot’ bearing which can have sliding top plate similar to (f)

- (3) *Knuckle bearings* (Fig. 28.5(c)). These are similar to rocker bearings.
- (4) *Leaf bearings* (Fig. 28.5(d)). These are formed of leaves of steel with a common pin. They will carry large vertical loads and permit large rotations

about the axis of the pin but not transversely. They have the benefit that they can be designed to resist uplift. It should be noted, however, that they are unlikely to be anything other than produced to order and that there may be other means of controlling comparatively small uplifts (e.g. 'pot' type bearing with separate vertical restraints). Leaf bearings have been used in suspension bridges to form the swing link bearings which are necessary to cater for large movements and uplifts (Fig. 28.5(e)).

- (5) *Spherical (PTFE, circular)* (Fig. 28.5(f)). These comprise a spherical lower surface which is lined with PTFE and a matched upper spherical surface of aluminium or stainless steel. This arrangement allows considerable rotation capacity in all directions. Horizontal translation is frequently achieved using another (flat) sliding surface above the upper part of the bearing.

An important consideration with spherical bearings is that in order to withstand any horizontal loads it is necessary to have a minimum co-existent vertical load to prevent instability.

Spherical bearings are capable of carrying high vertical loads and also permit higher rotations than many other types.

- (6) *Cylindrical (PTFE) 'anticlastic' bearings* (Fig. 28.5(g)). These are similar in concept to rocker bearings but instead of using (for example) steel on steel bearing surfaces they have enlarged bearing areas which are coated with PTFE on one surface and stainless steel or aluminium on the other. This produces a bearing with high rotation capabilities about an axis as well as high load-carrying capacity. One unit can be combined with another similar arrangement to provide rotation about an axis at right angles to the first and also with a sliding plate arrangement to provide translational capability.

- (7) *Disc or 'pot'* (Fig. 28.5(h)). These are often of similar proportions to spherical bearings but instead of a sliding spherical surface being used to provide rotation capability, a disc of elastomeric material is used, confined in a cylindrical pot. Loading is applied to the surface of the disc via a closely fitting steel piston. Under these conditions, the confined elastomer is in a near fluid state, and permits rotation in all directions without significant resistance. Sliding is achieved by means of a PTFE/sliding surface above the piston, in a similar manner to spherical bearings. Disc bearings are popular for many applications, as they tend to be cheaper than spherical bearings but can carry higher loadings than elastomeric-laminated bearings of comparable plan area. They have rotation capabilities intermediate between spherical and laminated bearings.

- (8) *Fabricated*. Fabricated bearings have become less popular largely through the availability of a wide range of proprietary units. They are used for footbridges and temporary works applications. There is, however, no reason why properly designed fabricated bearings should not be used to support a structure, particularly say, for a fixed bearing where there is no requirement for sliding surfaces. Guidance on design of bearings is given in References 1–8.

- (9) *Special*. Special bearings will always be required for particular locations. Perhaps the most common demands are for:

- (a) bearings which will resist horizontal loads only in order to restrain the structure in the horizontal plane, but without providing any vertical support (see section 28.2.4.2(3))
- (b) bearings which will withstand uplift under certain loading conditions.

Uplift bearings can be special versions of normal proprietary bearing types, or can use a proprietary bearing set in a subframe which controls the tendency to uplift within prescribed limits adopted in consultation with the bearing manufacturer.

### 28.2.3 Use of bearings

#### 28.2.3.1 *General*

The parameters which dictate the form of the bearing as a unit are discussed in section 28.2.1. It is also necessary to consider the action of the bearing in the broader concept of the behaviour of the two elements of structure which the unit connects.

#### 28.2.3.2 *Fixings*

Various forms of fixings are utilized to connect bearings to the structure. These include:

- (1) shear studs, usually in conjunction with a subsidiary plate which is tapped to receive the bearing fixing bolts,
- (2) square or cylindrical dowels, tapped to receive the bearing fixing bolts,
- (3) direct bolting of the bearing to the structure.

In all forms it is desirable to allow for tolerances in the processes of installation and possible need for replacement of the bearing. The system shown in Fig. 28.6

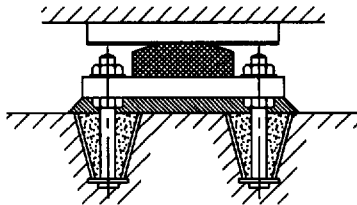


Fig. 28.6 Bearing fixing



allows for support of the bearing during fine adjustment, but requires large jacking capability (possibly more than a continuous structure could accommodate) to remove it.

In bearings subjected to dynamic loadings such as machine foundations, it is necessary to ensure that the fixings are vibration-proof.

### 28.2.3.3 *Effect on the structure*

The elements of the structure above and below the bearing are affected by the type of bearing, which can be classified as:

- (1) *fixed* – not permitting movement in any horizontal direction,
- (2) *guided* – movement, constrained by guides of some form, to be in one horizontal direction only,
- (3) *free* – movement permitted in all horizontal directions,
- (4) *elastomeric* which may be laminated or not. These bearings can be ‘fixed’ by means of steel dowels passing through them but are more often used ‘free’ in all directions and their capability to generate forces when shearing takes place is utilized to withstand horizontal loadings. If the whole structure is supported on such bearings it effectively ‘floats’, with all horizontal loads shared by all bearings. (See also section 28.2.4.2.)

If the bearings are fixed or guided, the neighbouring structure must be designed for the forces arising from the restraints. Even when the bearing is free in a particular direction and movement is permitted, some forces are developed – either from friction effects at the movement interfaces of a sliding mechanical bearing, or from shearing deformation in the case of an elastomeric bearing (see Fig. 28.7(a)).

In addition to forces developed laterally, the effects of the eccentricities produced by the movement must be allowed for, and also the rotation capability of the bearing in the transverse direction (see Figs 28.7(b), (c) and (d)). It is possible to control the extent of the additional eccentricity effects on a steel superstructure by use of a sliding bearing inverted which transfers the eccentricity to the substructure where it may be more easily accommodated. In this case however care should be taken to protect the sliding surfaces against falling dust, debris, etc. by use of a flexible skirt enclosure.

### 28.2.3.4 *Installation*

Bearings must be correctly installed into the structure. The procedure will depend upon the form of the structure above and below the bearing, and the type of bearing, but in general care should be taken not to load the bearing significantly before bedding materials between the bearing and the structure have fully cured,

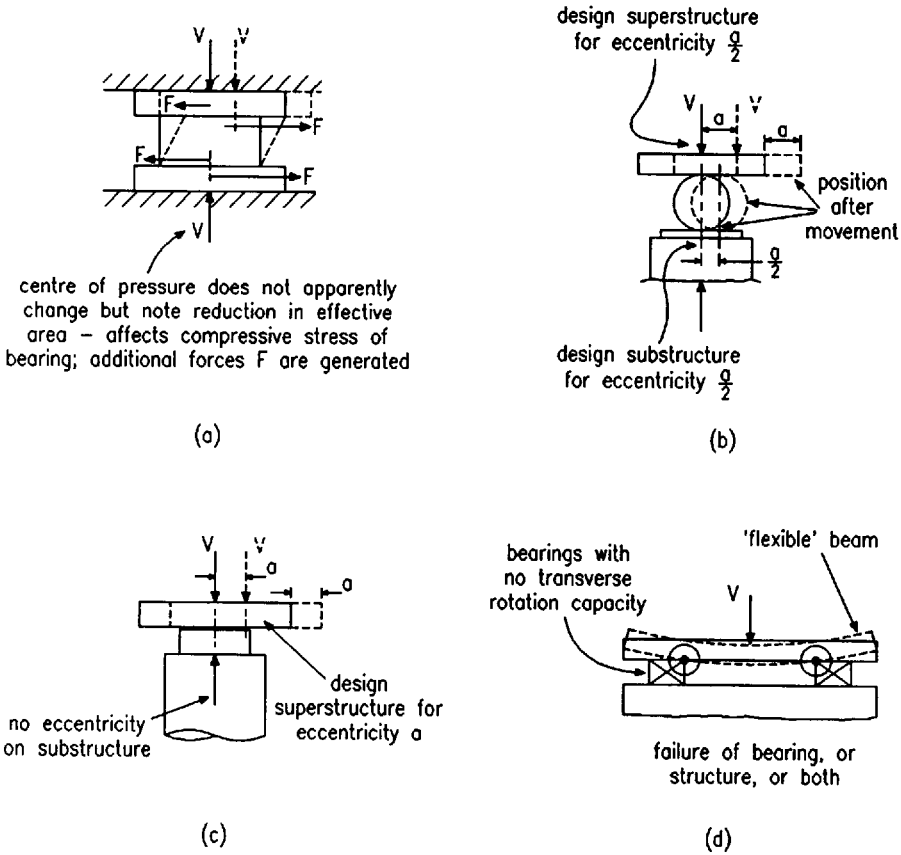


Fig. 28.7 Effect of bearing on structure: (a) elastomeric, (b) roller, (c) sliding, (d) need for transverse rotation capacity

or to load the bearing in a manner for which it has not been designed. A common cause of the latter effect is the incorporation of temporary packs or shims into the bedding in such a manner that they subsequently form hard spots under the bearing. (Note that there is, however, no fault in principle with the concept of temporary packing provided that it is responsibly carried out.)

Factory-assembled bearings are usually provided with transit straps to prevent inadvertent dismantling of the unit. When a significant irreversible movement is anticipated at a bearing, due to shrinkage or prestressing for example, an allowance for this movement may be pre-set in the factory. To allow for departure of the actual structure temperature, when the bearings are set, from the mean temperature assumed in design, it may be necessary to make alterations of the relative positions of the fixed and moving elements of the bearing. For bridges, Lee<sup>5</sup> suggests times

when this may be most conveniently carried out – when the bridge temperature is approximately equivalent to the air shade temperature. This can be taken as:

- (1) concrete bridges: 0900 BST  $\pm$  1 hour each day,
- (2) steel bridges: at about 0400 to 0600 BST each day during the summer, and at any time on ‘average’ days during the winter.

Further guidance on bridge temperatures is given in Reference 9.

Frequently bearings are incorporated into the structure using a bedding layer above and below the unit, typically of 25 mm thickness which allows some tolerance in fixing of the bearing, and will also permit final adjustment of the levels of the structure above during construction. The form of the bedding may be ‘dry pack’, trowelable or pourable material. Epoxy resin, sand/cement, sand/epoxy, or sand/polyester compounds are commonly used. The same material may also be used for filling the spaces around fixing devices once final positioning has been carried out.

## 28.2.4 Assemblies of bearings

### 28.2.4.1 General

The selection and use of bearings of various types has been discussed in terms of the individual units. The behaviour of the structure or substructure as a whole will now be considered, and the use of the four principal forms of bearing to control movement illustrated.

### 28.2.4.2 Structures straight in plan

As an example, the movement of a typical bridge deck will be considered in the horizontal plane, although the principles involved can equally be applied in other directions.

The four forms of bearing commonly available are given in section 28.2.3.3.

Consider the bridge deck shown in plan in Fig. 28.8.

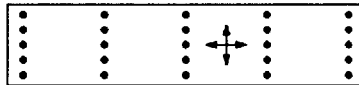


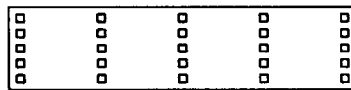
Fig. 28.8 Straight bridge deck

The deck vertical loading arises from dead and live loads, from which maximum and minimum values of bearing loads can be derived at each position. Longitudinal loading on the deck will arise from wind loads, braking and traction of vehicles, and also from the manner in which the chosen restraint system accommodates movements. Forces from similar effects are generated in the transverse direction also.

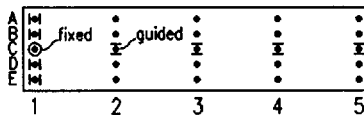
Thermal expansion and contraction of the deck is frequently the predominant reversible movement. This can normally be considered to act radially from a particular fixed point on the deck. The options for bearing arrangement are many, but three typical layouts are given in Fig. 28.9(a), (b) and (c). It should be remembered that whether a bearing accommodates horizontal movement through PTFE/sliding or by shearing of an elastomer block a horizontal force (due to friction or shear respectively) will be generated, and the bearing system should be arranged so that wherever possible these forces cancel one another out, and so minimize the net horizontal force to be resisted by the substructure.

- (1) In Figure 28.9(a) all the bearings are elastomeric with *no* fixed bearings. The horizontal loads in both directions are shared between all bearings and the structure ‘floats’.

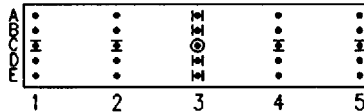
Thus all substructures will be loaded when horizontal loads or expansion/contraction occur. This system is economic, but is limited by the maximum capabilities of the bearings in rotation, load, and movement.



(a)



(b)



(c)

Fig. 28.9 Typical bearing layouts for straight bridge decks: (a) all elastomeric, (b) all mechanical (i), (c) all mechanical (ii)

- (2) In Fig. 28.9(b) all the bearings are mechanical (typically spherical or pot bearings). Line 'C' provides fixity in the transverse direction. Line 1 provides fixity in the longitudinal direction. All longitudinal forces from external sources are taken at abutment 1, together with longitudinal forces arising from friction at bearings on piers 2 to 5. At each pier transversely lateral loads are taken by 'C' line bearings. Friction forces due to transverse expansion, etc. will tend to cancel one another out.
- (3) The arrangement in Fig. 28.9(c) is better for longitudinal effects than that in Fig. 28.9(b) as friction forces in this direction tend to cancel one another out. It has the disadvantage that external loads are transmitted to an intermediate pier rather than an abutment. The forces due to movement of the deck are minimized in both horizontal directions. Occasionally, the line of fixed or guided bearings with both horizontal and vertical capability such as at 'C' may be replaced by two lines, one with bearings with vertical capability only, and one with bearings with horizontal capability only.

### 28.2.4.3 Structures curved in plan

If the structure shown in Fig. 28.9(b) is curved in plan, then any expansion or contraction movements longitudinally are accompanied by lateral movements also. This effect can be controlled in two ways:

- (1) set the bearing guides to permit radial expansion from a fixed point on the structure,
- (2) set the bearing guides tangential to the plan curvature, and so constrain the structure to follow this line when it moves (see Fig. 28.10).

In radially-guided structures the accuracy of setting out and alignment becomes more critical as the distance from the fixed point increases. In tangentially-guided structures, the structure is constrained to move along a particular path, and the horizontal forces developed in so doing must be taken into account in the design of the structure and supports.

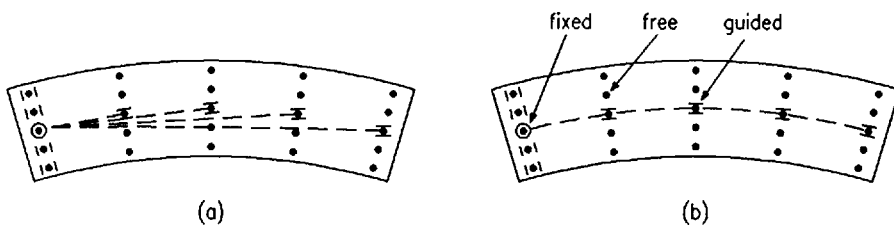


Fig. 28.10 Curved bridge deck: (a) radially-guided, (b) tangentially-guided

It should be noted that frequently bearings which are nominally 'guided' are manufactured with a gap tolerance at the guides. The actual value of this tolerance should be checked with the manufacturer of the particular bearing, but a value of 0.5 mm is typical. This tolerance can have a significant effect on the permissible accuracy of setting out of radially-guided structures, and the magnitude of the forces developed in tangentially-guided structures. (Reference 6.)

#### 28.2.4.4 Structures with fixed bearings and flexible supports

An alternative to the use of systems of guided bearings is to provide fixed bearings at more than one (possibly all) supports. In this case the supporting structures (e.g. bridge piers) have to be designed to flex and accommodate the necessary movements. They also have to cater for the forces developed by these movements in addition to any other design loading effects. This arrangement may be appropriate when it is required to share horizontal load effects over several supports, but it should be noted that replacement of the bearings may be more difficult owing to horizontal loads which may be locked into the bearing/support arrangement.

#### 28.2.4.5 Other considerations

- (1) *Wedging action.* It is possible to utilize a form of 'wedging action' to resist horizontal loadings by setting two (usually elastomeric) bearings on planes inclined to one another as shown in Fig. 28.11. Equally, it is also possible to develop the action inadvertently by errors in bearing setting out, and thus attract more loading than that for which the unit is designed. (See References 3, 4 and 6.)
- (2) *Shock transmission units (STUs).* Although not strictly bearings, these units can be utilized in conjunction with bearings to distribute certain components of loading to other parts of the structure. The units typically consist of a cylinder filled with putty-like material which is acted on by a piston with a hole in it through which the putty can flow. Slow, steadily applied forces such as thermal expansion forces will cause the putty to flow from one side of the piston to the other, and allow dissipation of the force through movement.

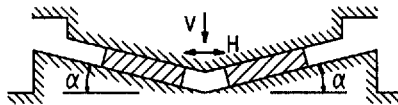


Fig. 28.11 Wedging action

Rapidly applied forces such as seismic loads, braking loads, or wind gusts are too fast to allow the flow to occur, and the unit therefore effectively transmits this 'shock' loading without significant movement. A description of the use of these devices is given in Reference 8.

## 28.3 Joints

### 28.3.1 General

The form of joints in a structure will vary to suit particular requirements at each position. The basic parameters to be considered in derivation of a joint detail are discussed below, although they are not all appropriate to every situation. Despite the fact that significant differences exist in the final application, many of the factors involved in joint design are common to both buildings and bridges. Joint detailing and construction is considerably facilitated by the many forms of proprietary sealants, gaskets, and fillers that are now commercially available for use as components, as well as complete prefabricated units which may be used in particular applications. The manufacturers of these products will generally be able to supply technical information on their products, and also to give guidance as to the suitability of items for use in particular applications.

### 28.3.2 Basic criteria

#### 28.3.2.1 *Form of the structure*

The form of the structure, and the location and orientation of the joint within the structure, will dictate to a large extent the arrangement of the detail. The basic categories of joint are:

- (1) *Wall joints*. These may be vertical (e.g. expansion joint in a building or a bridge substructure); or horizontal (e.g. joint between preformed cladding units on a building façade).
- (2) *Floor/roof joints*. Examples are expansion joints in a building, or road deck joints in a bridge.
- (3) *Internal/external joints*. This type of joint needs to be weather-proofed.

#### 28.3.2.2 *Material to be joined, and method of fixing*

The material either side of the joint may be steel or aluminium cladding, concrete, brickwork, blockwork, or various forms of surfacing. The detail of the joint will

vary considerably with the properties of the material and the method of fixing to be used. It is important to note that this may affect the stage of construction at which the joint is formed, e.g. PVC waterstops will need to be positioned before concreting of the walls on either side of them takes place. Where it is anticipated that the joint may need repair or replacement during the life of the structure (e.g. expansion joints on heavily trafficked bridges) the fixings of the joint should allow for easy removal and reinstatement.

**28.3.2.3 Weather-resistance**

It is important to consider the degree of weather-resistance required for a joint. In this respect, joints can be classified (in a somewhat over-simplified form) into three types (see Fig. 28.12(a), (b) and (c)):

- (a) 'Closed' joint, with a filler material and exterior sealant,
- (b) 'Closed' joint, with a compressible gasket and exterior sealant,
- (c) 'Open' joint, with a flexible membrane seal, and arrangements to drain rain-water, etc. from the inside surfaces of the joint which are 'open' to the weather.

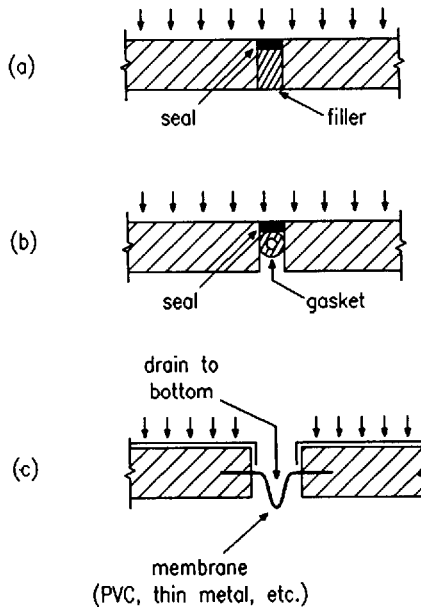


Fig. 28.12 Weather-resistance of joints: (a) closed, with filler, (b) closed, with gasket, (c) open, with membrane



Where appropriate, arrangements should be made at joints in buildings for continuity or sealing of insulation and vapour barriers, etc. to prevent formation of condensation, or loss of heat.

In structures where there is likely to be water in contact with the structural envelope, e.g. structures buried in ground which has a high water table, or water-retaining structures, flexible waterbars are usually incorporated at construction and movement joints. These have the effect of interrupting the path along which any water present has to travel.

Figure 28.13(a), (b) and (c) are typical of wall details in reinforced concrete or brickwork construction. A typical joint detail for steel cladding in a building is shown in Fig. 28.13(d), and Fig. 28.13(e) shows a detail suitable for a building roof joint, or small bridge deck movement joint.

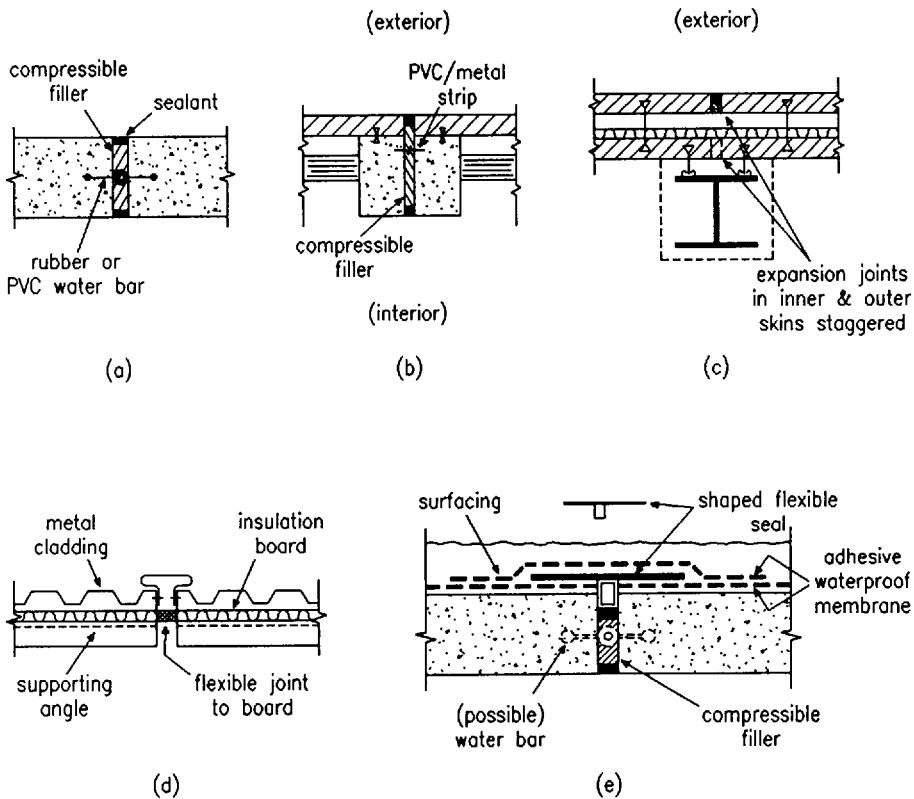


Fig. 28.13 Typical joint details: (a) concrete walls, (b) concrete columns, (c) brick walls, (d) cladding, (e) roof or bridge deck

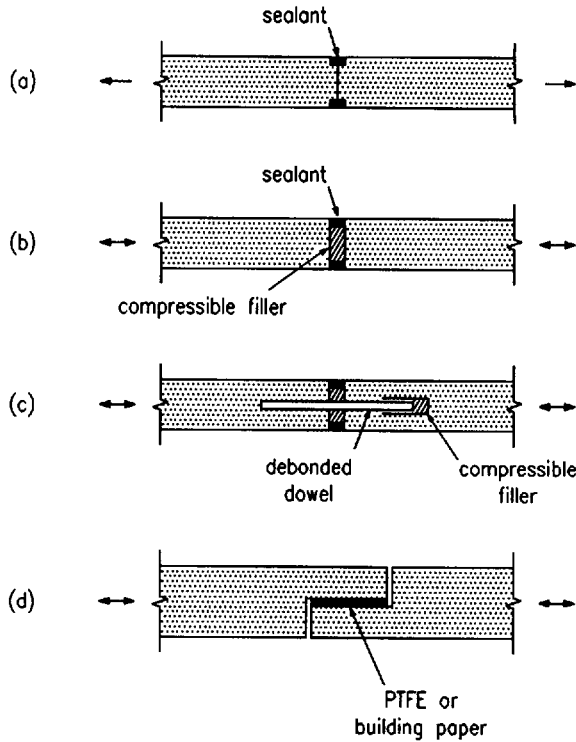


Fig. 28.14 Typical joint details allowing for moderate movements

#### 28.3.2.4 Direction of movement required

The direction of movement required at a joint will affect the form of the joint. All likely movements should be evaluated, as restraint of unanticipated movements may result in failure of the joint, or development of large restraint forces in the joint and the adjacent structure.

Typical broad classifications of joint by movement requirements are given in Fig. 28.14(a), (b), (c) and (d).

In order to illustrate the nature of additional movements which can occur in a structure, two particular cases relating to a bridge superstructure are considered (see Fig. 28.15(a) and (b)).

In Fig. 28.15(a), the bridge deck is set to allow radial expansion from a fixed point. It will be observed that the expansion joint will require both longitudinal and lateral movement capability.

Figure 28.15(b) represents a cross-section throughout the end of the last span of a bridge. In (i) the distance from the actual point of rotation to the joint is small,

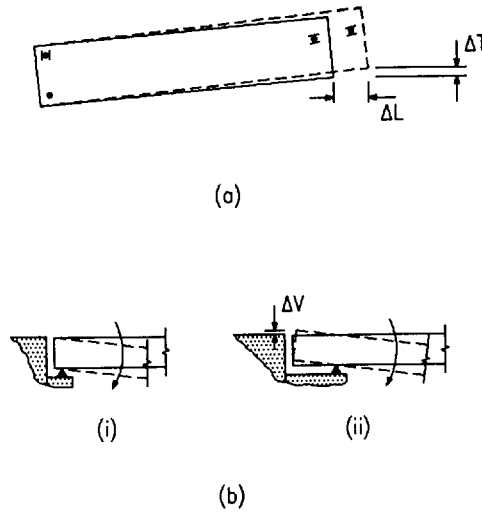


Fig. 28.15 Radial and rotational movement. (a) Radial expansion from a fixed point, (b) End rotation

and little vertical movement of the joint is necessary when flexure of the beam causes rotation. In (ii) the effect on the joint of a large overhang is demonstrated: a much larger vertical movement is induced. Further discussion of these and other related effects is given in References 3–6.

### 28.3.2.5 Magnitude of movement required

The magnitude of movement to be allowed for has a significant effect on the type of joint. Joints can be broadly classified into three groups on this basis:

- (1) *0–25 mm movement*: Common for buildings, where there is a tendency towards the use of larger numbers of joints, each with a small movement. The restricted amount of movement considerably facilitates joint construction as the discontinuity in the structure is smaller. Similar joints are used in bridge work for small-span bridges, or so-called ‘buried joints’ in the road surface. Typical examples of joints suitable for movements within this range are given in Fig. 28.14. They may be preformed units, but are more likely to be assemblies of proprietary components arranged to suit the particular requirements of the detail and its location.
- (2) *25–300 mm movement*: Joints capable of movements of this extent are more common in bridge work, and are usually prefabricated units, although a simple plate arrangement can be used in some cases (Fig. 28.16(a)). Two basic types of prefabricated units are common. Figure 28.16(b) shows the first

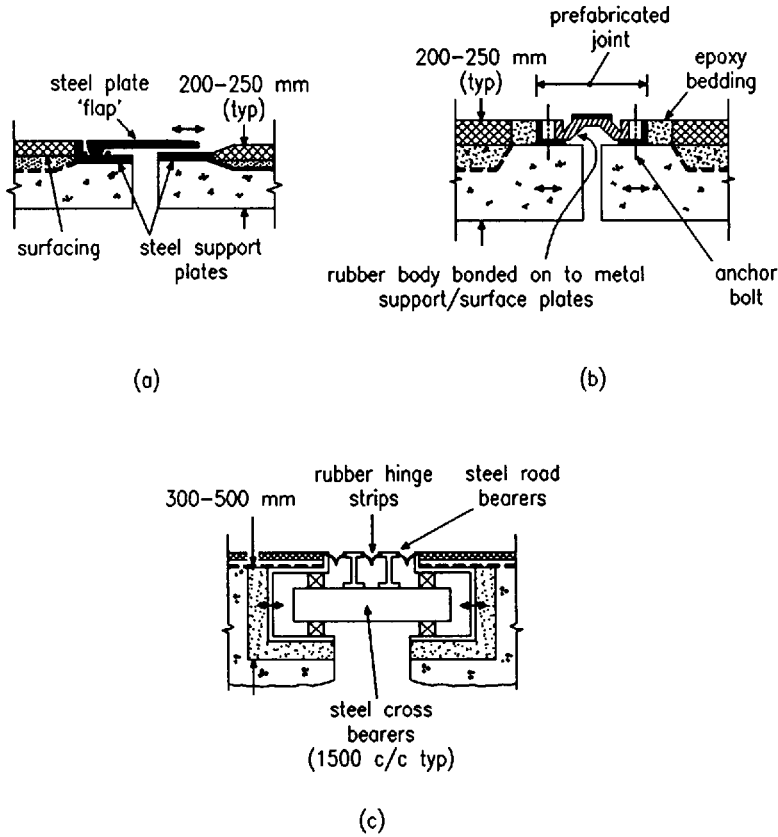


Fig. 28.16 Joints allowing for larger movements: (a) (b) 200–250 mm, (c) 300–500 mm

type, which uses an elastomeric material in its construction to accommodate the movement. Figure 28.16(c) shows the second type, which is suited to the larger movement ranges. This type uses an arrangement of mechanical components supported on stub beams to form a moving joint. Detailing of the structure must allow for the space required by these units.

- (3) *>300 mm movements*: Joints for movements of this magnitude are unusual and will be tailored to particular requirements, e.g. expansion joints for suspension bridge decks.

**28.3.2.6 Required performance of the joint surface**

The nature of effects acting on the surface of the joint should be considered. In building structures, this will frequently be limited to environmental effects on

exterior walls or roof, but consideration of the size of the joint gap is necessary in, say, a floor or roof joint where excessive gaps could prove hazardous to pedestrians, or could lead to jamming of the joint through ingress of debris, etc.

Joints on bridge decks are subject to heavy localized effects from wheel loads and corrosive effects from de-icing salts and spilt chemicals. As a result, the practicalities of maintenance and perhaps eventual replacement of such joints should be considered. The resistance to skidding of the surface of such joints is also important.

#### **28.3.2.7 Load generation at joints**

Frequently the loads generated by compression or extension of movement joints are insignificant in terms of overall structural behaviour. In some cases, however, the loads developed may be large enough to affect the design of other elements of the structure. A particular example is a large expansion joint of the elastomeric type in a bridge, where horizontal forces developed in moving the joint should be considered in design or selection of the bearing which is to form the fixed point of the deck.

### **28.4 Bearings and joints – other considerations**

In design and detailing on bearings and joints, it should be remembered that the positions where they exist may be positions of concentrated load application and/or significant discontinuity in the structure. Care should be taken in design to establish and preclude all likely means of deterioration and failure. This should extend to adequate supervision to ensure correct installation, as many problems have been attributed to substandard workmanship applied to an otherwise competent design.

The need for maintenance of all joints should be assessed, and adequate allowance made where necessary for inspection, servicing, and facility of replacement.

#### **References to Chapter 28**

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# Chapter 29

## Steel piles

by DENNIS WAITE

### 29.1 Bearing piles

#### 29.1.1 Uses

The very high strength to weight ratio and toughness of steel makes the material particularly suitable for certain piling applications:

- (1) where piles need to be handled, pitched and driven in long lengths, e.g. maritime structures, the ability to be transported and handled without concern for overstressing due to self-weight is an important consideration.
- (2) the ability to withstand high driving stresses enables steel piles to be installed without damage through difficult strata such as surface deposits of slag or old foundations and subsurface layers of boulders.
- (3) energy-absorbing structures such as jetties and dolphins are particularly suited to the use of steel by virtue of its ability to withstand large elastic deformation.

#### 29.1.2 Types of pile

Steel bearing piles are available in three basic profiles (see Fig. 29.1) and in two basic qualities of steel, grade 430A and grade 510A to BS EN 10025.

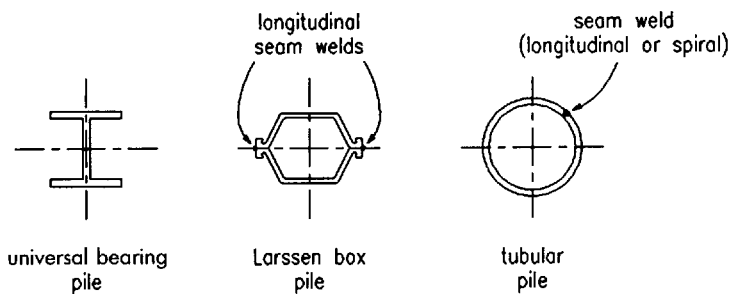


Fig. 29.1 Types of bearing pile

*Universal bearing piles*

These are H-sections produced on a universal rolling mill – hence their name. They are essentially the same as universal column sections, except that they have uniform thickness throughout the section (see Table 29.1).

They are used principally for land-sited structures where the full length of the pile is embedded, e.g. foundations for bridges and buildings.

They are not suitable for conditions where long lengths of the pile shaft are unsupported by surrounding soils, because buckling failure about the minor axis will occur at relatively low axial loads.

*Larssen box piles*

These are hollow multi-sided sections made by placing together two Larssen sheet piles in the form of a box profile and longitudinally welding the seams (see Table 29.2).

They are particularly suitable for marine structures, such as jetties and dolphins, where part of the pile shaft is exposed above sea bed level and the pile functions as a free-standing column.

*Tubular piles*

These are made by forming steel plate into tubes. They are available in a large range of diameters and wall thicknesses.

As with Larssen box piles they are most suitable for marine structures, especially where sited in deep water, e.g. berthing jetties for deep draught vessels.

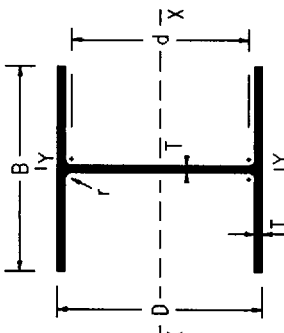
**29.1.3 Design***Loading*

Although the superstructures which the bearing piles are required to support are designed by methods using factored loading, it is important that the values used for the design of the bearing piles are working loads.

In most cases the loads are principally vertical, with relatively minor horizontal components. Small horizontal loads are commonly resisted by passive soil resistance on the side of the pile cap, rather than by bending in the pile itself. Where the horizontal loads are significant they are better resisted by the inclusion of raking piles which provide a foundation with greatly improved stiffness in the horizontal plane. The induced uplift forces resulting from the use of raking piles can be resisted by the weight of the superstructure or by tension in the associated piles (see Fig. 29.2).

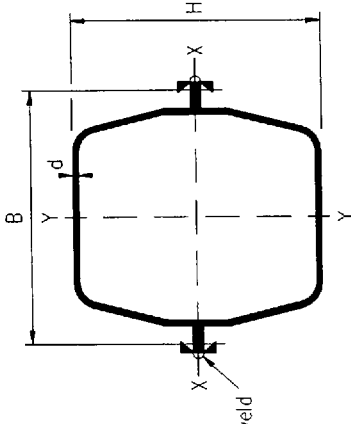


Table 29.1 Dimensions and properties of universal bearing piles



| Serial size (mm) | Mass (kg/m) | Depth of section (mm) | Width of section (mm) | Thickness of web and flange (mm) | Root radius (mm) | Depth between fillets (mm) | Ratio $\frac{D}{T}$ | Area of section (cm <sup>2</sup> ) | Second moment of area (cm <sup>4</sup> ) |        | Radius of gyration (cm) |      | Section modulus (cm <sup>3</sup> ) |      |
|------------------|-------------|-----------------------|-----------------------|----------------------------------|------------------|----------------------------|---------------------|------------------------------------|--|--------|-------------------------|------|------------------------------------|------|
|                  |             |                       |                       |                                  |                  |                            |                     |                                    | X-X                                      | Y-Y    | X-X                     | Y-Y  | X-X                                | Y-Y  |
| 356 × 368        | 174         | 361.5                 | 378.1                 | 20.4                             | 15.2             | 290                        | 17.7                | 222.2                              | 51 134                                   | 18 444 | 15.2                    | 9.11 | 2829                               | 976  |
|                  | 152         | 356.4                 | 375.5                 | 17.9                             | 15.2             | 290                        | 19.9                | 193.6                              | 43 916                                   | 15 799 | 15.1                    | 9.03 | 2464                               | 841  |
|                  | 133         | 351.9                 | 373.3                 | 15.6                             | 15.2             | 290                        | 22.5                | 169.0                              | 37 840                                   | 13 576 | 15.0                    | 8.96 | 2150                               | 727  |
|                  | 109         | 346.4                 | 370.5                 | 12.9                             | 15.2             | 290                        | 26.9                | 138.4                              | 30 515                                   | 10 901 | 14.8                    | 8.87 | 1762                               | 588  |
| 305 × 305        | 223         | 338.0                 | 325.4                 | 30.5                             | 15.2             | 247                        | 11.1                | 285.0                              | 52 817                                   | 17 570 | 13.6                    | 7.80 | 3126                               | 1080 |
|                  | 186         | 328.4                 | 320.5                 | 25.7                             | 15.2             | 247                        | 12.8                | 237.0                              | 42 625                                   | 14 108 | 13.4                    | 7.70 | 2597                               | 881  |
|                  | 149         | 318.2                 | 315.5                 | 20.6                             | 15.2             | 247                        | 15.4                | 190.0                              | 33 040                                   | 10 869 | 13.2                    | 7.60 | 2075                               | 689  |
|                  | 126         | 312.4                 | 312.5                 | 17.8                             | 15.2             | 247                        | 17.6                | 161.3                              | 27 526                                   | 9 013  | 13.1                    | 7.50 | 1760                               | 576  |
|                  | 110         | 307.9                 | 310.3                 | 15.4                             | 15.2             | 247                        | 20.0                | 140.4                              | 23 589                                   | 7 689  | 13.0                    | 7.40 | 1532                               | 496  |
|                  | 95          | 303.8                 | 308.3                 | 13.4                             | 15.2             | 247                        | 22.7                | 121.0                              | 20 111                                   | 6 529  | 12.9                    | 7.30 | 1324                               | 424  |
| 254 × 254        | 88          | 301.7                 | 307.2                 | 12.3                             | 15.2             | 247                        | 24.5                | 112.0                              | 18 402                                   | 5 959  | 12.8                    | 7.30 | 1220                               | 388  |
|                  | 79          | 299.2                 | 306.0                 | 11.1                             | 15.2             | 247                        | 27.0                | 100.4                              | 16 400                                   | 5 292  | 12.8                    | 7.26 | 1096                               | 346  |
| 203 × 203        | 85          | 254.3                 | 259.7                 | 14.3                             | 12.7             | 200                        | 17.8                | 108.1                              | 12 264                                   | 4 188  | 10.7                    | 6.22 | 965                                | 323  |
|                  | 71          | 249.9                 | 257.5                 | 12.1                             | 12.7             | 200                        | 20.6                | 91.0                               | 10 153                                   | 3 451  | 10.6                    | 6.10 | 813                                | 268  |
|                  | 63          | 246.9                 | 256.0                 | 10.6                             | 12.7             | 200                        | 23.3                | 79.7                               | 8 775                                    | 2 971  | 10.5                    | 6.11 | 711                                | 232  |
| 203 × 203        | 54          | 203.9                 | 207.2                 | 11.3                             | 10.2             | 161                        | 18.0                | 68.4                               | 4 987                                    | 1 683  | 8.54                    | 4.95 | 489                                | 162  |
|                  | 45          | 200.2                 | 205.4                 | 9.5                              | 10.2             | 161                        | 21.1                | 57.0                               | 4 079                                    | 1 539  | 8.46                    | 4.90 | 408                                | 133  |

Table 29.2 Dimensions and properties of Larssen box piles



| Section      | B<br>(mm)<br>(nom.) | H<br>(mm)<br>(nom.) | d<br>(mm) | Mass<br>per<br>metre<br>(kg) | Section area<br>(cm <sup>2</sup> ) |               | Least<br>rad. of<br>gyr.<br>(cm) | Approx<br>perim.<br>(mm) | Second moment of area<br>(cm <sup>4</sup> ) |              | Section modulus<br>(cm <sup>3</sup> ) |              |
|--------------|---------------------|---------------------|-----------|------------------------------|------------------------------------|---------------|----------------------------------|--------------------------|---|--------------|---------------------------------------|--------------|
|              |                     |                     |           |                              | Steel<br>only                      | Whole<br>pile |                                  |                          | About<br>X-X                                | About<br>Y-Y | About<br>X-X                          | About<br>Y-Y |
| 6W           | 525                 | 252                 | 7.8       | 89.4                         | 113.8                              | 1122          | 9.33                             | 1652                     | 10 028                                      | 39 280       | 796                                   | 1400         |
| 9W           | 525                 | 300                 | 8.9       | 102.0                        | 129.9                              | 1344          | 11.43                            | 1748                     | 16 976                                      | 43 812       | 1132                                  | 1562         |
| 12W          | 525                 | 349                 | 9.0       | 120.8                        | 153.9                              | 1589          | 13.00                            | 1872                     | 25 992                                      | 55 442       | 1490                                  | 1970         |
| 16W          | 525                 | 391                 | 10.5      | 136.6                        | 174.0                              | 1776          | 14.80                            | 1952                     | 38 126                                      | 60 920       | 1950                                  | 2164         |
| 20W          | 525                 | 447                 | 11.3      | 154.6                        | 196.9                              | 2005          | 16.63                            | 2084                     | 54 474                                      | 70 120       | 2438                                  | 2482         |
| 25W          | 525                 | 502                 | 12.1      | 175.8                        | 223.9                              | 2221          | 18.33                            | 2164                     | 75 240                                      | 80 082       | 2998                                  | 2830         |
| 32W          | 525                 | 502                 | 17.0      | 207.3                        | 264.1                              | 2224          | 18.02                            | 2168                     | 96 584                                      | 85 806       | 3848                                  | 3032         |
| 3            | 400                 | 299                 | 14.1      | 124.4                        | 158.6                              | 1020          | 11.22                            | 1596                     | 47 055                                      | 36 039       | 2199                                  | 1649         |
| 4A           | 400                 | 428                 | 15.7      | 148.0                        | 188.7                              | 1413          | 13.82                            | 1772                     | 106 780                                     | 67 756       | 4237                                  | 2920         |
| 6 (122 kg)   | 420                 | 502                 | 22.0      | 244.0                        | 310.6                              | 1794          | 14.77                            | 2080                     | 11 8588                                     | 69 859       | 4725                                  | 3011         |
| 6 (131 kg)   | 420                 | 502                 | 25.4      | 262.0                        | 333.6                              | 1794          | 14.47                            | 2080                     | 12 8448                                     | 71 392       | 5117                                  | 3077         |
| 6 (138.7 kg) | 420                 | 502                 | 28.6      | 277.4                        | 353.2                              | 1794          | 14.27                            | 2080                     |   |              |                                       |              |

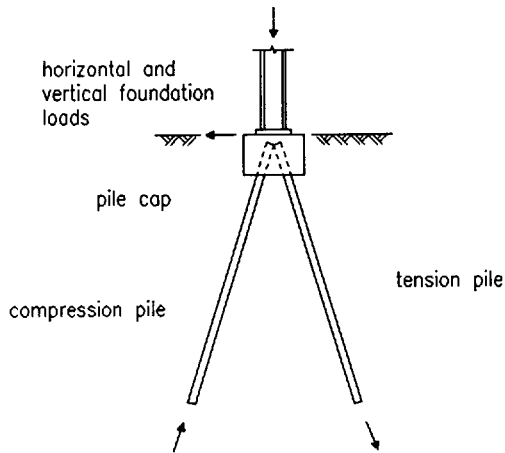


Fig. 29.2 Raking pile foundation

### *Design stresses*

Steel bearing piles are commonly designed on a working stress of 33% of yield stress. A driven pile is usually driven to a resistance of twice the working load to demonstrate an adequate factor of safety. Thus the average stress in the shaft is 66% of yield during driving. The remaining stress capacity up to yield is available to cater for the very high impact stresses which occur in the pile shaft immediately under the hammer. Steel, being an elastic material, shortens elastically under each blow of the hammer and so the high head stresses dissipate rapidly and affect only the top one or two centimetres of the shaft metal. Figure 29.3 shows the typical stress distribution.

### *Pile capacity*

In general, steel bearing piles are most cost effective if they can be designed to develop resistance through end bearing on rock, dense granular soils or very hard clay. In other soils it is difficult to utilize fully the strength of the steel without overstressing the soil.

When achieving end bearing on rock, it is usual to employ grade 50A steel, giving a considerable increase in capacity (37%), for a small cost increase (approximately 10%) compared with grade 43A steel.

Because the allowable axial stress is limited by the reserve of strength required for driving stresses, the pile is capable of carrying significant bending stress in addition to axial stress. The total combined stress should not exceed 0.5 yield stress.

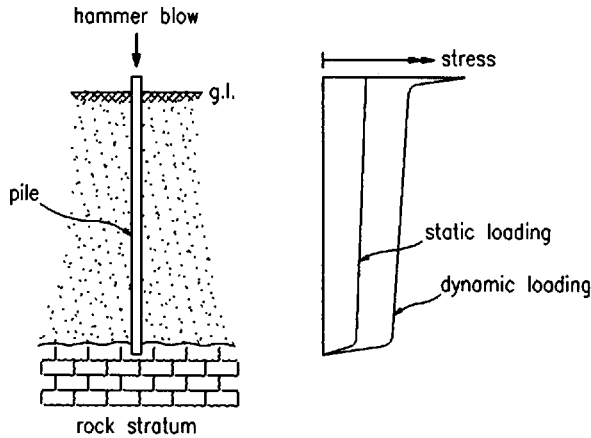


Fig. 29.3 Pile stresses

Alternatively, when the pile is likely to be subject to corrosion (see Table 29.10) and has to support only axial loading, the spare capacity in the static condition can be used to compensate for loss of metal thickness. This represents an increase in useful life of 67%.

In circumstances where the pile is driven through soft overburden to end resistance on rock the allowable design stress can be increased from 33% to 50% of yield stress since the high stresses at the head of the pile shaft will only be generated for a few blows of the hammer while the pile is being seated on the rock.

Unless any part of a pile passes through particularly weak soil, or is exposed above soil level, it will receive full lateral support and can be designed as a short column with no allowance for buckling failure.

Where a pile is exposed above soil level it must be designed as a free-standing column taking full account of slenderness ratios for the exposed part of the shaft.

A similar allowance must be made for those parts of any pile shaft which pass through particularly weak soils. Table 29.3 shows the degree of lateral restraint which may be assumed from various types of soil.

**Table 29.3** Lateral support for various soil types

| Soil type                    | Lateral support |
|------------------------------|-----------------|
| Granular                     | Full            |
| Cohesive:                    |                 |
| $c = 0-12.5 \text{ kN/m}^2$  | None            |
| $c = 12.5-20 \text{ kN/m}^2$ | Partial         |
| $c > 20 \text{ kN/m}^2$      | Full            |

### *Pile length*

There are many different ways of estimating the length of pile which is necessary to provide a given carrying capacity. The following formulae for granular soils and cohesive soils are commonly used but others are equally suitable.

#### (1) *Granular soils*

Meyerhof – based on standard penetration test (SPT).

End resistance  $400 \times N \times A$  kN ultimate

Shaft friction  $2 \times N \times a$  kN ultimate

where

$N$  = blows/300 mm (SPT)

$A$  = end area of pile ( $\text{m}^2$ )

$a$  = shaft area of pile ( $\text{m}^2$ )

For submerged soils,  $N = 0.67$  (blows/300 mm)

For H-piles,

$a$  = enclosing rectangle  $2 \times (B + D) \times \text{length}$

$A = B \times D$  (firm soils)

$= 0.5(B \times D)$  (soft soils)

#### (2) *Cohesive soils*

End resistance  $9 \times c \times A$  kN ultimate

Shaft resistance  $0.7 \times c \times a$  kN ultimate

where cohesion  $c$  is given in Table 29.3.

## **29.1.4 Installation**

### *Support and guidance*

Adequate positional and directional restraint during pitching and driving are essential if piles are to be driven within acceptable tolerance of head location and verticality/rake. Normal tolerance limits are 75 mm in any direction in plan at the pile head, 1:100 verticality for vertical piles and 1:75 for raking piles.

### *Splices*

Site butt splicing is frequently necessary when the required length of pile is too great to be delivered to site in one piece, or when an extension to the designed length is found to be necessary because the required resistance is not available at the anticipated depth. In both cases the butt weld is made after the first length of pile is driven until its upper end is just above ground level, the extension piece

then being positioned and welded on. Acceptance standards for the site welds are given in the British Steel Plc publication *Welding Quality Acceptance Standards for Site Butt Welds in Steel Bearing Piles*.

### 29.1.5 Evaluation of capacity

The safe load capacity of each pile must be demonstrated. The only certain way to do this is by static test loading. Unfortunately, to do this for every pile is neither practical nor economical for most projects.

Alternative, though less accurate, ways of evaluating piles are by:

- (1) calibration of the pile-driver by means of a test load
- (2) dynamic formula
- (3) stress wave analysis.

Pile head settlement is most accurately determined by static test load. Dynamic formulae give no indication of this value. Stress wave analysis will give an indication; the technique is rapidly improving.

#### *Static test loading*

The tests can be performed with kentledge loading or reaction anchors as shown in Fig. 29.4. Correct interpretation of the results of static test loading is essential.

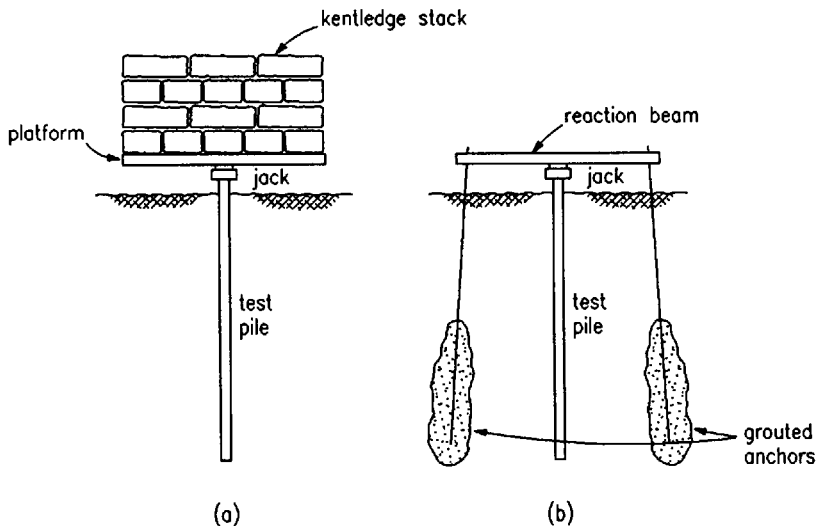


Fig. 29.4 Static load testing. (a) Kentledge test load. (b) Reaction test load

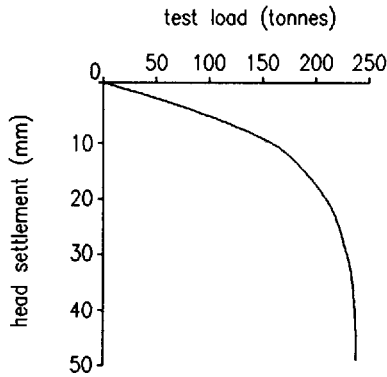


Fig. 29.5 Load-settlement plot

A plot of load/head settlement (Fig. 29.5) provides an understanding of pile head performance, which is an essential requirement for ensuring compatibility between superstructure and foundation, but it reveals only part of the picture of overall pile performance.

It is also very important to know the true limits of pile load capacity. Head settlement does not necessarily indicate toe settlement, which is the true indicator of pile failure. From the diagram in Fig. 29.5, a further diagram can be constructed by allowing for the effects of elastic shortening of the pile shaft, which will show load/toe settlement, Fig. 29.6.

Elastic shortening can be significant in steel piles, especially those which are long and fully stressed in grade 50A quality. Such shortening is of no consequence provided it is anticipated and allowed for in design and evaluation.

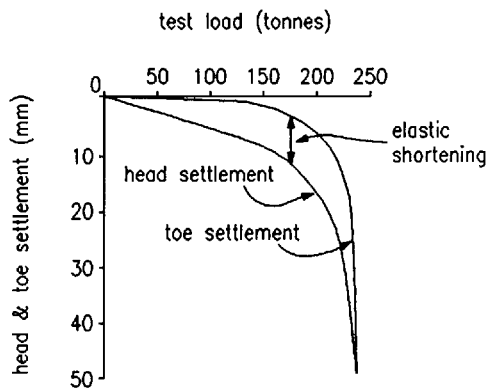


Fig. 29.6 Corrected load-settlement plot

*Pile-driver calibration*

To overcome the need to test load every pile, careful records taken during the driving of a subsequently satisfactorily test-loaded pile can be used to evaluate later piles. This system is reliable when the hammer, pile size, pile length, and geology remain unchanged for subsequent piles. However, as soon as any one of these elements is changed further test loading and recalibration is required.

*Dynamic formulae*

These are an attempt to relate the energy output of the impact hammer and the pile penetration per blow of the hammer to the static resistance of the pile. There are a number of such formulae available but all are to some degree unreliable. The resistance of the pile and soil under the influence of dynamic hammer loading may be very different to that under static loading.

Dynamic formulae are therefore useful in indicating relative, rather than absolute, values. Where there are relatively few piles in the project and test loading is not economic, dynamic formulae may be used, but with a suitably enhanced factor of safety.

The use of dynamic formulae also requires careful supervision of site operations. Drop hammers must be as truly 'free fall' as possible – ram guide and cable friction minimized, and drum inertia allowed for. Diesel hammers must not be allowed to overheat as this leads to marked reduction in energy output. Dolly material must be in good condition and pile heads undamaged at the time of taking readings.

Finally, and most important, redrive checks must be carried out to ensure that the resistance of the pile does not change after driving is completed. This is most likely to occur if pore water pressures in the soil are altered by the action of driving the piles. A significant change of pile resistance between the end of the initial drive and the commencement of the redrive means that dynamic formulae are completely unreliable for those circumstances.

*Stress wave analysis*

This is a relatively recent development which is gaining acceptance through the advent of direct on-site computer analysis of pile gauge readings. It provides information on pile toe resistance, pile shaft resistance, pile shaft integrity, and actual energy input to the pile head.

This form of evaluation provides valuable information as the pile is driven, which is an ideal arrangement. However, it still relies on relating dynamic resistance to static resistance and care must be taken to ensure the results are not misleading. Redrive checks are essential and a cross check by static loading may be advisable at the start of a large contract.



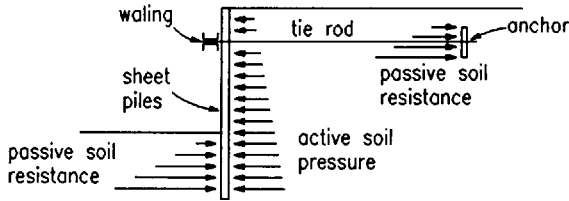


Fig. 29.7 Sheet pile retaining wall

## 29.2 Sheet piles

### 29.2.1 Uses

There are various types of earth-retaining structures. Where a differential surface level is to be established with a vertical interface, a retaining wall is used. Steel sheet piling is one form of retaining wall construction. Sheet piles resist soil and water pressures by functioning as a beam spanning vertically between points of support, as shown in Fig. 29.7.

Steel sheet piles are also used for the construction of temporary coffer-dams; the piles enable deep excavations to be made to facilitate construction below ground and water level of other permanent works. On completion of construction the sheet piles are usually extracted for re-use on other projects. Coffers-dams may consist of cantilever sheet pile walls when the excavated depth is small, or, for greater depths, the sheet piles are supported by one or more levels of internal supporting frames (see Fig. 29.8).

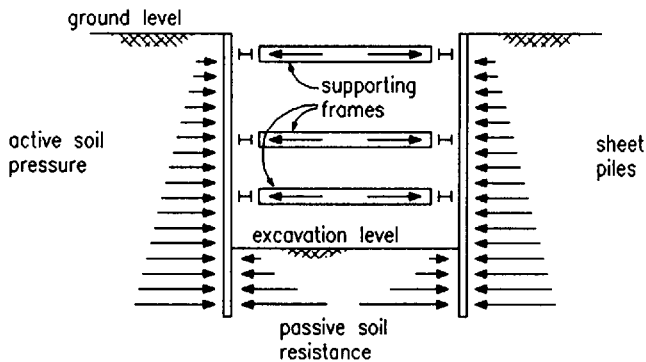


Fig. 29.8 Sheet pile coffer-dam

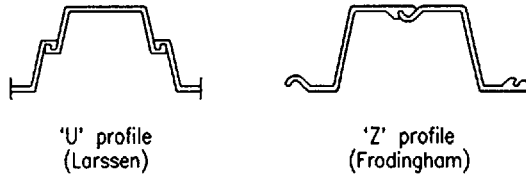


Fig. 29.9 Types of sheet pile

### 29.2.2 Types of piles

The section profile may be U or Z shape, as shown in Fig. 29.9. Details are given in Table 29.4(a) and (b). The essential difference between these sections and ordinary structural beams is their ability to interlock with each other to form a continuous membrane in the soil. Where the depth of excavation is small, trench sheet sections (Table 29.4(c)) may be used as an alternative to sheet piles.

### 29.2.3 Design

#### *Soil pressures*

Active soil pressure and passive soil resistance, at any given depth, are both a function of the effective vertical pressure at that depth and of the strength of the stratum being considered. The active pressure ( $p_a$ ) is always equal to, or less than, the vertical overburden pressure and the passive resistance ( $p_p$ ) is always equal to, or greater than, the overburden pressure.

For granular soils (sands, gravels, coarse silts, etc.), the expressions depicting the two conditions are:

$$p_a = \gamma h \times k_a$$

$$p_p = \gamma h \times k_p$$

where  $\gamma$  = effective density of the soil,

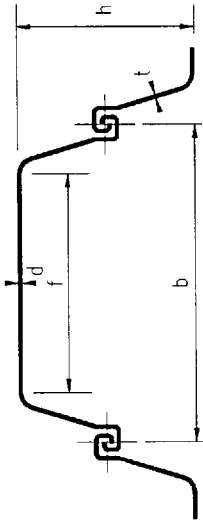
$h$  = depth of overburden,

$k_a$  = coefficient of active pressure,

$k_p$  = coefficient of passive resistance.

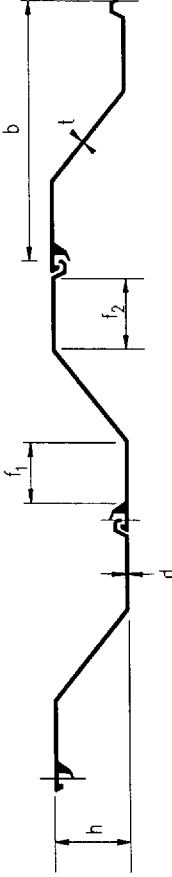
The expression for cohesive soils (clays) has two alternative forms, depending upon the geological history of the soil mass (normally, or over-consolidated) and upon the life requirement of the proposed earth-retaining structure (short-term temporary works, or long-term permanent works):

Table 29.4(a) Dimensions and properties of Larssen sheet piles



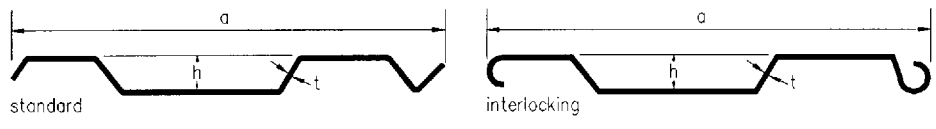
| Section | b<br>(mm)<br>(nom.) | h<br>(mm)<br>(nom.) | d<br>(mm) | t<br>(mm)<br>(nom.) | f<br>flat of pan<br>(mm) | Sectional<br>area<br>(cm <sup>2</sup><br>per metre<br>of wall) | Mass                        |                                       | Combined<br>second<br>moment of<br>area (cm <sup>4</sup><br>per metre) | Section<br>modulus<br>(cm <sup>3</sup><br>per metre) |
|---------|---------------------|---------------------|-----------|---------------------|--------------------------|--|-----------------------------|---------------------------------------|--|--|
|         |                     |                     |           |                     |                          |  | (kg per<br>linear<br>metre) | (kg per<br>m <sup>2</sup><br>of wall) |  |  |
| 6W      | 525                 | 212                 | 7.8       | 6.4                 | 331                      | 108  | 44.7                        | 85.1                                  | 6459   | 610  |
| 9W      | 525                 | 260                 | 8.9       | 6.4                 | 343                      | 124  | 51.0                        | 97.1                                  | 11726  | 902  |
| 12W     | 525                 | 306                 | 9.0       | 8.5                 | 343                      | 147  | 60.4                        | 115.1                                 | 18345  | 1199   |
| 16W     | 525                 | 348                 | 10.5      | 8.6                 | 341                      | 166  | 68.3                        | 130.1                                 | 27857  | 1601   |
| 20W     | 525                 | 400                 | 11.3      | 9.2                 | 333                      | 188  | 77.3                        | 147.2                                 | 40180  | 2009   |
| 25W     | 525                 | 454                 | 12.1      | 10.5                | 317                      | 213  | 87.9                        | 167.4                                 | 56727  | 2499   |
| 32W     | 525                 | 454                 | 17.0      | 10.5                | 317                      | 252  | 103.6                       | 197.4                                 | 73003  | 3216   |
| 3       | 400                 | 248                 | 14.1      | 8.5                 | 253                      | 198  | 62.2                        | 155.5                                 | 16980  | 1360   |
| 4A      | 400                 | 381                 | 15.7      | 9.6                 | 219                      | 236  | 74.0                        | 185.1                                 | 44916  | 2360   |
| 6       | 420                 | 440                 | 22.0      | 14.0                | 248                      | 370  | 122.0                       | 290.5                                 | 92452  | 4200   |
| 6       | 420                 | 440                 | 25.4      | 14.0                | 251                      | 397  | 131.0                       | 311.8                                 | 102861   | 4675   |
| 6       | 420                 | 440                 | 28.6      | 14.0                | 251                      | 421  | 138.7                       | 330.2                                 | 111450   | 5066   |

Table 29.4(b) Dimensions and properties of Frodingham sheet piles



| Section | b<br>(mm)<br>(nom.) | h<br>(mm)<br>(nom.) | d<br>(mm) | t<br>(mm)<br>(nom.) | f <sub>1</sub><br>(mm)<br>(nom.) | f <sub>2</sub><br>(mm)<br>(nom.) | Sectional<br>area<br>(cm <sup>2</sup><br>per metre<br>of wall) | Mass                        |                                       | Second<br>moment<br>of area<br>(cm <sup>4</sup> per<br>metre) | Section<br>modulus<br>(cm <sup>3</sup><br>per<br>metre) |
|---------|---------------------|---------------------|-----------|---------------------|----------------------------------|----------------------------------|--|-----------------------------|---------------------------------------|---|---|
|         |                     |                     |           |                     |                                  |                                  |  | (kg per<br>linear<br>metre) | (kg per<br>m <sup>2</sup><br>of wall) |   |   |
| 1BXN    | 476                 | 143                 | 12.7      | 12.7                | 78                               | 123                              | 166.5  | 62.1                        | 130.4                                 | 4919  | 688   |
| 1N      | 483                 | 170                 | 9.0       | 9.0                 | 105                              | 137                              | 126.0  | 47.8                        | 99.1                                  | 6048  | 713   |
| 2N      | 483                 | 235                 | 9.7       | 8.4                 | 97                               | 149                              | 143.0  | 54.2                        | 112.3                                 | 13513   | 1150  |
| 3N      | 483                 | 283                 | 11.7      | 8.9                 | 89                               | 145                              | 175.0  | 66.2                        | 137.1                                 | 23885   | 1688  |
| 3NA     | 483                 | 305                 | 9.7       | 9.5                 | 96                               | 146                              | 165.0  | 62.6                        | 129.8                                 | 25687   | 1690  |
| 4N      | 483                 | 330                 | 14.0      | 10.4                | 77                               | 127                              | 218.0  | 82.4                        | 170.8                                 | 39831   | 2414  |
| 5       | 425                 | 311                 | 17.0      | 11.9                | 89                               | 118                              | 302.0  | 100.8                       | 236.9                                 | 49262   | 3168  |

**Table 29.4(c)** Dimensions and properties of trench sheets



| Section      | <i>a</i><br>(mm) | Effective<br>width<br>per sheet | <i>h</i><br>(mm) | <i>t</i><br>(mm) | kg per<br>linear<br>metre | kg per<br>m <sup>2</sup> | Section<br>modulus<br>per sheet |
|--------------|------------------|---------------------------------|------------------|------------------|---------------------------|--------------------------|---------------------------------|
| Standard     | 350              | 330                             | 35               | 3.6              | 11.30                     | 34.30                    | 15.3                            |
| Interlocking | 460              | 432                             | 35               | 3.55             | 15.16                     | 35.09                    | 21.07                           |

- (1) Normally consolidated clays with cohesion, *c*, up to 50 kN/m<sup>2</sup>, temporary and permanent works

$$p_a = \gamma h - k_{ac} c \quad p_p = \gamma h + k_{pc} c$$

where  $k_{ac}$  = coefficient of active pressure,  
 $k_{pc}$  = coefficient of passive resistance.

- (2) Over-consolidated clays with cohesion, *c*, greater than 50 kN/m<sup>2</sup> temporary works

$$p_a = \gamma h - k_{ac} c \quad p_p = \gamma h + k_{pc} c$$

permanent works

$$p_a = \gamma h \times k_a \quad \phi'(C' = 0)$$

$$p_p = \gamma h \times k_p \quad \phi'(C' = 0)$$

Values of  $k_a$  and  $k_p$  are modified by the effects of wall friction ( $\delta$ ) which is taken as  $0.5\phi$  for steel piles. Values of  $k_{ac}$  and  $k_{pc}$  are modified by the effects of wall adhesion ( $c_w$ ) which, for active pressures, is taken as  $c_w = c$ , up to a maximum of 50 kN/m<sup>2</sup>, and for passive pressures, is taken as  $c_w = 0.5c$ , up to a maximum of 25 kN/m<sup>2</sup>. Tables 29.5 to 29.8 show values of  $k_a$ ,  $k_{ac}$ ,  $k_p$  and  $k_{pc}$ .

Active pressure and passive resistance are plotted as a net pressure diagram as shown in Fig. 29.10. From this diagram the required pile length, anchor loads (if any) and pile bending are determined.

There are two basic types of sheet pile structures:

- (1) cantilever wall
- (2) anchored wall.

The anchored wall can be designed such that the support mobilized from the soil at the bottom of the wall is sufficient to provide either 'fixed earth' support or 'free earth' support to the piles, the difference depending on the depth to which

**Table 29.5** Coefficients of active pressure for granular soils,  $k_a$

| Values of $\delta$ | Values of $\phi$ |      |      |      |      |
|--------------------|------------------|------|------|------|------|
|                    | 25°              | 30°  | 35°  | 40°  | 45°  |
| 0                  | 0.41             | 0.33 | 0.27 | 0.22 | 0.17 |
| 10°                | 0.37             | 0.31 | 0.25 | 0.20 | 0.16 |
| 20°                | 0.34             | 0.28 | 0.23 | 0.19 | 0.15 |
| 30°                | —                | 0.26 | 0.21 | 0.17 | 0.14 |

**Table 29.6** Coefficients of passive resistance for granular soils,  $k_p$

| Values of $\delta$ | Values of $\phi$ |     |     |      |
|--------------------|------------------|-----|-----|------|
|                    | 25°              | 30° | 35° | 40°  |
| 0                  | 2.5              | 3.0 | 3.7 | 4.6  |
| 10°                | 3.1              | 4.0 | 4.8 | 6.5  |
| 20°                | 3.7              | 4.9 | 6.0 | 8.8  |
| 30°                | —                | 5.8 | 7.3 | 11.4 |

**Table 29.7** Coefficients of active pressure for cohesive soils,  $k_{ac}$

|          | Values of $\delta$ | Values of $c_w/c$ | Values of $\phi$ |      |      |      |      |      |
|----------|--------------------|-------------------|------------------|------|------|------|------|------|
|          |                    |                   | 0°               | 5°   | 10°  | 15°  | 20°  | 25°  |
| $k_a$    | 0                  | All values        | 1.00             | 0.85 | 0.70 | 0.59 | 0.48 | 0.40 |
|          | $\phi$             |                   | 1.00             | 0.78 | 0.64 | 0.50 | 0.40 | 0.32 |
| $k_{ac}$ | 0                  | 0                 | 2.00             | 1.83 | 1.68 | 1.54 | 1.40 | 1.29 |
|          | 0                  | 1                 | 2.83             | 2.60 | 2.38 | 2.16 | 1.96 | 1.76 |
|          | $\phi$             | $\frac{1}{2}$     | 2.45             | 2.10 | 1.82 | 1.55 | 1.32 | 1.15 |
|          | $\phi$             | 1                 | 2.83             | 2.47 | 2.13 | 1.85 | 1.59 | 1.41 |

**Table 29.8** Coefficients of passive resistance for cohesive soils,  $k_{pc}$

|          | Values of $\delta$ | Values of $c_w/c$ | Values of $\phi$ |     |     |     |     |     |
|----------|--------------------|-------------------|------------------|-----|-----|-----|-----|-----|
|          |                    |                   | 0°               | 5°  | 10° | 15° | 20° | 25° |
| $k_p$    | 0                  | All values        | 1.0              | 1.2 | 1.4 | 1.7 | 2.1 | 2.5 |
|          | $\phi$             |                   | 1.0              | 1.3 | 1.6 | 2.2 | 2.9 | 3.9 |
| $k_{pc}$ | 0                  | 0                 | 2.0              | 2.2 | 2.4 | 2.6 | 2.8 | 3.1 |
|          | 0                  | $\frac{1}{2}$     | 2.4              | 2.6 | 2.9 | 3.2 | 3.5 | 3.8 |
|          | 0                  | 1                 | 2.6              | 2.9 | 3.2 | 3.6 | 4.0 | 4.4 |
|          | $\phi$             | $\frac{1}{2}$     | 2.4              | 2.8 | 3.3 | 3.8 | 4.5 | 5.5 |
|          | $\phi$             | 1                 | 2.6              | 2.9 | 3.4 | 3.9 | 4.7 | 5.7 |

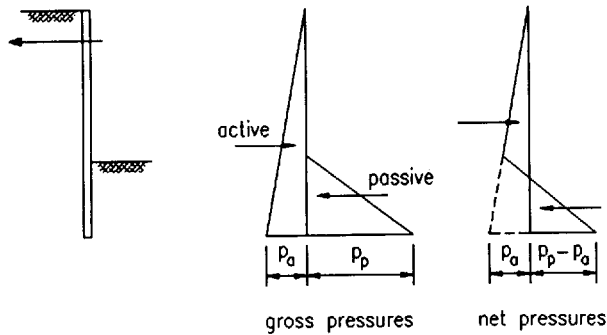


Fig. 29.10 Pressure diagrams

the piles are to penetrate. Figure 29.11 illustrates the pressure and bending moment for the various conditions.

Anchorage comprise a series of tie rods and passive anchor units, or pressure-grouted anchor tendons, at regular intervals along the length of the wall. Load is transferred from the piles to the anchors by means of walings, usually pairs of RSCs back to back with space between them to accommodate the tie rod.

When passive anchor units are used, the distance of the anchor unit from the front retaining wall must be carefully determined to ensure that the zone of unstable soil supported by the wall does not encroach upon the passive soils providing the resistance to the anchor unit. Figure 29.12 illustrates the requirement. Grouted anchors are normally designed and installed by specialist sub-contractors.

Walings are designed as beams spanning between the anchorages (taking advantage of continuity when the walings are continuous over several anchors). Adequate protection against corrosion is essential. Tie rods are selected from manufacturers' published safe load tables. Anchorages may be either steel sheet piles or concrete and either isolated or continuous.

### Coffer-dams

In the design of multi-frame coffer-dams the designer must be sure to check every condition of partial excavation which can occur during construction: the temporary condition of partial excavation in preparation for erection of each succeeding frame is often more critical than the fully excavated and framed condition (Figs 29.8 and 29.13).

The number and position of supporting frames is a function of the size of sheet pile, or vice versa. The position of the frames must also be considered with respect to the construction sequence of the permanent works which are built within the coffer-dam. Compatibility of the temporary and permanent works is vital if the project is to be executed efficiently and economically. For particularly

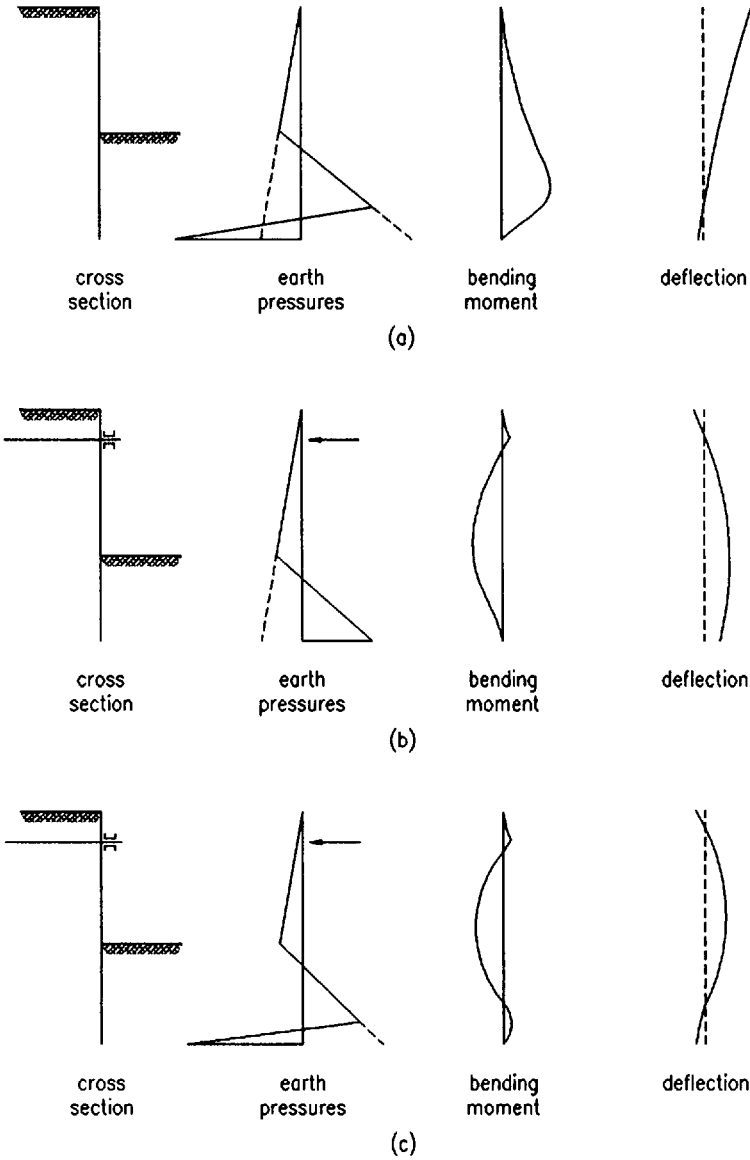


Fig. 29.11 Pressures, bending moments and deflections in retaining walls: (a) cantilever, (b) anchored, free earth support, (c) anchored, fixed earth support

complex permanent works it may preferable to form the coffer-dam as a circular structure which uses circular ring beam wales (in reality, ring struts), thus entirely eliminating cross strutting and creating an unobstructed construction space for the permanent works.



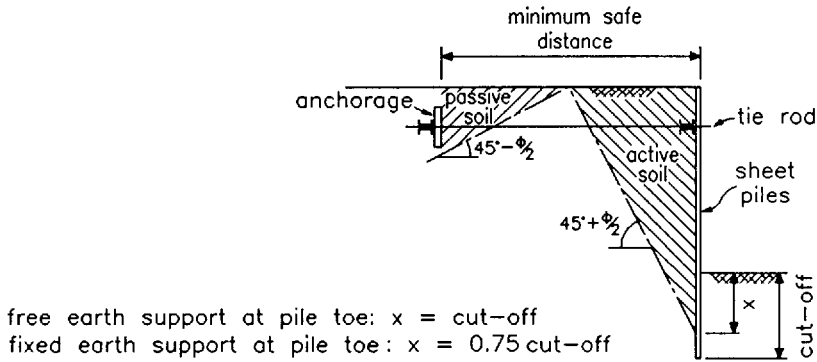


Fig. 29.12 Minimum safe distance of anchorage

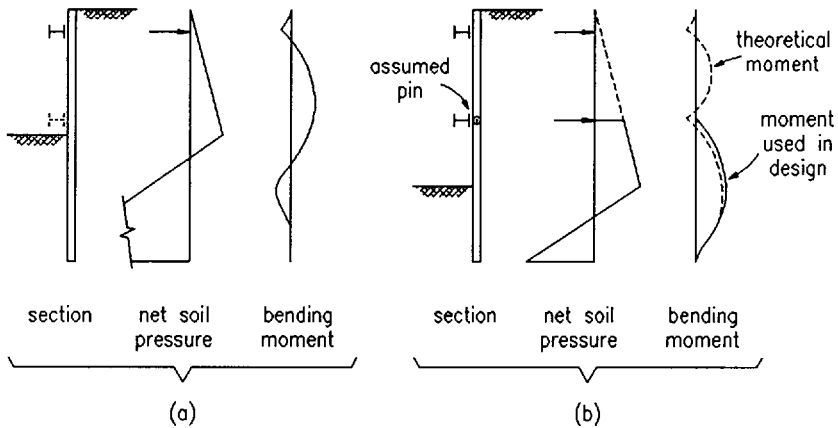
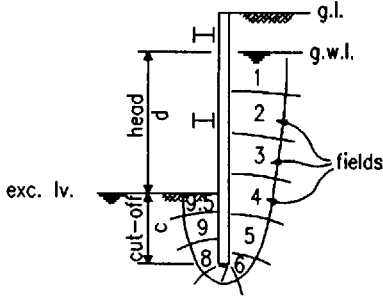


Fig. 29.13 Partial and fully excavated conditions. (a) Temporary condition, (b) final condition

When sheet piles are used for coffer-dams, the length of pile below formation level, the 'cut-off', is often critical to the stability of the bottom of the coffer-dam in terms of controlling the ingress of ground water, which can destabilize the passive zone, when working in permeable soils. Figure 29.14 shows how the overburden in the passive zone is reduced by the pressure of ground water flowing under the toes of the piles.

A flow net investigation, as shown in Fig. 29.14, will quickly demonstrate this and provide a check on the adequacy of the cut-off in general for the control of ground water flow.



$w$ =water density  
 $\gamma$ =soil density

no. of field =  $N(9.5)$

diff. head press =  $d \times w$

head loss/field =  $d \times w / N$

flow head at pile toe  
 (btm. of field no.8) =  $2.5d \times w / N$

total passive overburden  
 at pile toe =  $(\gamma + w) \times c$

effective passive %burden  
 at toe =  $(\gamma + w) \times c - 2.5d \times w / N$

Fig. 29.14 Ground water flow net

*Driving considerations*

The size of sheet pile section is frequently determined by the requirement that it must be capable of being driven to the design penetration in the ground without deformation. Table 29.9 gives some guidance to enable a pile of suitable driving properties to be selected.

**Table 29.9** Selection of pile size to suit driving conditions

| Dominant SPT value (N) | Minimum wall modulus (cm <sup>3</sup> /m of wall) |
|------------------------|---|
| 0-10                   | 450   |
| 11-20                  | 450   |
| 21-25                  | 850   |
| 26-30                  | 850   |
| 31-35                  | 1300  |
| 36-40                  | 1300  |
| 41-45                  | 2300  |
| 46-50                  | 2300  |
| 51-60                  | 3000  |
| 61-70                  | 3000  |
| 71-80                  | 4200  |
| 81-140                 | 4200  |

*NB* This table is based upon sheet pile sections of approximately 500 mm interlock centres installed with panel driving techniques. Wider sections and those installed by methods giving less control will require greater moduli.

*Durability*

The method of achieving the desired working life of the structure can make a very large difference to both first cost and maintenance costs. A steel structure deteriorates with the passage of time due to the effects of corrosion. However the rate of deterioration varies with the degree of aggressiveness of the environment to which the structure is exposed.

In sheet pile retaining walls, especially those in maritime locations, there are several different environmental zones (see Fig. 29.15(a)) which are, in order of decreasing aggressiveness:

- (1) high tide and splash zone,
- (2) low water zone,
- (3) intertidal zone,
- (4) atmospheric zone,
- (5) submerged zone,
- (6) embedded zone.

Recent research has evaluated the relative aggressiveness of each of these zones and typical rates of corrosion can now be ascribed to them. Values are given in Table 29.10. In many cases the effects of corrosion are such that no special measures are necessary since significant corrosion occurs only in locations where stresses are low and considerable loss of metal thickness is permissible (Fig. 29.15(c)).

If corrosion is still deemed to be a problem, its effects can be countered by using grade 50A steels in designs based on grade 43A stresses. This expedient has the benefit of increasing the permissible working stress by a precisely known amount and hence the working life by the same proportion. It also has the secondary benefit of providing a pile section with improved driving capability.

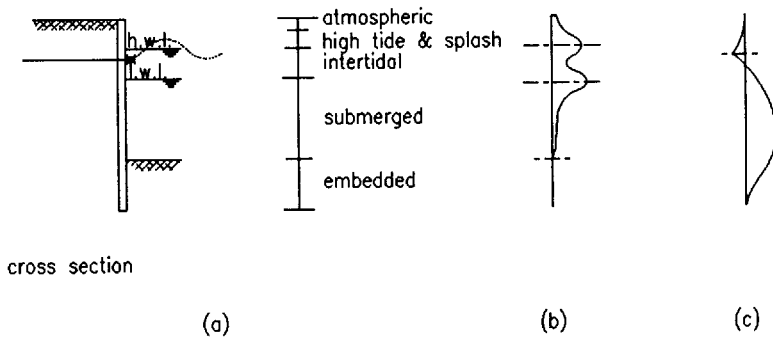


Fig. 29.15 Environmental zones. (a) Zones, (b) Corrosion rate, (c) Bending moment

Table 29.10 Effective life of sheet piling

| Frodingham | Section type |  | Environments              |                            |                                    |             |
|------------|--------------|--|---------------------------|----------------------------|------------------------------------|-------------|
|            | Larssen      | Permissible loss in thickness (mm) at position of maximum stress in pile | Atmospheric corrosion     | Splash and low water zones | Sea water immersion and tidal zone | Underground |
|            |              |  | 0.05 (mean)               | 0.09 (mean)                | 0.05 (mean)                        | 0.03 (max.) |
|            |              |  | Corrosion rates (mm/year) |                            |                                    |             |
|            |              |  | Effective life (years)    |                            |                                    |             |
|            | 6W, 9W       | 3.5  | 70                        | <sup>a</sup>               | <sup>a</sup>                       | 117         |
|            | 12W, 16W     | 4.5  | 90                        | 50                         | 90                                 | 120+        |
|            | 202, 3, 4A   | 5.0  | 100                       | 55                         | 100                                | 120+        |
| 1N         |              | 5.2  | 104                       | 58                         | 104                                | 120+        |
| 2N         |              | 5.4  | 108                       | 60                         | 108                                | 120+        |
| 3NA        |              | 5.5  | 110                       | 60                         | 110                                | 120+        |
| 3N         |              | 5.9  | 118                       | 65                         | 118                                | 120+        |
|            | 25W, 32W     | 6.0  | 120                       | 67                         | 120                                | 120+        |
|            | All No. 6    | 7.0  | 120+                      | 78                         | 120+                               | 120+        |
| 1BXN       |              | 7.2  | 120+                      | 80                         | 120+                               | 120+        |
| 4N         |              | 7.4  | 120+                      | 82                         | 120+                               | 120+        |
| 5          |              | 8.9  | 120+                      | 99                         | 120+                               | 120+        |

<sup>a</sup> Not suitable for marine environments


Alternatively the piles can be protected against the effects of corrosion by the application of paint coatings, but even with the best surface preparation and paints, these will only give an increase of life of 15 to 20 years before maintenance becomes necessary.

### Further reading for Chapter 29

- British Standards Institution (1943) *Code of practice for earth retaining structures*. CP2, BSI, London. (To be replaced by BS 8002: *Code of practice for earth retaining structures*.)
- British Standards Institution (1984–8) *Code of practice for maritime structures*. BS 6349, BSI, London.
- British Steel, General Steels (1988) *Piling Handbook*, 6th edn. British Steel plc.
- Henry F.D.C. (1985) *The Design and Construction of Engineering Foundations*. Chapman and Hall.
- Tomlinson M.J. (1969) *Foundation Design and Construction*. Pitman, London.

A worked example follows which is relevant to Chapter 29.



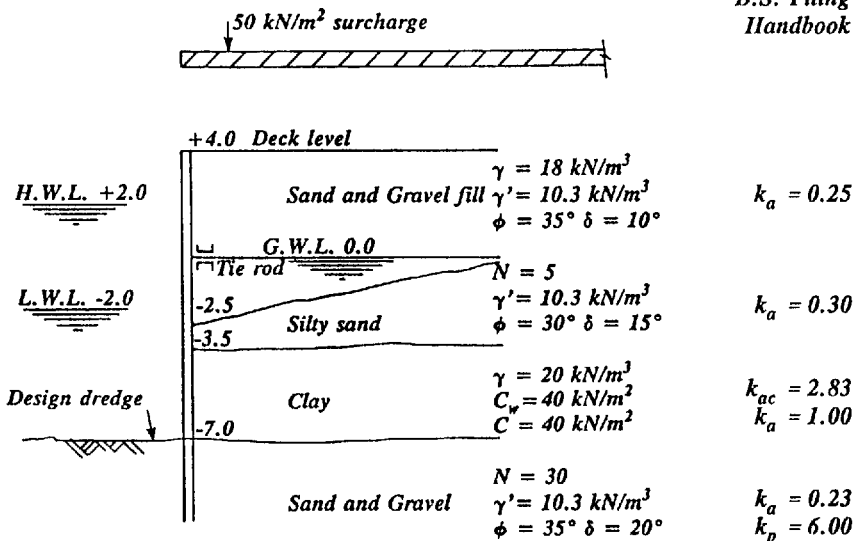
|  |   |                                   |  |
|--|---|-----------------------------------|--|
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|  |   | Design code<br><b>BS8002*</b>     | Made by <b>DW</b><br>Checked by <b>GWO</b> |

For construction of the quay wall it is proposed to use an anchored steel sheet pile wall. Fill behind wall to be dredged sand and gravel.

Crane rails will be mounted on ground beams carried on piled foundations, and on the cope beam at the head of the sheet pile wall.

**Sheet pile quay wall**


B.S. Piling Handbook




Ground water level will be related to tide level but, due to the low permeability of the sheet pile wall, will always lag behind the rising or falling tide.


Hence, assume ground water level to be at mid-tide level (+ 0.0)

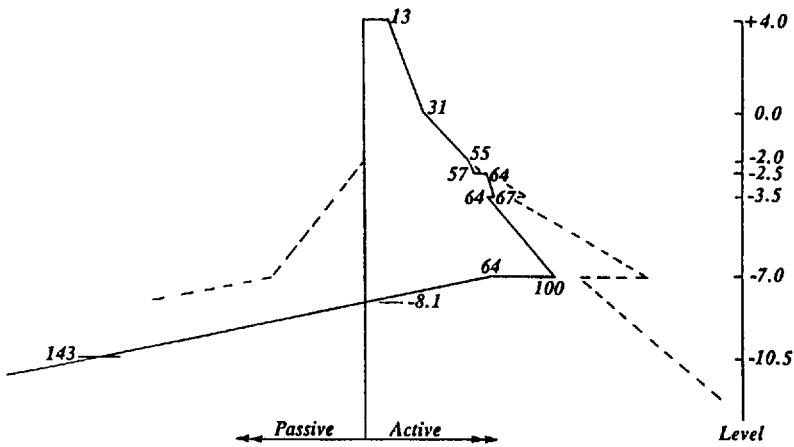
Worst tidal condition for wall design is low water (- 2.0)

|   |                                   |  |                           |
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| <p><b><u>Overburden pressures</u></b></p> <p><b>Active:</b> <span style="float: right;"><b>kN/m<sup>2</sup></b></span></p> <p><b>At +4.0 in fill</b> = 50 = 50</p> <p><b>At +0.0 in fill</b> = 50 + (4 × 18) = 122</p> <p><b>At -2.0 in fill</b> = 122 + (2 × 10.3) = 143</p> <p><b>At -2.5 in fill &amp; sand</b> = 143 + (0.5 × 10.3) = 148</p> <p><b>At -3.5 in sand</b> = 148 + (1 × 10.3) = 158</p> <p><b>At -3.5 in clay</b> = 158 + (3.5 × 9.8) = 192</p> <p><b>At -7.0 in clay</b> = 192 + (3.5 × 20) = 262</p> <p><b>At -7.0 in sand/gravel</b> = 262 - (7 × 9.8) = 193</p> <p><b>At -10.5 in sand/gravel</b> = 193 + (3.5 × 10.3) = 229</p> <p><b>Passive:</b> <span style="float: right;"><b>kN/m<sup>2</sup></b></span></p> <p><b>At -7.0</b> = 0 = 0</p> <p><b>At -10.5</b> = 3.5 × 10.3 = 36</p> <p><b><u>Active soil &amp; water pressures</u></b> <span style="float: right;"><b>kN/m<sup>2</sup></b></span></p> <p><b>At +4.0 in fill</b> = 50 × 0.25 = 13</p> <p><b>At +0.0 in fill</b> = 122 × 0.25 = 31</p> <p><b>At -2.0 in fill</b> = (143 × 0.25) + (2 × 9.8) = 55</p> <p><b>At -2.5 in fill</b> = (148 × 0.25) + (2.5 × 9.8) = 62</p> <p><b>At -2.5 in fill &amp; sand</b> = (148 × 0.30) + (2.5 × 9.8) = 69</p> <p><b>At -3.5 in sand</b> = (158 × 0.30) + (3.5 × 9.8) = 82</p> <p><b>At -3.5 in clay</b> = (192 × 1.0) - (2.83 × 40) = 79</p> |                                   |  |                           |



|   |  |   |                                      |
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|   | <p>Design code</p> <p><b>BS8002*</b></p>     | <p>Made by <b>DW</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no. <b>4</b></p>            |
| <i>kN/m<sup>2</sup></i>   |  |   |                                      |
| <i>At -7.0 in clay = (262 × 1.0) - (2.83 × 40) = 149</i>  |  |   |                                      |
| <i>At -7.0 in sand/gravel = (193 × 0.23) + (7 × 9.8) = 113</i>  |  |   |                                      |
| <i>At -10.5 in sand/gravel = (229 × 0.23) + (10.5 × 9.8) = 156</i>  |  |   |                                      |
| <u><i>Passive soil &amp; water pressures</i></u> <span style="float: right;"><i>kN/m<sup>2</sup></i></span>   |  |   |                                      |
| <i>At -2.0 in water = 0 = 0</i>   |  |   |                                      |
| <i>At -2.5 in water = 0.5 × 9.8 = 5</i>   |  |   |                                      |
| <i>At -3.5 in water = 1.5 × 9.8 = 15</i>  |  |   |                                      |
| <i>At -7.0 in water = 5 × 9.8 = 49</i>  |  |   |                                      |
| <i>At -10.5 in sand/gravel = (36 × 6) + (8.5 × 9.8) = 299</i>   |  |   |                                      |
| <u><i>Net soil &amp; water pressures</i></u> <span style="float: right;"><i>kN/m<sup>2</sup></i></span>   |  |   |                                      |
| <i>At +4.0 in fill = 13</i>   |  |   |                                      |
| <i>At +0.0 in fill = 31</i>   |  |   |                                      |
| <i>At -2.0 in fill = 55</i>   |  |   |                                      |
| <i>At -2.5 in fill = 62 - 5 = 57</i>  |  |   |                                      |
| <i>At -2.5 in silty sand = 69 - 5 = 64</i>  |  |   |                                      |
| <i>At -3.5 in silty sand = 82 - 15 = 67</i>   |  |   |                                      |
| <i>At -3.5 in clay = 79 - 15 = 64</i>   |  |   |                                      |
| <i>At -7.0 in clay = 149 - 49 = 100</i>   |  |   |                                      |
| <i>At -7.0 in sand/gravel = 113 - 49 = 64</i>   |  |   |                                      |
| <i>At -10.5 in sand/gravel = 156 - 299 = -143</i>   |  |   |                                      |

|  |   |                                   |  |
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Assume anchor level is at 0.0 level

Moment of net active pressure about 0.0


|                            |                     |          |
|----------------------------|---------------------|----------|
| $13 \times 4$              | $= 52 \times -2$    | $= -104$ |
| $18 \times 4 \times 0.5$   | $= 36 \times -1.33$ | $= -48$  |
| $31 \times 2$              | $= 62 \times 1.0$   | $= 62$   |
| $24 \times 2 \times 0.5$   | $= 24 \times 1.33$  | $= 32$   |
| $55 \times 0.5$            | $= 28 \times 2.25$  | $= 63$   |
| $2 \times 0.5 \times 0.5$  | $= 1 \times 2.33$   | $= 2$    |
| $64 \times 1$              | $= 64 \times 3.0$   | $= 192$  |
| $3 \times 1.0 \times 0.5$  | $= 2 \times 3.17$   | $= 6$    |
| $64 \times 3.5$            | $= 224 \times 5.25$ | $= 1176$ |
| $36 \times 3.5 \times 0.5$ | $= 63 \times 5.83$  | $= 367$  |
| $64 \times 1.1 \times 0.5$ | $= 35 \times 7.37$  | $= 258$  |

Total active pressure =  $\overline{591 \text{ kN}}$        $\overline{2006 \text{ kNm}}$

Design for "free earth support"

Penetration required below -8.1 level for factor of safety 1 against failure by forward movement of pile toe = x

Slope of pressure line below -8.1 =  $10.3 \times (6 - 0.23) = 59.4 \text{ kN/m}^2/\text{m}$

|   |  |   |                                      |
|---|--|---|--------------------------------------|
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|   | <p>Design code</p> <p><b>BS8002*</b></p>     | <p>Made by <b>DW</b></p> <p>Checked by <b>GWO</b></p> | <p>Sheet no.</p> <p><b>6</b></p>     |

$\therefore 59.4 \times x \times x \times 0.5 \times (0.67x + 8.1) = 2006$

$$19.9x^3 + 240.6x^2 = 2006$$

$$x = 2.6 \text{ m}$$

*Pile toe level for factor of safety 1 = -10.7*

*For factor of safety 2*

$$19.9x^3 + 240.6x^2 = 2006 \times 2$$

$$x = 3.6 \text{ m}$$

*Required actual pile toe level = -8.1 - 3.6 = -11.7* *Pile toe at -11.7*

*To find required anchor force at 0.0:*

*Moment of net active and passive pressures about and above -10.7 level*

*centre of active pressure occurs at*

$$+0.0 - \left[ \frac{2008}{592} \right] = -3.4 \text{ level}$$

$$592 \times (10.7 - 3.4) = 4322$$

$$-59.4 \times 2.6^2 \times 0.5 \times 0.87 = -175$$


$$\frac{4147}{10.7} \text{ kNm}$$

*Anchor force =  $\frac{4147}{10.7} = 388 \text{ kN/m}$*  *Anchor load = 388 kN/m*

*Depth of zero shear below -3.5 = y*

$$388 - 270 = 64x + (10.3 \times x^2 \times 0.5)$$

$$x = 1.7 \text{ m}$$

|  |   |                                   |  |                           |
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*Level of zero shear* = -5.2 m

*Moments about and above -5.2 level*

$388 \times 5.2 = 2018$

$-52 \times 7.2 = -374$

$-36 \times 6.53 = -235$

$-62 \times 4.2 = -260$

$-24 \times 3.87 = -93$

$-28 \times 2.95 = -83$

$-1 \times 2.87 = -3$

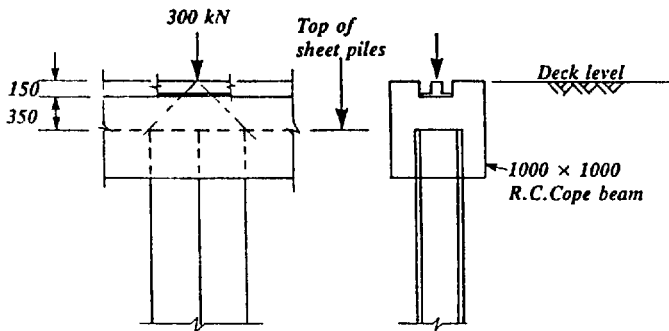
$-64 \times 2.2 = -141$

$-64 \times 1.7 \times 0.85 = -92$

$-10.3 \times 1.7^2 \times 0.5 \times 0.57 = -8$

$\therefore$  max. bending moment in pile = 729 kNm

*Axial load in sheet piles from crane*



|  |                                   |  |                           |
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load per metre run of wall

$$= \frac{300 \times 1.25}{(0.35 + 0.15) \times 2} = 375 \text{ kN}$$

Cope self-weight = 24

$$\underline{\underline{399 \text{ kN}}}$$

**SHEET PILE LOAD SUMMARY:**

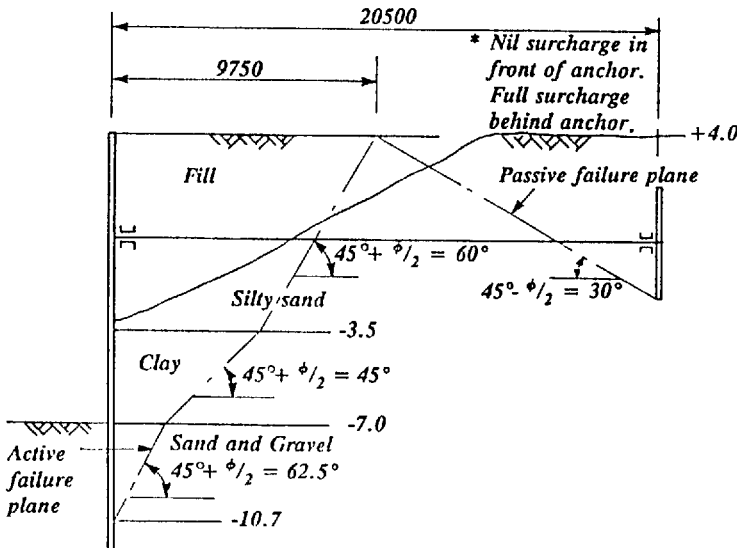
Max. axial = 399 kN/m  
 Max. bending moment = 729 kNm/m


Bearing piles supporting rear crane rail

Assume piles at 5 m centres

Max. axial load/pile = 300 crane  
 75 impact  
 120 ground beam SW  
 495 kN

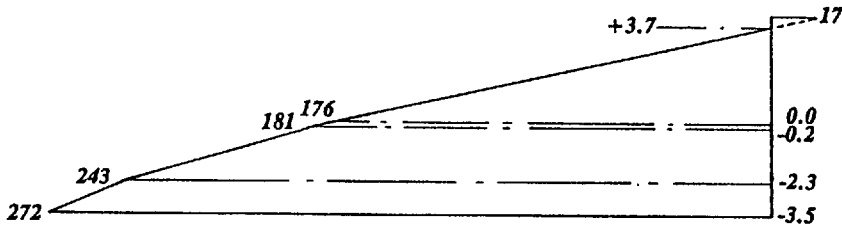
**Anchorage**



|  |   |                                   |  |
|--|---|-----------------------------------|--|
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*NB wall friction is not taken into account on anchorage soil pressures.*

$$\begin{aligned}
 p_a \text{ behind anchor at } +4.0 &= 50 \times 0.33 && = 17 \text{ kN/m}^2 \\
 p_a \text{ behind anchor at } 0.0 &= [50 + (4 \times 18)] \times 0.33 && = 40 \text{ kN/m}^2 \\
 p_a \text{ behind anchor at } -3.5 &= [122 + (3.5 \times 10.3)] \times 0.33 && = 52 \text{ kN/m}^2 \\
 p_p \text{ in front of anchor at } +4.0 &= 0 && = 0 \text{ kN/m}^2 \\
 p_p \text{ in front of anchor at } 0.0 &= (4 \times 18) \times 3 && = 216 \text{ kN/m}^2 \\
 p_p \text{ in front of anchor at } -3.5 &= [72 + (3.5 \times 10.3)] \times 3 && = 324 \text{ kN/m}^2 \\
 \text{Net } p_p \text{ in front of anchor at } +4.0 &= 0 - 17 && = -17 \text{ kN/m}^2 \\
 \text{Net } p_p \text{ in front of anchor at } 0.0 &= 216 - 40 && = 176 \text{ kN/m}^2 \\
 \text{Net } p_p \text{ in front of anchor at } -3.5 &= 324 - 52 && = 272 \text{ kN/m}^2
 \end{aligned}$$



$$\begin{aligned}
 p_p \text{ net down to } 0.0 &= 176 \times 3.7 \times 0.5 && = 325 \\
 p_p \text{ net } 0.0 \text{ to } -3.5 &= (176 + 272) \times 0.5 \times 3.5 && = 784 \\
 &&& \overline{1109 \text{ kN/m}}
 \end{aligned}$$

*Assume continuous anchor wall*

|  |                                   |  |
|--|-----------------------------------|--|
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*For factor of safety 2, required resistance/metre*

$$= 388 \times 2 = 776 \text{ kN}$$

$$\text{Required depth of anchor wall} = -3.5 + \frac{(1109 - 776)}{260 \text{ say}} = -2.3 \text{ m}$$

*∴ anchor wall toe at -2.3 m*

*Moment of passive resistance about and above -2.3 m*

$$\begin{aligned} 176 \times 3.7 \times 0.5 \times 3.53 &= 1149 \\ 176 \times 2.3 \times 1.15 &= 466 \\ 67 \times 2.3 \times 0.5 \times 0.77 &= 59 \\ \hline &1674 \text{ kNm} \end{aligned}$$

*For balanced anchor, tie level at anchor*

$$\text{tie level at anchor} = -2.3 + \frac{1674}{776} = -0.14 \text{ Allow } -0.2 \text{ m}$$

*∴ tie level at anchor = -0.2 m*

*For anchor location see calculation sheet 8*

*Anchor wall  
20.5 m  
behind front  
wall*

*(Passive and active failure planes must not intersect)*

$$\text{Top of anchor piles} = -0.2 + \left[ \frac{3.7 + 0.2}{2} \right] = +1.75 \text{ say } +1.8$$


*Anchor wall head at +1.8*

$$\text{Bending moment on anchor piles} = \frac{176 \times 3.7}{2} \times 1.43 = 466 \text{ kNm}$$


*(at 2 × working load)*

$$\begin{aligned} 179 \times 0.2 \times 0.1 &= 4 \\ \hline &470 \text{ kNm} \end{aligned}$$

$$\text{Bending moment at working load} = \frac{470}{2} = 235 \text{ kNm/m}$$

|  |                                   |  |
|--|-----------------------------------|--|
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| <p><b><u>Design of members</u></b></p> <p><b>Front wall sheet piles</b></p> <p><b>Max. bending moment = 729 kNm/m</b></p> <p><b>Axial load = 399 kN/m</b></p> <p><b>Try Larssen No. 6, ~ 25.4 mm thick, ~ BS 4360 Grade 50A</b></p> $f_{bc} = \frac{729 \times 1000}{4675} = 156 \text{ N/mm}^2$ $f_c = \frac{399 \times 10}{397} = 10 \text{ N/mm}^2$ $\frac{\ell}{r_{xx}} = \frac{10.7 \times 100}{16.1} = 66$ $p_c = 158 \times \frac{180}{230} = 123.6 \text{ N/mm}^2$ $p_{bc} = 180 \text{ N/mm}^2$ $\frac{156}{180} + \frac{10}{123.6} = 0.95 \text{ OK}$ <p><b>Use Larssen No. 6, ~ 25.4 mm thick, ~ Grade 50A, × 15.7 m long</b></p> <p><b>Anchor wall sheet piles</b></p> <p><b>Max. bending moment = 235 kNm/m</b></p> $\text{Required modulus} = \frac{235 \times 1000}{140} = 1679 \text{ cm}^3/\text{m}$ <p><b>(BS 4360 Grade 43A)</b></p> <p><b>Use Larssen 20W Grade 43A × 4.3 m long</b></p> |                                   |  |



|  |                                   |  |                           |
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**Bearing piles - centres to match tie rods**

**Load = 495 kN**

**Piles are fully embedded, full lateral support from soil, effective length is zero.**

**$p_c = 30\% \text{ yield stress} = 85 \text{ N/mm}^2 \sim \text{Grade 43A}$**

**Area required =  $\frac{495 \times 1000}{85 \times 100} = 58.2 \text{ cm}^2$**

**Use 254 × 254 × 63 UBP BS 4360 Grade 43A**

**Pile length (using Meyerhof)**

**End resistance in sand and gravel**

**=  $400 \times 30 \times 0.67 \times 0.25^2 = 502 \text{ kN}$**

**Shaft resistance in silty sand**

**=  $2 \times 5 \times 0.25 \times 4 \times 7.5 = 75 \text{ kN}$**

**Shaft resistance in clay**

**=  $0.7 \times 40 \times 0.25 \times 4 \times 3.5 = 98 \text{ kN}$**


**Shaft resistance in sand and gravel**

**=  $2 \times 30 \times 0.67 \times 0.25 \times 4 = 40 \text{ kN/m}$**

**For factor of safety 2, penetration required below -7.8 level**

**=  $\frac{(495 \times 2) - (502 + 75 + 98)}{40} = 7.9 \text{ m}$**       **Pile toe level -15.0**

**Pile length = 18.5 m**

|  |                                   |  |                           |
|--|-----------------------------------|--|---------------------------|
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Walings - front wall and anchor wall

Assume tie rods at 6 pile centres (2.52 m)

$$\text{Bending moment in wales} = \frac{388 \times 2.52^2}{12} = 205 \text{ kNm}$$

$$\text{Required modulus} = \frac{205 \times 1000}{165} = 1242 \text{ cm}^3$$

Use 2/381 × 102 × 55.1 RSC's - Grade 43A

$$\text{Web shear} = \frac{397 \times 1.26}{2} = 250 \text{ kN OK}$$

Tie bars

$$\text{Load per tie} = 388 \times 2.52 = 978 \text{ kN}$$

Use 2/75φ bars BS 4360 Grade 50B (rolled threads) × 21.1 m long, - inc. 1/turnbuckle & 1/coupler

2/75φ  
Grade 50B  
@ 200c/c

Bearing plates 400 × 200 × 30 Grade 43A

Anchor bolts

$$\text{Load per bolt} = 388 \times 0.42 \times 2 = 326 \text{ kN}$$

Use 60φ bolt BS 4360 Grade 50B (rolled threads) × 0.55 long

60φ  
Grade 50B

Washer plates 180 × 180 × 30 Grade 43A

Bearing plates 180 × 180 × 30 Grade 43A

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Subject  
**QUAY FACILITIES**

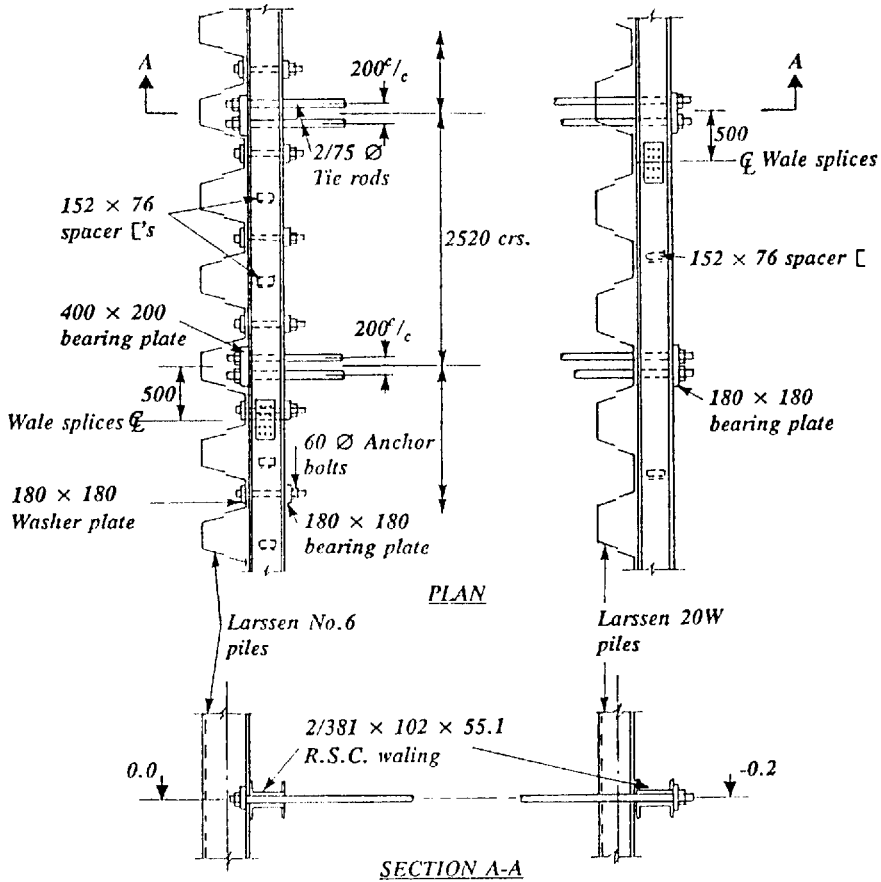
Design code  
**BS8002\***

Made by  
**DW**

Checked by  
**GWO**

Chapter ref.  
**29**

Sheet no. **14**



**TIE ROD & WALING DETAILS**

# Chapter 30

# Floors and orthotropic decks

by DICK STAINSBY

## 30.1 Steel plate floors

Steel plate used for floors, walkways or for staircase treads normally has a raised pattern of the non-slip type such as 'Durbar plate' supplied by British Steel. Where a plated area will have only occasional use, such as walkways for maintenance access, then plain plate may be used.

If properly designed, both plain and non-slip plates have a dual function in carrying floor loads and in acting as a horizontal diaphragm in place of a separate bracing system. For example, a plate may be connected to the top flange of crane gantry girders to act as a surge girder and also as a means of crane or maintenance access.

When steel plate floors are in situations where moisture or high humidity is present, then the plates should be continuously welded to the support members to avoid corrosion problems. In dry areas connections may be fastened by bolting with countersunk bolts, intermittent welds, or clips. When clips are used they must be arranged so that they cannot move out of position.

Plain plate is commonly available in grades 430B and 510B to BS EN 10025.

**Table 30.1** Plain plate

|                           |      |      |      |      |      |      |     |
|---------------------------|------|------|------|------|------|------|-----|
| Thickness (mm)            | 3    | 4.5  | 6    | 8    | 10   | 12.5 | 15  |
| Mass (kg/m <sup>2</sup> ) | 23.6 | 35.3 | 47.1 | 62.8 | 78.5 | 98.1 | 118 |

### *Durbar plate*

The pattern of Durbar plate is shown in Fig. 30.1. The pattern is raised 1.5 mm to 2.2 mm above the plate surface. When ordering, the thickness should be specified as 'thickness on plain'.

**Table 30.2** Durbar plate

|                           |      |      |      |      |      |      |
|---------------------------|------|------|------|------|------|------|
| Thickness on plain (mm)   | 3    | 4.5  | 6    | 8    | 10   | 12.5 |
| Mass (kg/m <sup>2</sup> ) | 24.9 | 36.9 | 48.7 | 64.4 | 80.1 | 99.7 |

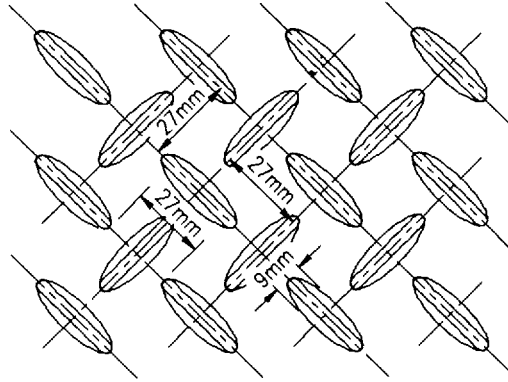


Fig. 30.1 Durbar plate

Durbar-pattern plate is free draining and can be matched width to length without affecting appearance.

Table 30.3 Recommended standard sizes for Durbar plate

|            |               |      |      |                          |      |      |      |
|------------|---------------|------|------|--------------------------|------|------|------|
| Width (mm) | 600           | 1000 | 1000 | 1250                     | 1500 | 1750 | 1830 |
| Length (m) | 2.0, 2.5, 3.0 |      |      | Any between 1.8 and 12.0 |      |      |      |

Durbar plate is commonly available in grade 430B and 510B to BS EN 10025, also ‘commercial quality’ with a UTS not less than 355 N/mm<sup>2</sup>.

### 30.1.1 Design of plates simply supported on four edges

This condition is for plates resting on four edges or attached by clips or tack welds only to supporting members. Plates supported on two edges, but with stiffeners in the other direction, can also be considered as simply supported on four edges.

#### (1) Uniform distributed loading

The design may be made using Pounder’s plate theory.

$$w = \frac{4p_y t^2}{3k B^2 \left[ 1 + \frac{14}{75} (1 - k) + \frac{20}{57} (1 - k)^2 \right]}$$

$$d = \frac{m^2 - 1}{m^2} \times \frac{5k w B^4}{32 \gamma_t E t^3} \left[ 1 + \frac{37}{175} (1 - k) + \frac{79}{201} (1 - k)^2 \right]$$

where  $w$  = uniformly distributed load on plate (ultimate) (N/mm<sup>2</sup>)  
 $d$  = maximum deflection (mm), occurring at serviceability

$$\frac{1}{m} = \text{Poisson's ratio } (m = 3)$$

$$L = \text{length of plate (mm)} \quad (L > B)$$

$$B = \text{breadth of plate (mm)}$$

$$t = \text{thickness of plate (mm)}$$

$$k = \left( \frac{L^4}{L^4 + B^4} \right)$$

$$p_y = \text{yield stress of plate (N/mm}^2\text{)}$$

$$E = \text{Young's modulus } 205 \times 10^3 \text{ (N/mm}^2\text{)}$$

$$\gamma_f = \text{load factor}$$

This formula, which is the basis of the first two load tables in the Appendix *Floor plate design tables*, assumes that there is no resistance to uplift in plate corners. Where such resistance is provided, higher design strength may be obtained by using References 1 or 2.

(2) Centre point loads (concentrated over a small circle of radius  $r$ )

The design may be made using formulae developed by Roark.<sup>1</sup>

*NB* There is a small amount of uplift (negative load) on the corners of the plate when design is made using the following formula. Fastening at each corner must be able to resist an uplift of 6% of the centre point load.

$$W = \frac{0.67\pi p_y t^2}{\left(1 + \frac{1}{m}\right) \ln \frac{2B}{\pi r} + \beta}$$

$$d = \frac{\alpha W B^2}{\gamma_f E t^3}$$

where  $W$  = concentrated load (ultimate) (N)

$d$  = maximum deflection (mm), occurring at serviceability

$L$  = length of plate (mm) ( $L > B$ )

$B$  = breadth of plate (mm)

$t$  = thickness of plate (mm)

$p_y$  = yield stress of plate (N/mm<sup>2</sup>)

$E$  = Young's modulus  $205 \times 10^3$  (N/mm<sup>2</sup>)

$\frac{1}{m}$  = Poisson's ratio ( $m = 3$ )

$r$  = radius of contact for a load concentrated on a small area (mm)

$\ln$  = natural logarithm of ( $2B/\pi r$ )

$\gamma_f$  = load factor

**Table 30.4** Values of  $\beta$  and  $\alpha$  for centre point loads on simply supported plates

| $L/B$    | 1.0    | 1.2    | 1.4    | 1.6    | 1.8    | 2.0    | $\infty$ |
|----------|--------|--------|--------|--------|--------|--------|----------|
| $\beta$  | 0.435  | 0.650  | 0.789  | 0.875  | 0.972  | 0.958  | 1.0      |
| $\alpha$ | 0.1267 | 0.1478 | 0.1621 | 0.1715 | 0.1770 | 0.1805 | 0.1851   |

### 30.1.2 Design of plates fixed on four edges

The plates must be secured by continuous bolting or welding which will achieve the fixed condition and prevent uplift which would otherwise occur at the plate corners.

(1) Uniformly distributed loading

The design may be made using Pounder's plate theory.

$$w = \frac{2p_y t^2}{kB^2 \left[ 1 + \frac{11}{35} (1 - k) + \frac{79}{141} (1 - k)^2 \right]}$$

$$d = \frac{m^2 - 1}{m^2} \times \frac{kWB^4}{32\gamma_f Et^3} \left( 1 + \frac{47}{210} (1 - k) + \frac{200}{517} (1 - k)^2 \right)$$

where  $L$  = length of plate (mm) ( $L > B$ )

$B$  = breadth of plate (mm)

$t$  = thickness of plate (mm)

$$k = \left( \frac{L^4}{L^4 + B^4} \right)$$

$p_y$  = yield stress of plate (N/mm<sup>2</sup>)

$w$  = uniformly distributed load on plate (ultimate) (N/mm<sup>2</sup>)

$E$  = Young's modulus  $205 \times 10^3$  (N/mm<sup>2</sup>)

$\frac{1}{m}$  = Poisson's ratio ( $m = 3$ )

$d$  = maximum deflection (mm), occurring at serviceability

$\gamma_f$  = load factor

This formula is the basis of the third load table in the Appendix *Floor plate design tables*.

(2) Centre point loads (concentrated over a small circle of radius  $r$ )

The design may be made using formulae developed by Roark.<sup>1</sup>

$$W = \frac{0.67\pi p_y t^2}{\left(1 + \frac{1}{m}\right) \ln \frac{2B}{\pi r} + \beta_1} \quad \text{OR} \quad \frac{p_y t^2}{\beta_2}$$

whichever is the lesser, where

$$d = \frac{\alpha WB^2}{\gamma_f Et^3}$$

$W$  = concentrated load (ultimate) (N)

$d$  = maximum deflection (mm), occurring at serviceability

$L$  = length of plate (mm) ( $L > B$ )

$B$  = breadth of plate (mm)

$t$  = thickness of plate (mm)

$p_y$  = yield stress of plate (N/mm<sup>2</sup>)

**Table 30.5** Values of  $\beta_1$ ,  $\beta_2$  and  $\alpha$  for centre point loads on fixed plates

| $L/B$     | 1.0    | 1.2    | 1.4    | 1.6    | 1.8    | 2.0    | $\infty$ |
|-----------|--------|--------|--------|--------|--------|--------|----------|
| $\beta_1$ | -0.238 | -0.078 | 0.011  | 0.053  | 0.068  | 0.067  | 0.067    |
| $\beta_2$ | 0.7542 | 0.8940 | 0.9624 | 0.9906 | 1.000  | 1.004  | 1.008    |
| $\alpha$  | 0.0611 | 0.0706 | 0.0754 | 0.0777 | 0.0786 | 0.0788 | 0.0791   |

$E$  = Young's modulus  $205 \times 10^3$  (N/mm<sup>2</sup>)

$\frac{1}{m}$  = Poisson's ratio ( $m = 3$ )

$r$  = radius of contact for a load concentrated on a small area (mm)

$\ln$  = natural logarithm of  $\frac{2B}{\pi r}$

$\gamma_f$  = load factor

### 30.1.3 Design criteria

#### *Imposed loading*

Walkway loading is specified in British Standard BS 6399: Part 1 *Loading for buildings*. Table 30.6 is an extract from table 10 dealing with workshops and factories.

Horizontal loading applied to handrailing should be taken as the following applied at 1.1 m above the walkway (irrespective of the handrail height):

|   |           |
|---|-----------|
| General duty – regular two-way pedestrian traffic           | 0.36 kN/m |
| Heavy duty – high-density pedestrian traffic: escape routes | 0.74 kN/m |
| Potentially crowded areas over 3 m wide                     | 3.00 kN/m |

(See also BS 5395: Part 3, *Code of practice for industrial type stairs, permanent ladders and walkways* and BS 6180, *Code of practice for protective barriers in and above buildings*.)

#### *Load factors*

When designing to BS 5950: Part 1, the load factors in Table 30.7 should be used.



**Table 30.6** Extract from table 10 of BS 6399: Part 1

| Floor area usage                           | Intensity of distribution (kN/m <sup>2</sup> ) | Concentrated load (kN) |
|--|--|------------------------|
| Factories, workshops and similar buildings | 5.0  | 4.5                    |
| Access hallways, stairs and footbridges    | 4.0  | 4.5                    |
| Factories, workshops and similar buildings | 5.0  | 4.5                    |
| Cat walks                                  | —  | 1 kN @ 1 m centres     |

**Table 30.7** Load factors

| Loading                        | Factor |
|--------------------------------|--------|
| Dead load                      | 1.4    |
| Vertical load                  | 1.6    |
| Horizontal load                | 1.6    |
| Vertical & horizontal combined | 1.4    |

### Deflection

Deflection of floor plating under the action of dead and imposed loads should not exceed  $B/100$ , where  $B$  is the minimum spanning dimension of the plate.

## 30.2 Open-grid flooring

Open-grid proprietary systems are often the economical solution for industrial flooring and walkways particularly where ventilation or light must be available through the flooring. They are generally available in spans up to 2.0 metres, but can be supplied to span 4.0 metres. The design allows spanning in one direction only. Stair treads are also available. (See Fig. 30.2.)

Open-grid systems are usually manufactured in grade 430 steel, with painted or galvanized finish. Aluminium and stainless steel types are also available. Load-carrying capacities and fixing details are readily available from suppliers' catalogues.

Open-grid flooring is manufactured in accordance with BS 4592: *Industrial type metal flooring, walkways and stair treads*. It has the following parts:

BS 4592: Part 1: 1987, *Specification for open bar gratings*

BS 4592: Part 2: 1987, *Specification for expanded metal grating panels*

BS 4592: Part 3: 1987, *Specification for cold formed planks*.

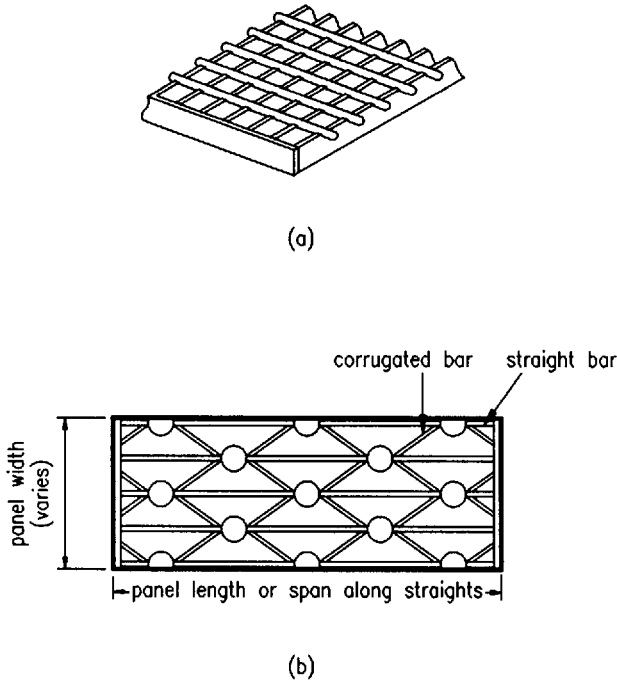


Fig. 30.2 Open grid flooring. (a) Open bar; (b) diamond pattern; (c) expanded metal; (d) Q-grating

### *Names and addresses of suppliers of open-grid flooring*

William Sharp Ltd, Bescot Crescent, Walsall WS1 4NE. Tel: 0922 27531, Fax 0922 23894

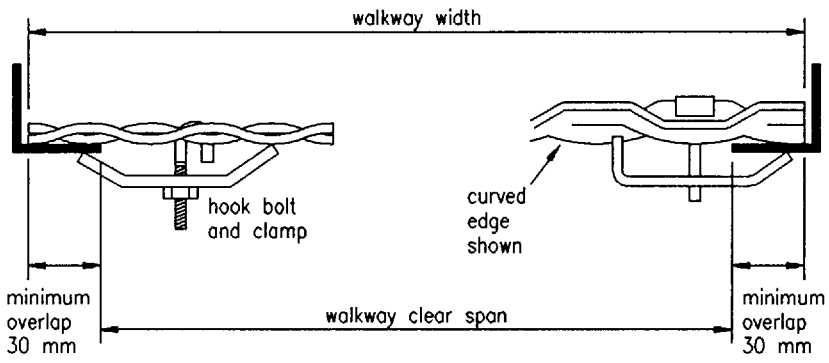
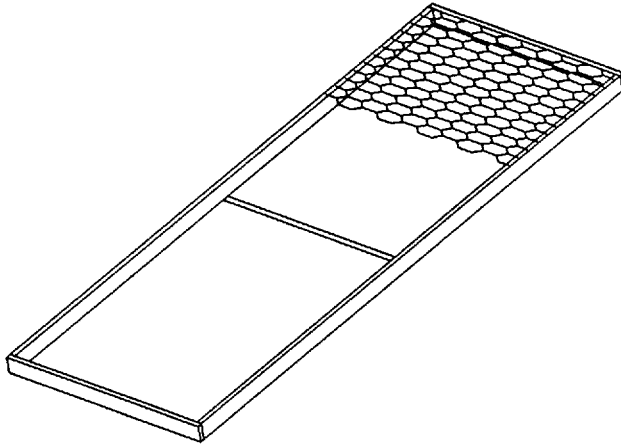
Steelway-Fensecure (Glynwed Engineering Ltd), Queensgate Works, Bilston Road, Wolverhampton, West Midlands, WV2 2NJ. Tel: 0902 451733, Fax 0902 452256

Lionweld Kennedy Ltd, Marsh Road, Middlesbrough, Cleveland TS1 5JS. Tel: 0642 245151, Fax 0642 224710

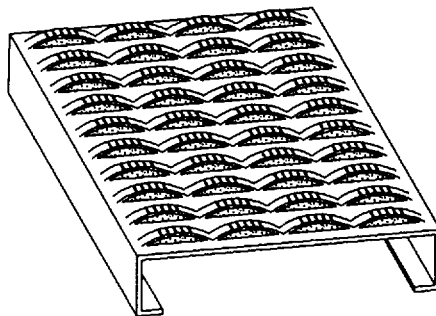
Expanded Metal Co. Ltd, Longhill Industrial Estate (North), Hartlepool, Cleveland TS25 1PR. Tel: 0429 867388, Fax 0429 866795

### **30.3 Orthotropic decks**

Orthotropic decks first came into regular use for long-span bridges in the 1950s. They replaced the earlier battle deck system where steel plates were supported on an independent grillage of steel plates.



(c)



(d)

Fig. 30.2 continued

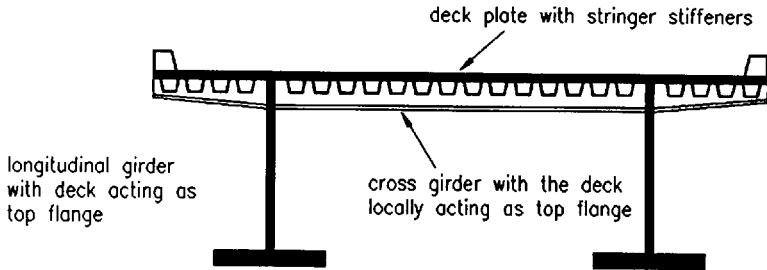


Fig. 30.3 Section through orthotropic deck

In the orthotropic system a stiffened plate deck is integral with the support members which together form the primary members of the bridge. A typical orthotropic bridge system is shown in Fig. 30.3.

All steel orthotropic decks are used when the dead weight of the bridge must be reduced to a minimum. They are therefore ideally suited to long-span bridges with single spans exceeding 120 metres, and are usually incorporated in suspension and cable-stayed bridges. Other applications are for bridges with moving or lifting spans.

It should be noted that for short-span bridges, steel/concrete composite decks are generally more economic than orthotropic decks. A composite deck of depth 250 mm will be three to four times the mass of an orthotropic deck but may be only one-third of the cost.

A typical orthotropic deck consists of a 12–15 mm plate stiffened with longitudinal stringers spaced at about 300 mm, intersecting with deeper transverse cross girders. Stringers are of the closed or open type.

### *Closed stringers*

The closed, torsionally stiff, stringers are formed as a 'vee' or a 'trough' and are rolled or pressed from plate of 6–10 mm thickness. They provide the lightest overall weight since they distribute heavy wheel loads most effectively between the members. Welding to the floor plates has been made with fillet or butt welds, but fatigue cracking of welds on closed section stringers has occurred on some bridges. This has been attributed to lack of penetration on the inaccessible side of the weld. Full penetration butt welds are now generally adopted but they are expensive and difficult to achieve. Closed stringers may be made in short lengths to fit between the cross girders or preferably longer lengths, slotted through to achieve a better fatigue life (Fig. 30.4).

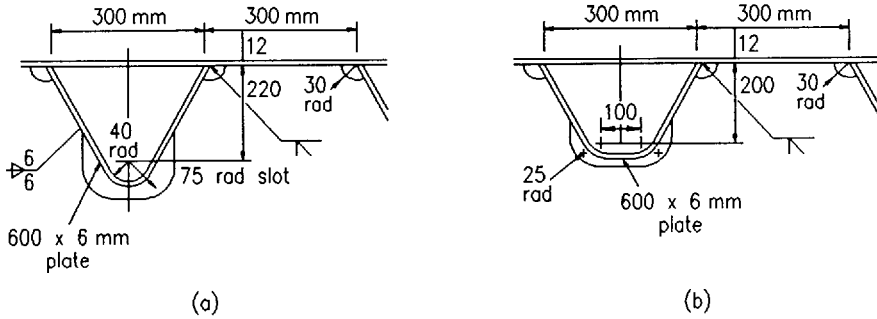


Fig. 30.4 Typical closed-section stringers: (a) vee trough; (b) trapezoidal trough

### Open stringers

Open-section, torsionally weak, stringers may be formed from flats, bulb flats or angles. A slightly greater dead weight results because the transverse distributive properties are less efficient than with closed stringers. However, the advantage is that welds to the floor plate can be made from both sides and take the form of fillet welds. Transverse bending stresses between the stringer and floor plate are far less severe than with closed section stiffeners, such that this form is far less fatigue sensitive. Again, the best fatigue performance is achieved when the stringers are slotted through the cross girders. Open-section stringers are suitable for many bridges including lifting or moving structures, railway bridges and footbridges (Fig. 30.5).

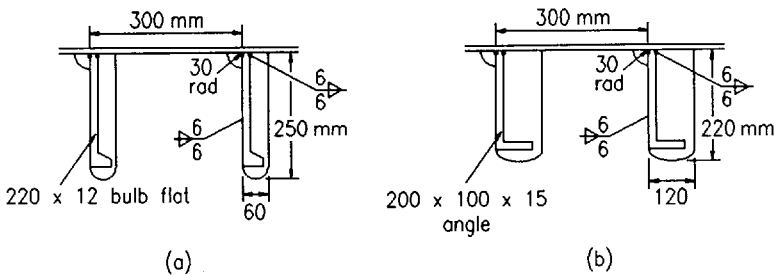


Fig. 30.5 Typical open-section stringers: (a) bulb flat; (b) angle

*Loading, analysis and design*

For loading to bridges reference should be made to BS 5400: Part 2: *Specification for loads*.

An analysis to take account of the distribution of point loads and partially distributed loads is best achieved with a bridge deck computer program, but hand methods of creating an 'influence surface' for moment and shears are available (see References 3 and 4).

Design should be made in accordance with BS 5400: Part 3: *Code of practice for design of steel bridges*. Fatigue considerations for bridgework are generally covered by BS 5400: Part 10: *Code of practice for fatigue*. It does not specifically deal with orthotropic decks for which it is necessary to consult research papers.<sup>5</sup>

**References to Chapter 30**

1. Young W.C. (1965) *Roark's Formulas for Stress and Strain*, 6th edn. McGraw-Hill, New York.
2. Timoshenko S. & Weinowsky-Krieger S. (1959) *Theory of Plates and Shells*, 2nd edn. McGraw-Hill, New York.
3. Pucher A. (1973) *Influence Surfaces of Elastic Plates*, 4th edn. Springer-Verlag, New York.
4. Dowling P. & Bawa A.S. (1975) Influence surfaces for orthotropic decks. *Proc. Instn Civ. Engrs*, **59**, Mar., 149–68.
5. Cunningham J.R. (1982) *Steel Bridge Decks, Fatigue Performance of Joints Between Longitudinal Stiffeners*. LR 1066, Transport and Road Research Laboratory, Crowthorne, Berks.

# Chapter 31

## Tolerances

by COLIN TAYLOR

### 31.1 Introduction

#### 31.1.1 Why set tolerances?

Compared to other structural materials, steel (and aluminium) structures can be made economically to much closer tolerances. Compared to mechanical parts, however, it is neither economic nor necessary to achieve extreme accuracy.

There are a number of distinct reasons why tolerances may need to be considered. It is important to be quite clear which actually apply in any given case, particularly when deciding the values to be specified, or when deciding the actions to be taken in cases of non-compliance.

**Table 31.1** Reasons for specifying tolerances

---

|                       |   |
|-----------------------|---|
| Structural safety     | Dimensions (particularly of cross-sections, straightness, etc.) associated with structural resistance and safety of the structure.  |
| Assembly requirements | Tolerances necessary to enable fabricated parts to be put together.   |
| Fit-up                | Requirements for fixing non-structural components, such as cladding panels, to the structure.   |
| Interference          | Tolerances to ensure that the structure does not foul with walls, door or window openings or service runs, etc.   |
| Clearances            | Clearances necessary between structures and moving parts, such as overhead travelling cranes, elevators, etc. or for rail tracks, and also between the structure and fixed or moving plant items. |
| Site boundaries       | Boundaries of sites to be respected for legal reasons. Besides plan position, this can include limits on the inclination of outer faces of tall buildings.  |
| Serviceability        | Floors must be sufficiently flat and even, and crane gantry tracks etc. must be accurately aligned, to enable the structure to fulfil its function.   |
| Appearance            | The appearance of a building may impose limits on verticality, straightness, flatness and alignment, though generally the tolerance limits required for other reasons will already be sufficient. |

---

The various reasons for specifying tolerances are outlined in Table 31.1. In all cases no closer tolerances than are actually needed should normally be specified, because while additional accuracy may be achievable, it generally increases the costs disproportionately.

### 31.1.2 Terminology

'Tolerance' as a general term means a permitted range of values. Other terms which need definition are given in Table 31.2.

**Table 31.2** Definitions – deviations and tolerances

|                     |   |
|---------------------|---|
| Deviation           | The difference between a specified value and the actual measured value, expressed vectorially (i.e. as a positive or negative value). |
| Permitted deviation | The vectorial limit specified for a particular deviation.   |
| Tolerance range     | The sum of the absolute values of the permitted deviations each side of a specified value.  |
| Tolerance limits    | The permitted deviations each side of a specified value, e.g. $\pm 3.5$ mm or $+5$ mm $-0$ mm.  |

### 31.1.3 Classes of tolerance

Table 31.3 defines the three classes of tolerances which are recognized in Eurocode 3.

**Table 31.3** Classes of tolerances

|                       |   |
|-----------------------|---|
| Normal tolerances     | Those which are generally necessary for all buildings. They include those normally required for structural safety, together with normal structural assembly tolerances.   |
| Particular tolerances | Tolerances which are closer than normal tolerances, but which apply only to <i>certain</i> components or only to <i>certain</i> dimensions. They may be necessary in specific cases for reasons of fit-up or interference or in order to respect clearances or boundaries.  |
| Special tolerances    | Tolerances which are closer than normal tolerances, and which apply to a <i>complete</i> structure or project. They may be necessary in specific cases for reasons of serviceability or appearance, or possibly for special structural reasons (such as dynamic or cyclic loading or critical design criteria), or for special assembly requirements (such as interchangeability or speed of assembly). |



It is important to draw attention to any particular or special tolerances when calling for tenders, as they usually have cost implications. Where nothing is stated, fabricators will automatically assume that only normal tolerances are required.

### 31.1.4 Types of tolerances

For structural steel there are three types of dimensional tolerance:

- (1) *Manufacturing tolerances*, such as plate thickness and the dimensions of rolled sections.
- (2) *Fabrication tolerances*, applicable in the workshops.
- (3) *Erection tolerances*, relevant to work on site.

Manufacturing tolerances are specified in standards such as BS 4, BS 4360, BS 4848, BS EN 10029 and various other BS EN standards currently in draft form. Only fabrication and erection tolerances will be covered here.

## 31.2 Standards

### 31.2.1 Relevant documents

The standards covering tolerances applicable to building steelwork are:

- (1) BS 5950 *Structural use of steelwork in building*.  
Part 2: *Specification for materials fabrication and erection: hot rolled sections*.  
Part 7: *Specification for materials and workmanship: cold formed sections and sheeting*.
- (2) *National structural steelwork specification for building construction* NSSS, 2nd edition.
- (3) Draft CEN TC 135 standard *Execution of steel structures: Part 1: General rules and rules for buildings*.
- (4) BS 5606 *Guide to accuracy in building*.

### 31.2.2 BS 5950 *Structural use of steelwork in building*

The specification of tolerances for building steelwork was first introduced into British Standards in BS 5950: Part 2: 1985. Only a limited amount of information could be agreed for inclusion at that time. This has since been supplemented in respect of cold formed steelwork by Part 7.

### **31.2.3 National structural steelwork specification (NSSS)**

The limitations of the tolerances specified in BS 5950: Part 2 have been extended by an extensive coverage of tolerances in the *National structural steelwork specification for building construction*, 2nd edition.

### **31.2.4 Draft CEN TC 135 standard *Execution of steel structures***

As part of the harmonization of construction standards in Europe, a draft has been produced for Part 1: *General rules and rules for buildings*. When the final version of this is issued as a European Standard (with a BS EN number) it will supersede BS 5950: Parts 2 and 7.

This document includes comprehensive recommendations for both erection and manufacturing tolerances. To a large extent these recommendations are consistent with BS 5950: Part 2 and the NSSS. However, some of them are more detailed.

### **31.2.5 BS 5606 *Guide to accuracy in building***

BS 5606 is concerned with buildings generally and is not specific to steelwork. The 1990 version has been rewritten as a Guide, following difficulties due to incorrect application of the previous (1978) version which was in the form of a Code.

BS 5606 is not intended as a document to be simply called up in a contract specification. It is primarily addressed to designers to explain the need for them to include means for adjustment, rather than to call for unattainable accuracy of construction. Provided that this advice is heeded, its tables of 'normal' accuracy can then be included in specifications, except where they conflict with overriding structural requirements. This can in fact happen, so it is important to remember that the requirements of BS 5950, or its BS EN successor, must always take precedence over BS 5606.

BS 5606 introduces the idea of 'characteristic accuracy', the concept that any construction process will inevitably lead to deviations from the target dimensions, and its objective is to advise designers on how to avoid resulting problems on site by appropriate detailing. The emphasis in BS 5606 is on the practical tolerances which will normally be achieved by good workmanship and proper site supervision. This can only be improved upon by adopting intrinsically more accurate techniques, which are likely to incur greater costs. These affect the fit-up, the boundary dimensions, the finishes and the interference problems. Data are given on the normal tolerances (to be expected and catered for in detailed design) under two headings:

- (1) Site construction (table 1 of BS 5606).
- (2) Manufacture (table 2 of BS 5606).

Unfortunately many of the values for site construction of steelwork are only estimated. No specific consideration is given in BS 5606 to dimensional tolerances necessary to comply with the assumptions inherent in structural design procedures, which may in fact be more stringent. It does however recognize that special accuracy may be necessary for particular details, joints and interfaces.

Another important point mentioned in BS 5606 is the need to specify methods of monitoring compliance, including methods of measurement. It has to be recognized that methods of measurement are also subject to deviations; for the methods necessary for monitoring site dimensions, these measurement deviations may in fact be quite significant compared to the permitted deviations of the structure itself.

### **31.3 Implications of tolerances**

#### **31.3.1 Member sizes**

##### ***31.3.1.1 Encasement***

The tolerances on cross-sectional dimensions have to be allowed for when encasing steel columns or other members, whether for appearance, fire resistance or structural reasons. It should not be forgotten that the permitted deviations represent a further variation over and above the difference between the serial size and the nominal size.

For example, a  $356 \times 406 \times 235$  UC has a nominal size of 381 mm deep by 395 mm wide, but with tolerances to BS 4 may actually measure 401 mm wide by 387 mm deep one side, and have a depth of 381 mm the other side. The same is true of continental sections. A  $400 \times 400 \times 237$  HD also has a nominal size of 381 mm deep by 395 mm wide, but with tolerances to Euronorm 34 may actually measure 398 mm wide by 389 mm deep one side, and have a depth of 380 mm the other side.

##### ***31.3.1.2 Fabrication***

Variations of cross-sectional dimensions (with permitted deviations) may also need to be allowed for, either in detailing the workmanship drawings or in the fabrication process itself, if problems are to be avoided during erection on site.

The most obvious case is a splice between two components of the same nominal size, where packs may be needed before the flange splice plates fit properly,

unless the components are carefully matched. Similarly variations in the depths of adjacent crane girders or runway beams may necessitate the provision of packs, unless the members are carefully matched.

Less obviously, if the sizes of columns vary, the lengths of beams connected between them will need some form of adjustment, even if the columns are accurately located and the beams are exactly to length.

### **31.3.2 Attachment of non-structural components**

It is good practice to ensure that all other items attached to the steel frame have adequate provision for adjustment in their fixings to cater for the effects of all steelwork tolerances, plus an allowance for deviations in their own dimensions. Where necessary, further allowances may be needed to cater for structural movements under load and for differential expansion due to temperature changes.

Where possible, the number of fixing points should be limited to three or four, only one of which should be positive with all the others having slotted holes or other means of adjustment.

### **31.3.3 Building envelope**

It must be appreciated that erection tolerances, including variation in the position of the site grid lines, will affect the exact location of the external building envelope relative to other buildings or to site boundaries, and there may be legal constraints to be respected which will have to be taken into account at the planning and preliminary stages of design.

These effects also need to be taken into account where a building is intended to have provision for future extension or where the project is an extension of an existing building, in which case deviations in the actual dimensions have to be catered for at the interface.

In the case of tall multi-storey buildings, the building envelope deviates increasingly with height compared to the location at ground level, even though permitted deviations for column lean generally reduce with height. Unless there are step-backs or other features with a similar effect, it may be necessary to impose particular tolerance limits on the outward deviations of the columns.

### **31.3.4 Lift shafts for elevators**

The deviations from verticality that can be tolerated in the construction of guides for 'lifts' or elevators are commonly more stringent than those for the construction of the building in which they operate. In low-rise buildings sufficient adjustment can

be provided in association with the clearances, but in tall buildings it becomes necessary either to impose 'special' tolerances on column verticality or else to impose 'particular' tolerances on those columns bounding the lift shaft.

In agreeing the limits to be observed with the lift supplier, it should not be overlooked that the horizontal deflections of the building due to wind load also have implications for the verticality of the lift shafts.

## **31.4 Fabrication tolerances**

### **31.4.1 Scope of fabrication tolerances**

The description 'fabrication tolerances' is used here to include tolerances for all normal workshop operations except welding. It thus covers tolerances for:

- (1) cross sections, other than rolled sections,
- (2) member length, straightness and squareness,
- (3) webs, stiffened plates and stiffeners,
- (4) holes, edges and notches,
- (5) bolted joints and splices,
- (6) column baseplates and cap plates.

However tolerances for cross sections of rolled sections and for thicknesses of plates and flats are treated as manufacturing tolerances. Welding tolerances (including tolerances on weld preparations and fit-up and sizes of permitted weld defects) are treated elsewhere.

### **31.4.2 Relation to erection tolerances**

An overriding requirement for accuracy of fabrication must always be to ensure that it is possible to erect the steelwork within the specified erection tolerances.

Due to the wide variety of steel structures and the even wider variety of their components, any recommended tolerances must always be specified in a very general way. Even if it were possible to specify fabrication tolerances in such a way that their cumulative effect would always permit the specified erection tolerances to be satisfied, the resulting permitted deviations would be so small as to be unreasonably expensive, if not impossible, to achieve.

Fortunately in most cases it is possible to rely on the inherent improbability of all unfavourable extreme deviations occurring together. Also the usually accepted values for fabrication tolerances do make some limited allowances for the need to avoid cumulative effects developing on site. They are tolerances that have been shown by experience to be workable, provided that simple means of adjustment are incorporated where the effects of a number of deviations could otherwise

become cumulative. For example, beams with bolted end cleats usually have sufficient adjustment available due to hole clearances, but where a line of beams all have end plate connections, provision for packing at intervals may be advisable, unless other measures are taken to ensure that the beams are not all systematically over-length or under-length by the normal permitted deviation. Other possible means for adjustment include threaded rods and slotted holes.

Where it can be seen from the drawings that the fabrication tolerances could easily accumulate in such a way as to create a serious problem in erection, either closer tolerances or means of adjustment should be considered; however the coincident occurrence of all extreme deviations is highly improbable, and judgement should be exercised both on the need for providing means of adjustment and on the range of adjustment to be incorporated.

### **31.4.3 Full contact bearing**

#### ***31.4.3.1 Application***

The requirements for contact surfaces in joints which are required to transmit compression by 'full contact bearing' probably cause more trouble than any other item in a fabrication specification, largely due to misapprehension of what is actually intended to be achieved.

First it is necessary to be clear about the kind of joint to which the requirements for full contact bearing should be applied. Figure 31.1(a) shows the normal case, where the profile of a member is required to be in full contact bearing on a baseplate or cap plate or division plate. The stress on the contact area equals the stress in the member, thus full contact is needed to transmit this stress from the member into the plate. Only that part of the plate in contact with the member need satisfy the full contact bearing criteria, though it may be easier to prepare the whole plate.

Figure 31.1(b) shows two end plates in simple bearing. The potential contact area is substantially larger than the cross-sectional area of the member, thus full contact bearing is not necessary. All that is needed is for the end plates to be square to the axis of the member. Another common case of simple bearing is shown in Fig. 31.1(c).

By contrast, the case shown in Fig. 31.1(d) is one where if full contact bearing is needed, it is also necessary to take special measures to ensure that the profiles of the two members align accurately, otherwise the area in contact may be significantly less than the area required to transmit the load. Particular tolerances should be specified in such cases, based on the maximum local reduction of area that can be accepted according to the design calculations. Alternatively a division plate could be introduced; if the stresses are high this may well prove to be the most practical solution.

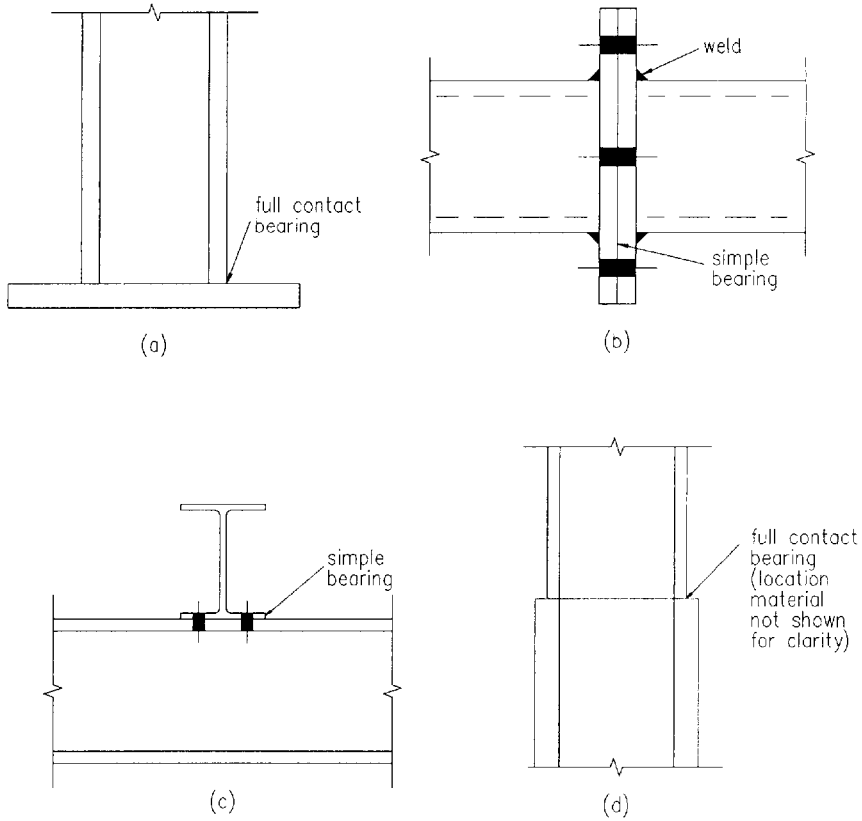


Fig. 31.1 Types of member-to-member bearing: (a) profile to plate, (b) plate to plate, (c) flange to flange, (d) profile to profile (accurate alignment necessary)

### 31.4.3.2 Requirements

Where full contact bearing is required, there are in fact three different criteria involved:

- (1) Squareness.
- (2) Flatness.
- (3) Smoothness.

### 31.4.3.3 Squareness

If the ends of a length of column are not square to its axis, then after erection either the column will not be vertical or else there may be tapered gaps at the

joints, depending on the extent to which surrounding parts of the structure prevent the column from tilting. Under load any such gap will try to close, exerting extra forces on the surrounding members. In addition, both a gap or a tilt will induce a local eccentricity in the column.

A practical erection criterion is that the column should not lean more than 1 in  $x$  (where  $x$  is 600 in NSSS and 500 in the CEN TC 135 draft). This slope is measured relative to a line joining the centres of each end of the column length, referred to as the over-all centreline. The column is also allowed a 'lack of straightness' tolerance of (length/1000), which corresponds to end slopes of about 1/300 (see Fig. 31.2(a)). It is thus necessary to specify end squareness criteria relative to the over-all centreline, rather than to the local centreline adjacent to the end (see Fig. 31.2(b)).

There is generally a design assumption that the line of action of the force in the column does not change direction at a braced joint by more than 1/250, requiring an end squareness in a simple bearing connection (relative to the over-all axis of the member) of 1/500 (see Fig. 31.2(c)). However, full contact bearing generally arises at column splices which are not at braced points, so an end squareness tolerance of 1/1000 is usually specified, producing a maximum change of slope of 1/500 (see Fig. 31.2(d)).

Once a column has been erected, it is more practical to measure the remaining gaps in a joint. These gaps are affected not only by the squareness of the ends but also by the second criterion, flatness.

#### **31.4.3.4 Flatness**

Ends have to be reasonably flat (as distinct from curved or grossly uneven) to enable the load to be transferred properly. Following a history of arguments over appropriate specifications, the American Institute of Steel Construction (AISC) commissioned some tests, which are the basis for their current specifications.

It was found that a surprisingly high tolerance was quite acceptable, and that beyond its limit (or to compensate for end squareness deviations) the use of localized packs or shims was acceptable. Basically similar rules are now beginning to appear in other specifications including the CEN TC 135 draft standard (see section 31.5.6 in relation to erection tolerances). This is an essentially simple and effective method of correcting excessive gaps on site (see also section 31.5.6). However, inserting shims into column joints is not a matter to be undertaken lightly. It is normally more economic to avoid the need for shimming by working to close fabrication tolerances in joints where full contact bearing is required.

#### **31.4.3.5 Smoothness**

In the light of the findings of the flatness tests, it can be appreciated that if absolute local flatness is not in fact needed, absolute smoothness is irrelevant also.



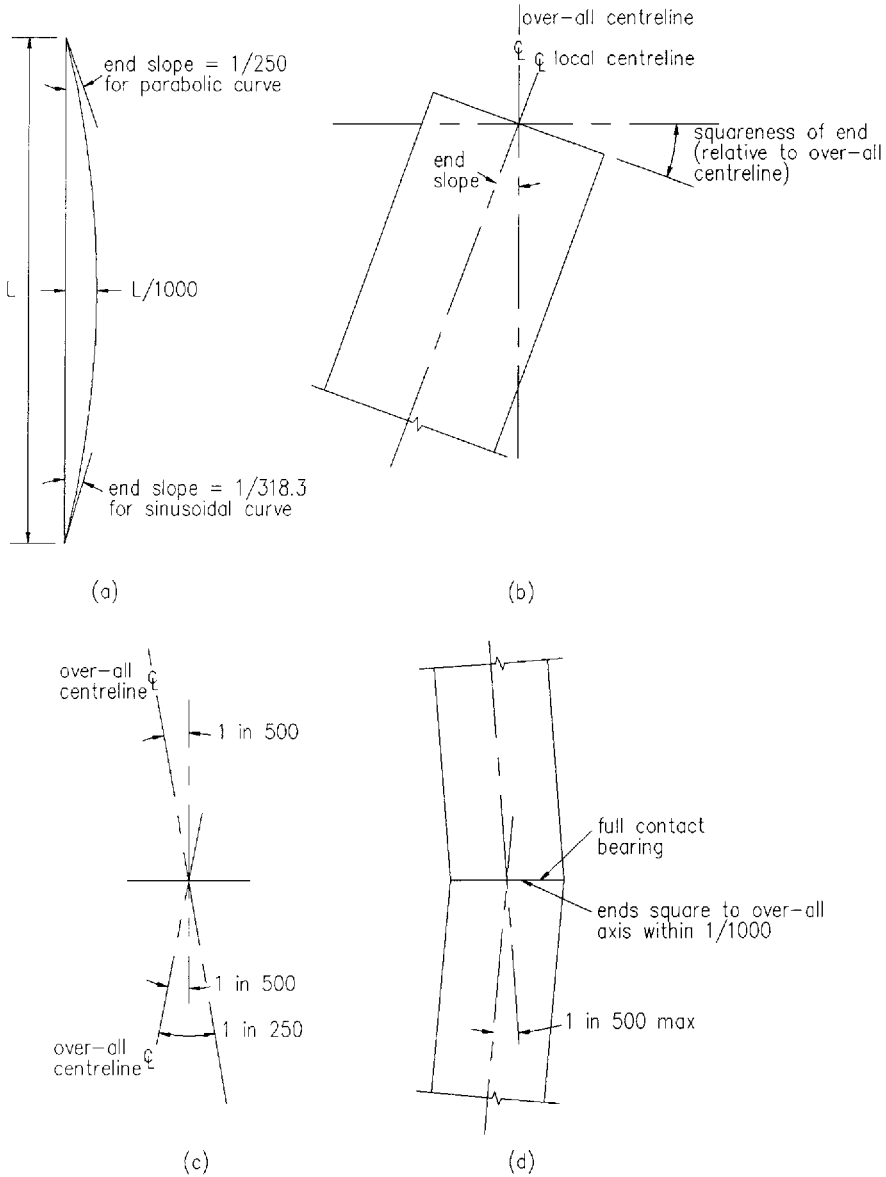


Fig. 31.2 Squareness of column ends. (a) Bow of 1/1000 giving end slopes of about 1/300. (b) Squareness of end measured relative to over-all centreline. (c) Change of direction at a braced joint. (d) End squareness at full contact bearing splice

The best description of the smoothness that is needed, is the smoothness of a surface produced by a good-quality modern saw in proper working order. This degree of smoothness is indeed very good.

Where sawing is not possible, ending machines (i.e. special end-milling machines) can be used for correcting the squareness (or flatness) of ends of built-up (fabricated) columns, such as box columns or other welded-up constructions. Where baseplates are not flat and are too thick to be pressed flat, either they are milled locally in the contact zone or else planing machines are used.

However it cannot be overemphasized that the normal preparation for a rolled section column required to transmit compression by full contact in bearing is by saw cutting square to the axis of the member.

It is, of course, unnecessary to flatten the undersides of baseplates supported on concrete foundations.

#### 31.4.4 Other compression joints

Compression joints, transferring compression through end plates in simple bearing, also need to have their ends square to the axis. If after the members have been firmly drawn together, a gap remains which would introduce eccentricity into the joint, it should be shimmed.

#### 31.4.5 Lap joints

Steel packs should be used where necessary to limit the maximum step between adjacent surfaces in a lap joint (see Fig. 31.3) to 2 mm with ordinary bolts or 1 mm (before tightening the bolts) where preloaded HSFG bolts are used.

#### 31.4.6 Beam end plates

Where the length of a beam with end plates is too short to fit between the supporting columns, or other supporting members, packs should be supplied to make up the difference.

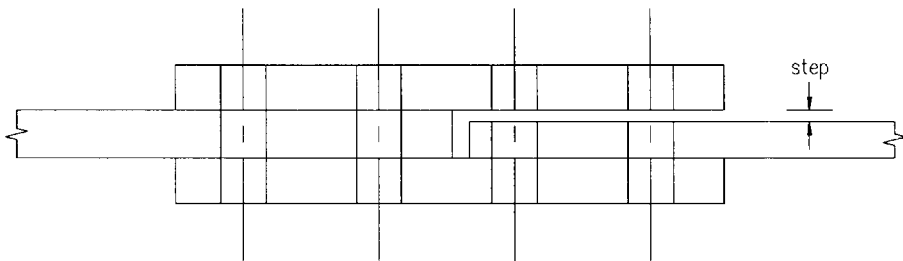


Fig. 31.3 Maximum step between adjacent surfaces

Gaps arising from distortion caused by welding, as shown in Fig. 31.4, need not be packed if the members can be firmly drawn together. However, they may need to be filled or sealed to avoid corrosion where the steelwork is external or is exposed to an aggressive internal environment.

### **31.4.7 Values for fabrication tolerances**

The values for fabrication tolerances currently given in the NSSS are reproduced for convenience in Table 31.4. Each of the specified criteria should be considered and satisfied separately. The cumulative effect of several permitted deviations should not be considered as overriding the specific criteria.

These values represent current practice at the time of writing and are taken from the second edition of the NSSS. However, it is likely that this will be updated, particularly when the CEN Standard comes into force. In any case, the latest relevant standards should always be specified.

The clause numbers referred to in Table 31.4 are clause numbers in the NSSS which should be referred to for further information.

## **31.5 Erection tolerances**

### **31.5.1 Importance of erection tolerances**

Erection tolerances potentially have a significant effect on structural behaviour. There are four matters to be considered:

- (1) overall position,
- (2) fixing bolts,
- (3) internal accuracy,
- (4) external envelope.

### **31.5.2 Erection – positional tolerance**

#### ***31.5.2.1 Setting out***

The position in plan, level and orientation can only be defined relative to some fixed references, such as the national grid and the Ordnance datum level. From the national system, it is usual to set subsidiary site datum points, and often a site datum level, and then refer the accuracy of the structure to these.

For any site the use of a grid of established column lines together with an established site level is strongly recommended. For a large site it is virtually

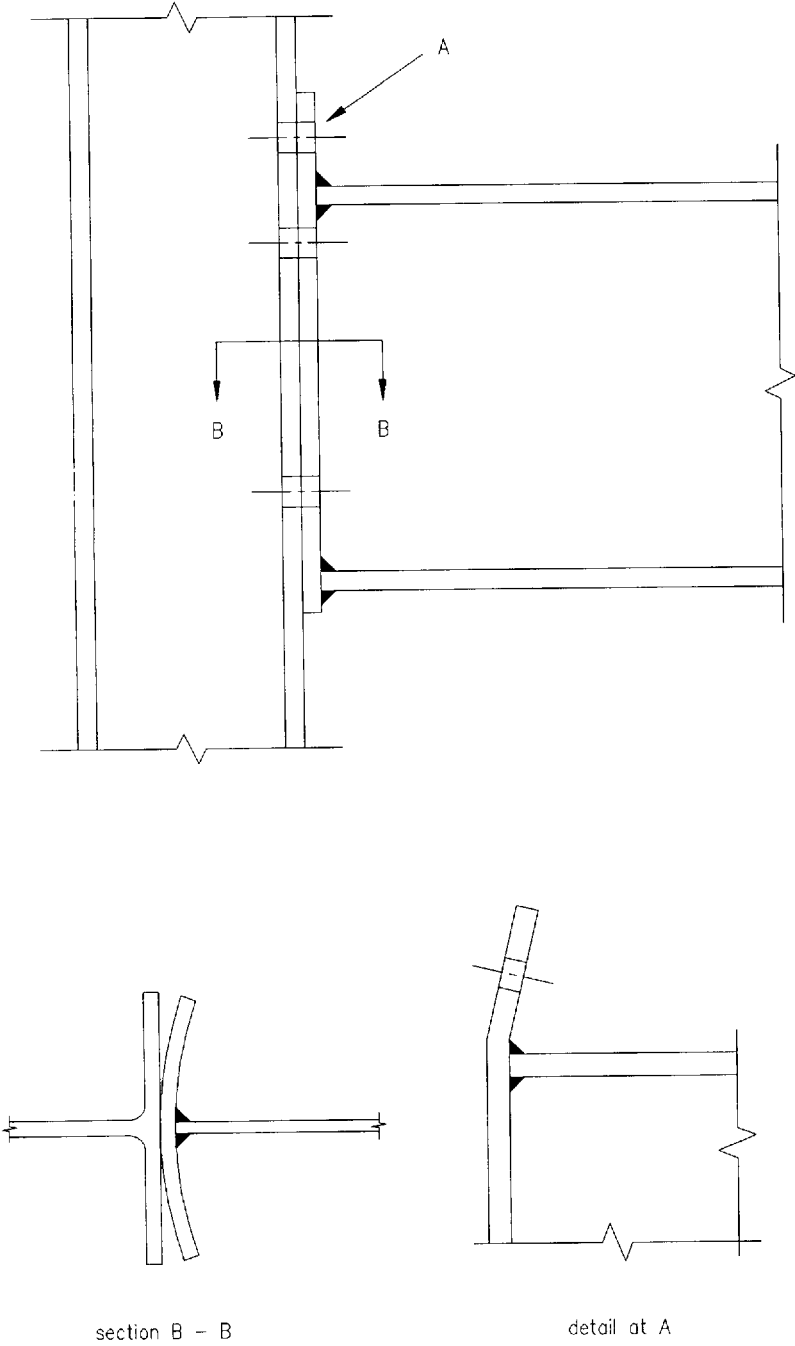


Fig. 31.4 End plate with welding (exaggerated)

Table 31.4 (Extract from National Structural Steelwork Specification)

## WORKMANSHIP - ACCURACY OF FABRICATION

### 7.1 PERMITTED DEVIATIONS

Permitted deviations in cross section, length, straightness, flatness, cutting, holing and position of fittings shall be as specified in clauses 7.2 to 7.5 below (see clause 3.4.6(i)).

Notes: Deviations marked \* are in accordance with BS 5950 Part 2  
 \*\* are modified BS 5950 Part 2 values  
 ‡ are not included in BS 5950 Part 2

### 7.2 PERMITTED DEVIATIONS IN ROLLED COMPONENTS AFTER FABRICATION (Including Structural Hollow Sections)

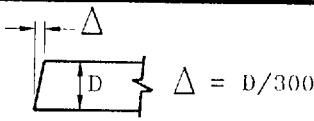
#### 7.2.1 Cross Section after Fabrication\*

In accordance with the tolerances specified in BS 4 or BS 4848 as appropriate.

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7.2.2 Squareness of Ends Not Prepared for Bearing\*\*

See also clause 4.3.3 (i).

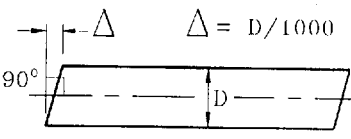


Plan or Elevation of End

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7.2.3 Squareness of Ends Prepared for Bearing \*\*


Prepare ends with respect to the longitudinal axis of the member.  
See also clause 4.3.3 (ii) and (iii).



Plan or Elevation

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7.2.4 Straightness on Both Axes \*\*

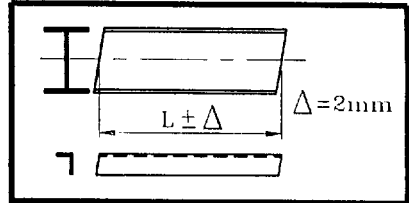


$\Delta = L/1000$  or 3mm  
whichever is greater

Table 31.4 (contd)

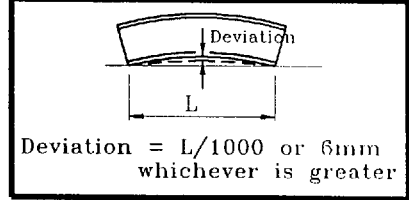
**7.2.5 Length \*\***

Length after cutting, measured on the centre line of the section or on the corner of angles.



**7.2.6 Curved or Cambered \*\***

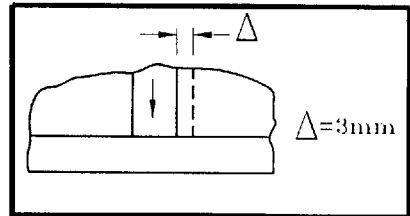
Deviation from intended curve or camber at mid-length of curved portion when measured with web horizontal.



**7.3 PERMITTED DEVIATIONS FOR ELEMENTS OF FABRICATED MEMBERS**

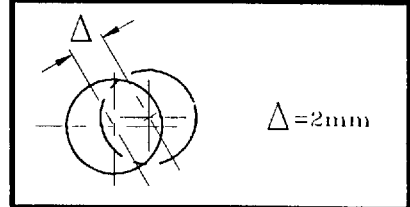
**7.3.1 Position of Fittings ‡**

Fittings and components whose location is critical to the force path in the structure, the deviation from the intended position shall not exceed  $\Delta$ .



**7.3.2 Position of Holes ‡**

The deviation from the intended position of an isolated hole, also a group of holes, relative to each other shall not exceed  $\Delta$ .



**7.3.3 Punched Holes ‡**

The distortion caused by a punched hole shall not exceed  $\Delta$ . (see clause 4.6.3.)

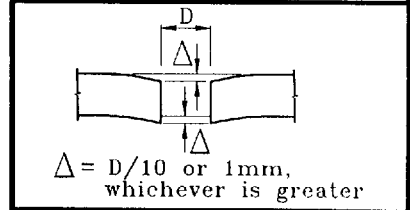
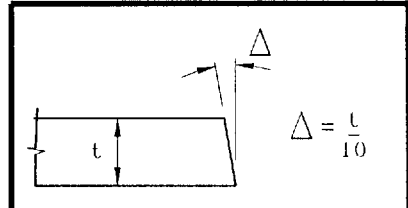


Table 31.4 (contd)

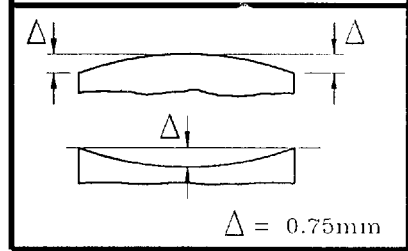
**7.3.4 Sheared or Cropped Edges of Plates or Angles ‡**

The deviation from a 90° edge shall not exceed  $\Delta$ .



**7.3.5 Flatness \*\***

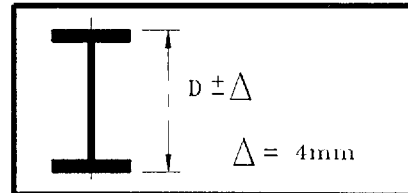
Where bearing is specified, the flatness shall be such that when measured against a straight edge not exceeding one metre long, which is laid against the full bearing surface in any direction, the gap does not exceed  $\Delta$ .



**7.4 PERMITTED DEVIATIONS IN PLATE GIRDER SECTIONS**

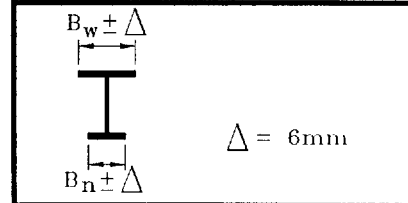
**7.4.1 Depth \***

Depth on centre line.



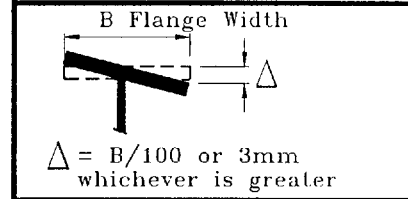
**7.4.2 Flange Width \***

Width of  $B_w$  or  $B_n$



**7.4.3 Squareness of Section \*\***

Out of Squareness of Flanges.



**7.4.4 Web Eccentricity \***

Intended position of web from one edge of flange.

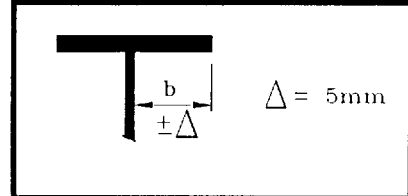
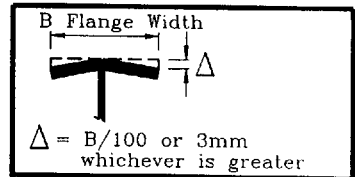


Table 31.4 (contd)

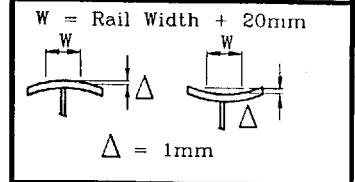
7.4.5 Flanges \*\*

Out of flatness.



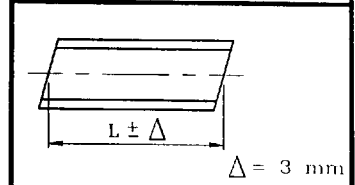
7.4.6 Top Flange of Crane Girder ±

Out of flatness where the Rail seats.



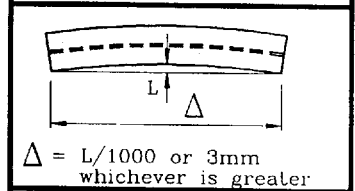
7.4.7 Length \*

Length on centre line.



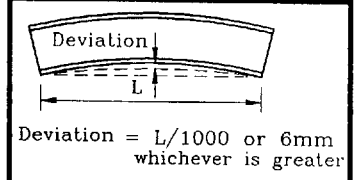
7.4.8 Flange Straightness \*

Straightness of individual flanges.



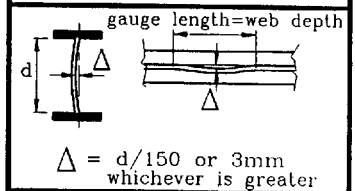
7.4.9 Camber \*\*

Deviation from intended camber at mid-length of curved portion when measured with web horizontal.



7.4.10 Web Distortion \*

Distortion on web depth or gauge length.



7.4.11 Cross Section at Bearings \*

Squareness of Flanges to Web.

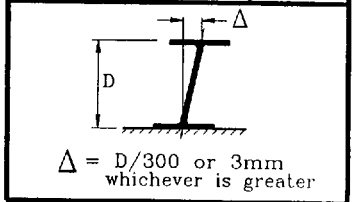
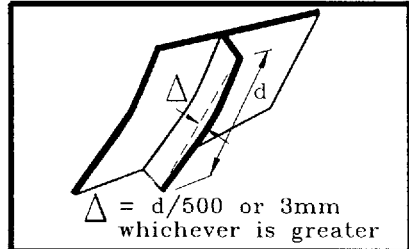




Table 31.4 (contd)

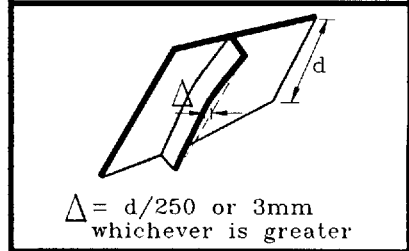
7.4.12 Web Stiffeners ‡

Straightness of stiffener out of plane with Web after welding.



7.4.13 Web Stiffeners ‡

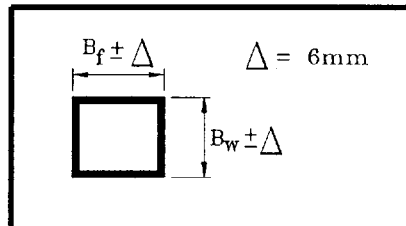
Straightness of stiffener in plane with Web after welding.



7.5 PERMITTED DEVIATIONS IN BOX SECTIONS

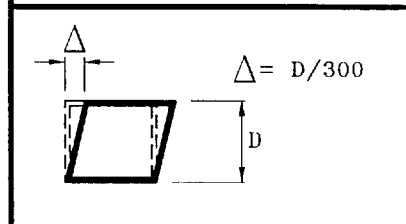
7.5.1 Plate Widths ‡

Width of  $B_f$  or  $B_w$



7.5.2 Squareness \*\*

Squareness at diaphragm positions.



7.5.3 Plate Distortion \*

Distortion on width or gauge length.

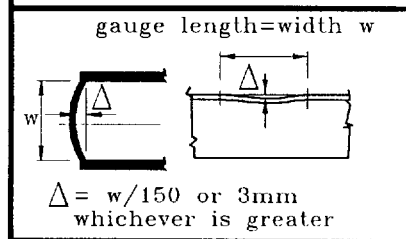
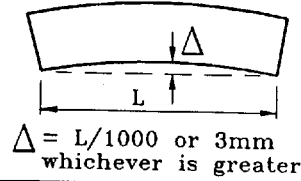


Table 31.4 (contd)

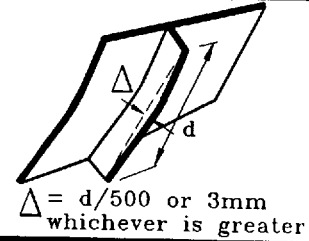
**7.5.4 Web or Flange Straightness ‡**

Straightness of individual web or flanges.



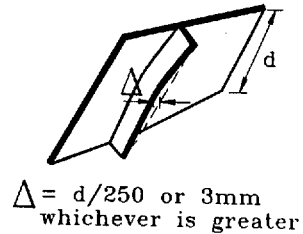
**7.5.5 Web Stiffeners ‡**

Straightness in plane with Plate after welding.



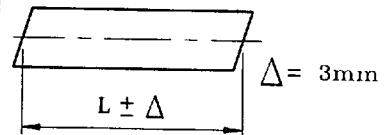
**7.5.6 Web Stiffeners ‡**

Straightness out of plane to Plate after welding.



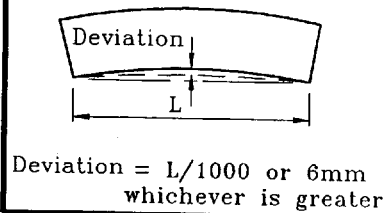
**7.5.7 Length \***

Length on centre line.



**7.5.8 Camber \*\***

Deviation from intended camber at mid-length of curved portion when measured with the uncambered side horizontal.



indispensable. To help appreciate this, consider what happens on the site of a steel structure.

### ***31.5.2.2 Site practice***

Normal site practice is for the supporting concrete foundations, and other supporting structures, to be prepared in advance of steel erection, generally by an organization separate from the steel erector. Depending on the system of holding-down bolts or other fixings to be used, this may involve casting-in of holding-down bolts, preparation of pockets in the concrete and preparation of surfaces to receive fixings to the steelwork.

Even with care, the standard of accuracy achievable is limited and the concrete requires time to harden to a sufficient strength for steel erection to proceed. Once all the foundations etc. are available for steel erection (or at least a sufficient proportion of them on a large site), it is prudent to survey them to review their accuracy.

### ***31.5.2.3 Established column lines and established site level***

From this survey it is convenient to introduce a grid of established column lines (ECL) and an established site level (ESL) of the foundations and other supporting structures in such a way that the positions and levels of steel columns etc. can readily be related to the site grid and site level.

The established column lines are defined as that grid of site grid lines that best represents the actual mean positions of the installed foundations and fixings. Similarly the established site level is defined as that level which best represents the actual mean level of the installed foundations. Of course it should also be verified that the deviation of the ECL grid and the ESL from those specified are within the relevant permitted deviations.

## **31.5.3 Erection – fixing bolts**

### ***31.5.3.1 Types of fixing bolts***

Fixing bolts include both holding-down bolts for columns and various types of fixing bolts used to locate or to support other members, such as beams or brackets carried by walls or concrete members.

Holding-down bolts and other fixing bolts are either:

- (1) fixed in position,
- (2) adjustable, in sleeves or pockets.

### **31.5.3.2 Fixed bolts**

Fixed bolts used to be solidly cast in, an operation requiring care and the use of jigs or templates to achieve accurately. However they are now also commonly produced by placing resin-grouted bolts in holes drilled in the concrete after casting. It may also be possible to use expanding bolts.

However fixed bolts are achieved, they need to be positioned accurately, as the only adjustment possible is in the steelwork, so relatively close tolerances are normally specified.

### **31.5.3.3 Adjustable bolts**

Adjustable bolts are placed in tubes or in tapered trapezoidal or conical holes cast in the concrete, so that a degree of movement of the threaded end of the bolt is possible, while the other end is held in place by a steel washer or other anchoring device embedded in the concrete.

This alternative permits the use of more easily achieved tolerances for the bolts, while using relatively simple details for the steelwork. Adjustment of the bolt necessitates its axis deviating from the vertical to some extent, and the holes in the steelwork need to be large enough to allow for this, particularly if the baseplate is thick. The use of loose plate washers is recommended to span oversize holes if necessary. If required they can be welded in place after the bolts are tightened, but this should not normally be necessary. 'Particular' tolerances need to be worked out for each case, depending on the details, including the length of the bolts, because this affects their slope.

### **31.5.3.4 Length of bolts**

The level of the top of an HD bolt is also important to ensure that the nuts can be fitted properly after erection. To provide the necessary tolerances for the fixing of the bolts, they should be longer than theoretically required, long threaded lengths should be provided and the nominal level for the top should be above the theoretical position.

Similar considerations apply to the lengths of fixing bolts located horizontally.

## **31.5.4 Erection – internal accuracy**

In terms of structural performance, the main erection tolerance is verticality of columns; positions of beams etc. on brackets may also be important. Levels of beams, particularly of one end relative to the other end and of one beam relative to the next one, are important in terms of serviceability.

Otherwise the internal accuracy of one part of the structure relative to another is largely a matter of assembly tolerances, provided that these do not cause any problem of fit-up, interference or clearances. Where the structural accuracy resulting from the assembly tolerances is liable to infringe any of these limits, 'particular' tolerances should be specified.

The necessary tolerances are specified in relation to readily identifiable points and levels. For columns and other vertical members, the reference points are conveniently defined as the actual centre of the member at each end of the fabricated piece. For beams and other horizontal members the reference points are more conveniently defined by the actual centre of the top surface at each end. Either the column system or the beam system should be used for any other cases, and the relevant system should be indicated on the erection drawings. The tolerances are then defined by the permitted deviations of these reference points from the established column lines ECL and established floor level EFL.

The concept of an ECL grid and an established site level ESL have already been explained in section 31.5.2.3. The established floor level EFL is defined as that level which best represents the actual mean level of the as-built floor levels. The EFL must not deviate from the specified floor level (relative to the ESL) by more than the permitted deviation for height of columns.

The reference points for each beam must then be within the permitted deviation from the EFL. In addition the difference in level of each end of a beam and the difference in level between adjacent beams must also be within their respective limits.

In the case of columns, the permitted deviations at each level form an 'envelope' within which the column must lie at all levels. In addition, the permitted inclination of each column within a storey height is limited, but except where columns are fabricated as individual storey-height pieces, the overall envelope normally governs.

### **31.5.5 Erection – external envelope**

Generally the same erection tolerances for verticality apply to external columns as to internal columns. When the envelope of extreme permitted deviations is plotted from the extreme position of the base (allowing for the permitted deviation of the ECL from the theoretical position as well as the permitted deviation of the column base from the ECL), it may be found that this is unacceptable in terms of site boundaries or building lines, especially for a tall multi-storey building. If so, 'particular' tolerances should be specified.

Fit-up problems with cladding could also occur if alternate adjacent columns at the periphery were allowed too large a deviation alternately in and out from the theoretical line of the building face. Even if the fit-up problems could be overcome, the visual appearance might be affected. Again, 'particular' tolerances should be specified if necessary.

### 31.5.6 Shimming full contact bearing splices

As mentioned in section 31.4.3.4 in relation to fabrication tolerances, tests commissioned by AISC, and used as the basis for several modern standards, showed that shims can be used to reduce gaps in full contact bearings to within the specified tolerances. Shimmed gaps up to 6.35 mm were tested, so it is not prudent to permit shimming for gaps exceeding 6 mm; gaps larger than this should be corrected by other means.

Gaps which would otherwise remain over the specified tolerance when the members are in their final alignment, should be shimmed. As the tests were on flat shims, it is acceptable to use flat shims in practice. In the tests the shims were of mild steel, and this is permitted in the AISC specification and in the CEN TC 135 draft.

The shims should be inserted such that no remaining gap exceeds the specified permitted deviation. Short lengths of shim are appropriate in a variety of thicknesses in steps not exceeding the permitted deviation. No more than three layers of shims should be used at any point, and preferably only one or two. The shims (and the lengths of columns) may be held in place by means of a partial penetration butt weld extending over the shims (see Fig. 31.5(a)).

In bolted compression splices, bolted 'finger' shims (shaped as indicated in Fig. 31.5(b)) can be used.

In some cases shims can be driven in, but if so they need to be fairly robust (usually over 2 mm thick), so shims of various thicknesses are needed throughout

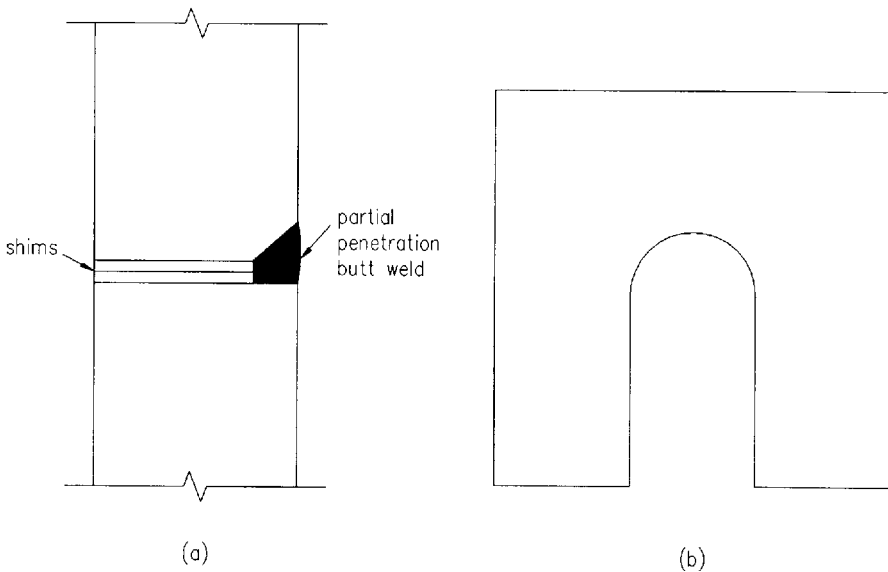


Fig. 31.5 Shims for full contact bearing. (a) Shims with partial penetration butt weld. (b) Finger shim

Table 31.5 (Extract from National Structural Steelwork Specification)

## WORKMANSHIP ACCURACY OF ERECTED STEELWORK

### 9.1 FOUNDATIONS

The Steelwork Contractor shall inspect the prepared foundations and holding down bolts for position and level not less than seven days before erection of steelwork starts. He shall then inform the Employer if he finds any discrepancies which are outside the deviations specified in clause 9.4 requesting that remedial work be carried out before erection commences.

### 9.2 STEELWORK

Permitted maximum deviations in erected steelwork shall be as specified in clause 9.5. All measurements shall be taken in calm weather, and due note is to be taken of temperature effects on the structure. (see clause 8.6.2.).

*Note: Deviations marked \* are in accordance with BS 5950 Part 2  
 \*\*are modified BS 5950 Part 2 values  
 ‡ are not included in BS 5950 Part 2*

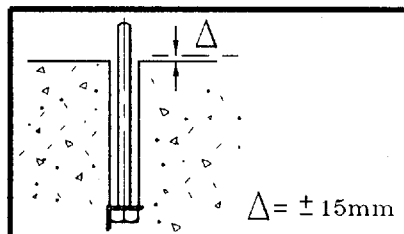
### 9.3 INFORMATION FOR OTHER CONTRACTORS

The Engineer shall advise contractors engaged in operations following steel erection of the deviations acceptable in this document in fabrication and erection, so that they can provide the necessary clearances and adjustments.

### 9.4 PERMITTED DEVIATIONS FOR FOUNDATIONS, WALLS AND FOUNDATION BOLTS

**9.4.1 Foundation Level ‡**

Deviation from exact level.



**9.4.2 Vertical Wall ‡**

Deviation from exact position at steelwork support point.

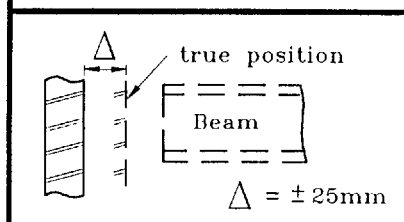
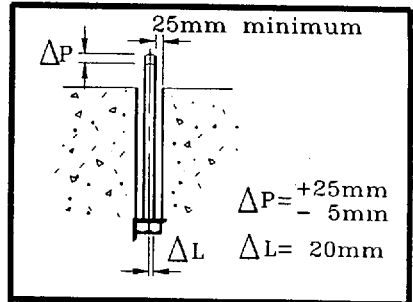


Table 31.5 (contd)

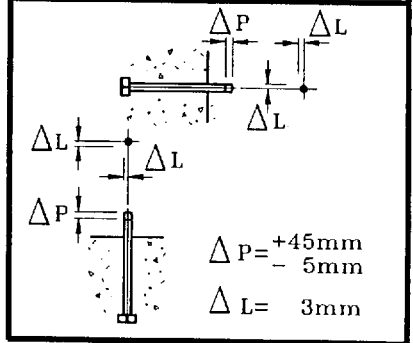
**9.4.3 Pre-set Foundation Bolt or Bolt Groups when Prepared for Adjustment \*\***

Deviation from the exact location and level and minimum movement in pocket.



**9.4.4 Pre-set Foundation Bolt or Bolt Groups when Not Prepared for Adjustment \*\***

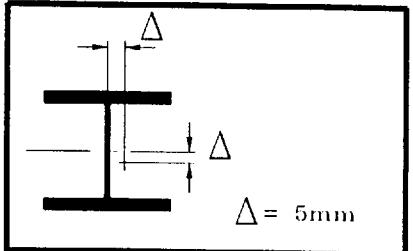
Deviation from the exact location, level and protrusion.



**9.5 PERMITTED DEVIATIONS OF ERECTED COMPONENTS**

**9.5.1 Position at Base of First Column Erected \*\***

Deviation of section centreline from the specified position.



**9.5.2 Overall Plan Dimensions ‡**

Deviation in length or width.

True overall dimension "L"  
 L < 30 metres,  $\Delta = 20\text{mm}$   
 L > 30 metres,  $\Delta = 20\text{mm} + 0.25(L-30)\text{mm}$   
 where L is in metres

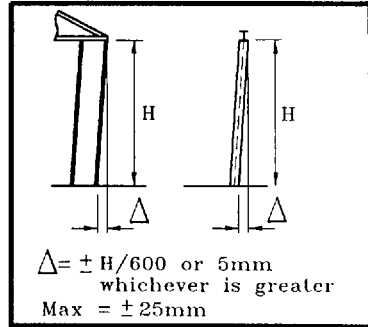


Table 31.5 (contd)

**9.5.3 Single Storey Columns Plumb\*\***

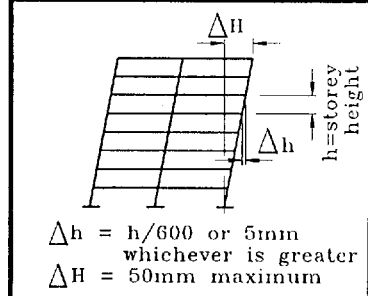
Deviation of top relative to base, excluding portal frame columns, on main axes.

See clauses 1.5 (iv) and 3.4.6 (iii) regarding pre-setting continuous frames.



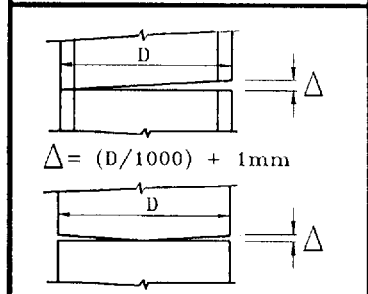
**9.5.4 Multi-storey Columns Plumb\*\***

Deviation in each storey and maximum deviation relative to base.



**9.5.5 Gap Between Bearing Surfaces ‡**

(See clauses 4.3.3 (iii), 6.2.1 and 7.2.3).



**9.5.6 Alignment of Adjacent Perimeter Columns ‡**

Deviation relative to the next column in line.

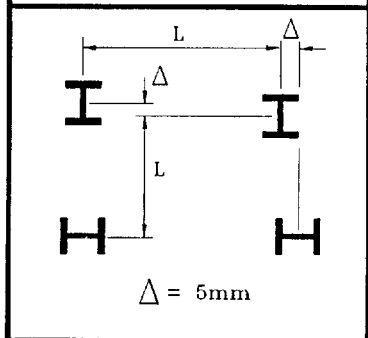
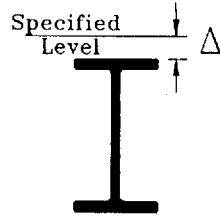


Table 31.5 (contd)

**9.5.7 Floor Beams Level\***

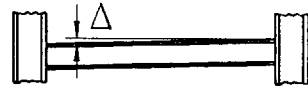
Deviation from specified level at supporting stanchion.



$$\Delta = \pm 10\text{mm}$$

**9.5.8 Floor Beams. Level at Each End of Same Beam ‡**

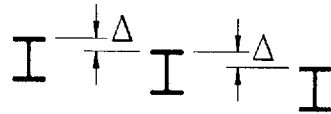
Deviation in level.



$$\Delta = 5\text{mm}$$

**9.5.9 Floor Beams. Level of Adjacent Beams within a distance of 5 metres\***

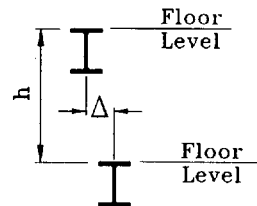
Deviation from relative levels (measured on centreline of top flange).



$$\Delta = \pm 5\text{mm}$$

**9.5.10 Beams Alignment ‡**

Deviation relative to an adjacent beam above or below.



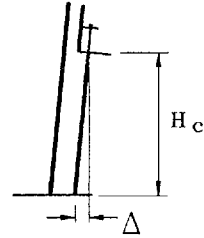
$$h < 3\text{m} \quad \Delta = 5\text{mm}$$

$$h > 3\text{m} \quad \Delta = h/600$$

Table 31.5 (contd)

9.5.11 Crane Gantry Columns Plumb ‡

Deviation of cap relative to base.



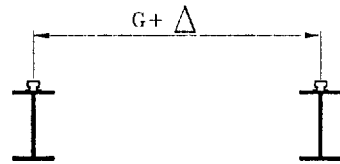
$$\Delta = \pm H_c/1000 \text{ or } 5\text{mm}$$

whichever is greater

$$\text{Max } = \pm 25\text{mm}$$

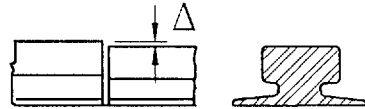
9.5.12 Crane Gantries Gauge of Rail Tracks ‡

Deviation from true gauge.



$$\Delta = \pm 10\text{mm}$$

9.5.13 Joints in Gantry Crane Rails ‡



$$\Delta = 0.5\text{mm}$$

the joint. Driven shims are best limited to vertical joints e.g. between a beam end plate and a column. More commonly the joint must be jacked or wedged open (or else the upper portion lifted by a crane) so that the shims can be inserted. Tapered shims are particularly difficult to insert; as they are not necessary they are best avoided.

### **31.5.7 Values for erection tolerances**

The values for erection tolerances are given in Table 31.5. Each of the specified criteria should be considered and satisfied separately. The permitted deviations should not be considered as cumulative, except to the extent that they are specified relative to points or lines that also have permitted deviations.

These values represent current practice at the time of writing and are taken from the second edition of the NSSS. However, it is likely that this will be updated, particularly when the CEN Standard comes into force. In any case, the latest relevant standards should always be used.

The clause numbers referred to in Table 31.5 are clause numbers in the NSSS which should be referred to for further information.

### **Further reading for Chapter 31**

1. British Standards Institution (1980) *Specification for hot rolled sections*. BS 4: Part 1: 1980, BSI, London.
2. British Standards Institution (1990) *Specification for hot rolled products of non-alloy structural steels and their technical delivery conditions*. BS EN 10025 1990, BSI, London.
3. British Standards Institution (1986) *Equal and unequal angles*. BS 4848: Part 4: 1986, BSI, London.
4. British Standards Institution (1990) *Guide to accuracy in building*. BS 5606 1990, BSI, London.
5. British Standards Institution (1985) *Specification for materials fabrication and erection: hot rolled sections*. BS 5950: Part 2: 1985, BSI, London.
6. British Standards Institution (1991) *Specification for tolerances and dimensions, shape and mass for hot rolled steel plates 3 mm thick and above*. BS EN 10029 1991, BSI, London.
7. CEN TC 135 Standard: *Execution of steel structures* (in draft at time of publication).
8. The British Constructional Steelwork Association (1991) *National structural steelwork specification for building structures*. Second edition, BCSA/SCI Publication No.203/91.

# Chapter 32

## Fabrication

by DAVID DIBB-FULLER

### 32.1 Introduction

The steel-framed building derives most of its competitive advantage from the virtues of prefabricated components which can be assembled speedily on site. Additional economies can be significant provided the designer seeks through his design to minimize the value added costs of fabrication. This is proper 'value engineering' of the product and is applied to perhaps the most influential sector of the delivered-to-site cost of structural steelwork.

This chapter explains the processes of fabrication and links them with design decisions. It is increasingly more important for the designer to understand the skills and techniques available from different fabricators so that he can adapt his design to keep overall costs down. The choice of fabricator can then be made on the basis of ability to conform in production engineering terms to design assumptions made much earlier. It is unacceptable to allow the fabricator or designer to undertake the production engineering element of design in perfect isolation; the dialogue between designers and fabricators must be a continuous one. The effects that fabrication and assembly have on design assumptions and vice versa and, in particular, the achievable fit-up of components and permissible limits of tolerance of the raw steel as received from the mill and their effect on component shape after fabrication are described.

Design must be viewed as a complete process covering strength and stiffness as well as production engineering. The most economical structures feature these principles in full measure.

### 32.2 Economy of fabrication

Structural form has a significant effect on the delivered-to-site cost of steelwork. This is due to a number of factors additional to the cost of raw steel from steel suppliers. Some forms will prove to be more costly from some fabricators than others; they tend to attract work by aligning their methods to specific market sectors. A few years ago the industrial building market was taken over by the introduction of the portal-framed structure. The fabricators in this sector adopted high-volume, low-cost production and deliberately excluded themselves from other

areas of the market. By the use of pre-engineered standards they were able to maximize repetition and minimize input from both design and drawing activities: a classic example of a combination of design and production engineering. Other fabricators specialize in tubular structures, lightweight sections and heavy sections. Fabricators who claim skill in all forms of structural steelwork rarely exhibit good economy in all of them and can prejudice their performance when carrying out work for which they are, in reality, poorly equipped.

### 32.2.1 Fabrication as a cost consideration

Figures 32.1 to 32.4 give an indication of the proportional costs associated with the fabrication and erection of structural steelwork. Actual costs in monetary terms have not been included as they will change with the demand level of the market. The proportions of cost will vary a little from fabricator to fabricator; those shown represent a reasonable average.

The cost headings are:

- raw steel
  - fabrication
  - painting
  - transport
  - erection
  - site painting.
- } fabrication shop activities

Raw steel cost covers the average cost of rolled steel in grade 43A delivered to the fabricator by the British Steel Corporation. No allowance has been made for extra costs arising from the use of stockholders' steel or the extremes of section variation.

Fabrication cost covers a number of different sized jobs and incorporates cleaning of the raw steel by shot blasting, preparation of small parts (cleats and plates and connection components), assembly of the components into complete structural members ready for shop-applied paint treatments. It also includes an allowance for consumables.

Paint cost covers the shop application of 75 microns of primer by spray immediately after fabrication. No allowance has been made for blast cleaning of areas affected by welding. A coverage allowance of 28 m<sup>2</sup>/tonne at the rate of 3 m<sup>2</sup>/litre has been made which represents the likely consumption for rolled section beams and columns. This allowance has been adjusted for various specific work types as described in the accompanying text.

Transport cost is based on 18 tonne loads per trailer which delivers finished products to sites within a fifty mile radius of the fabrication shop. Transport costs will rise for loads of less than 18 tonnes or when oversize components need special police escort or permission.

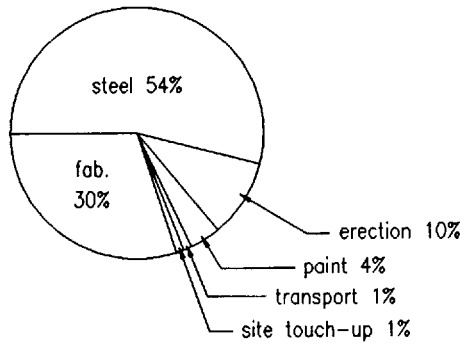


Fig. 32.1 Cost breakdown: portal-framed industrial buildings

The erection cost is average for the work type and includes preliminaries for high-rise multi-storey work. Erection costs are largely beyond the control of the smaller fabricators or fabricators who do not employ their own erection crews; in certain cases, this cost element can be more influential than fabrication.

The cost of site painting has been included but it only covers the average cost for touching-up damage to the primer coat. Other site-applied protection systems vary enormously in cost and so have not been considered.

### *Portal-framed industrial buildings*

The breakdown shown in Fig. 32.1 follows the assumptions given above. There is no adjustment in either the shop painting or the transport cost as this type of work fits the basic parameters well. It can be seen that design economies come principally from the weight of the structure combined with efficient fabrication processes.

### *Simple beam and column structures*

The breakdown shown in Fig. 32.2 incorporates the following limitations:

- (1) the maximum height of the building is three storeys,
- (2) erection is carried out using mobile cranes on the ground floor slab.

It can be seen that again tonnage and fabrication efficiencies are the dominant criteria; 83% of the costs arise from these elements with a slightly greater emphasis on tonnage than was the case with portal frames.

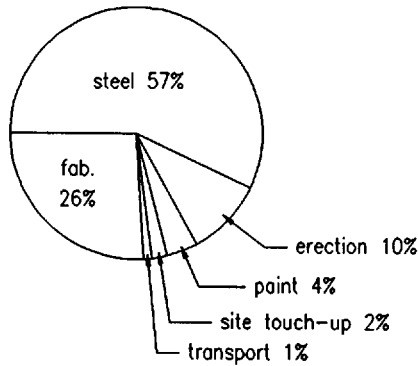


Fig. 32.2 Cost breakdown: simple beam and column structures

*High-rise multi-storey*

The breakdown shown in Fig. 32.3 incorporates the following adjustments:

- (1) the steel grade has been taken as grade 50B with an allowance for cambering and straightening,
- (2) the paint system generally is shot blast and 75 micron primer, 10% of steel coated with 100 micron primer,
- (3) no allowance has been made for any concrete encased beams or stanchions,
- (4) transport includes for off-site stockpiling, bundling and out-of-hours delivery to site (city centre sites often incur these costs).

This sector of the market has a very different cost profile to those already shown. Raw steel still dominates but erection charges have now overtaken the fabrication element. This type of steelwork lends itself particularly well to automated fabrication techniques featuring drilling lines.

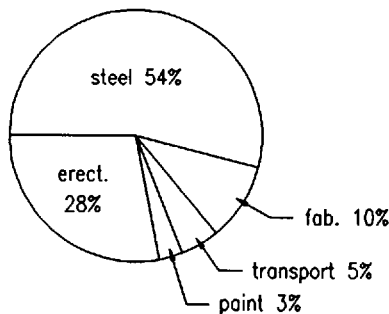


Fig. 32.3 Cost breakdown: high-rise multi-storey



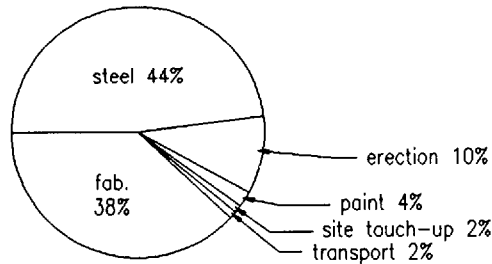


Fig. 32.4 Cost breakdown: lattice structures

### *Lattice structures*

This is perhaps the most difficult of the sectors on which to carry out an analysis as lattice structures vary enormously in size, complexity and element make-up. The costs shown in Fig. 32.4 are indicative and incorporate the following:

- (1) angle booms and lacings,
- (2) welded joints without gusset plates,
- (3) transportable lengths and widths with full-depth splices only.

Here fabrication is virtually the same cost as the raw steel. The designer should work very closely with the fabricator to ensure simplicity of assembly for this form of structure.

### **32.2.2 Production engineering**

Production engineering is concerned with the processes of material procurement, planning, manufacture and delivery. Some of these processes are entirely the province of the production engineer, others can be materially affected by those who specify the manufactured items.

In the context of structural steelwork these items are usually specified by the designer, in more detail than a pure performance specification, in terms of material quality, standard of workmanship and tolerances. However, the production engineer can contribute significantly to the cost effectiveness of the product when given the opportunity and the designer can assist also by considering the production engineering requirements.

Materials are specified largely by direct reference to British Standards which are wide in scope and, if used indiscriminately, can cause difficulties to the production engineer. Keeping the specification brief and relevant along with a restricted range of plate or section sizes will be of benefit. Small quantities with

large variations make material supply costly and prone to error. Choosing sections without regard to rolling programmes can delay manufacture and choice of uncommon section sizes may incur stockist charges. Some sections in the range are rolled infrequently and often to a minimum production run.

Planning the flow of work varies between fabricators but as a general rule the workpiece will travel through the factory in accordance with the work being carried out on it. Designing a beam which requires multiple different fabrication inputs will increase handling costs and reduce factory output. Whenever possible, fabrication should be kept to a minimum number of differing operations, e.g. keep welding away from beams which can be fabricated with bolted connections and vice versa. Mixing these operations increases costs despite the apparent material savings.

Economic delivery is linked to marshalling and transport efficiencies by ensuring that components are kept compact and that brackets are robust enough to withstand the inevitable handling mistakes which can damage flimsy attachments. Keeping the number of components required to a minimum certainly helps costs and has enormous impact on designing for production.

### **32.2.3 Design for production**

This is part of production engineering but focusses on the manufacturing operations themselves. The creation of production and design standards is more appropriate than standardizing complete buildings. Any manufacturing operation benefits from repetition yet in structural steelwork recently there has been a trend towards lower production runs and increasing complexity. Even within this environment, standards can be set up. What is needed is a dialogue between the designer and the production engineer. Each can understand the needs of the other and a consensus can be reached on what will be of benefit to the job in hand.

### **32.2.4 Standards**

Typical examples of production standards are:

- Limiting hole sizes simplifies bolt ordering and avoids tool changes for drills and punches.
- Standard hole patterns benefit those fabricators using computer-controlled punching and drilling lines. Keeping cross centres of holes standard has a similar effect as it increases repeatability of hole formation.
- The use of angle cleats of the same section throughout a job increases the potential for computerized production, particularly when the range of different cleat hole patterns is decreased.

- Keeping plate widths and thicknesses constant creates production standards which favour computer-controlled machinery, if material grades are also standardized.
- Where prefabrication primer paints are specified, keep welding to a minimum as the paint has to be removed local to the weld area to avoid porosity problems; the steel has then to be recycled through the spray booth.
- If specifying weld testing, consider how this is to be carried out and be sympathetic to the production cycle. Try to design connections for which testing can be achieved reliably rather than awkward details with difficult access or impossible geometries for ultrasonic readouts.

Typical examples of design standards are:

- The rationalization of end connection details which can increase repeatability and assist in creating longer production runs of components. Designing each connection to minimize material input may appear beneficial, but in fact it increases fabrication costs by lowering production runs and raising wastage rates. A 25% increase in connection material may represent only a 1% increase in overall job tonnage but save money by the resulting rationalization of components. A saving of course is also realized in design time and drawing costs.
- Maintaining uniform serial sizes which can result in increased repeatability of component assembly. The trade-off is weight versus workshop costs. In particular, the decision to splice a column on the grounds of material saving can incur increased costs for the column as a whole. A full-strength splice is very costly and rarely proves to be the economic solution.

It can be seen that design standards tend to rationalize components and details, thus setting the scene for production standards.

### 32.3 Welding

Fusion welding processes are used to join structural steel components together. These processes can be carried out either in the workshop or on site though it is generally accepted that site welding should not be used as a primary source of fabrication. Welding should only be undertaken by welders who are certificated to the appropriate level required by British Standards or other recognized authority.

Welding processes are classified by the protection medium used to shield the weld metal from the atmosphere. This protection ensures that a sound weld is produced free from contamination-induced cracks and porosity. The forms of protection used during the fabrication of structural steelwork are:

- (1) chemical;
- (2) gas-shielded.

Chemical protection covers many processes, with manual metal-arc (MMA) and submerged-arc welding being those used most commonly.

Gas shielding is achieved in a multitude of ways, the most common being a mixture of carbon dioxide and argon. This system is commonly referred to as MIG welding (metal inert gas) though strictly it is MIG/MAG (metal active gas). MIG welding is gradually superseding MMA welding for reasons of productivity and cost effectiveness. MIG welding can be operated either manually or with some degree of mechanization.

### 32.3.1 Shop welding processes

Stick welding is the traditional form of manual metal-arc welding. The consumable electrode is in stick form and usually covered in a flux which is the chemical protection medium.

The MMA process uses an electrode holder attached via cables to an electrical power source, either a.c. or d.c. (Fig. 32.5). The welding operation is carried out by hand with the rate of deposition controlled by the welder. Stick electrodes are available in diameters from 1.5 to 8 mm with various flux formulations. Joint access is good due to the compactness of the equipment and the ability to use short rods in particularly tight situations.

Figure 32.6 gives access requirements for MMA welding.

Automated methods normally employ submerged-arc techniques in which a heap of flux material laid along the joint receives the bare electrode during the welding operation. The flux buries the arc, acting as a chemical shield. Some automatic processes, however, use flux-coated electrodes. Automatic submerged-arc welding gives high quality results but is limited to uniform welds with long weld runs such as flange-to-web welds on plate girders. Access requirements for submerged-arc welding depend upon the particular equipment available; each

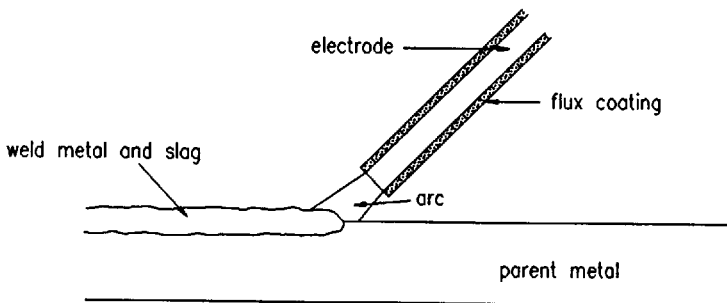


Fig. 32.5 Manual metal-arc welding

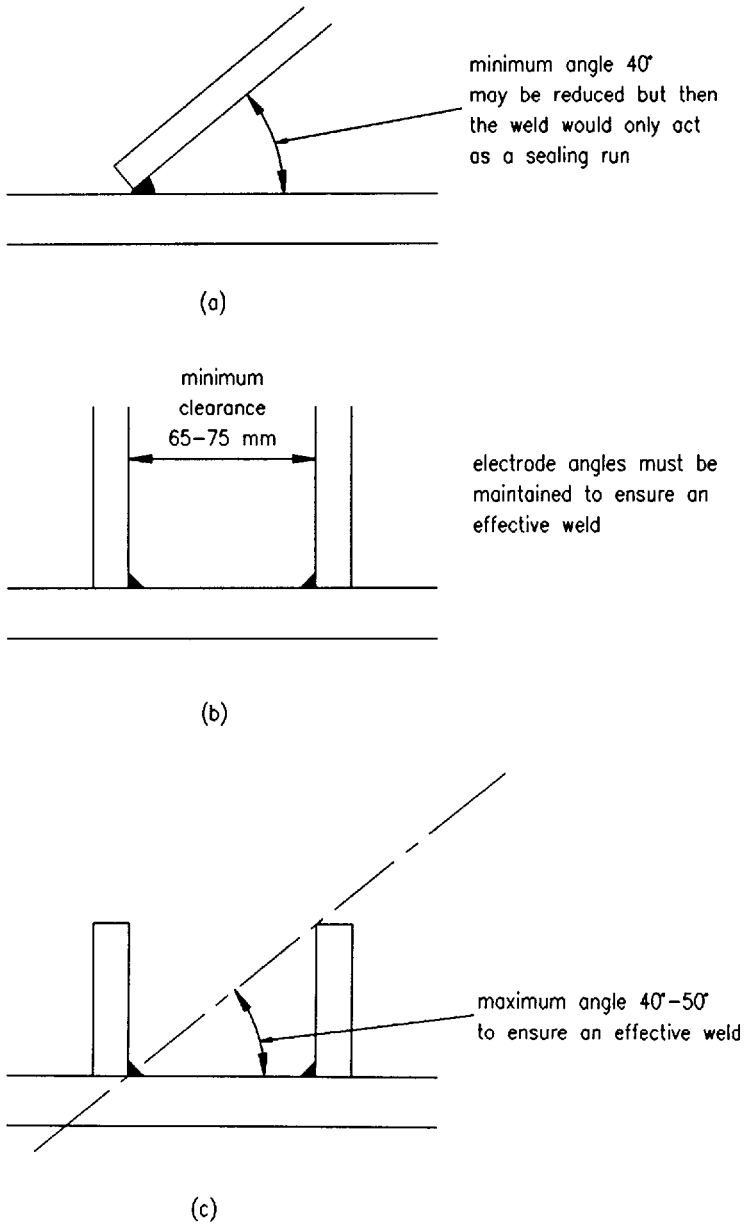


Fig. 32.6 Access requirements for manual metal-arc welding

joint should be considered with detailed knowledge of the welding gun carriage being employed (Fig. 32.7).

MIG welding can be semi-automatic or fully automatic. The electrode is fed through a water-cooled welding head from which it picks up its current and which

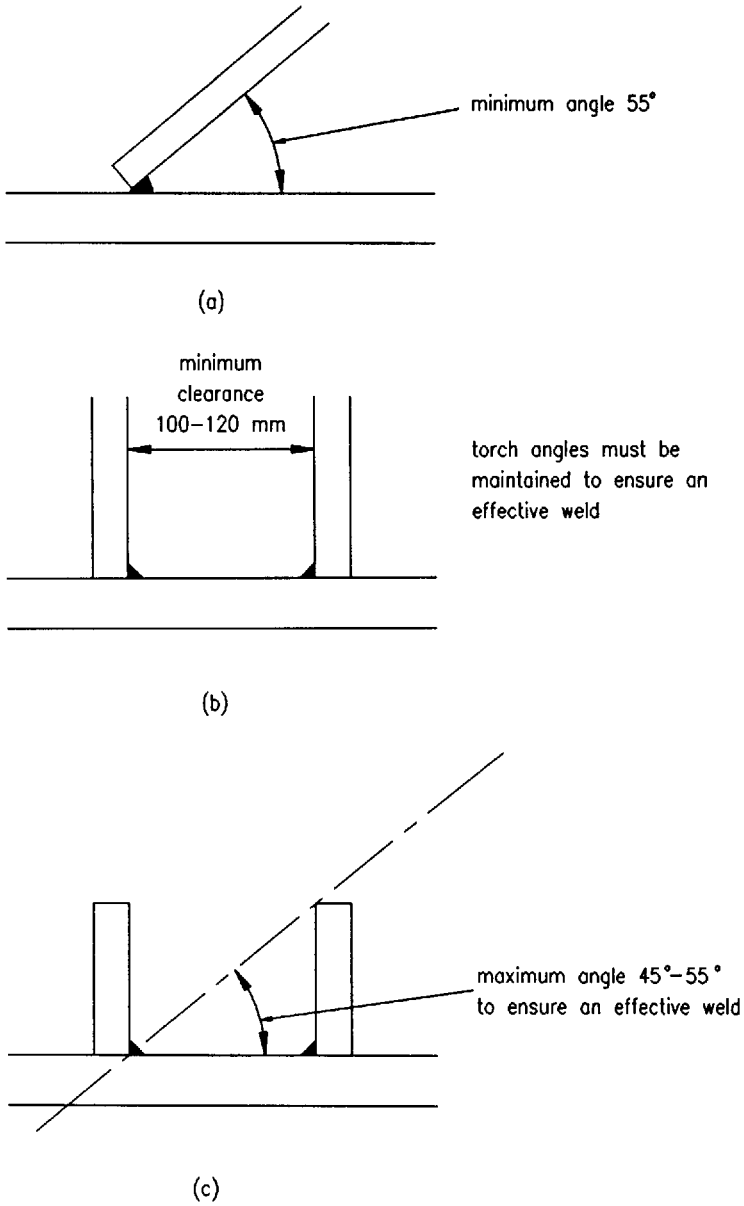


Fig. 32.7 Access requirements for submerged-arc welding

acts as a hood to direct the carbon dioxide into the arc area (Fig. 32.8). The electrode is fed at a constant rate selected to give the required current and the arc is controlled by the power source. The operator does not control the rate of deposition as it is semi-automatic. The process is confined to welding in the flat or

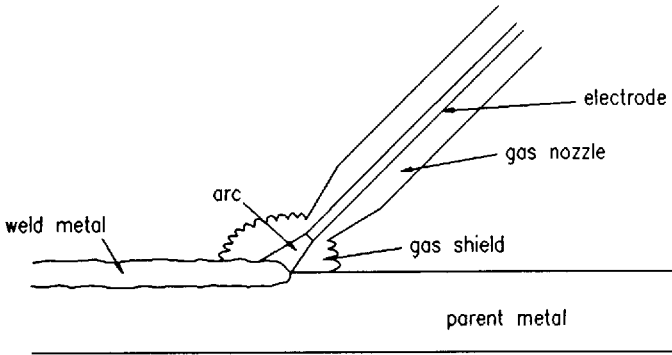


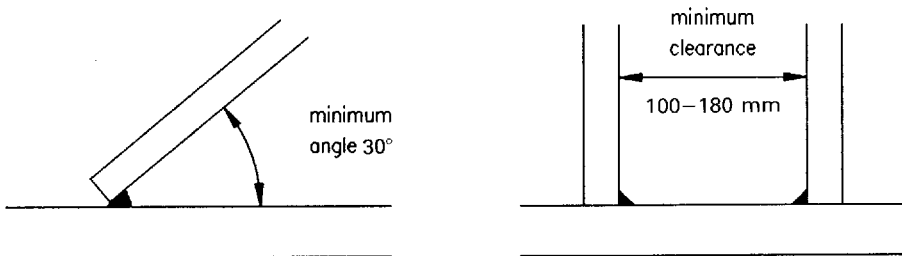
Fig. 32.8 Metal active (or inert) gas welding

horizontal-vertical position. Access is not as good as manual metal-arc. Figure 32.9 gives access requirements for MAG welding.

Other forms of welding may be used in specific circumstances. They are described here for the sake of completeness.

*Electro-slag welding*

This is a specialist form of welding used to join plates together at their edges. The weld is formed by the flow of electric current through a molten flux (slag). The joint is contained between sliding shoes and the electrode is fed automatically into the slag where it forms a pool of weld metal. As the pool increases in depth, the



due to the range of welding gun carriages available  
each joint should be considered separately

Fig. 32.9 Access requirements for metal active gas welding

shoes are moved up the joint leaving behind a solid joint. Welds of as much as 100 mm thickness can be successfully undertaken by the use of this process. Weld thicknesses of less than 25 mm are not suitable for this process.

### *Tungsten inert gas welding (TIG)*

Use is made of a tungsten electrode in a process somewhat similar to MIG welding. The weld metal in this case is shielded by an inert gas, argon, nitrogen or helium, although argon is the most widely used. The other significant difference arises from the fact that the electrode is not consumed and therefore the operator has to control the feed of filler metal, a very skilled operation. This form of welding is confined to high-quality, high-integrity applications within the aircraft, nuclear and chemical plant industries which use the more exotic metals.

#### **32.3.2 Access requirements**

The different welding processes make differing demands upon the space needed for access to the joint. Proper access is a prerequisite for a sound weld; poor access may give rise to incomplete or defective welds particularly where the angle of attack of the electrode is too shallow. MMA welding gives the best flexibility for access due to the compactness of the electrode. MIG welding is more restricted due to the need for clearance around the gas nozzle. All mechanized welding processes are extremely limited because the machinery involved restricts these processes to long welds between plates with the weld laid in the flat position.

Deposition rates are dependent upon welding current, electrode size and number of electrodes (only applicable to mechanized processes such as submerged-arc and electro-slag). Because of the short set-up times for MMA and MIG welding, relatively short lengths of weld can be formed economically. In this respect, there is no rule as to a minimum length, although due allowance must be made for start and stop lengths which reduce the effective length of a weld. Obviously, mechanized techniques are only viable for long runs and probably limited to large weld sections of at least 3 m in length.

#### **32.3.3 Weld defects**

Welding can create defects in either the weld metal or the parent metal. Some defects are metallurgical while others are a result of post-welding tension forces caused by cooling contraction. Poor weld preparation, weld geometry and poor technique are the primary source of defects.

Weld preparation induced defects include the following:



- undercut
- hydrogen cracking
- porosity
- lack of fusion
- slag inclusion
- root concavity
- excessive penetration
- excessive reinforcement
- lack of penetration
- lamellar tearing.

Poor process technique induced defects include the following:

- undercut
- overlap
- porosity
- lack of side wall fusion
- incomplete penetration
- crater pipes
- worm holes
- lamellar tearing
- hot cracking
- heat affected zone (HAZ) cracking.

The notching effect of undercuts and overlaps will be to weaken joints in members subject to fatigue loading patterns. Porosity is an undesirable defect which often gives cause for concern but in itself does not impair strength. Excessive porosity points to the possible existence of other defects associated with poor preparation or technique. HAZ cracking seriously undermines the structural strength of the joint as do hot cracking and lamellar tearing. Lack of side wall fusion can be tolerated provided it occurs infrequently along the weld and is of limited size. Ultrasonic testing will normally reveal these defects and give a good indication of their extent. Incomplete penetration points to poor technique or poor weld design both of which must be corrected. Back gouging root runs will often cure the problem and should be carried out and regarded as good welding practice. Slag inclusion can occur when multipass welds are used due to incomplete clearance of slag from earlier weld runs. When this defect occurs, it should be judged in a similar manner to lack of side wall fusion.

In all cases, the designer should weigh the existence of defects against the required performance of the joint. Critical highly-stressed joints may require very much higher standards of weld integrity than other joints. The lower characteristic strength of welds in some part recognizes that defects do occur and that it is not economic to demand perfect results for all weld situations. Visual inspection of a weld is important as the size and physical appearance of welds is some indication that the joint is sound.

## 32.4 Bolting

Shop bolting may form part of the fabrication process. There are implications arising from the use of shop bolting which need to be appreciated by the designer so that he can ensure that a cost penalty does not occur.

At one time it was common practice to assemble components in the workshop using bolts or rivets. With the increased implementation of welding, this practice has declined due to the costs associated with bolted fabrications. Instead of a simple run of fillet weld, holes need to be formed and bolts introduced, increasing total man hours and cost. In many respects the ease with which welding can be undertaken has diverted designers' attention from the use of shop bolting. Today, fabricators are looking at increased automation to keep costs down and machines have been developed which considerably speed up hole forming. The designer should look to maximize the benefits of automation by appreciating the place of shop bolting in modern fabrication.

### 32.4.1 Shop bolting

There are three ways in which shop bolting can be used:

- (1) permanently-bolted assemblies;
- (2) tack-bolted assemblies;
- (3) trial assembly.

There is still a demand for structural members to be bolted arising from a requirement to avoid welding because of the service conditions of the member under consideration. These may be low temperature criteria, the need to avoid welding stresses or the requirement for the component to be taken apart during service (e.g. bolted-on crane rails). For lattice structures, the designer should specify the bolting bearing in mind the effect of hole clearances around bolt shanks. HSFG bolts will not give problems but other bolts in clearance holes will allow a 'shake-out' which can cause significant additional displacement at joints. Typically, a truss with bolted connections may deflect due to the take-up of lack of fit in clearance holes to such an extent that it loses its theoretical camber. The use of close-tolerance bolts in holes of the same diameter reduces this effect without incurring the cost of turned and fitted bolts in reamed holes.

Tack bolting is used to position members prior to welding, combining the effective use of CNC punching or drilling with the speed and convenience of welding. The tack-bolted assemblies are self-aligning and so do not require expensive jiggling. The tack bolts are sacrificial as they cannot be considered as contributing to the strength of a welded joint. Tack bolting is used for lattice work where angles, channels or tees are used as the booms and lacings.

Large and complex assemblies which are to be bolted together on site may be trial assembled in the fabrication shop. This increases fabrication costs but may pay for itself many times over by ensuring that the steel delivered to site will fit. Restricting trial assembly to highly repetitive items or items critical to the site programme is to be recommended.

### 32.4.2 Types of bolt

The choice of which type of bolt to use may not necessarily be made on the basis of strength alone but may be influenced by the actual situation in which the bolt is used, e.g. in non-slip connections.

There are four basic types of bolts. They are structural bolts, friction-grip bolts, close-tolerance bolts and turned-barrel bolts.

#### *Structural bolts*

Bolts with low material strength and wide manufacturing tolerance were until recently known as 'black bolts' because of their appearance. Now they are called 'structural bolts', normally have a protective coating which gives them a bright appearance and are available in a range of tensile strengths.

#### *Friction-grip bolts*

Friction-grip bolts are normally supplied with a protective coating and are differentiated by material grade. Friction-grip bolts are used in connections which resist shear by clamping action in contrast to structural bolts which resist shear and bearing. When considering the use of friction-grip bolts during the fabrication process, adequate means of access must be provided so that the bolt can be properly tensioned.

#### *Close-tolerance bolts*

This type of bolt differs from a structural bolt in that it is manufactured to closer tolerances. To gain the full benefit of close-tolerance bolts, they should be used in close-fitting holes produced by reaming which adds considerably to the expense of fabrication. Where a limited slip connection is required, close-tolerance bolts can be used in holes of the same nominal diameter as the bolt but not reamed; this gives a connection which is subject to far less slip than would be the case for structural bolts in clearance holes.

### *Turned-barrel bolts*

The turned-barrel bolt is a close-tolerance bolt with a shank which is of a greater diameter than the threaded area. Typically, a 20 mm diameter turned-barrel bolt has a 22 mm shank. These bolts are used in reamed holes and the virtue of the increased shank diameter is that it ensures that the threads are not damaged during the insertion of the bolt.

### **32.4.3 Hole forming**

Most fabrication shops have a range of machines which can form holes in structural steelwork. There is a growing tendency towards the use of computer-controlled machines with which a number of fabrication activities, typically punching, marking, shearing and clipping, can be carried out on the one piece of equipment. Numerically-controlled drilling lines feature machines which carry out the drilling operation only although there are some which incorporate plate-burning facilities.

Despite the introduction of computer numerically controlled (CNC) machinery, use is still made of equipment which requires human operation. The traditional drilling machine is the radial drill, a manually-operated machine which drills individual holes in structural steelwork. Given the enormous difference in output between the two generations of machine, commercial pressures will ensure that the older type is removed from service. Therefore, only the features of modern equipment will be outlined here.

To gain the best output, CNC machines are incorporated in conveyor lines. There is an infeed line which takes the unprocessed raw steel and an outfeed line which distributes the finished product either to the despatch area or further along the fabrication cycle and into an assembly area. The infeed conveyor for punching and drilling machines that handle angles, flats, small channels and joists will normally be configured to handle 12 m long bars. There will be a marking unit which carries a set of marking dyes that stamp an identification mark on to the steel if required. There may be a number of hydraulic punch presses each suitable for accepting up to three punching tools and it is normal that the tool holders are quick-change units. Typically, hydraulic presses have 1000 kN capacity. The punch presses can form differently-shaped holes so that angles can be produced with slots. Some machines produce the slot by a series of circular punching operations, others have a single slot shaped dye.

Once the material has passed through the punch presses, it is then positioned for shearing. The hydraulic shear has a capacity of between 3000 and 5000 kN. Machines which incorporate drilling facilities can have these positioned next to the punch presses prior to the hydraulic shear. The output of the machine can be as high as a thousand holes per hour. Obviously, these machines can be obtained with different capacities so that if the work of the fabricator is at the light end of the section range, he does not need to purchase machines with large capacity.

For larger sections, where drilling and cutting are required, there are two basic machines available. One is a drilling and plate-cutting system which is used for heavy plates; the other machine is of a larger capacity and is used for drilling rolled sections of all sizes. Modern drills normally have three axis numeric control and air-cooled drills. These machines have sensors which can detect the position of the web to ensure that hole patterns are symmetrical about the web centreline.

Where components only need a small number of holes, mobile drills are used. These are normally magnetic limpet drills hand operated by the fabricator. The holes are formed with rotary-broach drill bits which have a central guide drill surrounded by a cylindrical cutter.

The fabricator will always carry out hole-forming operations prior to any further fabrication as the presence of any stiffeners or cleats on a bar would severely disrupt the input of NC machines.

## **32.5 Cutting and machining**

The fabrication processes of cutting and machining are tending towards greater automation. Many traditional methods are falling into disuse due to increased labour costs and low levels of productivity.

Universal beams, columns and the larger angles, tees and channels are normally cut to length by saws. Hollow sections are also treated in this way. Small sections of joist, channel, angle and flat are cut to length by shearing either as a separate operation or as part of a punching and cropping operation which is computer controlled. Large plate sections may be sheared but this involves specialist plant and equipment which is not available to all fabricators.

Machining can take a number of forms but commonly is the process of bringing surfaces into a closer tolerance of flatness and squareness than can be achieved by cold sawing or burning. Machining can be applied to the ends of rolled sections and the surfaces of plates. In the past, specifications often called for the ends of columns, which were transmitting loads through bearing, to be machined to ensure close contact. This process was known as 'ending'. Nowadays a good quality saw cut is accepted for column end bearing.

### **32.5.1 Cutting and shaping techniques**

#### *Flame cutting or burning*

This technique produces a cut by the use of a cutting torch. The process may be either manual or machine controlled. Manual cutting produces a rough edge profile which can be very jagged and may need further treatment to improve its appearance. Edges of plates cut manually require greater edge distances to holes

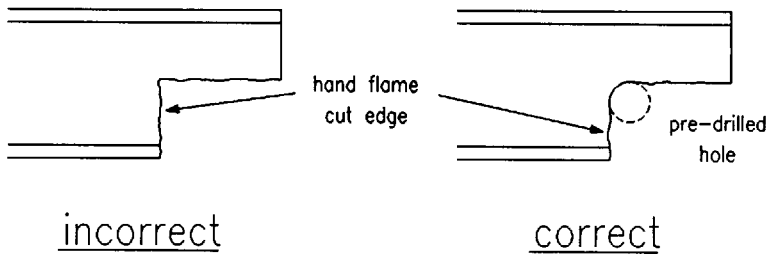


Fig. 32.10 Hand flame cutting

for this reason. Notches or holes with square corners should not be hand cut unless the corner is first radiused by a drilled hole, Fig. 32.10.

When flame cutting is carried out under machine control, the cut edge is smooth and therefore the restrictions on edge distances to holes are relaxed. Notches which are machine cut need radiusing either by a predrilled hole or by the control of the cutting machine. Unradiused notches are to be avoided due to their stress-raising characteristics. Notching or coping of beam ends can now be carried out by computer-controlled machines which burn the webs first and create the radiused corner then cut the flanges with a cut which coincides with the web cut. Numerically-controlled coping machines can cut top and bottom notches simultaneously and the notches can be of different dimensions.

Castellated beams are formed by cutting a web pattern along a UB or UC section followed by realignment and rewelding. The web cutting is always machine controlled to ensure accurate fit-up and an edge which is suitable for subsequent welding.

### *Arc plasma cutting*

Plates may be cut by arc plasma techniques. In this case the cutting energy is produced electrically by heating a gas in an electric arc produced between the tungsten electrode and the workpiece which ionizes the gas, enabling it to conduct an electric current. The high-velocity plasma jet melts the metal of the workpiece and blows it away. The cut so produced is very clean and its quality can be improved by using a water injection arc plasma torch. Plasma cutting can be used on thicknesses up to about 150 mm but the process is then substantially reduced in speed.

### *Shearing and cropping*

Sections can be cut to length or width by cropping or shearing using hydraulic shears. Heavy sections or long plates can be shaped and cut to length by specialist

plate shears. These are large and very expensive machines normally to be found in the workshops of those fabricators who specialize in plate girder work for bridges, power stations and other heavy steelwork fabrications. For the more commonplace range of smaller plates and sections, there is a range of equipment available which is suitable for cutting to length or shaping operations. These machines feature a range of shearing knives which can accept the differing section shapes. Shearing can be adjusted so that angled cuts may be made across a section. This is particularly useful for lacings of latticed structures. One version of the shear is a 'notcher' which can cut shaped notches. Special dies are made to suit the notch dimensions and it is possible to obtain dies to cut the ends of hollow sections in preparation for welding together.

### *Cold sawing*

When, because of either specification or size, a section cannot be cut to length by cropping or shearing, then it is normally sawn. All saws for structural applications are mechanical and feature some degree of computer control. Sawing is normally carried out after steel is shot blasted as the saw can be easily incorporated within the conveyor systems associated with shot blast plants.

There are three forms of mechanical saw, circular, band and hack. The circular saw has the blade rotating in a vertical plane which can cut either downwards or upwards, though the former is the more common. The blade is a large milling wheel approximately 5 mm thick. The diameter of the saw blade determines its capacity in terms of the maximum size of section which can be cut. Normally, fabricators will have saws capable of dealing with the largest sections produced by British Steel. For increased productivity, sections may be nested or stacked together and cut simultaneously. Some circular saws allow the blade to move transversely across the workpiece, which is useful for wide plates. Most circular saws can make raking cuts across a section of any angle though some saws are restricted to single side movement. The preferred axis of cut is across the  $Y-Y$  axis of the section. In the case of beams, channels and columns, this is with the web horizontal and the flange toes upwards. Depending on the control exercised, a circular saw can make a cut within the flatness and squareness tolerances necessary for end bearing of members. Tighter tolerances will require 'ending'.

Band saws have less capacity in terms of section size which can be cut. Generally, sections greater than 600 mm × 600 mm cannot be sawn using band saws. The saw blade is a continuous metal band edged with cutting teeth which is driven by an electric motor. The speed of cut is adjustable to suit the workpiece. Band saws can make mitre cuts and can cut through stacked sections. Cutting accuracy is dependent on machine set-up but should produce results similar to circular saws.

Hack saws are as the name implies mechanically driven reciprocating saws. They have normal format blades carried in a heavy duty hack saw frame. Hack saws have more limited cutting capacity than band saws and have the capability to produce mitre cuts.

All saws feature computer-controlled positioning carriages for accurate length set-up; most also have computer sensing for angle cuts. The highest output saws are circular saws.

### *Machining*

In metalworking terms, machining covers a very wide range of processes. In regard to structural steelwork, machining is limited. At its simplest it covers grinding of surfaces or edges to improve appearance, remove notches or in preparation for welding. Edge preparation for welding may be carried out by feeding material through a grinding machine or by hand grinding using a hand-held tool. Local tidying up of plate edges after burning by hand is normally done with hand-held tools.

The larger machining operations are confined to surface preparation of the ends of members or surfaces of plates which need to butt closely together. Grinding the surface of baseplates or splice plates to columns is often carried out to ensure the flatness of the plate surface. This is either performed prior to the delivery of plates to the fabricator or it is carried out by him. This process is called 'flash grinding'. The preparation of column ends is a specialist operation called 'ending'. An ending machine is a milling bed often mounted in a long trench or pit. This machine can be traversed along guide rails so that a number of columns can be processed one after the other. The columns are laid flat and adjusted so that they are normal to the milling axis. The milling machine then trims the column ends to produce a flat ground surface. This surface is the bearing surface between column lengths at splices or at the baseplate. 'Ending' and 'flash grinding' should be coincident and carried out after straightening the column length.

### *Gouging*

The gouging process is the removal of metal at the underside of butt welds. Gouging techniques are also used for the removal of defective material or welds. The various forms of gouging are flame gouging, air-arc gouging, oxygen-arc gouging and metal-arc gouging.

Flame gouging is an oxy fuel gas cutting process and uses the same torch but with a different nozzle. It is important that a proper gouging nozzle is adopted so that the gouging profile is correct.

Air-arc gouging uses the same equipment as manual metal arc welding. The process differs in that the electrode is made of a bonded mixture of carbon and graphite encased in a layer of copper and jets of compressed air are emitted from the specially designed electrode holder. These air jets blow away the parent metal from beneath the arc.

A special electrode holder is used in the oxygen-arc gouging process. A special tubular coated steel electrode controls the release of a supply of oxygen. Oxygen



is released once the arc is established and when the gouge is being made the oxygen flow is increased to a maximum.

Standard manual metal arc welding equipment is used for metal-arc gouging. The electrodes, however, are specially designed for cutting or gouging. This process relies on the metal being forced out of the cut by the arc and not blown away as in the other processes.

### 32.5.2 Surface preparation

Structural sections from the rolling mills may require surface cleaning prior to fabrication and painting. Hand preparation, such as wire brushing, does not normally conform to the requirements of modern paint or surface protection systems.

Blast cleaning is the accepted way of carrying out surface preparation. It involves blasting dry steelwork with either shot or grit at high velocity to remove rust, oil, paint, mill scale and any other surface contaminants. The most productive form of blast cleaning plant has special equipment comprising infeed conveyor, drying oven, blast chamber, spray chamber and outfeed conveyor.

Steel is loaded on to the infeed conveyor either as separate bars or side by side depending on the blast chamber passage opening. It then travels through the drying oven which ensures that any surface moisture is removed prior to blasting. The blast chamber receives the steel and passes it over racks and between the blasting turbines, which are impellers fed centrally with either shot or grit. The material is thrown out from the edge of the turbine and impacts against the steelwork. The speed of the turbine, its location and aperture determine the velocity and direction of the blasting medium. While many blast chambers operate in a satisfactory manner with four turbines, a better result is achieved on larger sections when six turbines are present (Fig. 32.11).

The blasting medium is retrieved from within the blast chamber and recycled until it is exhausted. Shot provides a good medium for steel which is to be painted; grit can cause excessive wear of the blast chamber and results in a surface which is more pitted, giving a reduced paint thickness over high points.

The steel leaves the blast chamber and immediately enters the spray chamber. Depending upon the requirements of the specification, the steel is then sprayed with a primer paint which protects it from flash rusting. The use of prefabrication primers should be discussed with the fabricator and paint system supplier as requirements may vary. For most structural applications in building work, there is little need to specify a prefabrication primer. Once the steel has passed through the spray chamber, it is fed on to the outfeed conveyor and continues to its next process centre.

The other form of blast cleaning is called 'vacu blasting', a manual method where the blasting medium is blown out of a hand-held nozzle under the pressure of compressed air. This process is normally performed in a special sealed cabinet

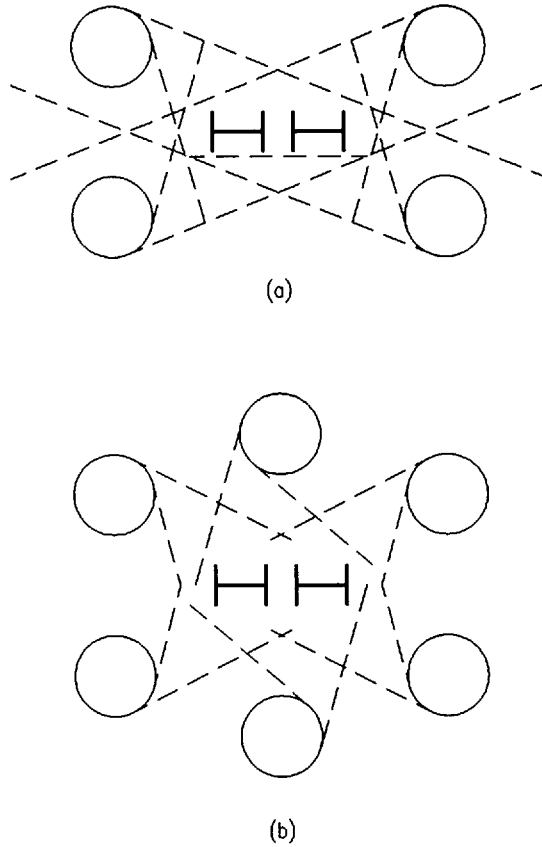


Fig. 32.11 Blast chambers: (a) four turbine, (b) six turbine

with the operator wearing protective clothing and breathing equipment. It relies heavily on the skill of the operator and does not give production rates approaching those of mechanical blasting plants.

Local areas of damage caused by welding can be cleaned by vacu blasting or by needle gunning. The needle gun has a set of hardened needles which are propelled and withdrawn rapidly. The action of the needles on the steel effectively removes weld slag and provides a good surface for painting. Needle gunning is not suitable for large areas or for heavily contaminated surfaces.

Surface preparation is intended to provide a uniform substrate for even paint application. It is important to consider the edges of plates where paint thickness is often low. A slight edge chamfer produced by grinding will improve paint film thickness performance.

### 32.5.3 Cambering, straightening and bending

Each of these operations has a different purpose. Cambering is done to compensate for anticipated deflections of beams or trusses under permanent loads, dead loads or superimposed dead loads such as finishes. Straightening is part of the fabrication process aimed at bringing sections back within straightness tolerances. Bending is to form the section to a shape which is outside normal cambering limits.

Rolled sections are normally bought in by the fabricator and then sent to specialist firms for cambering. The steel section is cold cambered by being passed between rolls. The rolls are adjusted on each pass until the required camber is achieved. The following cambers can be produced:

- circular profile (specify radius)
- parabolic profile (specify equation)
- specified offsets (tabulate co-ordinates)
- reverse cambers (circular, parabolic, offset or composite).

Bending is also carried out by specialists, the process being identical to that for cambering. Curves can be formed on either the  $X-X$  or  $Y-Y$  axes.

Straightening can be carried out by the fabricator or by the cambering specialists. Sections are often straightened by the fabricator by applying heat local to the flange or web. This is a skilled operation which achieves excellent results.

### 32.6 Handling and routing of steel

The fabrication process involves the movement of steel around the workshop from one process activity to the next. Clearly, all these movements should be planned so that the maximum throughput of work is achieved and costs are minimized. Even with the highly automated facilities available today, planning is essential as work centres may become overloaded and cause delays to other activities. In this respect, the work flow has to be balanced between work centres.

The routing of steel through a fabrication workshop is planned on the basis of the work content required on the workpiece. The workpiece will consist of one or more main components which may have smaller items attached (cleats, tabs and brackets). The main components are normally obtained from the steel mills though some fabricators obtain steel from stockholders. The steel is stored in a stockyard local to the workshop. The control of steel stock is an important management function which can balance the cash flow of the fabricator and provide clear identification of the steel for traceability purposes. Stock control systems are commonly computerized and should allow the fabricator to identify:

- (1) steel on order but not yet received,
- (2) steel which is in the stockyard and its location,

- (3) allocation of steel to particular contracts,
- (4) levels of unallocated steel (free stock).

Prior to the fabrication cycle, an estimate is made of the work content of a workpiece. This assessment may be crudely based upon tonnage or more commonly based upon time study data of previous similar work. The work content assessment is a production control function which will identify:

- (1) weight of finished product,
- (2) content of workpiece (parts list),
- (3) work centre activities required (sawing, drilling, welding, etc.),
- (4) labour content,
- (5) machine centre utilization.

Production control systems are now often computerized and can produce a detailed map of the movement of the workpiece and its component parts within the fabrication workshop. Computer systems can identify any potential overloads of work centres so that the production controller can specify an alternative path.

Generally, the cycle of work centre activity is as shown in Table 32.1 (the exact sequence of events may, however, vary between fabricators).

### **32.6.1 Lifting equipment in fabrication workshops**

Not all steel can be moved around a workshop on conveyor lines. It is not practical or cost effective to do so and would restrict the flexibility for planning workshop activities. Much of the steel will be moved by cranes of one form or another. Craneage capacity can be a restriction on the work which a fabricator can undertake. Restricted headroom is another annoying problem particularly when considering the fabrication of deep roof trusses. Knowing the fabricator's limitations in these regards is useful when making a selection.

There are various types of crane in common use in most workshops, they are:

- electric overhead travelling (EOT)
- goliath
- semi-goliath
- jib
- gantry.

EOT cranes are the main lifting vehicles in the larger fabrication workshops. Their capacity varies from fabricator to fabricator but rarely exceeds 30 tonnes SWL. EOT cranes run on rails supported on crane beams carried off either the main building stanchions or a separate gantry and are used for moving main

**Table 32.1** Sequence of activities in fabricating shops

|                                 |   |
|---------------------------------|---|
| Cleaning and cutting to length  | Shot blasting<br>Pre-fabrication priming<br>Sawing or burning   |
| Manufacture of attachments      | Preparation of: cleats<br>brackets<br>stiffening plates<br>end plates<br>baseplates   |
| Preparation of main components  | Pre-assembly: drilling<br>punching<br>coping<br>cropping<br>notching<br>cutting of openings   |
| Assembly of workpiece           | Marshalling of components<br>Setting-out of components<br>Shop bolting<br>Welding<br>Local drilling<br>Local cutting<br>Cleaning up |
| Quality control (assembly)      | Check assembly – dimensional<br>– NDT<br>– visual inspection  |
| Surface treatment               | Sign-off<br>Painting<br>Metal spraying } often by other<br>Galvanizing } specialists  |
| Quality control (final product) | Conformity with specification<br>Sign-off   |
| Transportation                  | Marshalling<br>Loading<br>Despatch  |

components and finished workpieces between work centres. Heavy components need turning over for welding and this is achieved by the use of EOT cranes.

Goliath and semi-goliath cranes are heavy-duty lifting devices which tend to be used on a more local basis within the workshop than EOT cranes. The goliath is a free-standing gantry supported on rails laid along the workshop floor. Semi-goliath cranes are ground rail supported on one side and gantry rail supported on the other. The lifting capacity of goliath-type cranes is normally less than that of an EOT crane though greater in some workshops where there are EOT crane support restrictions (Fig. 32.12).

Jib cranes are light-duty (1–3 tonne capacity) cranes mounted from building side stanchions and operating on a radial arm with a reach of up to 5 m. They are useful for lifting or turning the lighter components (Fig. 32.13).

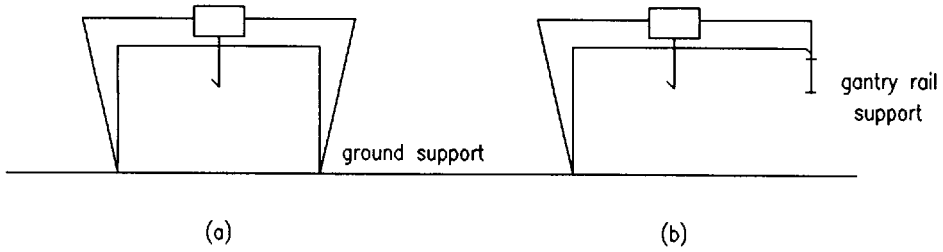


Fig. 32.12 Goliath cranes: (a) goliath, (b) semi-goliath

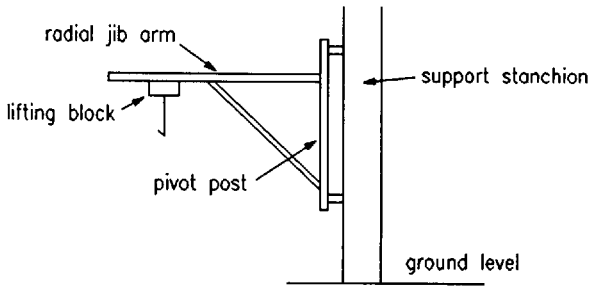


Fig. 32.13 Jib crane

Gantry cranes are purpose-built structures with limited lifting capacity (3–10 tonne). The lifting block travels along a gantry beam and is either underslung or top mounted. Gantry cranes are useful lifting devices where no building can be used to support an EOT crane and some gantry cranes feature EOT cranes riding on rails along side gantries. Stockyards normally are serviced by gantry cranes (Fig. 32.14).

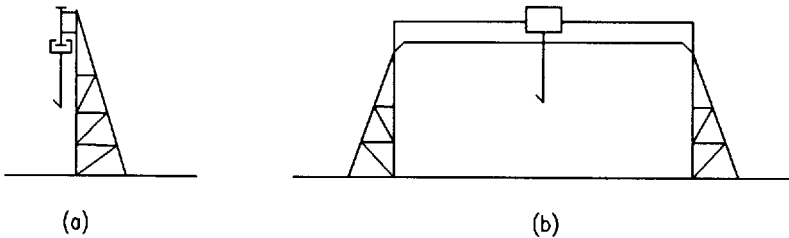


Fig. 32.14 Gantry cranes: (a) single underslung, (b) EOT

### 32.6.2 Conveyor systems

The use of factory automation is increasing the use of roller conveyor systems for moving main components. The roller conveyors can be designed so that they move steel between automated work centres either laterally across the workshop or longitudinally along it. The modern conveyor systems are computer controlled and bring steel accurately into position for the work centre activity to be performed. An example of a roller conveyor system is shown in Fig. 32.15.

Roller conveyors are suitable for steel which does not need turning and does not have cleats or brackets attached to it. Assembly work is not performed on conveyors but the assembly work benches are fed with components from conveyors or cranes.

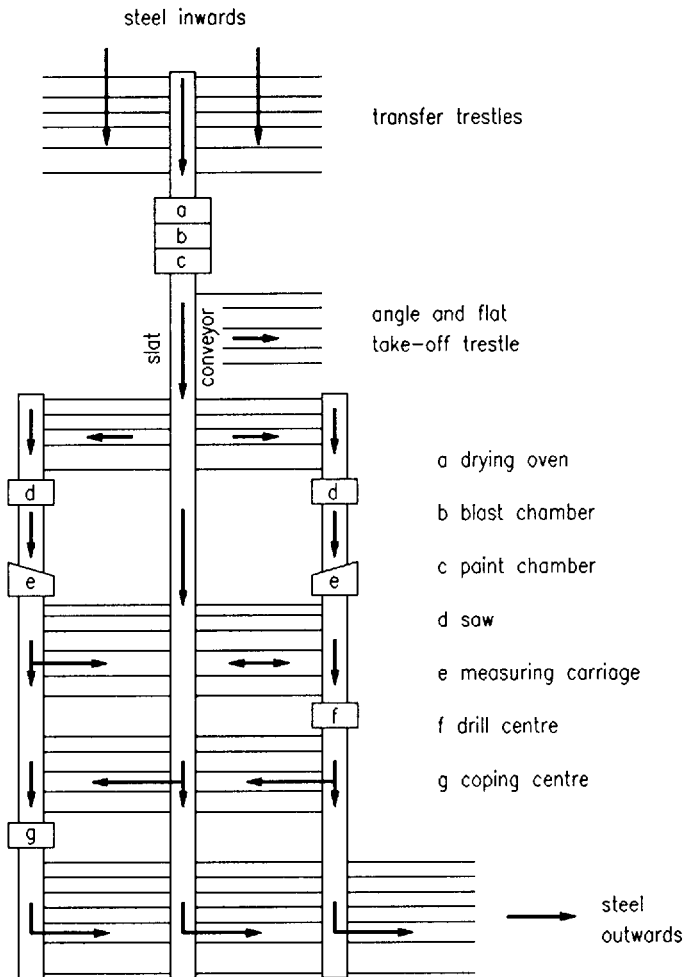


Fig. 32.15 Roller conveyor system

### 32.6.3 Handling aids

Most steelwork assemblies can be picked up easily using chains or strops but the designer should be alert to the possibility of having to provide for temporary lifting brackets suitably stiffened. This may prove necessary where it is important that a component is lifted in a particular way either for stability reasons or for reasons of strength. Lifting brackets need not be permanent of course but should be used and identified for the benefit of the fabricator who has to lift the component in his workshop.

The designer should also be cautious in his provision of welded-on brackets. Flimsy outstands *will* get damaged either in the workshop, during transport or on site. Flimsy brackets should be supplied separately for bolting on at site.

Some components by nature of their design or geometry may require to be lifted in a specific way using strongbacks or lifting beams. The designer must make the fabricator aware of this requirement to avoid possible accidental damage or injury to workshop staff; steel is a very unforgiving material.

The fabricator will normally organize transport of steel from the workshop to site. There are loading restrictions on vehicles in terms of weight, width, height and length.

## 32.7 Quality management

The key activities within any quality management system are quality assurance and quality control. These activities are fully embodied in many industry wide quality standards. While it is not a prerequisite that a manufacturer is registered under a standard based scheme, for appropriate levels of quality management to prevail, it does, however, allow specifiers to easily assess the relevance of the system under review. As far as design and manufacture of structural steelwork is concerned, there are a number of standards which apply. These standards are the basis for the formulation and implementation of appropriate quality management systems. British Standard 5750 provides an excellent basis for a system to be applied in structural steelwork manufacturing and design. The various parts of the standard give the opportunity for fabricators to develop quality management systems which cover design, manufacture and the erection of structural steelwork. The use of systems based on BS 5750 will allow progression to the International System Standard ISO 9000.

While the use of these standards is commended to those setting up quality management systems, it does not imply any formal recognition that compliance with the standard has been met. Formal recognition can be obtained by application for assessment of the quality management system by an independent body. The British Standards Institution will perform this assessment and provide registration to those companies which can successfully demonstrate compliance with the standard. Other registration schemes in the steelwork industry are run by Lloyd's



and Steelwork Construction Quality Assurance Ltd. Within the quality management system there must be written procedures to be followed which will give the basis for adequate QA and QC. A brief description of some of these relevant to the fabrication of structural steelwork are given below.

### 32.7.1 Traceability

It is necessary to demonstrate that both materials and manufacturing processes can be traced by a clear audit trail. This aspect of quality management allows the specifier to determine the source of material for the product he receives and the origin of workmanship. This is particularly important when a defect is discovered. In terms of fabrication, the materials should have the support of documentation from the steelmaker in the form of mill certificates. Suppliers of other materials or consumable items such as bolts, welding electrodes, etc., will also be required to give details which show appropriate manufacturing data. The fabrication process involves workmanship and evidence should be maintained which traces the source of workmanship on each item.

### 32.7.2 Inspection

This is a prime area of quality control. It is important that quality inspectors are independent of workshop management, that is they must be made responsible to a higher level of management in the company which is not concerned with the production of fabricated steel in the workshop. They may report to the quality manager of the company who in turn may report to the managing director. It is also important that all inspection activities are part of a predefined quality plan for the job in question. There should be no opportunity for the level or extent of inspection to be decided upon an *ad hoc* basis. The quality plan will define levels of inspection required and when the inspection is to take place, typically:

- (1) inspection of incoming materials or components,
- (2) inspection of fabricated assemblies during and/or after fabrication,
- (3) inspection of finished products prior to despatch,
- (4) calibration of measuring equipment,
- (5) certification of welders.

### 32.7.3 Defect feedback

At some stage or another, there will be occasions when defects are discovered in the fabricated item. This may be during inspection or on site. It is important that

the defect is reported and the quality management system must cater for this. The report should be formal and it must identify the defect and possible cause. This report is then acted upon to prevent recurrence of the defect. The audit trail of traceability and inspection should highlight the actual source of the defect and this may be corrected by defined and planned actions.

#### 32.7.4 Corrective action

All defects will cause corrective action to be taken. This action may take the form of revised procedures but more commonly will involve a process change. The most important corrective action is training as many defects stem from a lack of understanding on the part of someone in the production cycle. An important part of the prevention of recurrence of defects is trend analysis. Defects are recorded and trends studied which may highlight underlying problems which can be tackled. Occasionally, a finished product does not fully comply with the client's requirements and an approach may be made to determine if the product is suitable. While this process is going on the offending items must be put into quarantine areas which clearly distinguish them from others which do conform to requirements.

#### Further reading for Chapter 32

- British Standards Institution (1984) *Specification for arc welding of carbon and carbon manganese steels*. BS 5135, BSI, London.
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- Pratt J.L. (1989) *Introduction to the Welding of Structural Steelwork*, 3rd edn. SCI Publication 014, The Steel Construction Institute, Ascot, Berks.
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# Chapter 33

## Erection

by HARRY ARCH

### 33.1 Introduction

If a structure is to be erected, stage by stage, safely, within the shortest possible time and at the lowest possible cost, then positive action is required from all the parties concerned. The first step is for the designer to have clearly in mind the means by which it is to be erected. The second step is to convey these ideas to the fabricators and the erectors through an initial method statement.

Notes on the drawing and in the documentation to indicate where erection should start in order to establish initial stability are essential, as is a statement indicating the need for any temporary support or stiffening in cases where instability would result from omission or early removal of the temporary support or stiffening. The method which is decided upon should conform with the intention of the designer of the structure wherever possible. If the eventual decision is for an alternative method to be used, then that new method must be fully documented in order to satisfy all the parties involved that it is acceptable. The agreed method statement is used, together with other, more detailed, planning documents, to monitor the work as it progresses.

The number of pieces to be lifted into place, their average height, and the weight, size and final position of the maximum lift determine the capacity of the cranes deployed on site. Attempts should be made to optimize the choice by arranging that every lift matches the capacity of the crane at that particular jib length and radius. Every time a hook goes up with less than its rated load the crane is being under-utilized.

One option which has the dual advantages of reducing the number of small lifts and man hours at risk to be spent at height, is to consider sub-assembly at ground level. To be fully effective the connections for a sub-assembled unit must be considered at the design stage in order that all the splices can be easily made with entry from one direction, from above, as the sub-assembly is lowered into place.

Another option is to lift components in bundles for distribution and fixing from a high-level dispersal point.

Whether sub-assembly techniques are being considered or not, it is vital that the positioning of splices is fully considered. How is safe access to be arranged; can a welded connection be arranged to reduce the amount of positional welding? Could a bolted joint be substituted to produce a more economical connection, and one which is less susceptible to the influence of weather, less sensitive to

operator skills and easier to monitor and inspect using less sophisticated methods and equipment?

Finally, the method eventually selected must take account of the possibility that other contractors may have to be on site at the same time, using the same access routes and possibly even the same cranes. They may have to obtain access through parts of the structure left open by the omission of important structural members. Steps must be taken to ensure that the structure remains stable throughout such incomplete phases particularly where loads are to be imposed on the structure when components are missing. Members which are redundant in the completed frame can be vital during the erection phases.

Any temporary works which are needed to ensure the stability of the incomplete frame must receive full design attention, including foundations, connections, the permanent member to which they are connected, and the eventual removal method and timing within the overall programme.

### **33.2 The method statement**

Guidance Note GS 28 Parts 1 and 2, produced by the Health and Safety Executive, contains full details of the contents of a method statement. The main items are:

- (1) Arrangements for scheme management, including co-ordination and the responsibilities and authority of supervisory personnel at all levels
- (2) Erection sequences, noting the scheduled starting position, or positions if phased construction is required
- (3) Methods of ensuring stability at all times of individual members (including columns) and sub-assemblies, as well as the partially erected structure
- (4) The detailed method of erecting the structure, the erection scheme, devised to ensure that activities such as lifting, unslinging, initial connecting, alignment and final connecting can be carried out safely
- (5) Provisions to prevent falls from height, including safe means of access and safe places of work, special platforms and walkways, arranging to complete permanent walkways early, mobile towers, aerial platforms, slung, suspended or other scaffolds, secured ladders, safety harnesses and safety nets
- (6) Protection from falls of materials, tools and debris by the provision of barriers such as screens, fans and nets
- (7) The provision of suitable plant (including cranes), tools and equipment of sufficient strength and quantity
- (8) Contingency arrangements, for example, against a breakdown of essential plant, or if components are delivered out of sequence
- (9) Arrangements for delivery, stacking, storing, movement on site, on-site fabrication or pre-assembly and the siting of offices and mess rooms
- (10) Details of site features, layout and access, with notes on how they may affect proposed arrangements and methods of working.

These items enable the requirements of the Health and Safety at Work Act of 1974 to be satisfied. A complex job may require a series of complex method statements, each covering an aspect of the work.

The statement, or statements, should form a single document capable of modification if necessary, indexed for easy reference. It should follow a logical sequence, be completely unambiguous, refer to components or items of work using their drawing identification marks and exact location, and be dated and marked with modification letters, as is a drawing, in order to prevent the use of an out-of-date statement.

Repetitive or 'standard' jobs can be covered by standard sheets which should identify any critical stages of the work that they detail.

### 33.3 Programme

#### 33.3.1 Introduction

Construction planning begins with an understanding of the purpose of the project, and with a full and detailed evaluation of the site including ground conditions, the location of the site and what plant is available in the area. In the case of a building the initial site evaluation should consider whether there will be space around the building for cranes to work, whether they will have to climb with the building's own framework or whether tower cranes may be utilised.

The management team charged with responsibility for the initial design proposals must not produce their documents without taking account of all the contexts in which the project will have to be built as well as those in which it will operate.

Most aspects of construction work are seriously affected by weather; earth-moving by wet weather, concreting by cold weather, and steel erection by high winds. Considerations of extreme temperature and wind conditions can, for example, affect decisions about the use of site welding in major connections. Initial programming of the construction phases of a project must take account of these factors otherwise a programme can easily become meaningless but still have contractual implications.

It seldom happens that an erector has a free hand in the determination of the period of time within which his work on site must be completed. The client or his representatives will have integrated the steel erection phase with his overall programme for the total project. As shown in Fig. 33.1 there will be interlocking work processes to consider, starting with foundation completion and ending with following trades on floors and façades, etc. There may also be periods when access must be given to other contractors who have to work within the erection area, for instance, to install the boiler drums in a power station frame. A further particular case concerns railway possession periods.

Precast floor panels which the designer may have relied upon to give resistance to wind loading in the completed building have to be programmed too, as do the temporary bracings which will be needed before the floor panels can take up the

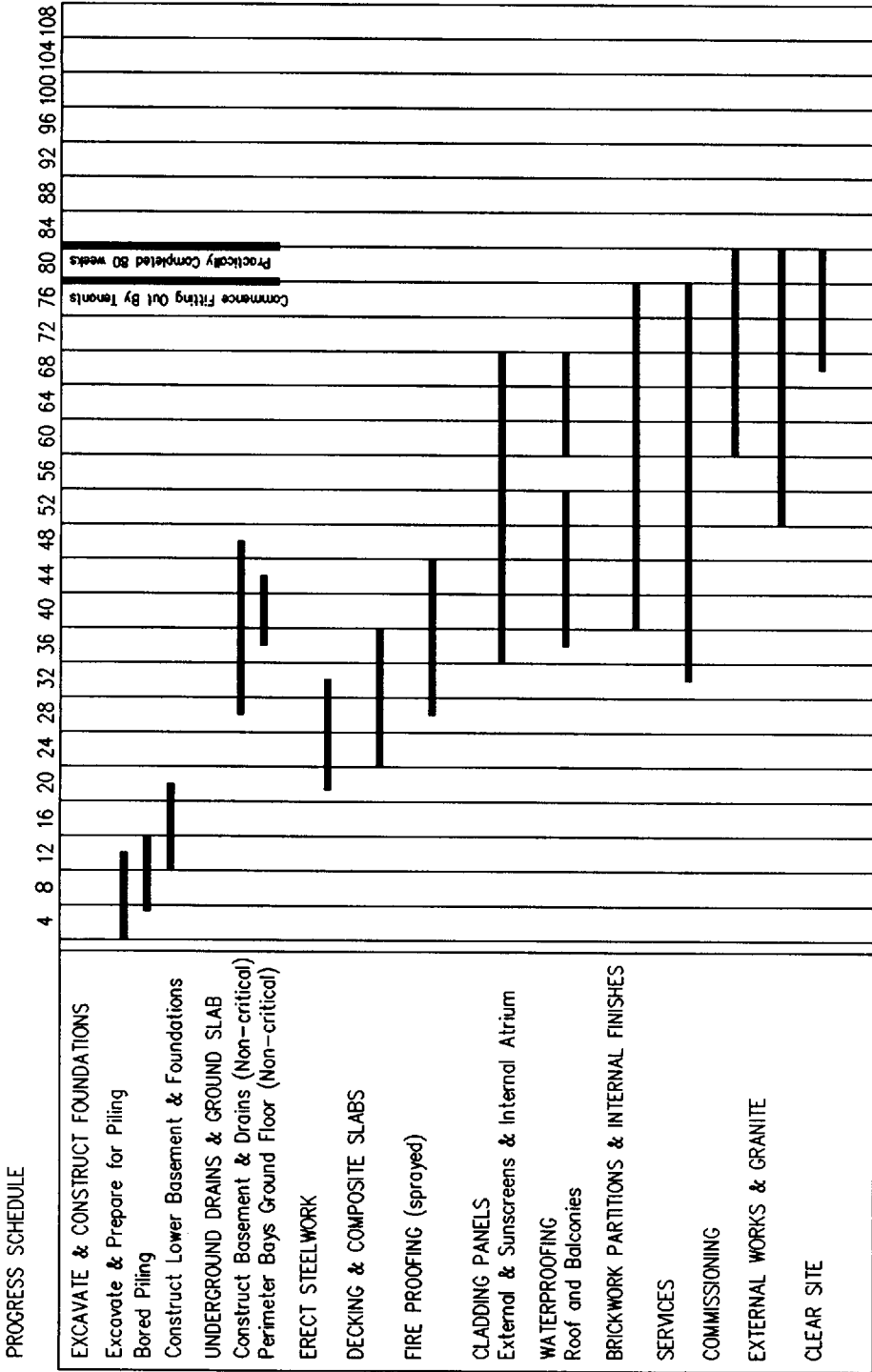


Fig. 33.1 Construction programme for typical multi-storey building (in weeks)

load. All of the foregoing conditions, and more, form the constraints within which the erectors' programme must be fitted.

### 33.3.2 Controlling the flow of materials to site

A job can only proceed smoothly on site with a regular flow of the materials required for its construction. The preparation of a delivery schedule based on a compromise between expected outputs, possibly from more than one fabricator, and the demands of the site programme is an early priority for the management team who must also consider the need to ensure early stability of the frame.

The almost inevitable lack of correlation between these demands often makes the provision of a stockyard on a site a necessity. A stockyard is additionally a surge tank which can absorb, for example, variations in transport or shipping times due to outside influences which, without a buffer stock of material, would leave the erection squads unemployed. As much as four weeks' erection work may have to be provided by the stockyard capacity.

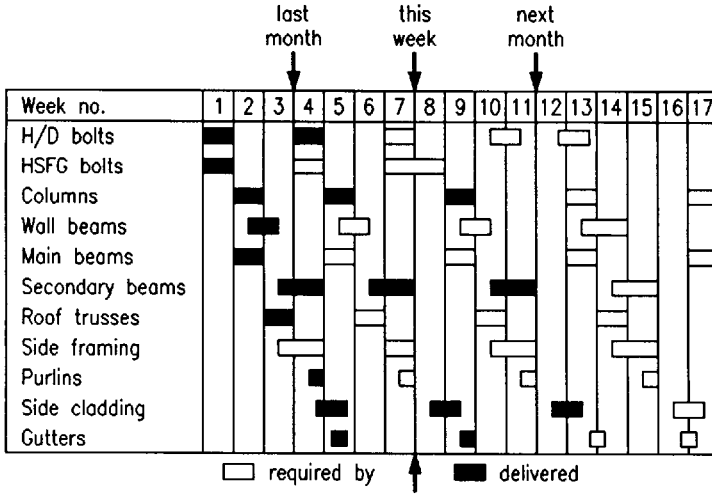
It may be found that the demands of the site and its sequenced delivery requirements will be beyond the capability of any one fabricator. Hence another early role of management is to plan the schedule for all the material requirements. Typically this will involve a purchasing department using specifications provided by the designers and detailers, working to the demands of the programme and the original cost estimate for the supply of each item required within the financial limit, to define delivery requirements.

The day-by-day monitoring of the actual performance of the suppliers in terms of the quality of the work, its adherence to the specifications of workmanship and tolerance and adherence to programme is a management responsibility. A typical delivery demand and monitoring chart is shown in Fig. 33.2 from which it can be seen that the job is short of bolts and side framing, main beams and wall beams are critical, but the site is clogged with unwanted columns, secondary beams, side cladding and gutters.

In addition it is always helpful as a visual check for all concerned in the office and eventually on site, to mark up a general arrangement drawing as each marked piece is received on site and stored, or taken to the erection front. The bolt lists prepared by the drawing office are similarly broken down into phased requirements and used to order and monitor deliveries into the site store.

### 33.3.3 Cash flow and material monitoring

There are two reasons for making a delivery schedule and then monitoring it. The first is to ensure that the site is not flooded with unwanted components while being at the same time unable to erect anything through the lack of an essential



items required  but not delivered  cause delay and waste money  
 items delivered  before required  divert resources and waste money

Fig. 33.2 Site delivery schedule

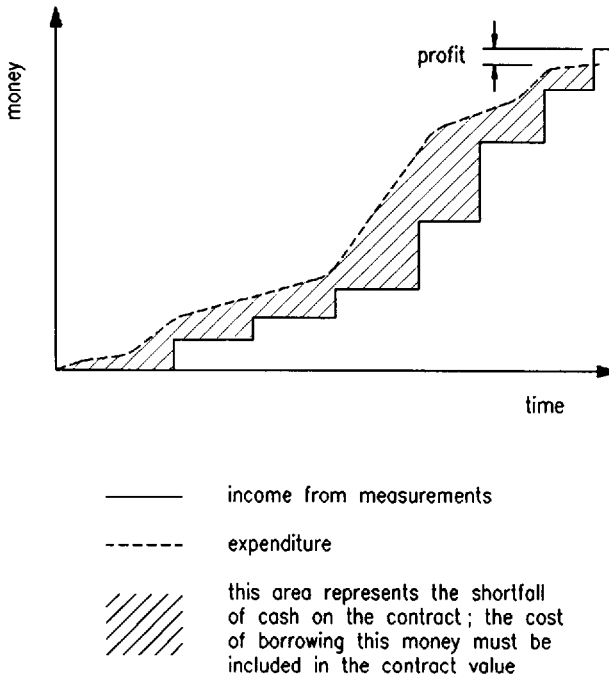


Fig. 33.3 Cash flow diagram



part. The second, which is often more important especially on a large job, is the determination of the cash flow out of, and into, the project account.

Cash flow is determined by a 'cash flow diagram' which plots cash requirements and availability month by month throughout the expected duration of the job, and compares the two (see Fig. 33.3).

The cost of the design, of the steel bolts, labour involved in fabrication, transport and erection are all items which produce the graph of expenditure. The other line charts the income expected from the stage payments which are made as work progresses.

As far as a client is concerned these payments may typically be after the completion of significant phases of construction. His income line will not begin until the whole is completed and his revenue starts to flow. The contractor's cash flow will be generated by stage payments as the job progresses.

The amounts by which expenditure exceeds income from month to month have to be financed; the cost of this finance is an important factor in the build-up of the cost of the project. There may additionally be considerations of possible fluctuations in exchange rates to be taken into account where part of the work has to be carried out in a different country.

## **33.4 Cranes and craneage**

### **33.4.1 Introduction**

On a large job cranes of varying size and capacity are provided to perform the various tasks: a heavy one for the main columns and a smaller one for the side framing posts and angles for instance. The number of pieces to be lifted in any one working period determines the number of cranes required to achieve the desired rate of working. In practice the choice of crane type and capacity is a compromise, with efforts being made to get as near to the optimum as possible.

In order to decide on a crane layout it is necessary to prepare a sketch or drawing of each critical lifting position showing, on a large scale, the position of the crane on the ground, the location of the hook on plan, the clearance between the jib and its load, and between the jib and the existing structure as the piece is being landed in its final position. These drawings will enable a check to be made of the match of each crane to its load, of the ability of the ground under the crane to sustain the crane with its load, and clearance to lift the component and place it in position. Of particular importance is the clearance needed by the tail of the crane as it slews. A series of these drawings will rapidly confirm whether a particular crane is suitable. If there is an anomalous heavy lift in the series, the designer can be asked whether a splice position can be moved to reduce weight.

Reports on overturned cranes and crippled jibs bear adequate testimony to the need to plan and to the extent to which it is neglected. The Code of Practice CP 3010 *The safe use of cranes* indicates clearly the dangers of improper use.

There are two ways in which the ingenuity of the erection planner can produce an economic scheme; first in his choice of crane and second in the organization of getting the material under the hook and up into place.

### 33.4.2 Types of crane

Cranes used on steel erection sites are of two main types: those described as 'mobile' which arrive on site ready to be used, needing only to have their jibs extended to the length required, and those that are delivered to site piece-small which have to be assembled before they can be used. They are fully described and their safe use is defined in CP 3010 *The safe use of cranes*.

#### *Mobile cranes*

This group includes truck, or wheel-mounted, and tracked cranes. Truck-mounted cranes are able to travel on the public roads under their own power, but with their jibs shortened. Mobile cranes mounted on crawler tracks are not permitted to travel on the road under their own power. A truck-mounted crane is a relevant

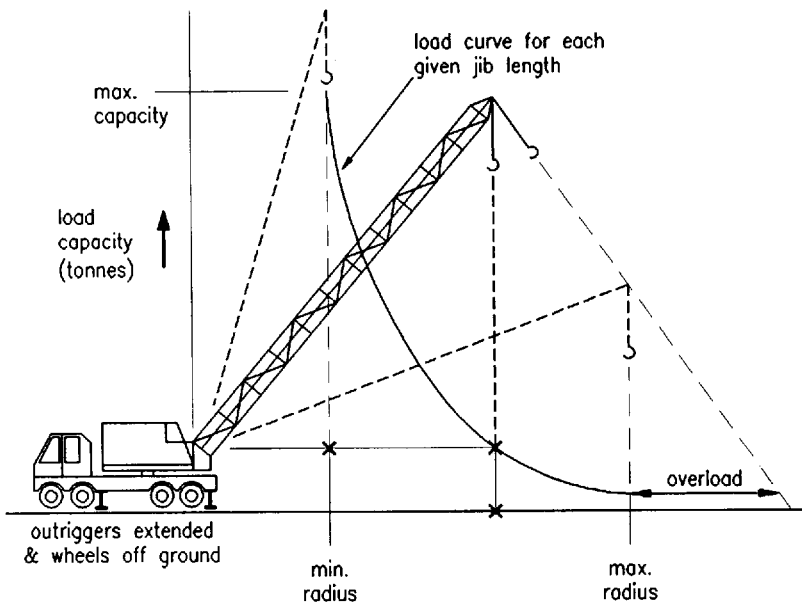


Fig. 33.4 Safe load diagram for a mobile crane

choice if a crane is only required on site for a short time; it can come and go relatively easily. However if a crane is to be on site for longer, the high transportation costs of moving a crawler crane around the country can be justified. The real advantage of a crawler crane is that its weight plus the reactions from the load being lifted are spread more widely by its tracks but it does not have the added stability of a truck-mounted crane with its outriggers set.

Both types are typically part of the erection fleet owned by steel erection and plant hire companies. The decision to hire from a plant hire company is often determined by the geography of the site – is it close to a plant hire company's yard or is it close to the contractor's own plant depot; is the crane to be used for short or long duration; and is the lift for which the crane is required one of a series or simply a 'one-off'?

Capacities of mobile cranes normally range up to 50 tonnes but exceptional cranes can lift up to 300 tonnes. Figures 33.4 and 33.5 provide performance data for a typical 25-tonne crane. It is most important to note that the rated capacity of a mobile crane and the load which can be safely lifted are two very different things. The maker's safe loading diagram for the crane must always be carefully consulted to see what load can be lifted with the jib length and the radius proposed. It is essential that a mobile crane is used on level ground so that no side loads are imposed on the jib structure.

| main boom capacities (tonnes) – through full 360° circle slew – with outriggers fully extended |                               |                          |                          |                          |                          |                          |                          |
|--|-------------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| boom length  |                               |                          |                          |                          |                          |                          |                          |
| radius<br>in<br>metres   | 10.07 m<br>fully<br>retracted | 10.07 m<br>to<br>12.50 m | 12.50 m<br>to<br>15.00 m | 15.00 m<br>to<br>17.50 m | 17.50 m<br>to<br>20.00 m | 20.00 m<br>to<br>22.50 m | 22.50 m<br>to<br>24.57 m |
| 3.0 m  | 25.40                         | 20.70                    | 20.10                    | 20.10                    |                          |                          |                          |
| 3.5 m  | 22.00                         | 20.00                    | 19.00                    | 18.80                    | 16.00                    |                          |                          |
| 4.0 m  | 19.50                         | 18.00                    | 17.80                    | 17.60                    | 15.50                    |                          |                          |
| 4.5 m  | 17.00                         | 16.80                    | 16.70                    | 16.50                    | 14.90                    | 12.70                    |                          |
| 5.0 m  | 15.30                         | 15.30                    | 15.30                    | 15.00                    | 13.90                    | 12.30                    | 10.40                    |
| 6.0 m  | 13.00                         | 12.80                    | 12.40                    | 12.40                    | 12.20                    | 11.60                    | 9.80                     |
| 7.0 m  | 10.50                         | 10.50                    | 10.50                    | 10.50                    | 10.50                    | 10.50                    | 9.40                     |
| 8.0 m  |                               | 8.30                     | 8.30                     | 8.30                     | 8.30                     | 8.30                     | 8.30                     |
| 10.0 m   |                               | 5.35                     | 5.35                     | 5.35                     | 5.35                     | 5.35                     | 5.35                     |
| 12.0 m   |                               |                          | 3.85                     | 3.85                     | 3.85                     | 3.85                     | 3.85                     |
| 14.0 m   |                               |                          |                          | 2.80                     | 2.80                     | 2.80                     | 2.80                     |
| 16.0 m   |                               |                          |                          |                          | 2.15                     | 2.15                     | 2.15                     |
| 18.0 m   |                               |                          |                          |                          |                          | 1.70                     | 1.70                     |
| 20.0 m   |                               |                          |                          |                          |                          | 1.30                     | 1.30                     |
| 22.0 m   |                               |                          |                          |                          |                          |                          | 0.90                     |

Fig. 33.5 Safe load charge for a 25-tonne capacity crane

*Mobility for non-mobile cranes*

Non-mobile cranes can be made mobile, but only normally by mounting them on rails. This has two advantages: the positioning of the crane can be more easily dictated and controlled, and the loads transmitted by the rails to the ground are in a precisely known location. Many a crane has collapsed because of insufficient support underneath but most rail-mounted crane failures have occurred from overloading.

Where the crane is to work over complex plant foundations the rail can be carried on a beam supported, if necessary, on piles especially driven for the purpose. If the rail is supported only by a beam on sleepers directly on the ground the load can be properly distributed by suitable spreaders. In either case the conditions will have been properly considered and designed for, instead of the often rather uninformed trust which is put in the capability of the ground to support a mobile crane and its outriggers.

*Non-mobile cranes*

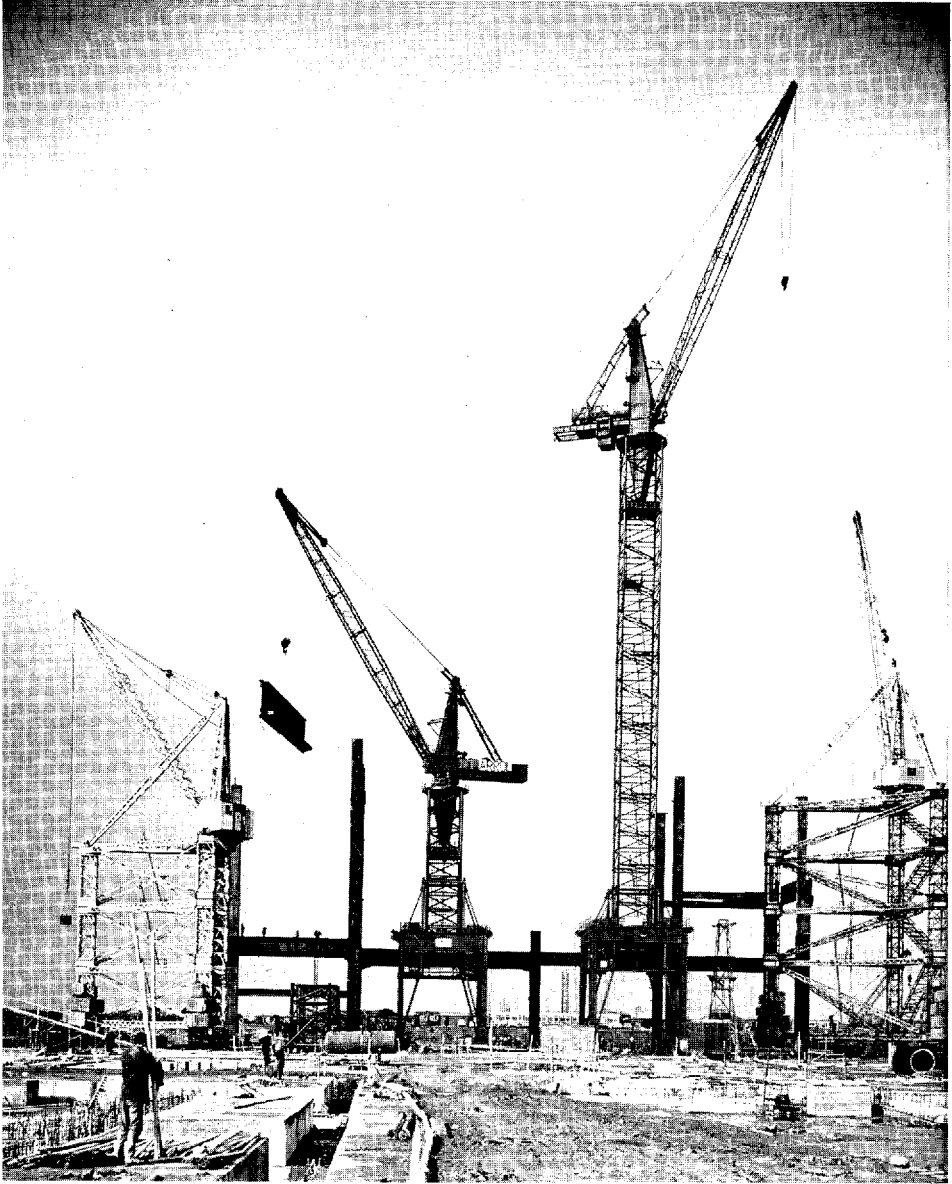
Non-mobile cranes are generally larger either in their capacity to reach to great heights, or in their capability of lifting their rated loads at a useful radius. It is in both of these respects that the mobile crane is deficient.

There are two main types of non-mobile cranes (see Fig. 33.6), the tower crane and the derrick; with each their size precludes the possibility of the crane arriving on site other than in pieces. So the disadvantage of a non-mobile crane is that it has to be assembled on site. Having been assembled it must receive a structural test in addition to the winch and stability tests required for all cranes before they can be put into service.

Derrick cranes, once very common, are still occasionally used where their particular advantages are relevant. The big advantage of a scotch derrick is its simplicity. It can be built using relatively unskilled labour, is easy to maintain and is less susceptible to breakdown than its more complicated sisters. Its disadvantages are that it takes up a large ground area, requires two standard gauge railway tracks for travelling and needs a great deal of ballast which has to be loaded on to the ends of its 'lying' and 'raking' legs. It also requires a secondary derrick on a lower gabbard, or supporting framework, for its erection.

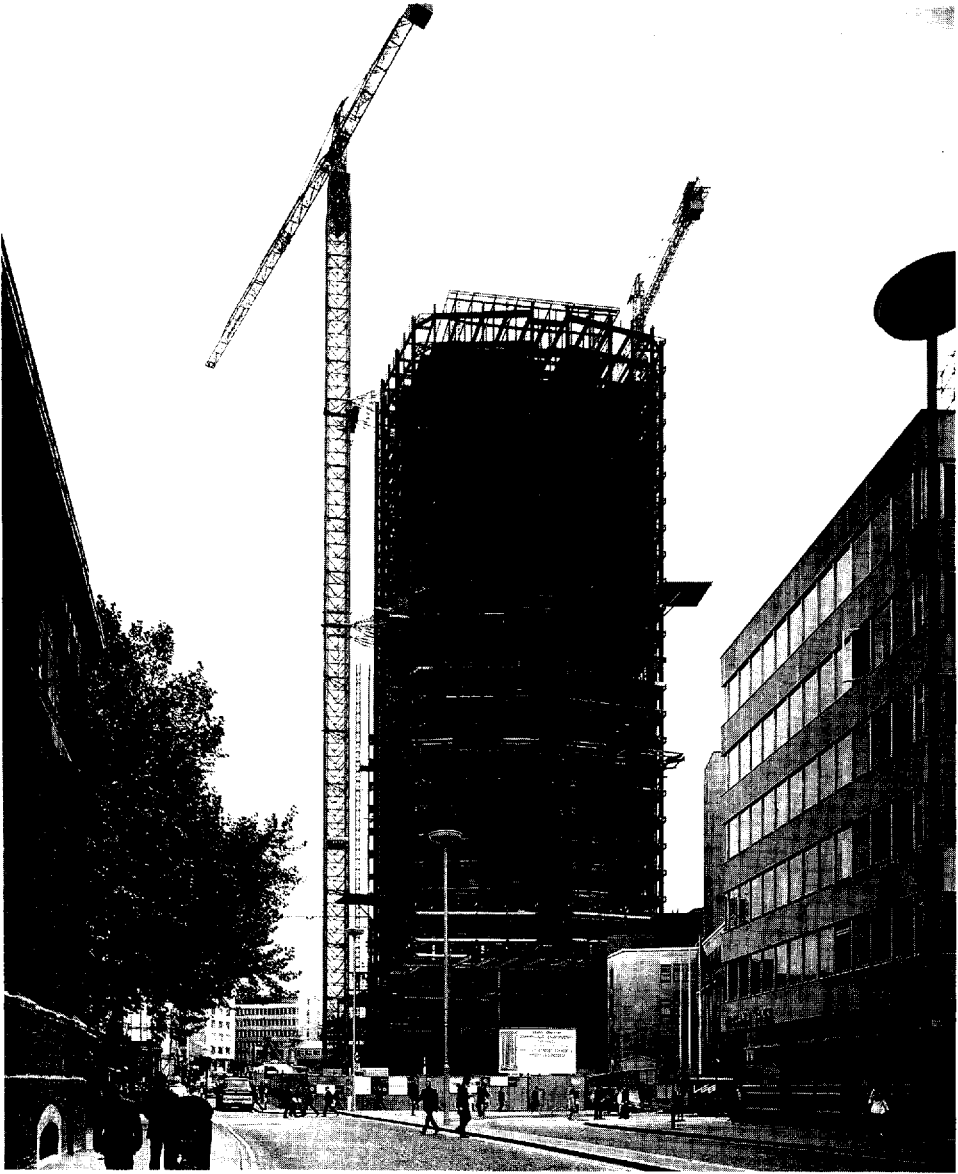
Where a tower crane is available with sufficient height and lifting capacity, it has several advantages (see Fig. 33.7).

- (1) It requires only two rails for it to be 'mobile', and these two rails, although at a wide gauge, take up less ground space than a derrick.
- (2) It carries most of its ballast at the top of the tower on the slewing jib/counter balance structure, and so very much less ballast is needed at the bottom – indeed in some cases there is no need for any ballast at all at the tower base or portal.



*Fig. 33.6* Types of non-mobile cranes: tower cranes and derricks

- (3) Because the jib of a tower crane is often horizontal, with the luffing of a derrick jib replaced by a travelling crab, the crane can work much closer to the structure and can reach over to positions inaccessible to a luffing jib crane.



*Fig. 33.7* A tower crane tied to the erected structure

- (4) A tower crane is 'self-erecting' in the sense that after initial assembly at or near ground level the telescoping tower eliminates the need for secondary cranes.
- (5) As shown in *Fig. 33.7* it can be tied into the structure it is erecting, thus permitting its use at heights beyond its free standing capacity.

### *Climbing cranes*

The wide spread of the reaction points needed to stabilize either a scotch derrick, or its first cousin the guy derrick, becomes an advantage if the crane is to be mounted on a structure. In a guy derrick, the fixed legs of a scotch derrick are replaced by a number of guy ropes arranged radially around the top of the mast, from the bottom of which the jib is mounted in the same way as that of a scotch derrick (see Fig. 33.8).

The guy derrick was for many years the standard method of erecting medium- or high-rise frames where the crane must climb with the structure. The hoisting winch can be remote from the crane structure in a guy derrick while a tower crane or scotch derrick carries its winch with it. The climbing process for the guy derrick is therefore much simplified and the winch power supplies need to be moved less often.

Once a suitable means of climbing a tower crane had been developed it became the standard solution for tall building construction. By arranging connection points at various levels of floor steelwork it is possible to give the tower both support and stability. This, together with the telescoping movements of the inner and outer portions of the tower, enables the crane's own equipment to be used to power the climbing mechanism.

Provided the designer of the framework has been aware of and has made provision in his design for the loads, vibrations and connection points from the crane, there is no limit to how far it can climb. Intermediate load transfer platforms, each with its own crane, can be provided if the capacity of the winch drum on the crane is unable to provide the full length of rope required for the height of the overall lift.

### *Cranes for the stockyard*

Stockyard cranes have to work hard. The tonnage in the job has to be handled twice in the same period of time, often with many fewer cranes. It is therefore important that cranes be selected and sited carefully to ensure maximum efficiency.

It is usual to arrange for stockyard cranes to be given a short length of track to enable them to cover a greater area than would be possible under a fixed crane. Tracks use up valuable area in a stockyard so the choice often falls on the goliath type crane (see Fig. 33.9). Running on only a single rail at each end it uses the minimum possible of that valuable space; furthermore only part of its coverage needs to be dedicated to actual transference of steel from and to the trucks, wagons and trailers. It also does not suffer the reduction in capacity that is incurred by jib cranes.

Where a contract involves the construction of a piece of industrial plant or a power house, for example, where all the lifts are concentrated in a relatively small area, a goliath type crane can also be used. The crane runs on tracks laid outside the limits of the structure and has sufficient headroom to lift items over the top of



*Fig. 33.8* A guy derrick used as a climbing crane

the unit being built. In exceptional cases such a goliath may be almost in the category of a special lifting device (see Fig. 33.10). One penalty of such an arrangement is that only one hook is available for all the lifts and programming must take this into account.



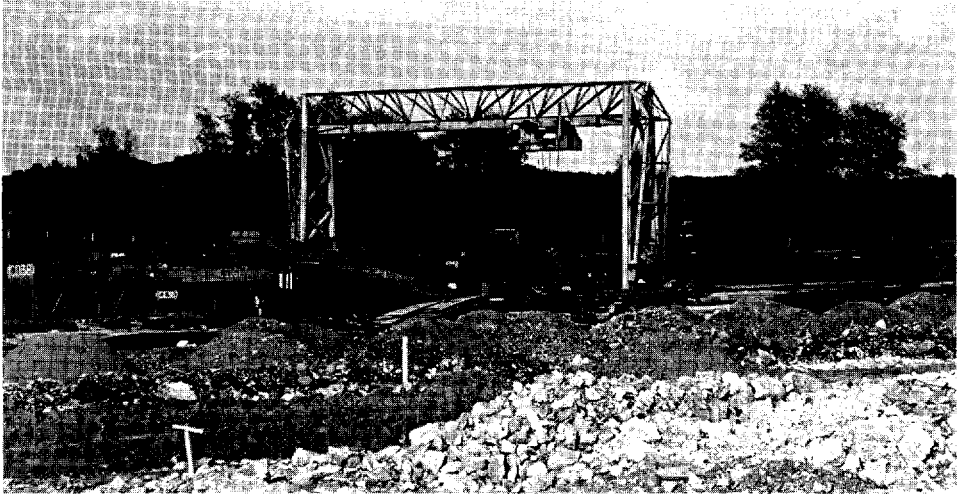


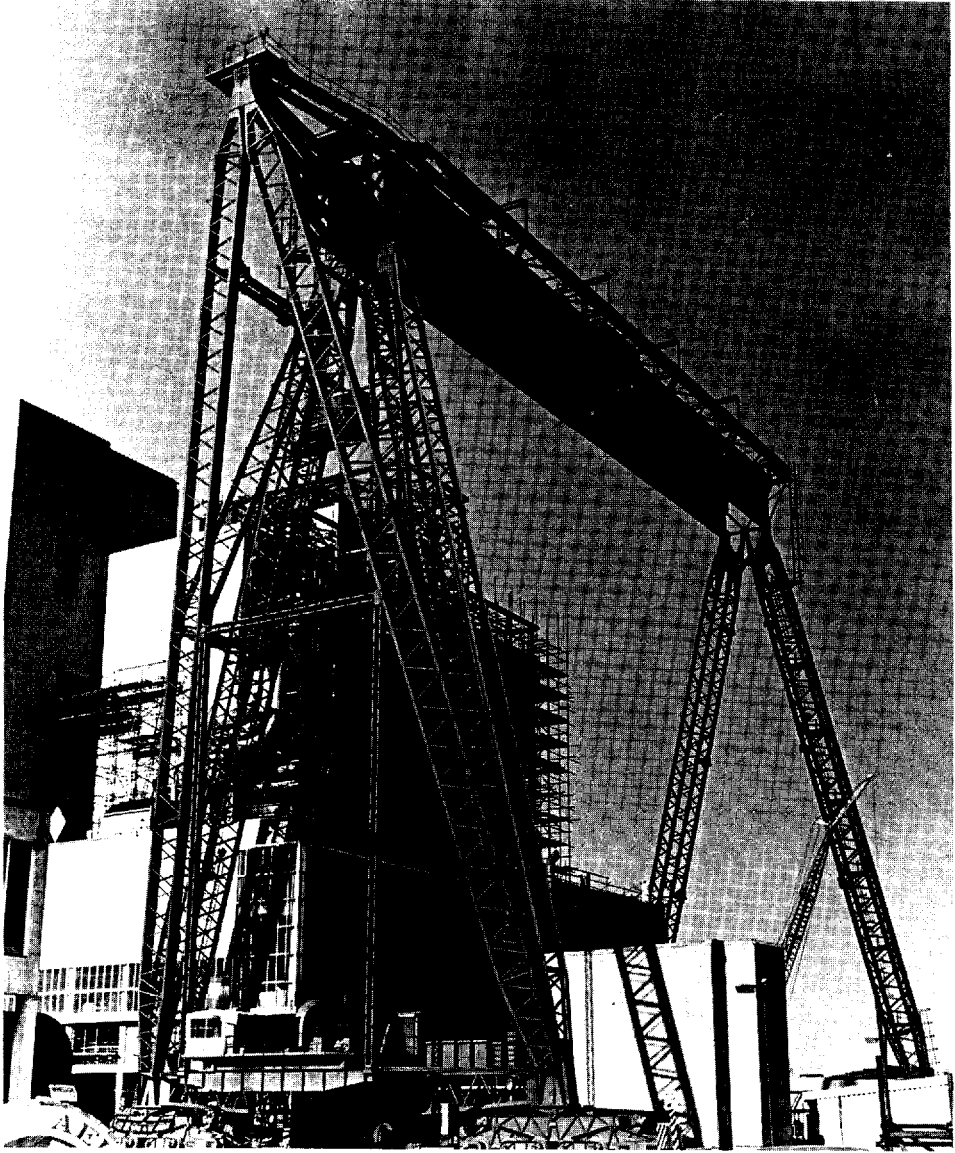
Fig. 33.9 A goliath crane serving a stockyard

### 33.4.3 Other solutions

If there is no suitable crane, or if there is no working place around or inside the building where a crane may be placed, then consideration must be given to the need for a special mounting device for a standard crane, or even a special lifting device to do the work of a crane, designed to be supported on the growing framework. In either event this is an example of a situation where the closest collaboration between the designer and the erector members of the management team is of paramount importance, and where a lack of adequate communications can lead to trouble.

Once the decision to consider the use of a special lifting device has been made, a new range of options becomes available. The most important of these is the possibility of sub-assembling larger and heavier components so reducing the number of man hours worked at height. This is particularly true in the case of bridgework, where substantial sums which would otherwise have to be expended on other temporary supports and stiffening can possibly be saved. The big disadvantage is that the special lifting device being considered is often so special that it is unlikely to be of use on another job and so the whole cost has to be written off on the one job for which it has been initially designed. (See Fig. 33.11.)

At the cost of only a slight increase in time, and of the labour force needed, it is possible to eliminate the not inconsiderable cost of bringing a crane on to a site where the frame is single-storey. With the help of a winch, powered by either compressed air or an internal combustion engine, and some blocks and tackle, a



*Fig. 33.10* A super goliath covering a complete project

light lattice guyed pole can be used to give very economic erection (see Fig. 33.12). In this instance the pole is carried in a cradle of wires attached at points on the tower. These connection points need to be carefully designed to be sure that they will carry the load and the tower structure will not be crippled.

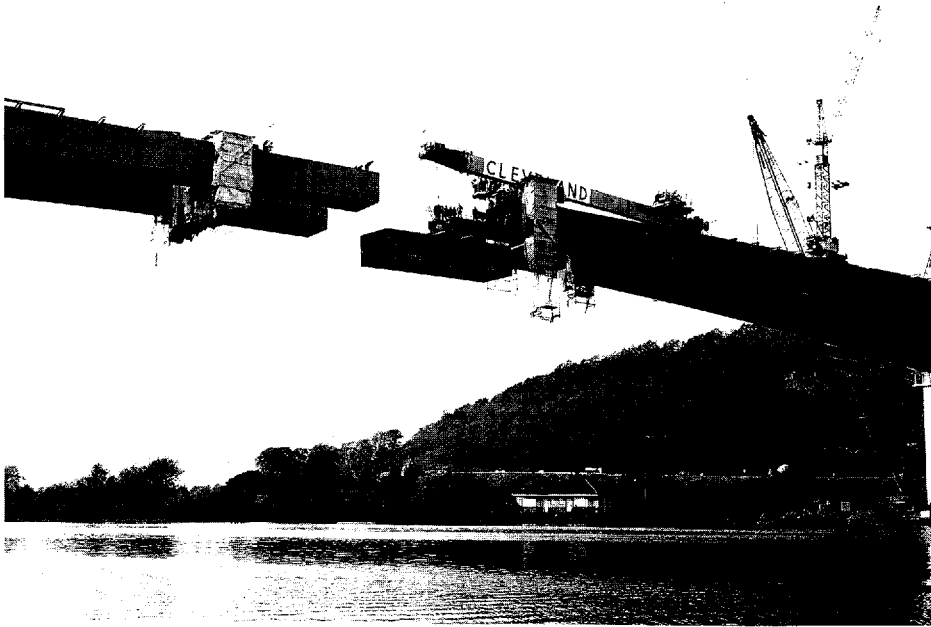


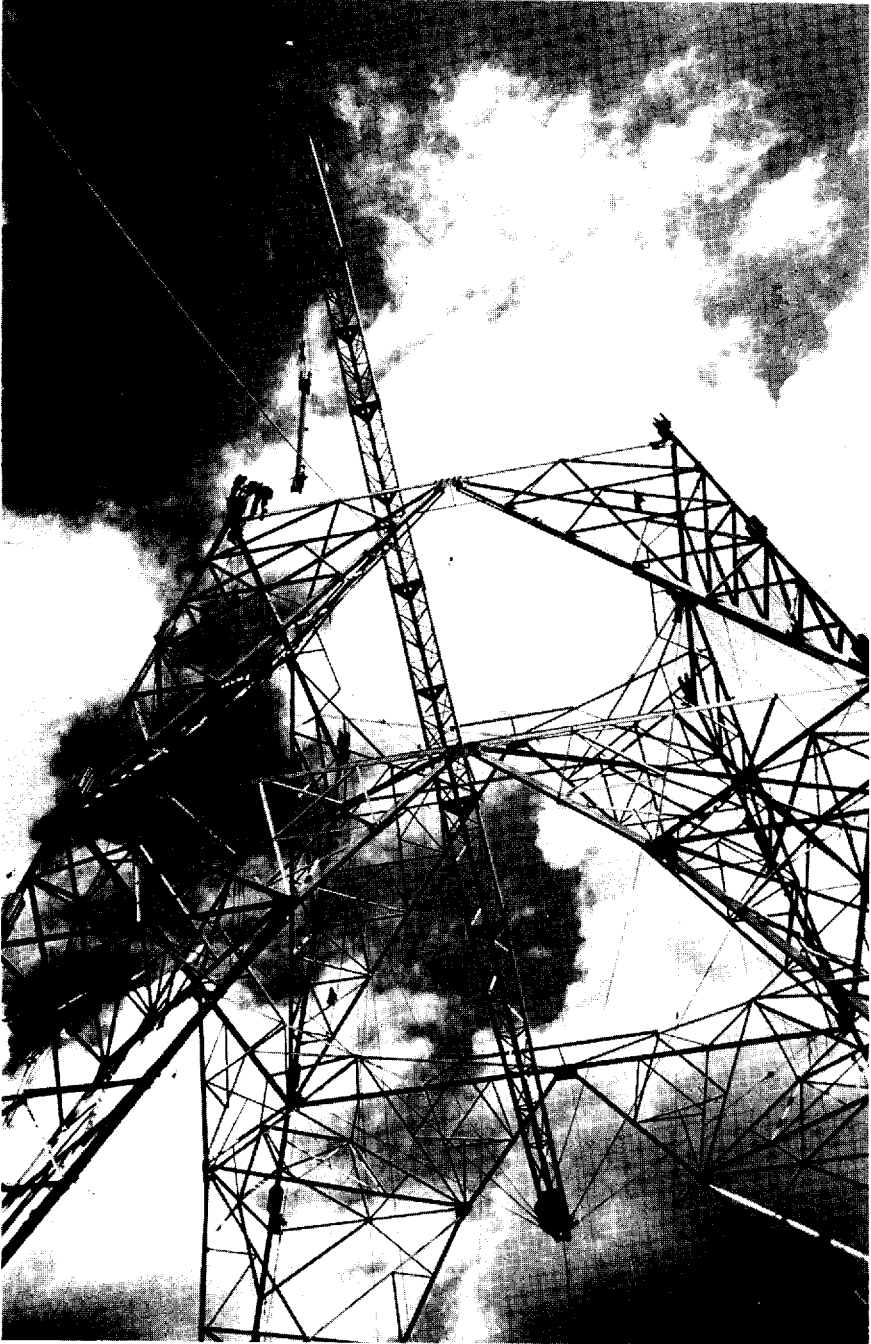
Fig. 33.11 A purpose-made lifting beam for cantilever bridge erection

It is vital that any pole is used in as near a vertical position as possible as the capacity drops off severely as the droop increases. This requires careful planning and the employment of a gang of men experienced in the use of the method.

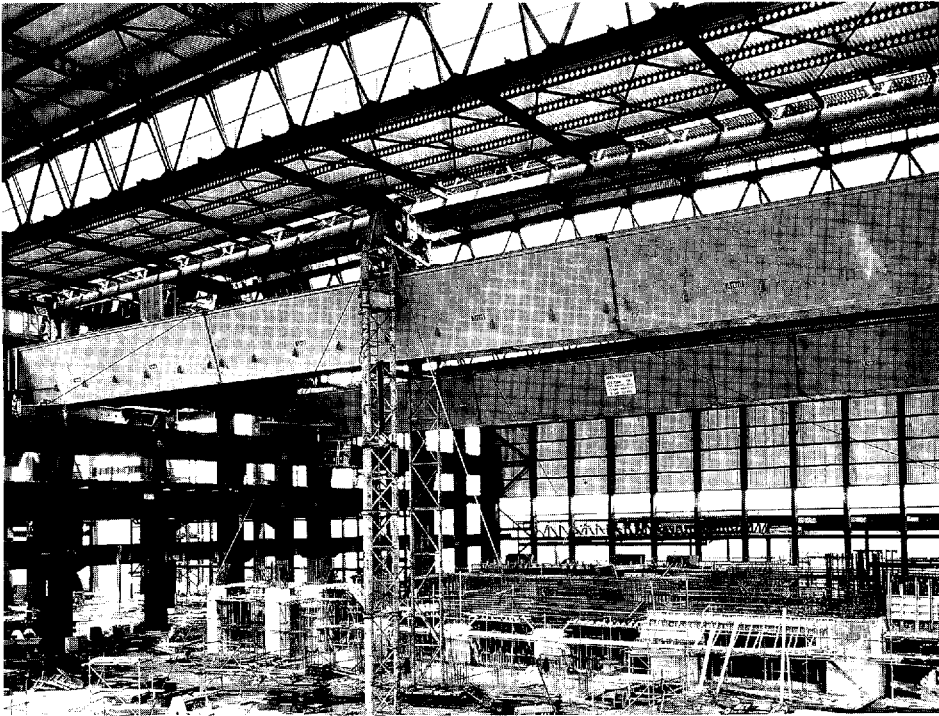
In a different context, pairs of heavier poles provided with a cat head to support the top block of the tackle can be used inside existing buildings to erect the components of, say, an overhead travelling crane, or to lift in a replacement girder (Fig. 33.13). The arrangements for a pole and its appurtenances take up much less floor space in a working bay than a mobile crane, which additionally needs a wide access route and space to manoeuvre itself into position. The method is particularly useful where headroom is restricted.

#### 33.4.4 Crane layout

Having decided on the type, size and number of cranes that are required to carry out the work, each has a designated range of positions relative to the work it is to perform. These positions are then co-ordinated into an overall plan which enables each crane to work without interfering with its neighbours, and at the same time enables each to work in a position where adequate support can safely be provided



*Fig. 33.12* An erection pole used to build a transmission tower



*Fig. 33.13* Two poles connected at their tops and guyed, used to erect a 160 tonne girder

(see Fig. 33.14). This plan will then form the basis of the erection method statement documentation.

A major factor in planning craneage is to ensure that access is available and adequate to enable the necessary quantity and size of components to be moved. On large green field developments these movements may often have to take place along common access roads used by all contractors and along routes which may be subject to weight or size restrictions. On a tight urban site the access may be no more than a narrow one-way street subject to major traffic congestion.

### **33.5 Use of sub-assemblies**

The crane layout shown in Fig. 33.14 makes use of a minimum amount of sub-assembly in the main rafter members of the portal frames, using the area behind the cranes on the erection front. If it has been decided to make use of much larger sub-assemblies on a larger frame, plans are drawn up to incorporate this into the design of the steelwork. The plans must also be incorporated into the erection

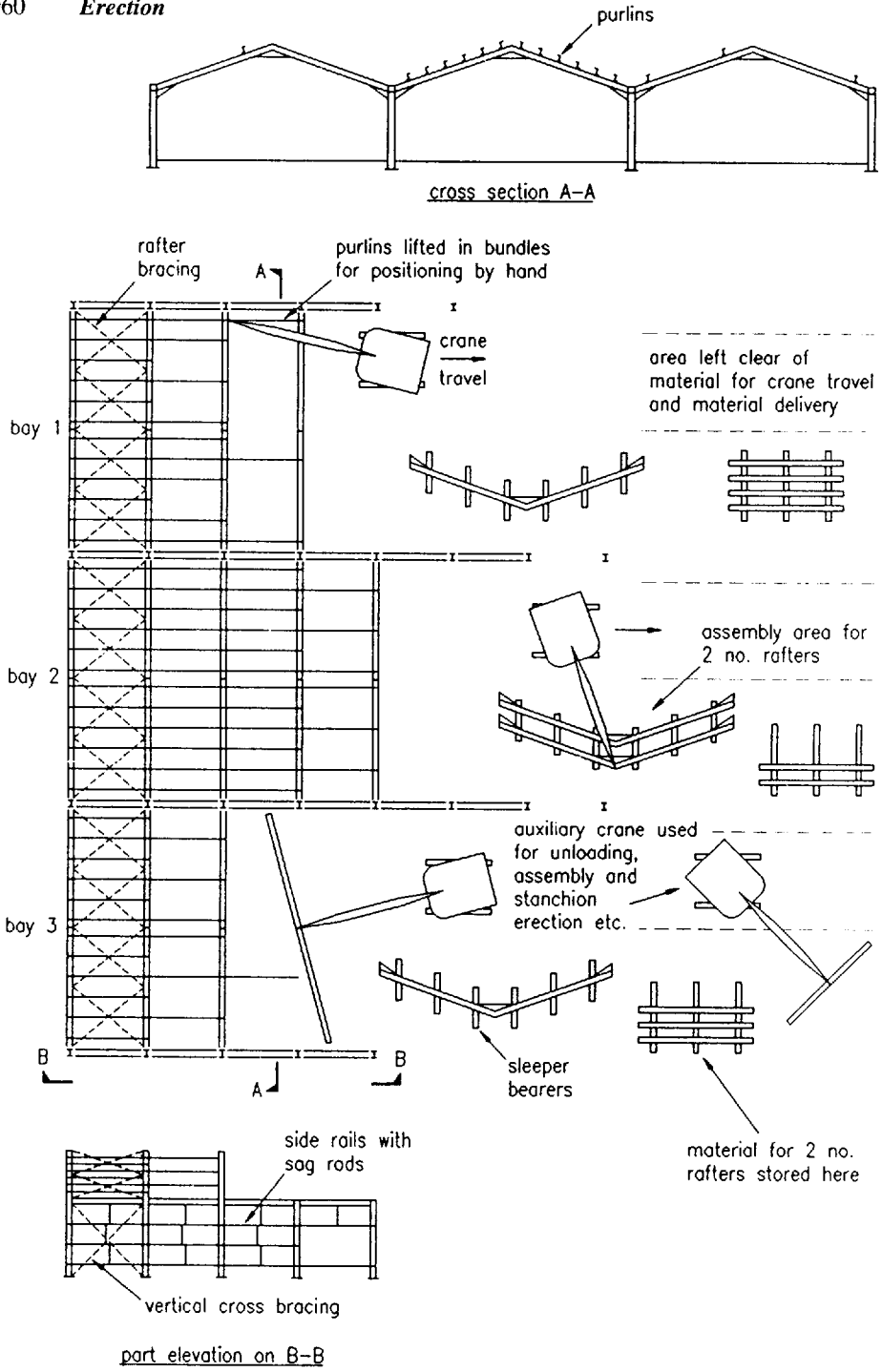


Fig. 33.14 Erection plan for multi-bay portal frame

method statement to show where and how the sub-assemblies are to be put together, transported and erected.

If the decision to sub-assemble has been made there will remain the further question of deciding whether an area in the stockyard is to be dedicated for this purpose, or whether the work will be done behind the cranes on the erection front so that the assembly can be lifted straight off the ground and into position as the crane is moved back.

The most common components to be assembled behind the crane are roof trusses or lattice girders which, because of their size, are almost always delivered to site 'piece small'. However, there is not always space for this to be done and other places have to be made available, possibly in the stockyard.

Where the potential sub-assembly area, and even the stockyard itself, is remote from the erection site, very careful investigations are needed before a decision to sub-assemble can be agreed. Local transportation size restrictions on the route to the erection cranes may rule it out.

There are three factors which affect the practicability and economy of sub-assembling a unit on the ground: (1) the weight of the eventual assembly including any lifting beams needed, (2) the degree to which the unit is capable of being temporarily stiffened without unduly increasing its weight, (3) the bulk of the unit – will it be possible to lift it to the height needed without fouling the crane jib?

It is often necessary to make a drawing or model of the crane jib and the unit at the point of highest lift before the last point can be checked satisfactorily.

Often a jig is used to represent the connection points of the unit to the building. A unit assembled on such a jig will fit when it is lifted, one built without a jig is very unlikely to fit. Sub-assembly is only worthwhile if the unit can be lifted and bolted into place almost as easily as a single beam. The object is to avoid carrying out operations at height which can easily be done at ground level.

## **33.6 Safety**

### **33.6.1 Introduction**

Everyone who is concerned in any way with the design and construction of any type of structure must constantly be reminding himself of the fact that while it is being erected it is not as stable and secure as it will be in its finished state. Most structures that have fallen, have fallen during erection. The men who have been killed or injured in an accident on a construction site, have suffered because of a lack of thought on someone's part somewhere along the way leading up to the event. BS 5531 and the Health and Safety Executive Guidance Note GS 28 are both aimed at improving the safety record during the erection process.

Accidents are caused by people. Accidents happen to people. People can prevent accidents. A weakness in the structure or in the overloading of a crane are both brought about by people, not by any fault in the inanimate objects which

failed. The designer, the planner, the erector, the man with the spanner, are all the people who with forethought and care could have prevented an accident happening.

The man who hits his own thumb with his hammer is a victim not only of his own clumsiness but also of the man who put him in the awkward working position that led to the bruised thumb, and of the designer who produced the awkward design of the detail that had to be hammered. If he subsequently falls and is fatally injured the responsibility pattern is the same as if he had just bruised his thumb.

Research into the causes of accidents has shown that management has the greatest contribution to make to the cause of an accident, followed by the victim of the accident, and lastly by his workmates. Management is taken here in a broad sense. No one involved can escape from their responsibility.

If the limits and tolerances of dimension, of workmanship, of temperature, of the wind, of the load factor designated for the particular component, all conspire together at their limit, only a small 'nudge' is needed to trigger a succession of events leading to a disaster. The 'domino effect' is not however an inevitability. The better the planning, the better the design, the more thought that has been devoted to real understanding of what is going on in a structure as it is slowly built up from its component parts, the more likely it is that the next domino will refuse to fall, and the dangerous occurrence will have been contained.

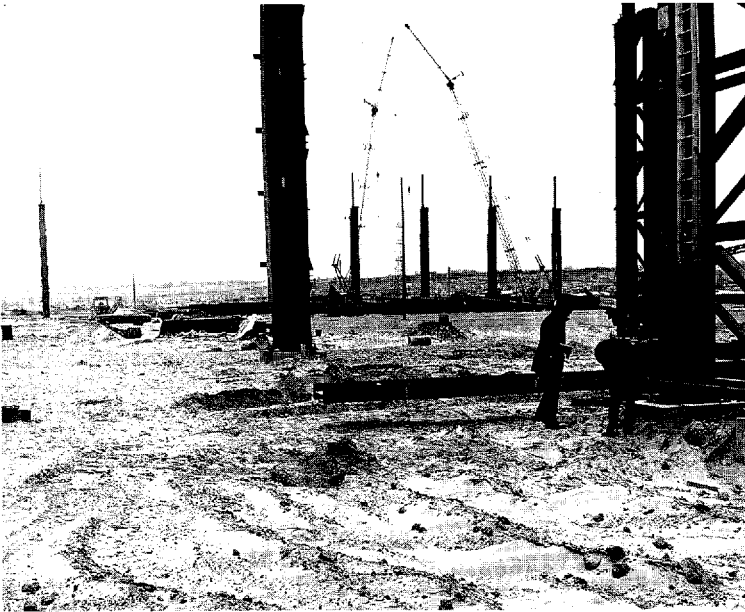
What can be done to build in a stop to prevent such a succession? The first step is to consider each potential hazard and be sure that something is done to cope with it. An example of this is in the design of the holding-down bolts. These may eventually only serve as locators, but when the column is first erected and before any bracing is fixed they are all that prevents that column from falling (see Fig. 33.15). It is subject to loading from the wind and from knocks and bumps as the connecting steelwork is attached. A concrete column in a similar situation has to be propped in four directions with temporary adjustable props each anchored at each end. Steel columns are much lighter and much simpler to place on end, but they do depend on their holding-down bolts for their first stability.

### **33.6.2 The safety of the workforce**

This is the aspect of site safety subject to statutory regulation, and to inspection by the Health and Safety Executive, in a way that the structural safety of a project is not.

Regulations lay down minimum acceptable standards for the width of working platforms, the height of guardrails, the fixing of ladders, and so on. They refer to use of safety belts and safety nets. They lay down the frequency with which a shackle or chain sling must be tested and the records that must be kept to show that this was done. Reference should be made to the appropriate regulation for the details of these requirements.





*Fig. 33.15* Initial column erection

By its very nature the erection of a structural frame is a process involving a certain amount of risk. The work is carried out at height above the ground, and until it has progressed to a certain point there is nothing to which a safe working platform can be attached; the process of erecting a safe platform can be as hazardous as the erection process itself. One solution is to provide mobile access equipment if ground conditions permit.

Different access platforms are appropriate in different circumstances. One advantage of modern composite floor construction is that the decking can quickly provide a safe working platform only requiring the addition of a handrail. Figure 33.16 shows a safe platform for the erection of bare steel work – a prefabricated platform slung over a convenient beam. In this case weather protection may be added for site welding.

There is a special onus on designers and planners to ensure that no platforms have to be put up for work that ought to have been done either in the fabrication shops or on the ground before the component concerned was lifted into place.

A prime consideration at planning stage is to see if a working platform can be eliminated altogether. Can the operation be carried out at ground level before the component is erected? If not, can the platform be designed so that it is assembled on the component while it is still on the ground? It is impracticable to have to consider the provision of a safe working platform in order to be able to safely erect the main safe working platform.

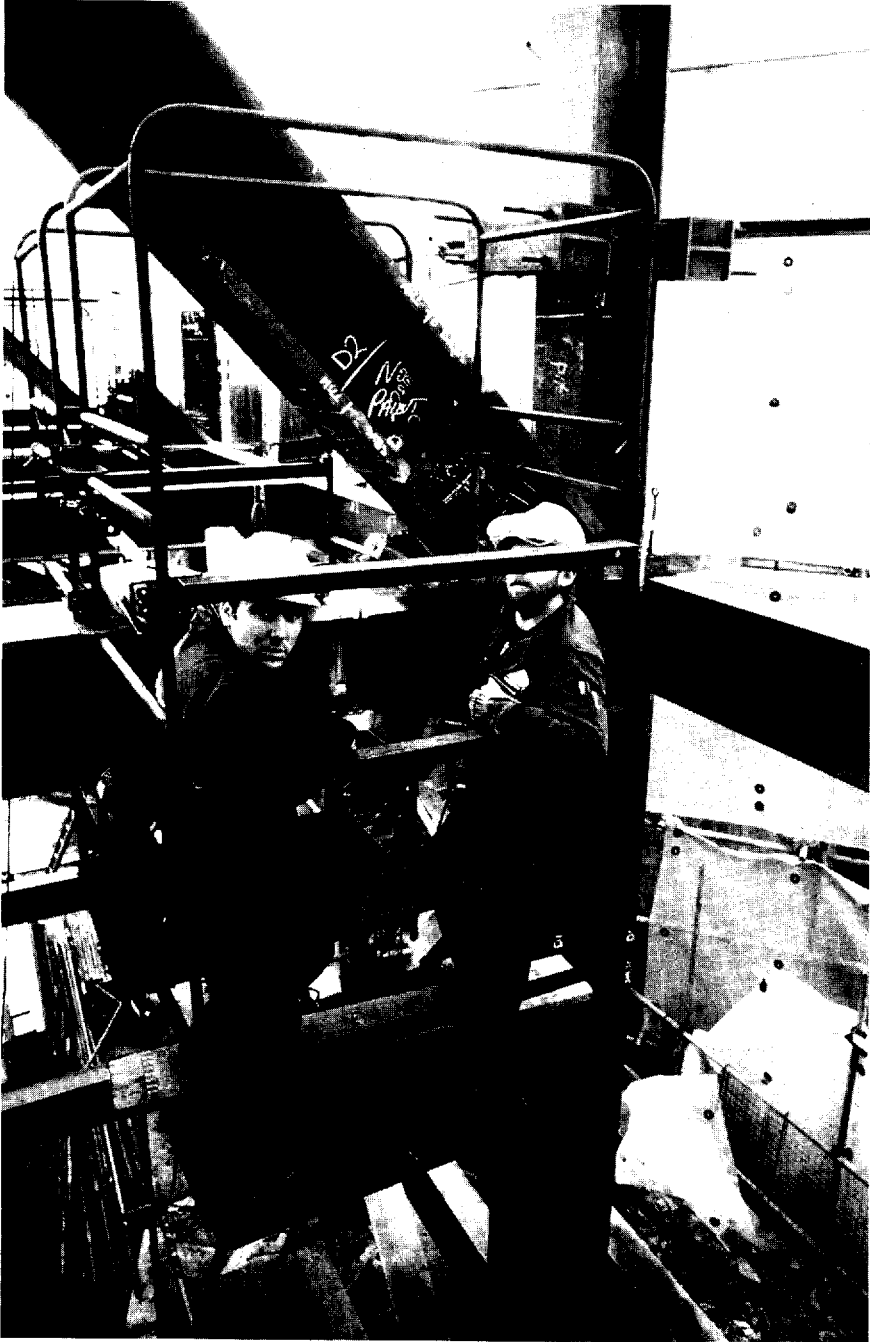


Fig. 33.16 A prefabricated working platform slung over a convenient beam

The object of safety procedures is to ensure that everything possible is done to eliminate the risk of an accident injuring or killing anyone working on the site. In summary, the methods of achieving safety are:

(1) Communication

Communication of the details of safety procedures to all concerned, with their implementation through the display of the regulations themselves in the form of abstracts, by issuing safety procedure documents and by running of training courses. Individuals must be aware of the location of particularly hazardous areas and the type of protection they have been given, the types of protective clothing and equipment that are available and how to obtain them, the restrictions in force on the site regarding the use of scaffolding or certain items of plant and any access restrictions to certain areas. They should be encouraged to tell someone in authority if they see a potential hazard developing before it causes an accident. (See Fig. 33.17).

(2) Equipment

Making the necessary equipment available on the site and maintaining it in good order. Equipment includes safety helmets, ladders and working platforms, safety belts and properly selected tools.

(3) Avoidance of working at height

Organization of the task so that the least amount of work possible has to be done at height:

- (a) by the use of sub-assembly techniques,
- (b) by the fixing of ladders and working platforms on to the steelwork on the ground before it is lifted into place,
- (c) by the early provision of horizontal access walkways,
- (d) by the provision of temporary staircases or hoists where appropriate.

All of these measures enable some of the hazards of working at height to be reduced by conferring on that work some of the advantages of ground level working.

(4) Fixing of portable equipment

Ensuring that portable equipment such as gas bottles and welding plant is firmly anchored while it is being used. The horizontal pull on a gas pipe or a welding cable being used at height is considerable, and easily able to dislodge the plant from a working platform, causing it to fall, possibly taking the operator with it. Care should also be taken to ensure that there are no flammable materials below on which sparks could fall.

(5) Design

Thoughtful design makes an important contribution to safety. The positioning of a splice so that it is just above rather than just below a floor level will reduce the risks in completing the splice on site. The arrangement of the splice so that the entry of the next component can be effected readily and without a fight, will reduce the risk of completing the splice up in the air.

1. EMPLOYEE JOINING THE COMPANY

- Discuss and obtain details of person's previous safety training experience.  
Details should be recorded.
- Show and explain company safety policy, organizations and arrangements.  
Supply copy or abbreviated version as necessary, OR confirm where it can be seen.
- Show and describe safety rules and procedures.  
Supply copy as necessary; OR confirm where details can be seen.
- Provide name and location of Safety Adviser.  
Details of Safety Supervisor/Safety Representatives (where appropriate) to be provided on site.
- Explain the necessity for personal protection.  
Highlight specific processes as necessary.
- Inform employees of their responsibility for health and safety at work.  
Safeguard/co-operation and mis-use of equipment.
- Explain the necessity for authorization in the use of plant machinery and equipment.  
Obtain details of previous experience – record. Arrange for training as necessary.
- Discuss importance of reporting dangerous incidents and defective plant and equipment.  
Explain system of reporting.
- Explain company procedures for grievances, disputes on safety matters.  
Whom to contact
- Explain method of communicating safety information within the company.  
Notice boards, Safety Bulletins, Safety Newsletters – as applicable.

*Fig. 33.17* Safety check lists

Lifting cleats and connections for heavy and complex components should be designed and incorporated in the shop fabrications as should fixing cleats, brackets or holes for working platforms and for safety belts or safety net anchorages. They will then be incorporated as part of the fabrication, rather than having to be provided by the erector while working at height. Access to a level should be provided by attaching the ladder, and the working platform that may be required, to the member at ground level prior to lifting. Ideally these connections should be designed so that they can be dismantled after the

## 2. EMPLOYEE'S FIRST VISIT TO SITE

A tour of the site should be made during the induction process to aid in the identification and location of key personnel and siting of equipment, fire and first aid points, etc.

- Confirm location of hazard areas.  
Fragile roofs, excavations, electricity, etc.
- Provide detail of first aid arrangements.  
Describe procedure for receiving first aid. Contact point/person.
- Confirm company policy for use of helmets.  
Areas where risk of head injury exist.
- Describe fire fighting arrangements.  
Confirm fire alarm points. Allocate fire assembly points. Ascertain knowledge of fire extinguishers – training as necessary.
- Describe accident procedure.  
Treatment – reporting. Accident book. Absence from work.
- Confirm protective clothing and equipment. Availability/use/issue.  
Issue relevant items. Record. Instruct in use. Storage – loss arrangements.
- Site tidiness.  
Storage/disposal of materials. Safe access, vermin, disease.
- Confirm authority to operate.  
Issue permit as necessary. Driver's licence. Site rules for plant and transport. Arrange training.
- Scaffolding – means of access.  
Highlight basic safety with work on scaffolding. Non use of incomplete scaffold. Access – to work place.
- Reporting defects. Malpractice. Safe systems of work.  
Stress need to report defects and malfunctions in plant and equipment. Horseplay. Safe practice.
- Locate and provide details of welfare facilities.  
Canteen opening times. Designated area where smoking is permitted. Storage of clothing, equipment and tools.

erector has left the platform and descended the ladder. He should not have to come down an unfixed ladder or stand on an unfixed platform as he removes these items after use.

Thought given to all these points at drawing board stage will reduce the risk inherent in a hastily improvised solution, often reached without proper consideration, and by unqualified personnel.

### 33.6.3 The safety of the structure

The stability of the structure itself, which is not prescribed by statutory regulations in the way that the safety of those working on it has been protected, is clearly the most important product of the care which has been lavished on its design.

Where a collapse of a partly-built structure occurs, the loss of life is generally heavy. One of the main indictments of the design process is that where there is a collapse the investigation and inquests which follow show that there have been lapses in the understanding of the behaviour of the incomplete structure, lapses in the detailed consideration of each and every temporary condition, and, most important of all, lapses in the communication of information to all involved. In the bridge collapse shown in Fig. 33.18, the temporary loading condition was not considered properly. At the point of failure of the bottom flange, a splice similar to that shown in Fig. 33.19 was not adequate to take the compression imposed during erection.

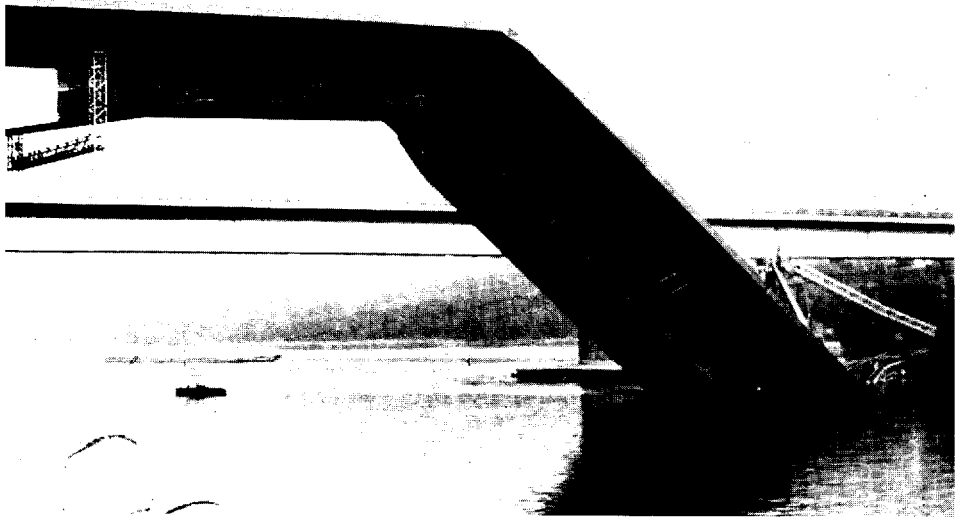
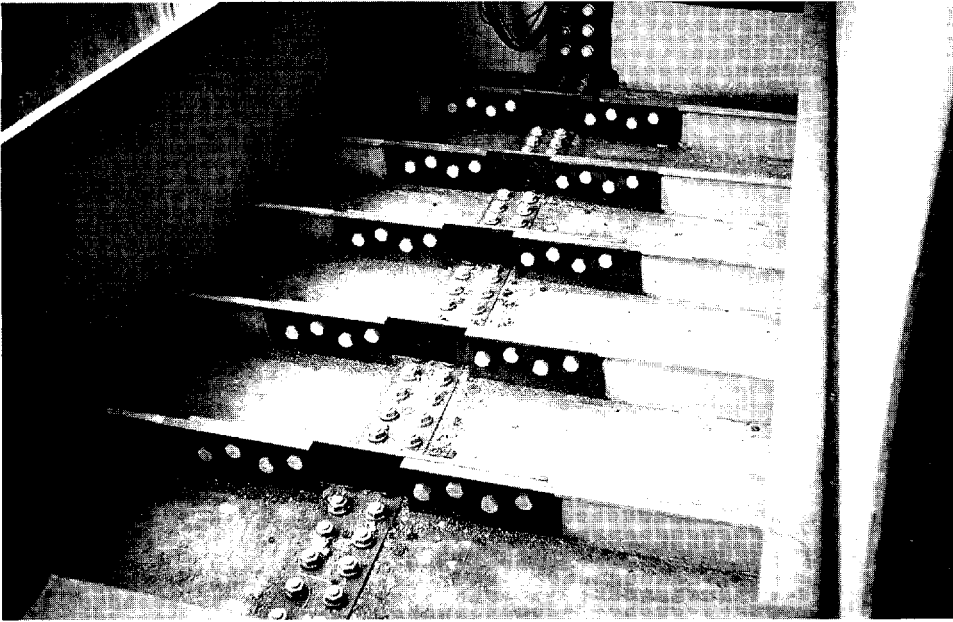


Fig. 33.18 Bridge failure during cantilever erection



*Fig. 33.19* Typical splice detail that is adequate in tension but would fail if subject to significant compression.

A designer must communicate his plan for building the structure to those who will actually have to do the building; nothing could be worse than the designer who has not even considered how his creation is to be turned into reality.

### *Columns*

The effective length, and even design condition of a column can change during the construction of a building. Each condition must be checked to ensure that the column is adequate for each one and the risks inherent at each stage must be assessed and provided for.

### *Plate girders and box girders*

The checks which are applied to the webs and stiffeners of a plate girder during its design normally take account only of conditions at points where stiffeners are located and at points where loads are applied to the girder. It may not be obvious to the designer of a bridge girder that it may be subjected to a rolling load when the bottom flange is rolled out over the piers, subjecting the girder to a compressive load which it is not required to carry in its permanent position.

### *Splices*

The effects of stress reversals are most severe on splice details which almost inevitably involve some degree of eccentricity that can trigger a collapse if the condition, transient though it is, has not been considered in design (see Fig. 32.19).

### *Bracings*

Bracing is built into all types of structures to give them a capability to withstand horizontal forces produced by wind, temperature and the movements of cranes and other plant in and on the building.

Erection cranes carried on the structure during its erection produce vibrations and also loads where no load is intended when the building is complete. Reactions to cranes slewing, luffing and hoisting are carried by the framework supporting the crane down to the ground; these loads and vibrations must be considered and the structure's ability to carry them assessed at the outset.

Temporary bracings required at some stages of the work must have properly designed connections and be specifically referred to in the erection method statement. Early or unauthorized removal of temporary bracings is a common cause of collapse in a partially completed frame.

Having considered the need for installing temporary bracings and the need to postpone fixing permanent bracings, consideration should be given to the overall economy of retaining the temporary bracings and perhaps leaving out the permanent bracings. It is a costly and potentially dangerous business to go back into a structure solely in order to take out temporary members, or to insert components that have had to be left out temporarily.

### *Temperatures and wind effects*

On a partly erected and unclad building frame the effects of temperature on the framework can exceed the effects of the wind. A tall framework will lean away from the sun in much the same way as a plant leans towards it as the sun moves round from east to west.

This must be recognized in any attempt to check the plumb of a building and should only be done on a cloudy day or after the whole structure has been allowed to reach a uniform temperature, say at night and then only when the temperature is at or near the design mean figure. Tightening the bolts in the bracing when a building is at non-uniform temperature can lock in the error and make it very difficult to correct later.

Wind effects can bring a building down if it is not adequately braced and guyed. The wind can have two effects: (1) pressure exerted on anything in its path (2) vibrations in a member obstructing its path. The problem is compounded by the



variability of the direction and speed of a wind, and by the variability of the aerodynamic shape of the structure as each new piece is added. Care must be taken to ensure that they have been properly considered at each stage of erection for potentially problem structures, for example, bridges erected by cantilevering. Bracings, guy ropes and damping weights may all have to be considered as methods of changing critical frequencies of vibration and of limiting movements as the job progresses.

#### **33.6.4 The safe use of cranes**

Mention has already been made of the UK Statutory Regulations. These lay down not only requirements for safe access and safe working but also a series of test requirements for cranes and other lifting appliances.

It is the responsibility of management to ensure that plant put on to a site has a sufficient capacity to do the job for which it is intended, and that it remains in good condition during the course of the project. Shackles and slings must have test certificates showing when they were last tested. Cranes must be tested to an overload after they have been assembled. The crane test is to ensure that the winch capacity, as well as the resistance to overturning and the integrity of the structure, is adequate.

British Standards lay down the various requirements for safe working. Lists of those standards, and the necessary forms to enable each of the tests to be recorded, must be provided by management, often in the form of a 'site pack' which the site agent must then display and bring into use as each test is carried out. It is the site agent's responsibility to ensure that these requirements are fulfilled. He may also be required to produce them from time to time for inspection by the factory inspector during one of his periodic visits to the site.

A crane which has been tested and used safely in many locations might overturn at its next location and use (see Fig. 33.20). The cause is often found to be that an inadequate foundation has been provided under the tracks or outriggers of the crane, i.e. adequate support under the tracks or outriggers is an absolute requirement. It is equally important that the crane should work on level ground, as an overload can easily be imposed, either directly or as a sideways twist to the jib, if the ground is not level.

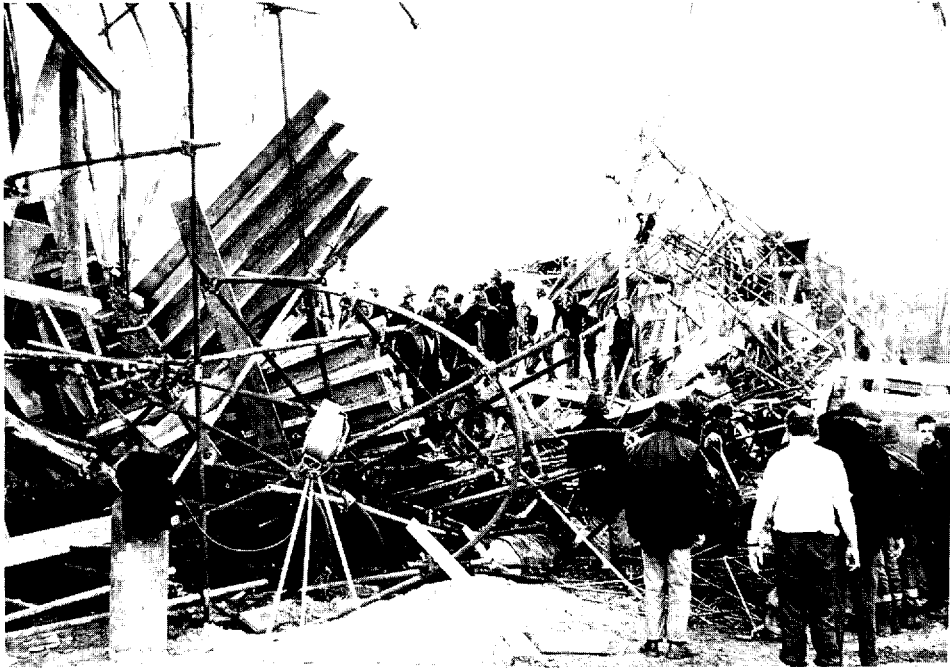
#### **33.6.5 Temporary supports and temporary conditions**

The design of the structure will have had a considerable amount of effort devoted to it. The design of the temporary works on which that structure may have to depend while it is being built may not have had so much attention. The number of collapses which have taken place after an initial failure in the temporary supports,



*Fig. 33.20* Crane overturning

suggests that temporary works seldom get the design attention they deserve (see Fig. 33.21). For example a temporary support may only be designed to take a vertical load. In practice the structure it is intended to support may move due to changes in temperature and wind loading – imposing significant additional horizontal loads.



*Fig. 33.21* Falsework collapse

Consideration starts at the foundations. Settlement in a trestle foundation can profoundly affect the stress distribution in the girder work that it supports. Settlement under a crane outrigger from a load applied only momentarily can lead to the collapse of the crane and its load.

The Code of Practice BS 5957 for falsework, which includes all temporary works, trestling, guy wires, etc., as well as temporary works associated with earth works, deals with a wide range of falsework types and should be carefully read and observed. Particular attention should be paid to the paragraphs dealing with communication, co-ordination and supervision since failure in any of these can lead to a failure of the falsework itself.

Re-used steelwork showing signs of severe corrosion must not be used for temporary falsework carrying critical loading, but in other situations re-used steel should be measured to be sure that it is adequate.

During construction a structure will move as its parts take up their design load. Connections to temporary supports have to be capable of absorbing these movements. Unless the design allows for these movements, eccentricities can result which will trigger a collapse. The cross-heads at the tops of bridge trestles are typically members which have a bad record of failure from this cause. They are often called upon to resist wind-induced loads, vibrations and temperature-induced

movements in the structure, in addition to their more obvious direct loading, and so must receive a special design study.

Very tall buildings and chimneys as well as bridges can be affected by wind-induced vibrations as can working platforms and those who have to work with them. The force of the wind can make welding impossible without adequate shelter; the fixings for a working platform must be able to take the load of the wind blowing on the area of shelter which the welder has to have for his work.

The rule that one should 'put' before one 'takes' is a good one. Too many examples exist of a collapse following the removal of guy wires before the bracing was fitted, or before column bases designed to be 'fixed' had been grouted and fixed in reality. What is needed here is a clear communication down to the foreman and the workforce of exactly which sequence of working must be followed. Supervision alone is unlikely to be looking in the right direction at the precise time the deed is done. The only way to be sure is to issue a clear directive coupled with an explanation of why the instruction is being given and to have a skilled workforce who know what they are doing.

Attention has already been drawn to the need for an organization chart. A second chart showing who needs to know what, and why, and when should also be produced. If the lines of communication and the patterns of responsibility up and down the various management levels and between the various organizations on the chart are to be effective there must be a conscious effort on the part of everyone, firstly to understand why the links are there, and secondly to ensure that the necessary information flows swiftly up and down the lines. Assumptions can be dangerous things: 'It is for the want of thinking that most men are undone.'

## **33.7 Site practice**

### **33.7.1 Setting-out tolerances**

Accuracy of setting out is a very important part of maintaining an acceptable control of tolerances and achieving a structure which is acceptable to all the following trades. (Chapter 31 discusses the topic of tolerances generally for structural steelwork.) It is concerned with the establishment of a grid of lines and the transfer of those lines to the foundations and columns, and with the establishment of accurate levels.

The site should be provided with a dumpy or quick-set level and with a simple theodolite. The advantage of a theodolite over a simpler box square is that the transit of the instrument can later be used for checking the plumb of the columns and the telescope for reading offsets to check their alignment.

Time spent on laying down and marking the cross-centre lines of the column bases on individual boards at each base and subsequently on to the concrete of the base is time very well spent. Lines should be drawn on chalked areas in such a way that the mark made is reasonably permanent and will not be washed away in

the first shower of rain. The base can then be quickly and accurately set in both directions and to the correct level on the pre-set pads. The value of this work is that it enables errors in the concrete work to be identified at a time when corrective measures can be undertaken. It also allows much argument, claim and counter claim, to be avoided. The accurate setting of grouted packer plates on which to land the column serves the same purpose. It will highlight concrete which is high and holding-down bolts which are low. It makes sense to discover these errors as early as possible.

Whether the column base is a socket type with shear connectors to the concrete, or if it has a plate or slab base plate, or even if it sits on a fabricated grillage, the same rule holds true. It is far easier to set, adjust and make true a pile of packers and a line than it is to start heaving the whole framework around after it has been erected. Final bolting can be done right away, without having to leave the connections loose to give the framework freedom to be moved into plumb and line as a later operation.

### 33.7.2 Slinging and lifting

Components, whether they are on transport or are lying in the stockyard, should always be landed on timber packers. The packers should be strong enough to support the weight of steel placed above them and thick enough to enable a sling to be slipped between each component.

The aim when lifting a component for transport only is to have it hang horizontally. This means that it is necessary to estimate its centre of gravity; easy for a simple beam but less easy for a complex component. The first lift should be made very slowly in order to check how it will behave, and also to check that the slings are properly bedded (see Fig. 33.22).

Most steelwork arrives on site with some or all of its paint treatment. The damage which slinging and handling can do must be put right and it is therefore very important to try to minimize damage to the paint. The same measures which achieve this saving also ensure that the load will not slip as it is being lifted and that the slings (chain or wire) are not themselves damaged as they bend sharply around the corners. Softwood packers should be used to ease these sharp corners.

Packers to prevent slipping are even more necessary if the piece being erected does not end up horizontal. The aim should always be to arrange the slinging in such a way that the piece hangs at the same attitude as that which it will assume in its erected position. Pieces being lifted are usually controlled by a light hand line affixed to one end. This hand line is there to control the swing of the piece in the wind, and not to pull it into level. Wherever possible non-metallic slings should be used. Their use will reduce damage to paintwork; they are less likely to slip than chain or wire slings.

In extreme cases two pieces may have to be erected simultaneously using two cranes. Staff working back at the office should have identified such possibilities

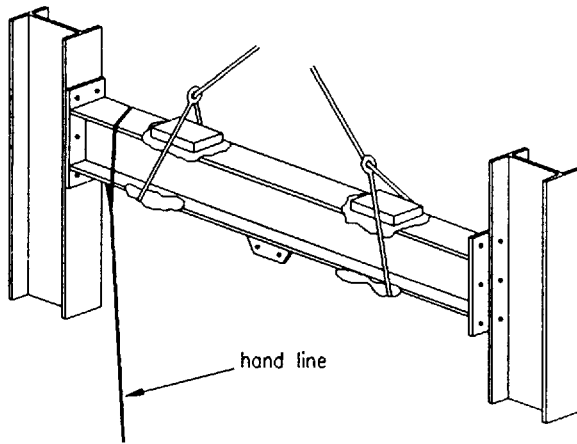


Fig. 33.22    Correct slinging practice

and placed them in the site erection method statement. It is too late to find out about it when the erection is attempted with only one crane, or with no plan made of how to pull back the head of the column.

Reference was made earlier to the need to consider the stiffness of large assemblies such as roof trusses as they are lifted from a horizontal position on the ground. Reference has also been made to the need to build assemblies in a jig to represent the various points at which connection has to be made in the main framework. Another jig for lifting can be useful particularly if there are many similar lifts to be made. This can be made to combine the need to stiffen with the need to connect to stiff points in the sub-frame, and the need to have the sub-frame hang in the correct attitude on the crane hook. The weight of any such stiffening and of any jig must of course be taken into account in allocating a crane to make the lift.

Some situations require that temporary stiffening be left in position after the initial erection until the permanent connections are made. This should also have been foreseen and sufficient stiffeners and lifting devices provided to avoid an unnecessary bottleneck caused by a shortage of a device for erection of the next sub-frame.

Where a particularly awkward or heavy lift has to be made a much quicker and safer job of slinging and lifting can be made if cleats for the slings have been incorporated in the fabrication. Each trial lift made after the first one wastes time until the piece hangs true. The drawing office knows exactly where the centre of gravity is.

A chart giving details of standard hand signals is illustrated in Fig. 33.23. Their use is essential when a banksman has to be used to control the rear end of the

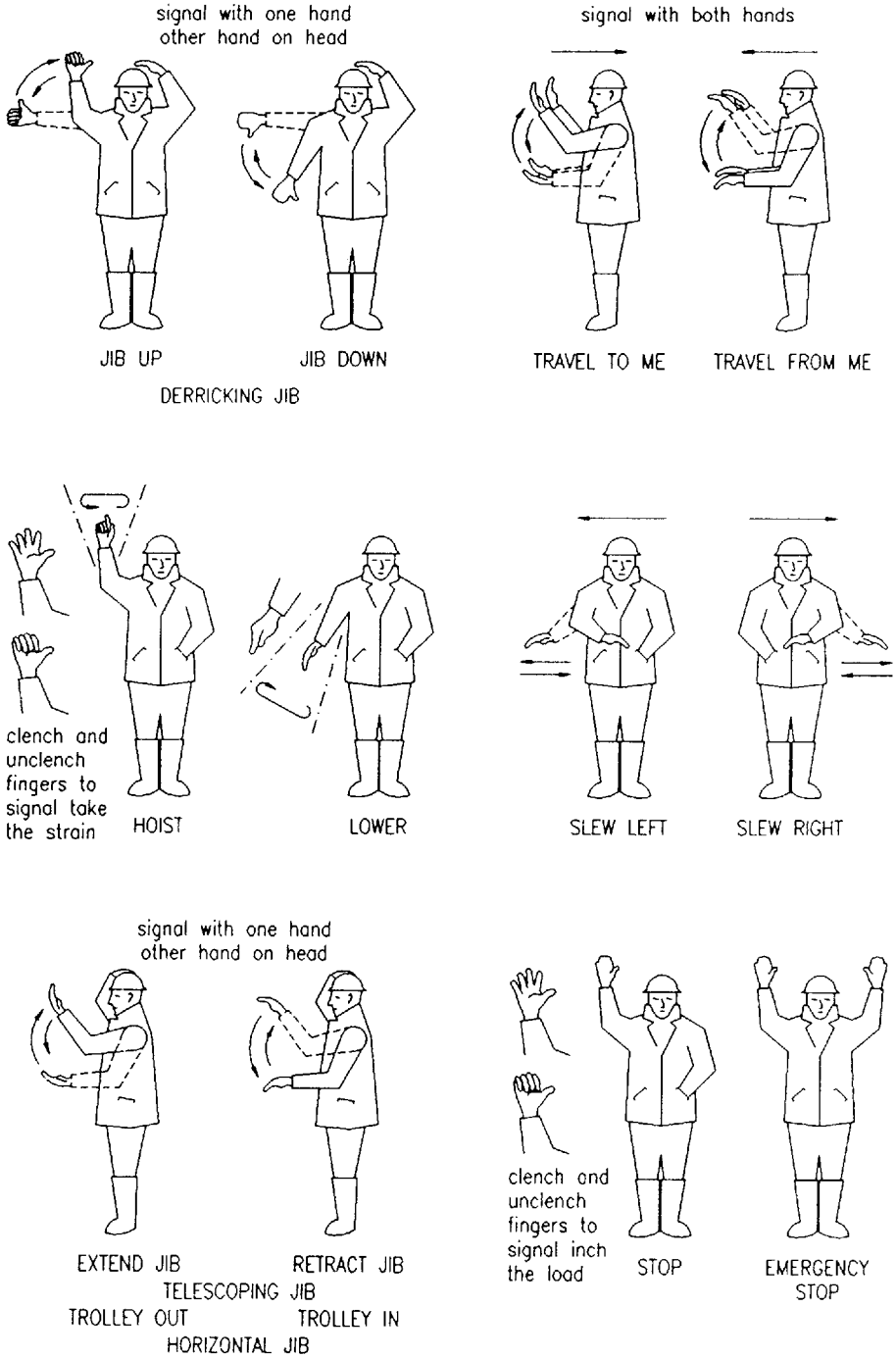


Fig. 33.23 Standard hand signals for lifting

transport bringing the component to the hook as it is reversed. The banksman is needed to relay the signal from the one man directing the movements of the crane if he is necessarily in such a position as to be out of sight of the crane driver. A clear system of signals should be agreed for the hand-over of control of the crane from the man on the ground to the man up on the steel who will control the actual landing of the component. A banksman may also be needed up on the steel if the crane driver cannot see clearly the top man who is giving the control instructions. It is vital that there is no confusion over who is giving instructions to the crane driver.

### **33.7.3 Lining, levelling and plumbing**

If, in spite of having taken care over the initial levelling of packers and of carefully positioning the column bases to the pre-set lines on the foundations, the structure still needs adjustment during lining, levelling and plumbing, then something must be wrong.

The first thing to check is that no error has been made in the erection. If nothing is out of place then the drawings and the fabrication need to be checked. If there is an error it will be necessary to take careful note of all the circumstances and advise all concerned immediately.

If the steelwork has just been thrown together with no great regard for accurate positioning it will be necessary to provide equipment and manpower to carry out the lining, levelling and plumbing. The equipment will include jacks, tirfor-type wire pullers with wires, straining screws, wedges, piano wires, and heavy plumb bobs with damping arrangements, all in addition to the level and simple theodolite which are needed for the basic check.

It is necessary to do the lining and levelling check before final bolting up is done. In practice this means that it must be done immediately following erection since it is a waste of time to have to slacken off bolts already tightened in order to be able to move the steelwork about. There is no way that erection can go ahead until the braced bay is bolted up and that cannot be done until it is level and plumb.

A supply of steel landing wedges and slip plates is needed to adjust the levels. They must be positioned in pairs opposite to each other on two sides of the base plate of the columns to be levelled. If the wedge is placed on one side only the column will be supported eccentrically and can in fact be brought down, especially if more than one column had been lifted on a series of wedges all driven in from the same direction. Alternatively toe jacks can be used in pairs to lift the columns. The engineer may direct that temporary packings be removed after the grouting medium has set. A temporary bench-mark should be established in the vicinity of the columns in a position where it cannot be disturbed. Its value should be agreed with the client's representative. The level will then be used to check the final setting with the seating packers inserted, and the column landed



back on them and bolted down with the holding-down bolts. The column can then be moved about in plan on these packers to bring it into line and bay length from its neighbours.

The position of a line, offset from the column centreline by an amount to clear the columns, should be marked and agreed. This line is then used either to string and strain a piano wire or to set and sight a theodolite telescope. Offsets from it will then give the amounts by which movements must be made.

Running dimensions from the previous column will give required movements longitudinally. Care should however be taken to watch the plumb of the columns in this direction in view of the tendency of steelwork to 'grow'. Regard should be paid to column-to-column dimensions rather than to running dimensions from the end of the building.

Having got the bases of the columns in their correct position and level, it is possible to check the plumb. The comments already made regarding temperature effects are relevant here too. It is a complete waste of time to check the plumb of a building which is not all at the same temperature, and in the case of a long building if the temperature is not at the standard which in the UK is normally 10°C.

The fact that the column bases are level does not mean that a level check is not needed on the various floors in a tall building. It is important however that the levels of any one floor are only checked for variations from a plane rather than on the basis of running vertical measurements from the base which are affected by temperature and the variable shortening effect on the lower columns as weight is added to them.

Plumb can be most readily checked with a theodolite using its vertical axis and reading against a rule held to zero on the column centreline. This eliminates the effect of rolling errors and is a check against the same centreline used in the fabrication shops. If a theodolite cannot be used a heavy plumb bob hung on a piano wire and provided with a simple damping arrangement, such as a bucket of water into which the bob is submerged, is a second best method. Measurements are made from the wire to the centrelines in the same way as before. The disadvantage of using a plumb wire is that all the operatives have to climb on the steel to take and then to check the readings. Optical or laser plumbing units are available; these are particularly useful for checking multi-storey frames.

Adjustments, and in extreme cases provision for holding the framework in its correct position, are normally only necessary if the frame is not self-stable. If it will eventually depend say on concrete diaphragm panels for stability, consideration should have been given at the design stage to one of two alternatives. Either the concrete panels should be erected with the steel frame or else temporary bracing should have been provided as part of the original planning. Any bracing must be positioned so that it can be left in place until after the concrete panel has been placed and fixed so as to be able to carry out its function.

If diagonal wires have to be used they should be tied off to the frame at node points rather than in mid-beam, in order to avoid bending members, and their ends fixed using timber packers in the same way as is done when the pieces are

slung for lifting. Turnbuckles or tirthor-type pullers provide the effort necessary to tension the wires. The sequence of placing, tensioning and ultimately removing these temporary arrangements should form part of the method statement prepared for the particular situation.

Once the components of the building have been pulled into position the final bolting up can be completed. In the case of a stiff-jointed frame, after the joints have been fully bolted or welded it is impossible to make any further adjustments.

#### **33.7.4 Site welding**

Special consideration must be given to the planning of the erection of a structural steel frame where site welding has been specified. Site welding has to be carried out in conditions of weather and in positions which make it more difficult and expensive than welding carried out in workshop conditions. In a workshop the work can be positioned to give optimum conditions for the deposition of the weld metal, while most welds on site are positional. Most site welding is carried out by manual metal arc and electrodes since this is more flexible in use and is more able to lay good weld fillets in the vertical up and overhead positions.

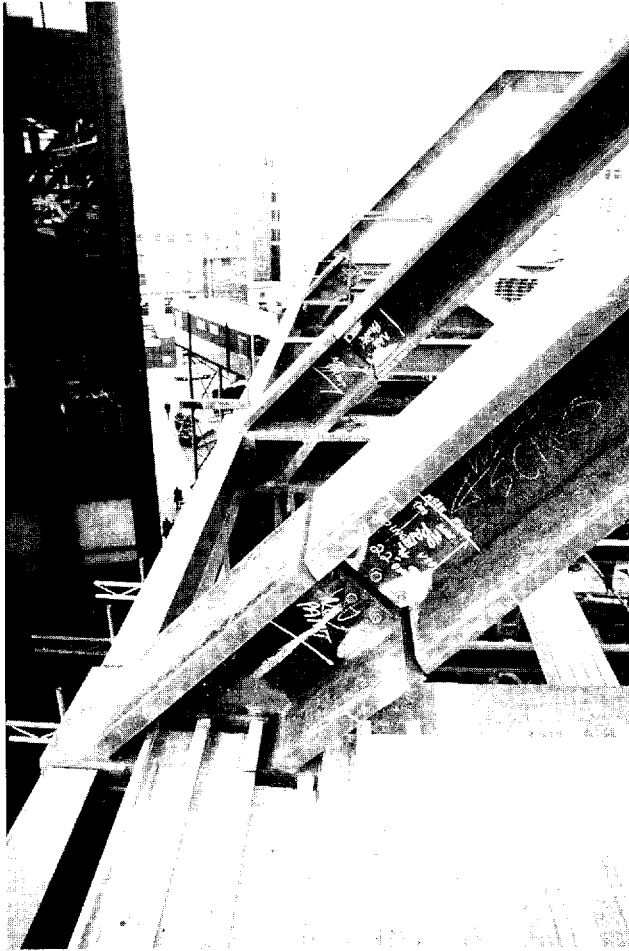
Some means must be provided for temporarily aligning adjacent components which are to be welded together, and of holding them in position until they are welded (see Fig. 33.24). The methods adopted to cope with the need for alignment may have to carry the weight of the components, and in some cases a substantial load from the growing structure.

Safe means of access and of working must be provided for the welder and his equipment. The working platform may also have to incorporate weather protection since wind and rain and cold can all adversely affect the quality of the weld being produced.

The design of the weld preparation on the components to be joined must take into account the position of these components in the structure. The erection method statement and the weld procedure statement for each joint must take all these factors into account. BS 5135 gives an outline of the many factors which must be defined in a weld procedure statement. Reference should also be made to BS 4870.

Provision must be made for the necessary run-off coupon plates for butt welds and for their subsequent removal. Run-off plates are required in order to ensure that the full quality of the weld metal being deposited is maintained along the full design length of the weld (see Fig. 33.25).

Also provision must be made in the initial setting and positioning of the components in order that the weld shrinkage which will take place as the joint cools will not result in loss of the required dimensional tolerances across the joints.

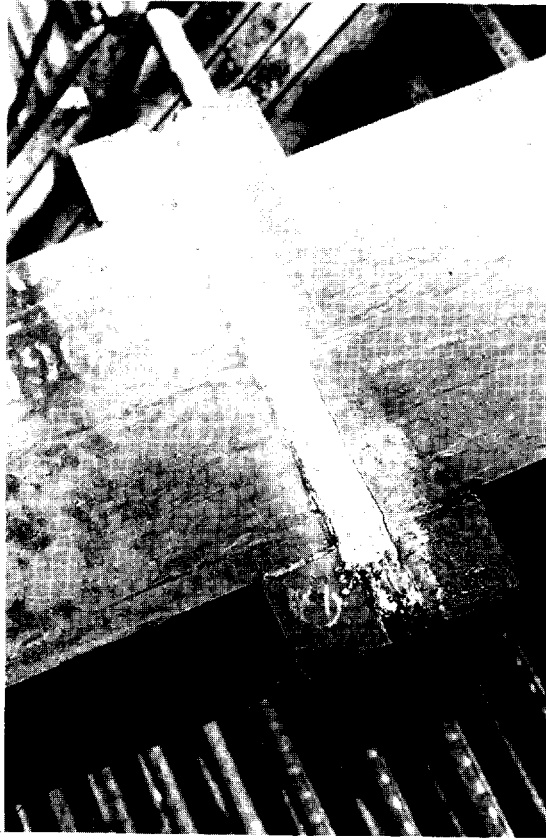


*Fig. 33.24* Temporary web splice plates supporting and aligning joint for site welding

### **33.7.5 Site bolting**

Wherever possible site splices should be designed to be bolted. This process is less affected by adverse weather than welding, uses simple equipment and presents much less complex problems regarding access for carrying out the work and for its subsequent inspection.

Impact wrenches and powered nut runners speed the tightening of bolts. When small quantities of HSFGB bolts are to be used, manual torque wrenches are available. Where large quantities of friction-grip bolts have to be tightened, an impact wrench is an essential tool. Where access is difficult, wrenches are made which run the nut up and are then used as manual ratchet wrenches to finally



*Fig. 33.25* Run-off plates for a butt weld

tighten the bolt. A large impact wrench able to tighten 33 mm bolts weighs 8.3 kg (18 lb) and consumes 21 l/s of air (44 ft<sup>3</sup>/min). The drive to the nut is through a square shaft and an interchangeable socket sized to fit the nut being tightened. The sockets are retained on the drive shaft by a pin which is in turn retained by a rubber ring. A range of sockets and adaptors is available enabling the usefulness of the wrenches to be increased.

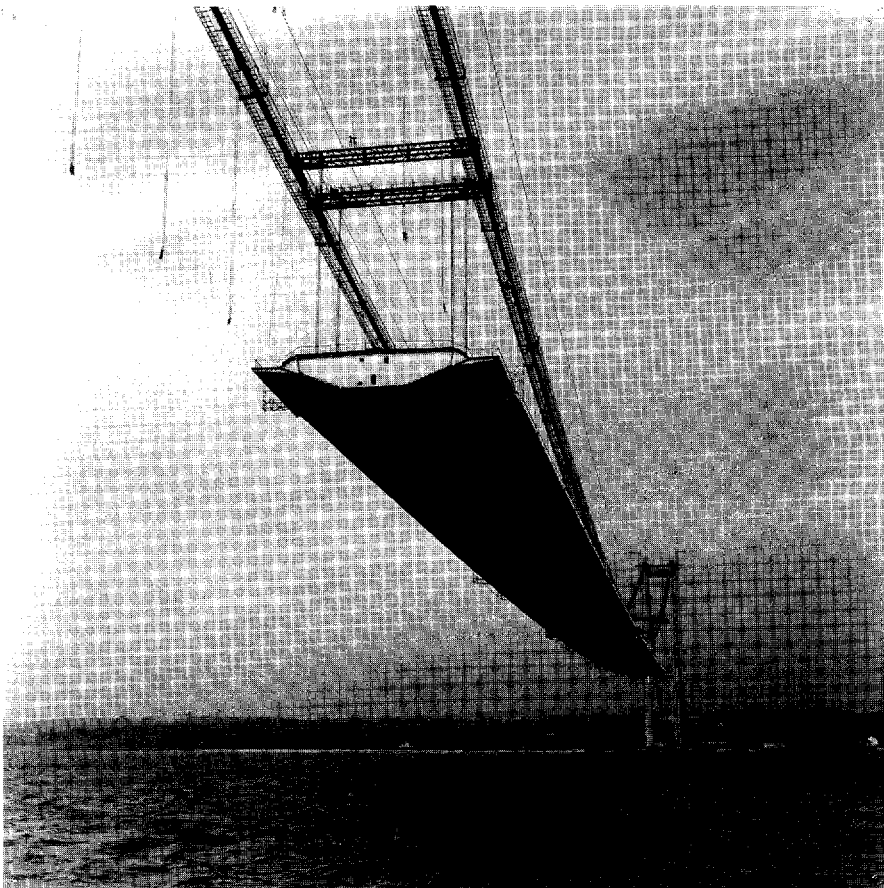
The podger spanner is the tool that is associated most closely with a steel erector. The pointed end is used for the initial lining of holes before the bolt is inserted and tightened with the jaws of the spanner.

Friction-grip bolts must be tightened first to bring the plates together and thereafter be brought up to the required preload either by applying a further part turn of the nut or by using a wrench calibrated to indicate that the required torque has been reached. The manual wrench has a break action which gives the indication by means of a spring without endangering the erector by a complete collapse. Alternatively load-indicating washers may be used to demonstrate that the bolt has been tightened to the requisite tension.

### 33.8 Special structures

While it is a mistake to consider that any structure is not special in some way, there are, nevertheless, a number of structures which, by their complexity, require special consideration when planning their erection and therefore their design. The length or height of the complete structure may bring it into this category, or the depth of individual members, or the fact that it is designed to move.

Temperature differentials over the depth of bridge box girders will produce changes in the camber of the girder. Temperature differentials over the width of a structure will produce changes in verticality. Temperature changes will affect the verticality of the columns at each end of a long single-storey factory building, or



*Fig. 33.26* Humber Bridge during erection

of a bridge. Some of these effects can be, and commonly are, accommodated by the provision of expansion joints, but others must be recognized in the planning and execution of the work.

The building of a suspension bridge and a cable-stayed bridge are perhaps the best examples where the movements and changes to the shape of the structure as it grows are most apparent. A radio telescope is the best example of a special structure which is designed to move and yet must maintain very close tolerances as the extremities of the structure are reached. Other structures move as they grow and their temporary supports can fail as a result. This is too often the result of a lack of appreciation of construction movements, vibrations from wind, or local loads from erection plant. But, with a suspension bridge (Fig. 33.26), the obvious complexities demand special attention and so it can truly be said that it is where a structure gives the appearance of simplicity that problems are most likely to arise.

## Chapter 34

# Fire protection and fire engineering

by JEF ROBINSON

### 34.1 Introduction

Fire safety must be regarded as a major priority at the earliest stage as it can have a major impact on the design of a building and its structural form. Nevertheless, it should not stifle aesthetic or functional freedom; 'fire engineering' techniques are now available which permit a more rational treatment of fire development and fire protection in buildings.

The strength of all materials reduces as their temperature increases. Steel is no exception. It is essential that the structure should not weaken in fire to the extent that collapse occurs prematurely, while the occupants are seeking to make their way to safety. For this reason it is necessary to provide a minimum degree of 'fire resistance' to the building structure. Additionally, a measure of 'property protection' is implied in the current Building Regulations, although in principle the only concern of the Regulations is safety of life.

There are two basic ways to provide fire resistance. First, to design the structure using the ordinary temperature properties of the material and then to insulate the members so that the temperature of the structure remains sufficiently low, or secondly, to take into account the high temperature properties of the material, in which case no insulation may be necessary.

The first method, the 'fire-protection' approach, is the most common at present but is a prescriptive method. Recent research has shown that the failure temperature of a member depends upon load, temperature gradient, dimensions and stress distribution. By quantifying these effects a more rational 'fire-resistance' approach is being developed which is the basis of the recently published BS 5950 Part 8: *Code of practice for fire resistant design*.<sup>1</sup>

### 34.2 Standards and Building Regulations

#### 34.2.1 Building Regulations

All buildings in the UK are required to comply with the Building Regulations<sup>2</sup> which are concerned with safety of life. The provisions of Approved Document B, for England and Wales, of the Regulations, dealing with structural fire precautions,

are aimed at reducing the danger to people who are in or around a building when a fire occurs, by containing the fire and ensuring the stability of the structure for sufficient time to allow the occupants to reach safety. Generally, in Scotland and Northern Ireland the provisions are similar. Approved Document B requires that adequate provision for fire safety be provided either by fulfilling the requirements laid down or by suitable alternative methods.

The fire-resistance requirements of Document B apply only to structural elements used in:

- (a) buildings, or parts of buildings, of more than one storey,
- (b) single-storey buildings built close to a property boundary.

The degree of fire resistance required of a structural member is governed by the building function (office, shop, factory, etc.), by the building height and by the compartment size in which the member is located.

Fire resistance provisions are expressed in units of time: ½, 1, 2, 3 and 4 hours. It is important to realise that these times are not allowable escape times for building occupants or even survival times for the structure. They are simply a convenient way of grading different categories of buildings by fire load, from those in which a fire is likely to be relatively small, such as low-rise offices, to those in which a fire might result in a major conflagration, such as a library. Fire-resistance requirements for structural elements are given in Reference 2.

### 34.2.2 BS 5950: Part 8

BS 5950: Part 8<sup>1</sup> permits two methods of assessing the fire resistance of bare steel members. The first, the 'load ratio' method consists of comparing the 'design temperature', which is defined as the temperature reached by an unprotected member in the required fire-resistance time, with the 'limiting temperature', which is the temperature at which it will fail. The load ratio is defined as:

$$\text{load ratio} = \frac{\text{load applied at the fire limit state}}{\text{load causing the member to fail under normal conditions}}$$

If the limiting temperature exceeds the design temperature no protection is necessary. The method permits designers to make use of reduced loads and higher strength steels to achieve improved fire-resistance times in unprotected sections.

The second method, which is applicable to beams only, gives benefits when members are partially exposed and when the temperature distribution is known. It consists of comparing the calculated moment capacity at the required fire-resistance time with the applied moment. When the moment capacity exceeds the applied moment no protection is necessary. This method of design is used for unusual structural forms such as 'shelf-angle' floor beams. Some examples of the use of the moment capacity method are given in the handbook to BS 5950: Part 8.



Limiting temperatures for various structural members are presented in the Appendix *Limiting temperatures*. These ‘failure’ temperatures are independent of the form or amount of fire protection. Beams supporting concrete floors fail at a much higher limiting temperature than columns, for example.

The rate of heating of a given section is related to its ‘section factor’ which is the ratio of the surface perimeter exposed to radiation and convection and the mass, which is directly related to cross-sectional area.

$$\text{section factor} = \frac{H_p}{A} = \frac{\text{perimeter of the section exposed to fire (m)}}{\text{cross-sectional area of the member (m}^2\text{)}}$$

A member with a low  $H_p/A$  value will heat up at a slower rate than one with a high  $H_p/A$  value and will require less insulation (fire protection) to achieve the same fire-resistance rating. Standard tables are available listing  $H_p/A$  ratios for structural sections (see the Appendix *Section factors for UBs, UCs, CHSs and RHSs*). These factors are calculated as indicated in Fig. 34.1.

Sections at the heavy end of the structural range have such low  $H_p/A$  ratios, and therefore such slow heating rates, that failure does not occur within  $\frac{1}{2}$  hour under standard BS 476 heating conditions even when they are unprotected.

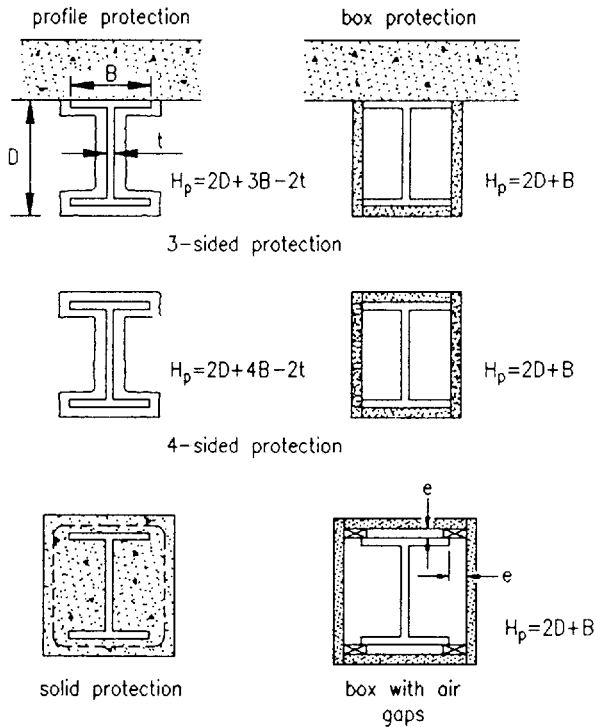


Fig. 34.1 Different forms of fire protection to I-section members

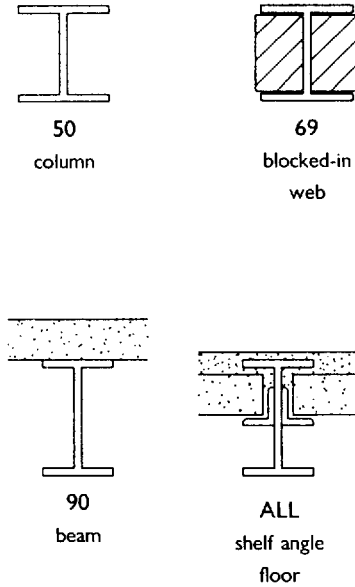


Fig. 34.2 Maximum ratios of  $H_p/A$  ( $m^{-1}$ ) of exposed steel to give 30 minutes fire resistance.

Limiting section factors for various structural elements are given in Fig. 34.2 (corresponding to a load ratio of 0.5).

Manufacturers of fire-protection products now give guidance on the required thickness of fire protection depending on the section factor of the member. The example of a table for a typical spray applied (profile protection) shown in the Appendix *Minimum thickness of spray protection* is taken from Reference 3.

Most fire-protection materials are assessed at a single limiting temperature of 550°C. However, the limiting temperatures of beams supporting concrete floors can be considerably higher, leading potentially to the use of less fire protection to the section. This is the basis of the approach in BS 5950: Part 8, under which, when fully implemented, manufacturers will provide thermal properties of their materials to enable design to any limiting temperature to be carried out.

### 34.3 Structural performance in fire

#### 34.3.1 Strength of steel at elevated temperatures

Steel begins to lose strength at about 200°C and continues to lose strength at an increasing rate up to a temperature of about 750°C when the rate of strength loss

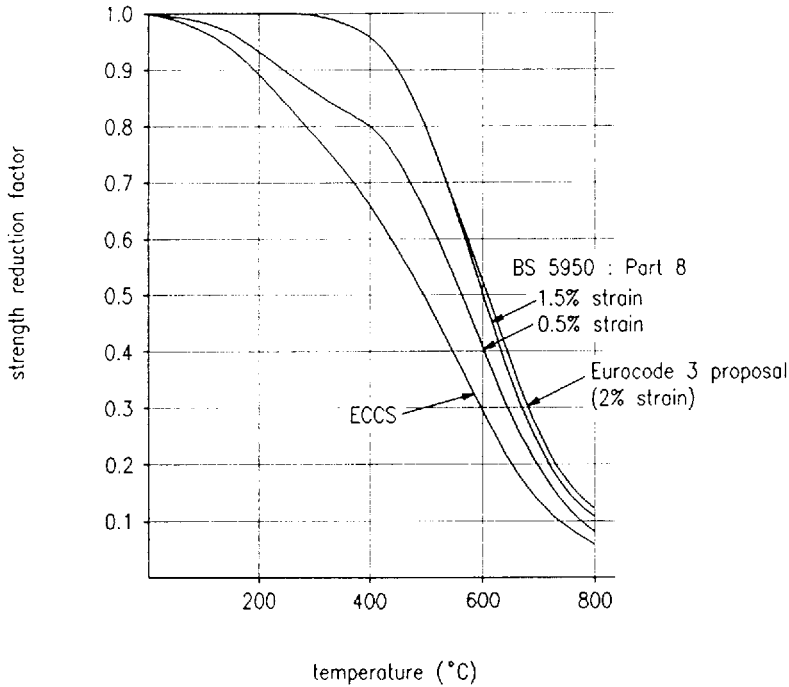


Fig. 34.3 Strength reduction factor for grade 43 steel at elevated temperatures

flattens off. This relationship is shown in Fig. 34.3. An important parameter is the strain at which the strength is assessed. It is reasonable to take a higher strain limit than in normal design, partly because there is a gradual increase of strength with strain at elevated temperatures, and partly because much higher deflections are attained in fire tests than in normal structural tests.

The relevant strain limit in BS 5950: Part 8 is 1.5%, which may be used for beam sections with 'robust' fire-protection materials, or for unprotected sections. A lower strain limit of 0.5% is used for more 'brittle' fire-protection materials, or for columns (in all cases). The 2% strain limit proposed in Eurocode 3, Part 10 gives results close to the 1.5% limit.

### 34.3.2 Performance of beams

Beams supporting concrete slabs behave better than uniformly heated sections, for which the material performance is the dominant factor. The concrete slab causes the top flange to be significantly cooler than the bottom flange and therefore the plastic neutral axis of the section rises close to the top flange (see Fig. 34.4).

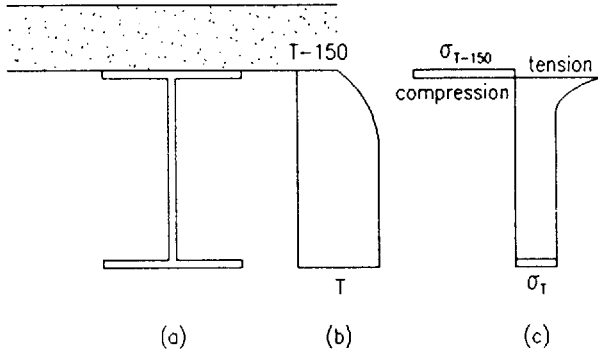


Fig. 34.4 Temperature and stress variation in I-beam supporting concrete slab when limiting temperature is reached. (a) Section through beam and slab. (b) Temperature variation. (c) Stress variation.

The section resistance is therefore determined by the strength of steel at 1.5% strain, but in this case, more of the web is effective in resisting tension.

The limiting temperatures of beams supporting concrete slabs are shown in Fig. 34.5 with the test results for a range of beam sizes and load ratios. These limiting temperatures are increased by about 60°C relative to a uniformly heated section.

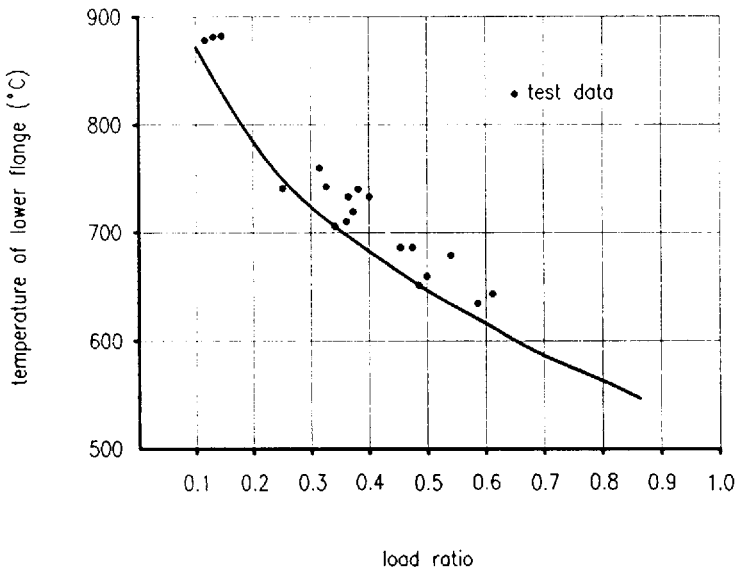


Fig. 34.5 Limiting temperatures for I-section beams supporting concrete floors

### 34.3.3 Performance of columns

Steel columns fail at a cross-section strain of less than 1%, and the 0.5% strain limit is taken as being appropriate when determining the limiting temperature of the members. This is applicable for columns up to the slenderness of 70 normally encountered in buildings.

The fire resistance of columns can be increased by partial protection in the form of concrete blocks or bricks, either by building into a wall or by fitting blocks between the flanges. A minimum fire resistance of 30 minutes can usually be achieved in this way.

Concrete-filled CHS or RHS columns can be used to provide typically 60 minutes fire resistance without additional fire protection. Intumescent coatings and reinforcement in the concrete can be used to provide enhanced fire resistance of these columns.

### 34.3.4 Performance of composite slabs

Modern steel frames often involve the use of composite slabs comprising steel decking acting compositely with the concrete floor (see Chapter 21). A large number of fire tests have now been carried out to justify the use of 90 minutes fire resistance for composite slabs with standard mesh reinforcement and no additional fire protection. Guidance is given in *Handbook to BS 5950: Part 8*.<sup>4</sup>

## 34.4 Methods of protection

Basic information on methods of protection is summarized in the Appendix.

### 34.4.1 Spray-applied protection

Sprays are the cheapest method with costs commonly in the range of £6 to £16/square metre applied (1990 prices), depending on the fire rating required and the size of the job. As implied, spray protection is applied around the exposed perimeter of the member and therefore the relevant section factors are for profile protection (see the Appendix *Limiting temperatures*). Application is fast and it is easy to protect complex shapes or connections. However, they are applied wet, which can create problems in winter conditions, they can be messy, and the appearance is often poor. For this reason they are generally used in hidden areas such as on beams above suspended ceilings, or in plant rooms.

### 34.4.2 Board protection

Boards tend to be more expensive, commonly in the range £9 to £30/square metre applied (1990 prices), because of the higher labour content in fixing. The price depends on the rating required and the surface finish chosen but tends to be less sensitive to job size. Board systems form a box around the section and therefore have a reduced heated perimeter in comparison to spray systems (see the Appendix *Limiting temperatures* and Fig. 34.1). They are dry fixed by gluing, stapling or screwing, so there is less interference with other trades on site, and the box appearance is often more suitable for frame elements, such as free-standing columns, which will be in view.

### 34.4.3 Intumescent coatings

Intumescent coatings achieve insulation in a totally different way; the insulating layer is formed only by the action of heat when the fire breaks out.

The coating is applied as a thin layer, perhaps as thin as 1 mm, but it contains a compound in its formulation which releases a gas when heat is applied. This gas inflates the coating into a thick carbonaceous foam, which provides heat insulation to the steel underneath. The coatings are available in a range of colours and may be used for aesthetic reasons on visible steelwork.

Two types of intumescent coating are currently available. The first, which is water resistant, has a maximum rating of 2 hours, but is expensive, costing up to £60/square metre (1990 prices). The second type has maximum ratings up to 1½ hours but is not so resistant to moisture and so is not recommended for wet applications such as swimming pools but is satisfactory in dry buildings. Costs range from about £10 to £20/square metre (1990 prices).

### 34.4.4 Concrete encasement

In comparison with these lightweight materials, protection by in situ concrete costs about £17 to £30/square metre of steelwork encased (1990 prices). However, concrete is often perceived as a 'traditional' fire-protection material and indeed data on its use is given in the Building Research Establishment publication *Guidelines for the Construction of Fire Resisting Structural Elements*.<sup>5</sup>

## 34.5 Fire testing

Fire testing requirements are based largely on the *Fire Grading of Buildings* report of 1946.<sup>6</sup> The fire-resistance periods refer to the time in a standard fire,

defined by BS 476: Parts 20 and 21,<sup>7</sup> that an element of structure (a column, beam, compartment wall, etc.) should maintain:

- (1) stability – it should not collapse under load at the fire limit state,
- (2) integrity – it should not crack or otherwise allow the passage of flame to an adjoining compartment,
- (3) insulation – it should not allow passage of heat by conduction which might induce ignition in an adjoining compartment.

The 'standard' fire time–temperature relationship defined in BS 476 is presented in Fig. 34.6. Most attention (and cost) is directed at satisfying the stability (or strength) criterion.

In a fire test columns are exposed to fire on all four sides and axially loaded vertically, whereas beams are loaded horizontally in bending and are exposed on three sides, the upper flange being in contact with the floor slab, which also acts as the furnace roof.

The stability limit is deemed to have been reached for columns when 'run-away' deflection occurs. For beams this is more accurately specified when the deflection rate reaches  $L^2/9000d$  (where  $L$  = beam span,  $d$  = beam depth), for deflections exceeding  $L/30$ . An upper limit on the total deflection is set at  $L/20$ .

Indicative (i.e. thermal) and loaded fire tests are also carried out on beams and columns to assess the performance of fire-protection materials. Interpolation from test results in Reference 3 is by an empirical method, but in BS 5950: Part 8 it is possible to use the thermal properties of the materials to assess the required protection. Some materials also benefit from stored moisture giving rise to the dwell in the temperature response shown in Fig. 34.7.

## 34.6 Fire engineering

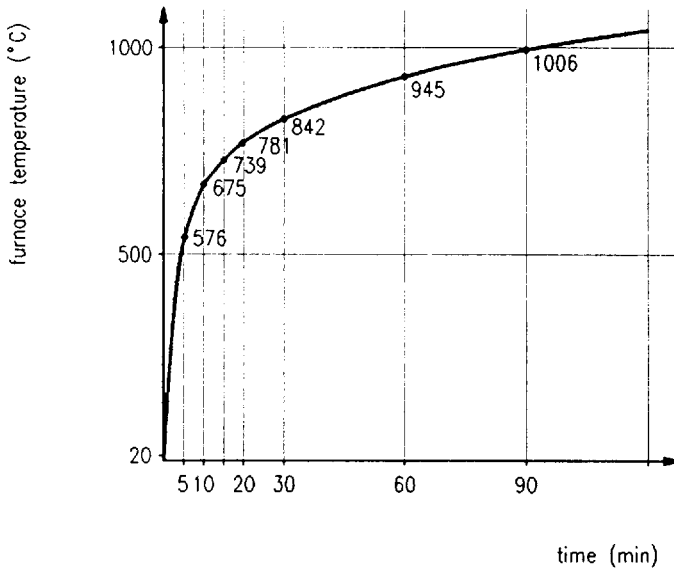
There are many special building forms which can take advantage of a rational approach, called 'fire engineering',<sup>8,9</sup> which takes account of the temperatures developed in a real fire, as opposed to a standard fire (see Fig. 34.6).

Essentially the fire engineering design method can be divided into two main steps:

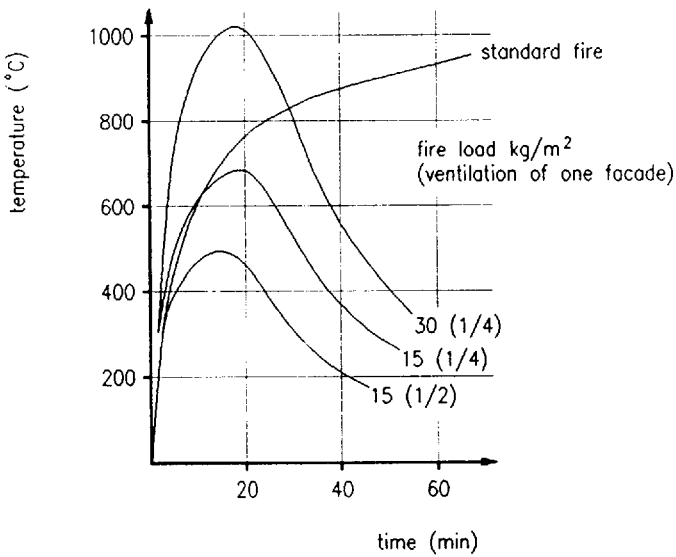
### (1) Determination of the fire load

The fire load of a compartment is the maximum heat that can theoretically be generated by the combustible items of contents and structure i.e. weight  $\times$  calorific value per unit weight.

Fire load is usually expressed in relation to floor area, sometimes as MJ/m<sup>2</sup> or Mcal/m<sup>2</sup> but more often converted to an equivalent weight of wood and expressed as 'kg wood/m<sup>2</sup>', (1 kg wood  $\equiv$  18 MJ). Standard data tables giving fire loads of different materials are available.<sup>8</sup>



(a)



(b)

Fig. 34.6 Temperature–time curves: (a) standard ISO fire test, (b) standard and natural fires in small compartments



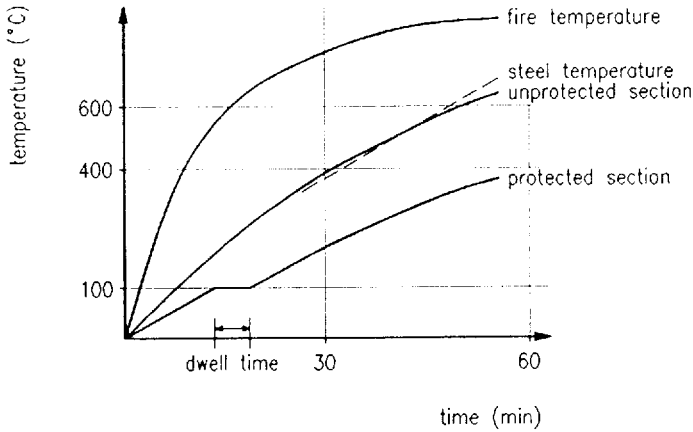


Fig. 34.7 Rate of heating in unprotected and protected sections

Examples of typical fire loads (wood equivalent) are:

|                    |                        |
|--------------------|------------------------|
| schools            | 15 kg/m <sup>2</sup>   |
| hospital wards     | 20 kg/m <sup>2</sup>   |
| hotels             | 25 kg/m <sup>2</sup>   |
| offices            | 35 kg/m <sup>2</sup>   |
| department stores  | 35 kg/m <sup>2</sup>   |
| textile warehouses | >200 kg/m <sup>2</sup> |

(2) Prediction of maximum compartment temperature

The heat that is retained in the burning compartment depends upon the thermal characteristics of the wall, floor and ceiling materials and the degree of ventilation. Sheet steel walls will dissipate heat by conduction and radiation while blockwork will retain heat in the compartment and lead to higher temperatures.

It is assumed that window glass breaks in fire conditions and calculations take into account the size and position of such ventilation. Openings close to the ceiling level of a compartment (or disintegrating roofing materials) will tend to dissipate heat whereas openings close to the floor will provide oxygen to feed the fire.

Since a great deal of data have been gathered over the years on the performance of materials in the standard fire test, methods have been sought to relate real fire conditions to standard fire performance in order that the existing data can be used in fire engineering. The 'time equivalent' or equivalent required fire resistance is given by:

$$T_{ceq} = CWQ_f$$

where  $Q_f$  = fire load density in MJ/m<sup>2</sup> i.e. the amount of combustible material per unit area of compartment floor,

$W$  = ventilation factor relating to the area and height of door and window openings,

$C$  = a constant relating to the thermal properties of the walls, floor and ceiling.

For large openings (greater than 10% of the floor area), the fire is 'fuel controlled' and  $W$  may be taken as 1.5. Conservatively,  $C$  may be taken as 0.09 for highly insulating materials.

It is not a concept that can be recommended for buildings that are subject to change of use, such as advance factory units, but many buildings are 'fixed' in terms of their occupancy (car parks, hospitals, swimming pools, etc.) and in such cases fire engineering is a valid approach. It is most appropriate for buildings of large volume with low fire load.

In the UK a number of buildings have been built using unprotected steel on fire engineering principles, one example being the north stand at Ibrox football ground in Glasgow.

Other examples of the use of calculation methods in determining structural response in fire are external steel in framed buildings,<sup>10</sup> and portal frames with fire-resistant boundary wall.<sup>11</sup>

## References to Chapter 34

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  11. Newman G.M. (1990) *Fire and Steel Construction – The Behaviour of Steel Portal Frames in Boundary Conditions*, 2nd edn. The Steel Construction Institute, Ascot, Berks.

### Further reading for Chapter 34

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EUROFER (1990) *Steel and Fire Safety – A Global Approach*. Eurofer, Brussels.  
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# Chapter 35

## Corrosion resistance

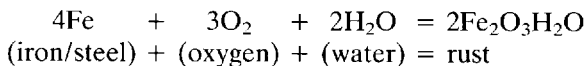
by KEN JOHNSON

### 35.1 The corrosion process

#### 35.1.1 General corrosion

Most corrosion of steel can be considered as an electrochemical process which occurs in stages. Initial attack occurs at anodic areas on the surface, where ferrous ions go into solution. Electrons are released from the anode and move through the metallic structure to the adjacent cathodic sites on the surface where they combine with oxygen and water to form hydroxyl ions. These react with the ferrous ions from the anode to produce ferrous hydroxide which itself is further oxidized in air to produce hydrated ferric oxide; red rust (Fig. 35.1).

The sum of these reactions is described by the following equation:



Two important points emerge:

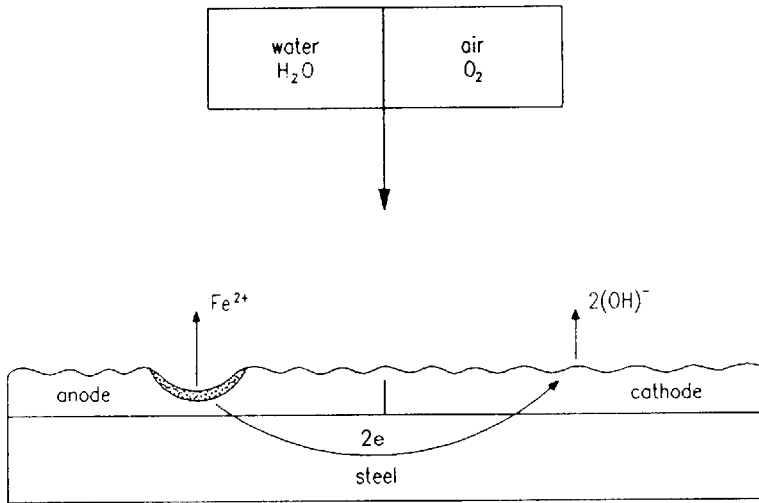
- (1) for iron or steel to corrode it is necessary to have the simultaneous presence of water and oxygen; in the absence of either, corrosion does not occur.
- (2) all corrosion occurs at the anode; no corrosion occurs at the cathode.

However, after a period of time, polarization effects such as the growth of corrosion products on the surface cause the corrosion process to be stifled. New, reactive anodic sites may then be formed thereby allowing further corrosion. Over long periods the loss of metal is reasonably uniform over the surface and so this case is usually described as 'general corrosion'.

#### 35.1.2 Other forms of corrosion

Various types of localized corrosion can also occur:

- (1) *Pitting corrosion*. In some circumstances the attack on the original anodic area is not stifled and continues deep into the metal, forming a corrosion pit.



reactions

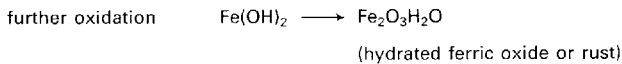
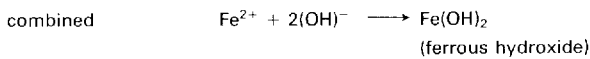
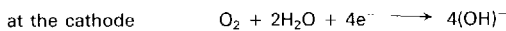


Fig. 35.1 Diagrammatic representation of the corrosion of steel

Pitting more often occurs with mild steels immersed in water or buried in soil rather than those exposed in air. Pitting can also occur on stainless steels in certain environments.

- (2) *Crevice corrosion*. Crevices can be formed by design-detailing, welding, surface debris, etc. Available oxygen in the crevice is quickly used by the corrosion process and, because of limited access, cannot be replaced. The entrance to the crevice becomes cathodic, since it can satisfy the oxygen-demanding cathode reaction. The tip of the crevice becomes a localized anode and high corrosion rates occur at this point.
- (3) *Bimetallic corrosion*. When two dissimilar metals are joined together in an electrolyte an electrical current passes between them and corrosion occurs on

**Table 35.1** Bimetallic corrosion and structural steelwork

|  |   |   |
|--|---|---|
| Magnesium and alloys<br>Zinc and alloys<br>Aluminium and alloys<br>Cadmium | ↑ | Tendency to inhibit corrosion of structural steels    |
| <hr/> Structural steels  |   |   |
| Cast irons<br>Stainless steels<br>Lead<br>Brasses<br>Copper<br>Bronzes     | ↓ | Tendency to accelerate corrosion of structural steels |

the anodic metal. Some metals (e.g. nickel and copper) cause steel to corrode preferentially whereas other metals corrode preferentially themselves, thereby protecting the steel. The tendency of dissimilar metals to bimetallic corrosion is partly dependent upon their respective positions in the galvanic series (Table 35.1): the further apart the two metals are in the series the greater the tendency. Other aspects which influence bimetallic corrosion are the nature of the electrolyte and the respective surface areas of the anodic and cathodic metals. Bimetallic corrosion is most serious for immersed or buried structures but should also be considered for steel in the atmosphere.

- (4) *Stress corrosion cracking.* This occurs under the simultaneous influence of a static tensile stress (or residual stress), which may be well below the yield strength of the steel, and a specific corrosive environment. Cracking occurs, which may lead to mechanical failure. This type of corrosion is not common with ferrous metals though some stainless steels are susceptible in chloride environments and mild steels can exhibit stress-corrosion cracking in the presence of nitrates or in highly alkaline solutions.
- (5) *Bacterial corrosion.* This can occur in soils and water as a result of microbiological activity. The most commonly encountered is that arising from the presence of sulphate-reducing bacteria. These reduce sulphates in the soil to sulphides and cause corrosion under anaerobic conditions (i.e. in the absence of oxygen). They are characterized by black corrosion products having the distinctive 'rotten-egg' smell of sulphide. Bacterial corrosion is most commonly encountered in pipelines and other buried structures and is rarely, if ever, found in driven steel piles.

### 35.1.3 Corrosion rates

The principal factors that determine the rate of corrosion of steel in air are:

- (1) the type and amount of pollution, e.g. sulphur dioxide, chlorides, dust
- (2) the 'time of wetness', i.e. the proportion of total time during which the surface is wet, due to rainfall, condensation, etc.
- (3) the temperature; though in the UK this is of less importance.

Within a given local environment corrosion rates can vary markedly. For example, steel may corrode more on a particular side of a building because it is in the shade and so remains wet for longer periods. Prevailing winds may carry airborne contaminants (e.g. chlorides, SO<sub>2</sub>) predominantly on to one face of a structure. It is therefore the 'microclimate' immediately surrounding the structure which determines corrosion rates for practical purposes.

## 35.2 Effect of the environment

Steel is most commonly used in the following environments:

- (1) *Rural atmospheric* – essentially inland, unpolluted environments; steel corrosion rates tend to be low, usually less than 50 microns per annum (NB 1 micron = 0.001 mm)
- (2) *Industrial atmospheric* – inland, polluted environments; corrosion rates are usually between 50–100 microns per annum, dependent upon level of SO<sub>2</sub>
- (3) *Marine atmospheric* – in the UK a two-kilometre strip around the coast is broadly considered as being in a marine environment; corrosion rates are usually between 50–100 microns per annum, largely dependent upon proximity to the sea
- (4) *Marine/industrial atmospheric* – polluted coastal environments which produce the highest corrosion rates e.g. between 50–150 microns/annum
- (5) *Sea-water immersion* – in tidal waters four vertical zones are usually encountered:
  - (a) the splash zone, immediately above the high-tide level, is usually the most corrosive zone with a mean corrosion rate of about 100 microns/annum
  - (b) the tidal zone, between high-tide and low-tide levels, is often covered with marine growths and exhibits low corrosion rates e.g. 50 microns/annum
  - (c) the low-water zone, a narrow band just below the low-water level, exhibits corrosion rates similar to the splash-zone
  - (d) the permanent immersion zone, from the low-water level down to bed level, exhibits low corrosion rates e.g. 50 microns/annum
- (6) *Fresh-water immersion* – corrosion rates are lower in fresh water than in salt water e.g. 30–50 microns/annum
- (7) *Soils* – the corrosion process is complex and very variable; various methods are used to assess the corrosivity of soils:

- (a) resistivity; generally high-resistance soils are least corrosive
- (b) redox potential; to assess the soil's capability of anaerobic bacterial corrosion
- (c) pH; highly acidic soils (e.g. pH less than 3.0) can be corrosive
- (d) water content; corrosion depends upon the presence of moisture in the soil, the position of the water-table has an important bearing.

Long buried steel structures, e.g. pipelines, are most susceptible to corrosion. Steel piles driven into undisturbed soils are much less susceptible due to the low availability of oxygen.

### **35.3 Design and corrosion**

Design can have an important bearing on the corrosion of steel structures. The prevention of corrosion should therefore be taken into account during the design stage of a project. The main points to be considered are:

- (1) Entrapment of moisture and dirt:
  - (a) avoid sharp edges, sharp corners, cavities, crevices
  - (b) welded joints are preferable to bolted joints
  - (c) avoid or seal lap joints
  - (d) edge-seal HSFG faying surfaces
  - (e) provide drainage holes for water, where necessary
  - (f) seal box sections
  - (g) provide free circulation of air around the structure.
- (2) Contact with other materials:
  - (a) avoid bimetallic connections or insulate the contact surfaces
  - (b) provide adequate depth of cover and quality of concrete (see BS 8110)
  - (c) separate steel and timber by the use of coatings or sheet plastics.
- (3) Coating application; design should ensure that the selected protective coatings can be applied efficiently:
  - (a) radius edges and corners
  - (b) provide vent-holes and drain-holes for items to be hot-dip galvanized
  - (c) provide adequate access for metal spraying, paint spraying, etc.
- (4) General factors:
  - (a) large flat surfaces are easier to protect than more complicated shapes
  - (b) ideally, locate load-bearing members in the least corrosive locations
  - (c) provide access for subsequent maintenance
  - (d) provide lifting lugs or brackets where possible to reduce damage during handling and erection.



BS 5493, Appendix A,<sup>1</sup> provides a detailed account of designing for the prevention of corrosion.

### 35.4 Surface preparation

Structural steel is a hot-rolled product. Sections leave the last rolling pass at about 1000°C and as they cool the steel surface reacts with oxygen in the atmosphere to produce mill-scale, a complex oxide which appears as a blue-grey tenacious scale completely covering the surface of the as-rolled steel section. Unfortunately, mill-scale is unstable. On weathering, water penetrates fissures in the scale and rusting of the steel surface occurs. The mill-scale loses adhesion and begins to shed. Mill-scale is therefore an unsatisfactory base and needs to be removed before protective coatings are applied.

As mill-scale sheds, further rusting occurs. Rust is a hydrated oxide of iron which forms at ambient temperatures, producing a layer on the surface which is itself an unsatisfactory base and also needs to be removed before protective coatings are applied.

Surface preparation of steel is therefore principally concerned with removal of mill-scale and rust. Various methods of surface preparation are available:

(1) *Manual preparation*

The simplest form of surface preparation. It involves chipping, scraping and brushing with hand-held implements. Although the method is not very effective (only about 30% removal of rust and scale can be achieved) it is nevertheless often used, usually for economic reasons. The degree of cleaning achieved can be specified by reference to the St series of photographic standards included in BS 7079 Part A1: 1989 (ISO 8501-1: 1988).

(2) *Mechanical preparation*

Similar to manual preparation but utilizes power-driven tools, e.g. rotary wire brushing. A marginal improvement in efficiency can be achieved (up to 35%), and the same photographic standards can be used. Care must be taken to avoid confusing burnished scale with clean steel, both of which have a similar appearance.

The above methods are used on site, usually after a weathering period to promote loosening of mill-scale. A suitable primer must then be applied, which is tolerant of poor surface preparation. Many modern primers are quite unsuitable for such surfaces and, indeed, the old tried and trusted red lead in oil primers (e.g. BS 2523 Type B) cannot be bettered for manually cleaned surfaces.

(3) *Flame cleaning*

Not used extensively in the UK. An oxy-gas flame is applied to the surface. Differential thermal expansion and steam generated behind the mill-scale

serve to loosen the mill-scale layer, which can then be removed by mechanical scraping.

(4) *Acid pickling*

The steel is immersed in a bath of suitably inhibited acids which dissolve or remove mill-scale and rust but do not appreciably attack the exposed steel surface. It can be 100% effective.

Acid pickling is always used on structural steel intended for hot-dip galvanizing but is now rarely used as a pre-treatment before painting.

(5) *Blast-cleaning*

Abrasive particles are projected at high speed on to the steel surface. The abrasive can consist of either spherical particles, described as 'shot', or angular particles, described as 'grit'.

The abrasive is projected towards the surface either in a jet of compressed air or by centrifugal impeller wheel. The particles impinge on the steel surface, removing scale and rust, producing a rough, clean surface. The size and shape of the surface roughness produced is largely dependent upon the size and shape of the abrasive used; angular grits produce angular surface profiles, round shots produce a rounded profile.

Grit-blast abrasives can be either metallic (e.g. chilled iron grit) or non-metallic (e.g. slag grit). The latter are used only once and are referred to as 'expendable'. They are used exclusively for site work. Metallic grits are expensive and are used only where they can be recycled.

Grit blasting is always used for metal-sprayed coatings, where adhesion is at least partly dependent upon mechanical keying. It is also used for some paint coatings, particularly on site and for primers where adhesion may be a problem (e.g. zinc silicates).

Shot-blast abrasives are always metallic, usually cast steel shot, and are used particularly on shot-blast plants, utilizing impeller wheels and abrasive recycling. They are the preferred abrasive for paints, particularly for thin film coatings (e.g. prefabrication primers).

Blast-cleaned surfaces are normally specified in terms of surface cleanliness and surface roughness. A number of standards have been used in the past, including BS 4232 and Swedish Standard SIS 055900. These are now superseded by ISO 8501-1: 1988 (BS 7079: Part A1: 1989) which utilises photographic replicas of four grades of surface cleanliness after blast-cleaning: Sa1, Sa2, Sa2.5 and Sa3.

Surface roughness of blast-cleaned surfaces is defined in ISO 8503-1: 1988 and Parts 2, 3 and 4 of this standard describe methods of measuring surface roughness.

(6) *Wet-blasting*

A further variation on the blast-cleaning process. In this process a small amount of water is entrained in the abrasive/compressed air stream. This is particularly useful in washing from the surface soluble iron salts that are formed in the rust by atmospheric pollutants (e.g. chlorides and sulphates) during weathering. These are often located deep in corrosion pits on the steel

surface and cannot be removed by conventional dry blast-cleaning methods. Wet-blasting has proved to be particularly useful on offshore structures and prior to maintenance painting of structures in heavily-polluted environments.

## **35.5 Metallic coatings**

There are four commonly used methods of applying metal coating to steel surfaces: hot-dip galvanizing, metal spraying, electroplating and sherardizing. The latter two processes are not used in structural steelwork but are used for fittings, fasteners and other small items.

In general the corrosion protection afforded by metallic coatings is largely dependent upon the choice of coating metal and its thickness and is not greatly influenced by the method of application.

### **35.5.1 Hot-dip galvanizing**

The most common method of applying a metal coating to structural steel is by galvanizing. Hot-dipping processes are used for the application of other metals, e.g. aluminium, lead/tin (terne), but these are not used on structural steelwork.

The galvanizing process involves the following stages:

- (1) The steel is cleaned of all rust and scale by acid pickling. This may be preceded by blast-cleaning to remove scale and roughen the surface but such surfaces are always subsequently pickled in hydrochloric acid producing ferric chloride on the steel surface which acts as a flux for the hot-dip process.
- (2) The cleaned and fluxed steel is dipped into a bath of molten zinc at a temperature of about 450°C at which the steel reacts with the molten zinc to form a series of zinc/iron alloys on its surface.
- (3) As the steel workpiece is removed from the bath a layer of relatively pure zinc is deposited on top of the alloy layers.

As the zinc solidifies it assumes a crystalline metallic lustre, usually referred to as 'spangling'. The thickness of the galvanized coating is influenced by various factors:

- (1) The size of the workpiece; thicker, heavier sections tend to produce heavier coatings.
- (2) The steel surface; blast-cleaned surfaces tend to produce heavier coatings.
- (3) The steel composition. Silicon, particularly, can have a marked effect on the coating weight deposited. The thickness of the coating varies with the silicon content of the steel and bath immersion time. These thick coatings sometimes have a dull dark-grey appearance and can be brittle and less adherent.

Since this is a bath-dipping process there is obviously some limitation on the size of components which can be galvanized. Double-dipping can often be used when the length or width of the workpiece exceeds the size of the bath.

Some aspects of design need to take the galvanizing process into account:

- (1) Filling, venting and draining. Holes not less than 10 mm diameter must be provided in hollow articles (e.g. tubes, rectangular hollow sections) to allow rapid access for molten zinc, venting of hot gases and subsequent draining of zinc.
- (2) Distortion of fabricated steelwork can be caused by differential thermal expansion and contraction and by relief of residual stresses.

The specification of hot-dip galvanized coatings for structural steelwork is covered by BS 729 which requires, for sections not less than 5 mm thick, a minimum mean zinc coating weight of 610 g/m<sup>2</sup>, equivalent to a coating thickness of 85 microns. The coating will usually protect the underlying steel for up to 30 years in a clean rural environment and between 10 and 25 years in marine and urban situations. However, in heavily-polluted environments durability can be reduced to less than 10 years.

For most applications galvanizing does not need to be painted. Where, for reasons of extra durability or decorative effect, there is a need to paint, then special primers are normally required such as calcium plumbate and etch primers.

### **35.5.2 Metal spray coatings**

An alternative method of applying a metallic coating to structural steelwork is by metal-spraying of either zinc or aluminium. The metal, in powder or wire form, is fed through a special spray-gun containing a heat source which can be either an oxy-gas flame or an electric-arc. Molten globules of the metal are blown by a compressed air jet on to the previously blast-cleaned steel surface. No alloying occurs and the coating which is produced consists of overlapping platelets of metal and is porous. The pores are subsequently sealed, either by applying a thin organic coating which soaks into the surface, or by allowing the metal coating to weather, when corrosion products block the pores.

The adhesion of sprayed metal coatings to steel surfaces is considered to be essentially mechanical in nature. It is therefore necessary to apply the coating to a clean roughened surface for which blast-cleaning with a coarse grit abrasive is normally specified, usually chilled-iron grit, but for steels with a hardness exceeding 360 HV, alumina or silicon carbide grits may be necessary.

Coating thickness varies from 100–250 microns for aluminium to 75–400 microns for zinc. The metals perform similarly in most environments but aluminium is more durable in highly industrial environments.

Metal spray coatings can be applied in the shops or at site and there is no limitation on the size of the workpiece, as there is with hot-dip galvanizing. Since the steel surface remains cool there are no distortion problems. However, metal spraying is considerably more expensive than hot-dip galvanizing.

For many applications metal-spray coatings are further protected by the subsequent application of paint coatings. A sealer is first applied which fills the pores in the metal spray coating and provides a smooth surface for application of the paint coating.

The protection of structural steelwork against atmospheric corrosion by metal-sprayed aluminium or zinc coatings is covered in BS 2569: Part 1:

## 35.6 Paint coatings

Painting is the principal method of protecting structural steelwork from corrosion.

### 35.6.1 Composition of paints and film-formation

Paints are made by mixing and blending three main components:

- (1) Pigments; finely ground inorganic or organic powders which provide colour, opacity, film-cohesion and sometimes corrosion-inhibition.
- (2) Binders; usually resins or oils but can be inorganic compounds such as soluble silicates. The binder is the film-forming component in the paint.
- (3) Solvents; used to dissolve the binder and to facilitate application of the paint. Solvents are usually organic liquids or water.

Paints are applied to steel surfaces by many methods but in all cases they produce a 'wet film'. The thickness of the 'wet film' can be measured, before the solvent evaporates, using a comb-gauge.

As the solvent evaporates, film-formation occurs, leaving the binder and pigments on the surface as a 'dry film'. The thickness of the 'dry film' can be measured, usually with a magnetic induction gauge.

The relationship between the applied 'wet film' thickness and the final 'dry film' thickness (d.f.t.) is determined by the percentage volume solids of the paint, i.e.

$$\text{d.f.t.} = \text{'wet film' thickness} \times \% \text{ vol. solids}$$

In general the corrosion protection afforded by a paint film is directly proportional to its dry film thickness.

### 35.6.2 Classification of paints

Since, in the broadest terms, a paint consists of a particular pigment, dispersed in a particular binder, dissolved in a particular solvent, the number of generic types of paint is limited. The most common methods of classifying paints are either by their pigmentation or by their binder-type.

Primers for steel are usually classified according to the main corrosion-inhibitive pigments used in their formulation, e.g. zinc phosphate, zinc chromate, red-lead, metallic-zinc. Each of these inhibitive pigments can be incorporated into a range of binder resins, e.g. zinc phosphate alkyd primers, zinc phosphate epoxy primers, zinc phosphate chlorinated-rubber primers.

Intermediate coats and finishing coats are usually classified according to their binders, e.g. vinyl finishes, urethane finishes.

### 35.6.3 Painting systems

Paints are usually applied one coat on top of another, each coat having a specific function or purpose.

The primer is applied directly on to the cleaned steel surface. Its purpose is to wet the surface and to provide good adhesion for subsequently applied coats. Primers for steel surfaces are also usually required to provide corrosion inhibition.

The intermediate coats (or undercoats) are applied to build the total film thickness of the system. This may involve the application of several coats.

The finishing coats provide the first-line defence against the environment and also determine the final appearance in terms of gloss, colour, etc.

The various superimposed coats within a painting system have, of course, to be compatible with one another. They may be all of the same generic type or may be different, e.g. chlor-rubber-based intermediate coats may be applied on to an epoxy primer. However, as a first precaution, all paints within a system should normally be obtained from the same manufacturer.

### 35.6.4 Main generic types of paint and their properties

- (1) *Air-drying paints*, e.g. oil-based, alkyd, epoxy-ester, dry and form a film by an oxidative process which involves absorption of oxygen from the atmosphere. They are therefore limited to relatively thin films. Once the film has formed it has limited solvent resistance and usually poor chemical resistance.
- (2) *One-pack chemical-resistant paints*, e.g. chlor-rubbers, vinyls, form a film by solvent evaporation and no oxidative process is involved. They can be applied as moderately thick films, although retention of solvent in the film can be a

problem at the upper end of the range. The film formed remains relatively soft, and has poor solvent resistance but good chemical resistance.

Bituminous paints also dry by solvent-evaporation. They are essentially solutions of either asphaltic bitumen or coal-tar pitch in organic solvents.

- (3) *Two-pack chemical-resistant paints*, e.g. epoxy, urethane, are supplied as two separate components, usually referred to as the base and the curing agent. When the two components are mixed, immediately before use, a chemical reaction begins. These materials therefore have a limited 'pot-life' by which the mixed coating must be applied. The polymerization reaction continues after the paint has been applied and after the solvent has evaporated to produce a densely cross-linked film which can be very hard and has good solvent and chemical resistance.

Liquid resins of low viscosity can be used in the formulation thereby avoiding the need for a solvent. Such coatings are referred to as 'solventless' or 'solvent-free' and can be applied as very thick films.

A summary of the main generic types of paint and their properties is shown in Table 35.2.

### **35.6.5 Blast-primers (also referred to as prefabrication primers, shop-primers, weldable primers, temporary primers, holding primers, etc.)**

These primers are used on structural steelwork, immediately after blast-cleaning, to hold the reactive blast-cleaned surface in a rust-free condition until final painting can be undertaken. They are mainly applied to steel plates and sections before fabrication. The main requirements of a blast-primer are as follows:

- (1) The primer should be capable of airless-spray application to produce a very thin even coating. Dry-film thickness is usually limited to 15–30 microns. Below 15 microns the peaks of the blast profile are not protected and 'rust-rashing' occurs on weathering. Above 30 microns the primer affects the quality of the weld and produces excessive weld-fume.
- (2) The primer must dry very quickly. Priming is often done in-line with automatic blast-cleaning plant which may be handling plates or sections at a pass-rate of 1–3 metres/minute. The interval between priming and handling is usually of the order of 1–10 minutes and hence the primer film must dry within this time.
- (3) Normal fabrication procedures e.g. welding, gas-cutting, must not be significantly impeded by the coating.
- (4) The primer should not cause excessive weld-porosity. (*NB* at the present time there are no blast-primers available which are compatible in this respect with the submerged-arc welding process and in this case the primer has to be removed before welding.)

**Table 35.2** Main generic types of paint and their properties

|                          | Cost        | Tolerance of poor surface preparation | Chemical resistance | Solvent resistance | Over-coatability after ageing   | Other comments   |
|--------------------------|-------------|---------------------------------------|---------------------|--------------------|---------------------------------|--|
| Bituminous               | Low         | Good                                  | Moderate            | Poor               | Good with coatings of same type | Limited to black and dark colours<br>Thermoplastic             |
| Oil based                | Low         | Good                                  | Poor                | Poor               | Good                            | Cannot be overcoated with paints based on strong solvent       |
| Alkyd, epoxy-ester, etc. | Low-medium  | Moderate                              | Poor                | Poor-moderate      | Good                            | Good decorative properties                                     |
| Chlor-rubber             | Medium      | Poor                                  | Good                | Poor               | Good                            | High-build films remain soft and are susceptible to 'sticking' |
| Vinyl                    | High        | Poor                                  | Good                | Poor               | Good                            |  |
| Epoxy                    | Medium-high | V. poor                               | V. good             | Good               | Poor                            | Very susceptible to chalking in UV                             |
| Urethane                 | High        | V. poor                               | V. good             | Good               | Poor                            | Better decorative properties than epoxies                      |
| Inorganic silicate       | High        | V. poor                               | Moderate            | Good               | Moderate                        | May require special surface preparation                        |



- (5) Weld-fumes emitted by the primer must not exceed the appropriate occupational exposure limits. Proprietary primers are tested and certificated by the North of England Industrial Health Service.
- (6) The primer coating should provide adequate protection. It should be noted that many manufacturers make misleading claims about the durability of their blast-primers and suggested exposure periods of 6–12 months are not uncommon. In practice, such claims are never met except in the least arduous conditions, e.g. indoor storage. In aggressive conditions, durability can be measured in weeks rather than months.
- (7) The primed surface, after weathering, should require the minimum of preparation for subsequent painting and must be compatible with the intended painting system.

Many proprietary blast-primers are available but they can be classified under the following main generic types:

- (1) *Etch primers* are based on polyvinyl butyral resin reinforced with a phenolic resin to uprate water resistance. The curing agent contains phosphoric acid or alkyl phosphates and can be added as a separate component immediately before application. Alternatively the primer can be supplied in a single-pack form.

In general, two-pack etch primers provide better durability than the one-pack types which are usually preferred because of their handling convenience, particularly on automatic spraying plants.

- (2) *Epoxy primers* are two-pack materials utilizing epoxy resins and usually either polyamide or polyamine curing agents. They are pigmented with a variety of inhibitive and non-inhibitive pigments. Zinc phosphate epoxy primers are the most frequently encountered and give the best durability within the group.
- (3) *Zinc epoxy primers* can be subdivided into zinc-rich and reduced-zinc types. Zinc-rich primers produce films which contains about 90% by weight of metallic zinc powder. These primers provide the highest order of protection of all blast-primers.

Reduced-zinc primers are formulated with metallic zinc content as low as 55% by weight on the dry film, the remainder of the pigmentation usually being made up with siliceous extenders. This reduces the cost of the primer, avoids possible difficulties with intercoat adhesion in marine environments, but slightly reduces the standard of protection that can be achieved.

Zinc epoxy primers all produce zinc oxide fumes during welding and gas-cutting which can cause a health-hazard. When exposed in either marine or highly industrial environments, zinc epoxy primers are prone to the formation of insoluble white zinc corrosion products which must be removed from the surface before subsequent overcoating.

- (4) *Zinc silicate primers* can be based upon either ethyl silicate or inorganic silicates e.g. sodium or potassium. Only the ethyl silicate primers are suitable as blast-primers.

Ethyl zinc silicate primers produce a level of protection which is comparable with the zinc-rich epoxy types and they suffer from the same drawbacks, e.g. formation of zinc salts and production of zinc oxide fumes during welding. They are however more expensive and usually are less convenient to use.

### **35.7 Application of paints**

The method of application and the conditions under which paints are applied have a significant effect on the quality and durability of the coating.

#### **35.7.1 Methods of application**

The standard methods used for applying paints to structural steelwork are brush, roller, conventional air-spray, and airless-spray, although other methods, e.g. dipping, can be used.

- (1) Brush. The simplest and also the slowest and therefore most expensive method. Nevertheless it has certain advantages over the other methods, e.g. better wetting of the surface; can be used in restricted spaces; useful for small areas; less wastage; less contamination of surroundings; can be used for application of certain toxic materials like lead-based primers which cannot be sprayed.
- (2) Roller. Much quicker than brushing; useful for large flat areas; demands suitable rheological properties of the paint.
- (3) Air-spray. The paint is atomized at the gun-nozzle by jets of compressed air; application rates are quicker than for brushing or rolling; paint wastage by overspray is high.
- (4) Airless-spray. The paint is atomized at the gun-nozzle by very high hydraulic pressures; application rates are higher than for air-spray and overspray wastage is greatly reduced.

Airless-spraying has become the most commonly used method of applying paint coatings to structural steelwork under controlled shop-conditions. Brush and roller application are more commonly used for site-application, though spraying methods are also used.

#### **35.7.2 Conditions for application**

The principal conditions which affect the application of paint coatings are temperature and humidity. These can be more easily controlled under shop-conditions than on site.

- (1) **Temperature.** Air temperature and steel temperature affect solvent evaporation, brushing and spraying properties, drying and curing times, pot-life of two-pack materials, etc. Heating, if required, should only be by indirect methods.
- (2) **Humidity.** Paints should not be applied when there is condensation present on the steel surface or the relative humidity of the atmosphere is such that it will affect the application or drying of the coating. Normal practice is to measure the steel temperature with a contact thermometer and to ensure that it is maintained at at least 3°C above dew-point.

## 35.8 Weathering steels

Weathering steels are high-strength, low-alloy weldable structural steels which possess excellent weathering resistance in many atmospheric conditions. They contain up to 3% of alloying elements, e.g. chromium, copper, nickel, phosphorus. On exposure to air, under suitable conditions, they form an adherent protective oxide coating. This acts as a protective film which, with time and under appropriate conditions, causes the corrosion rate to reduce until it reaches a low terminal level. Conventional coatings are therefore not usually necessary since the steel provides its own protection.

Weathering steels have properties comparable with those of grade 50 steels to BS 4360. They carry a material cost premium of about 25% over mild steel but in many cases this can be substantially reduced if advantage is taken of the greater corrosion resistance and 30% greater yield strength than mild steel.

BS 4360 *Specification for weldable structural steels* includes weathering steels, designated WR50 grades. Corten, one of the best known proprietary weathering steels, is also manufactured by British Steel, under licence to the United States Steel Corporation.

### 35.8.1 Formation of the protective oxide layer

During the early part of their life weathering steels corrode in a similar manner and at a similar rate to mild steels. As the protective oxide layer develops, the corrosion rate falls to a low terminal level (Fig. 35.2). The time required for a weathering steel to form a stable protective coating depends upon its orientation, the degree of atmospheric pollution and the frequency with which the surface is wetted and dried. The steel should be blast-cleaned, to remove mill-scale, before exposure in order to provide a sound uniform surface for the formation of the oxide coatings. Under appropriate conditions a stable oxide patina will be established in about two years, changing in colour from brown through to almost black, although the ultimate colour will depend upon the conditions of the site.

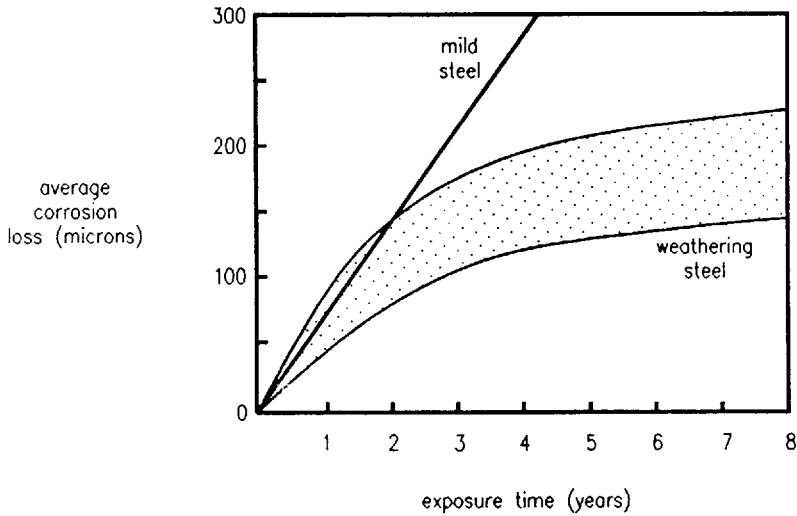


Fig. 35.2 Corrosion rates of mild and weathering steel in the UK

### 35.8.2 Precautions and limitations

During fabrication and erection care must be taken in handling and storage of bare weathering steel sections and sub-assemblies. Unsightly gouges, scratches, dents, etc. should be avoided. Scale and discoloration produced by welding should be removed from all exposed surfaces. Staining by concrete, mortar, oil, paint, marking crayons, etc. should be avoided. If such staining occurs additional cleaning is necessary to remove these blemishes.

Drainage of corrosion products can be expected during the first two or three years' exposure which can stain or streak adjacent materials, e.g. concrete piers. Provision should be made to divert this from vulnerable surfaces.

A continually wet surface will cause weathering steels to corrode at an unacceptably high rate. Detailing should therefore avoid crevices, or other water-retention areas. Drainage and ventilation should be provided. All interior surfaces, e.g. box girders, and faying surfaces should be painted or sealed to prevent entry of moisture. Bare weathering steel is not a completely maintenance-free material and structures should be periodically inspected to ensure that all joints and surfaces are performing satisfactorily.

Dissimilar metals such as stainless steel, anodized aluminium, copper, bronze and brass can generally be used adjacent to weathering steels providing the coupled area does not act as a crevice which might collect and hold water and debris. Zinc- and cadmium-coated items are not suitable for use in contact with weathering steels.

Weathering steels should not be used in the bare condition in certain environments, e.g. where

- (1) the steel surface would be exposed to recurrent wetting by salt water or salt water spray (the Department of Transport Standard BD/7/81 prohibits weathering steel bridges in highly marine environments or in situations where the steel would be subjected to de-icing salt spray).
- (2) high concentrations of strong chemical or industrial fume are present.
- (3) the steel is buried in soil as it will not provide corrosion resistance greater than mild steel. If, for example, columns are taken below ground level conventional methods of protection such as concrete encasement or a high-quality coating are generally suitable and the protection must extend for a small distance above the ground level.
- (4) the steel is immersed in water as it will not provide corrosion resistance greater than mild steel.

Bare weathering steels are not intended for interior architectural applications where the controlled atmosphere would restrict the development of the protective oxide layer.

### **35.8.3 Welding and bolted connections**

Weathering steels can be welded by all the usual methods, manual metal arc, gas shielded, submerged arc, and electrical resistance, including spot-welding. Mild steel electrodes can be used for ordinary single-pass welds for steel less than 12 mm thick since diffusion of alloyed base-metal into the filler-metal will result in a weld-bead having corrosion resistance and colour conversion similar to that of the weathering steel.

For multi-pass welds or where the weathering appearance of welded areas is particularly important, electrodes containing 2.5% – 3.5% nickel should be used.

Since any interruption in the surface of the structure can cause the oxide coating to develop unevenly, welds may be dressed flush.

For structural joints where high-strength bolts are required, ASTM A325, Type 3 bolts (Corten X) must be used. Where lower-strength bolts are satisfactory these may be in Corten A or stainless steel. Galvanized, sherardized or electroplated nuts and bolts are not suitable for use in weathering steel structures since, in time, the coatings will be consumed leaving an exposed fastener which is less corrosion resistant than the surrounding weathering steel.

### **35.8.4 Painting of weathering steels**

The painting requirements for weathering steels do not differ from those for mild steel. They require the same surface preparation and the same painting systems

may be used. Claims have been made that in many circumstances the durability of painting systems is greater on weathering steel than on mild steel.

## **35.9 The protective treatment specification**

### **35.9.1 Factors affecting choice**

For a given structure the following will be largely predetermined:

- (1) The expected life of the structure and the feasibility of maintenance
- (2) The environment/s to which the steelwork will be subjected
- (3) The size and shape of the structural members
- (4) The shop-treatment facilities which are available to the fabricator and/or his coatings sub-contractor
- (5) The site conditions which will determine whether the steelwork can be treated after erection
- (6) The money which is available to provide protection.

These facts, and possibly others, have to be considered before making decisions on:

- the types of coating to be used,
- the method of surface preparation,
- the method/s of application,
- the number of coats and the thickness of each coat.

In general, each case has to be decided on its own merits. However, the following points may be of assistance in making these decisions:

- (1) Protection requirements are minimal inside dry, heated buildings. Hidden steelwork in such situations requires no protection at all.
- (2) The durability of painting systems is increased several times over by using blast-cleaning rather than manual surface preparation.
- (3) Shot-blasting is preferred for most painting systems.
- (4) Grit-blasting is essential for metal-spraying and some primers, e.g. zinc silicates.
- (5) If blast-cleaning is to be used, two alternative process routes are available, i.e.
  - (a) blast/prime/fabricate/repair damage
  - (b) fabricate/blast/prime

The former is usually cheaper but requires the use of a weldable prefabrication primer.

- (6) Prefabrication primers have to be applied to blast-cleaned surfaces as thin films, usually 25 microns maximum. Their durability is therefore limited and further shop-coating is often desirable.
- (7) Manual preparation methods are dependent upon weathering to loosen the mill-scale. These methods are therefore not usually appropriate for shop-treatments. On site an adequate weathering period must be allowed.
- (8) Many modern primers based on synthetic resins are not compatible with manually prepared steel surfaces since they have a low tolerance for rust and scale.
- (9) Many oil-based and alkyd-based primers cannot be overcoated with finishing coats which contain strong solvents, e.g. chlorinated rubbers, epoxies, bituminous coatings, etc.
- (10) Two-pack epoxies have poor resistance to UV radiation and are highly susceptible to 'chalking'. Overcoating problems can arise with two-pack epoxies unless they are overcoated before the prior coat is fully cured. This is particularly relevant when an epoxy system is to be applied partly in the shops and partly on site.
- (11) Steelwork which is to be encased in concrete does not normally require any other protection, given an adequate depth of concrete cover (British Standard BS 8110).
- (12) Perimeter steelwork hidden in cavity walls falls into two categories:
  - (a) Where an air gap (40 mm min.) exists between the steelwork and the outer brick or stone leaf, then adequate protection can be achieved by applying relatively simple painting systems.
  - (b) Where the steelwork is in direct contact with the outer leaf, or is embedded in it, then the steel should be hot-dip galvanized and painted.
- (13) Where fire-protection systems are to be applied to the steelwork, consideration must be given to the question of compatibility between the corrosion-protection and the fire-protection systems.
- (14) New hot-dip galvanized surfaces can be difficult to paint and, unless special primers are used, adhesion problems can arise. Weathering the zinc surface before painting reduces this problem.
- (15) Metal spraying produces a porous coating which can be sealed by applying either a thin etch-primer or a bituminous solution. Further painting is then optional.
- (16) Particular attention should be paid to the treatment of weld areas. Flux residues and weld-spatter should be removed before application of coatings. In general the objective should be to achieve the same standard of surface preparation and coating on the weld area as on the general surface.
- (17) Black-bolted joints require protection of the contact surfaces. This is normally restricted to the priming coat, which can be applied either in the shops or on site before the joint is assembled.
- (18) For high-strength friction-grip bolted joints, the faying surfaces must be free of any contaminant or coating which would reduce the slip-factor required

on the joint. Some metal-spray coatings and some inorganic zinc silicate primers can be used but virtually all organic coatings adversely affect the slip-factor.

### 35.9.2 Writing the specification

The specification is intended to provide clear and precise instructions to the contractor on what is to be done and how it is to be done. It should be written in a logical sequence, starting with surface preparation, going through each paint-coat to be applied and finally dealing with specific areas e.g. welds. It should also be as brief as possible, consistent with providing all the necessary information. The most important items of a specification are as follows:

- (1) The method of surface preparation and the standard required, which can often be specified by reference to an appropriate standard, e.g. ISO 8501-1, Sa2-3
- (2) The maximum interval between surface preparation and subsequent priming.
- (3) The types of paint to be used, supported by standards where these exist.
- (4) The method/s of application to be used.
- (5) The number of coats to be applied and the interval between coats.
- (6) The wet and dry film thickness for each coat
- (7) Where each coat is to be applied (e.g. shop or site) and the application conditions that are required, in terms of temperature, humidity, etc.
- (8) Details for treatment of welds, connections, etc.
- (9) Rectification procedures for damage, etc.

Possibly the most convenient method of presenting this information is in tabular form and an example is shown in Table 35.3.

### Reference to Chapter 35

1. British Standards Institution (1977) *Code of practice for protective coating of iron and steel structures against corrosion*. BS 5493, BSI, London.

### Further reading for Chapter 35

See Appendix *Basic data on corrosion* for extracts from British Steel Publications *Corrosion Protection Guides*.



**Table 35.3** Protective coating specification for structural steelwork (example)

|                                     |  | Surface preparation                                   |                      | Before fabrication or After fabrication       |                        |
|-------------------------------------|--|---|----------------------|---|------------------------|
| Contract no. – 1234/56/R            |  | Shot-blast  |                      | Maximum interval before overcoating – 4 hours |                        |
| Client – J. Bloggs                  |  | Grit-blast  |                      | Level of inspection – Periodic                |                        |
| Project title – Docklands Warehouse |  | Other   |                      | Other comments –                              |                        |
| Date – 27.6.90                      |  | Standard – Sa. 2.5                                    |                      |   |                        |
|                                     |  | 1st coat  | 2nd coat             | 3rd coat                                      | 4th coat               |
|                                     |  | Shop or Site  | Shop or Site         | Shop or Site                                  | Shop or Site           |
| Brand name of paint                 |  | Excote 2  | Excote HB ZP         | Excote HB CR                                  | Excote CR              |
| Generic type                        |  | Zinc-rich epoxy                                       | Zinc phosphate epoxy | HB chlor rubber                               | Chlor rubber finish    |
| Reference number                    |  | 1/597/P   | 5/643/u              | 3/124/u                                       | 4/610/F                |
| Specification                       |  | BS 4652 Type 3  | N/A                  | N/A   | N/A                    |
| Supplier                            |  | A.N. Other  | A.N. Other           | A.N. Other                                    | A.N. Other             |
| Method of application               |  | Airless spray   | Airless spray        | Airless spray or brush                        | Airless spray or brush |
| Wet film thickness                  |  | N/A   | 150 µm               | 250 µm  | 75 µm                  |
| Dry film thickness                  |  | 20 µm   | 75 µm                | 75 µm   | 25 µm                  |
| Spreading rate                      |  | 10 m <sup>2</sup> /l                                  | 5 m <sup>2</sup> /l  | 2.5 m <sup>2</sup> /l                         | 10 m <sup>2</sup> /l   |
| Minimum temperature                 |  | 10°C  | 5°C                  | 5°C   | 5°C                    |
| Maximum relative humidity           |  | 95%   | 95%                  | 95%   | 95%                    |
| Overcoating period, minimum         |  | 4 hours   | 24 hours             | 48 hours                                      | N/A                    |
| Overcoating period, maximum         |  | 7 days  | 7 days               | N/A   | N/A                    |
| Inspection required                 |  | Full  | Full                 | Random  | Random                 |
| Treatment of welds:                 |  | Blast clean Sa. 2.5 and full system.                  |                      |   |                        |
| Treatment of bolted connections:    |  | HSFG faying surfaces left bare. Edges sealed on site. |                      |   |                        |
| Treatment of damaged areas:         |  | Abrade smooth or local blast cleaning. Full system.   |                      |   |                        |
| Other comments:                     |  | Site finish colour – BS 4800, 12 B 15.                |                      |   |                        |

# Appendix

|  |      |
|--|------|
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**Elastic properties of steel**

|   |  |
|---|--|
| Modulus of elasticity (Young's modulus) | $E = 205 \text{ kN/mm}^2$                                |
| Poisson's ratio                         | $\nu = 0.30$   |
| Coefficient of linear thermal expansion | $\alpha = 12 \times 10^{-6} \text{ per } ^\circ\text{C}$ |

Selection of BS 4360: 1990 and BS EN 10025: 1990 Weldable structural steel plate

| Grade               | Chemical composition (ladle), (max.) |        |        |       |       |             |       | Supply condition | UTS (N/mm <sup>2</sup> ) (min.) | Min. yield strength <16 | Mechanical properties |       |            | Charpy (J) |
|---------------------|--------------------------------------|--------|--------|-------|-------|-------------|-------|------------------|---------------------------------|-------------------------|-----------------------|-------|------------|------------|
|                     | C (%)                                | Mn (%) | Si (%) | P (%) | S (%) | Nb (%)      | V (%) |                  |                                 |                         | 16-40                 | 40-63 | 63-100     |            |
| Fe430A              | 0.25                                 | 1.60   | 0.50   | 0.050 | 0.045 |             |       |                  | 275                             | 265                     | 255                   | 235   | —          |            |
| Fe430B <sup>b</sup> | 0.21                                 |        |        | 0.045 |       |             |       |                  | 275                             | 265                     | 255                   | 235   | 27@ + 20°C |            |
| Fe430C <sup>b</sup> | 0.18                                 |        |        | 0.040 |       |             |       |                  | 275                             | 265                     | 255                   | 235   | 27@ 0°C    |            |
| Fe430D1/D2          | 0.18                                 |        |        | 0.035 | 0.030 |             |       | Normalized       | 275                             | 265                     | 255                   | 235   | 27@ - 20°C |            |
| 43EE                | 0.16                                 | 1.50   | 0.50   | 0.040 | 0.030 |             |       |                  | 275                             | 265                     | 255                   | 245   | 27@ - 50°C |            |
| Fe510B <sup>b</sup> | 0.24                                 | 1.60   | 0.55   | 0.045 | 0.045 |             |       |                  | 355                             | 345                     | 335                   | 315   | 27@ + 20°C |            |
| Fe510C <sup>b</sup> | 0.22                                 | 1.60   | 0.55   | 0.040 | 0.040 |             |       |                  | 355                             | 345                     | 335                   | 315   | 27@ 0°C    |            |
| Fe510D1/D2          | 0.22                                 | 1.60   | 0.55   | 0.035 | 0.035 |             |       |                  | 355                             | 345                     | 335                   | 315   | 27@ - 20°C |            |
| Fe510DD1/DD2        | 0.22                                 | 1.60   | 0.55   | 0.035 | 0.035 |             |       |                  | 355                             | 345                     | 335                   | 315   | 27@ - 20°C |            |
| 50EE                | 0.18                                 | 1.50   | 0.50   | 0.040 | 0.030 | 0.003/0.10  |       | Normalized       | 390                             | 390                     | 340                   | 325   | 27@ - 50°C |            |
| 50F                 | 0.16                                 | 1.50   | 0.50   | 0.025 | 0.025 | 0.003/0.008 |       | QT               | 490                             | 430 <sup>c</sup>        | —                     | —     | 27@ - 60°C |            |
| 55C                 | 0.22                                 | 1.60   | 0.60   | 0.040 | 0.040 | 0.003/0.10  |       | Normalized       | 450                             | 430 <sup>c</sup>        | —                     | —     | 27@ 0°C    |            |
| 55EE                | 0.22                                 | 1.60   | 0.50   | 0.040 | 0.030 | 0.003/0.10  |       | Normalized       | 450                             | 430 <sup>c</sup>        | 400                   | —     | 27@ - 50°C |            |
| 55F                 | 0.16                                 | 1.50   | 0.50   | 0.025 | 0.025 | 0.003/0.008 |       | QT               | 450                             | 430 <sup>c</sup>        | —                     | —     | 27@ - 60°C |            |
| WR50B <sup>a</sup>  | 0.19                                 | 1.25   | 0.65   | 0.040 | 0.050 | 0.10        |       | As-rolled        | 345                             | 345                     | 340 <sup>d</sup>      | —     | 27@ 0°C    |            |
| WR50C <sup>a</sup>  | 0.22                                 | 1.45   | 0.65   | 0.040 | 0.050 | 0.10        |       | or normalized    | 345                             | 345                     | 340 <sup>d</sup>      | —     | 27@ - 15°C |            |

<sup>a</sup> Cr 0.50/0.65, Cu 0.25/0.40, weather resisting grades

<sup>b</sup> N 0.009

<sup>c</sup> limit 25 mm

<sup>d</sup> limit 50 mm

The figures in this table are indicative only, and apply to plate material. There are many detailed additional requirements and differences in BS 4360. The figures in the table should under no circumstances be used for specification purposes. For full details reference should be made to BS 4360: 1990 and BS EN 10025: 1990.

Selection of BS 970: Part 1: 1991 Austenitic stainless steels

| Grade  | Chemical composition (max.) |        |        |       |       |        |        |        |            |  | Others (%) | UTS (N/mm <sup>2</sup> ) | Mechanical properties                |         |     |
|--------|-----------------------------|--------|--------|-------|-------|--------|--------|--------|------------|--|------------|--------------------------|--------------------------------------|---------|-----|
|        | C (%)                       | Mn (%) | Si (%) | P (%) | S (%) | Cr (%) | Mo (%) | Ni (%) | Others (%) | 0.2% proof stress (N/mm <sup>2</sup> ) |            |                          | 1% proof stress (N/mm <sup>2</sup> ) | HB max. |     |
| 304S11 | 0.030                       | 2.0    | 1.0    | 0.045 | 0.030 | 19     |        | 12     |            |  |            | 480                      | 180                                  | 215     | 183 |
| 304S15 | 0.06                        | 2.0    | 1.0    | 0.045 | 0.030 | 19     |        | 11     |            |  |            | 480                      | 195                                  | 230     | 183 |
| 304S31 | 0.07                        | 2.0    | 1.0    | 0.045 | 0.030 | 19     |        | 11     |            |  |            | 490                      | 195                                  | 230     | 183 |
| 321S31 | 0.08                        | 2.0    | 1.0    | 0.045 | 0.030 | 19     |        | 12     | Ti 5C      |  |            | 510                      | 200                                  | 235     | 183 |
| 347S31 | 0.08                        | 2.0    | 1.0    | 0.045 | 0.030 | 19     |        | 12     | Nb 10C     |  |            | 510                      | 205                                  | 240     | 183 |
| 316S11 | 0.030                       | 2.0    | 1.0    | 0.045 | 0.030 | 18.5   | 2.5    | 14     |            |  |            | 490                      | 190                                  | 225     | 183 |
| 316S31 | 0.07                        | 2.0    | 1.0    | 0.045 | 0.030 | 18.5   | 2.5    | 13.5   |            |  |            | 510                      | 205                                  | 240     | 183 |
| 310S31 | 0.15                        | 2.0    | 1.5    | 0.045 | 0.030 | 26     |        | 22     |            |  |            | 510                      | 205                                  | 240     | 207 |
| 320S31 | 0.08                        | 2.0    | 1.0    | 0.045 | 0.030 | 18.5   | 2.5    | 14     | Ti 5C      |  |            | 510                      | 210                                  | 245     | 183 |
| 303S31 | 0.12                        | 2.0    | 1.0    | 0.06  | 0.35  | 19     | 1.0    | 10     |            |  |            | 510                      | 190                                  | 225     | 183 |
| 325S31 | 0.12                        | 2.0    | 1.0    | 0.045 | 0.35  | 19     |        | 11     | Ti 5C      |  |            | 510                      | 200                                  | 235     | 183 |

The figures in this table are indicative only and should under no circumstances be used for specification purposes. For full details reference should be made to BS 970: Part 1: 1991.

|            |  | CANTILEVERS   |  |
|------------|--|---|--|
| LOADING    |  |   |  |
| MOMENT     | $M_x = \frac{Wx^2}{2a}$ $M_{max.} = \frac{Wa}{2}$  | $M_{max} = W\left(a + \frac{b}{2}\right)$   |  |
| SHEAR      | $R_A = W$  | $R_A = W$   |  |
| DEFLECTION | $d_C = \frac{W a^3}{8EI}$ $d_{max.} = \frac{W a^3}{8EI} \left(1 + \frac{4b}{3a}\right)$  | $d_{max} = \frac{W(8a^3 + 18a^2b + 12ab^2 + 3b^3)}{24EI}$                                 |  |
| LOADING    |  |   |  |
| MOMENT     | $M_{max.} = W\left(a + \frac{b}{2}\right)$   | $M_x = \frac{Wx^3}{3a^2}$ $M_A = \frac{Wa}{3}$  |  |
| SHEAR      | $R_A = W$  | $R_A = W$   |  |
| DEFLECTION | $d_{max.} = \frac{W}{24EI} x$ $(8a^3 + 18a^2b + 12ab^2 + 3b^3 + 12a^2c + 12abc + 4b^2c)$ | $d_C = \frac{W a^3}{15EI}$ $d_{max.} = \frac{W a^3}{15EI} \left(1 + \frac{5b}{4a}\right)$ |  |

|            |   | CANTILEVERS  |  |
|------------|---|--|--|
| LOADING    |   |  |  |
| MOMENT     | $M_x = \frac{Wx}{3} \left[ \left( \frac{x}{a} \right)^3 - \frac{3x}{a} + 2 \right]$ $M_A = \frac{2Wx}{3}$ | $M_{max.} = W \left( a + \frac{2b}{3} \right)$   |  |
| SHEAR      | $R_A = W$   | $R_A = W$  |  |
| DEFLECTION | $d_C = \frac{11Wx^3}{60EI}$ $d_{max.} = \frac{11Wx^3}{60EI} \left( 1 + \frac{15b}{11a} \right)$           | $d_{max.} = \frac{W(20a^3 + 50a^2b + 40ab^2 + 11b^3)}{60EI}$                           |  |
| LOADING    |   |  |  |
| MOMENT     | $M_x = P \cdot x$ $M_{max.} = P \cdot a$  | $M_{max.} = M_x = M_C$   |  |
| SHEAR      | $R_A = P$   | <p style="text-align: center;">No shears</p>   |  |
| DEFLECTION | $d_C = \frac{Pa^3}{3EI}$ $d_{max.} = \frac{Pa^3}{3EI} \left( 1 + \frac{3b}{2a} \right)$                   | $d_C = \frac{Ma^2}{2EI}$ $d_{max.} = \frac{Ma^2}{2EI} \left( 1 + \frac{2b}{a} \right)$ |  |

N.B. For anti-clockwise moments the deflection is upwards.

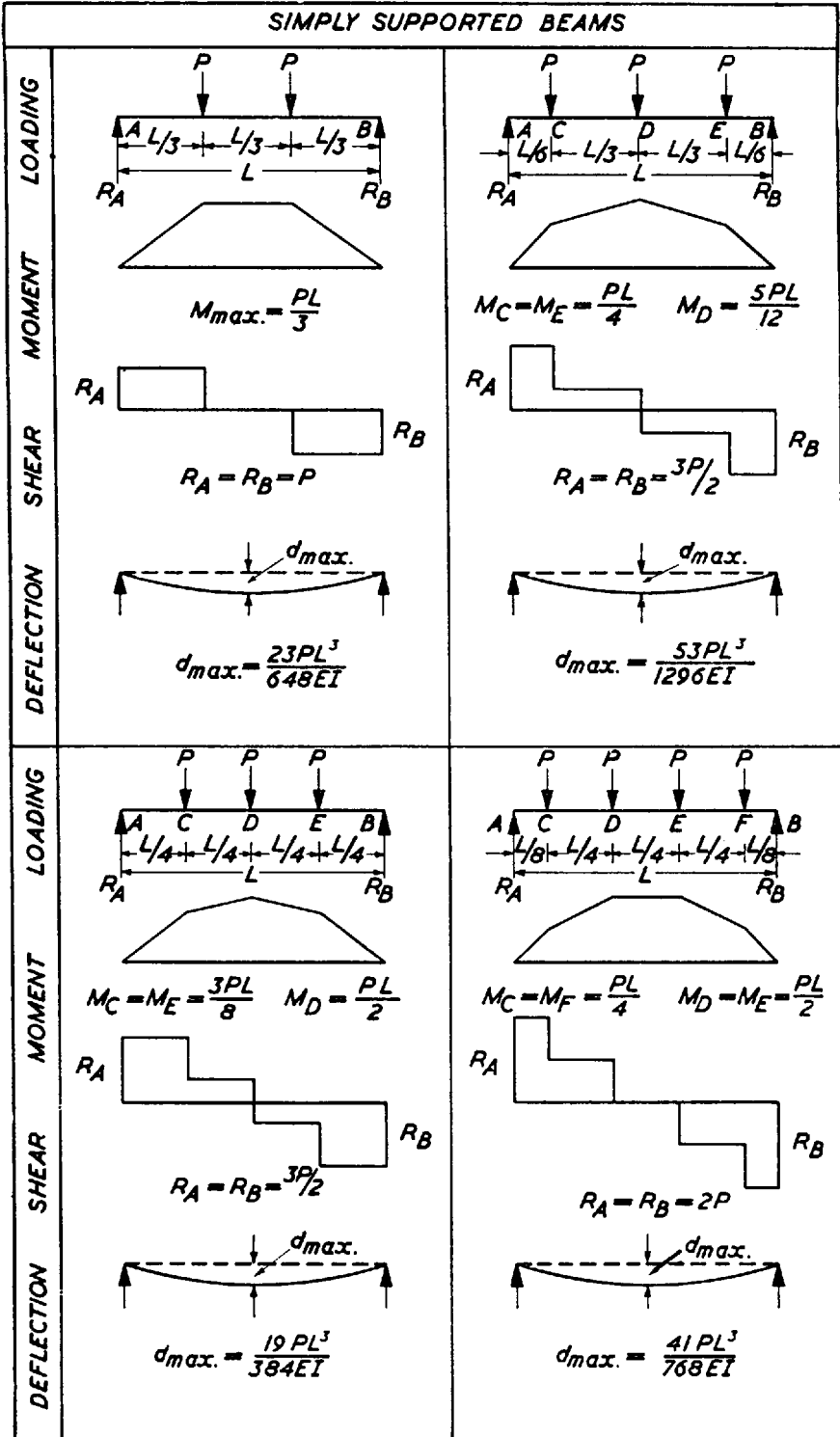
| SIMPLY SUPPORTED BEAMS |   |
|------------------------|---|
| LOADING                |   |
| MOMENT                 | $M_x = \frac{Wx}{2} \left(1 - \frac{x}{L}\right)$ $M_{max.} = \frac{WL}{8}$   |
| SHEAR                  | $R_A = R_B = \frac{W}{2}$   |
| DEFLECTION             | $d_{max.} = \frac{5}{384} \cdot \frac{WL^3}{EI}$  |
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{Wa}{4}$   |
| SHEAR                  | $R_A = R_B = \frac{W}{2}$   |
| DEFLECTION             | $d_{max.} = \frac{Wa(3L^2 - 2a^2)}{96EI}$   |
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{W}{b} \left( \frac{x_1^2 - a^2}{2} \right)$ <p>when <math>x_1 = a + \frac{Rab}{W}</math></p>  |
| SHEAR                  | $R_A = \frac{W(b+c)}{L}$ $R_B = \frac{W(b+a)}{L}$   |
| DEFLECTION             | <p>When <math>a = c</math></p> $d_{max.} = \frac{W}{384EI} (8L^3 - 4Lb^2 + b^3)$  |
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{W}{2} a \left(1 - \frac{a}{2L}\right)^2$ <p>when <math>x_1 = a \left(1 - \frac{a}{2L}\right)</math></p>   |
| SHEAR                  | $R_A = W \left(1 - \frac{a}{2L}\right)$ $R_B = \frac{Wa}{2L}$   |
| DEFLECTION             | <p>When <math>x &lt; a</math>,</p> $d = \frac{WL^3}{24aEI} [m^4 - 2n(2-n)m^2 + n^2(2-n)^2m]$ <p>When <math>x &gt; a</math>,</p> $d = \frac{WL^3}{24aEI} [m^3 - 6m^2 + m(4+n^2) - n^2]$ <p>where <math>m = x/L</math> and <math>n = a/L</math></p> |

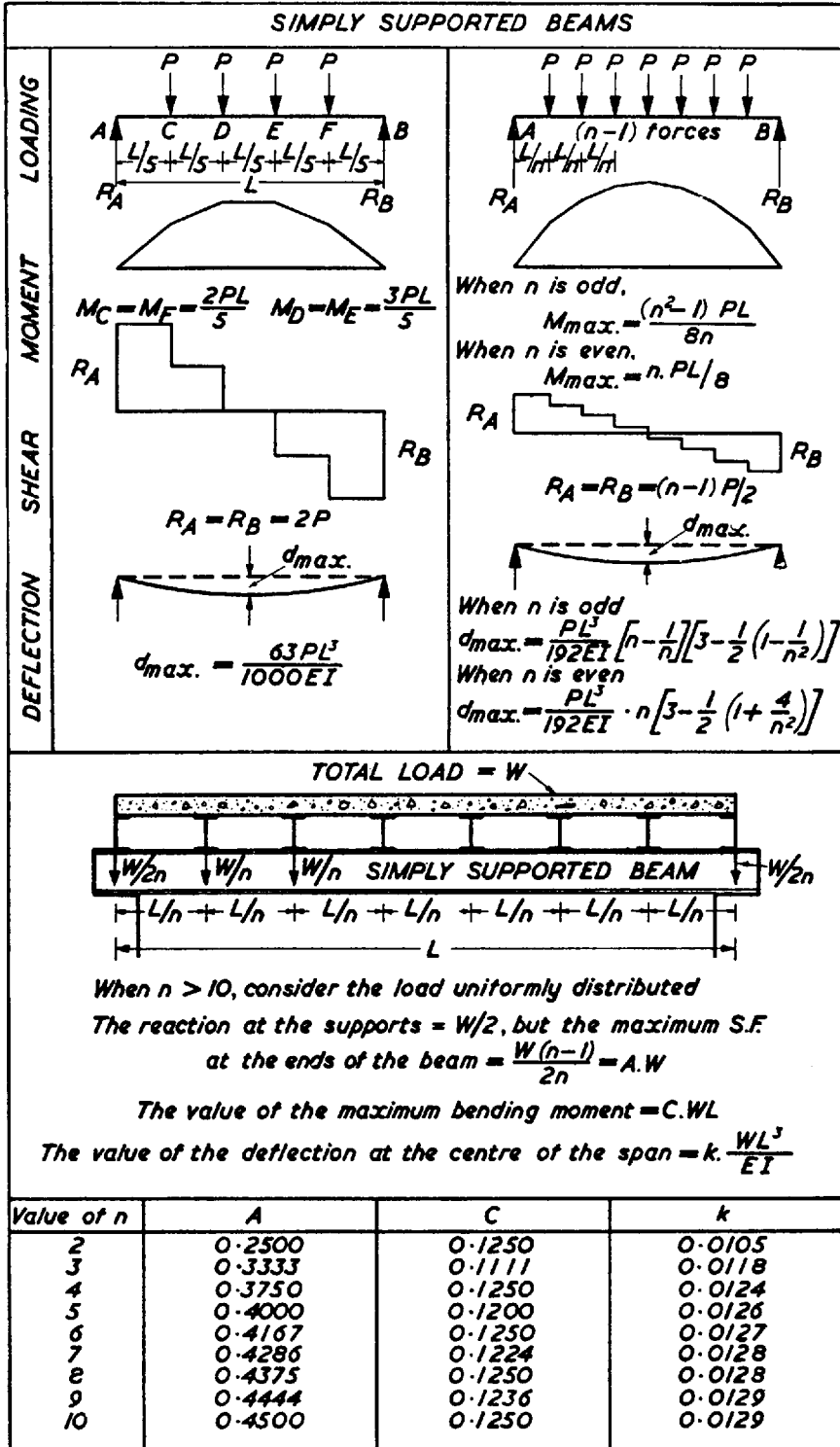


| SIMPLY SUPPORTED BEAMS |   |
|------------------------|---|
| LOADING                |   |
| MOMENT                 | $M_x = \frac{Wx}{3} \left( 1 - \frac{x^2}{L^2} \right)$ $M_{max.} = 0.128WL$ <p>when <math>x_1 = 0.5774L</math></p> |
| SHEAR                  | $R_A = W/3$ $R_B = 2W/3$  |
| DEFLECTION             | $d_{max.} = \frac{0.01304WL^3}{EI}$ <p>when <math>x = 0.5193L</math></p>  |
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{W}{4} \left( L - \frac{b}{3} \right)$   |
| SHEAR                  | $R_A = R_B = W/2$   |
| DEFLECTION             | $d_{max.} = \frac{W}{480EI} (8L^3 + 7aL^2 - 4a^2L - 4a^3)$  |
| LOADING                |   |
| MOMENT                 | $M_x = Wx \left( \frac{1}{2} - \frac{x}{L} + \frac{2x^2}{3L^2} \right)$ $M_{max.} = WL/12$                          |
| SHEAR                  | $R_A = R_B = \frac{W}{2}$   |
| DEFLECTION             | $d_{max.} = \frac{3WL^3}{320EI}$  |

|         |  | SIMPLY SUPPORTED BEAMS  |  |
|---------|--|---|--|
| LOADING |  |   |  |
|         |  |   |  |
|         |  |   |  |
|         |  |   |  |
| MOMENT  | $M_{max.} = \frac{W a}{6}$                                 | $M_{max.} = \frac{W a}{3} \left( 1 - m + \frac{2m}{3} \sqrt{\frac{m}{3}} \right)$<br>when $x = a \left( 1 - \sqrt{\frac{m}{3}} \right)$ |  |
|         | $R_A = R_B = W/2$  | $R_A = W \left( 1 - \frac{m}{3} \right)$<br>$R_B = \frac{W m}{3}$   |  |
|         | $d_{max.} = \frac{W a}{240 E I} (18 a^2 + 20 a b + 5 b^2)$ | —   |  |
|         |  |   |  |
| LOADING |  |   |  |
|         |  |   |  |
|         |  |   |  |
|         |  |   |  |
| MOMENT  | $M_{max.} = \frac{W a}{3}$                                 | $M_{max.} = \frac{2 W a}{3} \left( 1 - \frac{2m}{3} \right)^{3/2}$<br>when $x = a \sqrt{1 - \frac{2m}{3}}$                              |  |
|         | $R_A = R_B = W/2$  | $R_A = W \left( 1 - \frac{2m}{3} \right)$<br>$R_B = \frac{2 W m}{3}$  |  |
|         | $d_{max.} = \frac{W a}{120 E I} (16 a^2 + 20 a b + 5 b^2)$ | —   |  |
|         |  |   |  |

| SIMPLY SUPPORTED BEAMS |   |
|------------------------|---|
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{PL}{4}$   |
| SHEAR                  | $R_A = R_B = \frac{P}{2}$   |
| DEFLECTION             | $d_{max.} = \frac{PL^3}{48EI}$  |
| LOADING                |   |
| MOMENT                 | $M_{max.} = Pa$   |
| SHEAR                  | $R_A = R_B = P$   |
| DEFLECTION             | $d_{max.} = \frac{PL^3}{6EI} \left[ \frac{3a}{4L} - \left( \frac{a}{L} \right)^3 \right]$   |
| LOADING                |   |
| MOMENT                 | $M_{max.} = \frac{Pab}{L}$  |
| SHEAR                  | $R_A = \frac{Pb}{L} \quad R_B = \frac{Pa}{L}$   |
| DEFLECTION             | <p><i>d<sub>max</sub> always occurs within 0.0774 L of the centre of the beam. When <math>b \geq a</math>,</i></p> $d_{centre} = \frac{PL^3}{48EI} \left[ \frac{3a}{L} - 4 \left( \frac{a}{L} \right)^3 \right]$ <p><i>This value is always within 2.5% of the maximum value.</i></p> |
| LOADING                |   |
| MOMENT                 | $M_C = \frac{Pa(b+2c)}{L}$ $M_D = \frac{Pc(b+2a)}{L}$   |
| SHEAR                  | $R_A = \frac{P(b+2c)}{L}$ $R_B = \frac{P(b+2a)}{L}$   |
| DEFLECTION             | <p><i>For central deflection add the values for each P derived from the formula in the adjacent diagram.</i></p>  |



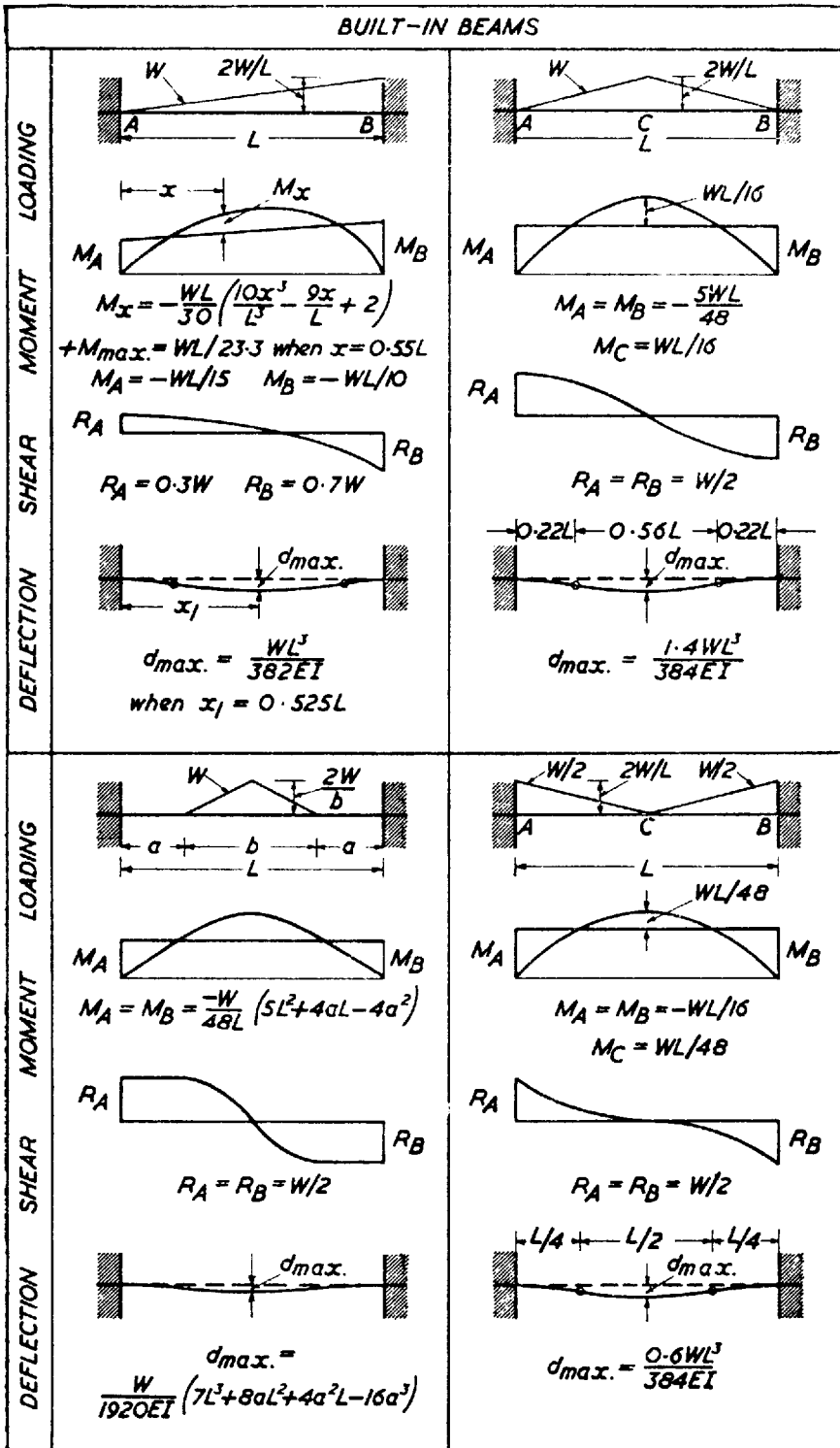


|            |            | SIMPLY SUPPORTED BEAMS  |   |
|------------|------------|---|---|
| LOADING    |            |   |   |
|            | MOMENT     | <p><math>M_{CA} = M \cdot a/L</math> <math>M_{CB} = M \cdot b/L</math></p>  | <p>① <math>M_A = M_B</math></p> <p>② <math>M_A &gt; M_B</math></p> <p>③ <math>M_A &gt; -M_B</math></p> <p>(<math>M_B</math> anti-clockwise)</p> <p>Shear diagram when <math>M_A \neq M_B</math></p> |
|            |            | SHEAR   | <p><math>R_A = R_B = M/L</math></p> <p>As shown <math>a &gt; b</math>.</p>  |
| DEFLECTION |            | <p><math>d_C = \frac{M \cdot ab}{3EI} \left( \frac{a}{L} - \frac{b}{L} \right)</math></p> <p>For anti-clockwise moments the deflections are reversed.</p> | <p>When <math>M_A = M_B</math>.</p> <p><math>d_{max.} = -\frac{ML^2}{8EI}</math></p>  |
|            | DEFLECTION |   |   |
| LOADING    |            | <p>2nd degree parabola. <math>W</math></p>  | <p>Complement of parabola. Total load = <math>W</math></p>  |
|            | MOMENT     | <p><math>M_x = \frac{WL}{2} (m^4 - 2m^3 + m)</math></p> <p><math>M_{max.} = \frac{5WL}{32}</math></p>   | <p><math>M_x = \frac{WL}{2} (m - 3m^2 + 4m^3 - 2m^4)</math></p> <p><math>M_{max.} = \frac{WL}{16}</math></p>  |
|            |            | SHEAR   | <p><math>R_A = R_B = W/2</math></p>   |
| DEFLECTION |            | <p><math>d_{max.} = \frac{6 \cdot 1WL^3}{384EI}</math></p>  | <p><math>d_{max.} = \frac{2 \cdot 8WL^3}{384EI}</math></p>  |
|            | DEFLECTION |   |   |

| SIMPLY SUPPORTED BEAMS |  |
|------------------------|--|
| LOADING                |  |
| MOMENT                 | $M_A = M_B = -\frac{wN^2}{2} \quad M_D = \frac{wL^2}{8} + M_A$   |
| SHEAR                  | $R_A = R_B = w\left(N + \frac{L}{2}\right)$  |
| DEFLECTION             | $d_C = d_E = \frac{wL^3 N}{24EI} (3n^3 + 6n^2 - 1)$ $d_D = \frac{wL^4}{384EI} (5 - 24n^2)$ <p style="text-align: center;">Where <math>n = N/L</math></p> |
| LOADING                |  |
| MOMENT                 | $M_A = -\frac{wN^2}{2}$  |
| SHEAR                  | $R_A = \frac{w(N+L)^2}{2L} \quad R_B = \frac{w(L+N)(L-N)}{2L}$   |
| DEFLECTION             | $d_C = \frac{wL^3 N}{24EI} (3n^3 + 4n^2 - 1)$ $d_x = \frac{wL^4}{24EI} [m^4 - 2m^3(1-n^2) + m(1-2n^2)]$ $d_D = -\frac{wL^3 Q}{24EI} (2n^2 - 1)$          |
| LOADING                |  |
| MOMENT                 | $M_A = -\frac{wN^2}{2}$  |
| SHEAR                  | $R_A = \frac{wN(2L+N)}{2L} \quad R_B = \frac{wN^2}{2L}$  |
| DEFLECTION             | $d_C = \frac{wLN^3}{24EI} \left(4 + 3\frac{N}{L}\right)$ $d_D = -\frac{0.032wL^2 N^2}{EI}$ $d_E = \frac{wLN^2 Q}{12EI}$                                  |

|   |   | BUILT-IN BEAMS  |  |
|---|---|---|--|
| LOADING   |   |   |  |
|   | MOMENT  |   |  |
|   |   | $M_A = M_B = -\frac{WL}{12}$ $M_C = \frac{WL}{24}$  | $M_A = M_B = -\frac{Wa}{12L}(3L-2a)$   |
|   | SHEAR   |   |  |
| $R_A = R_B = W/2$   |   | $R_A = R_B = W/2$   |  |
| DEFLECTION  |   |   |  |
|   | $d_{max.} = \frac{WL^3}{384EI}$   | $d_{max.} = \frac{Wa^2}{48EI}(L-a)$   |  |
| LOADING   |   |   |  |
|   | MOMENT  |   |  |
|   |   | $M_A = \frac{-W}{12L^2b} [e^3(4L-3e) - c^3(4L-3c)]$ $M_B = \frac{-W}{12L^2b} [d^3(4L-3d) - a^3(4L-3a)]$                 | $M_A = -\frac{WL}{12} \cdot m(3m^2 - 8m + 6)$ $M_B = -\frac{WL}{12} \cdot m^2(4 - 3m) + M_{max.} = \frac{WL}{12} m^2 \left( -\frac{3}{2}m^5 + 6m^4 - 6m^3 + 6m^2 + 15m - 8 \right)$ <p style="text-align: center;">When <math>x = \frac{9}{2}(m^3 - 2m^2 + 2)</math></p> |
|   | SHEAR   |   |  |
| <p>When <math>r</math> is the simple support reaction</p> $R_A = r_A + \frac{M_A - M_B}{L} \quad R_B = r_B + \frac{M_B - M_A}{L}$ |   | $R_A = \frac{W(m^3 - 2m^2 + 2)}{2} \quad R_B = \frac{W \cdot m^3(2 - m)}{2m}$   |  |
| DEFLECTION  |   |   |  |
|   | $\text{When } a=c, d_{max.} = \frac{W}{384EI} (L^3 + 2L^2a + 4La^2 - 8a^3)$ | <p>When <math>a=L/2</math> and <math>x_1 = 0.445L</math></p> $d_{max.} = \frac{WL^3}{333EI}$ $d_C = \frac{WL^3}{384EI}$ |  |



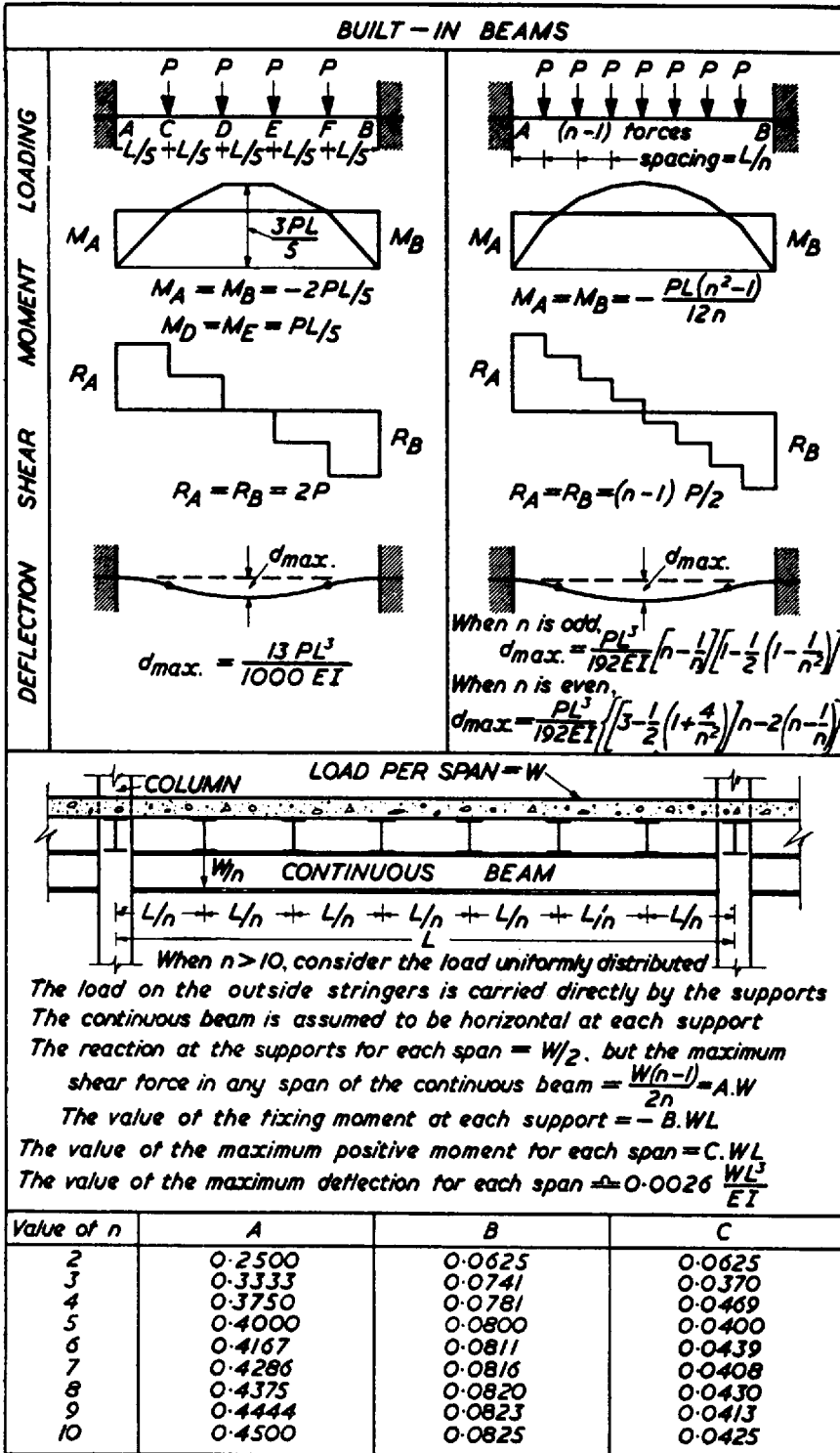


|                   |  | BUILT-IN BEAMS   |  |
|-------------------|--|--|--|
| LOADING           |  |  |  |
|                   | MOMENT                                   |  |  |
|                   |  | $M_A = M_B = -\frac{Wa}{12L}(2L-a)$  | $M_A = -\frac{Wa}{30L^2}(3a^2+10bL)$<br>$M_B = -\frac{Wa^2}{30L^2}(5L-3a)$<br>In AC, $M_x = R_B \cdot x + M_B - \frac{2W(x-b)^2}{6ab}$<br>In CB, $M_x = R_B \cdot x + M_B$ |
|                   | SHEAR                                    |  |  |
| $R_A = R_B = W/2$ |  | $R_A = \frac{W}{10L^3}(10L^3-5La^2+2a^3)$<br>$R_B = \frac{Wa^2}{10L^3}(5L-2a)$   |  |
| DEFLECTION        |  |  |  |
|                   | $d_{max.} = \frac{Wa^2}{480EI}(5L-4a)$   |  |  |
| LOADING           |  |  |  |
|                   | MOMENT                                   |  |  |
|                   |  | $M_A = M_B = -\frac{Wa}{12L}(4L-3a)$   | $M_A = -\frac{Wa}{15L^2}(10L^2-15aL+6a^2)$<br>$M_B = -\frac{Wa^2}{10L^2}(5L-4a)$   |
|                   | SHEAR                                    |  |  |
| $R_A = R_B = W/2$ |  | $R_A = \frac{W}{10L^2}(10L^3-15La^2+8a^3)$<br>$R_B = \frac{Wa^2}{10L^2}(15L-8a)$ |  |
| DEFLECTION        |  |  |  |
|                   | $d_{max.} = \frac{Wa^2}{480EI}(15L-16a)$ |  |  |

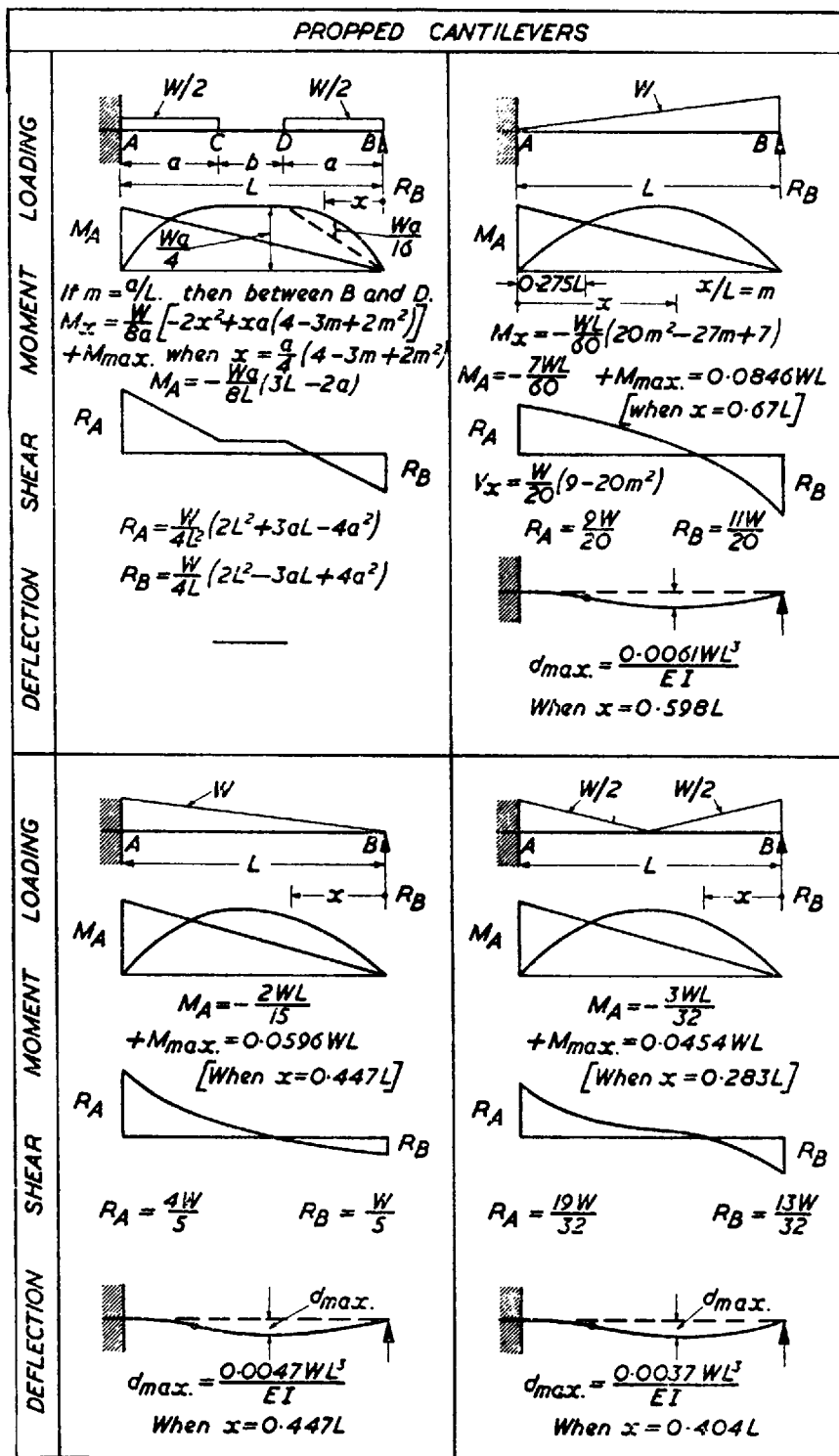
|                   |  | BUILT-IN BEAMS  |                      |
|-------------------|--|---|----------------------|
| LOADING           |  |   |                      |
|                   | MOMENT   |   |                      |
|                   |  | $M_A = M_B = -WL/10$  | $M_A = M_B = -WL/20$ |
|                   | SHEAR  |   |                      |
| $R_A = R_B = W/2$ |  | $R_A = R_B = W/2$   |                      |
| DEFLECTION        |  |   |                      |
|                   | $d_{max.} = \frac{1.3 WL^3}{384 EI}$   | $d_{max.} = \frac{0.4 WL^3}{384 EI}$  |                      |
| LOADING           |  |   |                      |
|                   | <p style="text-align: center;">symmetrical diagram</p>   |   |                      |
|                   | $M_A = M_B = -A_s/L$<br>where $A_s$ is the area of the 'free' bending moment diagram                           | $M_{AC} = M \cdot \frac{b}{L^2}(3a-L)$ $M_{BC} = -M \cdot \frac{a}{L^2}(3b-L)$<br>When $a/L = m$ , $M_{CA} = -M \cdot (1-m)(1-3m+6m^2)$ |                      |
|                   |  |   |                      |
| DEFLECTION        | $R_A = R_B = W/2$  | $R_A = R_B = \text{slope of moment diagram}$<br>$= \frac{M_{AC} + M_{CA}}{a} = \frac{M_{CB} + M_{BC}}{b}$                               |                      |
|                   |  |   |                      |
|                   | $d_{max. \text{ at } C} = \frac{A_s x - A_i x_i}{2EI}$<br>Where $A_i$ is the area of the fixing moment diagram | $d_C = \frac{M \cdot L^2 m^2 (1-m)^2 (1-2m)}{2EI}$<br>For anticlockwise moments reverse the deflections                                 |                      |

|                  |  | BUILT-IN BEAMS   |  |   |
|------------------|--|--|--|---|
| MOMENT · LOADING |  |  |  |   |
|                  |  | $-M_A = -M_B = M_C = PL/8$   | $M_A = -\frac{Pab^2}{L^2} \quad M_B = -\frac{Pba^2}{L^2}$ $M_C = \frac{2Pa^2b^2}{L^3}$ | $R_A = P\left(\frac{b}{L}\right)^2\left(1 + 2\frac{a}{L}\right)$ $R_B = P\left(\frac{a}{L}\right)^2\left(1 + 2\frac{b}{L}\right)$ |
|                  |  | $d_{max.} = \frac{PL^3}{192EI}$                                      |  | $d_C = \frac{Pa^3b^3}{3EIL^3}$ $d_{max.} = \frac{2Pa^2b^3}{3EI(3L-2a)^2} \text{ when } x = \frac{L^2}{3L-2a}$                     |
| SHEAR            |  | $R_A = R_B = P/2$  |  |   |
| DEFLECTION       |  | $d_{max.} = \frac{PL^3}{192EI}$                                      |  |   |
| MOMENT · LOADING |  |  |  |   |
|                  |  | $M_A = M_B = -\frac{Pa(L-a)}{L}$ $M_C = M_D = Pa^2/L$                | $M_A = M_B = -3PL/16$ $M_C = M_D = PL/16$  | $R_A = R_B = P$   |
|                  |  | $d_{max.} = \frac{PL^3}{6EI} \left[ \frac{3a^2(a)}{4L^2(L)} \right]$ |  | $d_{max.} = \frac{PL^3}{192EI}$   |
| SHEAR            |  | $R_A = R_B = P$  |  |   |
| DEFLECTION       |  | $d_{max.} = \frac{PL^3}{6EI} \left[ \frac{3a^2(a)}{4L^2(L)} \right]$ |  |   |

|            |                                  | BUILT-IN BEAMS                     |  |
|------------|----------------------------------|------------------------------------|--|
| LOADING    |                                  |                                    |  |
|            | MOMENT                           |                                    |  |
|            |                                  | SHEAR                              | $M_A = M_B = -2PL/9$<br>$M_C = M_D = PL/9$ |
| DEFLECTION |                                  |                                    |  |
|            |                                  | $R_A = R_B = P$                    | $R_A = R_B = 3P/2$                         |
|            |                                  |                                    |  |
|            | $d_{max.} = \frac{5PL^3}{648EI}$ | $d_{max.} = \frac{41PL^3}{5184EI}$ |  |
| LOADING    |                                  |                                    |  |
|            | MOMENT                           |                                    |  |
|            |                                  | SHEAR                              | $M_A = M_B = -5SPL/16$<br>$M_D = 3PL/16$   |
| DEFLECTION |                                  |                                    |  |
|            |                                  | $R_A = R_B = 3P/2$                 | $R_A = R_B = 2P$                           |
|            |                                  |                                    |  |
|            | $d_{max.} = \frac{PL^3}{96EI}$   | $d_{max.} = \frac{PL^3}{96EI}$     |  |



|                  |  | PROPPED CANTILEVERS   |  |
|------------------|--|---|--|
| MOMENT · LOADING |  |   |  |
|                  | $M_A = -\frac{WL}{8} \quad M_C = \frac{9WL}{128}$ $R_A = \frac{5W}{8} \quad R_B = \frac{3W}{8}$  | $M_A = -\frac{Wa}{8}(2-n)^2 \text{ where } a/L=n$ $+M_{max} = \frac{Wa}{8} \left[ \frac{(8-n^2(4-n))^2}{16} + 4-n(4-n) \right]$ $R_A = \frac{W}{8} [8-n^2(4-n)]$ $R_B = \frac{Wn^2}{8} (4-n)$ |  |
|                  | $d = \frac{WL^3}{48EI} (m - 3m^3 + 2m^4)$ $d_{max} = \frac{WL^3}{185EI}$   | $d_C = \frac{Wg^3}{48EI} (6 - 12n + 7n^2 - n^3)$  |  |
| SHEAR            |  |   |  |
|                  | $M_A = -\frac{Wb}{8} \frac{(2-n^2)}{(6-n^2)} \quad M_C = \frac{Wb}{8} (6n - n^3 - 4)$ $R_A = \frac{Wn}{8} (6 - n^2)$ $R_B = \frac{W}{8} (n^3 - 6n + 8)$  | $M_A = -\frac{W}{8L^2b} (d^2 - c^2) (2L^2 - c^2 - d^2)$ $R_A = r_A + \frac{MA}{L} \quad R_B = r_B - \frac{MA}{L}$   |  |
|                  | <p>When <math>x \leq a</math>, <math>d = \frac{WbL^2}{48EI} [(n^2 - 6)m^3 - (3n^2 - 6)m^2]</math></p> <p>When <math>x \geq a</math>, <math>d = \frac{WL^4}{48bEI} [2p^2 - p^3n(n^3 - 6n + 8) + pn^2(3n^2 - 8n + 6)]</math></p> | <p>Where <math>r_A</math> and <math>r_B</math> are the simple support reactions for the beam (<math>M_A</math> being considered positive)</p>   |  |
| DEFLECTION       |  |   |  |
|                  | $d = \frac{WL^3}{48EI} (m - 3m^3 + 2m^4)$ $d_{max} = \frac{WL^3}{185EI}$   | $d_C = \frac{Wg^3}{48EI} (6 - 12n + 7n^2 - n^3)$  |  |
|                  | <p>When <math>x \leq a</math>, <math>d = \frac{WbL^2}{48EI} [(n^2 - 6)m^3 - (3n^2 - 6)m^2]</math></p> <p>When <math>x \geq a</math>, <math>d = \frac{WL^4}{48bEI} [2p^2 - p^3n(n^3 - 6n + 8) + pn^2(3n^2 - 8n + 6)]</math></p> | <p>Where <math>r_A</math> and <math>r_B</math> are the simple support reactions for the beam (<math>M_A</math> being considered positive)</p>   |  |



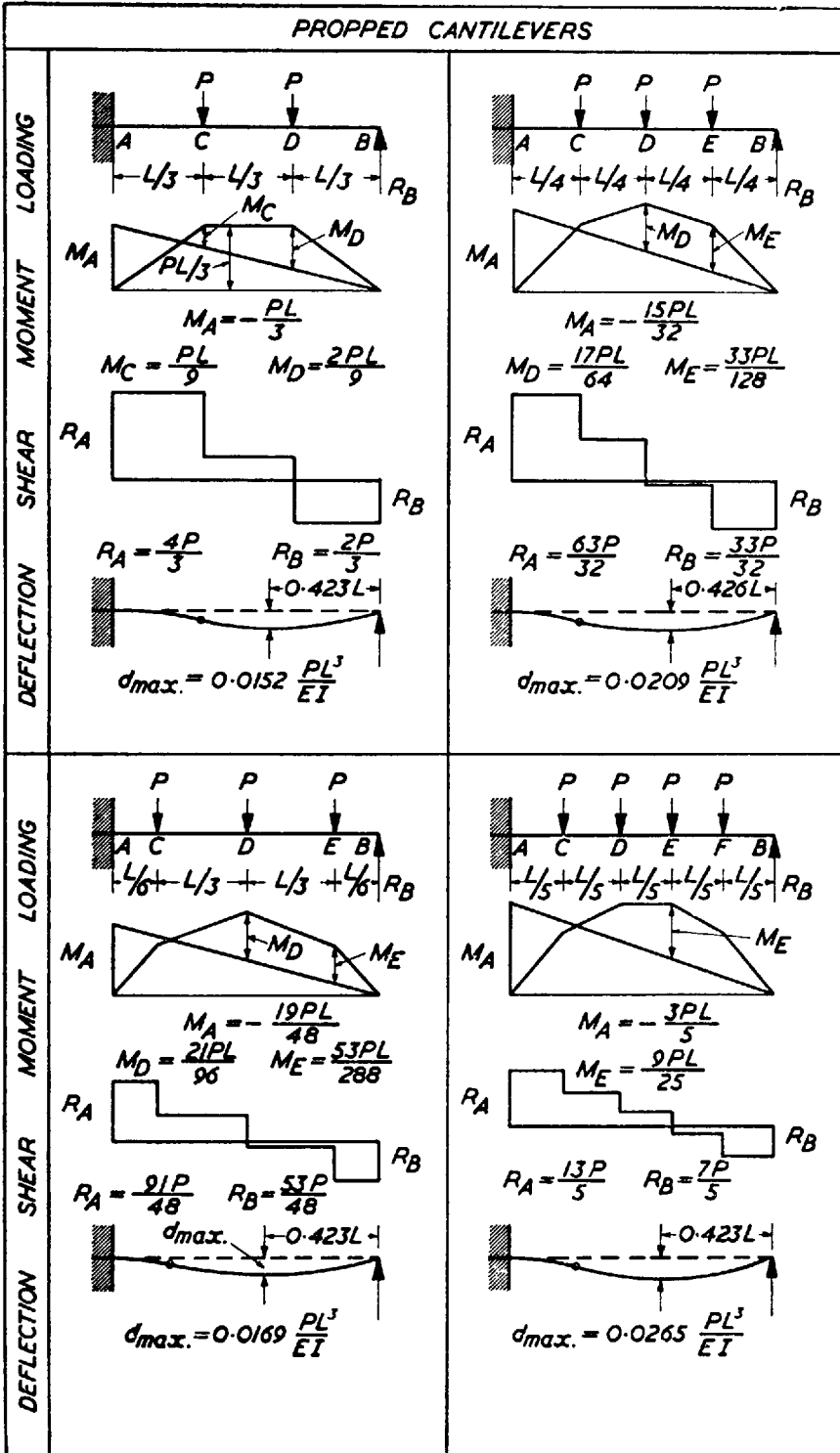


|         |  | PROPPED CANTILEVERS  |  |
|---------|--|--|--|
| LOADING |  |  |  |
|         |  |  |  |
| MOMENT  | Between C and A, $M_x = R_B \cdot x - \frac{W}{3a^2}(x-b)^3$<br>$M_A = -\frac{Wa}{60L^2}(3a^2 - 15aL + 20L^2)$<br>$+ M_{max.} \text{ when } x = b + \frac{a^2}{2L}\sqrt{1 - \frac{a}{5L}}$ | $M_x = R_B \cdot x - \frac{Wx^3}{3b^2}$<br>$M_A = -\frac{Wb}{15L^2}(5L^2 - 3b^2)$            |  |
|         |  |  |  |
| SHEAR   | $R_B = \frac{Wa^2}{20L^2}(5L - a)$<br>$R_A = W - R_B$  | $R_A = \frac{Wb}{5L^3}(5L^2 - b^2)$<br>$R_B = \frac{W}{5L^3}(b^3 + 5aL^2)$                   |  |
|         |  |  |  |
| LOADING |  |  |  |
|         | When $m = a/L$<br>$M_A = -Wa\left(\frac{m^2}{5} - \frac{3m}{4} + \frac{2}{3}\right)$<br>$M_C = R_B \cdot b$  | $M_x = R_A \cdot x + M_A - \frac{W}{3b^2}(x-a)^3$<br>$M_A = -\frac{Wb}{60L^2}(10L^2 - 3b^2)$ |  |
| MOMENT  | Between A and C<br>$V_x = R_A - Wx^2/a^2$  | Between C and B<br>$V_x = R_A - Wx^2/b^2$  |  |
|         |  |  |  |
| SHEAR   | $R_B = \frac{Wa^2}{20L^2}(15L - 4a)$<br>$R_A = W - R_B$  | $R_B = \frac{W}{20b^2L^2}[L^4(11L - 15a) + a^4(5L - a)]$<br>$R_A = W - R_B$                  |  |

|            |        | PROPPED CANTILEVERS  |   |
|------------|--------|--|---|
| LOADING    |        |  |   |
|            | MOMENT |  |   |
|            | SHEAR  |  |   |
| DEFLECTION |        |  |   |
|            |        | $W = w(L+a)$ $M_B = -\frac{w a^2}{2} \quad M_A = -\frac{w}{8}(L^2 - 2a^2)$ $+M_{max.} = \frac{w L^2}{128}(36p^4 - 28p^2 + 9)$ <p style="text-align: center;">when <math>x/L = \frac{5}{8} - \frac{3p^2}{4}</math></p> $R_A = wL \left( \frac{5}{8} - \frac{3p^2}{4} \right)$ $R_B = wL \left( \frac{3p^2}{4} + p + \frac{3}{8} \right)$ $d_D = \frac{w L^4}{48EI} \left[ (8p^2 + 6p^2 - 1)(p+q) - 2p^2 \right]$ $d_x = \frac{w L^4}{48EI} \left[ 2n^4 + (6p^2 - 5)n^2 - (6p^2 - 3)n^2 \right]$ <p style="text-align: center;"><math>d_{max.}</math> when <math>x/L = \frac{1}{18} \left[ 15 - 18p^2 \pm \sqrt{324p^4 - 156p^2 + 33} \right]</math></p> | $W = w.q$ $M_B = -2M_A = -\frac{w a^2}{2}$ $p = a/L$ $q = b/L$ $R_A = -\frac{3w a p}{4}$ $R_B = w a \left( 1 + \frac{3p}{4} \right)$ $d_D = \frac{w L^4}{48EI} \left[ p^2(8p+6)q + 6p^3(p+1) \right]$ $-d_{max.} = -\frac{w L^4 p^2}{54EI}$ |
| LOADING    |        |  |   |
|            | MOMENT |  |   |
|            | SHEAR  |  |   |
| DEFLECTION |        |  |   |
|            |        | $P$ $M_B = -2M_A = -Pa$ $p = a/L$ $q = b/L$ $R_A = -\frac{3Pp}{2}$ $R_B = P \left( 1 + \frac{3p}{2} \right)$ $d_D = \frac{P L^3 p}{12EI} (4p^2 + 6pq + 3p + 3q)$ $-d_{max.} = -\frac{P L^3 p}{27EI}$   | $M$ $M_B = -2M_A = -M$ $R_A = -R_B = -\frac{3M}{2L}$ $d_D = \frac{M}{4EI} \left[ L(a+b) + a^2 \left( 2 + \frac{4b}{a} \right) \right]$ $-d_{max.} = -\frac{M L^2}{27EI}$  |

|            |   | PROPPED CANTILEVERS   |  |
|------------|---|---|--|
| LOADING    |   |   |  |
|            |   |   |  |
| MOMENT     | $M_A = -\frac{Wa}{8L}(2L-a)$                                | $M_A = -\frac{Wa}{8L}(4L-3a)$   |  |
|            |   | When $x < a$ ,<br>$M_x = \frac{W}{24}(9n^2x - 12nx + 12x - 4xq^2)$<br>+ $M_{max}$ occurs when $q = \sqrt{\frac{3n^2}{4}} - n + 1$ |  |
| SHEAR      |   |   |  |
|            | $R_A = \frac{W}{8L^2}(4L^2 + 2aL - a^2)$<br>$R_B = W - R_A$ | $R_A = \frac{W}{8L^2}(4L^2 + 4aL - 3a^2)$<br>$R_B = W - R_A$  |  |
| LOADING    |   |   |  |
|            |   |   |  |
| MOMENT     | $M_A = -\frac{5WL}{32}$<br>+ $M_{max} = 0.0948WL$           | $M_A = \frac{W}{32L}(5L^2 + 4aL - 4a^2)$  |  |
|            |   |   |  |
| SHEAR      | $R_A = \frac{21W}{32} \quad R_B = \frac{11W}{32}$           | $R_A = \frac{W}{32L^2}(21L^2 + 4aL - 4a^2)$<br>$R_B = W - R_A$  |  |
|            |   |   |  |
| DEFLECTION | $d_{max} = 0.00727 \frac{WL^3}{EI}$                         |   |  |

|         |                     | PROPPED CANTILEVERS  |  |
|---------|---------------------|--|--|
| LOADING | 2nd degree parabola |  | complement of parabola<br>total load W   |
|         | MOMENT              |  |  |
| SHEAR   |                     | $M_A = -\frac{3WL}{20}$<br>$M_x = \frac{WL}{20} (10m^4 - 20m^3 + 7m)$<br>$+M_{max.} = 0.0888WL, \text{ when } x = 0.3985L$ | $M_A = -\frac{3WL}{40}$<br>$M_x = \frac{WL}{40} (-40m^4 + 80m^3 - 60m^2 + 17m)$<br>$+M_{max.} = 0.0399WL, \text{ when } x = 0.2343L$                                     |
|         | DEFLECTION          |  |  |
| LOADING |                     | $R_A = \frac{13W}{20}$ $R_B = \frac{7W}{20}$<br>$d_{max.} = 0.427L$  | $R_A = \frac{23W}{40}$ $R_B = \frac{17W}{40}$<br>$d_{max.} = 0.392L$   |
|         |                     | $d_{max.} = 0.00674 \frac{WL^3}{EI}$   | $d_{max.} = 0.00278 \frac{WL^3}{EI}$   |
| LOADING |                     |  |  |
|         | MOMENT              |  |  |
| SHEAR   |                     | $M_A = -\frac{3PL}{16}$<br>$M_C = \frac{5PL}{32}$  | $M_A = -\frac{Pb(L^2 - b^2)}{2L^2}$ $\text{max. } M_A = -0.193PL$<br>$M_C = \frac{Pb}{2} \left( 2 - \frac{3b}{L} + \frac{b^3}{L^3} \right)$ $\text{max. } M_C = 0.174PL$ |
|         | DEFLECTION          | $R_A = 11P/16$ $R_B = 5P/16$   | $R_A = \frac{Pa^2}{2L^3}(b+2L)$ $R_B = P - R_A$  |
|         |                     | $d_C = \frac{7PL^3}{768EI}$<br>$d_{max.} = 0.00932 \frac{PL^3}{EI}$  | $d_C = \frac{Pa^3b^2}{12EI L^3}(4L-a)$   |

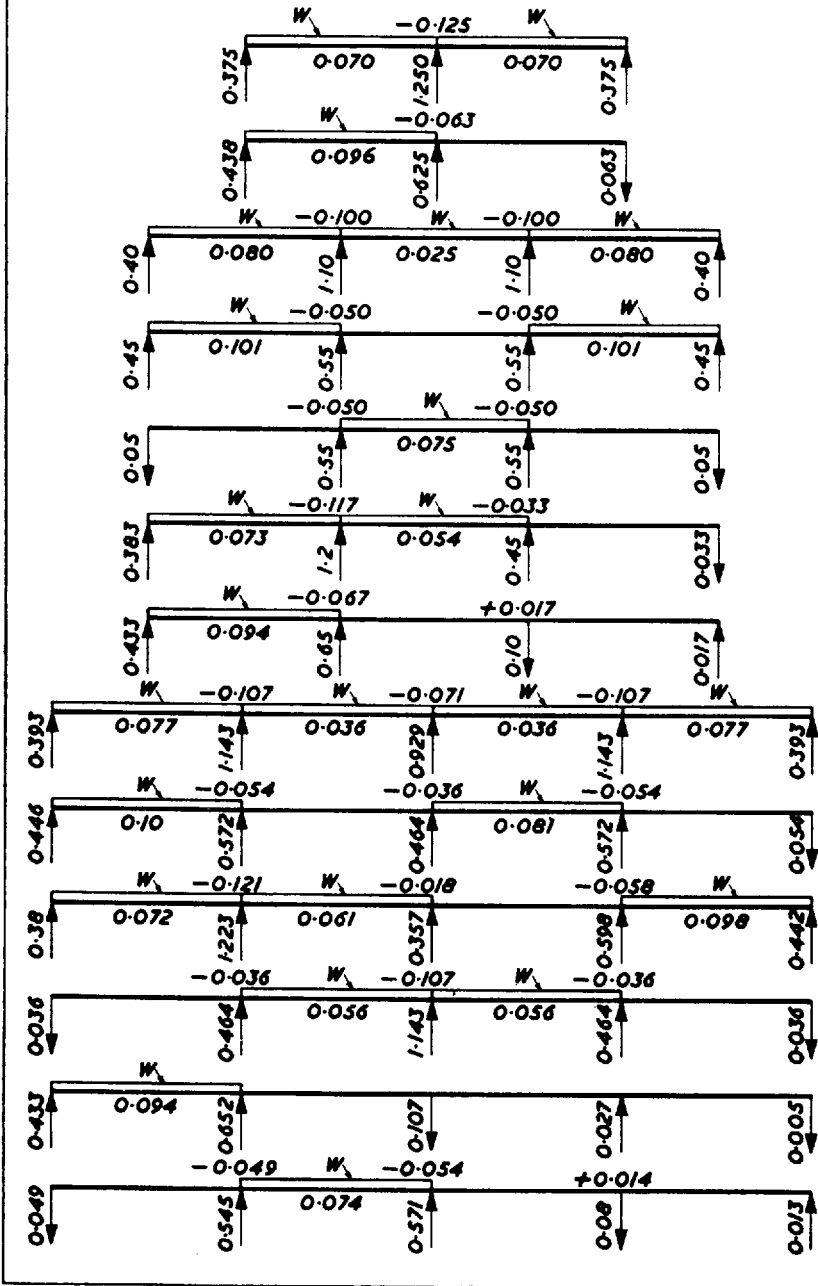


|            |  | PROPPED CANTILEVERS  |   |
|------------|--|--|---|
| LOADING    | MOMENT   |  |   |
|            |  | $M_A = -\frac{33PL}{64}$ $M_E = \frac{157PL}{512}$   | $M_A = -\frac{PL(n^2-1)}{8n}$                                   |
|            |  |  |   |
|            |  | $R_A = \frac{161P}{64}$ $R_B = \frac{95P}{64}$   | $R_A = \frac{P}{8n}(5n^2-4n-1)$ $R_B = \frac{P}{8n}(3n^2-4n+1)$ |
| DEFLECTION |  |  |   |
|            | $d_{max} = 0.0221 \frac{PL^3}{EI}$   | when n is large, $d_{max} \approx \frac{nPL^3}{185EI}$   |   |
| LOADING    | MOMENT   | Any symmetrical load W<br>   |   |
|            |  | $M_A = \frac{3AS}{2L}$   | ① $a=L$<br>$M_A = -M/2$   |
|            |  | $R_A = \frac{W}{2} + \frac{M_A}{L}$ $R_B = \frac{W}{2} - \frac{M_A}{L}$                                  | ② $a > 0.423L$<br>$M_{CB} = +$                                  |
|            |  |  | ③ $a = 0.423L$<br>$M_{CA} = +$                                  |
| DEFLECTION | $d_{max} = \frac{\text{Area } SXx}{EI}$ <p><i>dmax. occurs at point corresponding to X on B.M. diagram, the area R being equal to the area Q</i></p> | ④ $a < 0.423L$<br>$M_{CA} = +$   |   |
|            |  | $M_A = \frac{M}{2}(2-6n+3n^2)$ $M_{CA} = \frac{M}{2}(2-6n+9n^2-3n^3)$ $M_{CB} = \frac{3Mn}{2}(2-3n+n^2)$ |   |
|            |  | $R_A \uparrow$   |   |
|            |  | $-R_A = R_B = \frac{M+M_A}{L}$ <p>In Case 1, <math>R = 3M/2L</math><br/>Case 3, <math>R = M/L</math></p> |   |

**EQUAL SPAN CONTINUOUS BEAMS  
UNIFORMLY DISTRIBUTED LOADS**

Moment = coefficient x W x L  
Reaction = coefficient x W

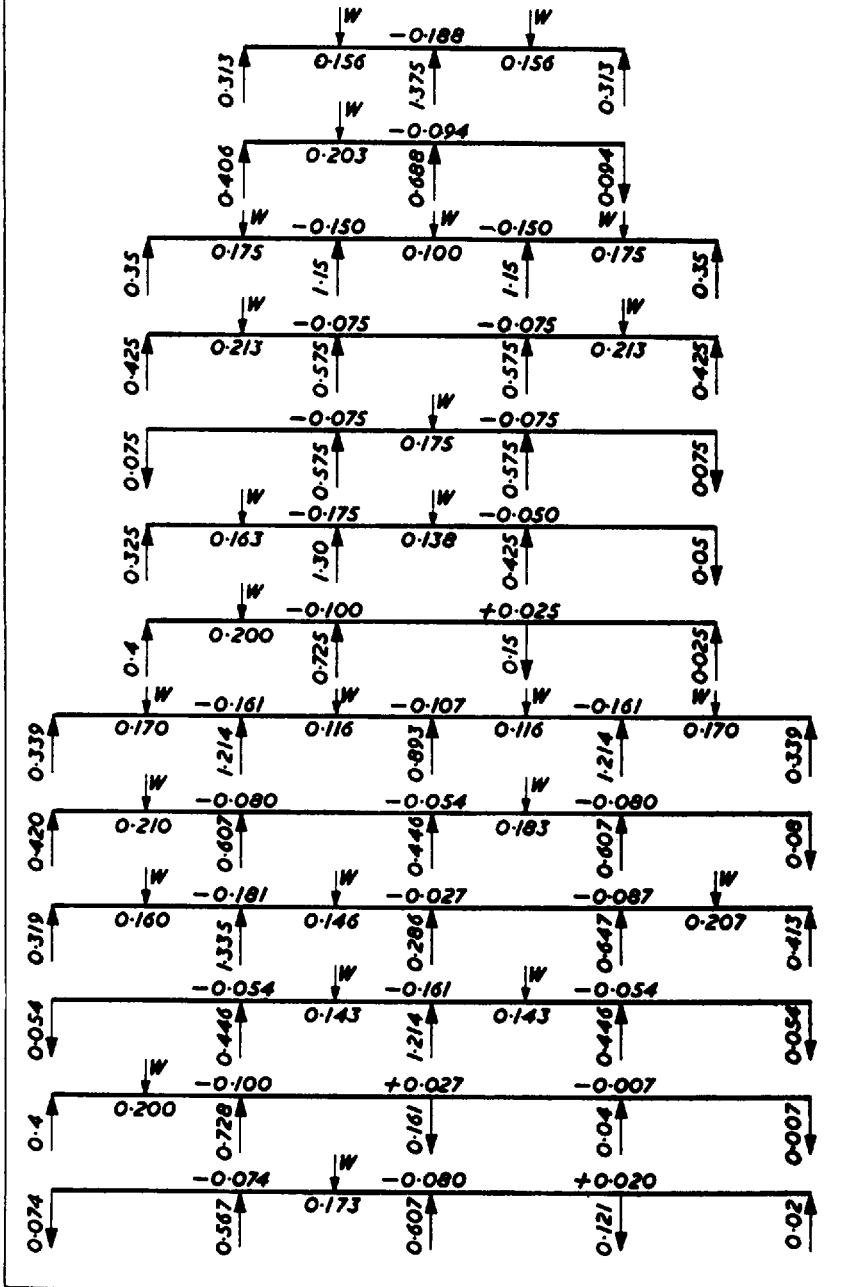
where W is the U.D.L. on one span only and L is one span



**EQUAL SPAN CONTINUOUS BEAMS  
CENTRAL POINT LOADS**

Moment = coefficient  $\times W \times L$   
Reaction = coefficient  $\times W$

where  $W$  is the Load on one span only and  $L$  is one span



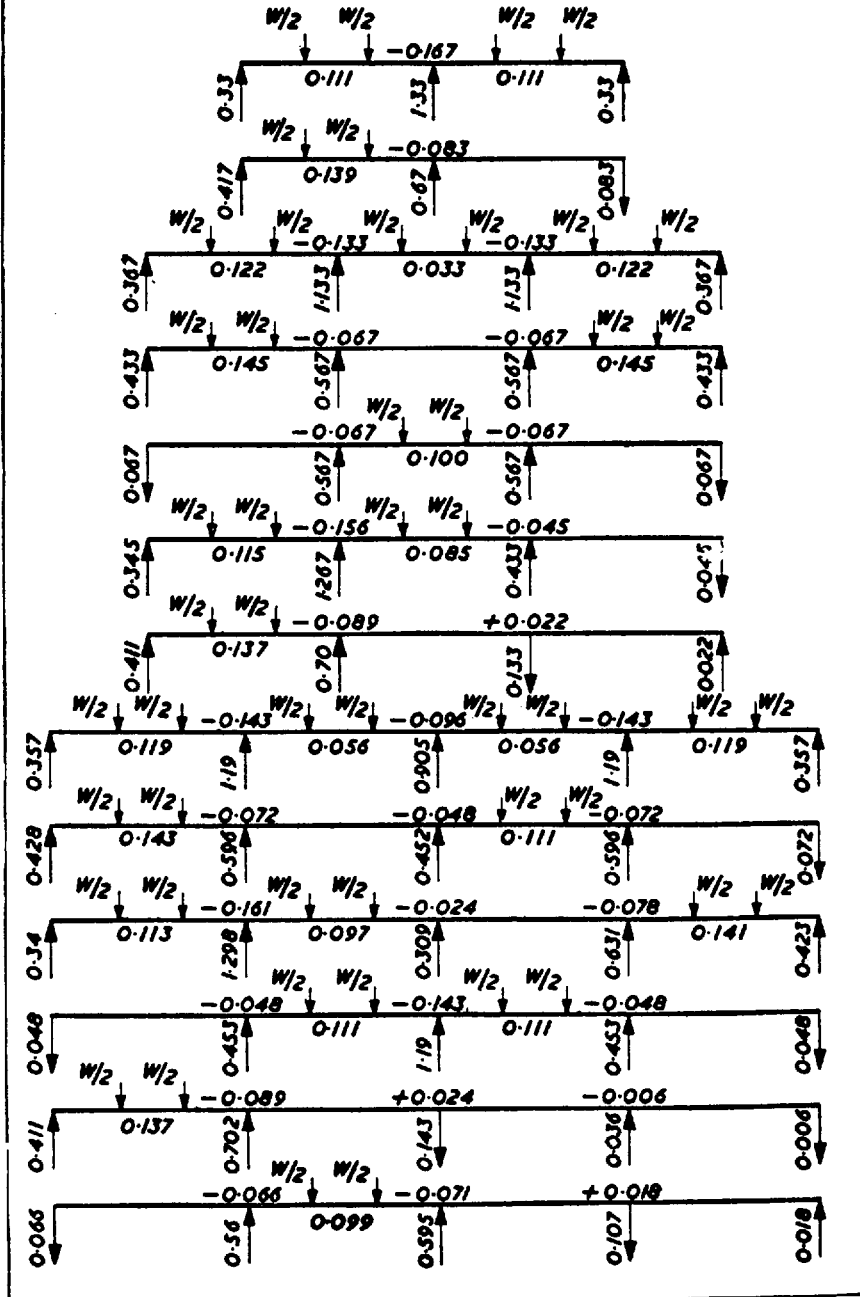


**EQUAL SPAN CONTINUOUS BEAMS  
POINT LOADS AT THIRD POINTS OF SPANS**

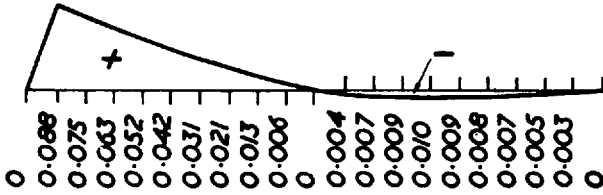
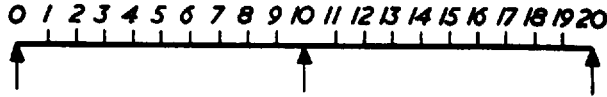
Moment = coefficient  $\times W \times L$

Reaction = coefficient  $\times W$

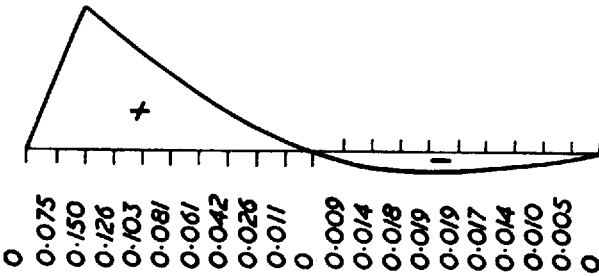
where  $W$  is the total load on one span only &  $L$  is one span



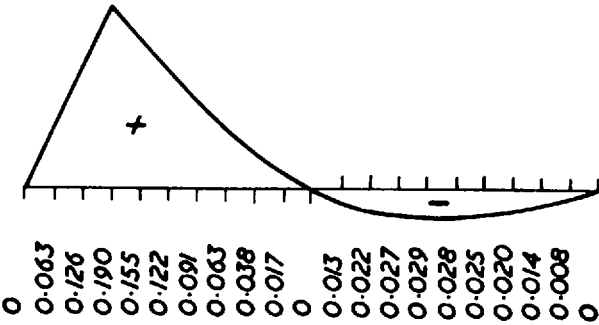
**Influence lines for bending moments – two-span beam**



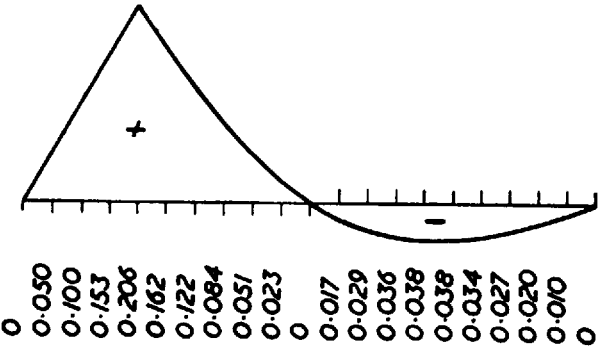
*Influence line for point 1*



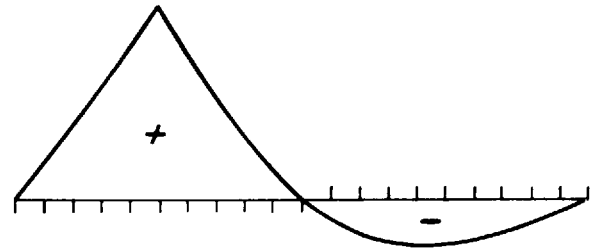
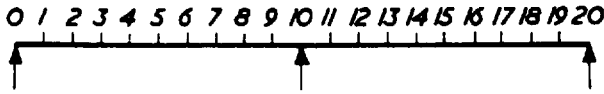
*Influence line for point 2*



*Influence line for point 3*

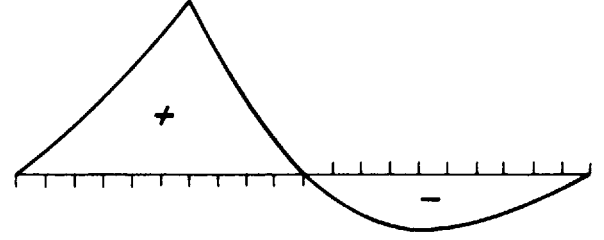


*Influence line for point 4*



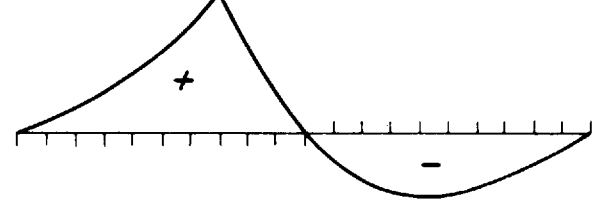
*Influence line for point 5*

0 0.038  
0.076  
0.116  
0.158  
0.203  
0.152  
0.105  
0.064  
0.028  
0 0.021  
0.036  
0.045  
0.048  
0.047  
0.042  
0.034  
0.024  
0.012  
0



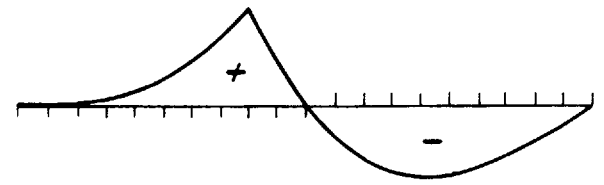
*Influence line for point 6*

0 0.025  
0.051  
0.079  
0.110  
0.144  
0.182  
0.127  
0.077  
0.034  
0 0.026  
0.043  
0.053  
0.058  
0.056  
0.050  
0.041  
0.029  
0.015  
0



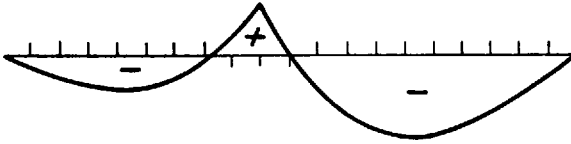
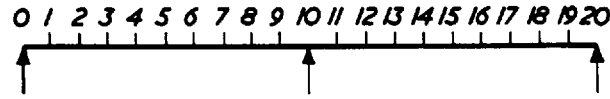
*Influence line for point 7*

0 0.013  
0.026  
0.042  
0.061  
0.084  
0.113  
0.148  
0.090  
0.040  
0 0.030  
0.050  
0.062  
0.067  
0.066  
0.059  
0.048  
0.034  
0.018  
0

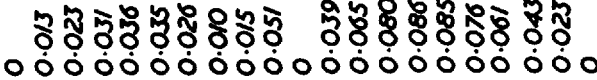


*Influence line for point 8*

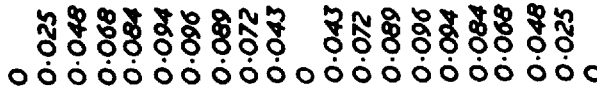
0 0.002  
0.006  
0.013  
0.025  
0.043  
0.069  
0.102  
0.046  
0 0.034  
0.058  
0.071  
0.077  
0.075  
0.067  
0.054  
0.038  
0.020  
0



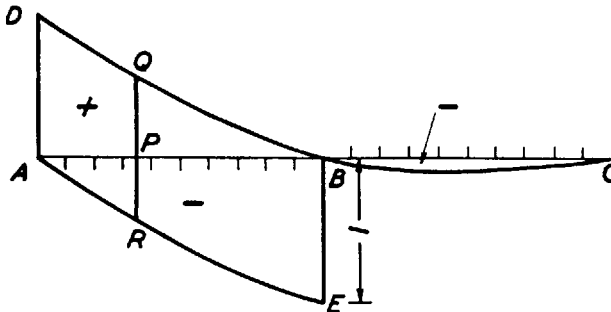
*Influence line for point 9*



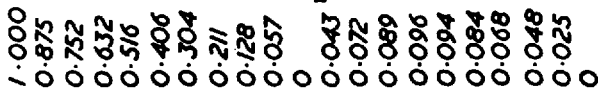
*Influence line for point 10*



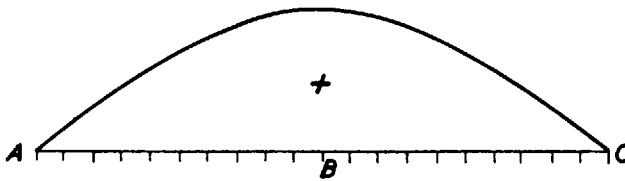
**Influence lines for reactions and shear forces – two-span beam**



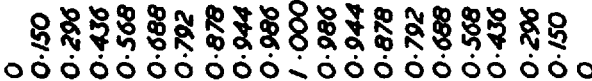
*Influence line for Reaction at A and S.F. envelope for span AB*



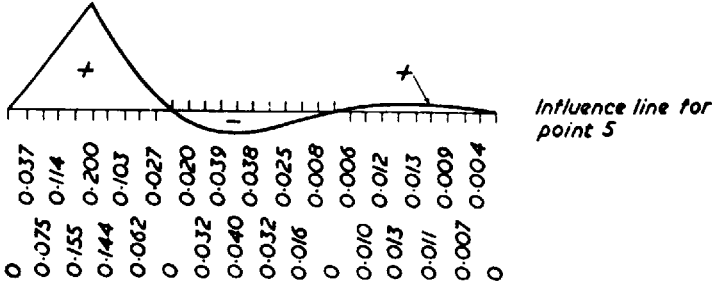
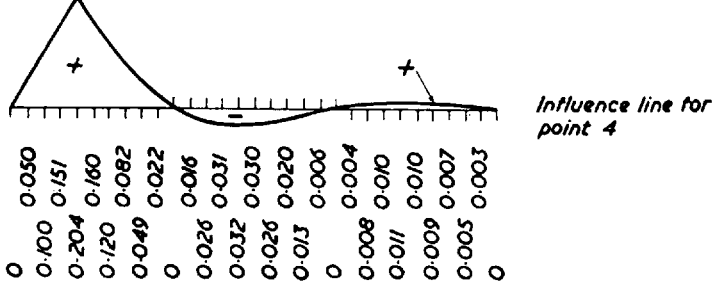
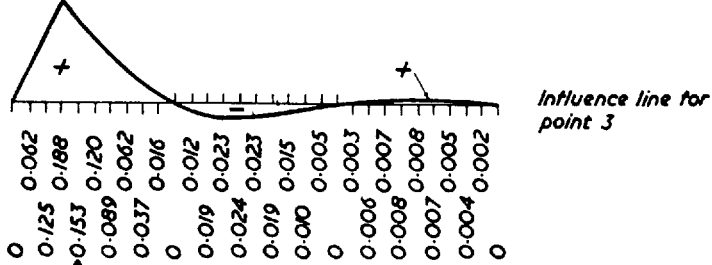
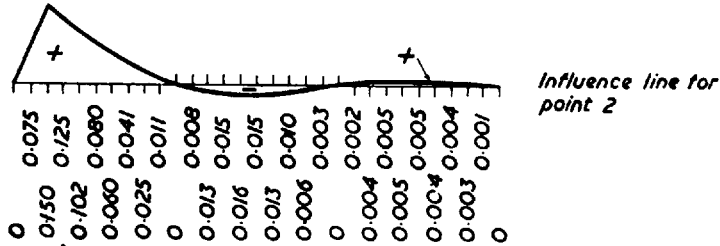
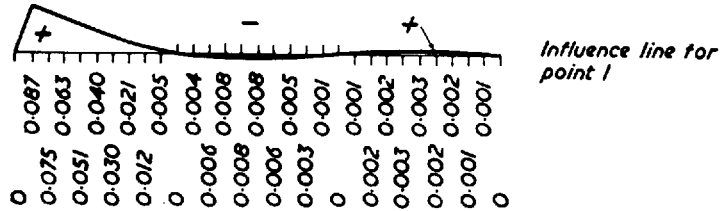
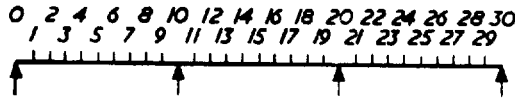
*Ordinates of line DBC*



*Influence line for Reaction at B*

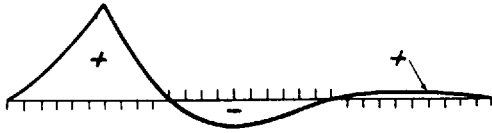
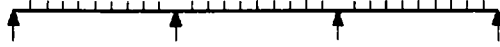


Influence lines for bending moments – three-span beam

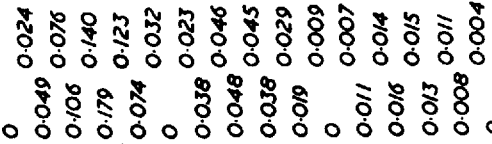


**Influence lines for bending moments – three-span beam**

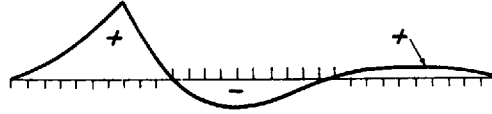
0 2 4 6 8 10 12 14 16 18 20 22 24 26 28 30  
 1 3 5 7 9 11 13 15 17 19 21 23 25 27 29



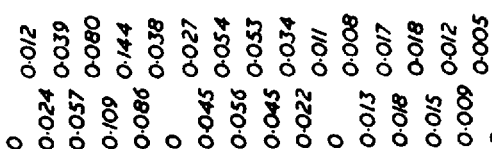
*Influence line for point 6*



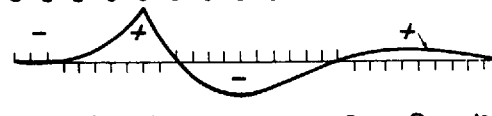
*Influence line for point 7*



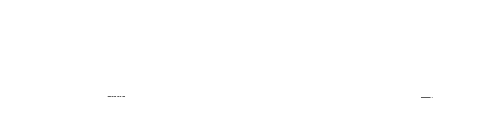
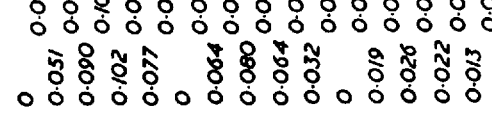
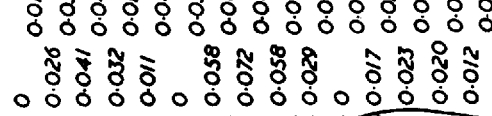
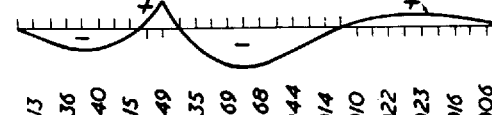
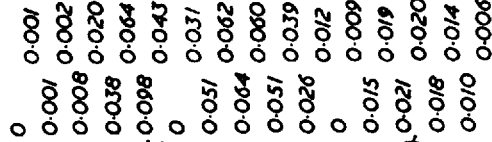
*Influence line for point 8*

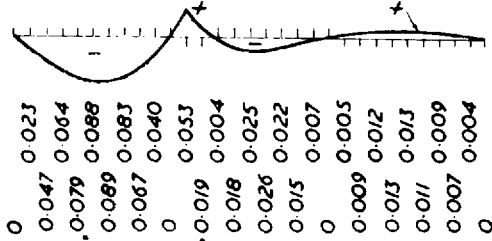
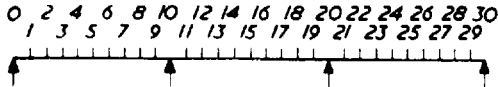


*Influence line for point 9*

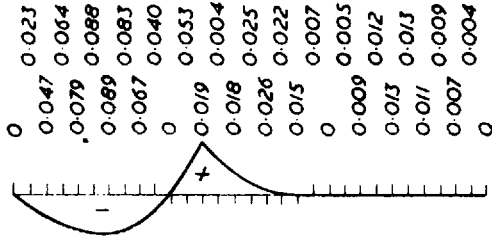


*Influence line for point 10*

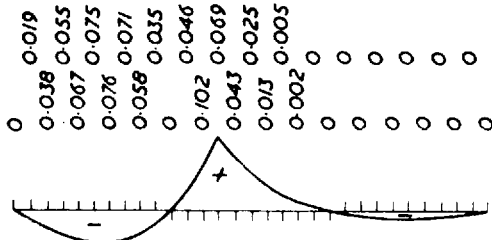




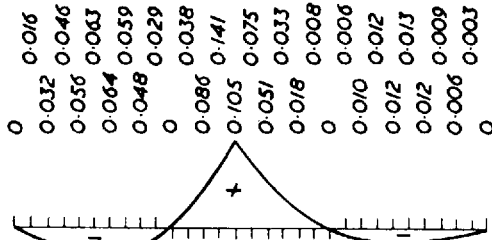
*Influence line for point 11*



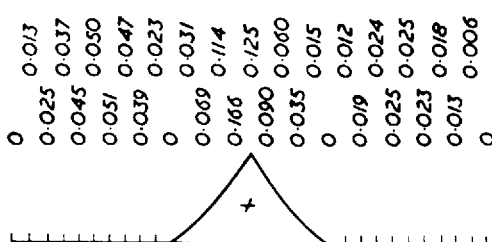
*Influence line for point 12*



*Influence line for point 13*



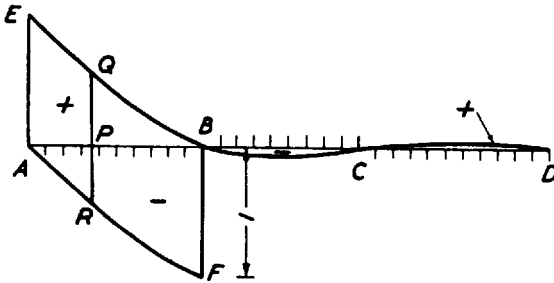
*Influence line for point 14*



*Influence line for point 15*

|    |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |
|----|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 0  | 0.010 | 0.019 | 0.034 | 0.038 | 0.036 | 0.029 | 0     | 0.023 | 0.052 | 0.128 | 0.128 | 0.052 | 0     | 0.018 | 0.029 | 0.038 | 0.038 | 0.034 | 0.019 | 0.010 | 0     |
| 1  | 0.013 | 0.025 | 0.045 | 0.051 | 0.039 | 0     | 0.069 | 0.165 | 0.090 | 0.035 | 0     | 0.019 | 0.012 | 0.025 | 0.025 | 0.023 | 0.013 | 0     | 0.006 | 0.006 | 0.006 |
| 2  | 0.016 | 0.032 | 0.056 | 0.064 | 0.048 | 0     | 0.086 | 0.105 | 0.051 | 0.018 | 0     | 0.010 | 0.012 | 0.012 | 0.012 | 0.006 | 0.003 | 0     | 0.003 | 0.003 | 0.003 |
| 3  | 0.019 | 0.038 | 0.067 | 0.076 | 0.058 | 0     | 0.102 | 0.043 | 0.013 | 0.002 | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     |
| 4  | 0.023 | 0.047 | 0.079 | 0.089 | 0.067 | 0     | 0.019 | 0.018 | 0.026 | 0.015 | 0     | 0.009 | 0.012 | 0.013 | 0.011 | 0.007 | 0.004 | 0     | 0.004 | 0.004 | 0.004 |
| 5  | 0.027 | 0.056 | 0.088 | 0.099 | 0.076 | 0     | 0.025 | 0.025 | 0.022 | 0.007 | 0     | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 0     | 0.005 | 0.005 | 0.005 |
| 6  | 0.031 | 0.064 | 0.096 | 0.107 | 0.084 | 0     | 0.031 | 0.031 | 0.028 | 0.015 | 0     | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0.007 | 0     | 0.007 | 0.007 | 0.007 |
| 7  | 0.036 | 0.071 | 0.103 | 0.114 | 0.090 | 0     | 0.036 | 0.036 | 0.033 | 0.020 | 0     | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0.008 | 0     | 0.008 | 0.008 | 0.008 |
| 8  | 0.040 | 0.077 | 0.110 | 0.121 | 0.096 | 0     | 0.040 | 0.040 | 0.037 | 0.024 | 0     | 0.009 | 0.009 | 0.009 | 0.009 | 0.009 | 0.009 | 0     | 0.009 | 0.009 | 0.009 |
| 9  | 0.044 | 0.082 | 0.116 | 0.127 | 0.101 | 0     | 0.044 | 0.044 | 0.041 | 0.028 | 0     | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0.010 | 0     | 0.010 | 0.010 | 0.010 |
| 10 | 0.048 | 0.087 | 0.121 | 0.132 | 0.105 | 0     | 0.048 | 0.048 | 0.045 | 0.032 | 0     | 0.011 | 0.011 | 0.011 | 0.011 | 0.011 | 0.011 | 0     | 0.011 | 0.011 | 0.011 |
| 11 | 0.053 | 0.092 | 0.126 | 0.137 | 0.110 | 0     | 0.053 | 0.053 | 0.050 | 0.036 | 0     | 0.012 | 0.012 | 0.012 | 0.012 | 0.012 | 0.012 | 0     | 0.012 | 0.012 | 0.012 |
| 12 | 0.057 | 0.096 | 0.131 | 0.142 | 0.114 | 0     | 0.057 | 0.057 | 0.054 | 0.040 | 0     | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 | 0.013 | 0     | 0.013 | 0.013 | 0.013 |
| 13 | 0.061 | 0.100 | 0.135 | 0.146 | 0.118 | 0     | 0.061 | 0.061 | 0.058 | 0.044 | 0     | 0.014 | 0.014 | 0.014 | 0.014 | 0.014 | 0.014 | 0     | 0.014 | 0.014 | 0.014 |
| 14 | 0.065 | 0.104 | 0.139 | 0.150 | 0.121 | 0     | 0.065 | 0.065 | 0.062 | 0.048 | 0     | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0.015 | 0     | 0.015 | 0.015 | 0.015 |
| 15 | 0.069 | 0.108 | 0.143 | 0.154 | 0.124 | 0     | 0.069 | 0.069 | 0.066 | 0.052 | 0     | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0.016 | 0     | 0.016 | 0.016 | 0.016 |
| 16 | 0.073 | 0.112 | 0.147 | 0.158 | 0.127 | 0     | 0.073 | 0.073 | 0.070 | 0.056 | 0     | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 | 0.017 | 0     | 0.017 | 0.017 | 0.017 |
| 17 | 0.077 | 0.116 | 0.151 | 0.162 | 0.130 | 0     | 0.077 | 0.077 | 0.074 | 0.060 | 0     | 0.018 | 0.018 | 0.018 | 0.018 | 0.018 | 0.018 | 0     | 0.018 | 0.018 | 0.018 |
| 18 | 0.081 | 0.120 | 0.155 | 0.166 | 0.133 | 0     | 0.081 | 0.081 | 0.078 | 0.064 | 0     | 0.019 | 0.019 | 0.019 | 0.019 | 0.019 | 0.019 | 0     | 0.019 | 0.019 | 0.019 |
| 19 | 0.085 | 0.124 | 0.159 | 0.170 | 0.136 | 0     | 0.085 | 0.085 | 0.082 | 0.068 | 0     | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0.020 | 0     | 0.020 | 0.020 | 0.020 |
| 20 | 0.089 | 0.128 | 0.163 | 0.171 | 0.139 | 0     | 0.089 | 0.089 | 0.086 | 0.072 | 0     | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0.021 | 0     | 0.021 | 0.021 | 0.021 |
| 21 | 0.093 | 0.132 | 0.167 | 0.172 | 0.142 | 0     | 0.093 | 0.093 | 0.090 | 0.076 | 0     | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0.022 | 0     | 0.022 | 0.022 | 0.022 |
| 22 | 0.097 | 0.136 | 0.171 | 0.173 | 0.145 | 0     | 0.097 | 0.097 | 0.094 | 0.080 | 0     | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0.023 | 0     | 0.023 | 0.023 | 0.023 |
| 23 | 0.101 | 0.140 | 0.175 | 0.174 | 0.148 | 0     | 0.101 | 0.101 | 0.098 | 0.084 | 0     | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0.024 | 0     | 0.024 | 0.024 | 0.024 |
| 24 | 0.105 | 0.144 | 0.179 | 0.175 | 0.151 | 0     | 0.105 | 0.105 | 0.102 | 0.088 | 0     | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0.025 | 0     | 0.025 | 0.025 | 0.025 |
| 25 | 0.109 | 0.148 | 0.183 | 0.176 | 0.154 | 0     | 0.109 | 0.109 | 0.106 | 0.092 | 0     | 0.026 | 0.026 | 0.026 | 0.026 | 0.026 | 0.026 | 0     | 0.026 | 0.026 | 0.026 |
| 26 | 0.113 | 0.152 | 0.187 | 0.177 | 0.157 | 0     | 0.113 | 0.113 | 0.110 | 0.096 | 0     | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0.027 | 0     | 0.027 | 0.027 | 0.027 |
| 27 | 0.117 | 0.156 | 0.191 | 0.178 | 0.160 | 0     | 0.117 | 0.117 | 0.114 | 0.100 | 0     | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0.028 | 0     | 0.028 | 0.028 | 0.028 |
| 28 | 0.121 | 0.160 | 0.195 | 0.179 | 0.163 | 0     | 0.121 | 0.121 | 0.118 | 0.104 | 0     | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0.029 | 0     | 0.029 | 0.029 | 0.029 |
| 29 | 0.125 | 0.164 | 0.199 | 0.180 | 0.166 | 0     | 0.125 | 0.125 | 0.122 | 0.108 | 0     | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0.030 | 0     | 0.030 | 0.030 | 0.030 |
| 30 | 0.129 | 0.168 | 0.203 | 0.181 | 0.169 | 0     | 0.129 | 0.129 | 0.126 | 0.112 | 0     | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0.031 | 0     | 0.031 | 0.031 | 0.031 |

**Influence lines for reactions and shear forces – three-span beam**



*Influence line for reaction at A and S.F. envelope for span AB*

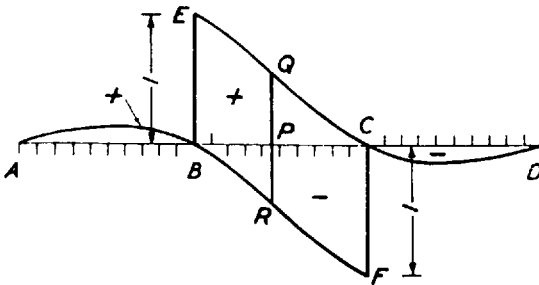
|       |       |       |       |       |       |       |       |       |       |   |       |       |       |       |       |       |       |       |       |   |       |       |       |       |       |       |       |       |       |   |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|
| 1.000 | 0.874 | 0.749 | 0.627 | 0.510 | 0.400 | 0.298 | 0.205 | 0.123 | 0.054 | 0 | 0.064 | 0.039 | 0.077 | 0.080 | 0.075 | 0.064 | 0.049 | 0.032 | 0.015 | 0 | 0.011 | 0.019 | 0.024 | 0.026 | 0.025 | 0.022 | 0.018 | 0.013 | 0.007 | 0 |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|

*Ordinates of line EBCD*



*Influence line for reaction at B*

|   |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |   |       |       |       |       |       |       |       |       |       |   |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|
| 0 | 0.159 | 0.315 | 0.464 | 0.602 | 0.725 | 0.830 | 0.914 | 0.973 | 1.000 | 0.963 | 0.805 | 0.696 | 0.575 | 0.448 | 0.321 | 0.200 | 0.091 | 0 | 0.068 | 0.115 | 0.143 | 0.154 | 0.150 | 0.134 | 0.109 | 0.077 | 0.040 | 0 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|



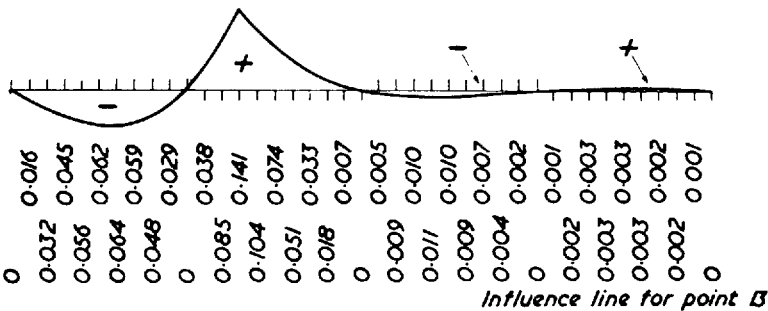
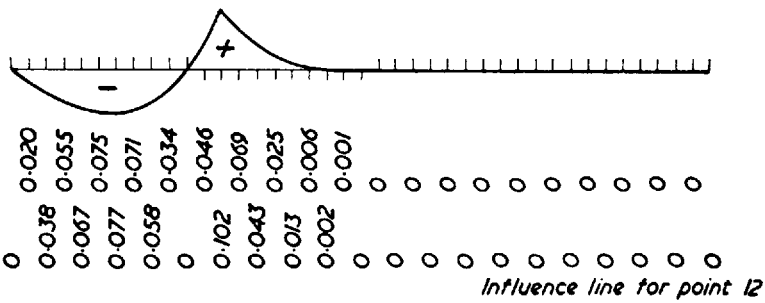
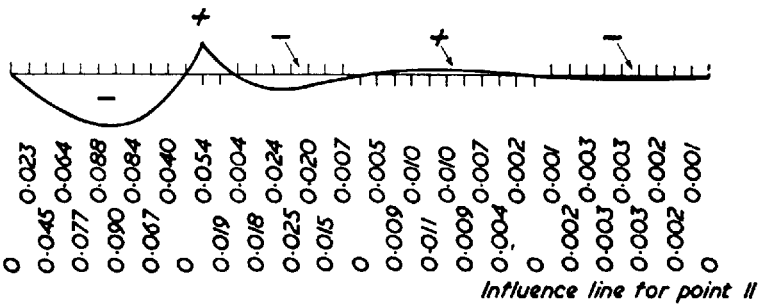
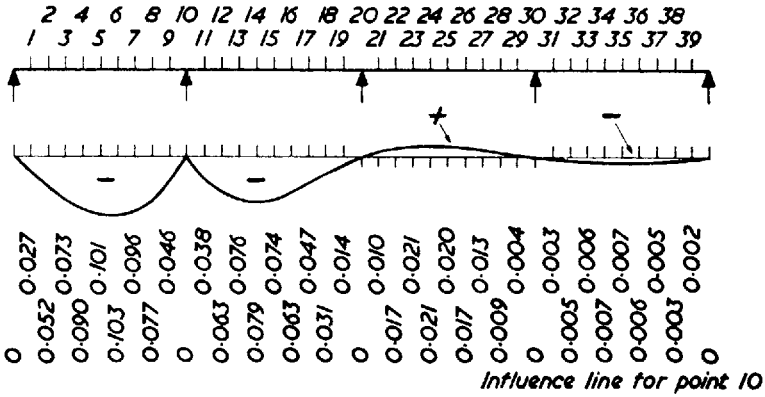
*S.F. envelope for span BC*

|   |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |   |       |       |       |       |       |       |       |       |   |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|---|
| 0 | 0.033 | 0.064 | 0.091 | 0.112 | 0.125 | 0.128 | 0.119 | 0.096 | 0.057 | 1.000 | 0.924 | 0.832 | 0.728 | 0.616 | 0.500 | 0.384 | 0.272 | 0.168 | 0.076 | 0 | 0.057 | 0.096 | 0.119 | 0.125 | 0.112 | 0.091 | 0.064 | 0.033 | 0 |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|---|-------|-------|-------|-------|-------|-------|-------|-------|---|

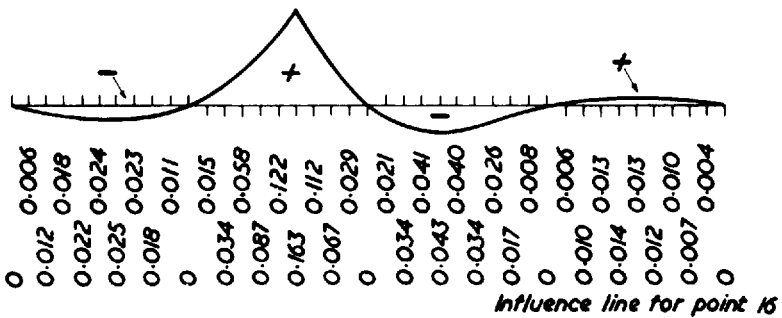
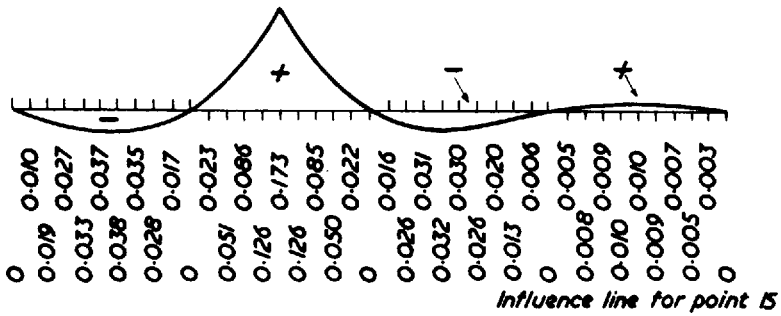
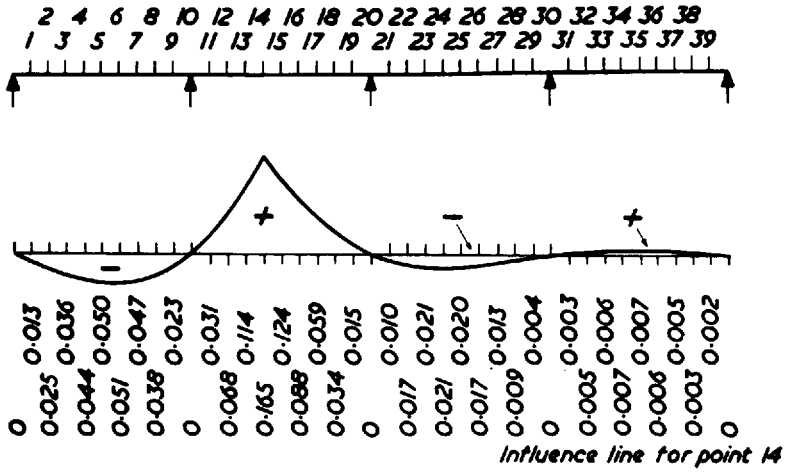
*Ordinates of line ABCE*

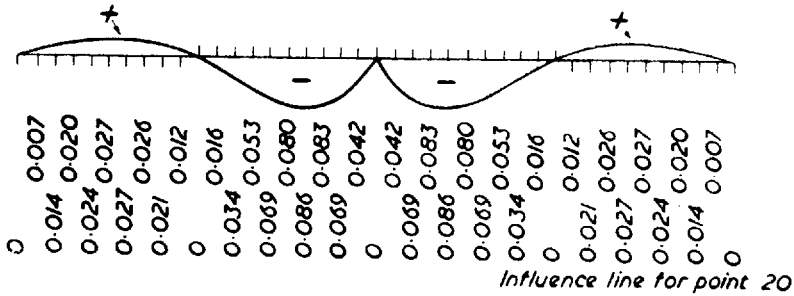
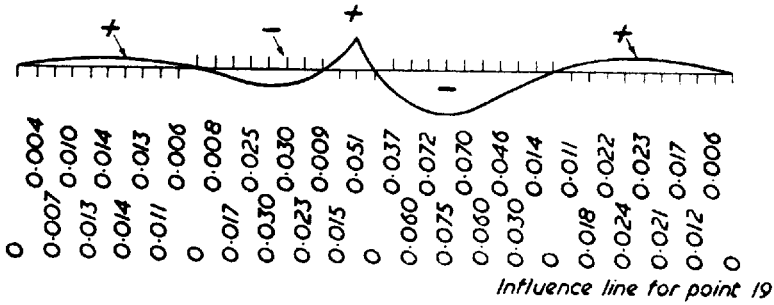
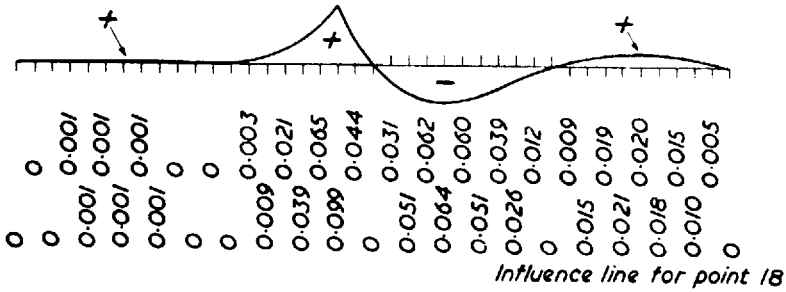
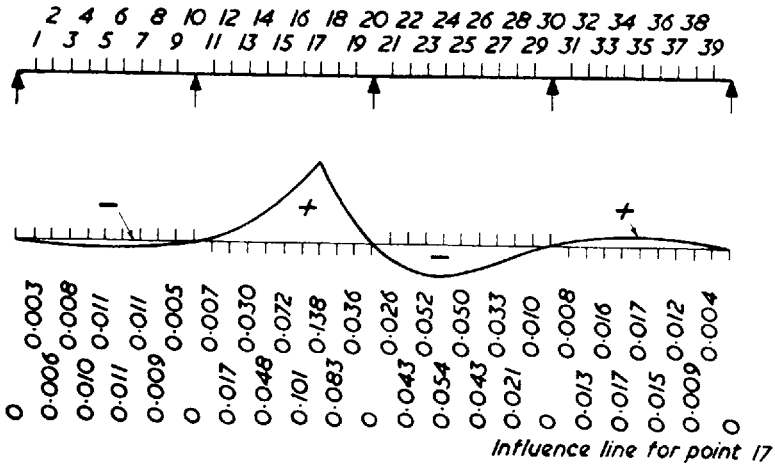


Influence lines for bending moments – four-span beam

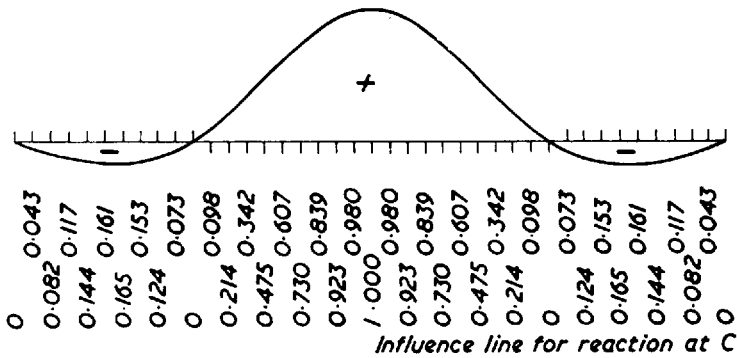
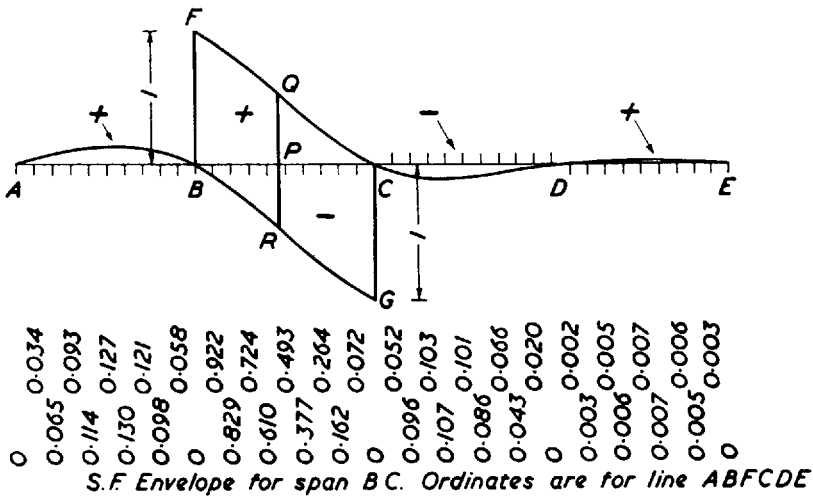
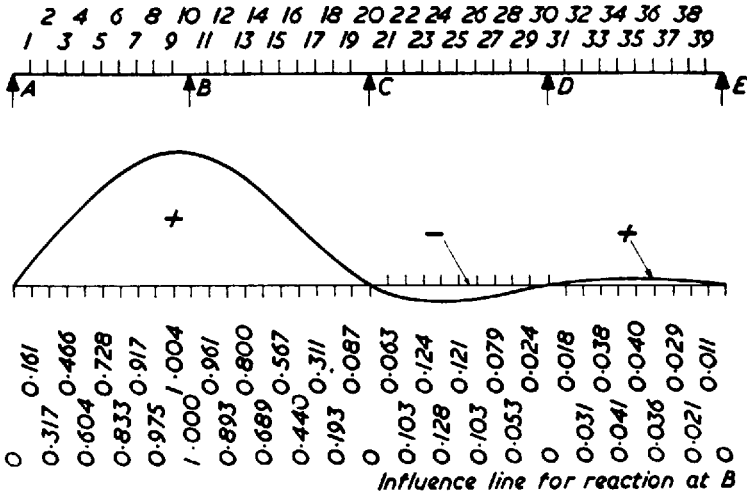


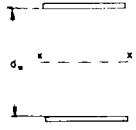
**Influence lines for bending moments – four-span beam**





**Influence lines for reactions and shear forces – four-span beam**





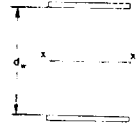
## SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF TWO FLANGES

per millimetre of width

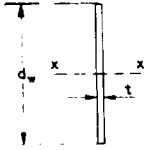
| Distance<br>$d$ ,<br>mm | THICKNESS OF EACH FLANGE IN MILLIMETRES |       |       |       |       |       |       |       |       |       |
|-------------------------|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                         | 10                                      | 12    | 15    | 18    | 20    | 22    | 25    | 28    | 30    | 32    |
| <b>1000</b>             | 510.1                                   | 614.5 | 772.7 | 932.8 | 1041  | 1149  | 1314  | 1480  | 1592  | 1705  |
| <b>1100</b>             | 616.1                                   | 742.0 | 932.5 | 1125  | 1255  | 1385  | 1582  | 1782  | 1916  | 2051  |
| <b>1200</b>             | 732.1                                   | 881.4 | 1107  | 1335  | 1489  | 1643  | 1876  | 2112  | 2270  | 2429  |
| <b>1300</b>             | 858.1                                   | 1033  | 1297  | 1564  | 1743  | 1923  | 2195  | 2469  | 2654  | 2839  |
| <b>1400</b>             | 994.1                                   | 1196  | 1502  | 1810  | 2017  | 2224  | 2539  | 2855  | 3068  | 3282  |
| <b>1500</b>             | 1140                                    | 1372  | 1721  | 2074  | 2311  | 2548  | 2907  | 3269  | 3512  | 3756  |
| <b>1600</b>             | 1296                                    | 1559  | 1956  | 2356  | 2625  | 2894  | 3301  | 3711  | 3986  | 4262  |
| <b>1700</b>             | 1462                                    | 1759  | 2206  | 2656  | 2959  | 3262  | 3720  | 4181  | 4490  | 4800  |
| <b>1800</b>             | 1638                                    | 1970  | 2471  | 2975  | 3313  | 3652  | 4164  | 4679  | 5024  | 5371  |
| <b>1900</b>             | 1824                                    | 2193  | 2750  | 3311  | 3687  | 4064  | 4632  | 5204  | 5588  | 5973  |
| <b>2000</b>             | 2020                                    | 2429  | 3045  | 3665  | 4081  | 4498  | 5126  | 5758  | 6182  | 6607  |
| <b>2100</b>             | 2226                                    | 2676  | 3355  | 4037  | 4495  | 4953  | 5645  | 6340  | 6806  | 7273  |
| <b>2200</b>             | 2442                                    | 2936  | 3680  | 4428  | 4929  | 5431  | 6189  | 6950  | 7460  | 7971  |
| <b>2300</b>             | 2668                                    | 3207  | 4019  | 4836  | 5383  | 5931  | 6757  | 7588  | 8144  | 8702  |
| <b>2400</b>             | 2904                                    | 3491  | 4374  | 5262  | 5857  | 6453  | 7351  | 8254  | 8858  | 9464  |
| <b>2500</b>             | 3150                                    | 3786  | 4744  | 5706  | 6351  | 6997  | 7970  | 8947  | 9602  | 10258 |
| <b>2600</b>             | 3406                                    | 4094  | 5129  | 6169  | 6865  | 7563  | 8614  | 9669  | 10376 | 11084 |
| <b>2700</b>             | 3672                                    | 4413  | 5528  | 6649  | 7399  | 8150  | 9282  | 10419 | 11180 | 11943 |
| <b>2800</b>             | 3948                                    | 4744  | 5943  | 7147  | 7953  | 8760  | 9976  | 11197 | 12014 | 12833 |
| <b>2900</b>             | 4234                                    | 5088  | 6373  | 7663  | 8527  | 9392  | 10695 | 12003 | 12878 | 13755 |
| <b>3000</b>             | 4530                                    | 5443  | 6818  | 8198  | 9121  | 10046 | 11439 | 12837 | 13772 | 14709 |
| <b>3100</b>             | 4836                                    | 5811  | 7277  | 8750  | 9735  | 10722 | 12207 | 13699 | 14696 | 15696 |
| <b>3200</b>             | 5152                                    | 6190  | 7752  | 9320  | 10369 | 11420 | 13001 | 14588 | 15650 | 16714 |
| <b>3300</b>             | 5478                                    | 6582  | 8242  | 9908  | 11023 | 12139 | 13820 | 15506 | 16634 | 17764 |
| <b>3400</b>             | 5814                                    | 6985  | 8747  | 10515 | 11697 | 12881 | 14664 | 16452 | 17648 | 18846 |
| <b>3500</b>             | 6160                                    | 7401  | 9266  | 11139 | 12391 | 13645 | 15532 | 17426 | 18692 | 19961 |
| <b>3600</b>             | 6516                                    | 7828  | 9801  | 11781 | 13105 | 14431 | 16426 | 18428 | 19766 | 21107 |
| <b>3700</b>             | 6882                                    | 8267  | 10351 | 12441 | 13839 | 15239 | 17345 | 19458 | 20870 | 22285 |
| <b>3800</b>             | 7258                                    | 8719  | 10916 | 13120 | 14593 | 16069 | 18289 | 20515 | 22004 | 23495 |
| <b>3900</b>             | 7644                                    | 9182  | 11495 | 13816 | 15367 | 16920 | 19257 | 21601 | 23168 | 24738 |
| <b>4000</b>             | 8040                                    | 9658  | 12090 | 14530 | 16161 | 17794 | 20251 | 22715 | 24362 | 26012 |
| <b>4100</b>             | 8446                                    | 10145 | 12700 | 15262 | 16975 | 18690 | 21270 | 23857 | 25586 | 27318 |
| <b>4200</b>             | 8862                                    | 10645 | 13325 | 16012 | 17809 | 19608 | 22314 | 25027 | 26840 | 28656 |
| <b>4300</b>             | 9288                                    | 11156 | 13964 | 16781 | 18663 | 20548 | 23382 | 26225 | 28124 | 30027 |
| <b>4400</b>             | 9724                                    | 11679 | 14619 | 17567 | 19537 | 21510 | 24476 | 27450 | 29438 | 31429 |
| <b>4500</b>             | 10170                                   | 12215 | 15289 | 18371 | 20431 | 22494 | 25595 | 28704 | 30782 | 32863 |
| <b>4600</b>             | 10626                                   | 12762 | 15974 | 19193 | 21345 | 23499 | 26739 | 29986 | 32156 | 34329 |
| <b>4700</b>             | 11092                                   | 13322 | 16673 | 20034 | 22279 | 24527 | 27907 | 31296 | 33560 | 35827 |
| <b>4800</b>             | 11568                                   | 13893 | 17388 | 20892 | 23233 | 25577 | 29101 | 32634 | 34994 | 37358 |
| <b>4900</b>             | 12054                                   | 14477 | 18118 | 21768 | 24207 | 26649 | 30320 | 34000 | 36458 | 38920 |
| <b>5000</b>             | 12550                                   | 15072 | 18863 | 22662 | 25201 | 27743 | 31564 | 35393 | 37952 | 40514 |

# SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF TWO FLANGES

per millimetre of width



| THICKNESS OF EACH FLANGE IN MILLIMETRES |       |       |       |       |       |       |       |       |       | Distance    |
|---|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------------|
| 35                                      | 38    | 40    | 45    | 50    | 55    | 60    | 65    | 70    | 75    | d,<br>mm    |
| 1875                                    | 2048  | 2164  | 2459  | 2758  | 3064  | 3374  | 3691  | 4013  | 4341  | <b>1000</b> |
| 2255                                    | 2461  | 2600  | 2951  | 3308  | 3671  | 4040  | 4416  | 4797  | 5184  | <b>1100</b> |
| 2670                                    | 2913  | 3076  | 3489  | 3908  | 4334  | 4766  | 5205  | 5651  | 6103  | <b>1200</b> |
| 3120                                    | 3402  | 3592  | 4072  | 4558  | 5052  | 5552  | 6060  | 6575  | 7097  | <b>1300</b> |
| 3604                                    | 3930  | 4148  | 4700  | 5258  | 5825  | 6398  | 6980  | 7569  | 8166  | <b>1400</b> |
| 4124                                    | 4495  | 4744  | 5372  | 6008  | 6652  | 7304  | 7965  | 8633  | 9309  | <b>1500</b> |
| 4679                                    | 5099  | 5380  | 6090  | 6808  | 7535  | 8270  | 9014  | 9767  | 10528 | <b>1600</b> |
| 5269                                    | 5740  | 6056  | 6853  | 7658  | 8473  | 9296  | 10129 | 10971 | 11822 | <b>1700</b> |
| 5893                                    | 6420  | 6772  | 7661  | 8558  | 9466  | 10382 | 11309 | 12245 | 13191 | <b>1800</b> |
| 6553                                    | 7137  | 7528  | 8513  | 9508  | 10513 | 11528 | 12554 | 13589 | 14634 | <b>1900</b> |
| 7248                                    | 7892  | 8324  | 9411  | 10508 | 11616 | 12734 | 13863 | 15003 | 16153 | <b>2000</b> |
| 7978                                    | 8686  | 9160  | 10354 | 11558 | 12774 | 14000 | 15238 | 16487 | 17747 | <b>2100</b> |
| 8742                                    | 9517  | 10036 | 11342 | 12658 | 13987 | 15326 | 16678 | 18041 | 19416 | <b>2200</b> |
| 9542                                    | 10387 | 10952 | 12374 | 13808 | 15254 | 16712 | 18183 | 19665 | 21159 | <b>2300</b> |
| 10377                                   | 11294 | 11908 | 13452 | 15008 | 16577 | 18158 | 19752 | 21359 | 22978 | <b>2400</b> |
| 11247                                   | 12240 | 12904 | 14575 | 16258 | 17955 | 19664 | 21387 | 23123 | 24872 | <b>2500</b> |
| 12151                                   | 13223 | 13940 | 15743 | 17558 | 19388 | 21230 | 23087 | 24957 | 26841 | <b>2600</b> |
| 13091                                   | 14245 | 15016 | 16955 | 18908 | 20875 | 22856 | 24852 | 26861 | 28884 | <b>2700</b> |
| 14066                                   | 15304 | 16132 | 18213 | 20308 | 22418 | 24542 | 26681 | 28835 | 31003 | <b>2800</b> |
| 15076                                   | 16401 | 17288 | 19516 | 21758 | 24016 | 26288 | 28576 | 30879 | 33197 | <b>2900</b> |
| 16120                                   | 17537 | 18484 | 20864 | 23258 | 25669 | 28094 | 30536 | 32993 | 35466 | <b>3000</b> |
| 17200                                   | 18710 | 19720 | 22256 | 24808 | 27376 | 29960 | 32561 | 35177 | 37809 | <b>3100</b> |
| 18315                                   | 19922 | 20996 | 23694 | 26408 | 29139 | 31886 | 34650 | 37431 | 40228 | <b>3200</b> |
| 19465                                   | 21171 | 22312 | 25177 | 28058 | 30957 | 33872 | 36805 | 39755 | 42722 | <b>3300</b> |
| 20649                                   | 22459 | 23668 | 26705 | 29758 | 32830 | 35918 | 39025 | 42149 | 45291 | <b>3400</b> |
| 21869                                   | 23784 | 25064 | 28277 | 31508 | 34757 | 38024 | 41310 | 44613 | 47934 | <b>3500</b> |
| 23124                                   | 25147 | 26500 | 29895 | 33308 | 36740 | 40190 | 43659 | 47147 | 50653 | <b>3600</b> |
| 24414                                   | 26549 | 27976 | 31558 | 35158 | 38778 | 42416 | 46074 | 49751 | 53447 | <b>3700</b> |
| 25738                                   | 27988 | 29492 | 33266 | 37058 | 40871 | 44702 | 48554 | 52425 | 56316 | <b>3800</b> |
| 27098                                   | 29466 | 31048 | 35018 | 39008 | 43018 | 47048 | 51099 | 55169 | 59259 | <b>3900</b> |
| 28493                                   | 30981 | 32644 | 36816 | 41008 | 45221 | 49454 | 53708 | 57983 | 62278 | <b>4000</b> |
| 29923                                   | 32535 | 34280 | 38659 | 43058 | 47479 | 51920 | 56383 | 60867 | 65372 | <b>4100</b> |
| 31387                                   | 34126 | 35956 | 40547 | 45158 | 49792 | 54446 | 59123 | 63821 | 68541 | <b>4200</b> |
| 32887                                   | 35756 | 37672 | 42479 | 47308 | 52159 | 57032 | 61928 | 66845 | 71784 | <b>4300</b> |
| 34422                                   | 37423 | 39428 | 44457 | 49508 | 54582 | 59678 | 64797 | 69939 | 75103 | <b>4400</b> |
| 35992                                   | 39128 | 41224 | 46480 | 51758 | 57060 | 62384 | 67732 | 73103 | 78497 | <b>4500</b> |
| 37596                                   | 40872 | 43060 | 48548 | 54058 | 59593 | 65150 | 70732 | 76337 | 81966 | <b>4600</b> |
| 39236                                   | 42653 | 44936 | 50660 | 56408 | 62180 | 67976 | 73797 | 79641 | 85509 | <b>4700</b> |
| 40911                                   | 44473 | 46852 | 52818 | 58808 | 64823 | 70862 | 76926 | 83015 | 89128 | <b>4800</b> |
| 42621                                   | 46330 | 48808 | 55021 | 61258 | 67521 | 73808 | 80121 | 86459 | 92822 | <b>4900</b> |
| 44365                                   | 48226 | 50804 | 57269 | 63758 | 70274 | 76814 | 83381 | 89973 | 96591 | <b>5000</b> |



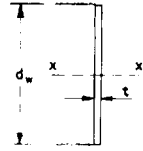
## SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF RECTANGULAR PLATES

about axis x-x

| Depth<br>d,<br>mm | THICKNESS t MILLIMETRES |       |       |       |       |       |
|-------------------|-------------------------|-------|-------|-------|-------|-------|
|                   | 3                       | 4     | 5     | 6     | 8     | 10    |
| <b>25</b>         | .391                    | .521  | .651  | .781  | 1.04  | 1.30  |
| <b>50</b>         | 3.13                    | 4.17  | 5.21  | 6.25  | 8.33  | 10.4  |
| <b>75</b>         | 10.5                    | 14.1  | 17.6  | 21.1  | 28.1  | 35.2  |
| <b>100</b>        | 25.0                    | 33.3  | 41.7  | 50.0  | 66.7  | 83.3  |
| <b>125</b>        | 48.8                    | 65.1  | 81.4  | 97.7  | 130   | 163   |
| <b>150</b>        | 84.4                    | 113   | 141   | 169   | 225   | 281   |
| <b>175</b>        | 134                     | 179   | 223   | 268   | 357   | 447   |
| <b>200</b>        | 200                     | 267   | 333   | 400   | 533   | 667   |
| <b>225</b>        | 285                     | 380   | 475   | 570   | 759   | 949   |
| <b>250</b>        | 391                     | 521   | 651   | 781   | 1042  | 1302  |
| <b>275</b>        | 520                     | 693   | 867   | 1040  | 1386  | 1733  |
| <b>300</b>        | 675                     | 900   | 1125  | 1350  | 1800  | 2250  |
| <b>325</b>        | 858                     | 1144  | 1430  | 1716  | 2289  | 2861  |
| <b>350</b>        | 1072                    | 1429  | 1786  | 2144  | 2858  | 3573  |
| <b>375</b>        | 1318                    | 1758  | 2197  | 2637  | 3516  | 4395  |
| <b>400</b>        | 1600                    | 2133  | 2667  | 3200  | 4267  | 5333  |
| <b>425</b>        | 1919                    | 2559  | 3199  | 3838  | 5118  | 6397  |
| <b>450</b>        | 2278                    | 3038  | 3797  | 4556  | 6075  | 7594  |
| <b>475</b>        | 2679                    | 3572  | 4465  | 5359  | 7145  | 8931  |
| <b>500</b>        | 3125                    | 4167  | 5208  | 6250  | 8333  | 10417 |
| <b>525</b>        | 3618                    | 4823  | 6029  | 7235  | 9647  | 12059 |
| <b>550</b>        | 4159                    | 5546  | 6932  | 8319  | 11092 | 13865 |
| <b>575</b>        | 4753                    | 6337  | 7921  | 9505  | 12674 | 15842 |
| <b>600</b>        | 5400                    | 7200  | 9000  | 10800 | 14400 | 18000 |
| <b>625</b>        | 6104                    | 8138  | 10173 | 12207 | 16276 | 20345 |
| <b>650</b>        | 6866                    | 9154  | 11443 | 13731 | 18308 | 22885 |
| <b>675</b>        | 7689                    | 10252 | 12814 | 15377 | 20503 | 25629 |
| <b>700</b>        | 8575                    | 11433 | 14292 | 17150 | 22867 | 28583 |
| <b>725</b>        | 9527                    | 12703 | 15878 | 19054 | 25405 | 31757 |
| <b>750</b>        | 10547                   | 14063 | 17578 | 21094 | 28125 | 35156 |
| <b>775</b>        | 11637                   | 15516 | 19395 | 23274 | 31032 | 38790 |
| <b>800</b>        | 12800                   | 17067 | 21333 | 25600 | 34133 | 42667 |
| <b>825</b>        | 14038                   | 18717 | 23396 | 28076 | 37434 | 46793 |
| <b>850</b>        | 15353                   | 20471 | 25589 | 30706 | 40942 | 51177 |
| <b>875</b>        | 16748                   | 22331 | 27913 | 33496 | 44661 | 55827 |
| <b>900</b>        | 18225                   | 24300 | 30375 | 36450 | 48600 | 60750 |

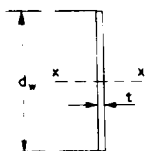
# SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF RECTANGULAR PLATES

about axis x-x



| THICKNESS t MILLIMETRES |       |        |        |        |        | Depth      |
|-------------------------|-------|--------|--------|--------|--------|------------|
| 12                      | 15    | 18     | 20     | 22     | 25     | d, mm      |
| 1.56                    | 1.95  | 2.34   | 2.60   | 2.86   | 3.26   | <b>25</b>  |
| 12.5                    | 15.6  | 18.8   | 20.8   | 22.9   | 26.0   | <b>50</b>  |
| 42.2                    | 52.7  | 63.3   | 70.3   | 77.3   | 87.9   | <b>75</b>  |
| 100                     | 125   | 150    | 167    | 183    | 208    | <b>100</b> |
| 195                     | 244   | 293    | 326    | 358    | 407    | <b>125</b> |
| 338                     | 422   | 506    | 563    | 619    | 703    | <b>150</b> |
| 536                     | 670   | 804    | 893    | 983    | 1117   | <b>175</b> |
| 800                     | 1000  | 1200   | 1333   | 1467   | 1667   | <b>200</b> |
| 1139                    | 1424  | 1709   | 1898   | 2088   | 2373   | <b>225</b> |
| 1563                    | 1953  | 2344   | 2604   | 2865   | 3255   | <b>250</b> |
| 2080                    | 2600  | 3120   | 3466   | 3813   | 4333   | <b>275</b> |
| 2700                    | 3375  | 4050   | 4500   | 4950   | 5625   | <b>300</b> |
| 3433                    | 4291  | 5149   | 5721   | 6293   | 7152   | <b>325</b> |
| 4288                    | 5359  | 6431   | 7146   | 7860   | 8932   | <b>350</b> |
| 5273                    | 6592  | 7910   | 8789   | 9668   | 10986  | <b>375</b> |
| 6400                    | 8000  | 9600   | 10667  | 11733  | 13333  | <b>400</b> |
| 7677                    | 9596  | 11515  | 12794  | 14074  | 15993  | <b>425</b> |
| 9113                    | 11391 | 13669  | 15188  | 16706  | 18984  | <b>450</b> |
| 10717                   | 13396 | 16076  | 17862  | 19648  | 22327  | <b>475</b> |
| 12500                   | 15625 | 18750  | 20833  | 22917  | 26042  | <b>500</b> |
| 14470                   | 18088 | 21705  | 24117  | 26529  | 30146  | <b>525</b> |
| 16638                   | 20797 | 24956  | 27729  | 30502  | 34661  | <b>550</b> |
| 19011                   | 23764 | 28516  | 31685  | 34853  | 39606  | <b>575</b> |
| 21600                   | 27000 | 32400  | 36000  | 39600  | 45000  | <b>600</b> |
| 24414                   | 30518 | 36621  | 40690  | 44759  | 50863  | <b>625</b> |
| 27463                   | 34328 | 41194  | 45771  | 50348  | 57214  | <b>650</b> |
| 30755                   | 38443 | 46132  | 51258  | 56384  | 64072  | <b>675</b> |
| 34300                   | 42875 | 51450  | 57167  | 62883  | 71458  | <b>700</b> |
| 38108                   | 47635 | 57162  | 63513  | 69864  | 79391  | <b>725</b> |
| 42188                   | 52734 | 63281  | 70313  | 77344  | 87891  | <b>750</b> |
| 46548                   | 58186 | 69823  | 77581  | 85339  | 96976  | <b>775</b> |
| 51200                   | 64000 | 76800  | 85333  | 93867  | 106667 | <b>800</b> |
| 56152                   | 70189 | 84227  | 93586  | 102945 | 116982 | <b>825</b> |
| 61413                   | 76766 | 92119  | 102354 | 112590 | 127943 | <b>850</b> |
| 66992                   | 83740 | 100488 | 111654 | 122819 | 139567 | <b>875</b> |
| 72900                   | 91125 | 109350 | 121500 | 133650 | 151875 | <b>900</b> |





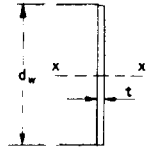
## SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF RECTANGULAR PLATES

about axis x-x

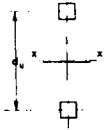
| Depth<br>d,<br>mm | THICKNESS t MILLIMETRES |         |         |         |         |          |
|-------------------|-------------------------|---------|---------|---------|---------|----------|
|                   | 3                       | 4       | 5       | 6       | 8       | 10       |
| 1000              | 25000                   | 33333   | 41667   | 50000   | 66667   | 83333    |
| 1100              | 33275                   | 44367   | 55458   | 66550   | 88733   | 110917   |
| 1200              | 43200                   | 57600   | 72000   | 86400   | 115200  | 144000   |
| 1300              | 54925                   | 73233   | 91542   | 109850  | 146467  | 183083   |
| 1400              | 68600                   | 91467   | 114333  | 137200  | 182933  | 228667   |
| 1500              | 84375                   | 112500  | 140625  | 168750  | 225000  | 281250   |
| 1600              | 102400                  | 136533  | 170667  | 204800  | 273067  | 341333   |
| 1700              | 122825                  | 163767  | 204708  | 245650  | 327533  | 409417   |
| 1800              | 145800                  | 194400  | 243000  | 291600  | 388800  | 486000   |
| 1900              | 171475                  | 228633  | 285792  | 342950  | 457267  | 571583   |
| 2000              | 200000                  | 266667  | 333333  | 400000  | 533333  | 666667   |
| 2100              | 231525                  | 308700  | 385875  | 463050  | 617400  | 771750   |
| 2200              | 266200                  | 354933  | 443667  | 532400  | 709867  | 887333   |
| 2300              | 304175                  | 405567  | 506958  | 608350  | 811133  | 1013917  |
| 2400              | 345600                  | 460800  | 576000  | 691200  | 921600  | 1152000  |
| 2500              | 390625                  | 520833  | 651042  | 781250  | 1041667 | 1302083  |
| 2600              | 439400                  | 585867  | 732333  | 878800  | 1171733 | 1464667  |
| 2700              | 492075                  | 656100  | 820125  | 984150  | 1312200 | 1640250  |
| 2800              | 548800                  | 731733  | 914667  | 1097600 | 1463467 | 1829333  |
| 2900              | 609725                  | 812967  | 1016208 | 1219450 | 1625933 | 2032417  |
| 3000              | 675000                  | 900000  | 1125000 | 1350000 | 1800000 | 2250000  |
| 3100              | 744775                  | 993033  | 1241292 | 1489550 | 1986067 | 2482583  |
| 3200              | 819200                  | 1092267 | 1365333 | 1638400 | 2184533 | 2730667  |
| 3300              | 898425                  | 1197900 | 1497375 | 1796850 | 2395800 | 2994750  |
| 3400              | 982600                  | 1310133 | 1637667 | 1965200 | 2620267 | 3275333  |
| 3500              | 1071875                 | 1429167 | 1786458 | 2143750 | 2858333 | 3572917  |
| 3600              | 1166400                 | 1555200 | 1944000 | 2332800 | 3110400 | 3888000  |
| 3700              | 1266325                 | 1688433 | 2110542 | 2532650 | 3376867 | 4221083  |
| 3800              | 1371800                 | 1829067 | 2286333 | 2743600 | 3658133 | 4572667  |
| 3900              | 1482975                 | 1977300 | 2471625 | 2965950 | 3954600 | 4943250  |
| 4000              | 1600000                 | 2133333 | 2666667 | 3200000 | 4266667 | 5333333  |
| 4100              | 1723025                 | 2297367 | 2871708 | 3446050 | 4594733 | 5743417  |
| 4200              | 1852200                 | 2469600 | 3087000 | 3704400 | 4939200 | 6174000  |
| 4300              | 1987675                 | 2650233 | 3312792 | 3975350 | 5300467 | 6625583  |
| 4400              | 2129600                 | 2839467 | 3549333 | 4259200 | 5678933 | 7098667  |
| 4500              | 2278125                 | 3037500 | 3796875 | 4556250 | 6075000 | 7593750  |
| 4600              | 2433400                 | 3244533 | 4055667 | 4866800 | 6489067 | 8111333  |
| 4700              | 2595575                 | 3460767 | 4325958 | 5191150 | 6921533 | 8651917  |
| 4800              | 2764800                 | 3686400 | 4608000 | 5529600 | 7372800 | 9216000  |
| 4900              | 2941225                 | 3921633 | 4902042 | 5882450 | 7843267 | 9804083  |
| 5000              | 3125000                 | 4166667 | 5208333 | 6250000 | 8333333 | 10416667 |

# SECOND MOMENTS OF AREA (cm<sup>4</sup>) OF RECTANGULAR PLATES

about axis x-x



| THICKNESS t MILLIMETRES |          |          |          |          |          | Depth                |
|-------------------------|----------|----------|----------|----------|----------|----------------------|
| 12                      | 15       | 18       | 20       | 22       | 25       | d <sub>w</sub><br>mm |
| 100000                  | 125000   | 150000   | 166667   | 183333   | 208333   | <b>1000</b>          |
| 133100                  | 166375   | 199650   | 221833   | 244017   | 277292   | <b>1100</b>          |
| 172800                  | 216000   | 259200   | 288000   | 316800   | 360000   | <b>1200</b>          |
| 219700                  | 274625   | 329550   | 366167   | 402783   | 457708   | <b>1300</b>          |
| 274400                  | 343000   | 411600   | 457333   | 503067   | 571667   | <b>1400</b>          |
| 337500                  | 421875   | 506250   | 562500   | 618750   | 703125   | <b>1500</b>          |
| 409600                  | 512000   | 614400   | 682667   | 750933   | 853333   | <b>1600</b>          |
| 491300                  | 614125   | 736950   | 818833   | 900717   | 1023542  | <b>1700</b>          |
| 583200                  | 729000   | 874800   | 972000   | 1069200  | 1215000  | <b>1800</b>          |
| 685900                  | 857375   | 1028850  | 1143167  | 1257483  | 1428958  | <b>1900</b>          |
| 800000                  | 1000000  | 1200000  | 1333333  | 1466667  | 1666667  | <b>2000</b>          |
| 926100                  | 1157625  | 1389150  | 1543500  | 1697850  | 1929375  | <b>2100</b>          |
| 1064800                 | 1331000  | 1597200  | 1774667  | 1952133  | 2218333  | <b>2200</b>          |
| 1216700                 | 1520875  | 1825050  | 2027833  | 2230617  | 2534792  | <b>2300</b>          |
| 1382400                 | 1728000  | 2073600  | 2304000  | 2534400  | 2880000  | <b>2400</b>          |
| 1562500                 | 1953125  | 2343750  | 2604167  | 2864583  | 3255208  | <b>2500</b>          |
| 1757600                 | 2197000  | 2636400  | 2929333  | 3222267  | 3661667  | <b>2600</b>          |
| 1968300                 | 2460375  | 2952450  | 3280500  | 3608550  | 4100625  | <b>2700</b>          |
| 2195200                 | 2744000  | 3292800  | 3658667  | 4024533  | 4573333  | <b>2800</b>          |
| 2438900                 | 3048625  | 3658350  | 4064833  | 4471317  | 5081042  | <b>2900</b>          |
| 2700000                 | 3375000  | 4050000  | 4500000  | 4950000  | 5625000  | <b>3000</b>          |
| 2979100                 | 3723875  | 4468650  | 4965167  | 5461683  | 6206458  | <b>3100</b>          |
| 3276800                 | 4096000  | 4915200  | 5461333  | 6007467  | 6826667  | <b>3200</b>          |
| 3593700                 | 4492125  | 5390550  | 5989500  | 6588450  | 7486875  | <b>3300</b>          |
| 3930400                 | 4913000  | 5895600  | 6550667  | 7205733  | 8188333  | <b>3400</b>          |
| 4287500                 | 5359375  | 6431250  | 7145833  | 7860417  | 8932292  | <b>3500</b>          |
| 4665600                 | 5832000  | 6998400  | 7776000  | 8553600  | 9720000  | <b>3600</b>          |
| 5065300                 | 6331625  | 7597950  | 8442167  | 9286383  | 10552708 | <b>3700</b>          |
| 5487200                 | 6859000  | 8230800  | 9145333  | 10059867 | 11431667 | <b>3800</b>          |
| 5931900                 | 7414875  | 8897850  | 9886500  | 10875150 | 12358125 | <b>3900</b>          |
| 6400000                 | 8000000  | 9600000  | 10666667 | 11733333 | 13333333 | <b>4000</b>          |
| 6892100                 | 8615125  | 10338150 | 11486833 | 12635517 | 14358542 | <b>4100</b>          |
| 7408800                 | 9261000  | 11113200 | 12348000 | 13582800 | 15435000 | <b>4200</b>          |
| 7950700                 | 9938375  | 11926050 | 13251167 | 14576283 | 16563958 | <b>4300</b>          |
| 8518400                 | 10648000 | 12777600 | 14197333 | 15617067 | 17746667 | <b>4400</b>          |
| 9112500                 | 11390625 | 13668750 | 15187500 | 16706250 | 18984375 | <b>4500</b>          |
| 9733600                 | 12167000 | 14600400 | 16222667 | 17844933 | 20278333 | <b>4600</b>          |
| 10382300                | 12977875 | 15573450 | 17303833 | 19034217 | 21629792 | <b>4700</b>          |
| 11059200                | 13824000 | 16588800 | 18432000 | 20275200 | 23040000 | <b>4800</b>          |
| 11764900                | 14706125 | 17647350 | 19608167 | 21568983 | 24510208 | <b>4900</b>          |
| 12500000                | 15625000 | 18750000 | 20833333 | 22916667 | 26041667 | <b>5000</b>          |



# SECOND MOMENT OF A PAIR OF UNIT AREAS

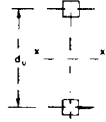
about axis  $x-x$

| Distance<br>$d$ ,<br>mm | 0     | 5     | 10    | 15    | 20    | 25    | 30    | 35    | 40    | 45    |
|-------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| <b>500</b>              | 1250  | 1275  | 1301  | 1326  | 1352  | 1378  | 1405  | 1431  | 1458  | 1485  |
| <b>550</b>              | 1513  | 1540  | 1568  | 1596  | 1625  | 1653  | 1682  | 1711  | 1741  | 1770  |
| <b>600</b>              | 1800  | 1830  | 1861  | 1891  | 1922  | 1953  | 1985  | 2016  | 2048  | 2080  |
| <b>650</b>              | 2113  | 2145  | 2178  | 2211  | 2245  | 2278  | 2312  | 2346  | 2381  | 2415  |
| <b>700</b>              | 2450  | 2485  | 2521  | 2556  | 2592  | 2628  | 2665  | 2701  | 2738  | 2775  |
| <b>750</b>              | 2813  | 2850  | 2888  | 2926  | 2965  | 3003  | 3042  | 3081  | 3121  | 3160  |
| <b>800</b>              | 3200  | 3240  | 3281  | 3321  | 3362  | 3403  | 3445  | 3486  | 3528  | 3570  |
| <b>850</b>              | 3613  | 3655  | 3698  | 3741  | 3785  | 3828  | 3872  | 3916  | 3961  | 4005  |
| <b>900</b>              | 4050  | 4095  | 4141  | 4186  | 4232  | 4278  | 4325  | 4371  | 4418  | 4465  |
| <b>950</b>              | 4513  | 4560  | 4608  | 4656  | 4705  | 4753  | 4802  | 4851  | 4901  | 4950  |
| <b>1000</b>             | 5000  | 5050  | 5101  | 5151  | 5202  | 5253  | 5305  | 5356  | 5408  | 5460  |
| <b>1050</b>             | 5513  | 5565  | 5618  | 5671  | 5725  | 5778  | 5832  | 5886  | 5941  | 5995  |
| <b>1100</b>             | 6050  | 6105  | 6161  | 6216  | 6272  | 6328  | 6385  | 6441  | 6498  | 6555  |
| <b>1150</b>             | 6613  | 6670  | 6728  | 6786  | 6845  | 6903  | 6962  | 7021  | 7081  | 7140  |
| <b>1200</b>             | 7200  | 7260  | 7321  | 7381  | 7442  | 7503  | 7565  | 7626  | 7688  | 7750  |
| <b>1250</b>             | 7813  | 7875  | 7938  | 8001  | 8065  | 8128  | 8192  | 8256  | 8321  | 8385  |
| <b>1300</b>             | 8450  | 8515  | 8581  | 8646  | 8712  | 8778  | 8845  | 8911  | 8978  | 9045  |
| <b>1350</b>             | 9113  | 9180  | 9248  | 9316  | 9385  | 9453  | 9522  | 9591  | 9661  | 9730  |
| <b>1400</b>             | 9800  | 9870  | 9941  | 10011 | 10082 | 10153 | 10225 | 10296 | 10368 | 10440 |
| <b>1450</b>             | 10513 | 10585 | 10658 | 10731 | 10805 | 10878 | 10952 | 11026 | 11101 | 11175 |
| <b>1500</b>             | 11250 | 11325 | 11401 | 11476 | 11552 | 11628 | 11705 | 11781 | 11858 | 11935 |
| <b>1550</b>             | 12013 | 12090 | 12168 | 12246 | 12325 | 12403 | 12482 | 12561 | 12641 | 12720 |
| <b>1600</b>             | 12800 | 12880 | 12961 | 13041 | 13122 | 13203 | 13285 | 13366 | 13448 | 13530 |
| <b>1650</b>             | 13613 | 13695 | 13778 | 13861 | 13945 | 14028 | 14112 | 14196 | 14281 | 14365 |
| <b>1700</b>             | 14450 | 14535 | 14621 | 14706 | 14792 | 14878 | 14965 | 15051 | 15138 | 15225 |
| <b>1750</b>             | 15313 | 15400 | 15488 | 15576 | 15665 | 15753 | 15842 | 15931 | 16021 | 16110 |
| <b>1800</b>             | 16200 | 16290 | 16381 | 16471 | 16562 | 16653 | 16745 | 16836 | 16928 | 17020 |
| <b>1850</b>             | 17113 | 17205 | 17298 | 17391 | 17485 | 17578 | 17672 | 17766 | 17861 | 17955 |
| <b>1900</b>             | 18050 | 18145 | 18241 | 18336 | 18432 | 18528 | 18625 | 18721 | 18818 | 18915 |
| <b>1950</b>             | 19013 | 19110 | 19208 | 19306 | 19405 | 19503 | 19602 | 19701 | 19801 | 19900 |
| <b>2000</b>             | 20000 | 20100 | 20201 | 20301 | 20402 | 20503 | 20605 | 20706 | 20808 | 20910 |
| <b>2050</b>             | 21013 | 21115 | 21218 | 21321 | 21425 | 21528 | 21632 | 21736 | 21841 | 21945 |
| <b>2100</b>             | 22050 | 22155 | 22261 | 22366 | 22472 | 22578 | 22685 | 22791 | 22898 | 23005 |
| <b>2150</b>             | 23113 | 23220 | 23328 | 23436 | 23545 | 23653 | 23762 | 23871 | 23981 | 24090 |
| <b>2200</b>             | 24200 | 24310 | 24421 | 24531 | 24642 | 24753 | 24865 | 24976 | 25088 | 25200 |
| <b>2250</b>             | 25313 | 25425 | 25538 | 25651 | 25765 | 25878 | 25992 | 26106 | 26221 | 26335 |
| <b>2300</b>             | 26450 | 26565 | 26681 | 26796 | 26912 | 27028 | 27145 | 27261 | 27378 | 27495 |
| <b>2350</b>             | 27613 | 27730 | 27848 | 27966 | 28085 | 28203 | 28322 | 28441 | 28561 | 28680 |
| <b>2400</b>             | 28800 | 28920 | 29041 | 29161 | 29282 | 29403 | 29525 | 29646 | 29768 | 29890 |
| <b>2450</b>             | 30013 | 30135 | 30258 | 30381 | 30505 | 30628 | 30752 | 30876 | 31001 | 31125 |
| <b>2500</b>             | 31250 | 31375 | 31501 | 31626 | 31752 | 31878 | 32005 | 32131 | 32258 | 32385 |
| <b>2550</b>             | 32513 | 32640 | 32768 | 32896 | 33025 | 33153 | 33282 | 33411 | 33541 | 33670 |
| <b>2600</b>             | 33800 | 33930 | 34061 | 34191 | 34322 | 34453 | 34585 | 34716 | 34848 | 34980 |
| <b>2650</b>             | 35113 | 35245 | 35378 | 35511 | 35645 | 35778 | 35912 | 36046 | 36181 | 36315 |
| <b>2700</b>             | 36450 | 36585 | 36721 | 36856 | 36992 | 37128 | 37265 | 37401 | 37538 | 37675 |

Second moments are tabulated in  $\text{cm}^4$  and are for unit areas of  $1 \text{ cm}^2$  each.

# SECOND MOMENT OF A PAIR OF UNIT AREAS

about axis  $x-x$

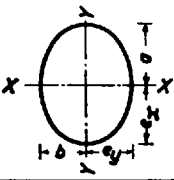
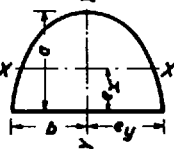
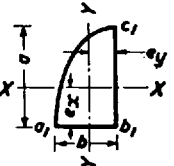
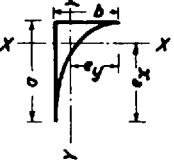
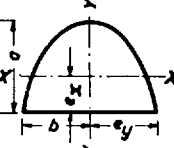
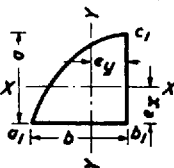
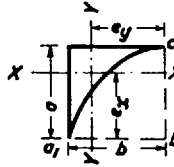
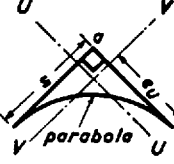


| Distance<br>$d$ ,<br>mm | 0      | 5      | 10     | 15     | 20     | 25     | 30     | 35     | 40     | 45     |
|-------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| <b>2750</b>             | 37813  | 37950  | 38088  | 38226  | 38365  | 38503  | 38642  | 38781  | 38921  | 39060  |
| <b>2800</b>             | 39200  | 39340  | 39481  | 39621  | 39762  | 39903  | 40045  | 40186  | 40328  | 40470  |
| <b>2850</b>             | 40613  | 40755  | 40898  | 41041  | 41185  | 41328  | 41472  | 41616  | 41761  | 41905  |
| <b>2900</b>             | 42050  | 42195  | 42341  | 42486  | 42632  | 42778  | 42925  | 43071  | 43218  | 43365  |
| <b>2950</b>             | 43513  | 43660  | 43808  | 43956  | 44105  | 44253  | 44402  | 44551  | 44701  | 44850  |
| <b>3000</b>             | 45000  | 45150  | 45301  | 45451  | 45602  | 45753  | 45905  | 46056  | 46208  | 46360  |
| <b>3050</b>             | 46513  | 46665  | 46818  | 46971  | 47125  | 47278  | 47432  | 47586  | 47741  | 47895  |
| <b>3100</b>             | 48050  | 48205  | 48361  | 48516  | 48672  | 48828  | 48985  | 49141  | 49298  | 49455  |
| <b>3150</b>             | 49613  | 49770  | 49928  | 50086  | 50245  | 50403  | 50562  | 50721  | 50881  | 51040  |
| <b>3200</b>             | 51200  | 51360  | 51521  | 51681  | 51842  | 52003  | 52165  | 52326  | 52488  | 52650  |
| <b>3250</b>             | 52813  | 52975  | 53138  | 53301  | 53465  | 53628  | 53792  | 53956  | 54121  | 54285  |
| <b>3300</b>             | 54450  | 54615  | 54781  | 54946  | 55112  | 55278  | 55445  | 55611  | 55778  | 55945  |
| <b>3350</b>             | 56113  | 56280  | 56448  | 56616  | 56785  | 56953  | 57122  | 57291  | 57461  | 57630  |
| <b>3400</b>             | 57800  | 57970  | 58141  | 58311  | 58482  | 58653  | 58825  | 58996  | 59168  | 59340  |
| <b>3450</b>             | 59513  | 59685  | 59858  | 60031  | 60205  | 60378  | 60552  | 60726  | 60901  | 61075  |
| <b>3500</b>             | 61250  | 61425  | 61601  | 61776  | 61952  | 62128  | 62305  | 62481  | 62658  | 62835  |
| <b>3550</b>             | 63013  | 63190  | 63368  | 63546  | 63725  | 63903  | 64082  | 64261  | 64441  | 64620  |
| <b>3600</b>             | 64800  | 64980  | 65161  | 65341  | 65522  | 65703  | 65885  | 66066  | 66248  | 66430  |
| <b>3650</b>             | 66613  | 66795  | 66978  | 67161  | 67345  | 67528  | 67712  | 67896  | 68081  | 68265  |
| <b>3700</b>             | 68450  | 68635  | 68821  | 69006  | 69192  | 69378  | 69565  | 69751  | 69938  | 70125  |
| <b>3750</b>             | 70313  | 70500  | 70688  | 70876  | 71065  | 71253  | 71442  | 71631  | 71821  | 72010  |
| <b>3800</b>             | 72200  | 72390  | 72581  | 72771  | 72962  | 73153  | 73345  | 73536  | 73728  | 73920  |
| <b>3850</b>             | 74113  | 74305  | 74498  | 74691  | 74885  | 75078  | 75272  | 75466  | 75661  | 75855  |
| <b>3900</b>             | 76050  | 76245  | 76441  | 76636  | 76832  | 77028  | 77225  | 77421  | 77618  | 77815  |
| <b>3950</b>             | 78013  | 78210  | 78408  | 78606  | 78805  | 79003  | 79202  | 79401  | 79601  | 79800  |
| <b>4000</b>             | 80000  | 80200  | 80401  | 80601  | 80802  | 81003  | 81205  | 81406  | 81608  | 81810  |
| <b>4050</b>             | 82013  | 82215  | 82418  | 82621  | 82825  | 83028  | 83232  | 83436  | 83641  | 83845  |
| <b>4100</b>             | 84050  | 84255  | 84461  | 84666  | 84872  | 85078  | 85285  | 85491  | 85698  | 85905  |
| <b>4150</b>             | 86113  | 86320  | 86528  | 86736  | 86945  | 87153  | 87362  | 87571  | 87781  | 87990  |
| <b>4200</b>             | 88200  | 88410  | 88621  | 88831  | 89042  | 89253  | 89465  | 89676  | 89888  | 90100  |
| <b>4250</b>             | 90313  | 90525  | 90738  | 90951  | 91165  | 91378  | 91592  | 91806  | 92021  | 92235  |
| <b>4300</b>             | 92450  | 92665  | 92881  | 93096  | 93312  | 93528  | 93745  | 93961  | 94178  | 94395  |
| <b>4350</b>             | 94613  | 94830  | 95048  | 95266  | 95485  | 95703  | 95922  | 96141  | 96361  | 96580  |
| <b>4400</b>             | 96800  | 97020  | 97241  | 97461  | 97682  | 97903  | 98125  | 98346  | 98568  | 98790  |
| <b>4450</b>             | 99013  | 99235  | 99458  | 99681  | 99905  | 100128 | 100352 | 100576 | 100801 | 101025 |
| <b>4500</b>             | 101250 | 101475 | 101701 | 101926 | 102152 | 102378 | 102605 | 102831 | 103058 | 103285 |
| <b>4550</b>             | 103513 | 103740 | 103968 | 104196 | 104425 | 104653 | 104882 | 105111 | 105341 | 105570 |
| <b>4600</b>             | 105800 | 106030 | 106261 | 106491 | 106722 | 106953 | 107185 | 107416 | 107648 | 107880 |
| <b>4650</b>             | 108113 | 108345 | 108578 | 108811 | 109045 | 109278 | 109512 | 109746 | 109981 | 110215 |
| <b>4700</b>             | 110450 | 110685 | 110921 | 111156 | 111392 | 111628 | 111865 | 112101 | 112338 | 112575 |
| <b>4750</b>             | 112813 | 113050 | 113288 | 113526 | 113765 | 114003 | 114242 | 114481 | 114721 | 114960 |
| <b>4800</b>             | 115200 | 115440 | 115681 | 115921 | 116162 | 116403 | 116645 | 116886 | 117128 | 117370 |
| <b>4850</b>             | 117613 | 117855 | 118098 | 118341 | 118585 | 118828 | 119072 | 119316 | 119561 | 119805 |
| <b>4900</b>             | 120050 | 120295 | 120541 | 120786 | 121032 | 121278 | 121525 | 121771 | 122018 | 122265 |
| <b>4950</b>             | 122513 | 122760 | 123008 | 123256 | 123505 | 123753 | 124002 | 124251 | 124501 | 124750 |

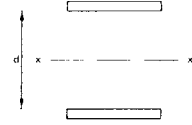
Second moments are tabulated in  $\text{cm}^4$  and are for unit areas of  $1 \text{ cm}^2$  each.

| GEOMETRICAL PROPERTIES OF PLANE SECTIONS  |                        |   |   |  |
|---|------------------------|---|---|--|
| Section                                   | Area                   | Position of Centroid                            | Moments of Inertia  | Section Moduli   |
| <b>TRIANGLE</b><br>                       | $A = \frac{bh}{2}$     | $e_x = \frac{h}{3}$                             | $I_{XX} = \frac{bh^3}{36}$<br>$I_{YY} = \frac{hb^3}{48}$<br>$I_{aa} = \frac{bh^3}{4}$<br>$I_{bb} = \frac{bh^3}{12}$ | $Z_{XX}$<br>base = $\frac{bh^2}{12}$<br>apex = $\frac{bh^2}{24}$<br>$Z_{YY} = \frac{bh^2}{24}$ |
| <b>RECTANGLE</b><br>                      | $A = bd$               | $e_x = \frac{h}{2}$                             | $I_{XX} = \frac{bd^3}{12}$<br>$I_{YY} = \frac{db^3}{12}$<br>$I_{bb} = \frac{bd^3}{3}$                               | $Z_{XX} = \frac{bd^2}{6}$<br>$Z_{YY} = \frac{db^2}{6}$   |
| <b>RECTANGLE</b><br>axis on diagonal<br>  | $A = bd$               | $e_x = \frac{bd}{\sqrt{b^2+d^2}}$               | $I_{XX} = \frac{b^3d^3}{6(b^2+d^2)}$  | $Z_{XX} = \frac{b^2d^2}{6\sqrt{b^2+d^2}}$  |
| <b>RECTANGLE</b><br>axis through C.G.<br> | $A = bd$               | $e_x = \frac{b \sin \theta + d \cos \theta}{2}$ | $I_{XX} = \frac{bd(b^2 \sin^2 \theta + d^2 \cos^2 \theta)}{12}$   | $Z_{XX} = \frac{bd(b^2 \sin^2 \theta + d^2 \cos^2 \theta)}{6(b \sin \theta + d \cos \theta)}$  |
| <b>SQUARE</b><br>                         | $A = s^2$              | $e_x = \frac{s}{2}$<br>$e_y = \frac{s}{2}$      | $I_{XX} = I_{YY} = \frac{s^4}{12}$<br>$I_{bb} = \frac{s^4}{3}$<br>$I_{VV} = \frac{s^4}{12}$                         | $Z_{XX} = Z_{YY} = \frac{s^3}{6}$<br>$Z_{VV} = \frac{s^3}{6\sqrt{2}}$                          |
| <b>TRAPEZIUM</b><br>                      | $A = \frac{d(a+b)}{2}$ | $e_x = \frac{d(2a+b)}{3(a+b)}$                  | $I_{XX} = \frac{d^3(a^2+4ab+b^2)}{36(a+b)}$<br>$I_{YY} = \frac{d(a^3+a^2b+ab^2+b^3)}{48}$                           | $Z_{XX} = \frac{I_{XX}}{d-e_x}$<br>(two values)<br>$Z_{YY} = \frac{2I_{YY}}{b}$                |
| <b>DIAMOND</b><br>                        | $A = \frac{bd}{2}$     | $e_x = \frac{d}{2}$                             | $I_{XX} = \frac{bd^3}{48}$<br>$I_{YY} = \frac{db^3}{48}$  | $Z_{XX} = \frac{bd^2}{24}$<br>$Z_{YY} = \frac{db^2}{24}$                                       |
| <b>HEXAGON</b><br>                        | $A = 0.866d^2$         | $e_x = 0.866d = d/2$                            | $I_{XX} = I_{YY} = I_{VV} = 0.061d^4$   | $Z_{XX} = 0.1203d^3$<br>$Z_{YY} = Z_{VV} = 0.1042d^3$  |

| GEOMETRICAL PROPERTIES OF PLANE SECTIONS |         |  |  |   |  |
|--|---------|--|--|---|--|
|  | Section | Area   | Position of Centroid   | Moments of Inertia  | Section Moduli   |
| OCTAGON                                  |         | $A = 0.8284d^2$<br>$s = 0.4142d$   | $e_x = \frac{d}{2}$<br>$e_y = 0.541d$  | $I_{XX} = I_{YY} = I_{YY}$<br>$= 0.0547d^4$   | $Z_{XX} = Z_{YY}$<br>$= 0.1095d^3$<br>$Z_{YY} = 0.1011d^3$   |
| POLYGON                                  |         | $A = \frac{ns^2 \cot \theta}{4}$<br>$A = nr^2 \tan \theta$<br>$A = \frac{nR^2 \sin 2\theta}{2}$<br><i>Regular figure</i> | $e = r$ or $R$<br>depending on the axis and value of $n$                               | $I_1 = I_2$<br>$= \frac{A(6R^2 - s^2)}{24}$<br>$= \frac{A(12r^2 + s^2)}{48}$  | $Z = \frac{I}{e}$  |
| CIRCLE                                   |         | $A = \pi r^2$<br>$A = 0.7854d^2$   | $e = r = \frac{d}{2}$  | $I = \frac{\pi d^4}{64}$<br>$I = 0.7854r^4$   | $Z = \frac{\pi d^3}{32}$<br>$Z = 0.7854r^3$  |
| SEMI-CIRCLE                              |         | $A = 1.5708r^2$  | $e_x = 0.424r$   | $I_{XX} = 0.1098r^4$<br>$I_{YY} = 0.3927r^4$  | $Z_{XX}$<br>base = $0.2587r^3$<br>crown = $0.1907r^3$<br>$Z_{YY} = 0.3927r^3$                              |
| SEGMENT                                  |         | $A = \frac{r^2(\pi\theta - \sin\theta)}{2(180 - \theta)}$  | $e_o = \frac{c^3}{12A}$<br>$e_x = e_o - r \cos \frac{\theta}{2}$                       | $I_{XX} = \frac{r^4(\pi\theta - \sin 2\theta)}{16(90 - \theta)}$<br>$\frac{20r^4(1 - \cos \theta)^3}{\pi\theta - 180 \sin \theta}$<br>$I_{YY} = \frac{r^4}{48}(\frac{\pi\theta}{30} - \theta \sin \theta + \sin 2\theta)$ | $Z_{XX}$<br>base = $I_{XX}/e_x$<br>crown = $\frac{I_{XX}}{b - e_x}$<br>$Z_{YY} = \frac{2I_{YY}}{c}$        |
| SECTOR                                   |         | $A = \frac{\theta}{360} \pi r^2$   | $e_x = \frac{2}{3} r \frac{c}{r}$<br>$e_y = \frac{r^2 c}{3A}$                          | $I_{XX} = I_o - \frac{360}{\theta} \sin^2 \frac{\theta}{2} \frac{4r^4}{5}$<br>$I_{YY} = \frac{r^4}{8}(\frac{\pi\theta}{180} - \sin \theta)$<br>$I_o = \frac{r^4}{8}(\frac{\pi\theta}{180} \sin \theta)$                   | $Z_{XX}$<br>centre = $I_{XX}/e_x$<br>crown = $\frac{I_{XX}}{r - e_x}$<br>$Z_{YY} = \frac{2I_{YY}}{c}$      |
| QUADRANT                                 |         | $A = \frac{\pi r^2}{4}$  | $e_x = 0.424r$<br>$e_y = 0.6r$<br>$e_u = 0.707r$                                       | $I_{XX} = I_{YY} = 0.0549r^4$<br>$I_{bb} = 0.1963r^4$<br>$I_{UU} = 0.0714r^4$<br>$I_{VV} = 0.0384r^4$   | <i>Minimum Values</i><br>$Z_{XX} = Z_{YY}$<br>$= 0.0953r^3$<br>$Z_{UU} = 0.1009r^3$<br>$Z_{VV} = 0.064r^3$ |
| COMPLEMENT                               |         | $A = 0.2146r^2$  | $e_x = 0.777r$<br>$e_y = 1.098r$<br>$e_u = 0.707r$<br>$e_o = 0.316r$<br>$e_b = 0.391r$ | $I_{XX} = I_{YY} = 0.0076r^4$<br>$I_{UU} = 0.012r^4$<br>$I_{VV} = 0.0031r^4$  | <i>Minimum Values</i><br>$Z_{XX} = Z_{YY}$<br>$= 0.0097r^3$<br>$Z_{UU} = 0.017r^3$<br>$Z_{VV} = 0.0079r^3$ |

| GEOMETRICAL PROPERTIES OF PLANE SECTIONS  |                        |   |  |  |
|---|------------------------|---|--|--|
| Section   | Area                   | Position of Centroid                          | Moments of Inertia   | Section Moduli   |
| <b>ELLIPSE</b><br>         | $A = \pi ab$           | $e_x = a$<br>$e_y = b$                        | $I_{XX} = 0.7854be^3$<br>$I_{YY} = 0.7854ab^3$   | $Z_{XX} = 0.7854bd^2$<br>$Z_{YY} = 0.7854ab^2$   |
| <b>SEMI-ELLIPSE</b><br>    | $A = \frac{\pi ab}{2}$ | $e_x = 0.424a$<br>$e_y = b$                   | $I_{XX} = 0.1098ba^3$<br>$I_{YY} = 0.3927ab^3$<br>$I_{base} = 0.3927ba^3$                                    | $Z_{XX} - base = 0.2587ba^2$<br>$Z_{XX} - crown = 0.1907ba^2$<br>$Z_{YY} = 0.3927ab^2$   |
| <b>1/4 ELLIPSE</b><br>     | $A = 0.7854ab$         | $e_x = 0.424a$<br>$e_y = 0.424b$              | $I_{XX} = 0.0549ba^3$<br>$I_{YY} = 0.0549ab^3$<br>$I_{b_1, a_1} = 0.1963ba^3$<br>$I_{b_1, c_1} = 0.1963ab^3$ | $Z_{XX} - base = 0.1293ba^2$<br>$Z_{XX} - crown = 0.0953ba^2$<br>$Z_{YY} - base = 0.1293ab^2$<br>$Z_{YY} - crown = 0.0953ab^2$ |
| <b>COMPLEMENT</b><br>     | $A = 0.2146ab$         | $e_x = 0.777a$<br>$e_y = 0.777b$              | $I_{XX} = 0.0076ba^3$<br>$I_{YY} = 0.0076ab^3$   | $Z_{XX} - base = 0.0338ba^2$<br>$Z_{XX} - apex = 0.0097ba^2$<br>$Z_{YY} - base = 0.0338ab^2$<br>$Z_{YY} - apex = 0.0097ab^2$   |
| <b>FULL PARABOLA</b><br> | $A = \frac{4ab}{3}$    | $e_x = \frac{2a}{5}$<br>$e_y = b$             | $I_{XX} = 0.0914ba^3$<br>$I_{YY} = 0.2666ab^3$<br>$I_{base} = 0.3048ba^3$                                    | $Z_{XX} - base = 0.2286ba^2$<br>$Z_{XX} - crown = 0.1524ba^2$<br>$Z_{YY} = 0.2666ab^2$   |
| <b>SEMI-PARABOLA</b><br> | $A = \frac{2ab}{3}$    | $e_x = \frac{2a}{5}$<br>$e_y = \frac{3b}{8}$  | $I_{XX} = 0.0457ba^3$<br>$I_{YY} = 0.0396ab^3$<br>$I_{b_1, a_1} = 0.1524ba^3$<br>$I_{b_1, c_1} = 0.1333ab^3$ | $Z_{XX} - base = 0.1143ba^2$<br>$Z_{XX} - crown = 0.076ba^2$<br>$Z_{YY} - base = 0.1055ab^2$<br>$Z_{YY} - crown = 0.0633ab^2$  |
| <b>COMPLEMENT</b><br>    | $A = \frac{ab}{3}$     | $e_x = \frac{7a}{10}$<br>$e_y = \frac{3b}{4}$ | $I_{XX} = 0.0176ba^3$<br>$I_{YY} = 0.0125ab^3$<br>$I_{a_1, b_1} = 0.181ba^3$<br>$I_{b_1, c_1} = 0.2ab^3$     | $Z_{XX} - base = 0.0587ba^2$<br>$Z_{XX} - apex = 0.0252ba^2$<br>$Z_{YY} - base = 0.05ab^2$<br>$Z_{YY} - apex = 0.0167ab^2$     |
| <b>FILLET</b><br>        | $A = \frac{s^2}{6}$    | $e_u = e_v = \frac{4s}{5}$                    | $I_{UU} = I_{VV} = 0.00524s^4$<br>$I_{ob} = 0.1119s^4$   | $Z_{UU} = Z_{VV}$<br>$Z_{base} = 0.0262s^3$<br>$Z_{apex} = 0.0066s^3$  |

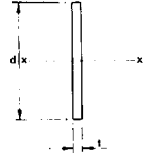
PLASTIC MODULUS OF TWO FLANGES



| Dist d<br>mm | Plastic Modulus $S_{xx}(\text{cm}^2)$ For Thickness $t(\text{mm})$ |       |      |      |      |      |      |      |      |      |      |      |      |
|--------------|--|-------|------|------|------|------|------|------|------|------|------|------|------|
|              | 15   | 20    | 25   | 30   | 35   | 40   | 45   | 50   | 55   | 60   | 65   | 70   | 75   |
| 1000         | 15.2   | 20.4  | 25.6 | 30.9 | 36.2 | 41.6 | 47.0 | 52.5 | 58.0 | 63.6 | 69.2 | 74.9 | 80.6 |
| 1100         | 16.7   | 22.4  | 28.1 | 33.9 | 39.7 | 45.6 | 51.5 | 57.5 | 63.5 | 69.6 | 75.7 | 81.9 | 88.1 |
| 1200         | 18.2   | 24.4  | 30.6 | 36.9 | 43.2 | 49.6 | 56.0 | 62.5 | 69.0 | 75.6 | 82.2 | 88.9 | 95.6 |
| 1300         | 19.7   | 26.4  | 33.1 | 39.9 | 46.7 | 53.6 | 60.5 | 67.5 | 74.5 | 81.5 | 88.7 | 95.9 | 103  |
| 1400         | 21.2   | 28.4  | 35.6 | 42.9 | 50.2 | 57.6 | 65.0 | 72.5 | 80.0 | 87.6 | 95.2 | 103  | 111  |
| 1500         | 22.7   | 30.4  | 38.1 | 45.9 | 53.7 | 61.6 | 69.5 | 77.5 | 85.5 | 93.6 | 102  | 110  | 118  |
| 1600         | 24.2   | 32.4  | 40.6 | 48.9 | 57.2 | 65.6 | 74.0 | 82.5 | 91.0 | 99.6 | 108  | 117  | 126  |
| 1700         | 25.7   | 34.4  | 43.1 | 51.9 | 60.7 | 69.6 | 78.5 | 87.5 | 96.5 | 106  | 115  | 124  | 133  |
| 1800         | 27.2   | 36.4  | 45.6 | 54.9 | 64.2 | 73.6 | 83.0 | 92.5 | 102  | 112  | 121  | 131  | 141  |
| 1900         | 28.7   | 38.4  | 48.1 | 57.9 | 67.7 | 77.6 | 87.5 | 97.5 | 108  | 118  | 128  | 138  | 148  |
| 2000         | 30.2   | 40.4  | 50.6 | 60.9 | 71.2 | 81.6 | 92.0 | 102  | 113  | 124  | 134  | 145  | 156  |
| 2100         | 31.7   | 42.4  | 53.1 | 63.9 | 74.7 | 85.6 | 96.5 | 107  | 119  | 130  | 141  | 152  | 163  |
| 2200         | 33.2   | 44.4  | 55.6 | 66.9 | 78.2 | 89.6 | 101  | 112  | 124  | 136  | 147  | 159  | 171  |
| 2300         | 34.7   | 46.4  | 58.1 | 69.9 | 81.7 | 93.6 | 106  | 117  | 130  | 142  | 154  | 166  | 178  |
| 2400         | 36.2   | 48.4  | 60.6 | 72.9 | 85.2 | 97.6 | 110  | 122  | 135  | 148  | 160  | 173  | 186  |
| 2500         | 37.7   | 50.4  | 63.1 | 75.9 | 88.7 | 102  | 115  | 127  | 141  | 154  | 167  | 180  | 193  |
| 2600         | 39.2   | 52.4  | 65.6 | 78.9 | 92.2 | 106  | 119  | 132  | 146  | 160  | 173  | 187  | 201  |
| 2700         | 40.7   | 54.4  | 68.1 | 81.9 | 95.7 | 110  | 124  | 137  | 152  | 166  | 180  | 194  | 208  |
| 2800         | 42.2   | 56.4  | 70.6 | 84.9 | 99.2 | 114  | 128  | 142  | 157  | 172  | 186  | 201  | 216  |
| 2900         | 43.7   | 58.4  | 73.1 | 87.9 | 103  | 118  | 133  | 147  | 163  | 178  | 193  | 208  | 223  |
| 3000         | 45.2   | 60.4  | 75.6 | 90.9 | 106  | 122  | 137  | 152  | 168  | 184  | 199  | 215  | 231  |
| 3100         | 46.7   | 62.4  | 78.1 | 93.9 | 110  | 126  | 142  | 157  | 174  | 190  | 206  | 222  | 238  |
| 3200         | 48.2   | 64.4  | 80.6 | 96.9 | 113  | 130  | 146  | 162  | 179  | 196  | 212  | 229  | 246  |
| 3300         | 49.7   | 66.4  | 83.1 | 99.9 | 117  | 134  | 151  | 167  | 185  | 202  | 219  | 236  | 253  |
| 3400         | 51.2   | 68.4  | 85.6 | 103  | 120  | 138  | 155  | 172  | 190  | 208  | 225  | 243  | 261  |
| 3500         | 52.7   | 70.4  | 88.1 | 106  | 124  | 142  | 160  | 177  | 196  | 214  | 232  | 250  | 268  |
| 3600         | 54.2   | 72.4  | 90.6 | 109  | 127  | 146  | 164  | 182  | 201  | 220  | 238  | 257  | 276  |
| 3700         | 55.7   | 74.4  | 93.1 | 112  | 131  | 150  | 169  | 187  | 207  | 226  | 245  | 264  | 283  |
| 3800         | 57.2   | 76.4  | 95.6 | 115  | 134  | 154  | 173  | 192  | 212  | 232  | 251  | 271  | 291  |
| 3900         | 58.7   | 78.4  | 98.1 | 118  | 138  | 158  | 178  | 197  | 218  | 238  | 258  | 278  | 298  |
| 4000         | 60.2   | 80.4  | 101  | 121  | 141  | 162  | 182  | 202  | 223  | 244  | 264  | 285  | 306  |
| 4100         | 61.7   | 82.4  | 103  | 124  | 145  | 166  | 187  | 207  | 229  | 250  | 271  | 292  | 313  |
| 4200         | 63.2   | 84.4  | 106  | 127  | 148  | 170  | 191  | 212  | 234  | 256  | 277  | 299  | 321  |
| 4300         | 64.7   | 86.4  | 108  | 130  | 152  | 174  | 196  | 217  | 240  | 262  | 284  | 306  | 328  |
| 4400         | 66.2   | 88.4  | 111  | 133  | 155  | 178  | 200  | 222  | 245  | 268  | 290  | 313  | 336  |
| 4500         | 67.7   | 90.4  | 113  | 136  | 159  | 182  | 205  | 227  | 251  | 274  | 297  | 320  | 343  |
| 4600         | 69.2   | 92.4  | 116  | 139  | 162  | 186  | 209  | 232  | 256  | 280  | 303  | 327  | 351  |
| 4700         | 70.7   | 94.4  | 118  | 142  | 166  | 190  | 214  | 237  | 262  | 286  | 310  | 334  | 358  |
| 4800         | 72.2   | 96.4  | 121  | 145  | 169  | 194  | 218  | 242  | 267  | 292  | 316  | 341  | 366  |
| 4900         | 73.7   | 98.4  | 123  | 148  | 173  | 198  | 223  | 247  | 273  | 298  | 323  | 348  | 373  |
| 5000         | 75.2   | 100.0 | 126  | 151  | 176  | 202  | 227  | 252  | 278  | 304  | 329  | 355  | 381  |

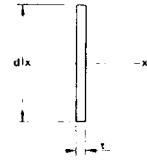


**PLASTIC MODULUS OF RECTANGLES**



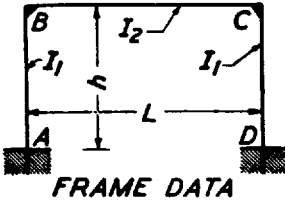
| Depth<br>d<br>mm | Plastic Modulus $S_{xx}(\text{cm}^3)$ For Thickness t(mm) |      |      |      |      |       |      |      |      |      |
|------------------|---|------|------|------|------|-------|------|------|------|------|
|                  | 5   | 6    | 7    | 8    | 9    | 10    | 12.5 | 15   | 20   | 25   |
| 25               | 0.78  | 0.93 | 1.09 | 1.25 | 1.41 | 1.56  | 1.95 | 2.34 | 3.13 | 3.91 |
| 50               | 3.13  | 3.75 | 4.37 | 5.00 | 5.62 | 6.25  | 7.81 | 9.37 | 12.5 | 15.6 |
| 75               | 7.03  | 8.44 | 9.84 | 11.3 | 12.7 | 14.1  | 17.6 | 21.1 | 28.1 | 35.2 |
| 100              | 12.5  | 15.0 | 17.5 | 20.0 | 22.5 | 25.0  | 31.2 | 37.5 | 50.0 | 62.5 |
| 125              | 19.5  | 23.4 | 27.3 | 31.2 | 35.2 | 39.1  | 48.8 | 58.6 | 78.1 | 97.7 |
| 150              | 28.1  | 33.8 | 39.4 | 45.0 | 50.6 | 56.2  | 70.3 | 84.4 | 112  | 141  |
| 175              | 38.3  | 45.9 | 53.6 | 61.2 | 68.9 | 76.6  | 95.7 | 115  | 153  | 191  |
| 200              | 50.0  | 60.0 | 70.0 | 80.0 | 90.0 | 100.0 | 125  | 150  | 200  | 250  |
| 225              | 63.3  | 75.9 | 88.6 | 101  | 114  | 127   | 158  | 190  | 253  | 316  |
| 250              | 78.1  | 93.7 | 109  | 125  | 141  | 156   | 195  | 234  | 312  | 391  |
| 275              | 94.5  | 113  | 132  | 151  | 170  | 189   | 236  | 284  | 378  | 473  |
| 300              | 112   | 135  | 158  | 180  | 203  | 225   | 281  | 338  | 450  | 563  |
| 325              | 132   | 158  | 185  | 211  | 238  | 264   | 330  | 396  | 528  | 650  |
| 350              | 153   | 184  | 214  | 245  | 276  | 306   | 383  | 459  | 613  | 766  |
| 375              | 176   | 211  | 246  | 281  | 316  | 352   | 439  | 527  | 703  | 879  |
| 400              | 200   | 240  | 280  | 320  | 360  | 400   | 500  | 600  | 800  | 1000 |
| 425              | 226   | 271  | 316  | 361  | 406  | 452   | 564  | 677  | 903  | 1130 |
| 450              | 253   | 304  | 354  | 405  | 456  | 506   | 633  | 759  | 1010 | 1270 |
| 475              | 282   | 338  | 395  | 451  | 508  | 564   | 705  | 846  | 1130 | 1410 |
| 500              | 312   | 375  | 437  | 500  | 562  | 625   | 781  | 937  | 1250 | 1560 |
| 525              | 345   | 413  | 482  | 551  | 620  | 689   | 861  | 1030 | 1380 | 1720 |
| 550              | 378   | 454  | 529  | 605  | 681  | 756   | 945  | 1130 | 1510 | 1890 |
| 575              | 413   | 496  | 579  | 661  | 744  | 827   | 1030 | 1240 | 1650 | 2070 |
| 600              | 450   | 540  | 630  | 720  | 810  | 900   | 1130 | 1350 | 1800 | 2250 |
| 625              | 488   | 586  | 684  | 781  | 879  | 977   | 1220 | 1460 | 1950 | 2440 |
| 650              | 528   | 634  | 739  | 845  | 951  | 1060  | 1320 | 1580 | 2110 | 2640 |
| 675              | 570   | 683  | 797  | 911  | 1030 | 1140  | 1420 | 1710 | 2280 | 2850 |
| 700              | 613   | 735  | 858  | 980  | 1100 | 1230  | 1530 | 1840 | 2450 | 3060 |
| 725              | 657   | 788  | 920  | 1050 | 1180 | 1310  | 1640 | 1970 | 2630 | 3290 |
| 750              | 703   | 844  | 984  | 1120 | 1270 | 1410  | 1760 | 2110 | 2810 | 3520 |
| 775              | 751   | 901  | 1050 | 1200 | 1350 | 1500  | 1880 | 2250 | 3000 | 3750 |
| 800              | 800   | 960  | 1120 | 1280 | 1440 | 1600  | 2000 | 2400 | 3200 | 4000 |
| 825              | 851   | 1020 | 1190 | 1360 | 1530 | 1700  | 2130 | 2550 | 3400 | 4250 |
| 850              | 903   | 1080 | 1260 | 1440 | 1630 | 1810  | 2260 | 2710 | 3610 | 4520 |
| 875              | 957   | 1150 | 1340 | 1530 | 1720 | 1910  | 2390 | 2870 | 3830 | 4790 |
| 900              | 1010  | 1210 | 1420 | 1620 | 1820 | 2020  | 2530 | 3040 | 4050 | 5060 |

PLASTIC MODULUS OF RECTANGLES



| Depth<br>d<br>mm | Plastic Modulus $S_{xx}(\text{cm}^3)$ For Thickness $t(\text{mm})$ |       |       |       |       |       |       |       |        |        |
|------------------|--|-------|-------|-------|-------|-------|-------|-------|--------|--------|
|                  | 5  | 6     | 7     | 8     | 9     | 10    | 12.5  | 15    | 20     | 25     |
| 1000             | 1250   | 1500  | 1750  | 2000  | 2250  | 2500  | 3120  | 3750  | 5000   | 6250   |
| 1100             | 1510   | 1810  | 2120  | 2420  | 2720  | 3020  | 3780  | 4540  | 6050   | 7560   |
| 1200             | 1800   | 2160  | 2520  | 2880  | 3240  | 3600  | 4500  | 5400  | 7200   | 9000   |
| 1300             | 2110   | 2530  | 2960  | 3380  | 3800  | 4220  | 5280  | 6340  | 8490   | 10600  |
| 1400             | 2450   | 2940  | 3430  | 3920  | 4410  | 4900  | 6130  | 7350  | 9800   | 12300  |
| 1500             | 2810   | 3370  | 3940  | 4500  | 5060  | 5620  | 7030  | 8440  | 11200  | 14100  |
| 1600             | 3200   | 3840  | 4480  | 5120  | 5760  | 6400  | 8000  | 9600  | 12800  | 16000  |
| 1700             | 3610   | 4330  | 5060  | 5780  | 6500  | 7220  | 9030  | 10800 | 14400  | 18100  |
| 1800             | 4050   | 4860  | 5670  | 6480  | 7290  | 8100  | 10100 | 12100 | 16200  | 20200  |
| 1900             | 4510   | 5410  | 6320  | 7220  | 8120  | 9020  | 11300 | 13500 | 18000  | 22600  |
| 2000             | 5000   | 6000  | 7000  | 8000  | 9000  | 10000 | 12500 | 15000 | 20000  | 25000  |
| 2100             | 5510   | 6620  | 7720  | 8820  | 9920  | 11000 | 13800 | 16500 | 22100  | 27600  |
| 2200             | 6050   | 7260  | 8470  | 9680  | 10900 | 12100 | 15100 | 18100 | 24200  | 30200  |
| 2300             | 6610   | 7930  | 9260  | 10600 | 11900 | 13200 | 16500 | 19800 | 26500  | 33100  |
| 2400             | 7200   | 8640  | 10100 | 11500 | 13000 | 14400 | 18000 | 21600 | 28800  | 36000  |
| 2500             | 7810   | 9370  | 10900 | 12500 | 14100 | 15600 | 19500 | 23400 | 31200  | 39100  |
| 2600             | 8450   | 10100 | 11800 | 13500 | 15200 | 16900 | 21100 | 25400 | 33800  | 42200  |
| 2700             | 9110   | 10900 | 12800 | 14600 | 16400 | 18200 | 22800 | 27300 | 36400  | 45600  |
| 2800             | 9800   | 11800 | 13700 | 15700 | 17600 | 19600 | 24500 | 29400 | 39200  | 49000  |
| 2900             | 10500  | 12600 | 14700 | 16800 | 18900 | 21000 | 26300 | 31500 | 42000  | 52600  |
| 3000             | 11200  | 13500 | 15700 | 18000 | 20200 | 22500 | 28100 | 33700 | 45000  | 56200  |
| 3100             | 12000  | 14400 | 16800 | 19200 | 21600 | 24000 | 30000 | 36000 | 48000  | 60100  |
| 3200             | 12800  | 15400 | 17900 | 20500 | 23000 | 25600 | 32000 | 38400 | 51200  | 64000  |
| 3300             | 13600  | 16300 | 19100 | 21800 | 24500 | 27200 | 34000 | 40800 | 54400  | 68100  |
| 3400             | 14400  | 17300 | 20200 | 23100 | 26000 | 28900 | 36100 | 43300 | 57800  | 72200  |
| 3500             | 15300  | 18400 | 21400 | 24500 | 27600 | 30600 | 38300 | 45900 | 61200  | 76600  |
| 3600             | 16200  | 19400 | 22700 | 25900 | 29200 | 32400 | 40500 | 48600 | 64800  | 81000  |
| 3700             | 17100  | 20500 | 24000 | 27400 | 30800 | 34200 | 42800 | 51300 | 68400  | 85600  |
| 3800             | 18000  | 21700 | 25300 | 28900 | 32500 | 36100 | 45100 | 54100 | 72200  | 90200  |
| 3900             | 19000  | 22800 | 26600 | 30400 | 34200 | 38000 | 47500 | 57000 | 76000  | 95100  |
| 4000             | 20000  | 24000 | 28000 | 32000 | 36000 | 40000 | 50000 | 60000 | 80000  | 100000 |
| 4100             | 21000  | 25200 | 29400 | 33600 | 37800 | 42000 | 52500 | 63000 | 84000  | 105000 |
| 4200             | 22100  | 26500 | 30900 | 35300 | 39700 | 44100 | 55100 | 66200 | 88200  | 110000 |
| 4300             | 23100  | 27700 | 32400 | 37000 | 41600 | 46200 | 57800 | 69300 | 92400  | 116000 |
| 4400             | 24200  | 29000 | 33900 | 38700 | 43600 | 48400 | 60500 | 72600 | 96800  | 121000 |
| 4500             | 25300  | 30400 | 35400 | 40500 | 45600 | 50600 | 63300 | 75900 | 101000 | 127000 |
| 4600             | 26500  | 31700 | 37000 | 42300 | 47600 | 52900 | 66100 | 79300 | 106000 | 132000 |
| 4700             | 27600  | 33100 | 38700 | 44200 | 49700 | 55200 | 69000 | 82900 | 110000 | 138000 |
| 4800             | 28800  | 34600 | 40300 | 46100 | 51800 | 57600 | 72000 | 86400 | 115000 | 144000 |
| 4900             | 30000  | 36000 | 42000 | 48000 | 54000 | 60000 | 75000 | 90000 | 120000 | 150000 |
| 5000             | 31200  | 37500 | 43700 | 50000 | 56200 | 62500 | 78100 | 93700 | 125000 | 156000 |

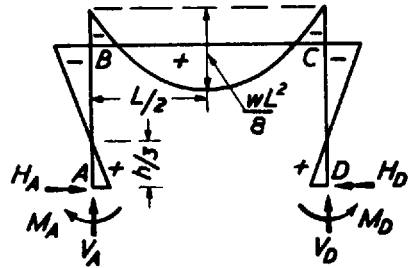
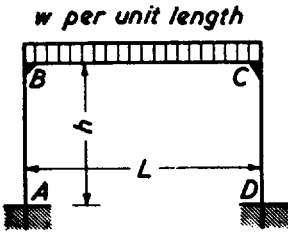
### Frame I



Coefficients:

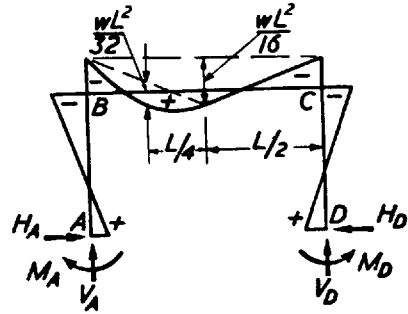
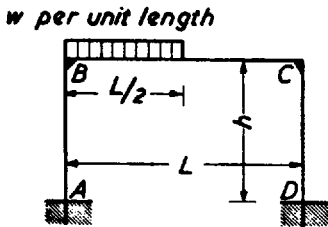
$$k = \frac{I_2}{I_1} \cdot \frac{h}{L}$$

$$N_1 = k + 2 \quad N_2 = 6k + 1$$



$$M_A = M_D = \frac{wL^2}{12N_1} \quad M_B = M_C = -\frac{wL^2}{6N_1} = -2M_A$$

$$M_{\max} = \frac{wL^2}{8} + M_B \quad V_A = V_D = \frac{wL}{2} \quad H_A = H_D = \frac{3M_A}{h}$$

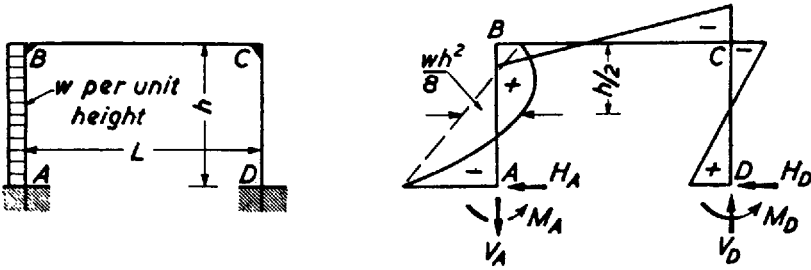


$$M_A = \frac{wL^2}{8} \left[ \frac{1}{3N_1} - \frac{1}{8N_2} \right] \quad M_B = -\frac{wL^2}{8} \left[ \frac{2}{3N_1} + \frac{1}{8N_2} \right]$$

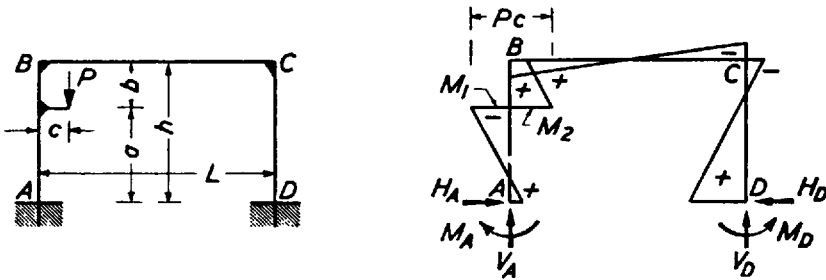
$$M_D = \frac{wL^2}{8} \left[ \frac{1}{3N_1} + \frac{1}{8N_2} \right] \quad M_C = -\frac{wL^2}{8} \left[ \frac{2}{3N_1} - \frac{1}{8N_2} \right]$$

$$V_D = \frac{wL}{8} \left[ 1 - \frac{1}{4N_2} \right] \quad V_A = \frac{wL}{2} - V_D \quad H_A = H_D = \frac{wL^2}{8hN_1}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

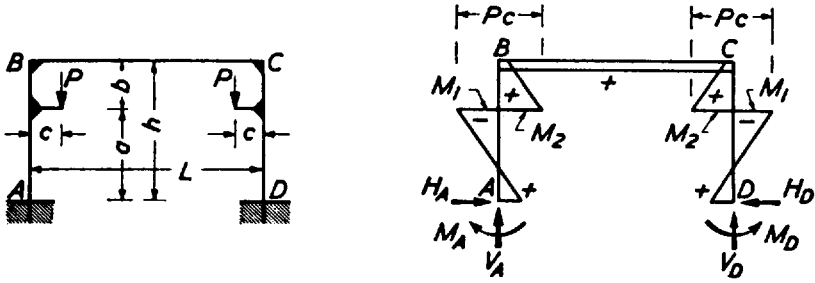


$$\begin{aligned}
 M_A &= \frac{wh^2}{4} \left[ -\frac{k+3}{6N_1} - \frac{4k+1}{N_2} \right] & M_B &= \frac{wh^2}{4} \left[ -\frac{k}{6N_1} + \frac{2k}{N_2} \right] \\
 M_D &= \frac{wh^2}{4} \left[ -\frac{k+3}{6N_1} + \frac{4k+1}{N_2} \right] & M_C &= \frac{wh^2}{4} \left[ -\frac{k}{6N_1} - \frac{2k}{N_2} \right] \\
 H_D &= \frac{wh(2k+3)}{8N_1} & H_A &= -(wh - H_D) & V_A &= -V_D = -\frac{wh^2k}{LN_2}
 \end{aligned}$$



$$\begin{aligned}
 \text{Constants: } a_1 &= \frac{a}{h} & b_1 &= \frac{b}{h} \\
 X_1 &= \frac{Pc}{2N_1} [1 + 2b_1k - 3b_1^2(k+1)] & X_2 &= \frac{Pcka_1(3a_1-2)}{2N_1} \\
 X_3 &= \frac{3Pcka_1}{N_2} \\
 M_A &= +X_1 - \left( \frac{Pc}{2} - X_3 \right) & M_B &= +X_2 + X_3 \\
 M_D &= +X_1 + \left( \frac{Pc}{2} - X_3 \right) & M_C &= +X_2 - X_3 \\
 H_A = H_D &= \frac{Pc}{2h} + \frac{X_1 - X_2}{h} & V_D &= \frac{2X_3}{L} & V_A &= P - V_D \\
 M_1 &= M_A - H_A a & M_2 &= M_B + H_D b
 \end{aligned}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



Constants:  $a_1 = \frac{a}{h}$      $b_1 = \frac{b}{h}$

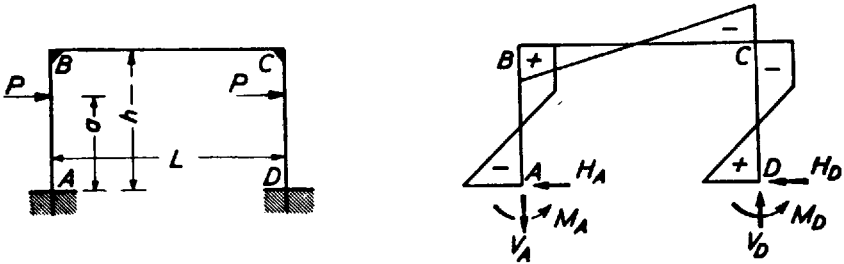
$$X_1 = \frac{Pc}{2N_1} [1 + 2b_1k - 3b_1^2(k+1)] \quad X_2 = \frac{Pcka_1(3a_1 - 2)}{2N_1}$$

$$M_A = M_D = \frac{Pc}{N_1} [1 + 2b_1k - 3b_1^2(k+1)] = 2X_1$$

$$M_B = M_C = \frac{Pcka_1(3a_1 - 2)}{N_1} = 2X_2$$

$$V_A = V_D = P \quad H_A = H_D = \frac{Pc + M_A - M_B}{h}$$

$$M_1 = M_A - H_A a \quad M_2 = M_B + H_D b$$



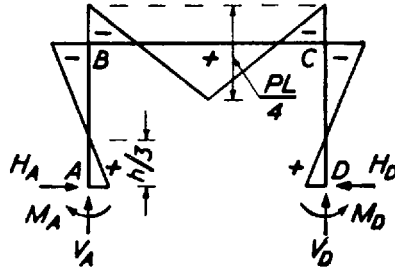
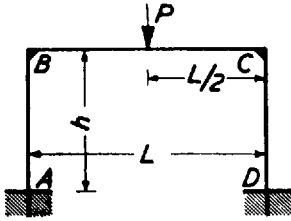
Constants:  $a_1 = \frac{a}{h}$      $X_1 = \frac{3Paa_1k}{N_2}$

$$M_A = -Pa + X_1 \quad M_B = X_1$$

$$M_D = +Pa - X_1 \quad M_C = -X_1$$

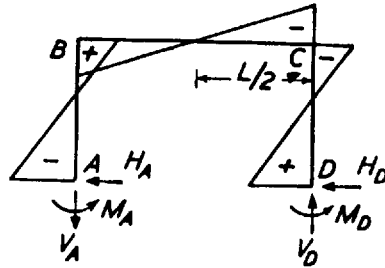
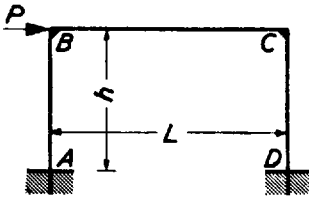
$$V_A = -V_D = -\frac{2X_1}{L} \quad H_A = -H_D = -P$$

*Extract: 'Kleinlogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.*



$$M_A = M_D = +\frac{PL}{8N_1} \quad M_B = M_C = -2M_A$$

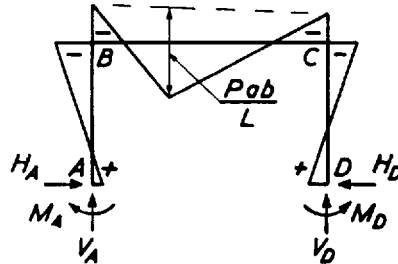
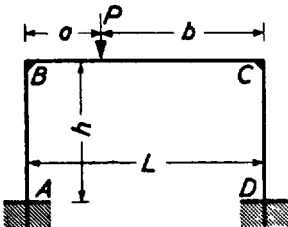
$$V_A = V_D = \frac{P}{2} \quad H_A = H_D = \frac{3M_A}{h}$$



$$M_A = -\frac{Ph}{2} \cdot \frac{3k+1}{N_2} \quad M_B = +\frac{Ph}{2} \cdot \frac{3k}{N_2}$$

$$M_D = +\frac{Ph}{2} \cdot \frac{3k+1}{N_2} \quad M_C = -\frac{Ph}{2} \cdot \frac{3k}{N_2}$$

$$H_A = -H_D = -\frac{P}{2} \quad V_A = -V_D = -\frac{2M_B}{L}$$



Constants:  $a_1 = a/L$      $b_1 = b/L$

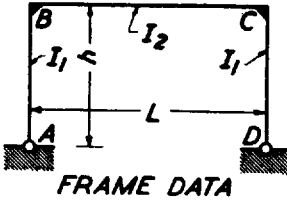
$$M_A = +\frac{Pab}{L} \left[ \frac{1}{2N_1} - \frac{b_1 - a_1}{2N_2} \right] \quad M = -\frac{Pab}{L} \left[ \frac{1}{N_1} + \frac{b_1 - a_1}{2N_2} \right]$$

$$M_D = +\frac{Pab}{L} \left[ \frac{1}{2N_1} + \frac{b_1 - a_1}{2N_2} \right] \quad M_C = -\frac{Pab}{L} \left[ \frac{1}{N_1} - \frac{b_1 - a_1}{2N_2} \right]$$

$$V_A = Pb_1 \left[ 1 + \frac{a_1(b_1 - a_1)}{N_2} \right] \quad V_D = P - V_A \quad H_A = H_D = \frac{3Pab}{2LhN_1}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

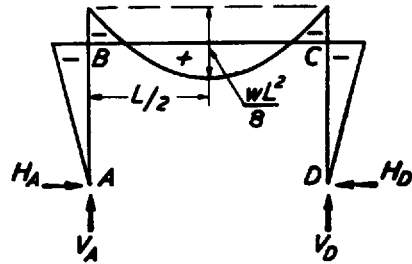
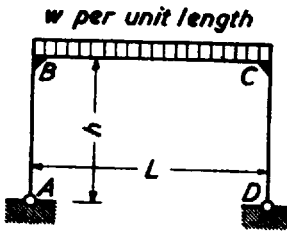
**Frame II**



Coefficients:

$$k = \frac{I_2}{I_1} \cdot \frac{h}{L}$$

$$N = 2k + 3$$

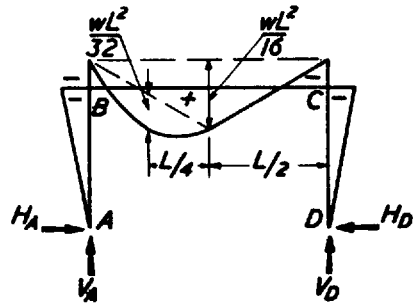
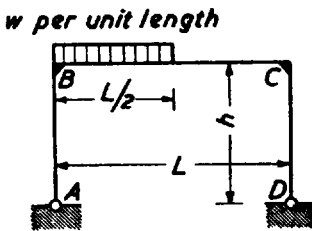


$$M_B = M_C = -\frac{wL^2}{4N}$$

$$M_{\max} = \frac{wL^2}{8} + M_B$$

$$V_A = V_D = \frac{wL}{2}$$

$$H_A = H_D = -\frac{M_B}{h}$$



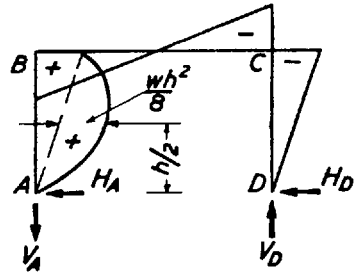
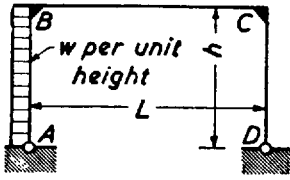
$$M_B = M_C = -\frac{wL^2}{8N}$$

$$V_A = \frac{3wL}{8}$$

$$V_D = \frac{wL}{8}$$

$$H_A = H_D = -\frac{M_B}{h}$$

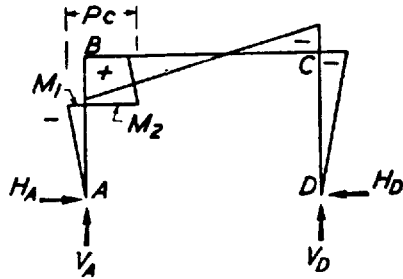
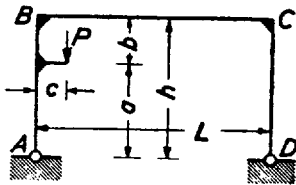
*Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.*



$$M_B = \frac{wh^2}{4} \left[ -\frac{k}{2N} + 1 \right] \quad H_D = -\frac{M_C}{h}$$

$$M_C = \frac{wh^2}{4} \left[ -\frac{k}{2N} - 1 \right] \quad H_A = -(wh - H_D)$$

$$V_A = -V_D = -\frac{wh^2}{2L}$$



Constant:  $a_1 = \frac{a}{h}$

$$M_B = \frac{Pc}{2} \left[ \frac{(3a_1^2 - 1)k}{N} + 1 \right] \quad H_A = H_D = -\frac{M_C}{h}$$

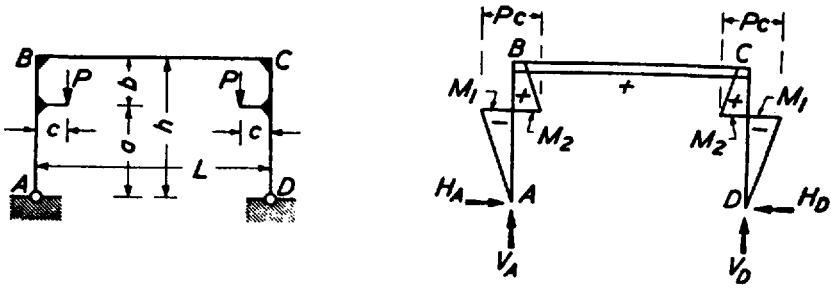
$$M_C = \frac{Pc}{2} \left[ \frac{(3a_1^2 - 1)k}{N} - 1 \right]$$

$$V_D = \frac{Pc}{L} \quad V_A = P - V_D$$

$$M_1 = -H_A a \quad M_2 = Pc - H_A a$$

Extract: 'Kleinlogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



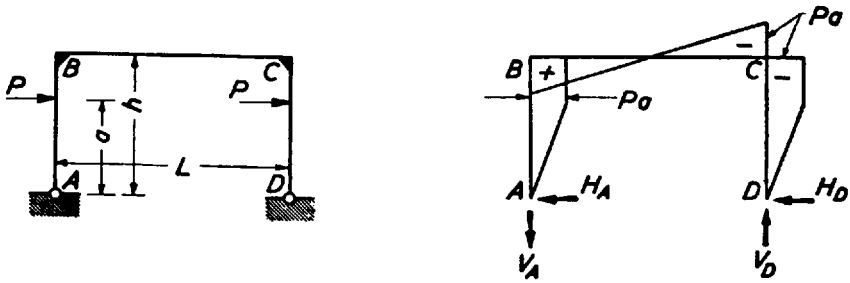


Constant:  $a_1 = \frac{a}{h}$

$$M_B = M_C = \frac{Pc(3a_1^2 - 1)k}{N}$$

$$H_A = H_D = \frac{Pc - M_B}{h} \quad V_A = V_D = P$$

$$M_1 = -H_A a \quad M_2 = Pc - H_A a$$

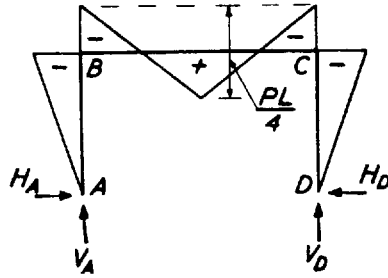
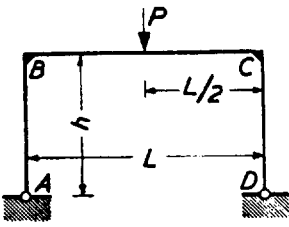


$$M_B = -M_C = Pa \quad H_A = H_D = P$$

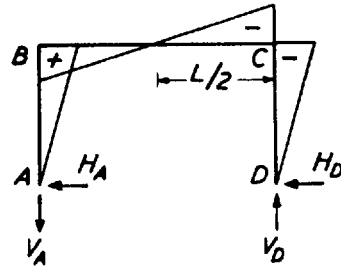
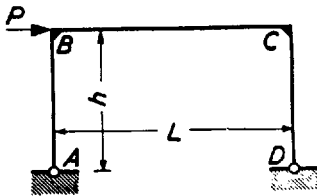
$$V_A = -V_D = -\frac{2Pa}{L}$$

Moment at loads =  $\pm Pa$

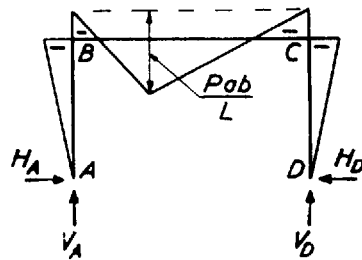
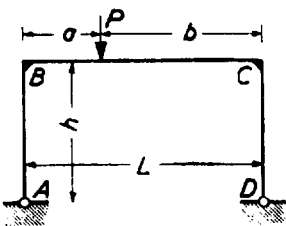
*Extract: 'Kleinlogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.*



$$M_B = M_C = -\frac{3PL}{8N} \quad V_A = V_D = \frac{P}{2} \quad H_A = H_D = -\frac{1M_B}{h}$$



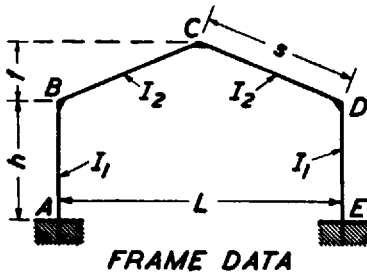
$$M_B = -M_C = +\frac{Ph}{2} \\ V_A = -V_D = -\frac{Ph}{L} \quad H_A = -H_D = -\frac{P}{2}$$



$$M_B = M_C = -\frac{Pab}{L} \cdot \frac{3}{2N} \\ V_A = \frac{Pb}{L} \quad V_D = \frac{Pa}{L} \quad H_A = H_D = -\frac{M_B}{h}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

**Frame III**



Coefficients:

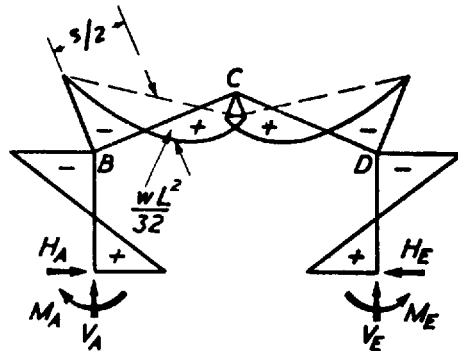
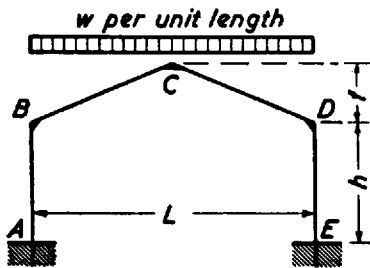
$$k = \frac{I_2}{I_1} \cdot \frac{h}{s} \quad \phi = \frac{f}{h}$$

$$m = 1 + \phi$$

$$B = 3k + 2 \quad C = 1 + 2m$$

$$K_1 = 2(k + 1 + m + m^2) \quad K_2 = 2(k + \phi^2)$$

$$R = \phi C - k \quad N_1 = K_1 K_2 - R^2 \quad N_2 = 3k + B$$



$$M_A = M_E = \frac{wL^2}{16} \cdot \frac{k(8 + 15\phi) + \phi(6 - \phi)}{N_1}$$

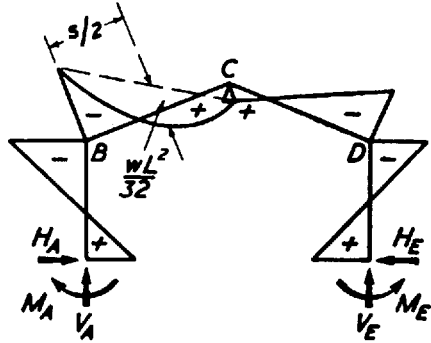
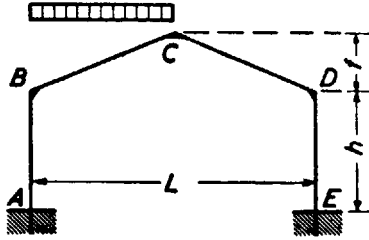
$$M_B = M_D = -\frac{wL^2}{16} \cdot \frac{k(16 + 15\phi) + \phi^2}{N_1}$$

$$M_C = \frac{wL^2}{8} - \phi M_A + m M_B$$

$$V_A = V_E = \frac{wL}{2} \quad H_A = H_E = \frac{M_A - M_B}{h}$$

*Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.*

w per unit length



$$\text{Constants: } *X_1 = \frac{wL^2}{32} \cdot \frac{k(8+15\phi) + \phi(6-\phi)}{N_1}$$

$$*X_2 = \frac{wL^2}{32} \cdot \frac{k(16+15\phi) + \phi^2}{N_1} \quad X_3 = \frac{wL^2}{32N_2}$$

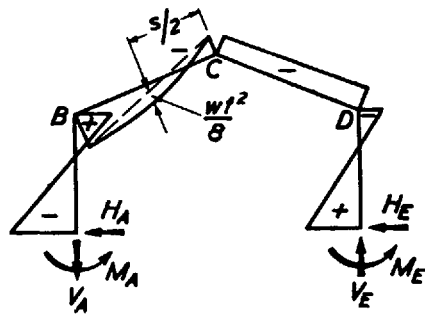
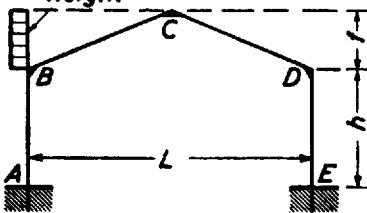
$$M_A = +X_1 - X_3 \quad M_B = -X_2 - X_3 \quad M_E = +X_1 + X_3 \quad M_D = -X_2 + X_3$$

$$*M_C = \frac{wL^2}{16} - \phi X_1 - mX_2$$

$$V_E = \frac{wL}{8} - \frac{2X_3}{L} \quad V_A = \frac{wL}{2} - V_E \quad H_A = H_E = \frac{X_1 + X_2}{h}$$

\* Note that  $X_1$ ,  $-X_3$  and  $M_C$  are respectively half the values of  $M_A (=M_E)$ ,  $M_B (=M_D)$  and  $M_C$  from the previous set of formulæ where the whole span was loaded.

w per unit height



$$\text{Constants: } X_1 = \frac{wf^2}{8} \cdot \frac{k(9\phi + 4) + \phi(6 + \phi)}{N_1}$$

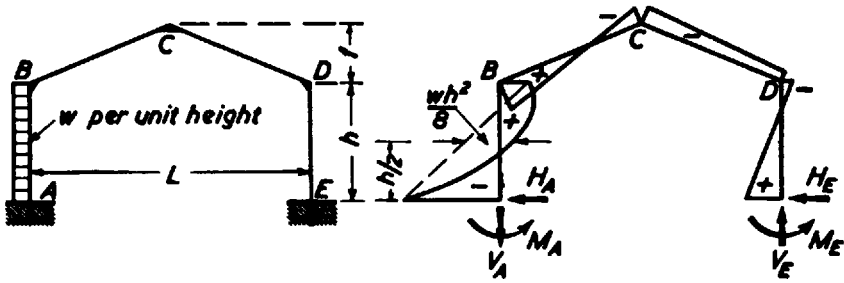
$$X_2 = \frac{wf^2}{8} \cdot \frac{k(8 + 9\phi) - \phi^2}{N_1} \quad X_3 = \frac{wf h}{8} \cdot \frac{4B + \phi}{N_2}$$

$$M_A = -X_1 - X_3 \quad M_B = +X_2 + \left(\frac{wf h}{2} - X_3\right)$$

$$M_E = -X_1 + X_3 \quad M_D = +X_2 - \left(\frac{wf h}{2} - X_3\right)$$

$$M_C = -\frac{wf^2}{4} + \phi X_1 + mX_2$$

$$V_A = -V_E = -\frac{wf h(2 + \phi)}{2L} + \frac{2X_3}{L} \quad H_E = \frac{wf}{2} - \frac{X_1 + X_2}{h} \quad H_A = -(wf - H_E)$$



$$\text{Constants: } X_1 = \frac{wh^2}{8} \cdot \frac{k(k+6) + k\phi(15+16\phi) + 6\phi^2}{N_1}$$

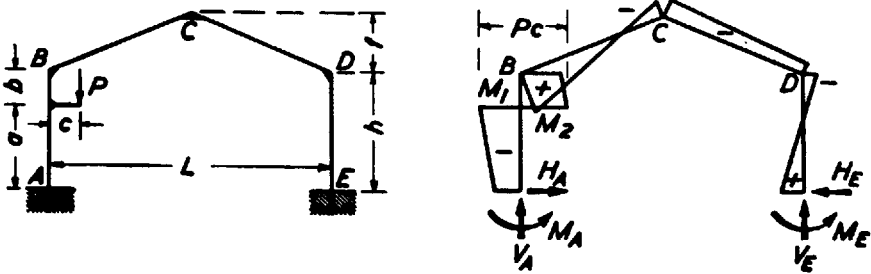
$$X_2 = \frac{wh^2k(9\phi + 8\phi^2 - k)}{8N_1} \quad X_3 = \frac{wh^2(2k+1)}{2N_2}$$

$$M_A = -X_1 - X_3 \quad M_B = +X_2 + \left(\frac{wh^2}{4} - X_3\right)$$

$$M_E = -X_1 + X_3 \quad M_D = +X_2 - \left(\frac{wh^2}{4} - X_3\right)$$

$$M_C = -\frac{whf}{4} + \phi X_1 + mX_2$$

$$V_A = -V_E = -\frac{wh^2}{2L} + \frac{2X_3}{L} \quad H_E = \frac{wh}{4} - \frac{X_1 + X_2}{h} \quad H_A = -(wh - H_E)$$



$$\text{Constants: } a_1 = \frac{a}{h} \quad b_1 = \frac{b}{h}$$

$$Y_1 = Pc[2\phi^2 - (1 - 3b_1^2)k] \quad Y_2 = Pc[\phi C - (3a_1^2 - 1)k]$$

$$X_1 = \frac{Y_1 K_1 - Y_2 R}{2N_1} \quad X_2 = \frac{Y_2 K_2 - Y_1 R}{2N_1} \quad X_3 = \frac{Pc}{2} \cdot \frac{B - 3(a_1 - b_1)k}{N_2}$$

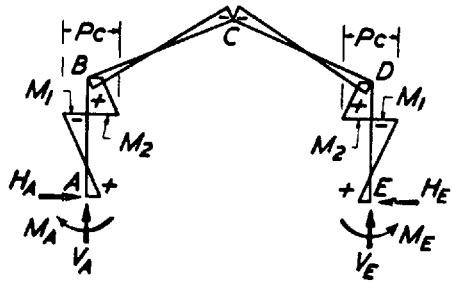
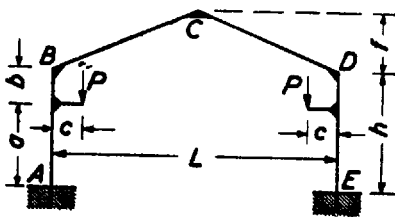
$$M_A = -X_1 - X_3 \quad M_B = +X_2 + \left(\frac{Pc}{2} - X_3\right)$$

$$M_E = -X_1 + X_3 \quad M_D = +X_2 - \left(\frac{Pc}{2} - X_3\right) \quad M_C = -\frac{\phi Pc}{2} + \phi X_1 + mX_2$$

$$M_1 = M_A - H_A a \quad M_2 = M_B + H_E b$$

$$V_E = \frac{Pc - 2X_3}{L} \quad V_A = P - V_E \quad H_A = H_E = \frac{Pc}{2h} - \frac{X_1 + X_2}{h}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



Constants:  $a_1 = \frac{a}{h}$      $b_1 = \frac{b}{h}$

$$Y_1 = Pc[2\phi^2 - (1 - 3b_1^2)k]$$

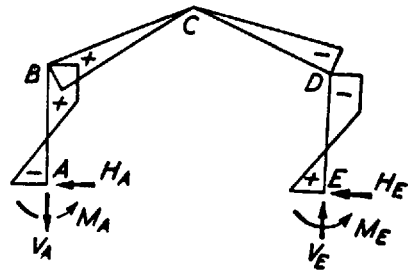
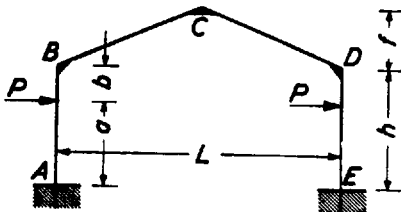
$$Y_2 = Pc[\phi C + (3a_1^2 - 1)k]$$

$$M_A = M_E = \frac{Y_2 R - Y_1 K_1}{N_1} \quad M_B = M_D = \frac{Y_2 K_2 - Y_1 R}{N_1}$$

$$M_C = -\phi(Pc + M_A) + mM_B$$

$$V_A = V_D = P \quad H_A = H_E = \frac{Pc + M_A - M_B}{h}$$

$$M_1 = M_A - H_A a \quad M_2 = M_B + H_E b$$

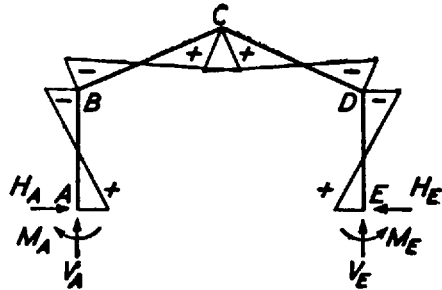
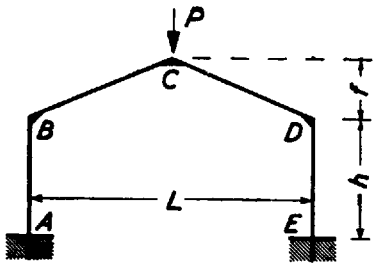


Constant:  $X_1 = \frac{Pa(B + 3b_1k)}{N_2}$

$$M_A = -M_E = -X_1 \quad M_B = -M_D = Pa - X_1 \quad M_C = 0$$

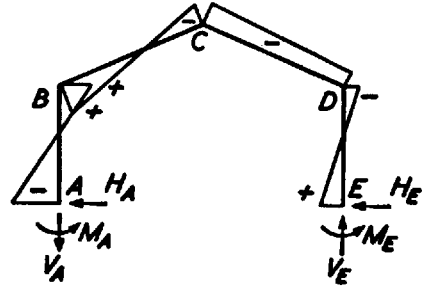
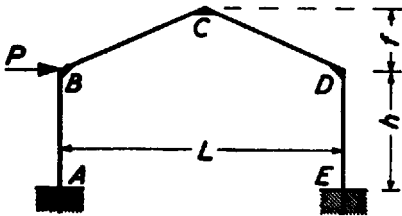
$$V_A = -V_E = -2 \left[ \frac{Pa - X_1}{L} \right] \quad H_A = -H_E = -P$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



$$M_A = M_E = \frac{3PL(k + 2k\phi + \phi)}{4N_1} \quad M_B = M_D = -\frac{3PLkm}{2N_1}$$

$$M_C = \frac{PL}{4} - \phi M_A + m M_B \quad V_A = V_E = P/2 \quad H_A = H_E = \frac{M_A - M_B}{h}$$

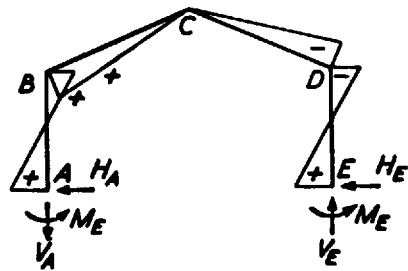
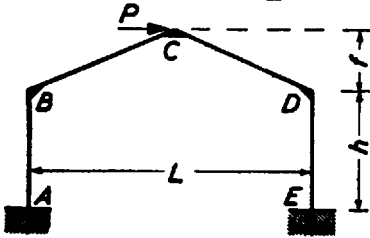


Constants:  $X_1 = \frac{3Pf(k + 2\phi k + \phi)}{2N_1}$      $X_2 = \frac{3Pfmk}{N_1}$      $X_3 = \frac{PhB}{2N_2}$

$$M_A = -X_1 - X_3 \quad M_B = +X_2 + \left(\frac{Ph}{2} - X_3\right)$$

$$M_E = -X_1 + X_3 \quad M_D = +X_2 - \left(\frac{Ph}{2} - X_3\right) \quad M_C = -\frac{Pf}{2} + \phi X_1 + m X_2$$

$$V_A = -V_E = -\frac{Ph - 2X_3}{L} \quad H_E = \frac{P}{2} - \frac{X_1 + X_2}{h} \quad H_A = -(P - H_E)$$

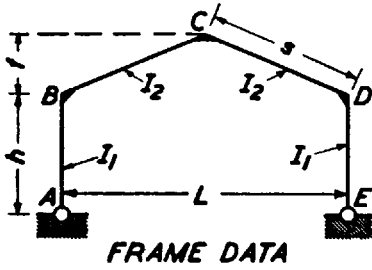


$$M_A = -M_E = -\frac{PhB}{2N_2} \quad M_B = -M_D = +\frac{3Phk}{2N_2} \quad M_C = 0$$

$$V_A = -V_E = -\frac{P(h+f) + 2M_A}{L} \quad H_A = -H_E = -\frac{P}{2}$$

Extract: 'Kleinlogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

Frame IV



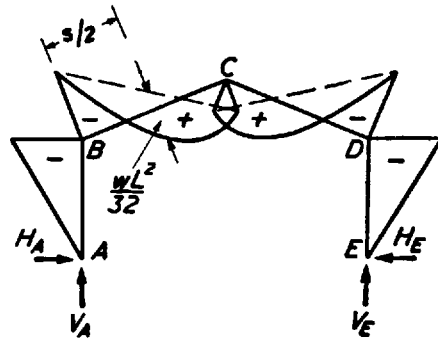
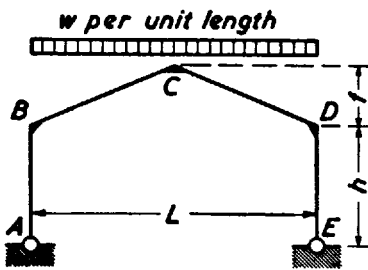
Coefficients:

$$k = \frac{I_2}{I_1} \cdot \frac{h}{s}$$

$$\phi = \frac{f}{h}$$

$$m = 1 + \phi$$

$$B = 2(k + 1) + m \quad C = 1 + 2m \quad N = B + mC$$



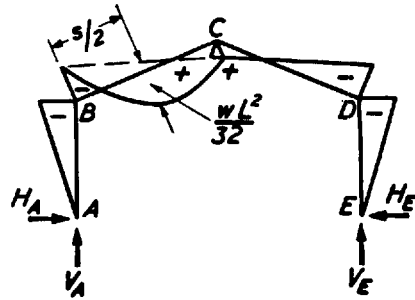
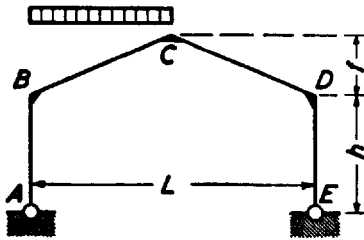
$$M_B = M_D = -\frac{wL^2(3 + 5m)}{16N} \quad M_C = \frac{wL^2}{8} + mM_B$$

$$H_A = H_E = -\frac{M_B}{h} \quad V_A = V_E = \frac{wL}{2}$$

Extract: 'Kleinlogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



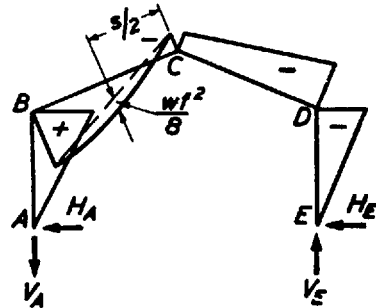
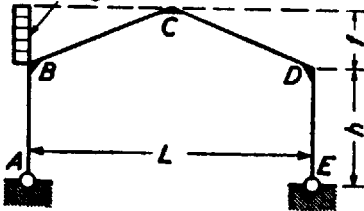
*w per unit length*



$$M_B = M_D = -\frac{wL^2(3+5m)}{32N} \quad M_C = \frac{wL^2}{16} + mM_B$$

$$H_A = H_E = -\frac{M_B}{h} \quad V_A = \frac{3wL}{8} \quad V_E = \frac{wL}{8}$$

*w per unit height*



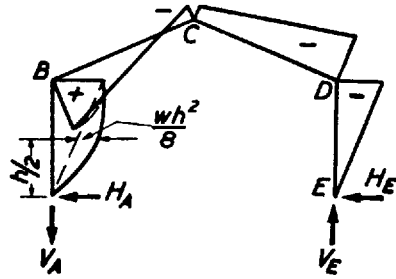
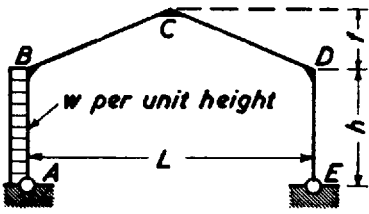
Constant:  $X = \frac{wf^2(C+m)}{8N}$

$$M_B = +X + \frac{wfh}{2} \quad M_C = -\frac{wf^2}{4} + mX$$

$$M_D = +X - \frac{wfh}{2} \quad V_A = -V_E = -\frac{wfh(1+m)}{2L}$$

$$H_A = -\frac{X}{h} - \frac{wf}{2} \quad H_E = -\frac{X}{h} + \frac{wf}{2}$$

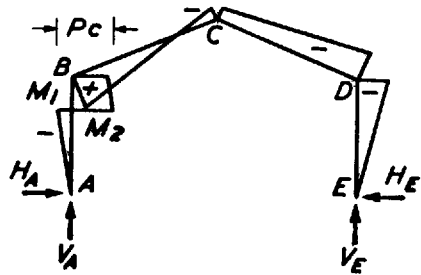
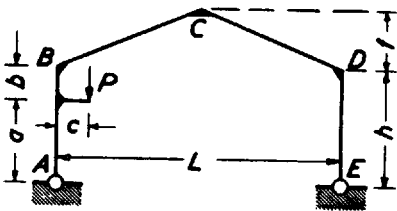
Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.



$$M_D = -\frac{wh^2}{8} \cdot \frac{2(B+C)+k}{N} \quad M_B = \frac{wh^2}{2} + M_D$$

$$M_C = \frac{wh^2}{4} + mM_D$$

$$V_A = -V_E = -\frac{wh^2}{2L} \quad H_E = -\frac{M_D}{h} \quad H_A = -(wh - H_E)$$



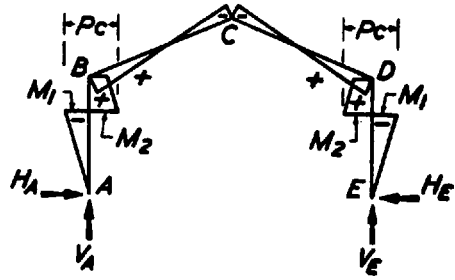
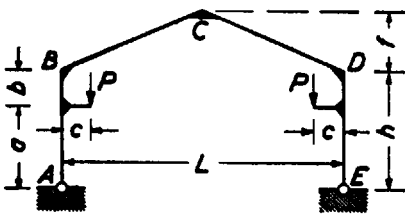
$$\text{Constants: } a_1 = \frac{a}{h} \quad X = \frac{Pc}{2} \cdot \frac{B+C-k(3a_1^2-1)}{N}$$

$$M_B = Pc - X \quad M_D = -X \quad M_C = \frac{Pc}{2} - mX$$

$$M_1 = -a_1X \quad M_2 = Pc - a_1X$$

$$V_E = \frac{Pc}{L} \quad V_A = P - V_E \quad H_A = H_E = \frac{X}{h}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

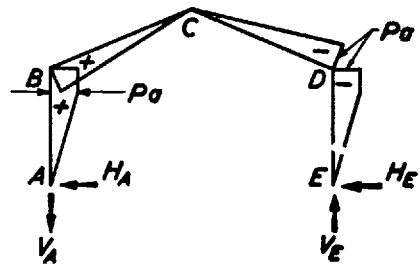
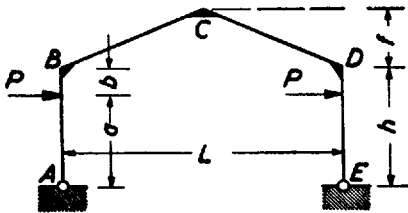


Constant:  $a_1 = \frac{a}{h}$

$$M_B = M_D = Pc \cdot \frac{\phi C + k(3a_1^2 - 1)}{N} \quad M_C = -\phi Pc + mM_B$$

$$H_A = H_E = \frac{Pc - M_B}{h} \quad V_A = V_E = P$$

$$M_1 = -a_1(Pc - M_B) \quad M_2 = (1 - a_1)Pc + a_1M_B$$

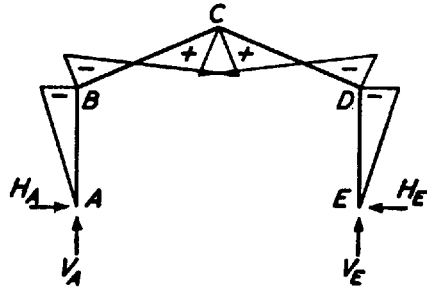
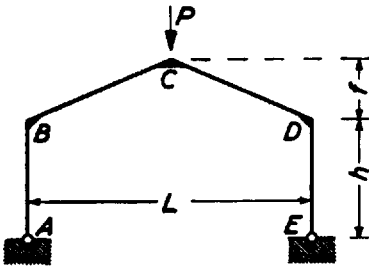


$$M_B = -M_D = Pa \quad M_C = 0$$

$$H_A = -H_E = -P \quad V_A = -V_E = -\frac{2Pa}{L}$$

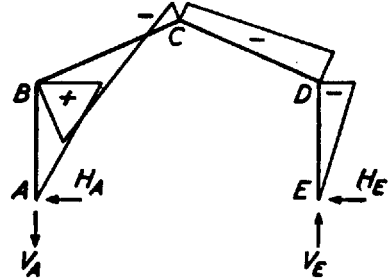
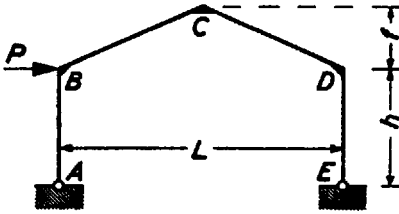
Moment at loads =  $\pm Pa$

*Extract: 'Kleinogel, Rahmenformeln' 11, Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.*



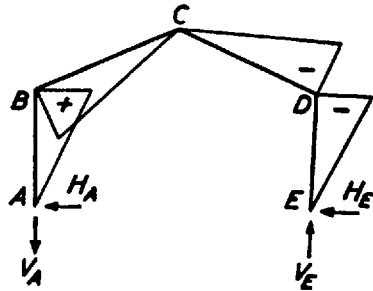
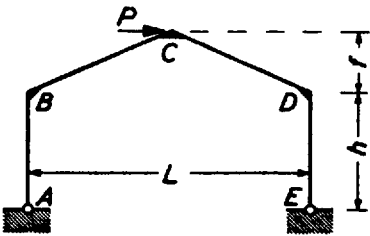
$$M_B = M_D = -\frac{PL}{4} \cdot \frac{C}{N} \quad M_C = +\frac{PL}{4} \cdot \frac{B}{N}$$

$$V_A = V_E = \frac{P}{2} \quad H_A = H_E = -\frac{M_B}{h}$$



$$M_D = -\frac{Ph(B+C)}{2N} \quad M_B = Ph + M_D \quad M_C = \frac{Ph}{2} + mM_D$$

$$V_A = -V_E = -\frac{Ph}{L} \quad H_E = -\frac{M_D}{h} \quad H_A = -(P - H_E)$$



$$M_B = -M_D = +\frac{Ph}{2} \quad M_C = 0 \quad V_A = -V_E = -\frac{Phm}{L} \quad H_A = -H_E = -\frac{P}{2}$$

Extract: 'Kleinogel, Rahmenformeln' 11. Auflage Berlin—Verlag von Wilhelm Ernst & Sohn.

## **Explanatory notes on section dimensions and properties**

### **1 General**

#### ***1.1 Material***

The structural components referred to in this handbook are of weldable structural steels to BS 4360: 1990 and BS EN 10025: 1990.

#### ***1.2 Sections***

The structural sections referred to in this handbook are produced to the following specifications:

Universal beams, columns, joists and channels:

BS 4: Structural steel sections

Part 1: 1980 Specification for hot rolled sections

Including Amendments 1 (September 1981), 2 (May 1982), 3 (February 1986), 4 (June 1987) and 5 (June 1988)

Structural hollow sections:

BS 4848: Hot rolled structural steel sections

Part 2: 1991 Specification for hot-finished hollow sections

Some other hollow sections currently in regular production are also included.

Equal and unequal angles:

BS 4848: Hot rolled structural steel sections

Part 4: 1972 Equal and unequal angles

Including Amendments 1 (February 1974), 2 (October 1982) and 3 (February 1986)

#### ***1.3 Dimensional units***

The dimensions of sections are given in millimetres (mm). For tolerances on shape, reference should be made to the above standards.

#### ***1.4 Property units***

Generally the centimetre (cm) is used for the calculated properties but for surface areas and for the warping constant ( $H$ ), the metre (m) and the decimetre (dm) respectively are used.

$$\begin{aligned}
 \text{NB } 1 \text{ dm} &= 0.1 \text{ m} = 100 \text{ mm} \\
 1 \text{ dm}^6 &= 1 \times 10^{-6} \text{ m}^6 = 1 \times 10^{12} \text{ mm}^6
 \end{aligned}$$

### 1.5 Mass and force units

The units used are the kilogram (kg), the newton (N) and the metre per second per second ( $\text{m/s}^2$ ) so that  $1 \text{ N} = 1 \text{ kg} \times 1 \text{ m/s}^2$ . For convenience a standard value of the acceleration due to gravity has been generally accepted as  $9.80665 \text{ m/s}^2$ . Thus the force exerted by 1 kg under the action of gravity is 9.80665 N and the force exerted by 1 tonne (1000 kg) is 9.80665 kilonewtons (kN).

## 2 Dimensions of sections

### 2.1 Masses

The masses per metre have been calculated assuming that the density of steel is  $7850 \text{ kg/m}^3$ . The values listed are subject to a rolling margin of  $2\frac{1}{2}\%$ .

In all cases including compound sections the tabulated masses are for the steel section alone and no allowance has been made for connecting material or fittings.

### 2.2 Ratios for local buckling

The ratios of the flange outstand to thickness ( $b/T$ ) and the web depth to thickness ( $d/t$ ) are given for I, H and channel sections. The ratios of the outside diameter to thickness ( $D/t$ ) are given for circular hollow sections. The ratios  $d/t$  and  $b/t$  are also given for square and rectangular hollow sections. They have been calculated using the dimensions specified in Figure 3 of BS 5950: Part 1 and are for use when element and section class are being checked to the limits given in Table 7 of BS 5950: Part 1.

### 2.3 Dimensions for detailing

The dimensions  $C$ ,  $N$  and  $n$  have the meanings given in the figures at the head of the tables and have been calculated as follows.

#### 2.3.1 Universal beams, columns and bearing piles

$$N = \left[ \frac{B - t}{2} \right] + 10 \text{ mm to the nearest 2 mm above}$$

$$n = \left[ \frac{D - d}{2} \right] \text{ mm to the nearest 2 mm above}$$

$$C = \frac{t}{2} + 2 \text{ mm to the nearest mm}$$

### 2.3.2 Joists

$$N = \left[ \frac{B - t}{2} \right] + 6 \text{ mm to the nearest 2 mm above}$$

$$n = \left[ \frac{D - d}{2} \right] \text{ mm to the nearest 2 mm above}$$

$$C = \frac{t}{2} + 2 \text{ mm to the nearest mm}$$

*NB* Flanges of BS 4 joists have an 8° taper.

### 2.3.3 Channels

$$N = (B - t) + 6 \text{ mm to the nearest 2 mm above}$$

$$n = \left[ \frac{D - d}{2} \right] \text{ mm to the nearest 2 mm above}$$

$$C = t + 2 \text{ mm to the nearest mm}$$

*NB* All channels are rolled with a 5° taper on the inside of the flanges.

### 2.3.4 Castellated sections

Generally the depth of the castellated section  $D_c$  is given by

$$D_c = D + D_s/2$$

where  $D$  is the actual depth of the original section, and

$D_s$  is the serial depth of the original section, except as noted below.

The value of  $D_c$  has now been calculated from the metric dimensions of  $D$  and  $D_s$ .

The exceptions to the above are columns in the 356 × 406 series and the column core section for which  $D_s = 381$  mm and 406.4 mm respectively.

### 3 Section properties

#### 3.1 General

All section properties have been accurately calculated and rounded to three significant figures except those above 1000 which have been rounded to four significant figures. The section properties have been calculated from the metric dimensions given in BS 4 and BS 4848: Parts 2 and 4 as appropriate. In BS 4: Part 1: 1980, the section properties are calculated from the original dimensions in inch units. For angles, BS 4848: Part 4: 1972 repeats the values from ISO 657-1 which are calculated assuming the toe radius equals half the root radius. The section properties in this publication are therefore more accurate, but differ slightly in some cases from those listed in the current version of the relevant British Standards.

#### 3.2 Sections other than hollow sections

##### 3.2.1 Second moment of area ( $I$ )

The second moment of area of the sections, often referred to as moment of inertia, has been calculated taking into account all radii and fillets of the sections.

##### 3.2.2 Radius of gyration ( $r$ )

The radius of gyration is a parameter used in buckling calculations and is derived from

$$r = \left[ \frac{I}{A} \right]^{\frac{1}{2}}$$

where  $A$  is the cross-sectional area.

For castellated sections, the radius of gyration is that at the net section as required for use in design to BS 5950.

##### 3.2.3 Elastic modulus ( $Z$ )

The elastic modulus, or section modulus, is a parameter used to calculate the moment capacity from the design strength of the stress at the extreme fibre from a known moment. It is derived from

$$Z = \frac{I}{y}$$

where  $y$  is the distance to the extreme fibre of the section from the neutral axis.



For castellated sections, the elastic moduli given are those at the net section. The elastic moduli of the tee are calculated at the outer face of the flange and toe of the tee formed at the net section.

For channels, the elastic modulus about the minor ( $y$ - $y$ ) axis is given at the toe of the section

$$\text{i.e. } y = B - C_y$$

where  $B$  is the width of the section, and

$C_y$  is the distance from the centroid to the outer face of the web.

For angles, the elastic moduli about both axes are given at the toes of the section

$$\text{i.e. } y_x = A - c_x \quad y_y = B - c_y$$

where  $A$  is the leg length perpendicular to the  $x$ - $x$  axis,

$B$  is the leg length perpendicular to the  $y$ - $y$  axis,

$c_x$  and  $c_y$  are the distance of the centre of gravity from the back of the angle, referred to the  $x$ - $x$  axis and  $y$ - $y$  axis respectively.

### 3.2.4 Buckling parameter ( $u$ ) and torsional index ( $x$ )

The buckling parameter and torsional index are parameters used in buckling calculations and have been derived as follows:

(1) For flanged sections symmetrical about the minor axis

$$u = \left[ \frac{4S_x^2 \gamma}{A^2 h^2} \right]^{\frac{1}{4}}$$

$$x = 0.566h \left[ \frac{A}{J} \right]^{\frac{1}{2}}$$

(2) For flanged sections symmetrical about the major axis

$$u = \left[ \frac{I_y S_x^2 \gamma}{A^2 H^2} \right]^{\frac{1}{4}}$$

$$x = 1.132 \left[ \frac{AH}{I_y J} \right]^{\frac{1}{2}}$$

where  $S_x$  is the plastic modulus about the major axis,

$$\gamma = \left[ 1 - \frac{I_y}{I_x} \right],$$

$I_x$  is the second moment of area about the major axis,

$I_y$  is the second moment of area about the minor axis,

$A$  is the cross-sectional area,

$h$  is the distance between shear centres of flanges (for T sections,  $h$  is the distance between the shear centre of the flange and the toe of the web),  
 $H$  is the warping constant, and  
 $J$  is the torsion constant.

*NB* For bisymmetric sections either of the above expressions for  $u$  and  $x$  may be used.

### 3.2.5 Warping constant ( $H$ ) and torsion constant ( $J$ )

The warping constants and torsion constants are complex expressions which may be derived from a number of different sources.

### 3.2.6 Plastic modulus ( $S$ )

The full and reduced plastic moduli under axial load about both principal axes are tabulated for sections other than angle sections. Values for angle sections are excluded as BS 5950 requires that they be designed using the elastic modulus.

When a section is loaded to full plasticity by a combination of bending and axial thrust about the major axis the neutral axis shifts and may be in either the web or the tension flange depending on the relative value of bending and thrust. Different formulae giving the reduced plastic modulus under combined loading have to be used. Further details for calculating the reduced plastic modulus can be obtained from *The Plastic Properties of Rolled Sections* published by the British Welding Research Association (now The Welding Institute). They incorporate the term  $n$  where

$$n = \frac{F}{A_g p_y}$$

where  $F$  is the factored axial load,  
 $A_g$  is the gross cross-sectional area, and  
 $p_y$  is the design strength of the steel.

For each section there is a 'change' value of  $n$ .

If the value of  $n$  calculated is less than the change value the neutral axis is in the web and the formula for lower values of  $n$  must be used. If  $n$  is greater than the change value the neutral axis lies in the tension flange and the formula for higher values of  $n$  must be used. The same principles apply to  $I$ -sections loaded axially and bent about the minor axis, lower and higher values of  $n$  indicating that the neutral axis lies inside or outside the web respectively.

The reduced plastic modulus of channels bending about the minor axis depends on whether the stresses induced by the loading are the same or of opposite kind towards the back of the channel, any moment due to eccentricity of load being

assessed relative to the centroidal axis. Where the stresses are of the same kind they cause an initial rise of minor axis moment capacity when lower values of  $n$  apply.

### 3.3 Hollow sections

#### 3.3.1 Common properties

For second moment of area, radius of gyration and elastic modulus see notes 3.2.1, 3.2.2 and 3.2.3.

#### 3.3.2 Torsion constant ( $J$ )

For circular hollow sections

$$J = 2I$$

For square and rectangular hollow sections

$$J = \frac{t^3 h}{3} + 2k A_h$$

where  $I$  is the second moment of area,

$t$  is the thickness of section,

$h$  is the mean perimeter =  $2 [(B - t) + (D - t)] - 2R_c (4 - \pi)$ ,

$A_h$  is the area enclosed by mean perimeter =  $(B - t)(D - t) - R_c^2 (4 - \pi)$ ,

$$k = \frac{2A_h t}{h},$$

$B$  is the breadth of section,

$D$  is the depth of section, and

$R_c$  is the average of internal and external corner radii.

#### 3.3.3 Torsion modulus constant ( $C$ )

For circular hollow sections

$$C = 2Z$$

For square and rectangular hollow sections

$$C = \frac{J}{t + \frac{k}{t}}$$

where  $Z$  is the elastic modulus and  $J$ ,  $t$  and  $k$  are as defined in note 3.3.2.

### 3.3.4 Plastic modulus of hollow sections

The full plastic modulus only is given in the tables. When a member is subject to axial loads as well as bending stresses, the plastic modulus needs modification to take account of the reduction in plastic moment of resistance.

The following expressions give the values of the reduced plastic moduli to be used.

For circular hollow sections

$$S_r = S \cos \left( \frac{n\pi}{2} \right)$$

For square and rectangular hollow sections, bending about major axis

$$S_{rx} = S_x - \frac{A^2 n^2}{8t} \quad \text{for } n \leq \frac{2t(D - 2t)}{A}$$

i.e. PNA in the webs

$$S_{rx} = \frac{A^2}{4(B - t)} (1 - n) \left[ \frac{2D(B - t)}{A} + n - 1 \right] \quad \text{for } n > \frac{2t(D - 2t)}{A}$$

i.e. PNA in the flanges

bending about minor axis

$$S_{ry} = S_y - \frac{A^2 n^2}{8t} \quad \text{for } n \leq \frac{2t(B - 2t)}{A}$$

i.e. PNA in the webs

$$S_{ry} = \frac{A^2}{4(D - t)} (1 - n) \left[ \frac{2B(D - t)}{A} + n - 1 \right] \quad \text{for } n > \frac{2t(B - 2t)}{A}$$

i.e. PNA in the flanges

where  $S$ ,  $S_x$ ,  $S_y$  are the full plastic moduli about the relevant axes,

$$n = \frac{F}{Ap_y}$$

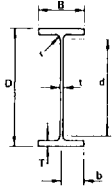
$F$  is the factored axial load,

$A$  is the gross cross-sectional area,

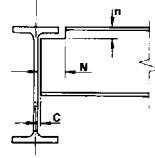
$p_y$  is the design strength of the steel,

$D$ ,  $B$  and  $t$  are as defined in note 3.3.2, and

PNA is plastic neutral axis.



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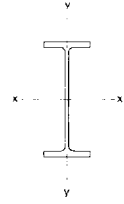


**DIMENSIONS**

| Designation | Mass Per Metre | Depth Of Section D | Width Of Section B | Thickness |          | Root Radius r | Depth Between Fillets d | Ratios For Local Buckling |         | Dimensions For Detailing |       |                | Surface Area             |                          |
|-------------|----------------|--------------------|--------------------|-----------|----------|---------------|-------------------------|---------------------------|---------|--------------------------|-------|----------------|--------------------------|--------------------------|
|             |                |                    |                    | Web t     | Flange T |               |                         | Flange b/T                | Web d/t | End Clearance C          | Notch |                | Per Metre m <sup>2</sup> | Per Tonne m <sup>2</sup> |
|             |                |                    |                    |           |          |               |                         |                           |         |                          | N     | n              |                          |                          |
| Serial Size | kg             | mm                 | mm                 | mm        | mm       | mm            | mm                      |                           |         | mm                       | mm    | m <sup>2</sup> | m <sup>2</sup>           |                          |
| 914x419     | 388            | 920.5              | 420.5              | 21.5      | 36.6     | 24.1          | 799.1                   | 5.74                      | 37.2    | 13                       | 210   | 62             | 3.44                     | 8.86                     |
|             | 343            | 911.4              | 418.5              | 19.4      | 32.0     | 24.1          | 799.2                   | 6.54                      | 41.2    | 12                       | 210   | 58             | 3.42                     | 9.96                     |
| 914x305     | 289            | 926.6              | 307.8              | 19.6      | 32.0     | 19.1          | 824.4                   | 4.81                      | 42.1    | 12                       | 156   | 52             | 3.01                     | 10.4                     |
|             | 253            | 918.5              | 305.5              | 17.3      | 27.9     | 19.1          | 824.5                   | 5.47                      | 47.7    | 11                       | 156   | 48             | 2.99                     | 11.8                     |
|             | 224            | 910.3              | 304.1              | 15.9      | 23.9     | 19.1          | 824.3                   | 6.36                      | 51.8    | 10                       | 156   | 44             | 2.97                     | 13.3                     |
|             | 201            | 903.0              | 303.4              | 15.2      | 20.2     | 19.1          | 824.4                   | 7.51                      | 54.2    | 10                       | 156   | 40             | 2.96                     | 14.7                     |
| 838x292     | 226            | 850.9              | 293.8              | 16.1      | 26.8     | 17.8          | 761.7                   | 5.48                      | 47.3    | 10                       | 150   | 46             | 2.81                     | 12.5                     |
|             | 194            | 840.7              | 292.4              | 14.7      | 21.7     | 17.8          | 761.7                   | 6.74                      | 51.8    | 9                        | 150   | 40             | 2.79                     | 14.4                     |
|             | 176            | 834.9              | 291.6              | 14.0      | 18.8     | 17.8          | 761.7                   | 7.76                      | 54.4    | 9                        | 150   | 38             | 2.78                     | 15.8                     |
| 762x267     | 197            | 769.6              | 268.0              | 15.6      | 25.4     | 16.5          | 685.8                   | 5.28                      | 44.0    | 10                       | 138   | 42             | 2.55                     | 13.0                     |
|             | 173            | 762.0              | 266.7              | 14.3      | 21.6     | 16.5          | 685.8                   | 6.17                      | 48.0    | 9                        | 138   | 40             | 2.53                     | 14.6                     |
|             | 147            | 753.9              | 265.3              | 12.9      | 17.5     | 16.5          | 685.9                   | 7.58                      | 53.2    | 8                        | 138   | 34             | 2.51                     | 17.1                     |
| 686x254     | 170            | 692.9              | 255.8              | 14.5      | 23.7     | 15.2          | 615.1                   | 5.40                      | 42.4    | 9                        | 132   | 40             | 2.35                     | 13.8                     |
|             | 152            | 687.6              | 254.5              | 13.2      | 21.0     | 15.2          | 615.2                   | 6.06                      | 46.6    | 9                        | 132   | 38             | 2.34                     | 15.4                     |
|             | 140            | 683.5              | 253.7              | 12.4      | 19.0     | 15.2          | 615.1                   | 6.68                      | 49.6    | 8                        | 132   | 36             | 2.33                     | 16.6                     |
|             | 125            | 677.9              | 253.0              | 11.7      | 16.2     | 15.2          | 615.1                   | 7.81                      | 52.6    | 8                        | 132   | 32             | 2.32                     | 18.5                     |
| 610x305     | 238            | 633.0              | 311.5              | 18.6      | 31.4     | 16.5          | 537.2                   | 4.96                      | 28.9    | 11                       | 158   | 48             | 2.45                     | 10.3                     |
|             | 179            | 617.5              | 307.0              | 14.1      | 23.6     | 16.5          | 537.3                   | 6.50                      | 38.1    | 9                        | 158   | 42             | 2.41                     | 13.4                     |
|             | 149            | 609.6              | 304.8              | 11.9      | 19.7     | 16.5          | 537.2                   | 7.74                      | 45.1    | 8                        | 158   | 38             | 2.39                     | 16.0                     |
| 610x229     | 140            | 617.0              | 230.1              | 13.1      | 22.1     | 12.7          | 547.4                   | 5.21                      | 41.8    | 9                        | 120   | 36             | 2.11                     | 15.0                     |
|             | 125            | 611.9              | 229.0              | 11.9      | 19.6     | 12.7          | 547.3                   | 5.84                      | 46.0    | 8                        | 120   | 34             | 2.09                     | 16.8                     |
|             | 113            | 607.3              | 228.2              | 11.2      | 17.3     | 12.7          | 547.3                   | 6.60                      | 48.9    | 8                        | 120   | 30             | 2.08                     | 18.4                     |
|             | 101            | 602.2              | 227.6              | 10.6      | 14.8     | 12.7          | 547.2                   | 7.69                      | 51.6    | 7                        | 120   | 28             | 2.07                     | 20.5                     |
| 533x210     | 122            | 544.6              | 211.9              | 12.8      | 21.3     | 12.7          | 476.6                   | 4.97                      | 37.2    | 8                        | 110   | 34             | 1.89                     | 15.5                     |
|             | 109            | 539.5              | 210.7              | 11.6      | 18.8     | 12.7          | 476.5                   | 5.60                      | 41.1    | 8                        | 110   | 32             | 1.88                     | 17.2                     |
|             | 101            | 536.7              | 210.1              | 10.9      | 17.4     | 12.7          | 476.5                   | 6.04                      | 43.7    | 7                        | 110   | 32             | 1.87                     | 18.5                     |
|             | 92             | 533.1              | 209.3              | 10.2      | 15.6     | 12.7          | 476.5                   | 6.71                      | 46.7    | 7                        | 110   | 30             | 1.86                     | 20.2                     |
|             | 82             | 528.3              | 208.7              | 9.6       | 13.2     | 12.7          | 476.5                   | 7.91                      | 49.6    | 7                        | 110   | 26             | 1.85                     | 22.6                     |
| 457x191     | 98             | 467.4              | 192.8              | 11.4      | 19.6     | 10.2          | 407.8                   | 4.92                      | 35.8    | 8                        | 102   | 30             | 1.67                     | 17.0                     |
|             | 89             | 463.6              | 192.0              | 10.6      | 17.7     | 10.2          | 407.8                   | 5.42                      | 38.5    | 7                        | 102   | 28             | 1.66                     | 18.6                     |
|             | 82             | 460.2              | 191.3              | 9.9       | 16.0     | 10.2          | 407.8                   | 5.98                      | 41.2    | 7                        | 102   | 28             | 1.65                     | 20.1                     |
|             | 74             | 457.2              | 190.5              | 9.1       | 14.5     | 10.2          | 407.8                   | 6.57                      | 44.8    | 7                        | 102   | 26             | 1.64                     | 22.2                     |
|             | 67             | 453.6              | 189.9              | 8.5       | 12.7     | 10.2          | 407.8                   | 7.48                      | 48.0    | 6                        | 102   | 24             | 1.63                     | 24.4                     |
| 457x152     | 82             | 465.1              | 153.5              | 10.7      | 18.9     | 10.2          | 406.9                   | 4.06                      | 38.0    | 7                        | 82    | 30             | 1.51                     | 18.4                     |
|             | 74             | 461.3              | 152.7              | 9.9       | 17.0     | 10.2          | 406.9                   | 4.49                      | 41.1    | 7                        | 82    | 28             | 1.50                     | 20.2                     |
|             | 67             | 457.2              | 151.9              | 9.1       | 15.0     | 10.2          | 406.8                   | 5.06                      | 44.7    | 7                        | 82    | 26             | 1.49                     | 22.2                     |
|             | 60             | 454.7              | 152.9              | 8.0       | 13.3     | 10.2          | 407.7                   | 5.75                      | 51.0    | 6                        | 84    | 24             | 1.49                     | 24.8                     |
|             | 52             | 449.8              | 152.4              | 7.6       | 10.9     | 10.2          | 407.6                   | 6.99                      | 53.6    | 6                        | 84    | 22             | 1.48                     | 28.4                     |

FOR EXPLANATION OF TABLES SEE NOTE 2

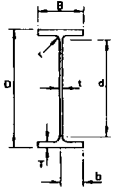
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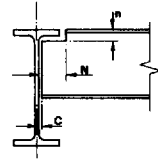
PROPERTIES

| Designation |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 | Plastic Modulus |                 | Buckling Parameter | Torsional Index | Warping Constant | Torsional Constant | Area of Section |
|-------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|------------------|--------------------|-----------------|
| Serial Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        | Axis y-y        | Axis x-x        | Axis y-y        | u                  | x               | H                | J                  | A               |
| mm          | kg             | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |                    |                 | dm <sup>6</sup>  | cm <sup>4</sup>    | cm <sup>2</sup> |
| 914x419     | 388            | 719300                | 45440           | 38.1               | 9.58     | 15630           | 2161            | 17670           | 3342            | 0.884              | 26.7            | 88.8             | 1739               | 495             |
|             | 343            | 625200                | 39160           | 37.8               | 9.46     | 13720           | 1871            | 15470           | 2890            | 0.883              | 30.1            | 75.7             | 1193               | 437             |
| 914x305     | 289            | 504800                | 15610           | 37.0               | 6.50     | 10900           | 1015            | 12590           | 1603            | 0.866              | 31.9            | 31.2             | 930                | 369             |
|             | 253            | 436400                | 13300           | 36.8               | 6.42     | 9503            | 871             | 10940           | 1371            | 0.866              | 36.2            | 26.4             | 626                | 323             |
|             | 224            | 376300                | 11240           | 36.3               | 6.27     | 8268            | 739             | 9533            | 1163            | 0.861              | 41.3            | 22.1             | 422                | 286             |
|             | 201            | 325900                | 9433            | 35.6               | 6.06     | 7217            | 622             | 8372            | 983             | 0.853              | 46.7            | 18.4             | 294                | 257             |
| 838x292     | 226            | 339700                | 11360           | 34.3               | 6.27     | 7985            | 773             | 9155            | 1212            | 0.870              | 35.0            | 19.3             | 514                | 289             |
|             | 194            | 279200                | 9066            | 33.6               | 6.06     | 6641            | 620             | 7640            | 974             | 0.862              | 41.6            | 15.2             | 306                | 247             |
|             | 176            | 246000                | 7791            | 33.1               | 5.90     | 5892            | 534             | 6806            | 841             | 0.856              | 46.5            | 13.0             | 221                | 224             |
| 762x267     | 197            | 239800                | 8175            | 30.9               | 5.71     | 6232            | 610             | 7164            | 959             | 0.869              | 33.2            | 11.3             | 404                | 251             |
|             | 173            | 205200                | 6850            | 30.5               | 5.58     | 5385            | 514             | 6195            | 807             | 0.864              | 38.1            | 9.39             | 287                | 220             |
|             | 147            | 168800                | 5462            | 30.0               | 5.39     | 4478            | 412             | 5169            | 648             | 0.857              | 45.1            | 7.40             | 160                | 188             |
| 686x254     | 170            | 170300                | 6630            | 28.0               | 5.53     | 4916            | 518             | 5631            | 811             | 0.872              | 31.8            | 7.42             | 308                | 217             |
|             | 152            | 150400                | 5784            | 27.8               | 5.46     | 4375            | 455             | 5001            | 710             | 0.871              | 35.5            | 6.43             | 220                | 194             |
|             | 140            | 136300                | 5183            | 27.6               | 5.39     | 3967            | 409             | 4558            | 638             | 0.868              | 38.7            | 5.72             | 169                | 178             |
|             | 125            | 118000                | 4383            | 27.2               | 5.24     | 3481            | 346             | 3994            | 542             | 0.862              | 43.9            | 4.80             | 116                | 159             |
| 610x305     | 238            | 207700                | 15850           | 26.1               | 7.22     | 6564            | 1018            | 7462            | 1576            | 0.886              | 21.1            | 14.3             | 790                | 304             |
|             | 179            | 151500                | 11400           | 25.8               | 7.08     | 4907            | 742             | 5515            | 1143            | 0.886              | 27.5            | 10.0             | 340                | 228             |
|             | 149            | 124700                | 9308            | 25.6               | 6.99     | 4093            | 611             | 4575            | 938             | 0.886              | 32.5            | 8.10             | 201                | 190             |
| 610x229     | 140            | 111700                | 4499            | 25.0               | 5.03     | 3619            | 391             | 4139            | 611             | 0.875              | 30.6            | 3.98             | 216                | 178             |
|             | 125            | 98500                 | 3932            | 24.9               | 4.97     | 3219            | 343             | 3673            | 535             | 0.873              | 34.1            | 3.45             | 154                | 159             |
|             | 113            | 87380                 | 3434            | 24.6               | 4.88     | 2878            | 301             | 3287            | 470             | 0.869              | 37.9            | 2.99             | 112                | 144             |
|             | 101            | 75820                 | 2915            | 24.2               | 4.75     | 2518            | 256             | 2887            | 401             | 0.863              | 42.9            | 2.51             | 77.6               | 129             |
| 533x210     | 122            | 76190                 | 3388            | 22.1               | 4.66     | 2798            | 320             | 3203            | 500             | 0.876              | 27.6            | 2.32             | 179                | 156             |
|             | 109            | 66800                 | 2939            | 21.9               | 4.60     | 2476            | 279             | 2827            | 435             | 0.875              | 30.9            | 1.99             | 126                | 139             |
|             | 101            | 61650                 | 2696            | 21.8               | 4.57     | 2237            | 257             | 2619            | 400             | 0.874              | 33.1            | 1.62             | 102                | 129             |
|             | 92             | 56330                 | 2389            | 21.7               | 4.50     | 2076            | 228             | 2366            | 356             | 0.871              | 36.4            | 1.60             | 76.3               | 118             |
|             | 82             | 47520                 | 2004            | 21.3               | 4.36     | 1799            | 192             | 2058            | 300             | 0.864              | 41.6            | 1.33             | 51.5               | 105             |
| 457x191     | 98             | 45770                 | 2347            | 19.1               | 4.33     | 1959            | 243             | 2234            | 379             | 0.881              | 25.8            | 1.18             | 121                | 125             |
|             | 89             | 41140                 | 2063            | 19.0               | 4.26     | 1775            | 218             | 2020            | 339             | 0.879              | 28.2            | 1.04             | 91.3               | 114             |
|             | 82             | 37090                 | 1871            | 18.8               | 4.23     | 1612            | 196             | 1832            | 304             | 0.877              | 30.9            | 0.923            | 69.2               | 105             |
|             | 74             | 33430                 | 1674            | 18.7               | 4.20     | 1462            | 176             | 1659            | 273             | 0.876              | 33.8            | 0.820            | 52.2               | 95.1            |
|             | 67             | 29410                 | 1452            | 18.5               | 4.12     | 1297            | 153             | 1472            | 237             | 0.872              | 37.9            | 0.706            | 37.1               | 85.5            |
| 457x152     | 82             | 36250                 | 1144            | 18.6               | 3.31     | 1559            | 149             | 1802            | 236             | 0.872              | 27.3            | 0.570            | 89.5               | 105             |
|             | 74             | 32470                 | 1013            | 18.5               | 3.26     | 1408            | 133             | 1624            | 209             | 0.870              | 30.0            | 0.500            | 66.8               | 95.1            |
|             | 67             | 28600                 | 879             | 18.3               | 3.21     | 1251            | 116             | 1442            | 183             | 0.867              | 33.5            | 0.430            | 47.6               | 85.3            |
|             | 60             | 25450                 | 795             | 18.3               | 3.24     | 1119            | 104             | 1283            | 163             | 0.869              | 37.6            | 0.387            | 33.5               | 75.8            |
|             | 52             | 21370                 | 645             | 17.9               | 3.11     | 950             | 84.6            | 1096            | 133             | 0.859              | 43.9            | 0.311            | 21.4               | 66.6            |

FOR EXPLANATION OF TABLES SEE NOTE 3



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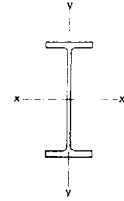


**DIMENSIONS**

| Designation       |                      | Depth Of Section D<br>mm | Width Of Section B<br>mm | Thickness   |                | Root Radius r<br>mm | Depth Between Fillets d<br>mm | Ratios For Local Buckling |         | Dimensions For Detailing |         |         | Surface Area                |                             |
|-------------------|----------------------|--------------------------|--------------------------|-------------|----------------|---------------------|-------------------------------|---------------------------|---------|--------------------------|---------|---------|-----------------------------|-----------------------------|
| Serial Size<br>mm | Mass Per Metre<br>kg |                          |                          | Web t<br>mm | Flange T<br>mm |                     |                               | Flange b/T                | Web d/t | End Clearance C<br>mm    | Notch   |         | Per Metre<br>m <sup>2</sup> | Per Tonne<br>m <sup>2</sup> |
|                   |                      |                          |                          |             |                |                     |                               |                           |         |                          | N<br>mm | n<br>mm |                             |                             |
| 406x178           | 74                   | 412.8                    | 179.7                    | 9.7         | 16.0           | 10.2                | 360.4                         | 5.62                      | 37.2    | 7                        | 96      | 28      | 1.51                        | 20.4                        |
|                   | 67                   | 409.4                    | 178.8                    | 8.8         | 14.3           | 10.2                | 360.4                         | 6.25                      | 41.0    | 6                        | 96      | 26      | 1.50                        | 22.4                        |
|                   | 60                   | 406.4                    | 177.8                    | 7.8         | 12.8           | 10.2                | 360.4                         | 6.95                      | 46.2    | 6                        | 96      | 24      | 1.49                        | 24.8                        |
|                   | 54                   | 402.6                    | 177.6                    | 7.6         | 10.9           | 10.2                | 360.4                         | 8.15                      | 47.4    | 6                        | 96      | 22      | 1.48                        | 27.5                        |
| 406x140           | 46                   | 402.3                    | 142.4                    | 6.9         | 11.2           | 10.2                | 359.5                         | 6.36                      | 52.1    | 5                        | 78      | 22      | 1.34                        | 29.2                        |
|                   | 39                   | 397.3                    | 141.8                    | 6.3         | 8.6            | 10.2                | 359.7                         | 8.24                      | 57.1    | 5                        | 78      | 20      | 1.33                        | 34.1                        |
| 356x171           | 67                   | 364.0                    | 173.2                    | 9.1         | 15.7           | 10.2                | 312.2                         | 5.52                      | 34.3    | 7                        | 94      | 26      | 1.39                        | 20.7                        |
|                   | 57                   | 358.6                    | 172.1                    | 8.0         | 13.0           | 10.2                | 312.2                         | 6.62                      | 39.0    | 6                        | 94      | 24      | 1.37                        | 24.1                        |
|                   | 51                   | 355.6                    | 171.5                    | 7.3         | 11.5           | 10.2                | 312.2                         | 7.46                      | 42.8    | 6                        | 94      | 22      | 1.37                        | 26.8                        |
|                   | 45                   | 352.0                    | 171.0                    | 6.9         | 9.7            | 10.2                | 312.2                         | 8.81                      | 45.2    | 5                        | 94      | 20      | 1.36                        | 30.1                        |
| 356x127           | 39                   | 352.8                    | 126.0                    | 6.5         | 10.7           | 10.2                | 311.0                         | 5.89                      | 47.8    | 5                        | 70      | 22      | 1.18                        | 30.2                        |
|                   | 33                   | 348.5                    | 125.4                    | 5.9         | 8.5            | 10.2                | 311.1                         | 7.38                      | 52.7    | 5                        | 70      | 20      | 1.17                        | 35.4                        |
| 305x165           | 54                   | 310.9                    | 166.8                    | 7.7         | 13.7           | 8.9                 | 265.7                         | 6.09                      | 34.5    | 6                        | 90      | 24      | 1.26                        | 23.3                        |
|                   | 46                   | 307.1                    | 165.7                    | 6.7         | 11.8           | 8.9                 | 265.7                         | 7.02                      | 39.7    | 5                        | 90      | 22      | 1.25                        | 27.1                        |
|                   | 40                   | 303.8                    | 165.1                    | 6.1         | 10.2           | 8.9                 | 265.6                         | 8.09                      | 43.5    | 5                        | 90      | 20      | 1.24                        | 31.0                        |
| 305x127           | 48                   | 310.4                    | 125.2                    | 8.9         | 14.0           | 8.9                 | 264.6                         | 4.47                      | 29.7    | 6                        | 70      | 24      | 1.09                        | 22.7                        |
|                   | 42                   | 306.6                    | 124.3                    | 8.0         | 12.1           | 8.9                 | 264.6                         | 5.14                      | 33.1    | 6                        | 70      | 22      | 1.08                        | 25.7                        |
|                   | 37                   | 303.8                    | 123.5                    | 7.2         | 10.7           | 8.9                 | 264.6                         | 5.77                      | 36.8    | 6                        | 70      | 20      | 1.07                        | 29.0                        |
| 305x102           | 33                   | 312.7                    | 102.4                    | 6.6         | 10.8           | 7.6                 | 275.9                         | 4.74                      | 41.8    | 5                        | 58      | 20      | 1.01                        | 30.6                        |
|                   | 28                   | 308.9                    | 101.9                    | 6.1         | 8.9            | 7.6                 | 275.9                         | 5.72                      | 45.2    | 5                        | 58      | 18      | 1.00                        | 35.7                        |
|                   | 25                   | 304.8                    | 101.6                    | 5.8         | 6.8            | 7.6                 | 276.0                         | 7.47                      | 47.6    | 5                        | 58      | 16      | 0.991                       | 39.7                        |
| 254x146           | 43                   | 259.6                    | 147.3                    | 7.3         | 12.7           | 7.6                 | 219.0                         | 5.90                      | 30.0    | 6                        | 82      | 22      | 1.08                        | 25.1                        |
|                   | 37                   | 256.0                    | 146.4                    | 6.4         | 10.9           | 7.6                 | 219.0                         | 6.72                      | 34.2    | 5                        | 80      | 20      | 1.07                        | 29.0                        |
|                   | 31                   | 251.5                    | 146.1                    | 6.1         | 8.6            | 7.6                 | 219.1                         | 8.49                      | 35.9    | 5                        | 82      | 18      | 1.06                        | 34.3                        |
| 254x102           | 28                   | 260.4                    | 102.1                    | 6.4         | 10.0           | 7.6                 | 225.2                         | 5.11                      | 35.2    | 5                        | 58      | 18      | 0.903                       | 32.3                        |
|                   | 25                   | 257.0                    | 101.9                    | 6.1         | 8.4            | 7.6                 | 225.0                         | 6.07                      | 36.9    | 5                        | 58      | 16      | 0.896                       | 35.9                        |
|                   | 22                   | 254.0                    | 101.5                    | 5.8         | 6.8            | 7.6                 | 225.2                         | 7.47                      | 38.8    | 5                        | 58      | 16      | 0.890                       | 40.4                        |
| 203x133           | 30                   | 206.8                    | 133.8                    | 6.3         | 9.6            | 7.6                 | 172.4                         | 6.97                      | 27.4    | 5                        | 74      | 18      | 0.923                       | 30.8                        |
|                   | 25                   | 203.2                    | 133.4                    | 5.8         | 7.8            | 7.6                 | 172.4                         | 8.55                      | 29.7    | 5                        | 74      | 16      | 0.915                       | 36.6                        |
| 203x102           | 23                   | 203.2                    | 101.6                    | 5.2         | 9.3            | 7.6                 | 169.4                         | 5.46                      | 32.6    | 5                        | 60      | 18      | 0.789                       | 34.3                        |
| 178x102           | 19                   | 177.8                    | 101.6                    | 4.7         | 7.9            | 7.6                 | 146.8                         | 6.43                      | 31.2    | 4                        | 60      | 16      | 0.740                       | 38.9                        |
| 152x89            | 16                   | 152.4                    | 88.9                     | 4.6         | 7.7            | 7.6                 | 121.8                         | 5.77                      | 26.5    | 4                        | 54      | 16      | 0.638                       | 39.9                        |
| 127x76            | 13                   | 127.0                    | 76.2                     | 4.2         | 7.6            | 7.6                 | 96.6                          | 5.01                      | 23.0    | 4                        | 46      | 16      | 0.537                       | 41.3                        |

FOR EXPLANATION OF TABLES SEE NOTE 2

UNIVERSAL BEAMS



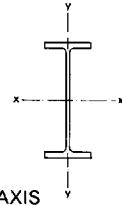
PROPERTIES

| Designation    |                   | Second Moment Of Area    |                          | Radius Of Gyration |             | Elastic Modulus          |                          | Plastic Modulus          |                          | Buckling Parameter | Torsional Index | Warping Constant  | Torsional Constant | Area of Section   |
|----------------|-------------------|--------------------------|--------------------------|--------------------|-------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------|-----------------|-------------------|--------------------|-------------------|
| Serial Size mm | Mass Per Metre kg | Axis x-x cm <sup>4</sup> | Axis y-y cm <sup>4</sup> | Axis x-x cm        | Axis y-y cm | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | u                  | x               | H dm <sup>6</sup> | J cm <sup>4</sup>  | A cm <sup>2</sup> |
|                |                   | 406x178                  | 74                       | 27430              | 1551        | 17.0                     | 4.03                     | 1329                     | 173                      | 1509               | 268             | 0.880             | 27.5               | 0.610             |
|                | 67                | 24330                    | 1365                     | 16.9               | 3.99        | 1189                     | 153                      | 1346                     | 237                      | 0.880              | 30.5            | 0.533             | 46.1               | 85.5              |
|                | 60                | 21540                    | 1201                     | 16.8               | 3.97        | 1060                     | 135                      | 1195                     | 209                      | 0.881              | 33.8            | 0.465             | 33.0               | 76.1              |
|                | 54                | 18670                    | 1019                     | 16.5               | 3.86        | 927                      | 115                      | 1051                     | 178                      | 0.872              | 38.4            | 0.391             | 22.9               | 68.6              |
| 406x140        | 46                | 15670                    | 540                      | 16.3               | 3.03        | 779                      | 75.9                     | 889                      | 119                      | 0.870              | 38.8            | 0.207             | 19.2               | 59.0              |
|                | 39                | 12410                    | 410                      | 15.9               | 2.89        | 625                      | 57.8                     | 718                      | 90.7                     | 0.859              | 47.6            | 0.155             | 10.5               | 49.2              |
| 356x171        | 67                | 19540                    | 1362                     | 15.1               | 3.99        | 1073                     | 157                      | 1213                     | 243                      | 0.886              | 24.4            | 0.413             | 55.7               | 85.5              |
|                | 57                | 16060                    | 1106                     | 14.9               | 3.91        | 896                      | 129                      | 1009                     | 198                      | 0.883              | 28.9            | 0.330             | 33.1               | 72.2              |
|                | 51                | 14160                    | 968                      | 14.8               | 3.87        | 796                      | 113                      | 895                      | 174                      | 0.882              | 32.2            | 0.287             | 23.6               | 64.6              |
|                | 45                | 12080                    | 810                      | 14.6               | 3.77        | 686                      | 94.7                     | 773                      | 146                      | 0.875              | 37.0            | 0.237             | 15.7               | 57.0              |
| 356x127        | 39                | 10100                    | 358                      | 14.3               | 2.69        | 573                      | 56.8                     | 654                      | 88.9                     | 0.872              | 35.2            | 0.105             | 14.9               | 49.4              |
|                | 33                | 8192                     | 280                      | 14.0               | 2.58        | 470                      | 44.7                     | 539                      | 70.2                     | 0.864              | 42.3            | 0.0810            | 8.65               | 41.8              |
| 305x165        | 54                | 11690                    | 1061                     | 13.1               | 3.94        | 752                      | 127                      | 843                      | 195                      | 0.891              | 23.7            | 0.234             | 34.3               | 66.2              |
|                | 46                | 9935                     | 896                      | 13.0               | 3.90        | 647                      | 108                      | 722                      | 166                      | 0.891              | 27.2            | 0.195             | 22.2               | 58.8              |
|                | 40                | 8551                     | 766                      | 12.9               | 3.85        | 563                      | 92.8                     | 626                      | 142                      | 0.888              | 31.0            | 0.165             | 14.9               | 51.6              |
| 305x127        | 48                | 9507                     | 460                      | 12.5               | 2.75        | 613                      | 73.5                     | 706                      | 116                      | 0.874              | 23.3            | 0.101             | 31.5               | 60.9              |
|                | 42                | 8159                     | 389                      | 12.4               | 2.70        | 532                      | 62.6                     | 612                      | 98.4                     | 0.872              | 26.5            | 0.0843            | 21.1               | 53.4              |
|                | 37                | 7162                     | 337                      | 12.3               | 2.67        | 471                      | 54.6                     | 540                      | 85.6                     | 0.871              | 29.6            | 0.0724            | 14.9               | 47.4              |
| 305x102        | 33                | 6501                     | 194                      | 12.5               | 2.15        | 416                      | 37.9                     | 481                      | 60.0                     | 0.866              | 31.6            | 0.0442            | 12.2               | 41.8              |
|                | 28                | 5439                     | 158                      | 12.2               | 2.08        | 352                      | 30.9                     | 408                      | 49.2                     | 0.859              | 36.9            | 0.0355            | 7.69               | 36.4              |
|                | 25                | 4364                     | 119                      | 11.8               | 1.96        | 286                      | 23.5                     | 336                      | 37.8                     | 0.844              | 44.1            | 0.0265            | 4.57               | 31.2              |
| 254x146        | 43                | 6554                     | 677                      | 10.9               | 3.51        | 505                      | 92.0                     | 568                      | 141                      | 0.890              | 21.1            | 0.103             | 24.0               | 55.0              |
|                | 37                | 5547                     | 571                      | 10.8               | 3.47        | 433                      | 78.0                     | 485                      | 119                      | 0.889              | 24.3            | 0.0857            | 15.4               | 47.4              |
|                | 31                | 4428                     | 448                      | 10.5               | 3.35        | 352                      | 61.3                     | 395                      | 94.2                     | 0.879              | 29.5            | 0.0660            | 8.65               | 39.9              |
| 254x102        | 28                | 4013                     | 178                      | 10.5               | 2.21        | 308                      | 34.9                     | 354                      | 54.8                     | 0.873              | 27.4            | 0.0279            | 9.68               | 36.3              |
|                | 25                | 3420                     | 149                      | 10.3               | 2.15        | 266                      | 29.2                     | 307                      | 46.1                     | 0.865              | 31.3            | 0.0230            | 6.52               | 32.3              |
|                | 22                | 2853                     | 119                      | 10.0               | 2.06        | 225                      | 23.5                     | 260                      | 37.3                     | 0.854              | 36.1            | 0.0182            | 4.23               | 28.3              |
| 203x133        | 30                | 2888                     | 384                      | 8.72               | 3.18        | 279                      | 57.4                     | 313                      | 88.0                     | 0.882              | 21.5            | 0.0373            | 10.2               | 38.0              |
|                | 25                | 2349                     | 309                      | 8.54               | 3.10        | 231                      | 46.3                     | 259                      | 71.2                     | 0.876              | 25.5            | 0.0295            | 6.05               | 32.2              |
| 203x102        | 23                | 2091                     | 163                      | 8.49               | 2.37        | 206                      | 32.1                     | 232                      | 49.5                     | 0.890              | 22.5            | 0.0153            | 6.87               | 29.0              |
| 178x102        | 19                | 1357                     | 138                      | 7.49               | 2.39        | 153                      | 27.2                     | 171                      | 41.9                     | 0.889              | 22.6            | 0.00998           | 4.37               | 24.2              |
| 152x89         | 16                | 838                      | 90.4                     | 6.40               | 2.10        | 110                      | 20.3                     | 124                      | 31.4                     | 0.889              | 19.5            | 0.00473           | 3.61               | 20.5              |
| 127x76         | 13                | 477                      | 56.2                     | 5.33               | 1.83        | 75.1                     | 14.7                     | 85.0                     | 22.7                     | 0.893              | 16.2            | 0.00200           | 2.92               | 16.8              |

FOR EXPLANATION OF TABLES SEE NOTE 3



UNIVERSAL BEAMS



PLASTIC MODULI-MAJOR AXIS

PLASTIC MODULI-MINOR AXIS

| Designation |                   | Plastic Modulus Axis x-x cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |       |                |                    |      |                   | Plastic Modulus Axis y-y cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |                    |      |         |    |    |
|-------------|-------------------|--|---|-------|----------------|--------------------|------|-------------------|--|---|--------------------|------|---------|----|----|
| Serial Size | Mass Per Metre kg |  | Lower Values Of n                         |       | Change Formula | Higher Values Of n |      | Lower Values Of n |  | Change Formula                            | Higher Values Of n |      |         |    |    |
|             |                   |  | K1  | K2    |                | At n =             | K3   | K4                |  |   | K1                 | K2   | At n =  | K3 | K4 |
| 914x419     | 388               | 17670                                    | 17670                                     | 28490 | 0.367          | 1463               | 14.6 | 3342              | 3342                                     | 665                                       | 0.400              | 8096 | 0.266   |    |    |
|             | 343               | 15470                                    | 15470                                     | 24630 | 0.375          | 1148               | 16.3 | 2890              | 2890                                     | 524                                       | 0.404              | 7192 | 0.250   |    |    |
| 914x305     | 289               | 12590                                    | 12590                                     | 17390 | 0.457          | 1111               | 14.4 | 1603              | 1603                                     | 368                                       | 0.492              | 5153 | 0.0864  |    |    |
|             | 253               | 10940                                    | 10940                                     | 15060 | 0.462          | 857                | 16.3 | 1371              | 1371                                     | 284                                       | 0.492              | 4498 | 0.0777  |    |    |
|             | 224               | 9533                                     | 9533                                      | 12830 | 0.479          | 675                | 18.3 | 1163              | 1163                                     | 224                                       | 0.507              | 4085 | 0.0421  |    |    |
|             | 201               | 8372                                     | 8372                                      | 10850 | 0.510          | 549                | 20.1 | 983               | 983                                      | 183                                       | 0.534              | 3877 | -0.0185 |    |    |
| 838x292     | 226               | 9155                                     | 9155                                      | 12930 | 0.444          | 712                | 16.2 | 1212              | 1212                                     | 245                                       | 0.475              | 3750 | 0.112   |    |    |
|             | 194               | 7640                                     | 7640                                      | 10360 | 0.474          | 525                | 18.8 | 974               | 974                                      | 181                                       | 0.501              | 3361 | 0.0526  |    |    |
|             | 176               | 6806                                     | 6806                                      | 8959  | 0.498          | 434                | 20.5 | 841               | 841                                      | 150                                       | 0.522              | 3173 | 0.00571 |    |    |
| 762x267     | 197               | 7164                                     | 7164                                      | 10070 | 0.447          | 589                | 15.4 | 959               | 959                                      | 204                                       | 0.479              | 2984 | 0.107   |    |    |
|             | 173               | 6195                                     | 6195                                      | 8488  | 0.466          | 458                | 17.3 | 807               | 807                                      | 159                                       | 0.495              | 2696 | 0.0694  |    |    |
|             | 147               | 5169                                     | 5169                                      | 6845  | 0.493          | 336                | 20.1 | 648               | 648                                      | 117                                       | 0.517              | 2398 | 0.0156  |    |    |
| 686x254     | 170               | 5631                                     | 5631                                      | 8106  | 0.431          | 461                | 15.3 | 811               | 811                                      | 170                                       | 0.463              | 2398 | 0.139   |    |    |
|             | 152               | 5001                                     | 5001                                      | 7135  | 0.438          | 372                | 16.9 | 710               | 710                                      | 137                                       | 0.468              | 2159 | 0.124   |    |    |
|             | 140               | 4558                                     | 4558                                      | 6419  | 0.448          | 316                | 18.3 | 638               | 638                                      | 116                                       | 0.475              | 2009 | 0.105   |    |    |
|             | 125               | 3994                                     | 3994                                      | 5435  | 0.473          | 254                | 20.3 | 542               | 542                                      | 93.8                                      | 0.497              | 1869 | 0.0552  |    |    |
| 610x305     | 238               | 7462                                     | 7462                                      | 12420 | 0.348          | 744                | 11.9 | 1576              | 1576                                     | 365                                       | 0.387              | 3590 | 0.304   |    |    |
|             | 179               | 5515                                     | 5515                                      | 9189  | 0.353          | 424                | 15.6 | 1143              | 1143                                     | 210                                       | 0.382              | 2657 | 0.295   |    |    |
|             | 149               | 4575                                     | 4575                                      | 7607  | 0.356          | 299                | 18.4 | 938               | 938                                      | 148                                       | 0.381              | 2209 | 0.269   |    |    |
| 610x229     | 140               | 4139                                     | 4139                                      | 6055  | 0.421          | 346                | 14.9 | 611               | 611                                      | 129                                       | 0.454              | 1745 | 0.159   |    |    |
|             | 125               | 3673                                     | 3673                                      | 5331  | 0.427          | 278                | 16.5 | 535               | 535                                      | 104                                       | 0.457              | 1568 | 0.146   |    |    |
|             | 113               | 3287                                     | 3287                                      | 4660  | 0.443          | 230                | 18.1 | 470               | 470                                      | 85.9                                      | 0.471              | 1456 | 0.114   |    |    |
|             | 101               | 2887                                     | 2887                                      | 3952  | 0.468          | 185                | 20.0 | 401               | 401                                      | 69.6                                      | 0.493              | 1358 | 0.0643  |    |    |
| 533x210     | 122               | 3203                                     | 3203                                      | 4748  | 0.411          | 288                | 13.7 | 500               | 500                                      | 112                                       | 0.447              | 1382 | 0.178   |    |    |
|             | 109               | 2827                                     | 2827                                      | 4154  | 0.419          | 230                | 15.3 | 435               | 435                                      | 89.3                                      | 0.451              | 1237 | 0.164   |    |    |
|             | 101               | 2619                                     | 2619                                      | 3829  | 0.423          | 200                | 16.4 | 400               | 400                                      | 77.8                                      | 0.453              | 1154 | 0.155   |    |    |
|             | 92                | 2366                                     | 2366                                      | 3406  | 0.433          | 167                | 17.8 | 356               | 356                                      | 65.2                                      | 0.461              | 1067 | 0.134   |    |    |
|             | 82                | 2058                                     | 2058                                      | 2853  | 0.459          | 132                | 19.9 | 300               | 300                                      | 51.8                                      | 0.485              | 986  | 0.0818  |    |    |
| 457x191     | 98                | 2234                                     | 2234                                      | 3442  | 0.389          | 204                | 13.3 | 379               | 379                                      | 84.0                                      | 0.425              | 977  | 0.222   |    |    |
|             | 89                | 2020                                     | 2020                                      | 3079  | 0.397          | 170                | 14.5 | 339               | 339                                      | 70.4                                      | 0.430              | 897  | 0.207   |    |    |
|             | 82                | 1832                                     | 1832                                      | 2758  | 0.405          | 143                | 15.8 | 304               | 304                                      | 59.3                                      | 0.436              | 828  | 0.191   |    |    |
|             | 74                | 1659                                     | 1659                                      | 2485  | 0.409          | 119                | 17.2 | 273               | 273                                      | 49.5                                      | 0.437              | 755  | 0.182   |    |    |
|             | 67                | 1472                                     | 1472                                      | 2151  | 0.425          | 96.9               | 19.0 | 237               | 237                                      | 40.3                                      | 0.451              | 693  | 0.151   |    |    |
| 457x152     | 82                | 1802                                     | 1802                                      | 2558  | 0.436          | 179                | 12.6 | 236               | 236                                      | 58.9                                      | 0.476              | 701  | 0.129   |    |    |
|             | 74                | 1624                                     | 1624                                      | 2285  | 0.444          | 149                | 13.8 | 209               | 209                                      | 49.0                                      | 0.480              | 642  | 0.113   |    |    |
|             | 67                | 1442                                     | 1442                                      | 2001  | 0.455          | 120                | 15.2 | 183               | 183                                      | 39.8                                      | 0.488              | 583  | 0.0915  |    |    |
|             | 60                | 1283                                     | 1283                                      | 1796  | 0.451          | 94.6               | 17.2 | 163               | 163                                      | 31.6                                      | 0.480              | 517  | 0.0991  |    |    |
|             | 52                | 1096                                     | 1096                                      | 1461  | 0.487          | 73.6               | 19.4 | 133               | 133                                      | 24.7                                      | 0.513              | 483  | 0.0266  |    |    |

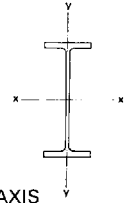
$n = F / (Ag \cdot py)$ . Where F is the factored axial load and Ag is the gross cross sectional area.

For lower values of n reduced plastic modulus(Sr) =  $K1 \cdot K2 \cdot n^2$

For higher values of n reduced plastic modulus(Sr) =  $K3(1-n)(K4 + n)$

FOR EXPLANATION OF TABLES SEE NOTE 3

UNIVERSAL BEAMS



PLASTIC MODULI-MAJOR AXIS

PLASTIC MODULI-MINOR AXIS

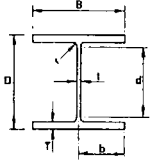
| Designation    |                   | Plastic Modulus Axis X-X cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                       |                    |      | Plastic Modulus Axis Y-Y cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                       |                    |        |
|----------------|-------------------|--|---|------|-----------------------|--------------------|------|--|---|------|-----------------------|--------------------|--------|
| Serial Size mm | Mass Per Metre kg |  | Lower Values Of n                         |      | Change Formula At n = | Higher Values Of n |      |  | Lower Values Of n                         |      | Change Formula At n = | Higher Values Of n |        |
|                |                   |  | K1  | K2   |                       | K3                 | K4   |  | K1  | K2   |                       | K3                 | K4     |
| 406x178        | 74                | 1509                                     | 1509                                      | 2342 | 0.387                 | 127                | 14.5 | 268                                      | 268                                       | 55.0 | 0.420                 | 688                | 0.227  |
|                | 67                | 1346                                     | 1346                                      | 2079 | 0.391                 | 103                | 16.0 | 237                                      | 237                                       | 44.7 | 0.421                 | 617                | 0.219  |
|                | 60                | 1195                                     | 1195                                      | 1857 | 0.390                 | 82.0               | 17.9 | 209                                      | 209                                       | 35.6 | 0.416                 | 544                | 0.222  |
|                | 54                | 1051                                     | 1051                                      | 1546 | 0.421                 | 66.7               | 19.7 | 178                                      | 178                                       | 29.2 | 0.446                 | 514                | 0.158  |
| 406x140        | 46                | 889                                      | 889                                       | 1261 | 0.443                 | 61.7               | 18.2 | 119                                      | 119                                       | 21.6 | 0.470                 | 367                | 0.114  |
|                | 39                | 718                                      | 718                                       | 962  | 0.485                 | 43.4               | 21.5 | 90.7                                     | 90.7                                      | 15.2 | 0.508                 | 328                | 0.0305 |
| 356x171        | 67                | 1213                                     | 1213                                      | 2010 | 0.353                 | 106                | 13.7 | 243                                      | 243                                       | 50.3 | 0.387                 | 563                | 0.295  |
|                | 57                | 1009                                     | 1009                                      | 1631 | 0.367                 | 76.3               | 16.0 | 198                                      | 198                                       | 36.4 | 0.397                 | 482                | 0.266  |
|                | 51                | 895                                      | 895                                       | 1430 | 0.375                 | 61.4               | 17.7 | 174                                      | 174                                       | 29.4 | 0.402                 | 434                | 0.251  |
|                | 45                | 773                                      | 773                                       | 1178 | 0.402                 | 48.1               | 19.9 | 146                                      | 146                                       | 23.1 | 0.426                 | 397                | 0.198  |
| 356x127        | 39                | 654                                      | 654                                       | 939  | 0.435                 | 49.0               | 16.8 | 88.9                                     | 88.9                                      | 17.3 | 0.464                 | 267                | 0.132  |
|                | 33                | 539                                      | 539                                       | 739  | 0.467                 | 35.4               | 19.5 | 70.2                                     | 70.2                                      | 12.5 | 0.492                 | 236                | 0.0676 |
| 305x165        | 54                | 843                                      | 843                                       | 1511 | 0.319                 | 70.0               | 14.1 | 195                                      | 195                                       | 37.4 | 0.351                 | 412                | 0.362  |
|                | 46                | 722                                      | 722                                       | 1289 | 0.323                 | 52.4               | 16.2 | 166                                      | 166                                       | 28.1 | 0.350                 | 353                | 0.356  |
|                | 40                | 626                                      | 626                                       | 1093 | 0.334                 | 40.7               | 18.3 | 142                                      | 142                                       | 22.0 | 0.359                 | 314                | 0.333  |
| 305x127        | 48                | 706                                      | 706                                       | 1041 | 0.412                 | 74.3               | 11.7 | 116                                      | 116                                       | 29.8 | 0.454                 | 318                | 0.178  |
|                | 42                | 612                                      | 612                                       | 890  | 0.422                 | 57.6               | 13.2 | 98.4                                     | 98.4                                      | 23.2 | 0.460                 | 281                | 0.157  |
|                | 37                | 540                                      | 540                                       | 782  | 0.427                 | 45.9               | 14.7 | 85.6                                     | 85.6                                      | 18.5 | 0.461                 | 250                | 0.146  |
| 305x102        | 33                | 481                                      | 481                                       | 663  | 0.458                 | 43.0               | 14.2 | 60.0                                     | 60.0                                      | 14.0 | 0.493                 | 193                | 0.0845 |
|                | 28                | 408                                      | 408                                       | 543  | 0.487                 | 32.8               | 16.1 | 49.2                                     | 49.2                                      | 10.7 | 0.518                 | 176                | 0.0275 |
|                | 25                | 336                                      | 336                                       | 420  | 0.540                 | 24.3               | 18.5 | 37.8                                     | 37.8                                      | 7.99 | 0.567                 | 167                | -0.788 |
| 254x146        | 43                | 568                                      | 568                                       | 1036 | 0.310                 | 51.5               | 12.9 | 141                                      | 141                                       | 29.1 | 0.345                 | 290                | 0.380  |
|                | 37                | 485                                      | 485                                       | 878  | 0.316                 | 38.5               | 14.7 | 119                                      | 119                                       | 21.9 | 0.346                 | 250                | 0.369  |
|                | 31                | 395                                      | 395                                       | 653  | 0.357                 | 27.5               | 17.3 | 94.2                                     | 94.2                                      | 15.8 | 0.384                 | 223                | 0.286  |
| 254x102        | 28                | 354                                      | 354                                       | 515  | 0.423                 | 32.5               | 13.5 | 54.8                                     | 54.8                                      | 12.7 | 0.459                 | 157                | 0.156  |
|                | 25                | 307                                      | 307                                       | 427  | 0.453                 | 25.8               | 15.1 | 46.1                                     | 46.1                                      | 10.1 | 0.486                 | 146                | 0.0956 |
|                | 22                | 260                                      | 260                                       | 344  | 0.492                 | 19.9               | 17.0 | 37.3                                     | 37.3                                      | 7.8  | 0.521                 | 137                | 0.0173 |
| 203x133        | 30                | 313                                      | 313                                       | 573  | 0.310                 | 27.2               | 13.5 | 88.0                                     | 88.0                                      | 17.5 | 0.343                 | 181                | 0.381  |
|                | 25                | 259                                      | 259                                       | 447  | 0.337                 | 19.6               | 15.7 | 71.2                                     | 71.2                                      | 12.7 | 0.366                 | 158                | 0.327  |
| 203x102        | 23                | 232                                      | 232                                       | 404  | 0.330                 | 20.9               | 13.1 | 49.5                                     | 49.5                                      | 10.3 | 0.364                 | 107                | 0.341  |
| 178x102        | 19                | 171                                      | 171                                       | 311  | 0.314                 | 14.5               | 13.8 | 41.9                                     | 41.9                                      | 8.21 | 0.346                 | 86.9               | 0.374  |
| 152x89         | 16                | 124                                      | 124                                       | 228  | 0.306                 | 12.0               | 12.0 | 31.4                                     | 31.4                                      | 6.89 | 0.342                 | 63.4               | 0.390  |
| 127x76         | 13                | 85.0                                     | 85.0                                      | 167  | 0.278                 | 9.38               | 10.4 | 22.7                                     | 22.7                                      | 5.54 | 0.318                 | 42.5               | 0.447  |

n = F/(Ag.py). Where F is the factored axial load and Ag is the gross cross sectional area.

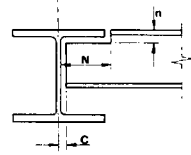
For lower values of n reduced plastic modulus(Sr) = K1-K2n<sup>2</sup>

For higher values of n reduced plastic modulus(Sr) = K3(1-n)(K4 + n)

FOR EXPLANATION OF TABLES SEE NOTE 3



UNIVERSAL COLUMNS

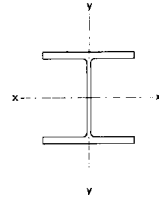


DIMENSIONS

| Designation       |                      | Depth Of Section D<br>mm | Width Of Section B<br>mm | Thickness      |                   | Root Radius<br>r<br>mm | Depth Between Fillets<br>d<br>mm | Ratios For Local Buckling |            | Dimensions For Detailing |       |    | Surface Area                |                             |
|-------------------|----------------------|--------------------------|--------------------------|----------------|-------------------|------------------------|----------------------------------|---------------------------|------------|--------------------------|-------|----|-----------------------------|-----------------------------|
| Serial Size<br>mm | Mass Per Metre<br>kg |                          |                          | Web<br>t<br>mm | Flange<br>T<br>mm |                        |                                  | Flange<br>b/T             | Web<br>d/t | End Clearance<br>C<br>mm | Notch |    | Per Metre<br>m <sup>2</sup> | Per Tonne<br>m <sup>2</sup> |
|                   |                      | N<br>mm                  | n<br>mm                  |                |                   |                        |                                  |                           |            |                          |       |    |                             |                             |
| 356x406           | 634                  | 474.7                    | 424.1                    | 47.6           | 77.0              | 15.2                   | 290.3                            | 2.75                      | 6.10       | 26                       | 200   | 94 | 2.52                        | 3.98                        |
|                   | 551                  | 455.7                    | 418.5                    | 42.0           | 67.5              | 15.2                   | 290.3                            | 3.10                      | 6.91       | 23                       | 200   | 84 | 2.48                        | 4.49                        |
|                   | 467                  | 436.6                    | 412.4                    | 35.9           | 58.0              | 15.2                   | 290.2                            | 3.56                      | 8.08       | 20                       | 200   | 74 | 2.42                        | 5.19                        |
|                   | 393                  | 419.1                    | 407.0                    | 30.6           | 49.2              | 15.2                   | 290.3                            | 4.14                      | 9.49       | 17                       | 200   | 66 | 2.38                        | 6.05                        |
|                   | 340                  | 406.4                    | 403.0                    | 26.5           | 42.9              | 15.2                   | 290.2                            | 4.70                      | 11.0       | 15                       | 200   | 60 | 2.35                        | 6.90                        |
|                   | 287                  | 393.7                    | 399.0                    | 22.6           | 36.5              | 15.2                   | 290.3                            | 5.47                      | 12.8       | 13                       | 200   | 52 | 2.31                        | 8.06                        |
|                   | 235                  | 381.0                    | 395.0                    | 18.5           | 30.2              | 15.2                   | 290.2                            | 6.54                      | 15.7       | 11                       | 200   | 46 | 2.28                        | 9.70                        |
| COLCORE           | 477                  | 427.0                    | 424.4                    | 48.0           | 53.2              | 15.2                   | 290.2                            | 3.99                      | 6.05       | 26                       | 200   | 70 | 2.43                        | 5.09                        |
| 356x368           | 202                  | 374.7                    | 374.4                    | 16.8           | 27.0              | 15.2                   | 290.3                            | 6.93                      | 17.3       | 10                       | 190   | 44 | 2.19                        | 10.8                        |
|                   | 177                  | 368.3                    | 372.1                    | 14.5           | 23.8              | 15.2                   | 290.3                            | 7.82                      | 20.0       | 9                        | 190   | 40 | 2.17                        | 12.3                        |
|                   | 153                  | 362.0                    | 370.2                    | 12.6           | 20.7              | 15.2                   | 290.2                            | 8.94                      | 23.0       | 8                        | 190   | 36 | 2.15                        | 14.1                        |
|                   | 129                  | 355.6                    | 368.3                    | 10.7           | 17.5              | 15.2                   | 290.2                            | 10.5                      | 27.1       | 7                        | 190   | 34 | 2.14                        | 16.6                        |
| 305x305           | 283                  | 365.3                    | 321.8                    | 26.9           | 44.1              | 15.2                   | 246.7                            | 3.65                      | 9.17       | 15                       | 158   | 60 | 1.94                        | 6.85                        |
|                   | 240                  | 352.6                    | 317.9                    | 23.0           | 37.7              | 15.2                   | 246.8                            | 4.22                      | 10.7       | 14                       | 158   | 54 | 1.90                        | 7.94                        |
|                   | 198                  | 339.9                    | 314.1                    | 19.2           | 31.4              | 15.2                   | 246.7                            | 5.00                      | 12.8       | 12                       | 158   | 48 | 1.87                        | 9.45                        |
|                   | 158                  | 327.2                    | 310.6                    | 15.7           | 25.0              | 15.2                   | 246.8                            | 6.21                      | 15.7       | 10                       | 158   | 42 | 1.84                        | 11.6                        |
|                   | 137                  | 320.5                    | 308.7                    | 13.8           | 21.7              | 15.2                   | 246.7                            | 7.11                      | 17.9       | 9                        | 158   | 38 | 1.82                        | 13.3                        |
|                   | 118                  | 314.5                    | 306.8                    | 11.9           | 18.7              | 15.2                   | 246.7                            | 8.20                      | 20.7       | 8                        | 158   | 34 | 1.81                        | 15.3                        |
|                   | 97                   | 307.8                    | 304.8                    | 9.9            | 15.4              | 15.2                   | 246.6                            | 9.90                      | 24.9       | 7                        | 158   | 32 | 1.79                        | 18.4                        |
| 254x254           | 167                  | 289.1                    | 264.5                    | 19.2           | 31.7              | 12.7                   | 200.3                            | 4.17                      | 10.4       | 12                       | 134   | 46 | 1.58                        | 9.44                        |
|                   | 132                  | 276.4                    | 261.0                    | 15.6           | 25.3              | 12.7                   | 200.4                            | 5.16                      | 12.8       | 10                       | 134   | 38 | 1.54                        | 11.7                        |
|                   | 107                  | 266.7                    | 258.3                    | 13.0           | 20.5              | 12.7                   | 200.3                            | 6.30                      | 15.4       | 9                        | 134   | 34 | 1.52                        | 14.2                        |
|                   | 89                   | 260.4                    | 255.9                    | 10.5           | 17.3              | 12.7                   | 200.4                            | 7.40                      | 19.1       | 7                        | 134   | 30 | 1.50                        | 16.9                        |
|                   | 73                   | 254.0                    | 254.0                    | 8.6            | 14.2              | 12.7                   | 200.2                            | 8.94                      | 23.3       | 6                        | 134   | 28 | 1.48                        | 20.3                        |
| 203x203           | 86                   | 222.3                    | 208.8                    | 13.0           | 20.5              | 10.2                   | 160.9                            | 5.09                      | 12.4       | 9                        | 108   | 32 | 1.24                        | 14.4                        |
|                   | 71                   | 215.9                    | 206.2                    | 10.3           | 17.3              | 10.2                   | 160.9                            | 5.96                      | 15.6       | 7                        | 108   | 28 | 1.22                        | 17.2                        |
|                   | 60                   | 209.6                    | 205.2                    | 9.3            | 14.2              | 10.2                   | 160.8                            | 7.23                      | 17.3       | 7                        | 108   | 26 | 1.20                        | 20.1                        |
|                   | 52                   | 206.2                    | 203.9                    | 8.0            | 12.5              | 10.2                   | 160.8                            | 8.16                      | 20.1       | 6                        | 108   | 24 | 1.19                        | 23.0                        |
|                   | 46                   | 203.2                    | 203.2                    | 7.3            | 11.0              | 10.2                   | 160.8                            | 9.24                      | 22.0       | 6                        | 108   | 22 | 1.19                        | 25.8                        |
| 152x152           | 37                   | 161.8                    | 154.4                    | 8.1            | 11.5              | 7.6                    | 123.6                            | 6.71                      | 15.3       | 6                        | 84    | 20 | 0.912                       | 24.6                        |
|                   | 30                   | 157.5                    | 152.9                    | 6.6            | 9.4               | 7.6                    | 123.5                            | 8.13                      | 18.7       | 5                        | 84    | 18 | 0.900                       | 30.0                        |
|                   | 23                   | 152.4                    | 152.4                    | 6.1            | 6.8               | 7.6                    | 123.6                            | 11.2                      | 20.3       | 5                        | 84    | 16 | 0.889                       | 38.7                        |

FOR EXPLANATION OF TABLES SEE NOTE 2

UNIVERSAL COLUMNS

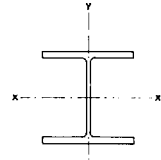


PROPERTIES

| Designation |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 | Plastic Modulus |                 | Buckling Parameter | Torsional Index | Warping Constant | Torsional Constant | Area of Section |
|-------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|------------------|--------------------|-----------------|
| Serial Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        | Axis y-y        | Axis x-x        | Axis y-y        | u                  | x               | H                | J                  | A               |
| mm          | kg             | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |                    |                 | dm <sup>6</sup>  | cm <sup>4</sup>    | cm <sup>2</sup> |
| 356x406     | 634            | 275000                | 98190           | 18.5               | 11.0     | 11590           | 4631            | 14240           | 7112            | 0.843              | 5.46            | 38.8             | 13730              | 808             |
|             | 551            | 227000                | 82670           | 18.0               | 10.9     | 9964            | 3951            | 12080           | 6057            | 0.841              | 6.06            | 31.1             | 9232               | 702             |
|             | 467            | 183100                | 67930           | 17.5               | 10.7     | 8388            | 3295            | 10010           | 5040            | 0.839              | 6.86            | 24.3             | 5817               | 595             |
|             | 393            | 146700                | 55370           | 17.1               | 10.5     | 7001            | 2721            | 8225            | 4154            | 0.837              | 7.87            | 18.9             | 3545               | 501             |
|             | 340            | 122500                | 46850           | 16.8               | 10.4     | 6029            | 2325            | 6997            | 3543            | 0.836              | 8.85            | 15.5             | 2340               | 433             |
|             | 287            | 99930                 | 38680           | 16.5               | 10.3     | 5077            | 1939            | 5814            | 2949            | 0.835              | 10.2            | 12.3             | 1441               | 366             |
|             | 235            | 79150                 | 31040           | 16.2               | 10.2     | 4155            | 1572            | 4691            | 2386            | 0.834              | 12.1            | 9.55             | 813                | 300             |
| COLCORE     | 477            | 172500                | 68090           | 16.9               | 10.6     | 8078            | 3209            | 9704            | 4981            | 0.815              | 6.90            | 23.8             | 5705               | 607             |
| 356x368     | 202            | 66330                 | 23630           | 16.0               | 9.57     | 3541            | 1262            | 3978            | 1917            | 0.843              | 13.4            | 7.14             | 561                | 258             |
|             | 177            | 57110                 | 20450           | 15.9               | 9.52     | 3101            | 1099            | 3455            | 1667            | 0.844              | 15.0            | 6.07             | 382                | 226             |
|             | 153            | 48640                 | 17510           | 15.8               | 9.46     | 2687            | 946             | 2970            | 1433            | 0.844              | 17.0            | 5.10             | 262                | 196             |
|             | 129            | 40300                 | 14580           | 15.6               | 9.39     | 2266            | 792             | 2485            | 1198            | 0.843              | 19.8            | 4.17             | 154                | 165             |
| 305x305     | 283            | 78800                 | 24540           | 14.8               | 8.25     | 4314            | 1525            | 5101            | 2337            | 0.855              | 7.65            | 6.33             | 2034               | 360             |
|             | 240            | 64150                 | 20220           | 14.5               | 8.14     | 3639            | 1272            | 4243            | 1945            | 0.854              | 8.74            | 5.01             | 1270               | 305             |
|             | 198            | 50860                 | 16240           | 14.2               | 8.02     | 2993            | 1034            | 3438            | 1577            | 0.854              | 10.2            | 3.86             | 735                | 252             |
|             | 158            | 38690                 | 12500           | 13.9               | 7.89     | 2365            | 805             | 2675            | 1225            | 0.852              | 12.5            | 2.85             | 376                | 201             |
|             | 137            | 32770                 | 10650           | 13.7               | 7.82     | 2045            | 690             | 2293            | 1049            | 0.851              | 14.2            | 2.38             | 249                | 174             |
|             | 118            | 27610                 | 9006            | 13.6               | 7.76     | 1756            | 587             | 1952            | 892             | 0.851              | 16.2            | 1.97             | 160                | 150             |
|             | 97             | 22200                 | 7272            | 13.4               | 7.68     | 1443            | 477             | 1589            | 724             | 0.850              | 19.3            | 1.55             | 91.1               | 123             |
| 254x254     | 167            | 29920                 | 9792            | 11.9               | 6.79     | 2070            | 740             | 2418            | 1131            | 0.852              | 8.49            | 1.62             | 625                | 212             |
|             | 132            | 22550                 | 7506            | 11.6               | 6.67     | 1632            | 575             | 1872            | 877             | 0.850              | 10.3            | 1.18             | 321                | 169             |
|             | 107            | 17500                 | 5894            | 11.3               | 6.57     | 1312            | 466             | 1484            | 695             | 0.848              | 12.4            | 0.893            | 173                | 137             |
|             | 89             | 14280                 | 4835            | 11.2               | 6.52     | 1097            | 378             | 1225            | 574             | 0.849              | 14.5            | 0.714            | 103                | 114             |
|             | 73             | 11370                 | 3880            | 11.1               | 6.46     | 895             | 306             | 990             | 463             | 0.849              | 17.3            | 0.558            | 57.5               | 92.9            |
| 203x203     | 86             | 9461                  | 3114            | 9.27               | 5.32     | 851             | 298             | 979             | 455             | 0.849              | 10.2            | 0.317            | 138                | 110             |
|             | 71             | 7634                  | 2530            | 9.16               | 5.28     | 707             | 245             | 801             | 373             | 0.852              | 11.9            | 0.249            | 81.0               | 90.9            |
|             | 60             | 6103                  | 2047            | 8.96               | 5.19     | 582             | 199             | 654             | 303             | 0.847              | 14.1            | 0.195            | 46.9               | 76.0            |
|             | 52             | 5254                  | 1767            | 8.90               | 5.16     | 510             | 173             | 567             | 263             | 0.848              | 15.8            | 0.166            | 31.9               | 66.4            |
|             | 46             | 4565                  | 1539            | 8.81               | 5.12     | 449             | 151             | 497             | 230             | 0.846              | 17.7            | 0.142            | 22.2               | 58.8            |
| 152x152     | 37             | 2213                  | 706             | 6.84               | 3.87     | 274             | 91.5            | 309             | 140             | 0.848              | 13.3            | 0.0399           | 19.3               | 47.3            |
|             | 30             | 1748                  | 560             | 6.75               | 3.82     | 222             | 73.3            | 248             | 112             | 0.848              | 16.0            | 0.0307           | 10.6               | 38.4            |
|             | 23             | 1258                  | 402             | 6.51               | 3.68     | 165             | 52.7            | 184             | 80.5            | 0.837              | 20.5            | 0.0213           | 4.82               | 29.7            |

FOR EXPLANATION OF TABLES SEE NOTE 3

UNIVERSAL COLUMNS

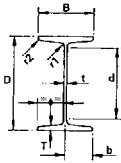


PLASTIC MODULI-MAJOR AXIS

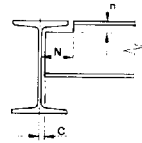
PLASTIC MODULI-MINOR AXIS

| Designation |                   | Plastic Modulus Axis x-x cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |       |                       |                    |      | Plastic Modulus Axis y-y cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                       |                    |       |
|-------------|-------------------|--|---|-------|-----------------------|--------------------|------|--|---|------|-----------------------|--------------------|-------|
| Serial Size | Mass Per Metre kg |  | Lower Values Of n                         |       | Change Formula At n = | Higher Values Of n |      |  | Lower Values Of n                         |      | Change Formula At n = | Higher Values Of n |       |
|             |                   |  | K1  | K2    |                       | K3                 | K4   |  | K1  | K2   |                       | K3                 | K4    |
| 356x406     | 634               | 14240                                    | 14240                                     | 34270 | 0.189                 | 3847               | 3.98 | 7112                                     | 7112                                      | 3436 | 0.280                 | 10520              | 0.623 |
|             | 551               | 12080                                    | 12080                                     | 29300 | 0.192                 | 2942               | 4.43 | 6057                                     | 6057                                      | 2701 | 0.273                 | 9047               | 0.617 |
|             | 467               | 10010                                    | 10010                                     | 24690 | 0.193                 | 2150               | 5.04 | 5040                                     | 5040                                      | 2030 | 0.263                 | 7574               | 0.615 |
|             | 393               | 8225                                     | 8225                                      | 20470 | 0.196                 | 1540               | 5.81 | 4154                                     | 4154                                      | 1495 | 0.256                 | 6301               | 0.609 |
|             | 340               | 6997                                     | 6997                                      | 17660 | 0.196                 | 1163               | 6.56 | 3543                                     | 3543                                      | 1152 | 0.249                 | 5391               | 0.609 |
|             | 287               | 5814                                     | 5814                                      | 14800 | 0.198                 | 839                | 7.58 | 2949                                     | 2949                                      | 849  | 0.243                 | 4517               | 0.605 |
|             | 235               | 4691                                     | 4691                                      | 12150 | 0.197                 | 570                | 9.02 | 2386                                     | 2386                                      | 590  | 0.235                 | 3659               | 0.606 |
| COLCORE     | 477               | 9704                                     | 9704                                      | 19220 | 0.253                 | 2175               | 4.96 | 4981                                     | 4981                                      | 2160 | 0.337                 | 8586               | 0.495 |
| 356x368     | 202               | 3978                                     | 3978                                      | 9908  | 0.208                 | 446                | 9.85 | 1917                                     | 1917                                      | 444  | 0.244                 | 3021               | 0.584 |
|             | 177               | 3455                                     | 3455                                      | 8775  | 0.206                 | 343                | 11.1 | 1667                                     | 1667                                      | 345  | 0.237                 | 2613               | 0.589 |
|             | 153               | 2970                                     | 2970                                      | 7594  | 0.206                 | 260                | 12.6 | 1433                                     | 1433                                      | 264  | 0.233                 | 2252               | 0.588 |
|             | 129               | 2485                                     | 2485                                      | 6376  | 0.207                 | 186                | 14.8 | 1198                                     | 1198                                      | 192  | 0.230                 | 1890               | 0.586 |
| 305x305     | 283               | 5101                                     | 5101                                      | 12070 | 0.206                 | 1010               | 5.52 | 2337                                     | 2337                                      | 889  | 0.273                 | 3626               | 0.588 |
|             | 240               | 4243                                     | 4243                                      | 10140 | 0.208                 | 735                | 6.33 | 1945                                     | 1945                                      | 661  | 0.266                 | 3040               | 0.585 |
|             | 198               | 3438                                     | 3438                                      | 8298  | 0.210                 | 508                | 7.44 | 1577                                     | 1577                                      | 469  | 0.259                 | 2485               | 0.580 |
|             | 158               | 2675                                     | 2675                                      | 6421  | 0.216                 | 326                | 9.09 | 1225                                     | 1225                                      | 308  | 0.256                 | 1964               | 0.569 |
|             | 137               | 2293                                     | 2293                                      | 5497  | 0.219                 | 247                | 10.3 | 1049                                     | 1049                                      | 237  | 0.254                 | 1696               | 0.563 |
|             | 118               | 1952                                     | 1952                                      | 4708  | 0.220                 | 184                | 11.8 | 892                                      | 892                                       | 178  | 0.250                 | 1447               | 0.562 |
|             | 97                | 1589                                     | 1589                                      | 3838  | 0.222                 | 126                | 14.1 | 724                                      | 724                                       | 123  | 0.247                 | 1183               | 0.557 |
| 254x254     | 167               | 2418                                     | 2418                                      | 5875  | 0.203                 | 427                | 6.19 | 1131                                     | 1131                                      | 390  | 0.261                 | 1749               | 0.594 |
|             | 132               | 1872                                     | 1872                                      | 4560  | 0.208                 | 273                | 7.54 | 877                                      | 877                                       | 257  | 0.256                 | 1376               | 0.584 |
|             | 107               | 1484                                     | 1484                                      | 3690  | 0.214                 | 181                | 9.05 | 695                                      | 695                                       | 175  | 0.254                 | 1108               | 0.573 |
|             | 89                | 1225                                     | 1225                                      | 3074  | 0.208                 | 127                | 10.7 | 574                                      | 574                                       | 124  | 0.241                 | 904                | 0.585 |
|             | 73                | 990                                      | 990                                       | 2510  | 0.208                 | 85.6               | 12.8 | 463                                      | 463                                       | 85.0 | 0.235                 | 731                | 0.584 |
| 203x203     | 86                | 979                                      | 979                                       | 2330  | 0.213                 | 145                | 7.42 | 455                                      | 455                                       | 136  | 0.263                 | 723                | 0.574 |
|             | 71                | 801                                      | 801                                       | 2006  | 0.205                 | 101                | 8.76 | 373                                      | 373                                       | 95.7 | 0.245                 | 582                | 0.591 |
|             | 60                | 654                                      | 654                                       | 1554  | 0.221                 | 70.7               | 10.3 | 303                                      | 303                                       | 68.9 | 0.256                 | 493                | 0.559 |
|             | 52                | 567                                      | 567                                       | 1376  | 0.218                 | 54.3               | 11.6 | 263                                      | 263                                       | 53.4 | 0.249                 | 425                | 0.565 |
|             | 46                | 497                                      | 497                                       | 1185  | 0.224                 | 42.9               | 12.9 | 230                                      | 230                                       | 42.6 | 0.252                 | 378                | 0.553 |
| 152x152     | 37                | 309                                      | 309                                       | 689   | 0.237                 | 36.3               | 9.53 | 140                                      | 140                                       | 34.5 | 0.277                 | 236                | 0.526 |
|             | 30                | 248                                      | 248                                       | 558   | 0.238                 | 24.2               | 11.5 | 112                                      | 112                                       | 23.4 | 0.271                 | 189                | 0.525 |
|             | 23                | 184                                      | 184                                       | 361   | 0.284                 | 14.6               | 14.5 | 80.5                                     | 80.5                                      | 14.5 | 0.313                 | 154                | 0.432 |

$n = F / (A_g \cdot p_y)$ . Where F is the factored axial load and  $A_g$  is the gross cross sectional area.  
 For lower values of n reduced plastic modulus( $S_r$ ) =  $K1 \cdot K2n^2$   
 For higher values of n reduced plastic modulus( $S_r$ ) =  $K3(1-n)(K4+n)$   
 FOR EXPLANATION OF TABLES SEE NOTE 3



JOISTS



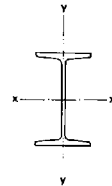
DIMENSIONS

| Designation    | Mass Per Metre kg | Depth Of Section D mm | Width Of Section B mm | Thickness |             | Root Radius r1 mm | Toe Radius r2 mm | Depth Between Fillets d mm | Ratios For Local Buckling |         | Dimensions For Detailing |       |    | Surface Area             |                          |
|----------------|-------------------|-----------------------|-----------------------|-----------|-------------|-------------------|------------------|----------------------------|---------------------------|---------|--------------------------|-------|----|--------------------------|--------------------------|
|                |                   |                       |                       | Web t mm  | Flange T mm |                   |                  |                            | Flange b/T                | Web d/t | End Clearance C mm       | Notch |    | Per Metre m <sup>2</sup> | Per Tonne m <sup>2</sup> |
| Serial Size mm |                   |                       |                       |           |             |                   |                  |                            |                           |         | N mm                     | n mm  |    |                          |                          |
| 254x203        | 81.85             | 254.0                 | 203.2                 | 10.2      | 19.9        | 19.6              | 9.7              | 166.6                      | 5.11                      | 16.3    | 7                        | 104   | 44 | 1.21                     | 14.8                     |
| 254x114        | 37.20             | 254.0                 | 114.3                 | 7.6       | 12.8        | 12.4              | 6.1              | 199.3                      | 4.46                      | 26.2    | 6                        | 60    | 28 | 0.899                    | 24.2                     |
| 203x152        | 52.09             | 203.2                 | 152.4                 | 8.9       | 16.5        | 15.5              | 7.6              | 133.2                      | 4.62                      | 15.0    | 6                        | 78    | 36 | 0.932                    | 17.9                     |
| 152x127        | 37.20             | 152.4                 | 127.0                 | 10.4      | 13.2        | 13.5              | 6.6              | 94.3                       | 4.81                      | 9.07    | 7                        | 66    | 30 | 0.737                    | 19.8                     |
| 127x114        | 29.76             | 127.0                 | 114.3                 | 10.2      | 11.5        | 9.9               | 4.8              | 79.5                       | 4.97                      | 7.79    | 7                        | 60    | 24 | 0.846                    | 21.7                     |
|                | 26.79             | 127.0                 | 114.3                 | 7.4       | 11.4        | 9.9               | 5.0              | 79.5                       | 5.01                      | 10.7    | 6                        | 60    | 24 | 0.850                    | 24.3                     |
| 114x114        | 26.79             | 114.3                 | 114.3                 | 9.5       | 10.7        | 14.2              | 3.2              | 60.8                       | 5.34                      | 6.40    | 7                        | 60    | 28 | 0.618                    | 23.1                     |
| 102x102        | 23.07             | 101.6                 | 101.6                 | 9.5       | 10.3        | 11.1              | 3.2              | 55.2                       | 4.93                      | 5.81    | 7                        | 54    | 24 | 0.549                    | 23.8                     |
| 102x44         | 7.44              | 101.6                 | 44.5                  | 4.3       | 6.1         | 6.9               | 3.3              | 74.6                       | 3.65                      | 17.3    | 4                        | 28    | 14 | 0.350                    | 47.0                     |
| 89x89          | 19.35             | 88.9                  | 88.9                  | 9.5       | 9.9         | 11.1              | 3.2              | 44.2                       | 4.49                      | 4.65    | 7                        | 46    | 24 | 0.476                    | 24.6                     |
| 76x76          | 14.67             | 76.2                  | 80.0                  | 8.9       | 8.4         | 9.4               | 4.6              | 38.1                       | 4.76                      | 4.28    | 6                        | 42    | 20 | 0.419                    | 28.5                     |
|                | 12.65             | 76.2                  | 76.2                  | 5.1       | 8.4         | 9.4               | 4.6              | 38.1                       | 4.54                      | 7.47    | 5                        | 42    | 20 | 0.411                    | 32.5                     |

◆ Check availability of section.

FOR EXPLANATION OF TABLES SEE NOTE 2

JOISTS

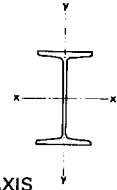


PROPERTIES

| Designation | Mass Per Metre kg | Second Moment Of Area    |                          | Radius Of Gyration |             | Elastic Modulus          |                          | Plastic Modulus          |                          | Buckling Parameter u | Torsional Index x | Warping Constant H dm <sup>6</sup> | Torsional Constant J cm <sup>4</sup> | Area of Section A cm <sup>2</sup> |
|-------------|-------------------|--------------------------|--------------------------|--------------------|-------------|--------------------------|--------------------------|--------------------------|--------------------------|----------------------|-------------------|------------------------------------|--------------------------------------|-----------------------------------|
|             |                   | Axis x-x cm <sup>4</sup> | Axis y-y cm <sup>4</sup> | Axis x-x cm        | Axis y-y cm | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> |                      |                   |                                    |                                      |                                   |
| 254x203     | 81.85             | 12020                    | 2280                     | 10.7               | 4.67        | 947                      | 224                      | 1077                     | 371                      | 0.890                | 11.0              | 0.312                              | 152                                  | 105                               |
| 254x114     | 37.20             | 5082                     | 269                      | 10.4               | 2.39        | 400                      | 47.1                     | 459                      | 79.1                     | 0.885                | 18.7              | 0.0392                             | 25.2                                 | 47.3                              |
| 203x152     | 52.09             | 4798                     | 816                      | 8.49               | 3.50        | 472                      | 107                      | 541                      | 176                      | 0.891                | 10.7              | 0.0711                             | 64.8                                 | 66.6                              |
| 152x127     | 37.20             | 1818                     | 378                      | 6.19               | 2.82        | 239                      | 59.6                     | 279                      | 99.8                     | 0.866                | 9.33              | 0.0183                             | 33.9                                 | 47.5                              |
| 127x114     | 29.76             | 979                      | 242                      | 5.12               | 2.54        | 154                      | 42.3                     | 181                      | 70.8                     | 0.853                | 8.76              | 0.00807                            | 20.8                                 | 37.4                              |
|             | 26.79             | 946                      | 236                      | 5.26               | 2.63        | 149                      | 41.3                     | 172                      | 68.2                     | 0.868                | 9.32              | 0.00788                            | 16.9                                 | 34.2                              |
| 114x114     | 26.79             | 736                      | 224                      | 4.62               | 2.55        | 129                      | 39.2                     | 151                      | 65.8                     | 0.841                | 7.92              | 0.00601                            | 18.9                                 | 34.5                              |
| 102x102     | 23.07             | 486                      | 154                      | 4.07               | 2.29        | 95.6                     | 30.3                     | 113                      | 50.6                     | 0.836                | 7.43              | 0.00321                            | 14.2                                 | 29.3                              |
| 102x44      | 7.44              | 153                      | 7.82                     | 4.01               | 0.907       | 30.1                     | 3.51                     | 35.4                     | 6.03                     | 0.872                | 14.9              | 0.000178                           | 1.25                                 | 9.50                              |
| 89x89       | 19.35             | 307                      | 101                      | 3.51               | 2.02        | 69.0                     | 22.8                     | 82.7                     | 38.0                     | 0.830                | 6.57              | 0.00158                            | 11.5                                 | 24.9                              |
| 76x76       | 14.67             | 172                      | 60.9                     | 3.00               | 1.78        | 45.2                     | 15.2                     | 54.2                     | 25.8                     | 0.820                | 6.42              | 0.000700                           | 6.83                                 | 19.1                              |
|             | 12.65             | 158                      | 51.8                     | 3.12               | 1.79        | 41.5                     | 13.6                     | 48.7                     | 22.4                     | 0.852                | 7.22              | 0.000595                           | 4.59                                 | 16.2                              |

FOR EXPLANATION OF TABLES SEE NOTE 3

**JOISTS**

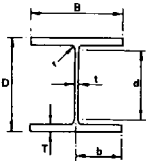


**PLASTIC MODULI-MAJOR AXIS**

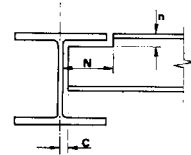
**PLASTIC MODULI-MINOR AXIS**

| Designation    |                   | Plastic Modulus Axis X-X cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                       |                    | Plastic Modulus Axis Y-Y cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                       |                    |      |       |
|----------------|-------------------|--|---|------|-----------------------|--------------------|--|---|------|-----------------------|--------------------|------|-------|
| Serial Size mm | Mass Per Metre kg |  | Lower Values Of n                         |      | Change Formula At n = | Higher Values Of n |  | Lower Values Of n                         |      | Change Formula At n = | Higher Values Of n |      |       |
|                |                   |  | K1  | K2   |                       | K3                 |  | K4  | K1   |                       | K2                 | K3   | K4    |
| 254x203        | 81.85             | 1077                                     | 1077                                      | 2677 | 0.205                 | 143                | 8.25                                     | 371                                       | 371  | 107                   | 0.248              | 573  | 0.597 |
| 254x114        | 37.20             | 459                                      | 459                                       | 737  | 0.363                 | 51.8               | 10.6                                     | 79.1                                      | 79.1 | 22.1                  | 0.408              | 185  | 0.282 |
| 203x152        | 52.09             | 541                                      | 541                                       | 1245 | 0.224                 | 76.9               | 7.80                                     | 176                                       | 176  | 54.5                  | 0.272              | 284  | 0.561 |
| 152x127        | 37.20             | 279                                      | 279                                       | 542  | 0.270                 | 47.2               | 6.67                                     | 99.8                                      | 99.8 | 37.0                  | 0.334              | 178  | 0.471 |
| 127x114        | 29.76             | 181                                      | 181                                       | 342  | 0.279                 | 32.1               | 6.38                                     | 70.8                                      | 70.8 | 27.5                  | 0.347              | 129  | 0.454 |
|                | 26.79             | 172                                      | 172                                       | 396  | 0.221                 | 27.1               | 7.02                                     | 68.2                                      | 68.2 | 23.1                  | 0.275              | 109  | 0.567 |
| 114x114        | 26.79             | 151                                      | 151                                       | 313  | 0.247                 | 28.1               | 6.00                                     | 65.8                                      | 65.8 | 26.0                  | 0.315              | 111  | 0.517 |
| 102x102        | 23.07             | 113                                      | 113                                       | 226  | 0.255                 | 22.4               | 5.64                                     | 50.6                                      | 50.6 | 21.2                  | 0.329              | 86.6 | 0.502 |
| 102x44         | 7.44              | 35.4                                     | 35.4                                      | 52.5 | 0.398                 | 5.38               | 7.97                                     | 6.03                                      | 6.03 | 2.22                  | 0.460              | 15.3 | 0.214 |
| 89x89          | 19.35             | 82.7                                     | 82.7                                      | 163  | 0.256                 | 18.4               | 5.01                                     | 38.0                                      | 38.0 | 17.4                  | 0.340              | 64.7 | 0.503 |
| 76x76          | 14.67             | 54.2                                     | 54.2                                      | 103  | 0.267                 | 12.2               | 4.98                                     | 25.8                                      | 25.8 | 12.0                  | 0.354              | 45.0 | 0.480 |
|                | 12.65             | 48.7                                     | 48.7                                      | 129  | 0.181                 | 9.26               | 5.68                                     | 22.4                                      | 22.4 | 8.66                  | 0.239              | 32.4 | 0.649 |

$n = F/(Ag.py)$ . Where F is the factored axial load and Ag is the gross cross sectional area.  
 For lower values of n reduced plastic modulus(Sr) = K1-K2n<sup>2</sup>  
 For higher values of n reduced plastic modulus(Sr) = K3(1-n)(K4+n)  
 FOR EXPLANATION OF TABLES SEE NOTE 3



**UNIVERSAL BEARING PILES**

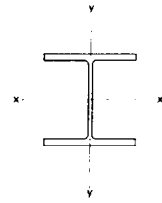


**DIMENSIONS**

| Designation    |                   | Depth Of Section D mm | Width Of Section B mm | Thickness |      | Root Radius r mm | Depth Between Fillets d mm | Ratios For Local Buckling |         | Dimensions For Detailing |       |      | Surface Area             |                          |
|----------------|-------------------|-----------------------|-----------------------|-----------|------|------------------|----------------------------|---------------------------|---------|--------------------------|-------|------|--------------------------|--------------------------|
| Serial Size mm | Mass Per Metre kg |                       |                       | t mm      | T mm |                  |                            | Flange b/T                | Web d/t | End Clearance C mm       | Notch |      | Per Metre m <sup>2</sup> | Per Tonne m <sup>2</sup> |
|                |                   |                       |                       |           |      |                  |                            |                           |         |                          | N mm  | n mm |                          |                          |
| 356x368        | 174               | 361.5                 | 378.1                 | 20.4      | 20.4 | 15.2             | 290.3                      | 9.27                      | 14.2    | 12                       | 190   | 36   | 2.17                     | 12.5                     |
|                | 152               | 356.4                 | 375.5                 | 17.9      | 17.9 | 15.2             | 290.2                      | 10.5                      | 16.2    | 11                       | 190   | 34   | 2.15                     | 14.2                     |
|                | 133               | 351.9                 | 373.3                 | 15.6      | 15.6 | 15.2             | 290.3                      | 12.0                      | 18.6    | 10                       | 190   | 32   | 2.14                     | 16.1                     |
|                | 109               | 346.4                 | 370.5                 | 12.9      | 12.9 | 15.2             | 290.2                      | 14.4                      | 22.5    | 8                        | 190   | 30   | 2.12                     | 19.5                     |
| 305x305        | 223               | 338.0                 | 325.4                 | 30.5      | 30.5 | 15.2             | 246.6                      | 5.33                      | 8.09    | 17                       | 158   | 46   | 1.89                     | 8.48                     |
|                | 186               | 328.3                 | 320.5                 | 25.6      | 25.6 | 15.2             | 246.7                      | 6.26                      | 9.64    | 15                       | 158   | 42   | 1.86                     | 10.0                     |
|                | 149               | 318.5                 | 315.6                 | 20.7      | 20.7 | 15.2             | 246.7                      | 7.62                      | 11.9    | 12                       | 158   | 36   | 1.83                     | 12.3                     |
|                | 126               | 312.4                 | 312.5                 | 17.7      | 17.7 | 15.2             | 246.6                      | 8.83                      | 13.9    | 11                       | 158   | 34   | 1.81                     | 14.4                     |
|                | 110               | 307.9                 | 310.3                 | 15.4      | 15.4 | 15.2             | 246.7                      | 10.1                      | 16.0    | 10                       | 158   | 32   | 1.80                     | 16.4                     |
|                | 95                | 303.8                 | 308.3                 | 13.4      | 13.4 | 15.2             | 246.6                      | 11.5                      | 18.4    | 9                        | 158   | 30   | 1.79                     | 18.8                     |
|                | 88                | 301.7                 | 307.2                 | 12.3      | 12.3 | 15.2             | 246.7                      | 12.5                      | 20.1    | 8                        | 158   | 28   | 1.78                     | 20.2                     |
|                | 79                | 299.2                 | 306.0                 | 11.1      | 11.1 | 15.2             | 246.6                      | 13.8                      | 22.2    | 8                        | 158   | 28   | 1.77                     | 22.5                     |
| 254x254        | 85                | 254.3                 | 259.7                 | 14.3      | 14.3 | 12.7             | 200.3                      | 9.08                      | 14.0    | 9                        | 134   | 28   | 1.50                     | 17.6                     |
|                | 71                | 249.9                 | 257.5                 | 12.1      | 12.1 | 12.7             | 200.3                      | 10.6                      | 16.6    | 8                        | 134   | 26   | 1.48                     | 20.9                     |
|                | 63                | 246.9                 | 256.0                 | 10.6      | 10.6 | 12.7             | 200.3                      | 12.1                      | 18.9    | 7                        | 134   | 24   | 1.47                     | 23.4                     |
| 203x203        | 54                | 203.9                 | 207.2                 | 11.3      | 11.3 | 10.2             | 160.9                      | 9.17                      | 14.2    | 8                        | 108   | 22   | 1.20                     | 22.2                     |
|                | 45                | 200.2                 | 205.4                 | 9.5       | 9.5  | 10.2             | 160.8                      | 10.8                      | 16.9    | 7                        | 108   | 20   | 1.19                     | 26.3                     |

FOR EXPLANATION OF TABLES SEE NOTE 2

UNIVERSAL BEARING PILES



PROPERTIES

| Designation |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 | Plastic Modulus |                 | Buckling Parameter | Torsional Index | Warping Constant  | Torsional Constant | Area of Section   |
|-------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|-------------------|--------------------|-------------------|
| Serial Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        | Axis y-y        | Axis x-x        | Axis y-y        | u                  | x               | H dm <sup>6</sup> | J cm <sup>4</sup>  | A cm <sup>2</sup> |
|             |                | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |                    |                 |                   |                    |                   |
| 356x368     | 174            | 51020                 | 18400           | 15.2               | 9.11     | 2823            | 974             | 3187            | 1494            | 0.821              | 15.8            | 5.35              | 332                | 222               |
|             | 152            | 43950                 | 15810           | 15.1               | 9.03     | 2466            | 842             | 2766            | 1290            | 0.821              | 17.8            | 4.53              | 224                | 194               |
|             | 133            | 37730                 | 13540           | 15.0               | 8.96     | 2144            | 725             | 2391            | 1109            | 0.822              | 20.2            | 3.83              | 149                | 168               |
|             | 109            | 30620                 | 10940           | 14.8               | 8.87     | 1768            | 591             | 1957            | 901             | 0.823              | 24.1            | 3.04              | 85.2               | 139               |
| 305x305     | 223            | 52840                 | 17590           | 13.6               | 7.86     | 3127            | 1081            | 3664            | 1683            | 0.826              | 9.51            | 4.16              | 955                | 285               |
|             | 186            | 42580                 | 14090           | 13.4               | 7.71     | 2594            | 879             | 3002            | 1363            | 0.827              | 11.1            | 3.23              | 562                | 237               |
|             | 149            | 33050                 | 10870           | 13.2               | 7.56     | 2075            | 689             | 2370            | 1063            | 0.828              | 13.5            | 2.41              | 296                | 190               |
|             | 126            | 27540                 | 9019            | 13.1               | 7.47     | 1763            | 577             | 1996            | 888             | 0.829              | 15.6            | 1.96              | 186                | 162               |
|             | 110            | 23650                 | 7680            | 13.0               | 7.40     | 1530            | 495             | 1720            | 760             | 0.830              | 17.7            | 1.64              | 123                | 140               |
|             | 95             | 20170                 | 6552            | 12.9               | 7.34     | 1328            | 425             | 1484            | 651             | 0.830              | 20.1            | 1.38              | 81.7               | 122               |
|             | 88             | 18380                 | 5949            | 12.8               | 7.30     | 1218            | 387             | 1356            | 593             | 0.831              | 21.7            | 1.25              | 63.6               | 112               |
|             | 79             | 16430                 | 5306            | 12.8               | 7.26     | 1098            | 347             | 1218            | 530             | 0.831              | 23.8            | 1.10              | 47.2               | 101               |
| 254x254     | 85             | 12250                 | 4181            | 10.7               | 6.22     | 963             | 322             | 1089            | 495             | 0.826              | 15.7            | 0.602             | 81.2               | 108               |
|             | 71             | 10140                 | 3448            | 10.6               | 6.15     | 812             | 268             | 910             | 411             | 0.827              | 18.2            | 0.487             | 49.5               | 91.0              |
|             | 63             | 8764                  | 2967            | 10.5               | 6.11     | 710             | 232             | 791             | 355             | 0.827              | 20.6            | 0.414             | 33.6               | 79.6              |
| 203x203     | 54             | 4979                  | 1678            | 8.54               | 4.96     | 488             | 162             | 552             | 249             | 0.827              | 15.9            | 0.156             | 32.1               | 68.2              |
|             | 45             | 4092                  | 1374            | 8.46               | 4.90     | 409             | 134             | 458             | 205             | 0.828              | 18.6            | 0.125             | 19.2               | 57.1              |

FOR EXPLANATION OF TABLES SEE NOTE 3

PLASTIC MODULI-MAJOR AXIS

PLASTIC MODULI-MINOR AXIS

| Serial Size | Mass Per Metre | Plastic Modulus Axis x-x | Reduced Value Of Modulus Under Axial Load |      |                |                    | Plastic Modulus Axis y-y | Reduced Value Of Modulus Under Axial Load |      |                |                    |      |        |
|-------------|----------------|--------------------------|---|------|----------------|--------------------|--------------------------|---|------|----------------|--------------------|------|--------|
|             |                |                          | Lower Values Of n                         |      | Change Formula | Higher Values Of n |                          | Lower Values Of n                         |      | Change Formula | Higher Values Of n |      |        |
|             |                |                          | K1  | K2   |                | At n =             |                          | K3  | K4   |                | K1                 | K2   | At n = |
| 356x368     | 174            | 3187                     | 3187                                      | 6022 | 0.294          | 326                | 11.3                     | 1494                                      | 1494 | 340            | 0.333              | 2932 | 0.412  |
|             | 152            | 2766                     | 2766                                      | 5246 | 0.295          | 251                | 12.7                     | 1290                                      | 1290 | 263            | 0.329              | 2545 | 0.410  |
|             | 133            | 2391                     | 2391                                      | 4549 | 0.296          | 191                | 14.5                     | 1109                                      | 1109 | 202            | 0.326              | 2197 | 0.408  |
|             | 109            | 1957                     | 1957                                      | 3741 | 0.297          | 132                | 17.3                     | 901                                       | 901  | 139            | 0.322              | 1794 | 0.407  |
| 305x305     | 223            | 3664                     | 3664                                      | 6656 | 0.296          | 625                | 6.70                     | 1683                                      | 1683 | 601            | 0.362              | 3257 | 0.410  |
|             | 186            | 3002                     | 3002                                      | 5486 | 0.298          | 439                | 7.85                     | 1363                                      | 1363 | 428            | 0.355              | 2674 | 0.404  |
|             | 149            | 2370                     | 2370                                      | 4360 | 0.301          | 287                | 9.53                     | 1063                                      | 1063 | 283            | 0.347              | 2112 | 0.399  |
|             | 126            | 1996                     | 1996                                      | 3690 | 0.302          | 210                | 11.0                     | 888                                       | 888  | 209            | 0.342              | 1778 | 0.396  |
|             | 110            | 1720                     | 1720                                      | 3192 | 0.303          | 160                | 12.5                     | 760                                       | 760  | 160            | 0.338              | 1530 | 0.394  |
|             | 95             | 1484                     | 1484                                      | 2764 | 0.304          | 121                | 14.2                     | 651                                       | 651  | 122            | 0.334              | 1317 | 0.393  |
|             | 88             | 1356                     | 1356                                      | 2533 | 0.304          | 103                | 15.4                     | 593                                       | 593  | 103            | 0.332              | 1202 | 0.392  |
|             | 79             | 1218                     | 1218                                      | 2282 | 0.304          | 84.1               | 16.9                     | 530                                       | 530  | 84.7           | 0.330              | 1076 | 0.392  |
| 254x254     | 85             | 1089                     | 1089                                      | 2037 | 0.298          | 113                | 11.2                     | 495                                       | 495  | 115            | 0.337              | 980  | 0.405  |
|             | 71             | 910                      | 910                                       | 1711 | 0.299          | 81.2               | 13.0                     | 411                                       | 411  | 82.9           | 0.332              | 818  | 0.403  |
|             | 63             | 791                      | 791                                       | 1494 | 0.300          | 62.6               | 14.7                     | 355                                       | 355  | 64.1           | 0.329              | 709  | 0.402  |
| 203x203     | 54             | 552                      | 552                                       | 1029 | 0.299          | 56.5               | 11.3                     | 249                                       | 249  | 57.0           | 0.338              | 495  | 0.402  |
|             | 45             | 458                      | 458                                       | 859  | 0.300          | 40.1               | 13.3                     | 205                                       | 205  | 40.8           | 0.333              | 410  | 0.400  |

$n = F/(Ag \cdot py)$ . Where F is the factored axial load and Ag is the gross cross sectional area.

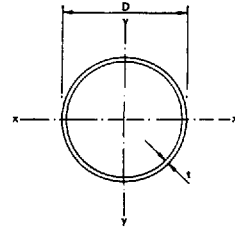
For lower values of n reduced plastic modulus(Sr) =  $K1 \cdot K2 \cdot n^2$

For higher values of n reduced plastic modulus(Sr) =  $K3(1-n)(K4 + n)$

FOR EXPLANATION OF TABLES SEE NOTE 3



**CIRCULAR HOLLOW SECTIONS**

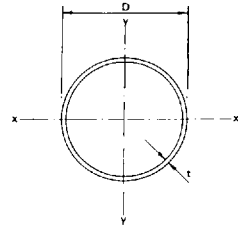


**DIMENSIONS AND PROPERTIES**

| Designation               |                    | Mass Per Metre<br>kg | Area Of Section<br>A, cm <sup>2</sup> | Ratio For Local Buckling<br>D/t | Second Moment Of Area<br>I, cm <sup>4</sup> | Radius Of Gyration<br>r, cm | Elastic Modulus<br>Z, cm <sup>3</sup> | Plastic Modulus<br>S, cm <sup>3</sup> | Torsional Constants |                    | Surface Area Per Metre<br>m <sup>2</sup> |
|---------------------------|--------------------|----------------------|---------------------------------------|---------------------------------|---|-----------------------------|---------------------------------------|---------------------------------------|---------------------|--------------------|--|
| Outside Diameter<br>D, mm | Thickness<br>t, mm |                      |                                       |                                 |   |                             |                                       |                                       | J, cm <sup>4</sup>  | C, cm <sup>3</sup> |  |
| 21.3                      | 3.2)               | 1.43                 | 1.82                                  | 6.66                            | 0.768                                       | 0.650                       | 0.722                                 | 1.06                                  | 1.54                | 1.44               | 0.0669                                   |
| 26.9                      | 3.2)               | 1.87                 | 2.38                                  | 8.41                            | 1.70  | 0.846                       | 1.27                                  | 1.81                                  | 3.40                | 2.54               | 0.0845                                   |
| 33.7                      | 2.6)               | 1.99                 | 2.54                                  | 13.0                            | 3.09  | 1.10                        | 1.84                                  | 2.52                                  | 6.18                | 3.68               | 0.106                                    |
|                           | 3.2)               | 2.41                 | 3.07                                  | 10.5                            | 3.60  | 1.08                        | 2.14                                  | 2.99                                  | 7.20                | 4.28               | 0.106                                    |
|                           | 4.0)               | 2.93                 | 3.73                                  | 8.43                            | 4.19  | 1.06                        | 2.49                                  | 3.66                                  | 8.38                | 4.96               | 0.106                                    |
| 42.4                      | 2.6)               | 2.55                 | 3.25                                  | 16.3                            | 6.46  | 1.41                        | 3.05                                  | 4.12                                  | 12.9                | 6.10               | 0.133                                    |
|                           | 3.2)               | 3.09                 | 3.94                                  | 13.2                            | 7.62  | 1.39                        | 3.59                                  | 4.93                                  | 15.2                | 7.18               | 0.133                                    |
|                           | 4.0)               | 3.79                 | 4.83                                  | 10.6                            | 8.99  | 1.36                        | 4.24                                  | 5.92                                  | 18.0                | 8.48               | 0.133                                    |
| 48.3                      | 3.2)               | 3.56                 | 4.53                                  | 15.1                            | 11.6  | 1.60                        | 4.90                                  | 6.52                                  | 23.2                | 9.60               | 0.152                                    |
|                           | 4.0)               | 4.37                 | 5.57                                  | 12.1                            | 13.8  | 1.57                        | 5.70                                  | 7.87                                  | 27.6                | 11.4               | 0.152                                    |
|                           | 5.0)               | 5.34                 | 6.80                                  | 9.66                            | 16.2  | 1.54                        | 6.69                                  | 9.42                                  | 32.4                | 13.4               | 0.152                                    |
| 60.3                      | 3.2)               | 4.51                 | 5.74                                  | 18.8                            | 23.5  | 2.02                        | 7.78                                  | 10.4                                  | 47.0                | 15.6               | 0.189                                    |
|                           | 4.0)               | 5.55                 | 7.07                                  | 15.1                            | 28.2  | 2.00                        | 9.34                                  | 12.7                                  | 56.4                | 18.7               | 0.189                                    |
|                           | 5.0)               | 6.82                 | 8.69                                  | 12.1                            | 33.5  | 1.96                        | 11.1                                  | 15.3                                  | 67.0                | 22.2               | 0.189                                    |
| 76.1                      | 3.2)               | 5.75                 | 7.33                                  | 23.8                            | 48.8  | 2.58                        | 12.8                                  | 17.0                                  | 97.6                | 25.6               | 0.239                                    |
|                           | 4.0)               | 7.11                 | 9.06                                  | 19.0                            | 59.1  | 2.55                        | 15.5                                  | 20.8                                  | 118                 | 31.0               | 0.239                                    |
|                           | 5.0)               | 8.77                 | 11.2                                  | 15.2                            | 70.9  | 2.52                        | 18.6                                  | 25.3                                  | 142                 | 37.2               | 0.239                                    |
| 88.9                      | 3.2)               | 6.76                 | 8.62                                  | 27.8                            | 79.2  | 3.03                        | 17.8                                  | 23.5                                  | 158                 | 35.6               | 0.279                                    |
|                           | 4.0)               | 8.38                 | 10.7                                  | 22.2                            | 96.3  | 3.00                        | 21.7                                  | 28.9                                  | 193                 | 43.4               | 0.279                                    |
|                           | 5.0)               | 10.3                 | 13.2                                  | 17.8                            | 116   | 2.97                        | 26.2                                  | 35.2                                  | 232                 | 52.4               | 0.279                                    |
| 114.3                     | 3.6)               | 9.83                 | 12.5                                  | 31.8                            | 192   | 3.92                        | 33.6                                  | 44.1                                  | 384                 | 67.2               | 0.359                                    |
|                           | 5.0)               | 13.5                 | 17.2                                  | 22.9                            | 257   | 3.87                        | 45.0                                  | 59.8                                  | 514                 | 90.0               | 0.359                                    |
|                           | 6.3)               | 16.8                 | 21.4                                  | 18.1                            | 313   | 3.82                        | 54.7                                  | 73.6                                  | 626                 | 109                | 0.359                                    |
| 139.7                     | 5.0)               | 16.6                 | 21.2                                  | 27.9                            | 481   | 4.77                        | 68.8                                  | 90.8                                  | 962                 | 138                | 0.439                                    |
|                           | 6.3)               | 20.7                 | 26.4                                  | 22.2                            | 589   | 4.72                        | 84.3                                  | 112                                   | 1178                | 169                | 0.439                                    |
|                           | 8.0)               | 26.0                 | 33.1                                  | 17.5                            | 720   | 4.66                        | 103                                   | 139                                   | 1440                | 206                | 0.439                                    |
| 168.3                     | 10.0)              | 32.0                 | 40.7                                  | 14.0                            | 862   | 4.60                        | 123                                   | 169                                   | 1724                | 246                | 0.439                                    |
|                           | 5.0)               | 20.1                 | 25.7                                  | 33.7                            | 856   | 5.78                        | 102                                   | 133                                   | 1712                | 204                | 0.529                                    |
|                           | 6.3)               | 25.2                 | 32.1                                  | 26.7                            | 1053  | 5.73                        | 125                                   | 165                                   | 2106                | 250                | 0.529                                    |
| 193.7                     | 8.0)               | 31.6                 | 40.3                                  | 21.0                            | 1297  | 5.67                        | 154                                   | 206                                   | 2594                | 308                | 0.529                                    |
|                           | 10.0)              | 39.0                 | 49.7                                  | 16.8                            | 1564  | 5.61                        | 186                                   | 251                                   | 3128                | 372                | 0.529                                    |
|                           | 5.0)               | 23.3                 | 29.6                                  | 38.7                            | 1320  | 6.67                        | 136                                   | 178                                   | 2640                | 272                | 0.609                                    |
| 219.1                     | 6.3)               | 29.1                 | 37.1                                  | 30.7                            | 1630  | 6.63                        | 168                                   | 221                                   | 3260                | 336                | 0.609                                    |
|                           | 8.0)               | 36.6                 | 46.7                                  | 24.2                            | 2016  | 6.57                        | 208                                   | 276                                   | 4032                | 416                | 0.609                                    |
|                           | 10.0)              | 45.3                 | 57.7                                  | 19.4                            | 2442  | 6.50                        | 252                                   | 338                                   | 4884                | 504                | 0.609                                    |
| 16.0±◆                    | 12.5               | 55.9                 | 71.2                                  | 15.5                            | 2934  | 6.42                        | 303                                   | 411                                   | 5868                | 606                | 0.609                                    |
|                           | 16.0±◆             | 70.1                 | 89.3                                  | 12.1                            | 3554  | 6.31                        | 367                                   | 507                                   | 7108                | 734                | 0.609                                    |
|                           | 20.0±◆             |                      |                                       |                                 |   |                             |                                       |                                       |                     |                    |  |
| 219.1                     | 5.0)               | 26.4                 | 33.6                                  | 43.8                            | 1928  | 7.57                        | 176                                   | 229                                   | 3856                | 352                | 0.688                                    |
|                           | 6.3)               | 33.1                 | 42.1                                  | 34.8                            | 2386  | 7.53                        | 218                                   | 285                                   | 4772                | 436                | 0.688                                    |
|                           | 8.0)               | 41.6                 | 53.1                                  | 27.4                            | 2960  | 7.47                        | 270                                   | 367                                   | 5920                | 540                | 0.688                                    |
| 16.0±◆                    | 10.0)              | 51.6                 | 65.7                                  | 21.9                            | 3698  | 7.40                        | 328                                   | 438                                   | 7196                | 656                | 0.688                                    |
|                           | 12.5               | 63.7                 | 81.1                                  | 17.5                            | 4345  | 7.32                        | 397                                   | 534                                   | 8690                | 794                | 0.688                                    |
|                           | 16.0±◆             | 80.1                 | 102                                   | 13.7                            | 5297  | 7.20                        | 483                                   | 661                                   | 10590               | 966                | 0.688                                    |
| 20.0±◆                    | 98.2               | 125                  | 11.0                                  | 6261                            | 7.07  | 572                         | 795                                   | 12520                                 | 1144                | 0.688              |  |

) Sections marked thus are rolled in grade 43C only  
 ± Sections marked thus are seamless and rolled in grade 50B only  
 ◆ Check availability of section  
 FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

CIRCULAR HOLLOW SECTIONS

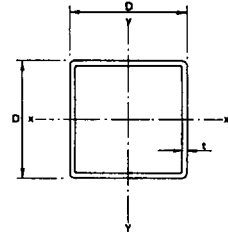


DIMENSIONS AND PROPERTIES

| Designation           | Mass Per Metre | Area Of Section | Ratio For Local Buckling | Second Moment Of Area | Radius Of Gyration | Elastic Modulus | Plastic Modulus   | Torsional Constants |                   | Surface Area Per Metre |                |
|-----------------------|----------------|-----------------|--------------------------|-----------------------|--------------------|-----------------|-------------------|---------------------|-------------------|------------------------|----------------|
|                       |                |                 |                          |                       |                    |                 |                   | J                   | C                 |                        |                |
| Outside Diameter D mm | Thickness t mm | kg              | A cm <sup>2</sup>        | D/t                   | I cm <sup>4</sup>  | r cm            | Z cm <sup>3</sup> | S cm <sup>3</sup>   | J cm <sup>4</sup> | C cm <sup>3</sup>      | m <sup>2</sup> |
| 244.5                 | 6.3            | 37.0            | 47.1                     | 38.8                  | 3346               | 8.42            | 274               | 358                 | 6692              | 548                    | 0.768          |
|                       | 8.0            | 46.7            | 59.4                     | 30.6                  | 4160               | 8.37            | 340               | 448                 | 8320              | 680                    | 0.768          |
|                       | 10.0           | 57.8            | 73.7                     | 24.5                  | 5073               | 8.30            | 415               | 550                 | 10150             | 830                    | 0.768          |
|                       | 12.5           | 71.5            | 91.1                     | 19.6                  | 6147               | 8.21            | 503               | 673                 | 12290             | 1006                   | 0.768          |
|                       | 16.0           | 90.2            | 115                      | 15.3                  | 7533               | 8.10            | 616               | 837                 | 15070             | 1232                   | 0.768          |
|                       | 20.0 ‡         | 111             | 141                      | 12.2                  | 8957               | 7.97            | 733               | 1011                | 17910             | 1466                   | 0.768          |
| 25.0 ‡                | 135            | 172             | 9.78                     | 10520                 | 7.81               | 860             | 1210              | 21040               | 1720              | 0.768                  |                |
| 273.0                 | 6.3            | 41.4            | 52.8                     | 43.3                  | 4696               | 9.43            | 344               | 448                 | 9392              | 688                    | 0.858          |
|                       | 8.0            | 52.3            | 66.6                     | 34.1                  | 5852               | 9.37            | 429               | 562                 | 11700             | 858                    | 0.858          |
|                       | 10.0           | 64.9            | 82.6                     | 27.3                  | 7154               | 9.31            | 524               | 692                 | 14310             | 1048                   | 0.858          |
|                       | 12.5           | 80.3            | 102                      | 21.8                  | 8697               | 9.22            | 637               | 849                 | 17390             | 1274                   | 0.858          |
|                       | 16.0           | 101             | 129                      | 17.1                  | 10710              | 9.10            | 784               | 1058                | 21420             | 1568                   | 0.858          |
|                       | 20.0 ‡         | 125             | 159                      | 13.6                  | 12800              | 8.97            | 938               | 1283                | 25600             | 1876                   | 0.858          |
| 25.0 ‡                | 153            | 195             | 10.9                     | 15130                 | 8.81               | 1108            | 1543              | 30260               | 2216              | 0.858                  |                |
| 323.9                 | 6.3            | 49.3            | 62.9                     | 51.4                  | 7929               | 11.2            | 490               | 636                 | 15860             | 980                    | 1.02           |
|                       | 8.0            | 62.3            | 79.4                     | 40.5                  | 9910               | 11.2            | 612               | 799                 | 19820             | 1224                   | 1.02           |
|                       | 10.0           | 77.4            | 98.6                     | 32.4                  | 12160              | 11.1            | 751               | 986                 | 24320             | 1502                   | 1.02           |
|                       | 12.5           | 96.0            | 122                      | 25.9                  | 14850              | 11.0            | 917               | 1213                | 29700             | 1834                   | 1.02           |
|                       | 16.0           | 121             | 155                      | 20.2                  | 18390              | 10.9            | 1136              | 1518                | 36780             | 2272                   | 1.02           |
|                       | 20.0 ‡         | 150             | 191                      | 16.2                  | 22140              | 10.8            | 1367              | 1850                | 44280             | 2734                   | 1.02           |
| 25.0 ‡                | 184            | 235             | 13.0                     | 26400                 | 10.6               | 1630            | 2239              | 52800               | 3260              | 1.02                   |                |
| 355.6                 | 8.0            | 68.6            | 87.4                     | 44.5                  | 13200              | 12.3            | 742               | 967                 | 26400             | 1484                   | 1.12           |
|                       | 10.0           | 85.2            | 109                      | 35.6                  | 16220              | 12.2            | 912               | 1195                | 32440             | 1824                   | 1.12           |
|                       | 12.5           | 106             | 135                      | 28.4                  | 19850              | 12.1            | 1117              | 1472                | 39700             | 2234                   | 1.12           |
|                       | 16.0           | 134             | 171                      | 22.2                  | 24660              | 12.0            | 1367              | 1847                | 49320             | 2774                   | 1.12           |
|                       | 20.0 ‡         | 166             | 211                      | 17.8                  | 29790              | 11.9            | 1676              | 2255                | 59580             | 3352                   | 1.12           |
|                       | 25.0 ‡         | 204             | 260                      | 14.2                  | 35680              | 11.7            | 2007              | 2738                | 71360             | 4014                   | 1.12           |
| 406.4                 | 10.0           | 97.8            | 125                      | 40.6                  | 24480              | 14.0            | 1205              | 1572                | 48960             | 2410                   | 1.28           |
|                       | 12.5           | 121             | 155                      | 32.5                  | 30030              | 13.9            | 1478              | 1940                | 60060             | 2956                   | 1.28           |
|                       | 16.0           | 154             | 196                      | 25.4                  | 37450              | 13.8            | 1843              | 2440                | 74900             | 3686                   | 1.28           |
|                       | 20.0 ‡         | 191             | 243                      | 20.3                  | 45430              | 13.7            | 2236              | 2989                | 90860             | 4472                   | 1.28           |
|                       | 25.0 ‡         | 235             | 300                      | 16.3                  | 54700              | 13.5            | 2692              | 3642                | 109400            | 5384                   | 1.28           |
|                       | 32.0 ‡         | 295             | 376                      | 12.7                  | 66430              | 13.3            | 3269              | 4497                | 132900            | 6538                   | 1.28           |
| 457.0                 | 10.0           | 110             | 140                      | 45.7                  | 35090              | 15.8            | 1536              | 1998                | 70180             | 3072                   | 1.44           |
|                       | 12.5           | 137             | 175                      | 36.6                  | 43140              | 15.7            | 1888              | 2470                | 86280             | 3776                   | 1.44           |
|                       | 16.0           | 174             | 222                      | 28.6                  | 53960              | 15.6            | 2361              | 3113                | 107900            | 4722                   | 1.44           |
|                       | 20.0 ‡         | 216             | 275                      | 22.9                  | 65680              | 15.5            | 2874              | 3822                | 131400            | 5748                   | 1.44           |
|                       | 25.0 ‡         | 266             | 339                      | 18.3                  | 79420              | 15.3            | 3475              | 4671                | 158800            | 6950                   | 1.44           |
|                       | 32.0 ‡         | 335             | 427                      | 14.3                  | 97010              | 15.1            | 4246              | 5791                | 194000            | 8492                   | 1.44           |
| 40.0 ‡                | 411            | 524             | 11.4                     | 114900                | 14.8               | 5031            | 6977              | 229800              | 10060             | 1.44                   |                |
| 508.0                 | 10.0           | 123             | 156                      | 50.8                  | 48520              | 17.6            | 1910              | 2480                | 97040             | 3820                   | 1.60           |
|                       | 12.5           | 153             | 195                      | 40.6                  | 59760              | 17.5            | 2353              | 3070                | 119500            | 4706                   | 1.60           |
|                       | 16.0           | 194             | 247                      | 31.7                  | 74910              | 17.4            | 2949              | 3874                | 149800            | 5898                   | 1.60           |
|                       | 20.0 ‡         | 241             | 307                      | 25.4                  | 91430              | 17.3            | 3600              | 4766                | 182900            | 7200                   | 1.60           |
|                       | 25.0 ‡         | 298             | 379                      | 20.3                  | 110900             | 17.1            | 4367              | 5837                | 221800            | 8734                   | 1.60           |
|                       | 32.0 ‡         | 376             | 479                      | 15.9                  | 136100             | 16.9            | 5360              | 7261                | 272200            | 10720                  | 1.60           |
| 40.0 ‡                | 462            | 588             | 12.7                     | 162200                | 16.6               | 6385            | 8782              | 324400              | 12770             | 1.60                   |                |
| 50.0 ‡                | 565            | 719             | 10.2                     | 190900                | 16.3               | 7515            | 10530             | 381800              | 15030             | 1.60                   |                |

+ Sections marked thus are not included in BS4848: Part 2  
 ‡ Sections marked thus are seamless and rolled in grade 50B only  
 † Check availability of section  
 FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

**SQUARE HOLLOW SECTIONS**

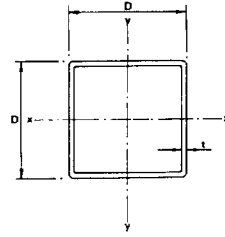


**DIMENSIONS AND PROPERTIES**

| Designation  |                   | Mass Per Metre<br>kg | Area Of Section<br>$A_2$<br>cm <sup>2</sup> | Ratio For Local Buckling<br>d/t | Second Moment Of Area<br>I<br>cm <sup>4</sup> | Radius Of Gyration<br>r<br>cm | Elastic Modulus<br>Z<br>cm <sup>3</sup> | Plastic Modulus<br>S<br>cm <sup>3</sup> | Torsional Constants  |                      | Surface Area Per Metre<br>m <sup>2</sup> |
|--------------|-------------------|----------------------|---|---------------------------------|---|-------------------------------|---|---|----------------------|----------------------|--|
| Size<br>D mm | Thickness<br>t mm |                      |   |                                 |   |                               |   |   | J<br>cm <sup>4</sup> | C<br>cm <sup>3</sup> |  |
| 20x20        | 2.0               | 1.12                 | 1.42  | 7.00                            | 0.759   | 0.731                         | 0.759                                   | 0.951                                   | 1.22                 | 1.07                 | 0.0757                                   |
|              | 2.5               | 1.35                 | 1.72  | 5.00                            | 0.865   | 0.709                         | 0.865                                   | 1.12                                    | 1.41                 | 1.21                 | 0.0746                                   |
| 25x25        | 2.0               | 1.43                 | 1.82  | 9.50                            | 1.59  | 0.935                         | 1.27                                    | 1.56                                    | 2.52                 | 1.81                 | 0.0957                                   |
|              | 2.5               | 1.74                 | 2.22  | 7.00                            | 1.85  | 0.914                         | 1.48                                    | 1.86                                    | 2.97                 | 2.09                 | 0.0946                                   |
|              | 3.0               | 2.04                 | 2.60  | 5.33                            | 2.06  | 0.892                         | 1.65                                    | 2.12                                    | 3.36                 | 2.31                 | 0.0936                                   |
|              | 3.2               | 2.15                 | 2.74  | 4.81                            | 2.14  | 0.883                         | 1.71                                    | 2.21                                    | 3.49                 | 2.38                 | 0.0931                                   |
| 30x30        | 2.5               | 2.14                 | 2.72  | 9.00                            | 3.40  | 1.12                          | 2.27                                    | 2.79                                    | 5.40                 | 3.22                 | 0.115                                    |
|              | 3.0               | 2.51                 | 3.20  | 7.00                            | 3.84  | 1.10                          | 2.56                                    | 3.21                                    | 6.17                 | 3.61                 | 0.114                                    |
|              | 3.2               | 2.65                 | 3.38  | 6.38                            | 4.00  | 1.09                          | 2.67                                    | 3.37                                    | 6.45                 | 3.75                 | 0.113                                    |
| 40x40        | 2.5               | 2.92                 | 3.72  | 13.0                            | 8.67  | 1.53                          | 4.33                                    | 5.21                                    | 13.6                 | 6.23                 | 0.155                                    |
|              | 3.0               | 3.45                 | 4.40  | 10.3                            | 9.96  | 1.51                          | 4.98                                    | 6.07                                    | 15.7                 | 7.11                 | 0.154                                    |
|              | 3.2               | 3.66                 | 4.66  | 9.50                            | 10.4  | 1.50                          | 5.22                                    | 6.40                                    | 16.5                 | 7.43                 | 0.153                                    |
|              | 4.0               | 4.46                 | 5.68  | 7.00                            | 12.1  | 1.46                          | 6.07                                    | 7.61                                    | 19.5                 | 8.56                 | 0.151                                    |
|              | 5.0               | 5.40                 | 6.88  | 5.00                            | 13.8  | 1.42                          | 6.92                                    | 8.92                                    | 22.6                 | 9.65                 | 0.149                                    |
| 50x50        | 2.5               | 3.71                 | 4.72  | 17.0                            | 17.7  | 1.94                          | 7.07                                    | 8.38                                    | 27.4                 | 10.2                 | 0.195                                    |
|              | 3.0               | 4.39                 | 5.60  | 13.7                            | 20.5  | 1.91                          | 8.20                                    | 9.83                                    | 32.0                 | 11.8                 | 0.194                                    |
|              | 3.2               | 4.66                 | 5.94  | 12.6                            | 21.6  | 1.91                          | 8.62                                    | 10.4                                    | 33.8                 | 12.4                 | 0.193                                    |
|              | 4.0               | 5.72                 | 7.28  | 9.50                            | 25.5  | 1.87                          | 10.2                                    | 12.5                                    | 40.4                 | 14.5                 | 0.191                                    |
|              | 5.0               | 6.97                 | 8.88  | 7.00                            | 29.6  | 1.83                          | 11.9                                    | 14.9                                    | 47.6                 | 16.7                 | 0.189                                    |
|              | 6.3               | 8.49                 | 10.8  | 4.94                            | 33.9  | 1.77                          | 13.6                                    | 17.5                                    | 55.3                 | 18.9                 | 0.186                                    |
| 60x60        | 3.0               | 5.34                 | 6.80  | 17.0                            | 36.6  | 2.32                          | 12.2                                    | 14.5                                    | 56.9                 | 17.7                 | 0.234                                    |
|              | 3.2               | 5.67                 | 7.22  | 15.7                            | 38.7  | 2.31                          | 12.9                                    | 15.3                                    | 60.1                 | 18.6                 | 0.233                                    |
|              | 4.0               | 6.97                 | 8.88  | 12.0                            | 46.1  | 2.28                          | 15.4                                    | 18.6                                    | 72.4                 | 22.1                 | 0.231                                    |
|              | 5.0               | 8.54                 | 10.9  | 9.00                            | 54.4  | 2.24                          | 18.1                                    | 22.3                                    | 86.3                 | 25.8                 | 0.229                                    |
|              | 6.3               | 10.5                 | 13.3  | 6.52                            | 63.4  | 2.18                          | 21.1                                    | 26.6                                    | 102                  | 29.7                 | 0.226                                    |
|              | 8.0               | 12.8                 | 16.3  | 4.50                            | 72.4  | 2.11                          | 24.1                                    | 31.4                                    | 119                  | 33.5                 | 0.223                                    |
| 70x70        | 3.0               | 6.28                 | 8.00  | 20.3                            | 59.6  | 2.73                          | 17.0                                    | 20.0                                    | 92.1                 | 24.8                 | 0.274                                    |
|              | 3.6               | 7.46                 | 9.50  | 16.4                            | 69.5  | 2.70                          | 19.9                                    | 23.6                                    | 108                  | 28.7                 | 0.272                                    |
|              | 5.0               | 10.1                 | 12.9  | 11.0                            | 90.1  | 2.64                          | 25.7                                    | 31.2                                    | 142                  | 36.8                 | 0.269                                    |
|              | 6.3               | 12.5                 | 15.9  | 8.11                            | 106   | 2.59                          | 30.4                                    | 37.6                                    | 169                  | 43.0                 | 0.266                                    |
|              | 8.0               | 15.3                 | 19.5  | 5.75                            | 123   | 2.51                          | 35.3                                    | 45.0                                    | 200                  | 49.4                 | 0.263                                    |
| 80x80        | 3.0               | 7.22                 | 9.20  | 23.7                            | 90.6  | 3.14                          | 22.7                                    | 26.5                                    | 139                  | 33.1                 | 0.314                                    |
|              | 3.6               | 8.59                 | 10.9  | 19.2                            | 106   | 3.11                          | 26.5                                    | 31.3                                    | 164                  | 38.5                 | 0.312                                    |
|              | 5.0               | 11.7                 | 14.9  | 13.0                            | 139   | 3.05                          | 34.7                                    | 41.7                                    | 217                  | 49.8                 | 0.309                                    |
|              | 6.3               | 14.4                 | 18.4  | 9.70                            | 165   | 3.00                          | 41.3                                    | 50.5                                    | 261                  | 58.8                 | 0.306                                    |
|              | 8.0               | 17.8                 | 22.7  | 7.00                            | 194   | 2.92                          | 48.6                                    | 60.9                                    | 312                  | 68.5                 | 0.303                                    |
| 90x90        | 3.6               | 9.27                 | 12.4  | 22.0                            | 154   | 3.52                          | 34.1                                    | 40.0                                    | 237                  | 49.7                 | 0.352                                    |
|              | 5.0               | 13.3                 | 16.9  | 15.0                            | 202   | 3.46                          | 45.0                                    | 53.6                                    | 315                  | 64.9                 | 0.349                                    |
|              | 6.3               | 16.4                 | 20.9  | 11.3                            | 242   | 3.41                          | 53.9                                    | 65.3                                    | 381                  | 77.1                 | 0.346                                    |
|              | 8.0               | 20.4                 | 25.9  | 8.25                            | 288   | 3.33                          | 64.0                                    | 79.2                                    | 459                  | 90.7                 | 0.343                                    |
| 100x100      | 4.0               | 12.0                 | 15.3  | 22.0                            | 234   | 3.91                          | 46.8                                    | 54.9                                    | 361                  | 68.2                 | 0.391                                    |
|              | 5.0               | 14.8                 | 18.9  | 17.0                            | 283   | 3.87                          | 56.6                                    | 67.1                                    | 439                  | 81.9                 | 0.389                                    |
|              | 6.3               | 18.4                 | 23.4  | 12.9                            | 341   | 3.81                          | 68.2                                    | 82.0                                    | 533                  | 97.9                 | 0.386                                    |
|              | 8.0               | 22.9                 | 29.1  | 9.50                            | 408   | 3.74                          | 81.5                                    | 99.9                                    | 646                  | 116                  | 0.383                                    |
|              | 10.0              | 27.9                 | 35.5  | 7.00                            | 474   | 3.65                          | 94.9                                    | 119                                     | 761                  | 134                  | 0.379                                    |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

SQUARE HOLLOW SECTIONS



DIMENSIONS AND PROPERTIES

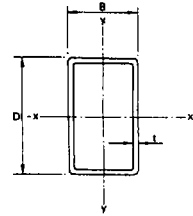
| Designation |           | Mass<br>Per<br>Metre<br>kg | Area<br>Of<br>Section<br>A<br>cm <sup>2</sup> | Ratio<br>For<br>Local<br>Buckling<br>d/t | Second Moment<br>Of Area<br>I<br>cm <sup>4</sup> | Radius<br>Of Gyration<br>r<br>cm | Elastic<br>Modulus<br>Z<br>cm <sup>3</sup> | Plastic<br>Modulus<br>S <sub>c</sub><br>cm <sup>3</sup> | Torsional<br>Constants |                      | Surface<br>Area<br>Per<br>Metre<br>m <sup>2</sup> |
|-------------|-----------|----------------------------|---|--|--|----------------------------------|--|---|------------------------|----------------------|---|
| Size        | Thickness |                            |   |  |  |                                  |  |   | J<br>cm <sup>4</sup>   | C<br>cm <sup>3</sup> |   |
| D           | t         |                            |   |  |  |                                  |  |   |                        |                      |   |
| D<br>mm     | t<br>mm   |                            |   |  |  |                                  |  |   |                        |                      |   |
| 120x120     | 5.0       | 18.0                       | 22.9  | 21.0                                     | 503  | 4.69                             | 83.8                                       | 98.4  | 775                    | 122                  | 0.469   |
|             | 6.3       | 22.3                       | 28.5  | 16.0                                     | 610  | 4.63                             | 102  | 121   | 949                    | 147                  | 0.466   |
|             | 8.0       | 27.9                       | 35.5  | 12.0                                     | 738  | 4.56                             | 123  | 149   | 1159                   | 176                  | 0.463   |
|             | 10.0      | 34.2                       | 43.5  | 9.00                                     | 870  | 4.47                             | 145  | 178   | 1381                   | 206                  | 0.459   |
|             | 12.5      | 41.6                       | 53.0  | 6.60                                     | 1009   | 4.36                             | 168  | 212   | 1624                   | 237                  | 0.453   |
| 140x140     | 5.0+      | 21.1                       | 26.9  | 25.0                                     | 814  | 5.50                             | 116  | 136   | 1251                   | 170                  | 0.549   |
|             | 6.3+      | 26.3                       | 33.5  | 19.2                                     | 994  | 5.45                             | 142  | 168   | 1538                   | 206                  | 0.546   |
|             | 8.0+      | 32.9                       | 41.9  | 14.5                                     | 1212   | 5.38                             | 173  | 207   | 1889                   | 249                  | 0.543   |
|             | 10.0+     | 40.4                       | 51.5  | 11.0                                     | 1441   | 5.29                             | 206  | 250   | 2269                   | 294                  | 0.539   |
|             | 12.5+     | 49.5                       | 63.0  | 8.20                                     | 1691   | 5.18                             | 242  | 299   | 2695                   | 342                  | 0.533   |
| 150x150     | 5.0       | 22.7                       | 28.9  | 27.0                                     | 1009   | 5.91                             | 135  | 157   | 1548                   | 197                  | 0.589   |
|             | 6.3       | 28.3                       | 36.0  | 20.8                                     | 1236   | 5.86                             | 165  | 194   | 1907                   | 240                  | 0.586   |
|             | 8.0       | 35.4                       | 45.1  | 15.7                                     | 1510   | 5.78                             | 201  | 240   | 2348                   | 291                  | 0.583   |
|             | 10.0      | 43.6                       | 55.5  | 12.0                                     | 1803   | 5.70                             | 240  | 290   | 2829                   | 345                  | 0.579   |
|             | 12.5      | 53.4                       | 68.0  | 9.00                                     | 2125   | 5.59                             | 283  | 348   | 3372                   | 403                  | 0.573   |
| 16.0        | 66.4      | 84.5                       | 6.38  | 2500                                     | 5.44   | 333                              | 421  | 4029  | 468                    | 0.566                |   |
| 160x160     | 5.0+      | 24.2                       | 30.9  | 29.0                                     | 1234   | 6.32                             | 154  | 179   | 1890                   | 226                  | 0.629   |
|             | 6.0+      | 28.9                       | 36.8  | 23.7                                     | 1450   | 6.28                             | 181  | 212   | 2230                   | 264                  | 0.627   |
|             | 6.3+      | 30.3                       | 38.5  | 22.4                                     | 1513   | 6.27                             | 189  | 222   | 2330                   | 276                  | 0.626   |
|             | 8.0+      | 37.9                       | 48.3  | 17.0                                     | 1853   | 6.19                             | 232  | 275   | 2875                   | 335                  | 0.623   |
|             | 10.0+     | 46.7                       | 59.5  | 13.0                                     | 2219   | 6.11                             | 277  | 333   | 3473                   | 399                  | 0.619   |
| 12.5+       | 57.3      | 73.0                       | 9.80  | 2627                                     | 6.00   | 328                              | 402  | 4154  | 468                    | 0.613                |   |
| 180x180     | 6.3       | 34.2                       | 43.6  | 25.6                                     | 2186   | 7.08                             | 243  | 283   | 3357                   | 355                  | 0.706   |
|             | 8.0       | 43.0                       | 54.7  | 19.5                                     | 2689   | 7.01                             | 299  | 352   | 4156                   | 434                  | 0.703   |
|             | 10.0      | 53.0                       | 67.5  | 15.0                                     | 3237   | 6.92                             | 360  | 429   | 5041                   | 519                  | 0.699   |
|             | 12.5      | 65.2                       | 83.0  | 11.4                                     | 3856   | 6.82                             | 428  | 519   | 6062                   | 613                  | 0.693   |
|             | 16.0      | 81.4                       | 104   | 8.25                                     | 4607   | 6.66                             | 512  | 634   | 7339                   | 725                  | 0.686   |
| 200x200     | 5.0+      | 30.5                       | 38.9  | 37.0                                     | 2460   | 7.95                             | 246  | 284   | 3752                   | 362                  | 0.789   |
|             | 6.3       | 38.2                       | 48.6  | 28.7                                     | 3033   | 7.90                             | 303  | 353   | 4647                   | 444                  | 0.786   |
|             | 8.0       | 48.0                       | 61.1  | 22.0                                     | 3744   | 7.83                             | 374  | 439   | 5770                   | 545                  | 0.783   |
|             | 10.0      | 59.3                       | 75.5  | 17.0                                     | 4525   | 7.74                             | 452  | 536   | 7020                   | 655                  | 0.779   |
|             | 12.5      | 73.0                       | 93.0  | 13.0                                     | 5419   | 7.63                             | 542  | 651   | 8479                   | 779                  | 0.773   |
| 16.0        | 91.5      | 117                        | 9.50  | 6524                                     | 7.48   | 652                              | 799  | 10330   | 929                    | 0.766                |   |
| 250x250     | 6.3       | 48.1                       | 61.2  | 36.7                                     | 6049   | 9.94                             | 484  | 559   | 9228                   | 712                  | 0.986   |
|             | 8.0       | 60.5                       | 77.1  | 28.2                                     | 7510   | 9.87                             | 601  | 699   | 11510                  | 890                  | 0.983   |
|             | 10.0      | 75.0                       | 95.5  | 22.0                                     | 9141   | 9.78                             | 731  | 858   | 14090                  | 1065                 | 0.979   |
|             | 12.5      | 92.6                       | 118   | 17.0                                     | 11050  | 9.68                             | 884  | 1048  | 17146                  | 1279                 | 0.973   |
|             | 16.0      | 117                        | 149   | 12.6                                     | 13480  | 9.53                             | 1078                                       | 1298  | 21110                  | 1548                 | 0.966   |
| 300x300     | 6.3+      | 57.9                       | 73.8  | 44.6                                     | 10600  | 12.0                             | 706  | 812   | 16120                  | 1043                 | 1.19  |
|             | 8.0       | 73.1                       | 93.1  | 34.5                                     | 13210  | 11.9                             | 881  | 1018  | 20170                  | 1294                 | 1.18  |
|             | 10.0      | 90.7                       | 116   | 27.0                                     | 16150  | 11.8                             | 1077                                       | 1254  | 24780                  | 1575                 | 1.18  |
|             | 12.5      | 112                        | 143   | 21.0                                     | 19630  | 11.7                             | 1309                                       | 1538  | 30290                  | 1905                 | 1.17  |
|             | 16.0      | 142                        | 181   | 15.7                                     | 24160  | 11.6                             | 1610                                       | 1916  | 37570                  | 2327                 | 1.17  |
| 350x350     | 8.0       | 85.7                       | 109   | 40.7                                     | 21240  | 14.0                             | 1214                                       | 1398  | 32350                  | 1789                 | 1.38  |
|             | 10.0      | 106                        | 136   | 32.0                                     | 26050  | 13.9                             | 1489                                       | 1725  | 39840                  | 2186                 | 1.38  |
|             | 12.5      | 132                        | 168   | 25.0                                     | 31810  | 13.8                             | 1817                                       | 2122  | 48870                  | 2655                 | 1.37  |
|             | 16.0      | 167                        | 213   | 18.9                                     | 39370  | 13.6                             | 2250                                       | 2655  | 60900                  | 3265                 | 1.37  |
| 400x400     | 10.0      | 122                        | 156   | 37.0                                     | 39350  | 15.9                             | 1968                                       | 2272  | 60030                  | 2896                 | 1.58  |
|             | 12.5      | 152                        | 193   | 29.0                                     | 48190  | 15.8                             | 2409                                       | 2800  | 73820                  | 3530                 | 1.57  |
|             | 16.0      | 192                        | 245   | 22.0                                     | 59910  | 15.7                             | 2995                                       | 3514  | 92310                  | 4363                 | 1.57  |
|             | 20.0±     | 237                        | 302   | 17.0                                     | 72390  | 15.5                             | 3620                                       | 4292  | 112300                 | 5240                 | 1.56  |

+ Sections marked thus are not included in BS4848: Part 2

± Sections marked thus are rolled in grade 50C only

FOR EXPLANATIONS OF TABLES SEE NOTES 2 AND 3

**RECTANGULAR HOLLOW SECTIONS**

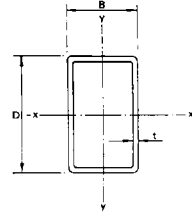


**DIMENSIONS AND PROPERTIES**

| Designation       |                      | Mass Per Metre<br>kg | Area Of Section<br>cm <sup>2</sup> | Ratios for Local Buckling |      | Second Moment Of Area       |                             | Radius Of Gyration |                | Elastic Modulus             |                             | Plastic Modulus             |                             | Torsional Constants  |                      | Surface Area Per Metre<br>m <sup>2</sup> |
|-------------------|----------------------|----------------------|------------------------------------|---------------------------|------|-----------------------------|-----------------------------|--------------------|----------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|----------------------|----------------------|--|
| Size<br>D B<br>mm | Thickness<br>t<br>mm |                      |                                    | d/t                       | b/t  | Axis x-x<br>cm <sup>4</sup> | Axis y-y<br>cm <sup>4</sup> | Axis x-x<br>cm     | Axis y-y<br>cm | Axis x-x<br>cm <sup>3</sup> | Axis y-y<br>cm <sup>3</sup> | Axis x-x<br>cm <sup>3</sup> | Axis y-y<br>cm <sup>3</sup> | J<br>cm <sup>4</sup> | C<br>cm <sup>3</sup> |  |
| 50x25             | 2.5                  | 2.72                 | 3.47                               | 17.0                      | 7.00 | 10.6                        | 3.44                        | 1.75               | 0.996          | 4.25                        | 2.75                        | 5.41                        | 3.26                        | 8.41                 | 4.62                 | 0.145                                    |
|                   | 3.0                  | 3.22                 | 4.10                               | 13.7                      | 5.33 | 12.2                        | 3.89                        | 1.73               | 0.975          | 4.88                        | 3.11                        | 6.30                        | 3.77                        | 9.64                 | 5.21                 | 0.144                                    |
|                   | 3.2                  | 3.41                 | 4.34                               | 12.6                      | 4.81 | 12.8                        | 4.05                        | 1.72               | 0.966          | 5.11                        | 3.24                        | 6.64                        | 3.96                        | 10.1                 | 5.42                 | 0.143                                    |
| 50x30             | 2.5                  | 2.92                 | 3.72                               | 17.0                      | 9.00 | 12.0                        | 5.30                        | 1.80               | 1.19           | 4.81                        | 3.53                        | 6.01                        | 4.16                        | 11.7                 | 5.74                 | 0.155                                    |
|                   | 3.0                  | 3.45                 | 4.40                               | 13.7                      | 7.00 | 13.9                        | 6.04                        | 1.78               | 1.17           | 5.54                        | 4.03                        | 7.01                        | 4.83                        | 13.5                 | 6.52                 | 0.154                                    |
|                   | 3.2                  | 3.66                 | 4.66                               | 12.6                      | 6.38 | 14.5                        | 6.31                        | 1.77               | 1.16           | 5.82                        | 4.21                        | 7.39                        | 5.08                        | 14.2                 | 6.81                 | 0.153                                    |
|                   | 4.0                  | 4.46                 | 5.68                               | 9.50                      | 4.50 | 17.0                        | 7.25                        | 1.73               | 1.13           | 6.80                        | 4.83                        | 8.81                        | 6.01                        | 16.6                 | 7.79                 | 0.151                                    |
| 5.0               | 5.40                 | 6.88                 | 7.00                               | 3.00                      | 19.5 | 8.13                        | 1.68                        | 1.09               | 7.79           | 5.42                        | 10.4                        | 6.98                        | 19.0                        | 8.71                 | 0.149                |  |
| 60x40             | 2.5                  | 3.71                 | 4.72                               | 21.0                      | 13.0 | 23.1                        | 12.2                        | 2.21               | 1.61           | 7.71                        | 6.10                        | 9.43                        | 7.09                        | 25.0                 | 9.74                 | 0.195                                    |
|                   | 3.0                  | 4.39                 | 5.60                               | 17.0                      | 10.3 | 26.9                        | 14.1                        | 2.19               | 1.59           | 8.96                        | 7.04                        | 11.1                        | 8.29                        | 29.2                 | 11.2                 | 0.194                                    |
|                   | 3.2                  | 4.66                 | 5.94                               | 15.7                      | 9.50 | 28.3                        | 14.8                        | 2.18               | 1.58           | 9.44                        | 7.39                        | 11.7                        | 8.75                        | 30.8                 | 11.8                 | 0.193                                    |
|                   | 4.0                  | 5.72                 | 7.28                               | 12.0                      | 7.00 | 33.6                        | 17.3                        | 2.15               | 1.54           | 11.2                        | 8.67                        | 14.1                        | 10.5                        | 36.6                 | 13.7                 | 0.191                                    |
|                   | 5.0                  | 6.97                 | 8.88                               | 9.00                      | 5.00 | 39.2                        | 20.0                        | 2.10               | 1.50           | 13.1                        | 10.0                        | 16.8                        | 12.4                        | 43.0                 | 15.8                 | 0.189                                    |
|                   | 6.3                  | 8.49                 | 10.8                               | 6.52                      | 3.35 | 45.1                        | 22.6                        | 2.04               | 1.45           | 15.0                        | 11.3                        | 19.9                        | 14.6                        | 49.7                 | 17.7                 | 0.186                                    |
| 80x40             | 3.0                  | 5.34                 | 6.80                               | 23.7                      | 10.3 | 55.0                        | 18.2                        | 2.85               | 1.64           | 13.8                        | 9.10                        | 17.3                        | 10.5                        | 43.7                 | 15.3                 | 0.234                                    |
|                   | 3.2                  | 5.67                 | 7.22                               | 22.0                      | 9.50 | 58.1                        | 19.1                        | 2.84               | 1.63           | 14.5                        | 9.56                        | 18.3                        | 11.1                        | 46.1                 | 16.1                 | 0.233                                    |
|                   | 4.0                  | 6.97                 | 8.88                               | 17.0                      | 7.00 | 69.6                        | 22.6                        | 2.80               | 1.59           | 17.4                        | 11.3                        | 22.2                        | 13.4                        | 55.1                 | 18.9                 | 0.231                                    |
|                   | 5.0                  | 8.54                 | 10.9                               | 13.0                      | 5.00 | 82.4                        | 26.2                        | 2.75               | 1.55           | 20.6                        | 13.1                        | 26.7                        | 15.9                        | 65.0                 | 21.9                 | 0.229                                    |
|                   | 6.3                  | 10.5                 | 13.3                               | 9.70                      | 3.35 | 96.5                        | 29.8                        | 2.69               | 1.50           | 24.1                        | 14.9                        | 31.9                        | 18.8                        | 75.8                 | 24.9                 | 0.226                                    |
|                   | 8.0                  | 12.8                 | 16.3                               | 7.00                      | 2.00 | 111                         | 33.1                        | 2.61               | 1.42           | 27.7                        | 16.6                        | 37.8                        | 21.8                        | 86.3                 | 27.6                 | 0.223                                    |
| 90x50             | 3.0                  | 6.28                 | 8.00                               | 27.0                      | 13.7 | 85.4                        | 33.8                        | 3.27               | 2.05           | 19.0                        | 13.5                        | 23.4                        | 15.5                        | 76.4                 | 22.4                 | 0.274                                    |
|                   | 3.6                  | 7.46                 | 9.50                               | 22.0                      | 10.9 | 99.8                        | 39.1                        | 3.24               | 2.03           | 22.2                        | 15.6                        | 27.6                        | 18.1                        | 89.3                 | 25.9                 | 0.272                                    |
|                   | 5.0                  | 10.1                 | 12.9                               | 15.0                      | 7.00 | 130                         | 50.0                        | 3.18               | 1.97           | 28.9                        | 20.0                        | 36.6                        | 23.9                        | 116                  | 32.9                 | 0.269                                    |
|                   | 6.3                  | 12.5                 | 15.9                               | 11.3                      | 4.94 | 154                         | 58.1                        | 3.12               | 1.91           | 34.2                        | 23.3                        | 44.2                        | 28.5                        | 138                  | 38.2                 | 0.266                                    |
|                   | 8.0                  | 15.3                 | 19.5                               | 8.25                      | 3.25 | 180                         | 66.3                        | 3.04               | 1.84           | 40.0                        | 26.5                        | 53.0                        | 33.7                        | 161                  | 43.4                 | 0.263                                    |
| 100x50            | 3.0                  | 6.75                 | 8.60                               | 30.3                      | 13.7 | 111                         | 37.1                        | 3.59               | 2.06           | 22.2                        | 14.8                        | 27.6                        | 16.9                        | 88.3                 | 25.0                 | 0.294                                    |
|                   | 3.2                  | 7.18                 | 9.14                               | 28.2                      | 12.6 | 117                         | 39.1                        | 3.58               | 2.07           | 23.5                        | 15.6                        | 29.2                        | 17.9                        | 93.3                 | 26.4                 | 0.293                                    |
|                   | 4.0                  | 8.86                 | 11.3                               | 22.0                      | 9.50 | 142                         | 46.7                        | 3.55               | 2.03           | 28.4                        | 18.7                        | 35.7                        | 21.7                        | 113                  | 31.4                 | 0.291                                    |
|                   | 5.0                  | 10.9                 | 13.9                               | 17.0                      | 7.00 | 170                         | 55.1                        | 3.50               | 1.98           | 34.0                        | 22.0                        | 43.3                        | 26.1                        | 135                  | 37.0                 | 0.289                                    |
|                   | 6.3                  | 13.4                 | 17.1                               | 12.9                      | 4.94 | 202                         | 64.2                        | 3.44               | 1.94           | 40.5                        | 25.7                        | 52.5                        | 31.3                        | 160                  | 43.0                 | 0.286                                    |
|                   | 8.0                  | 16.6                 | 21.1                               | 9.50                      | 3.25 | 238                         | 73.5                        | 3.36               | 1.86           | 47.6                        | 29.4                        | 63.1                        | 37.1                        | 187                  | 49.1                 | 0.283                                    |
| 100x60            | 3.0                  | 7.22                 | 9.20                               | 30.3                      | 17.0 | 125                         | 56.2                        | 3.69               | 2.47           | 25.0                        | 18.7                        | 30.5                        | 21.3                        | 121                  | 30.7                 | 0.314                                    |
|                   | 3.6                  | 8.59                 | 10.9                               | 24.8                      | 13.7 | 147                         | 65.4                        | 3.66               | 2.45           | 29.3                        | 21.8                        | 36.0                        | 25.1                        | 142                  | 35.6                 | 0.312                                    |
|                   | 5.0                  | 11.7                 | 14.9                               | 17.0                      | 9.00 | 192                         | 84.7                        | 3.60               | 2.39           | 38.5                        | 28.2                        | 48.1                        | 33.3                        | 187                  | 45.9                 | 0.309                                    |
|                   | 6.3                  | 14.4                 | 18.4                               | 12.9                      | 6.52 | 230                         | 99.9                        | 3.54               | 2.33           | 46.0                        | 33.3                        | 58.4                        | 40.2                        | 224                  | 53.9                 | 0.306                                    |
|                   | 8.0                  | 17.8                 | 22.7                               | 9.50                      | 4.50 | 272                         | 116                         | 3.46               | 2.26           | 54.4                        | 38.7                        | 70.5                        | 48.1                        | 266                  | 62.4                 | 0.303                                    |
| 120x60            | 3.6                  | 9.72                 | 12.4                               | 30.3                      | 13.7 | 230                         | 76.9                        | 4.31               | 2.49           | 38.3                        | 25.6                        | 47.6                        | 29.2                        | 183                  | 43.3                 | 0.352                                    |
|                   | 5.0                  | 13.3                 | 16.9                               | 21.0                      | 9.00 | 304                         | 99.9                        | 4.24               | 2.43           | 50.7                        | 33.3                        | 63.9                        | 38.8                        | 242                  | 56.0                 | 0.349                                    |
|                   | 6.3                  | 16.4                 | 20.9                               | 16.0                      | 6.52 | 366                         | 118                         | 4.18               | 2.38           | 61.0                        | 39.4                        | 78.0                        | 46.9                        | 290                  | 66.0                 | 0.346                                    |
|                   | 8.0                  | 20.4                 | 25.9                               | 12.0                      | 4.50 | 437                         | 138                         | 4.10               | 2.31           | 72.8                        | 45.9                        | 94.8                        | 56.4                        | 344                  | 76.8                 | 0.343                                    |
| 120x80            | 5.0                  | 14.8                 | 18.9                               | 21.0                      | 13.0 | 370                         | 195                         | 4.43               | 3.21           | 61.7                        | 48.8                        | 75.4                        | 56.7                        | 401                  | 77.9                 | 0.389                                    |
|                   | 6.3                  | 18.4                 | 23.4                               | 16.0                      | 9.70 | 447                         | 234                         | 4.37               | 3.16           | 74.6                        | 58.4                        | 92.3                        | 69.1                        | 486                  | 93.0                 | 0.386                                    |
|                   | 8.0                  | 22.9                 | 29.1                               | 12.0                      | 7.00 | 537                         | 278                         | 4.29               | 3.09           | 89.5                        | 69.4                        | 113                         | 83.9                        | 586                  | 110                  | 0.383                                    |
|                   | 10.0                 | 27.9                 | 35.5                               | 9.00                      | 5.00 | 628                         | 320                         | 4.20               | 3.00           | 105                         | 80.0                        | 134                         | 99.4                        | 688                  | 126                  | 0.379                                    |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

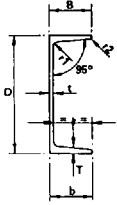
RECTANGULAR HOLLOW SECTIONS



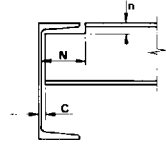
DIMENSIONS AND PROPERTIES

| Designation       |                      | Mass Per Metre<br>kg | Area Of Section<br>cm <sup>2</sup> | Ratios for Local Buckling |      | Second Moment Of Area       |                             | Radius Of Gyration |                | Elastic Modulus             |                             | Plastic Modulus             |                             | Torsional Constants  |                                   | Surface Area Per Metre<br>m <sup>2</sup> |
|-------------------|----------------------|----------------------|------------------------------------|---------------------------|------|-----------------------------|-----------------------------|--------------------|----------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|----------------------|-----------------------------------|--|
| Size<br>D B<br>mm | Thickness<br>t<br>mm |                      |                                    | d/t                       | b/t  | Axis X-X<br>cm <sup>4</sup> | Axis Y-Y<br>cm <sup>4</sup> | Axis X-X<br>cm     | Axis Y-Y<br>cm | Axis X-X<br>cm <sup>3</sup> | Axis Y-Y<br>cm <sup>3</sup> | Axis X-X<br>cm <sup>3</sup> | Axis Y-Y<br>cm <sup>3</sup> | J<br>cm <sup>4</sup> | C <sub>x</sub><br>cm <sup>3</sup> |  |
| 150x100           | 5.0                  | 18.7                 | 23.9                               | 27.0                      | 17.0 | 747                         | 396                         | 5.59               | 4.07           | 89.5                        | 79.1                        | 121                         | 90.9                        | 806                  | 127                               | 0.489                                    |
|                   | 6.3                  | 23.3                 | 29.7                               | 20.8                      | 12.9 | 910                         | 479                         | 5.53               | 4.02           | 121                         | 95.9                        | 148                         | 111                         | 985                  | 153                               | 0.466                                    |
|                   | 8.0                  | 29.1                 | 37.1                               | 15.7                      | 9.50 | 1106                        | 577                         | 5.46               | 3.94           | 147                         | 115                         | 183                         | 137                         | 1202                 | 184                               | 0.463                                    |
|                   | 10.0                 | 35.7                 | 45.5                               | 12.0                      | 7.00 | 1312                        | 678                         | 5.37               | 3.86           | 175                         | 136                         | 220                         | 164                         | 1431                 | 215                               | 0.479                                    |
|                   | 12.5                 | 43.6                 | 55.5                               | 9.00                      | 5.00 | 1532                        | 781                         | 5.25               | 3.75           | 204                         | 156                         | 263                         | 194                         | 1680                 | 246                               | 0.473                                    |
| 160x80            | 5.0                  | 18.0                 | 22.9                               | 29.0                      | 13.0 | 753                         | 251                         | 5.74               | 3.31           | 94.1                        | 62.8                        | 117                         | 71.7                        | 599                  | 106                               | 0.469                                    |
|                   | 6.3                  | 22.3                 | 28.5                               | 22.4                      | 9.70 | 917                         | 302                         | 5.68               | 3.26           | 115                         | 75.6                        | 144                         | 87.7                        | 729                  | 127                               | 0.466                                    |
|                   | 8.0                  | 27.9                 | 35.5                               | 17.0                      | 7.00 | 1113                        | 361                         | 5.60               | 3.19           | 139                         | 90.2                        | 177                         | 107                         | 882                  | 151                               | 0.463                                    |
|                   | 10.0                 | 34.2                 | 43.5                               | 13.0                      | 5.00 | 1318                        | 419                         | 5.50               | 3.10           | 165                         | 105                         | 213                         | 127                         | 1041                 | 175                               | 0.459                                    |
|                   | 12.5                 | 41.6                 | 53.0                               | 9.80                      | 3.40 | 1536                        | 476                         | 5.38               | 3.00           | 192                         | 119                         | 254                         | 150                         | 1206                 | 199                               | 0.453                                    |
| 200x100           | 5.0                  | 22.7                 | 28.9                               | 37.0                      | 17.0 | 1509                        | 509                         | 7.23               | 4.20           | 151                         | 102                         | 186                         | 115                         | 1202                 | 172                               | 0.589                                    |
|                   | 6.3                  | 28.3                 | 36.0                               | 28.7                      | 12.9 | 1851                        | 618                         | 7.17               | 4.14           | 185                         | 124                         | 231                         | 141                         | 1473                 | 208                               | 0.586                                    |
|                   | 8.0                  | 35.4                 | 45.1                               | 22.0                      | 9.50 | 2269                        | 747                         | 7.09               | 4.07           | 227                         | 149                         | 286                         | 174                         | 1802                 | 251                               | 0.583                                    |
|                   | 10.0                 | 43.6                 | 55.5                               | 17.0                      | 7.00 | 2718                        | 891                         | 7.00               | 3.98           | 272                         | 176                         | 346                         | 209                         | 2154                 | 296                               | 0.579                                    |
|                   | 12.5                 | 53.4                 | 68.0                               | 13.0                      | 5.00 | 3218                        | 1022                        | 6.88               | 3.88           | 322                         | 204                         | 417                         | 249                         | 2541                 | 342                               | 0.573                                    |
| 200x120           | 5.0                  | 24.2                 | 30.9                               | 37.0                      | 21.0 | 1699                        | 767                         | 7.42               | 4.98           | 170                         | 128                         | 206                         | 144                         | 1646                 | 210                               | 0.629                                    |
|                   | 6.0                  | 28.9                 | 36.8                               | 30.3                      | 17.0 | 2000                        | 899                         | 7.37               | 4.94           | 200                         | 150                         | 244                         | 171                         | 1940                 | 245                               | 0.627                                    |
|                   | 6.3                  | 30.3                 | 38.5                               | 28.7                      | 16.0 | 2087                        | 937                         | 7.36               | 4.93           | 209                         | 156                         | 255                         | 178                         | 2025                 | 256                               | 0.626                                    |
|                   | 8.0                  | 37.9                 | 48.3                               | 22.0                      | 12.0 | 2564                        | 1140                        | 7.28               | 4.86           | 256                         | 190                         | 316                         | 220                         | 2491                 | 310                               | 0.623                                    |
|                   | 10.0                 | 46.7                 | 59.5                               | 17.0                      | 9.00 | 3079                        | 1356                        | 7.19               | 4.77           | 308                         | 226                         | 384                         | 266                         | 2997                 | 357                               | 0.619                                    |
| 250x150           | 5.0                  | 30.5                 | 38.9                               | 47.0                      | 27.0 | 3382                        | 1535                        | 9.33               | 6.28           | 271                         | 205                         | 326                         | 229                         | 3275                 | 337                               | 0.789                                    |
|                   | 6.3                  | 38.2                 | 48.6                               | 36.7                      | 20.8 | 4178                        | 1886                        | 9.27               | 6.23           | 334                         | 252                         | 405                         | 284                         | 4049                 | 413                               | 0.786                                    |
|                   | 8.0                  | 48.0                 | 61.1                               | 28.2                      | 15.7 | 5167                        | 2317                        | 9.19               | 6.16           | 413                         | 309                         | 505                         | 353                         | 5014                 | 506                               | 0.783                                    |
|                   | 10.0                 | 59.3                 | 75.5                               | 22.0                      | 12.0 | 6259                        | 2784                        | 9.10               | 6.07           | 501                         | 371                         | 618                         | 430                         | 6082                 | 606                               | 0.779                                    |
|                   | 12.5                 | 73.0                 | 93.0                               | 17.0                      | 9.00 | 7518                        | 3310                        | 8.99               | 5.97           | 601                         | 441                         | 751                         | 520                         | 7317                 | 717                               | 0.773                                    |
| 300x200           | 6.3                  | 48.1                 | 61.2                               | 44.6                      | 28.7 | 7880                        | 4216                        | 11.3               | 8.30           | 525                         | 422                         | 627                         | 475                         | 8468                 | 681                               | 0.986                                    |
|                   | 8.0                  | 60.5                 | 77.1                               | 34.5                      | 22.0 | 9798                        | 5219                        | 11.3               | 8.23           | 653                         | 522                         | 785                         | 593                         | 10550                | 840                               | 0.983                                    |
|                   | 10.0                 | 75.0                 | 95.5                               | 27.0                      | 17.0 | 11940                       | 6331                        | 11.2               | 8.14           | 796                         | 633                         | 964                         | 726                         | 12890                | 1016                              | 0.979                                    |
|                   | 12.5                 | 92.6                 | 118                                | 21.0                      | 13.0 | 14460                       | 7619                        | 11.1               | 8.04           | 964                         | 762                         | 1179                        | 886                         | 15650                | 1217                              | 0.973                                    |
|                   | 16.0                 | 117                  | 149                                | 15.7                      | 9.50 | 17700                       | 9238                        | 10.9               | 7.89           | 1180                        | 924                         | 1462                        | 1094                        | 19230                | 1469                              | 0.966                                    |
| 400x200           | 8.0                  | 73.1                 | 93.1                               | 47.0                      | 22.0 | 19710                       | 6695                        | 14.5               | 8.48           | 985                         | 669                         | 1210                        | 746                         | 15720                | 1135                              | 1.18                                     |
|                   | 10.0                 | 90.7                 | 116                                | 37.0                      | 17.0 | 24140                       | 8138                        | 14.5               | 8.39           | 1207                        | 814                         | 1492                        | 916                         | 19240                | 1377                              | 1.18                                     |
|                   | 12.5                 | 112                  | 143                                | 29.0                      | 13.0 | 29410                       | 9820                        | 14.3               | 8.29           | 1471                        | 962                         | 1831                        | 1120                        | 23410                | 1657                              | 1.17                                     |
|                   | 16.0                 | 142                  | 181                                | 22.0                      | 9.50 | 36300                       | 11950                       | 14.2               | 8.14           | 1815                        | 1195                        | 2285                        | 1388                        | 28840                | 2011                              | 1.17                                     |
| 450x250           | 8.0                  | 85.7                 | 109                                | 53.2                      | 28.2 | 30270                       | 12200                       | 16.7               | 10.6           | 1345                        | 976                         | 1630                        | 1086                        | 27080                | 1629                              | 1.38                                     |
|                   | 10.0                 | 106                  | 136                                | 42.0                      | 22.0 | 37180                       | 14900                       | 16.6               | 10.5           | 1653                        | 1192                        | 2013                        | 1338                        | 33250                | 1986                              | 1.38                                     |
|                   | 12.5                 | 132                  | 168                                | 33.0                      | 17.0 | 45470                       | 18100                       | 16.5               | 10.4           | 2021                        | 1448                        | 2478                        | 1642                        | 40670                | 2407                              | 1.37                                     |
|                   | 16.0                 | 167                  | 213                                | 25.1                      | 12.6 | 56420                       | 22250                       | 16.3               | 10.2           | 2508                        | 1780                        | 3103                        | 2047                        | 50480                | 2948                              | 1.37                                     |
| 500x200           | 8.0                  | 85.7                 | 109                                | 59.5                      | 22.0 | 34270                       | 8170                        | 17.7               | 8.65           | 1371                        | 817                         | 1716                        | 900                         | 21100                | 1430                              | 1.38                                     |
|                   | 10.0                 | 106                  | 136                                | 47.0                      | 17.0 | 42110                       | 9945                        | 17.6               | 8.57           | 1684                        | 994                         | 2119                        | 1105                        | 25840                | 1738                              | 1.38                                     |
|                   | 12.5                 | 132                  | 168                                | 37.0                      | 13.0 | 51510                       | 12020                       | 17.5               | 8.46           | 2060                        | 1202                        | 2609                        | 1354                        | 31480                | 2097                              | 1.37                                     |
|                   | 16.0                 | 167                  | 213                                | 28.2                      | 9.50 | 63930                       | 14670                       | 17.3               | 8.31           | 2557                        | 1467                        | 3267                        | 1683                        | 38830                | 2554                              | 1.37                                     |
| 500x300           | 10.0                 | 122                  | 156                                | 47.0                      | 27.0 | 54120                       | 24560                       | 18.7               | 12.6           | 2165                        | 1638                        | 2609                        | 1834                        | 52400                | 2696                              | 1.58                                     |
|                   | 12.5                 | 152                  | 193                                | 37.0                      | 21.0 | 66360                       | 29970                       | 18.5               | 12.5           | 2655                        | 1998                        | 3218                        | 2257                        | 64310                | 3282                              | 1.57                                     |
|                   | 16.0                 | 192                  | 245                                | 28.2                      | 15.7 | 82670                       | 37080                       | 18.4               | 12.3           | 3307                        | 2472                        | 4042                        | 2825                        | 80220                | 4046                              | 1.57                                     |
|                   | 20.0                 | 237                  | 302                                | 22.0                      | 12.0 | 100100                      | 44550                       | 18.2               | 12.1           | 4006                        | 2970                        | 4942                        | 3442                        | 97310                | 4845                              | 1.56                                     |

+ Sections marked thus are not included in BS4848: Part 2  
 ‡ Sections marked thus are rolled in grade 50C only  
 FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3



**CHANNELS**

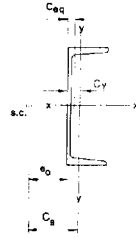


**DIMENSIONS**

| Designation     |                   | Depth Of Section D mm | Width Of Section B mm | Thickness |             | Root Radius r1 mm | Toe Radius r2 mm | Depth Between Fillets d mm | Ratios For Local Buckling |         | Dimensions For Detailing |       |    | Surface Area             |                          |
|-----------------|-------------------|-----------------------|-----------------------|-----------|-------------|-------------------|------------------|----------------------------|---------------------------|---------|--------------------------|-------|----|--------------------------|--------------------------|
| Nominal Size mm | Mass Per Metre kg |                       |                       | Web t mm  | Flange T mm |                   |                  |                            | Flange b/T                | Web d/t | End Clearance C mm       | Notch |    | Per Metre m <sup>2</sup> | Per Tonne m <sup>2</sup> |
|                 |                   |                       |                       |           |             |                   |                  |                            |                           |         | N mm                     | n mm  |    |                          |                          |
| 432x102         | 65.54             | 431.8                 | 101.6                 | 12.2      | 16.8        | 15.2              | 4.8              | 362.5                      | 6.05                      | 29.7    | 14                       | 96    | 36 | 1.22                     | 18.6                     |
| 381x102         | 55.10             | 381.0                 | 101.6                 | 10.4      | 16.3        | 15.2              | 4.8              | 312.6                      | 6.23                      | 30.1    | 12                       | 98    | 36 | 1.12                     | 20.3                     |
| 305x102         | 46.18             | 304.8                 | 101.6                 | 10.2      | 14.8        | 15.2              | 4.8              | 239.3                      | 6.86                      | 23.5    | 12                       | 98    | 34 | 0.966                    | 20.9                     |
| 305x89          | 41.69             | 304.8                 | 88.9                  | 10.2      | 13.7        | 13.7              | 3.2              | 245.4                      | 6.49                      | 24.1    | 12                       | 86    | 30 | 0.920                    | 22.1                     |
| 254x89          | 35.74             | 254.0                 | 88.9                  | 9.1       | 13.6        | 13.7              | 3.2              | 194.7                      | 6.54                      | 21.4    | 11                       | 86    | 30 | 0.820                    | 23.0                     |
| 254x76          | 28.29             | 254.0                 | 76.2                  | 8.1       | 10.9        | 12.2              | 3.2              | 203.9                      | 6.99                      | 25.2    | 10                       | 76    | 26 | 0.774                    | 27.4                     |
| 229x89          | 32.76             | 228.6                 | 88.9                  | 8.6       | 13.3        | 13.7              | 3.2              | 169.9                      | 6.68                      | 19.8    | 11                       | 88    | 30 | 0.770                    | 23.5                     |
| 229x76          | 26.06             | 228.6                 | 76.2                  | 7.6       | 11.2        | 12.2              | 3.2              | 177.8                      | 6.80                      | 23.4    | 10                       | 76    | 26 | 0.725                    | 27.8                     |
| 203x89          | 29.78             | 203.2                 | 88.9                  | 8.1       | 12.9        | 13.7              | 3.2              | 145.2                      | 6.89                      | 17.9    | 10                       | 88    | 30 | 0.720                    | 24.2                     |
| 203x76          | 23.82             | 203.2                 | 76.2                  | 7.1       | 11.2        | 12.2              | 3.2              | 152.4                      | 6.80                      | 21.5    | 9                        | 76    | 26 | 0.675                    | 28.3                     |
| 178x89          | 26.81             | 177.8                 | 88.9                  | 7.6       | 12.3        | 13.7              | 3.2              | 121.0                      | 7.23                      | 15.9    | 10                       | 88    | 30 | 0.671                    | 25.0                     |
| 178x76          | 20.84             | 177.8                 | 76.2                  | 6.6       | 10.3        | 12.2              | 3.2              | 128.8                      | 7.40                      | 19.5    | 9                        | 76    | 26 | 0.625                    | 30.0                     |
| 152x89          | 23.84             | 152.4                 | 88.9                  | 7.1       | 11.6        | 13.7              | 3.2              | 96.9                       | 7.66                      | 13.6    | 9                        | 88    | 28 | 0.621                    | 26.0                     |
| 152x76          | 17.88             | 152.4                 | 76.2                  | 6.4       | 9.0         | 12.2              | 2.4              | 105.9                      | 8.47                      | 16.5    | 8                        | 76    | 24 | 0.575                    | 32.2                     |
| 127x64          | 14.90             | 127.0                 | 63.5                  | 6.4       | 9.2         | 10.7              | 2.4              | 84.0                       | 6.90                      | 13.1    | 8                        | 64    | 22 | 0.476                    | 32.0                     |
| 102x51          | 10.42             | 101.6                 | 50.8                  | 6.1       | 7.6         | 9.1               | 2.4              | 65.8                       | 6.68                      | 10.8    | 8                        | 52    | 18 | 0.379                    | 36.3                     |
| 76x38           | 6.70              | 76.2                  | 38.1                  | 5.1       | 6.8         | 7.6               | 2.4              | 45.8                       | 5.60                      | 8.98    | 7                        | 40    | 16 | 0.282                    | 42.1                     |

◆ Check availability of section  
FOR EXPLANATION OF TABLES SEE NOTE 2

CHANNELS



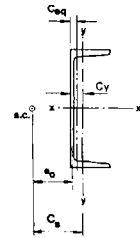
PROPERTIES

| Designation  |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 | Plastic Modulus |                 | Buckling Parameter | Torsional Index | Warping Constant | Torsional Constant | Area of Section |
|--------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|------------------|--------------------|-----------------|
| Nominal Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        | Axis y-y        | Axis x-x        | Axis y-y        | u                  | x               | H                | J                  | A               |
| mm           | kg             | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |                    |                 | dm <sup>6</sup>  | cm <sup>4</sup>    | cm <sup>2</sup> |
| 432x102      | 65.54          | 21370                 | 627             | 16.0               | 2.74     | 990             | 79.9            | 1205            | 153             | 0.875              | 24.5            | 0.216            | 61.5               | 83.4            |
| 381x102      | 55.10          | 14870                 | 579             | 14.6               | 2.87     | 781             | 75.7            | 931             | 144             | 0.895              | 22.6            | 0.153            | 46.4               | 70.1            |
| 305x102      | 46.18          | 8208                  | 489             | 11.8               | 2.91     | 539             | 66.5            | 638             | 128             | 0.899              | 18.8            | 0.0842           | 35.9               | 58.9            |
| 305x89       | 41.69          | 7078                  | 326             | 11.5               | 2.47     | 464             | 48.6            | 559             | 92.9            | 0.887              | 20.3            | 0.0552           | 28.1               | 53.3            |
| 254x89       | 35.74          | 4445                  | 302             | 9.89               | 2.58     | 350             | 46.7            | 414             | 89.6            | 0.906              | 17.0            | 0.0347           | 23.2               | 45.4            |
| 254x76       | 28.29          | 3355                  | 162             | 9.67               | 2.12     | 264             | 28.1            | 316             | 53.9            | 0.886              | 21.2            | 0.0194           | 12.3               | 35.9            |
| 228x89       | 32.76          | 3383                  | 285             | 9.01               | 2.61     | 296             | 44.8            | 348             | 86.3            | 0.912              | 15.5            | 0.0263           | 20.6               | 41.6            |
| 229x76       | 26.06          | 2615                  | 159             | 8.87               | 2.19     | 229             | 28.3            | 271             | 54.5            | 0.901              | 18.7            | 0.0151           | 11.6               | 33.2            |
| 203x89       | 29.78          | 2482                  | 265             | 8.11               | 2.64     | 245             | 42.4            | 287             | 81.7            | 0.916              | 14.0            | 0.0192           | 18.1               | 37.9            |
| 203x76       | 23.82          | 1955                  | 152             | 8.02               | 2.24     | 192             | 27.7            | 226             | 53.5            | 0.911              | 16.5            | 0.0112           | 10.6               | 30.4            |
| 178x89       | 26.81          | 1753                  | 241             | 7.17               | 2.66     | 197             | 39.3            | 230             | 75.4            | 0.915              | 12.6            | 0.0134           | 15.3               | 34.1            |
| 178x76       | 20.84          | 1338                  | 134             | 7.10               | 2.25     | 151             | 24.8            | 176             | 48.1            | 0.911              | 15.3            | 0.00765          | 8.26               | 26.6            |
| 152x89       | 23.84          | 1168                  | 216             | 6.20               | 2.66     | 153             | 35.8            | 178             | 68.3            | 0.909              | 11.2            | 0.00882          | 12.7               | 30.4            |
| 152x76       | 17.88          | 852                   | 114             | 6.11               | 2.23     | 112             | 21.0            | 130             | 41.2            | 0.901              | 14.4            | 0.00486          | 6.05               | 22.8            |
| 127x64       | 14.80          | 482                   | 67.2            | 5.04               | 1.88     | 76.0            | 15.2            | 89.4            | 29.3            | 0.909              | 11.7            | 0.00188          | 5.00               | 19.0            |
| 102x51       | 10.42          | 207                   | 29.0            | 3.95               | 1.48     | 40.8            | 8.14            | 48.7            | 15.7            | 0.900              | 10.8            | 0.000512         | 2.56               | 13.3            |
| 76x38        | 6.70           | 74.3                  | 10.7            | 2.95               | 1.12     | 19.5            | 4.09            | 23.5            | 7.78            | 0.908              | 9.06            | 0.000101         | 1.26               | 8.56            |

FOR EXPLANATION OF TABLES SEE NOTE 3



**CHANNELS**

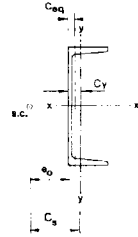


**PLASTIC MODULI-MAJOR AXIS**

| Designation        |                      | Area of Section<br>cm <sup>2</sup> | Dimension |          |          |           | Plastic Modulus Axis x-x<br>cm <sup>3</sup> | Reduced Value Of Modulus Under Axial Load |      |                          |                    |      |
|--------------------|----------------------|------------------------------------|-----------|----------|----------|-----------|---|---|------|--------------------------|--------------------|------|
| Nominal Size<br>mm | Mass Per Metre<br>kg |                                    | eo<br>cm  | Cs<br>cm | Cy<br>cm | Ceq<br>cm |   | Lower Values Of n                         |      | Change Formula<br>At n = | Higher Values Of n |      |
|                    |                      |                                    |           |          |          |           |   | K1  | K2   |                          | K3                 | K4   |
| 432x102            | 65.54                | 83.4                               | 3.13      | 4.83     | 2.31     | 0.966     | 1205  | 1205                                      | 1427 | 0.579                    | 177                | 9.17 |
| 381x102            | 55.10                | 70.1                               | 3.44      | 5.44     | 2.52     | 0.920     | 931   | 931                                       | 1181 | 0.514                    | 125                | 9.65 |
| 305x102            | 46.18                | 58.9                               | 3.59      | 5.73     | 2.65     | 0.966     | 638   | 638                                       | 849  | 0.473                    | 89.1               | 9.07 |
| 305x89             | 41.69                | 53.3                               | 2.93      | 4.60     | 2.18     | 0.874     | 559   | 559                                       | 696  | 0.527                    | 83.0               | 8.79 |
| 254x89             | 35.74                | 45.4                               | 3.20      | 5.16     | 2.42     | 0.894     | 414   | 414                                       | 567  | 0.450                    | 60.5               | 8.55 |
| 254x76             | 28.29                | 35.9                               | 2.55      | 4.00     | 1.85     | 0.707     | 316   | 316                                       | 398  | 0.519                    | 44.4               | 9.28 |
| 229x89             | 32.76                | 41.6                               | 3.32      | 5.42     | 2.53     | 1.10      | 348   | 348                                       | 504  | 0.413                    | 50.9               | 8.35 |
| 229x76             | 26.06                | 33.2                               | 2.70      | 4.32     | 2.00     | 0.727     | 271   | 271                                       | 363  | 0.467                    | 37.9               | 9.01 |
| 203x89             | 29.78                | 37.9                               | 3.44      | 5.68     | 2.65     | 1.40      | 287   | 287                                       | 444  | 0.374                    | 42.3               | 8.10 |
| 203x76             | 23.82                | 30.4                               | 2.84      | 4.62     | 2.14     | 0.892     | 226   | 226                                       | 325  | 0.418                    | 31.7               | 8.73 |
| 178x89             | 26.81                | 34.1                               | 3.55      | 5.93     | 2.76     | 1.70      | 230   | 230                                       | 383  | 0.336                    | 34.5               | 7.81 |
| 178x76             | 20.84                | 26.6                               | 2.93      | 4.80     | 2.20     | 1.09      | 176   | 176                                       | 267  | 0.386                    | 24.5               | 8.65 |
| 152x89             | 23.84                | 30.4                               | 3.65      | 6.16     | 2.87     | 1.99      | 178   | 178                                       | 326  | 0.296                    | 27.5               | 7.42 |
| 152x76             | 17.88                | 22.8                               | 2.96      | 4.85     | 2.21     | 1.15      | 130   | 130                                       | 203  | 0.371                    | 18.3               | 8.49 |
| 127x64             | 14.90                | 19.0                               | 2.46      | 4.08     | 1.94     | 1.09      | 89.4  | 89.4                                      | 141  | 0.360                    | 15.0               | 7.07 |
| 102x51             | 10.42                | 13.3                               | 1.89      | 3.10     | 1.51     | 0.759     | 48.7  | 48.7                                      | 72.1 | 0.390                    | 9.09               | 6.41 |
| 76x38              | 6.70                 | 8.56                               | 1.43      | 2.37     | 1.19     | 0.673     | 23.5  | 23.5                                      | 35.9 | 0.366                    | 5.01               | 5.51 |

eo is the distance from the centre of the web to the shear centre.  
 Cs is the distance from the centroidal axis to the shear centre.  
 Cy is the distance from the back of the web to the centroidal axis.  
 Ceq is the distance from the back of the web to the equal area axis.  
 $n = F / (Ag \cdot p_v)$  Where F is the factored axial load and Ag is the gross cross sectional area.  
 For lower values of n reduced plastic modulus(Sr) =  $K1 - K2n^2$   
 For higher values of n reduced plastic modulus(Sr) =  $K3[1 - n / (K4 + n)]$   
 FOR EXPLANATION OF TABLES SEE NOTE 3

CHANNELS

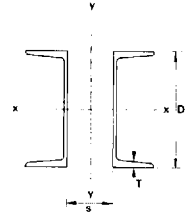


PLASTIC MODULI-MINOR AXIS

| Designation           |                            | Dimension<br>Cy<br>cm | Plastic<br>Modulus<br>Axis<br>Y-Y<br>cm <sup>3</sup> | Reduced Value Of Plastic Modulus Under Axial Load About Centroidal Axis     |      |       |                    |      |       |                             |   |      |       |                    |      |      |
|-----------------------|----------------------------|-----------------------|--|---|------|-------|--------------------|------|-------|-----------------------------|---|------|-------|--------------------|------|------|
| Nominal<br>Size<br>mm | Mass<br>Per<br>Metre<br>kg |                       |  | Axial load and moment inducing stresses<br>of same kind towards back of web |      |       |                    |      |       | Change<br>Formula<br>At n = | Axial load and moment inducing stresses<br>of opposite kind towards back of web |      |       |                    |      |      |
|                       |                            |                       |  | Lower Values Of n   |      |       | Higher Values Of n |      |       |                             | Lower Values Of n   |      |       | Higher Values Of n |      |      |
|                       |                            |                       |  | K1  | K2   | K3    | K1                 | K2   | K3    |                             | K1  | K2   | K3    | K1                 | K2   | K3   |
| 432x102               | 65.54                      | 2.31                  | 153  | 153   | 40.4 | 2.79  | 125                | 453  | 0.720 | 0.261                       | 153   | 40.4 | 2.79  | 153                | 40.4 | 2.79 |
| 381x102               | 55.10                      | 2.52                  | 144  | 144   | 32.3 | 3.47  | 139                | 329  | 0.580 | 0.130                       | 144   | 32.3 | 3.47  | 144                | 32.3 | 3.47 |
| 305x102               | 46.18                      | 2.65                  | 128  | 128   | 28.4 | 3.51  | 127                | 251  | 0.490 | 0.0528                      | 128   | 28.4 | 3.51  | 128                | 28.4 | 3.51 |
| 305x89                | 41.69                      | 2.18                  | 92.9   | 92.6  | 23.1 | 3.00  | 87.1               | 223  | 0.610 | 0.166                       | 92.6  | 23.1 | 3.00  | 92.6               | 23.1 | 3.00 |
| 254x89                | 35.74                      | 2.42                  | 89.6   | 89.6  | 20.4 | 3.39  | 89.5               | 165  | 0.460 | 0.0204                      | 89.6  | 20.4 | 3.39  | 89.6               | 20.4 | 3.39 |
| 254x76                | 28.29                      | 1.85                  | 53.9   | 54.1  | 12.8 | 3.24  | 51.7               | 126  | 0.590 | 0.146                       | 54.1  | 12.8 | 3.24  | 54.1               | 12.8 | 3.24 |
| 229x89                | 32.76                      | 2.53                  | 86.3   | 86.4  | 89.9 | 0.670 | 86.2               | 153  | 0.440 | 0.0538                      | 86.4  | 89.9 | 0.670 | 86.6               | 19.0 | 3.55 |
| 229x76                | 26.06                      | 2.00                  | 54.5   | 54.2  | 12.1 | 3.50  | 54.0               | 105  | 0.490 | 0.0494                      | 54.2  | 12.1 | 3.50  | 54.2               | 12.1 | 3.50 |
| 203x89                | 29.78                      | 2.66                  | 81.7   | 81.6  | 85.2 | 0.560 | 80.6               | 143  | 0.440 | 0.129                       | 81.6  | 85.2 | 0.560 | 82.7               | 17.7 | 3.67 |
| 203x76                | 23.82                      | 2.14                  | 53.5   | 53.3  | 54.4 | 0.700 | 53.2               | 95.1 | 0.440 | 0.0474                      | 53.3  | 54.4 | 0.700 | 53.4               | 11.3 | 3.72 |
| 178x89                | 26.81                      | 2.76                  | 75.4   | 75.4  | 77.1 | 0.470 | 73.1               | 133  | 0.450 | 0.207                       | 75.4  | 77.1 | 0.470 | 78.0               | 16.4 | 3.74 |
| 178x76                | 20.84                      | 2.20                  | 48.1   | 48.1  | 48.7 | 0.610 | 47.6               | 85.9 | 0.450 | 0.115                       | 48.1  | 48.7 | 0.610 | 48.6               | 9.91 | 3.90 |
| 152x89                | 23.84                      | 2.87                  | 68.3   | 68.1  | 67.1 | 0.400 | 63.5               | 123  | 0.480 | 0.286                       | 68.1  | 67.1 | 0.400 | 72.4               | 15.1 | 3.75 |
| 152x76                | 17.88                      | 2.21                  | 41.2   | 41.3  | 40.0 | 0.600 | 40.5               | 74.9 | 0.460 | 0.150                       | 41.3  | 40.0 | 0.600 | 42.0               | 8.51 | 3.92 |
| 127x64                | 14.90                      | 1.94                  | 29.3   | 29.3  | 29.4 | 0.540 | 28.8               | 51.4 | 0.440 | 0.150                       | 29.3  | 29.4 | 0.540 | 29.8               | 7.09 | 3.20 |
| 102x51                | 10.42                      | 1.51                  | 15.7   | 15.7  | 15.2 | 0.660 | 15.7               | 27.2 | 0.430 | 0.0671                      | 15.7  | 15.2 | 0.660 | 15.8               | 4.34 | 2.63 |
| 76x38                 | 6.70                       | 1.19                  | 7.78   | 7.76  | 7.60 | 0.580 | 7.71               | 13.2 | 0.420 | 0.0927                      | 7.76  | 7.60 | 0.580 | 7.80               | 2.39 | 2.26 |

Cy is the distance from the back of the web to the centroidal axis.  
 $n = F/(Ag \cdot py)$ . Where F is the factored axial load and Ag is the gross cross sectional area.  
 For axial load and moment inducing stresses of same kind towards back of web, reduced plastic modulus(Sr) = K1 + K2n(K3-n)  
 For axial load and moment inducing stresses of opposite kind towards back of web, reduced plastic modulus(Sr) = K1-K2n(K3+n)  
 FOR EXPLANATION OF TABLES SEE NOTE 3

**COMPOUND STRUTS  
TWO CHANNELS LACED**

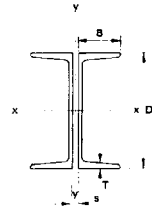


**GROSS DIMENSIONS AND SECTION PROPERTIES**

| Composed Of Two Channels | Total Mass Per Metre | Total Area      | Space Between Webs | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 | Plastic Modulus |                 |
|--------------------------|----------------------|-----------------|--------------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|
|                          |                      |                 |                    | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        | Axis y-y        | Axis x-x        | Axis y-y        |
| mm                       | kg                   | cm <sup>2</sup> | s mm               | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |
| 432x102                  | 131                  | 167             | 270                | 42750                 | 42990           | 16.0               | 16.0     | 1980            | 1817            | 2411            | 2639            |
| 381x102                  | 110                  | 140             | 240                | 29740                 | 30690           | 14.6               | 14.8     | 1561            | 1385            | 1862            | 2035            |
| 305x102                  | 92.4                 | 118             | 180                | 16420                 | 16990           | 11.8               | 12.0     | 1077            | 887             | 1276            | 1372            |
| 305x89                   | 83.4                 | 107             | 190                | 14160                 | 15190           | 11.5               | 11.9     | 929             | 826             | 1117            | 1244            |
| 254x89                   | 71.5                 | 90.9            | 150                | 8891                  | 9546            | 9.89               | 10.2     | 700             | 582             | 828             | 901             |
| 254x76                   | 56.6                 | 71.8            | 160                | 6710                  | 7297            | 9.67               | 10.1     | 528             | 467             | 632             | 708             |
| 229x89                   | 65.5                 | 83.3            | 130                | 6766                  | 7364            | 9.01               | 9.40     | 592             | 478             | 696             | 752             |
| 229x76                   | 52.1                 | 66.4            | 140                | 5231                  | 5704            | 8.87               | 9.26     | 458             | 390             | 542             | 598             |
| 203x89                   | 59.6                 | 75.9            | 110                | 4985                  | 5566            | 8.11               | 8.57     | 491             | 387             | 573             | 618             |
| 203x76                   | 47.6                 | 60.8            | 120                | 3910                  | 4330            | 8.02               | 8.44     | 385             | 318             | 452             | 495             |
| 178x89                   | 53.6                 | 68.3            | 80                 | 3506                  | 3600            | 7.17               | 7.26     | 394             | 279             | 459             | 461             |
| 178x76                   | 41.7                 | 53.1            | 100                | 2676                  | 3024            | 7.10               | 7.55     | 301             | 240             | 351             | 383             |
| 152x89                   | 47.7                 | 60.8            | 60                 | 2337                  | 2527            | 6.20               | 6.45     | 307             | 213             | 356             | 357             |
| 152x76                   | 35.8                 | 45.6            | 70                 | 1703                  | 1714            | 6.11               | 6.13     | 224             | 154             | 260             | 260             |
| 127x64                   | 29.8                 | 38.0            | 55                 | 965                   | 970             | 5.04               | 5.05     | 152             | 107             | 179             | 178             |
| 102x51                   | 20.8♦                | 26.5            | 45                 | 415                   | 433             | 3.95               | 4.04     | 81.6            | 59.1            | 97.3            | 99.8            |
| 76x38                    | 13.4♦                | 17.1            | 30                 | 149                   | 146             | 2.95               | 2.92     | 39.0            | 27.4            | 46.9            | 46.1            |

♦ Check availability of section

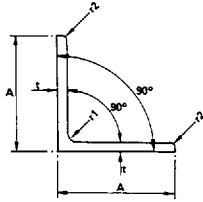
COMPOUND STRUTS  
TWO CHANNELS BACK TO BACK



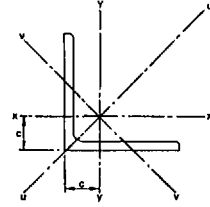
GROSS DIMENSIONS AND SECTION PROPERTIES

| Composed Of Two Channels<br>mm | Total Mass Per Metre<br>kg | Total Area<br>cm <sup>2</sup> | Properties About Axis x-x          |                       |                                    |                                    | Radius of Gyration r <sub>yy</sub> About Axis y-y in cm |      |      |      |      |
|--------------------------------|----------------------------|-------------------------------|------------------------------------|-----------------------|------------------------------------|------------------------------------|---|------|------|------|------|
|                                |                            |                               | I <sub>xx</sub><br>cm <sup>4</sup> | r <sub>xx</sub><br>cm | Z <sub>xx</sub><br>cm <sup>3</sup> | S <sub>xx</sub><br>cm <sup>3</sup> | Space between webs in mm                                |      |      |      |      |
|                                |                            |                               |                                    |                       |                                    |                                    | 0   | 8    | 10   | 12   | 15   |
| 432x102                        | 131                        | 167                           | 42750                              | 16.0                  | 1980                               | 2411                               | 3.59  | 3.86 | 3.93 | 4.00 | 4.11 |
| 381x102                        | 110                        | 140                           | 29740                              | 14.6                  | 1561                               | 1862                               | 3.82  | 4.09 | 4.17 | 4.24 | 4.35 |
| 305x102                        | 92.4                       | 118                           | 16420                              | 11.8                  | 1077                               | 1276                               | 3.94  | 4.22 | 4.29 | 4.37 | 4.48 |
| 305x89                         | 83.4                       | 107                           | 14160                              | 11.5                  | 929                                | 1117                               | 3.30  | 3.57 | 3.65 | 3.72 | 3.84 |
| 254x89                         | 71.5                       | 90.9                          | 8891                               | 9.89                  | 700                                | 828                                | 3.54  | 3.82 | 3.90 | 3.97 | 4.09 |
| 254x76                         | 56.6                       | 71.8                          | 6710                               | 9.67                  | 528                                | 632                                | 2.82  | 3.10 | 3.17 | 3.25 | 3.36 |
| 229x89                         | 65.5                       | 83.3                          | 6766                               | 9.01                  | 592                                | 696                                | 3.64  | 3.93 | 4.00 | 4.08 | 4.20 |
| 229x76                         | 52.1                       | 66.4                          | 5231                               | 8.87                  | 458                                | 542                                | 2.97  | 3.25 | 3.32 | 3.40 | 3.52 |
| 203x89                         | 59.6                       | 75.9                          | 4985                               | 8.11                  | 491                                | 573                                | 3.74  | 4.03 | 4.11 | 4.19 | 4.30 |
| 203x76                         | 47.6                       | 60.8                          | 3910                               | 8.02                  | 385                                | 452                                | 3.09  | 3.38 | 3.46 | 3.54 | 3.65 |
| 178x89                         | 53.6                       | 68.3                          | 3506                               | 7.17                  | 394                                | 459                                | 3.83  | 4.13 | 4.20 | 4.28 | 4.40 |
| 178x76                         | 41.7                       | 53.1                          | 2676                               | 7.10                  | 301                                | 351                                | 3.15  | 3.44 | 3.52 | 3.59 | 3.71 |
| 152x89                         | 47.7                       | 60.8                          | 2337                               | 6.20                  | 307                                | 356                                | 3.91  | 4.22 | 4.29 | 4.37 | 4.49 |
| 152x76                         | 35.8                       | 45.6                          | 1703                               | 6.11                  | 224                                | 260                                | 3.14  | 3.43 | 3.51 | 3.59 | 3.71 |
| 127x64                         | 29.8                       | 38.0                          | 965                                | 5.04                  | 152                                | 179                                | 2.70  | 3.00 | 3.08 | 3.16 | 3.28 |
| 102x51                         | 20.8◆                      | 26.5                          | 415                                | 3.95                  | 81.6                               | 97.3                               | 2.12  | 2.42 | 2.50 | 2.58 | 2.70 |
| 76x38                          | 13.4◆                      | 17.1                          | 149                                | 2.95                  | 39.0                               | 46.9                               | 1.64  | 1.95 | 2.03 | 2.11 | 2.24 |

◆ Check availability of section  
Properties about y-y axis:  
I<sub>yy</sub> = (Total area) (r<sub>yy</sub>)<sup>2</sup>  
Z<sub>yy</sub> = I<sub>yy</sub> (B + 0.5s)  
where s is the space between webs



**EQUAL ANGLES**



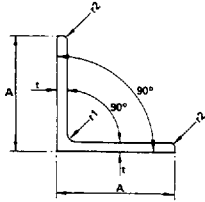
**DIMENSIONS AND PROPERTIES**

| Designation |           | Mass Per Metre<br>kg | Radius |     | Area Of Section<br>cm <sup>2</sup> | Distance Of Centre Of Gravity<br>cx and cy<br>cm | Second Moment Of Area            |                             |                             | Radius Of Gyration  |                |                | Elastic Modulus<br>Axis X-X, Y-Y<br>cm <sup>3</sup> |
|-------------|-----------|----------------------|--------|-----|------------------------------------|--|----------------------------------|-----------------------------|-----------------------------|---------------------|----------------|----------------|---|
| Size        | Thickness |                      | Root   | Toe |                                    |  | Axis X-X, Y-Y<br>cm <sup>4</sup> | Axis U-U<br>cm <sup>4</sup> | Axis V-V<br>cm <sup>4</sup> | Axis X-X, Y-Y<br>cm | Axis U-U<br>cm | Axis V-V<br>cm |   |
| A           | A         | t                    | r1     | r2  |                                    |  |                                  |                             |                             |                     |                |                |   |
| 250x250     | 35        | 128                  | 20.0   | 4.8 | 164                                | 7.51   | 9305                             | 14720                       | 3886                        | 7.54                | 9.49           | 4.88           | 532   |
|             | 32        | 118                  | 20.0   | 4.8 | 151                                | 7.40   | 8650                             | 13710                       | 3592                        | 7.58                | 9.54           | 4.89           | 491   |
|             | 28        | 104                  | 20.0   | 4.8 | 133                                | 7.25   | 7741                             | 12290                       | 3194                        | 7.63                | 9.61           | 4.90           | 436   |
|             | 25        | 93.6                 | 20.0   | 4.8 | 120                                | 7.14   | 7030                             | 11170                       | 2890                        | 7.67                | 9.67           | 4.92           | 394   |
| 200x200     | 24        | 71.1                 | 18.0   | 4.8 | 90.8                               | 5.85   | 3356                             | 5322                        | 1391                        | 6.08                | 7.65           | 3.91           | 237   |
|             | 20        | 59.9                 | 18.0   | 4.8 | 76.6                               | 5.70   | 2877                             | 4569                        | 1185                        | 6.13                | 7.72           | 3.93           | 201   |
|             | 18        | 54.2                 | 18.0   | 4.8 | 69.4                               | 5.62   | 2627                             | 4174                        | 1090                        | 6.15                | 7.76           | 3.95           | 183   |
|             | 16        | 48.5                 | 18.0   | 4.8 | 62.0                               | 5.54   | 2369                             | 3765                        | 973                         | 6.18                | 7.79           | 3.96           | 164   |
| 150x150     | 18        | 40.1                 | 16.0   | 4.8 | 51.2                               | 4.38   | 1060                             | 1680                        | 440                         | 4.55                | 5.73           | 2.93           | 99.8  |
|             | 15        | 33.8                 | 16.0   | 4.8 | 43.2                               | 4.26   | 909                              | 1442                        | 375                         | 4.59                | 5.78           | 2.95           | 84.6  |
|             | 12        | 27.3                 | 16.0   | 4.8 | 35.0                               | 4.14   | 748                              | 1187                        | 308                         | 4.62                | 5.82           | 2.97           | 68.9  |
|             | 10        | 23.0                 | 16.0   | 4.8 | 29.5                               | 4.06   | 635                              | 1008                        | 262                         | 4.64                | 5.85           | 2.99           | 58.0  |
| 120x120     | 15        | 26.6                 | 13.0   | 4.8 | 34.0                               | 3.52   | 448                              | 710                         | 186                         | 3.63                | 4.57           | 2.34           | 52.8  |
|             | 12        | 21.6                 | 13.0   | 4.8 | 27.6                               | 3.41   | 371                              | 589                         | 153                         | 3.66                | 4.62           | 2.35           | 43.1  |
|             | 10        | 18.2                 | 13.0   | 4.8 | 23.3                               | 3.32   | 316                              | 502                         | 130                         | 3.69                | 4.65           | 2.37           | 36.4  |
|             | 8         | 14.7                 | 13.0   | 4.8 | 18.8                               | 3.24   | 259                              | 411                         | 107                         | 3.71                | 4.67           | 2.38           | 29.5  |
| 100x100     | 15        | 21.9                 | 12.0   | 4.8 | 28.0                               | 3.02   | 250                              | 395                         | 105                         | 2.99                | 3.76           | 1.94           | 35.8  |
|             | 12        | 17.8                 | 12.0   | 4.8 | 22.8                               | 2.91   | 208                              | 330                         | 86.5                        | 3.02                | 3.81           | 1.95           | 29.4  |
|             | 10+       | 15.0                 | 12.0   | 4.8 | 19.2                               | 2.83   | 178                              | 283                         | 73.7                        | 3.05                | 3.84           | 1.96           | 24.8  |
|             | 8         | 12.2                 | 12.0   | 4.8 | 15.6                               | 2.75   | 146                              | 232                         | 60.5                        | 3.07                | 3.86           | 1.97           | 20.2  |
| 90x90       | 12        | 15.9                 | 11.0   | 4.8 | 20.3                               | 2.66   | 149                              | 235                         | 62.0                        | 2.70                | 3.40           | 1.75           | 23.5  |
|             | 10        | 13.4                 | 11.0   | 4.8 | 17.2                               | 2.58   | 128                              | 202                         | 52.9                        | 2.73                | 3.43           | 1.76           | 19.9  |
|             | 8         | 10.9                 | 11.0   | 4.8 | 13.9                               | 2.50   | 105                              | 167                         | 43.4                        | 2.75                | 3.46           | 1.77           | 16.2  |
|             | 7♦        | 9.61                 | 11.0   | 4.8 | 12.3                               | 2.46   | 93.2                             | 148                         | 38.6                        | 2.76                | 3.47           | 1.77           | 14.3  |
|             | 6         | 8.30                 | 11.0   | 4.8 | 10.6                               | 2.41   | 81.0                             | 128                         | 33.6                        | 2.76                | 3.48           | 1.78           | 12.3  |
| 80x80       | 10        | 11.9                 | 10.0   | 4.8 | 15.1                               | 2.34   | 87.6                             | 139                         | 36.4                        | 2.41                | 3.03           | 1.55           | 15.5  |
|             | 8         | 9.63                 | 10.0   | 4.8 | 12.3                               | 2.26   | 72.4                             | 115                         | 29.9                        | 2.43                | 3.06           | 1.56           | 12.6  |
|             | 6         | 7.34                 | 10.0   | 4.8 | 9.36                               | 2.17   | 56.0                             | 88.7                        | 23.2                        | 2.45                | 3.08           | 1.57           | 9.60  |

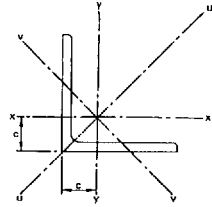
+ Section not included in BS4848: Part 4

♦ Check availability of section

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3



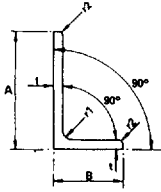
EQUAL ANGLES



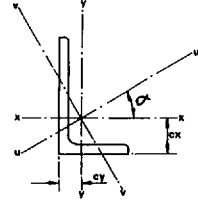
DIMENSIONS AND PROPERTIES

| Designation |           | Mass<br>Per<br>Metre | Radius |          | Area<br>Of<br>Section | Distance Of<br>Centre Of<br>Gravity<br>cx and cy | Second Moment Of Area |                 |                 | Radius Of Gyration |             |             | Elastic<br>Modulus |                  |
|-------------|-----------|----------------------|--------|----------|-----------------------|--|-----------------------|-----------------|-----------------|--------------------|-------------|-------------|--------------------|------------------|
| Size        | Thickness |                      | Root   | Toe      |                       |  | Axis<br>x-x, y-y      | Axis<br>u-u     | Axis<br>v-v     | Axis<br>x-x, y-y   | Axis<br>u u | Axis<br>v-v |                    | Axis<br>x-x, y-y |
| A<br>mm     | A<br>mm   | t<br>mm              | kg     | r1<br>mm | r2<br>mm              | cm <sup>2</sup>                                  | cm                    | cm <sup>4</sup> | cm <sup>4</sup> | cm <sup>4</sup>    | cm          | cm          | cm                 | cm <sup>3</sup>  |
| 70x70       | 10        | 10.3                 | 9.0    | 2.4      | 13.1                  | 2.10   | 58.0                  | 91.6            | 24.4            | 2.10               | 2.64        | 1.36        | 11.8               |                  |
|             | 8         | 8.36                 | 9.0    | 2.4      | 10.7                  | 2.02   | 48.3                  | 76.5            | 20.1            | 2.12               | 2.67        | 1.37        | 9.70               |                  |
|             | 6         | 6.38                 | 9.0    | 2.4      | 8.19                  | 1.94   | 37.7                  | 59.8            | 15.6            | 2.15               | 2.70        | 1.38        | 7.46               |                  |
| 60x60       | 10        | 8.69                 | 8.0    | 2.4      | 11.1                  | 1.85   | 35.3                  | 55.6            | 15.0            | 1.78               | 2.24        | 1.16        | 8.51               |                  |
|             | 8         | 7.09                 | 8.0    | 2.4      | 9.07                  | 1.78   | 29.6                  | 46.7            | 12.4            | 1.80               | 2.27        | 1.17        | 7.00               |                  |
|             | 6         | 5.42                 | 8.0    | 2.4      | 6.95                  | 1.70   | 23.2                  | 36.8            | 9.64            | 1.83               | 2.30        | 1.18        | 5.39               |                  |
|             | 5         | 4.57                 | 8.0    | 2.4      | 5.86                  | 1.65   | 19.8                  | 31.4            | 8.23            | 1.84               | 2.31        | 1.18        | 4.56               |                  |
| 50x50       | 8         | 5.82                 | 7.0    | 2.4      | 7.44                  | 1.53   | 16.5                  | 25.9            | 6.96            | 1.49               | 1.87        | 0.968       | 4.74               |                  |
|             | 6         | 4.47                 | 7.0    | 2.4      | 5.72                  | 1.45   | 13.0                  | 20.6            | 5.43            | 1.51               | 1.90        | 0.974       | 3.67               |                  |
|             | 5         | 3.77                 | 7.0    | 2.4      | 4.83                  | 1.41   | 11.1                  | 17.7            | 4.63            | 1.52               | 1.91        | 0.979       | 3.11               |                  |
|             | 4         | 3.06                 | 7.0    | 2.4      | 3.92                  | 1.37   | 9.16                  | 14.5            | 3.82            | 1.53               | 1.92        | 0.987       | 2.52               |                  |
|             | 3         | 2.33                 | 7.0    | 2.4      | 2.99                  | 1.32   | 7.06                  | 11.1            | 2.97            | 1.54               | 1.93        | 0.996       | 1.92               |                  |
| 45x45       | 6         | 4.00                 | 7.0    | 2.4      | 5.12                  | 1.33   | 9.30                  | 14.7            | 3.90            | 1.35               | 1.89        | 0.872       | 2.93               |                  |
|             | 5         | 3.38                 | 7.0    | 2.4      | 4.33                  | 1.29   | 7.99                  | 12.6            | 3.33            | 1.36               | 1.71        | 0.877       | 2.48               |                  |
|             | 4         | 2.74                 | 7.0    | 2.4      | 3.52                  | 1.24   | 6.58                  | 10.4            | 2.75            | 1.37               | 1.72        | 0.883       | 2.02               |                  |
|             | 3         | 2.09                 | 7.0    | 2.4      | 2.69                  | 1.20   | 5.08                  | 8.03            | 2.14            | 1.37               | 1.73        | 0.892       | 1.54               |                  |
| 40x40       | 6         | 3.52                 | 6.0    | 2.4      | 4.49                  | 1.20   | 6.37                  | 10.1            | 2.68            | 1.19               | 1.50        | 0.773       | 2.28               |                  |
|             | 5         | 2.97                 | 6.0    | 2.4      | 3.80                  | 1.17   | 5.48                  | 8.68            | 2.29            | 1.20               | 1.51        | 0.776       | 1.93               |                  |
|             | 4         | 2.42                 | 6.0    | 2.4      | 3.09                  | 1.12   | 4.53                  | 7.18            | 1.89            | 1.21               | 1.52        | 0.781       | 1.58               |                  |
|             | 3         | 1.84                 | 6.0    | 2.4      | 2.36                  | 1.08   | 3.51                  | 5.55            | 1.47            | 1.22               | 1.53        | 0.788       | 1.20               |                  |
| 30x30       | 5         | 2.18                 | 5.0    | 2.4      | 2.78                  | 0.919  | 2.17                  | 3.42            | 0.919           | 0.883              | 1.11        | 0.575       | 1.04               |                  |
|             | 4         | 1.78                 | 5.0    | 2.4      | 2.27                  | 0.879  | 1.81                  | 2.85            | 0.756           | 0.893              | 1.12        | 0.577       | 0.852              |                  |
|             | 3         | 1.36                 | 5.0    | 2.4      | 1.74                  | 0.836  | 1.41                  | 2.23            | 0.588           | 0.900              | 1.13        | 0.581       | 0.652              |                  |
| 25x25       | 5         | 1.77                 | 3.5    | 2.4      | 2.25                  | 0.796  | 1.19                  | 1.87            | 0.515           | 0.728              | 0.912       | 0.478       | 0.701              |                  |
|             | 4         | 1.45                 | 3.5    | 2.4      | 1.84                  | 0.758  | 1.00                  | 1.58            | 0.421           | 0.737              | 0.926       | 0.478       | 0.574              |                  |
|             | 3         | 1.11                 | 3.5    | 2.4      | 1.41                  | 0.718  | 0.784                 | 1.24            | 0.325           | 0.745              | 0.939       | 0.480       | 0.440              |                  |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3



**UNEQUAL ANGLES**

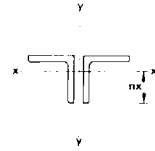
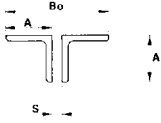


**DIMENSIONS AND PROPERTIES**

| Designation |                         | Mass Per Metre       | Radius               |                   | Area Of Section      | Distance Centre Of Gravity |                      | Second Moment Of Area |                     |                     |                     | Radius Of Gyration   |                      |                      |                      | Elastic Modulus      |                      | Angle x-x Axis to u-u Axis Tan $\alpha$ |       |
|-------------|-------------------------|----------------------|----------------------|-------------------|----------------------|----------------------------|----------------------|-----------------------|---------------------|---------------------|---------------------|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|---|-------|
| Size        | Thick-ness              |                      | Root                 | Toe               |                      | cx cm                      | cy cm                | Axis                  | Axis                | Axis                | Axis                | Axis                 | Axis                 | Axis                 | Axis                 | Axis                 | Axis                 |   |       |
| A mm        | B mm                    | t mm                 | r1 mm                | r2 mm             | cm <sup>2</sup>      |                            |                      | x-x cm <sup>4</sup>   | y-y cm <sup>4</sup> | u-u cm <sup>4</sup> | v-v cm <sup>4</sup> | x-x cm               | y-y cm               | u-u cm               | v-v cm               | x-x cm <sup>3</sup>  | y-y cm <sup>3</sup>  |   |       |
| 200x150     | 18                      | 47.1                 | 15.0                 | 4.8               | 60.1                 | 6.34                       | 3.86                 | 2390                  | 1155                | 2922                | 623                 | 6.30                 | 4.38                 | 6.97                 | 3.22                 | 175                  | 104                  | 0.549                                   |       |
|             | 15                      | 39.6                 | 15.0                 | 4.8               | 50.6                 | 6.22                       | 3.75                 | 2037                  | 989                 | 2495                | 531                 | 6.34                 | 4.42                 | 7.02                 | 3.24                 | 148                  | 87.8                 | 0.551                                   |       |
|             | 12                      | 32.0                 | 15.0                 | 4.8               | 40.9                 | 6.10                       | 3.63                 | 1667                  | 812                 | 2045                | 435                 | 6.38                 | 4.45                 | 7.07                 | 3.26                 | 120                  | 71.4                 | 0.553                                   |       |
| 200x100     | 15                      | 33.7                 | 15.0                 | 4.8               | 43.1                 | 7.17                       | 2.23                 | 1772                  | 303                 | 1879                | 197                 | 6.41                 | 2.65                 | 6.60                 | 2.13                 | 138                  | 39.0                 | 0.260                                   |       |
|             | 12                      | 27.3                 | 15.0                 | 4.8               | 34.9                 | 7.04                       | 2.11                 | 1454                  | 252                 | 1544                | 162                 | 6.45                 | 2.68                 | 6.65                 | 2.15                 | 112                  | 31.9                 | 0.263                                   |       |
|             | 10                      | 23.0                 | 15.0                 | 4.8               | 29.4                 | 6.95                       | 2.03                 | 1233                  | 215                 | 1310                | 138                 | 6.48                 | 2.70                 | 6.68                 | 2.17                 | 94.5                 | 26.9                 | 0.265                                   |       |
| 150x90      | 15                      | 26.6                 | 12.0                 | 4.8               | 34.0                 | 5.21                       | 2.24                 | 764                   | 207                 | 844                 | 127                 | 4.74                 | 2.47                 | 4.99                 | 1.93                 | 78.0                 | 30.6                 | 0.354                                   |       |
|             | 12                      | 21.6                 | 12.0                 | 4.8               | 27.6                 | 5.09                       | 2.12                 | 630                   | 172                 | 698                 | 104                 | 4.78                 | 2.50                 | 5.03                 | 1.95                 | 63.6                 | 25.0                 | 0.359                                   |       |
|             | 10                      | 18.2                 | 12.0                 | 4.8               | 23.2                 | 5.00                       | 2.04                 | 536                   | 147                 | 595                 | 89.1                | 4.81                 | 2.52                 | 5.06                 | 1.96                 | 53.6                 | 21.2                 | 0.361                                   |       |
| 150x75      | 15                      | 24.8                 | 11.0                 | 4.8               | 31.7                 | 5.53                       | 1.81                 | 715                   | 120                 | 756                 | 79.2                | 4.75                 | 1.95                 | 4.89                 | 1.58                 | 75.5                 | 21.1                 | 0.254                                   |       |
|             | 12                      | 20.2                 | 11.0                 | 4.8               | 25.7                 | 5.41                       | 1.70                 | 591                   | 100                 | 626                 | 65.2                | 4.79                 | 1.98                 | 4.93                 | 1.59                 | 61.6                 | 17.3                 | 0.259                                   |       |
|             | 10                      | 17.0                 | 11.0                 | 4.8               | 21.7                 | 5.32                       | 1.62                 | 503                   | 86.3                | 534                 | 55.7                | 4.82                 | 2.00                 | 4.96                 | 1.60                 | 52.0                 | 14.7                 | 0.262                                   |       |
| 137x102     | 9.5 +<br>7.9 +<br>6.4 + | 17.3<br>14.5<br>11.7 | 11.0<br>11.0<br>11.0 | 4.8<br>4.8<br>4.8 | 22.0<br>18.4<br>15.0 | 4.23<br>4.16<br>4.09       | 2.50<br>2.44<br>2.37 | 415<br>351<br>289     | 198<br>168<br>138   | 506<br>428<br>352   | 107<br>90.4<br>74.7 | 4.35<br>4.36<br>4.38 | 3.00<br>3.02<br>3.03 | 4.80<br>4.82<br>4.84 | 2.20<br>2.22<br>2.23 | 43.8<br>36.8<br>30.0 | 25.7<br>21.6<br>17.6 | 0.543<br>0.544<br>0.544                 |       |
|             | 125x75                  | 12                   | 17.8                 | 11.0              | 4.8                  | 22.7                       | 4.31                 | 1.84                  | 355                 | 96.0                | 392                 | 58.8                 | 3.95                 | 2.06                 | 4.16                 | 1.61                 | 43.4                 | 17.0                                    | 0.354 |
|             |                         | 10                   | 15.0                 | 11.0              | 4.8                  | 19.2                       | 4.23                 | 1.76                  | 303                 | 82.5                | 336                 | 50.2                 | 3.98                 | 2.08                 | 4.19                 | 1.62                 | 36.7                 | 14.4                                    | 0.358 |
| 8           |                         | 12.2                 | 11.0                 | 4.8               | 15.5                 | 4.14                       | 1.68                 | 249                   | 68.1                | 275                 | 41.2                | 4.00                 | 2.10                 | 4.21                 | 1.63                 | 29.7                 | 11.7                 | 0.360                                   |       |
| 100x75      | 12                      | 15.4                 | 10.0                 | 4.8               | 19.7                 | 3.27                       | 2.03                 | 189                   | 90.3                | 230                 | 49.5                | 3.10                 | 2.14                 | 3.42                 | 1.59                 | 28.1                 | 16.5                 | 0.540                                   |       |
|             | 10                      | 13.0                 | 10.0                 | 4.8               | 16.6                 | 3.19                       | 1.95                 | 162                   | 77.7                | 198                 | 42.2                | 3.12                 | 2.16                 | 3.45                 | 1.59                 | 23.8                 | 14.0                 | 0.544                                   |       |
|             | 8                       | 10.6                 | 10.0                 | 4.8               | 13.5                 | 3.10                       | 1.87                 | 133                   | 64.2                | 163                 | 34.7                | 3.14                 | 2.18                 | 3.48                 | 1.61                 | 19.3                 | 11.4                 | 0.547                                   |       |
| 100x65      | 10                      | 12.3                 | 10.0                 | 4.8               | 15.6                 | 3.36                       | 1.63                 | 154                   | 51.1                | 175                 | 30.2                | 3.14                 | 1.81                 | 3.35                 | 1.39                 | 23.2                 | 10.5                 | 0.410                                   |       |
|             | 8                       | 9.94                 | 10.0                 | 4.8               | 12.7                 | 3.28                       | 1.56                 | 127                   | 42.3                | 144                 | 24.9                | 3.17                 | 1.83                 | 3.38                 | 1.40                 | 18.9                 | 8.56                 | 0.414                                   |       |
|             | 7                       | 8.77                 | 10.0                 | 4.8               | 11.2                 | 3.23                       | 1.51                 | 113                   | 37.7                | 128                 | 22.1                | 3.18                 | 1.84                 | 3.39                 | 1.41                 | 16.6                 | 7.56                 | 0.415                                   |       |
| 80x60       | 8                       | 8.34                 | 8.0                  | 4.8               | 10.6                 | 2.55                       | 1.56                 | 65.8                  | 31.5                | 80.2                | 17.1                | 2.49                 | 1.72                 | 2.75                 | 1.27                 | 12.1                 | 7.09                 | 0.544                                   |       |
|             | 7                       | 7.36                 | 8.0                  | 4.8               | 9.35                 | 2.50                       | 1.52                 | 58.5                  | 28.1                | 71.4                | 15.2                | 2.50                 | 1.73                 | 2.76                 | 1.27                 | 10.6                 | 6.26                 | 0.545                                   |       |
|             | 6                       | 6.37                 | 8.0                  | 4.8               | 8.08                 | 2.46                       | 1.48                 | 50.9                  | 24.5                | 62.2                | 13.2                | 2.51                 | 1.74                 | 2.77                 | 1.28                 | 9.19                 | 5.41                 | 0.546                                   |       |
| 75x50       | 8                       | 7.39                 | 7.0                  | 2.4               | 9.44                 | 2.53                       | 1.29                 | 52.4                  | 18.6                | 60.1                | 10.9                | 2.36                 | 1.40                 | 2.52                 | 1.07                 | 10.5                 | 5.00                 | 0.430                                   |       |
|             | 6                       | 5.65                 | 7.0                  | 2.4               | 7.22                 | 2.44                       | 1.21                 | 40.9                  | 14.6                | 47.1                | 8.48                | 2.38                 | 1.42                 | 2.55                 | 1.08                 | 8.10                 | 3.87                 | 0.436                                   |       |
|             | 65x50                   | 8                    | 6.75                 | 6.0               | 2.4                  | 8.61                       | 2.12                 | 1.37                  | 34.9                | 17.8                | 43.1                | 9.62                 | 2.01                 | 1.44                 | 2.24                 | 1.06                 | 7.97                 | 4.92                                    | 0.569 |
| 6           |                         | 5.16                 | 6.0                  | 2.4               | 6.59                 | 2.04                       | 1.30                 | 27.4                  | 14.1                | 34.0                | 7.49                | 2.04                 | 1.46                 | 2.27                 | 1.07                 | 6.14                 | 3.90                 | 0.575                                   |       |
| 5           |                         | 4.35                 | 6.0                  | 2.4               | 5.55                 | 2.00                       | 1.26                 | 23.3                  | 12.0                | 29.0                | 6.38                | 2.05                 | 1.47                 | 2.28                 | 1.07                 | 5.18                 | 3.21                 | 0.577                                   |       |
| 60x30       | 6                       | 3.99                 | 6.0                  | 2.4               | 5.09                 | 2.20                       | 0.724                | 18.3                  | 3.05                | 19.3                | 2.01                | 1.90                 | 0.774                | 1.95                 | 0.629                | 4.82                 | 1.34                 | 0.252                                   |       |
|             | 5                       | 3.37                 | 6.0                  | 2.4               | 4.30                 | 2.16                       | 0.684                | 15.7                  | 2.64                | 16.6                | 1.72                | 1.91                 | 0.783                | 1.96                 | 0.632                | 4.08                 | 1.14                 | 0.256                                   |       |
|             | 40x25                   | 4                    | 1.93                 | 4.0               | 2.4                  | 2.45                       | 1.36                 | 0.621                 | 3.86                | 1.15                | 4.32                | 0.692                | 1.26                 | 0.685                | 1.33                 | 0.532                | 1.46                 | 0.612                                   | 0.380 |

+ Sections marked thus are not included in BS4848: Part4  
FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

COMPOUND EQUAL ANGLES  
LEGS BACK TO BACK



GROSS DIMENSIONS AND SECTION PROPERTIES

| Composed Of Two Angles |         |         | Total Mass Per Metre<br>kg | Distance nx<br>cm | Total Area<br>cm <sup>2</sup> | Properties About Axis x-x |           |                        | Radius Of Gyration ryy About Axis y-y in cm |      |      |      |    |
|------------------------|---------|---------|----------------------------|-------------------|-------------------------------|---------------------------|-----------|------------------------|---|------|------|------|----|
| A<br>mm                | A<br>mm | t<br>mm |                            |                   |                               | Ixx<br>cm <sup>4</sup>    | rxx<br>cm | Zxx<br>cm <sup>3</sup> | Back To Back Spacing, s, in mm              |      |      |      |    |
|                        |         |         |                            |                   |                               |                           |           |                        | 0   | 8    | 10   | 12   | 15 |
| 250x250                | 35      | 256     | 17.5                       | 327               | 18610                         | 7.54                      | 1064      | 10.6                   | 10.9  | 11.0 | 11.1 | 11.2 |    |
|                        | 32      | 236     | 17.6                       | 301               | 17300                         | 7.58                      | 983       | 10.6                   | 10.9  | 10.9 | 11.0 | 11.1 |    |
|                        | 28      | 208     | 17.8                       | 266               | 15480                         | 7.83                      | 872       | 10.5                   | 10.8  | 10.9 | 10.9 | 11.1 |    |
|                        | 25      | 187     | 17.9                       | 239               | 14060                         | 7.87                      | 787       | 10.5                   | 10.8  | 10.8 | 10.9 | 11.0 |    |
| 200x200                | 24      | 142     | 14.1                       | 182               | 6713                          | 6.08                      | 474       | 8.44                   | 8.72  | 8.79 | 8.86 | 8.97 |    |
|                        | 20      | 120     | 14.3                       | 153               | 5754                          | 6.13                      | 402       | 8.37                   | 8.65  | 8.72 | 8.79 | 8.90 |    |
|                        | 18      | 108     | 14.4                       | 139               | 5253                          | 6.15                      | 365       | 8.34                   | 8.61  | 8.68 | 8.75 | 8.86 |    |
|                        | 16      | 97.0    | 14.5                       | 124               | 4737                          | 6.18                      | 328       | 8.30                   | 8.57  | 8.64 | 8.71 | 8.82 |    |
| 150x150                | 18      | 80.2    | 10.6                       | 102               | 2120                          | 4.55                      | 200       | 6.31                   | 6.60  | 6.67 | 6.74 | 6.86 |    |
|                        | 15      | 67.6    | 10.7                       | 86.4              | 1817                          | 4.59                      | 169       | 6.26                   | 6.54  | 6.61 | 6.68 | 6.79 |    |
|                        | 12      | 54.6    | 10.9                       | 70.0              | 1496                          | 4.62                      | 138       | 6.21                   | 6.48  | 6.55 | 6.62 | 6.73 |    |
|                        | 10      | 46.0    | 10.9                       | 58.9              | 1270                          | 4.64                      | 116       | 6.17                   | 6.44  | 6.51 | 6.58 | 6.68 |    |
| 120x120                | 15      | 53.2    | 8.48                       | 68.0              | 896                           | 3.63                      | 106       | 5.06                   | 5.34  | 5.42 | 5.49 | 5.61 |    |
|                        | 12      | 43.2    | 8.59                       | 55.2              | 742                           | 3.66                      | 86.3      | 5.00                   | 5.28  | 5.36 | 5.43 | 5.54 |    |
|                        | 10      | 36.4    | 8.68                       | 46.5              | 632                           | 3.69                      | 72.9      | 4.96                   | 5.24  | 5.31 | 5.38 | 5.50 |    |
|                        | 8       | 29.4    | 8.76                       | 37.6              | 517                           | 3.71                      | 59.1      | 4.92                   | 5.19  | 5.27 | 5.34 | 5.45 |    |
| 100x100                | 15      | 43.8    | 6.98                       | 55.9              | 500                           | 2.99                      | 71.7      | 4.25                   | 4.55  | 4.62 | 4.70 | 4.82 |    |
|                        | 12      | 35.6    | 7.09                       | 45.5              | 416                           | 3.02                      | 58.7      | 4.20                   | 4.48  | 4.56 | 4.63 | 4.75 |    |
|                        | 10+     | 30.0    | 7.17                       | 38.4              | 356                           | 3.05                      | 49.7      | 4.16                   | 4.44  | 4.51 | 4.59 | 4.70 |    |
|                        | 8       | 24.4    | 7.25                       | 31.1              | 293                           | 3.07                      | 40.4      | 4.12                   | 4.39  | 4.47 | 4.54 | 4.65 |    |
| 90x90                  | 12      | 31.8    | 6.34                       | 40.6              | 297                           | 2.70                      | 46.9      | 3.80                   | 4.09  | 4.16 | 4.24 | 4.35 |    |
|                        | 10      | 26.8    | 6.42                       | 34.3              | 255                           | 2.73                      | 39.8      | 3.76                   | 4.04  | 4.12 | 4.19 | 4.31 |    |
|                        | 8       | 21.8    | 6.50                       | 27.8              | 210                           | 2.75                      | 32.3      | 3.72                   | 4.00  | 4.07 | 4.14 | 4.26 |    |
|                        | 7♦      | 19.2    | 6.54                       | 24.5              | 186                           | 2.76                      | 28.5      | 3.69                   | 3.97  | 4.04 | 4.12 | 4.23 |    |
|                        | 6       | 16.6    | 6.59                       | 21.2              | 162                           | 2.76                      | 24.6      | 3.67                   | 3.94  | 4.02 | 4.09 | 4.20 |    |
| 80x80                  | 10      | 23.8    | 5.66                       | 30.2              | 175                           | 2.41                      | 31.0      | 3.36                   | 3.65  | 3.72 | 3.80 | 3.92 |    |
|                        | 8       | 19.3    | 5.74                       | 24.6              | 145                           | 2.43                      | 25.2      | 3.31                   | 3.60  | 3.67 | 3.75 | 3.87 |    |
|                        | 6       | 14.7    | 5.83                       | 18.7              | 112                           | 2.45                      | 19.2      | 3.27                   | 3.55  | 3.62 | 3.70 | 3.81 |    |
| 70x70                  | 10      | 20.6    | 4.90                       | 26.3              | 116                           | 2.10                      | 23.7      | 2.97                   | 3.27  | 3.34 | 3.42 | 3.54 |    |
|                        | 8       | 16.7    | 4.98                       | 21.4              | 96.6                          | 2.12                      | 19.4      | 2.93                   | 3.22  | 3.30 | 3.38 | 3.49 |    |
|                        | 6       | 12.8    | 5.06                       | 16.4              | 75.4                          | 2.15                      | 14.9      | 2.89                   | 3.18  | 3.25 | 3.33 | 3.44 |    |
| 60x60                  | 10      | 17.4    | 4.15                       | 22.2              | 70.6                          | 1.78                      | 17.0      | 2.57                   | 2.87  | 2.95 | 3.03 | 3.15 |    |
|                        | 8       | 14.2    | 4.22                       | 18.1              | 59.1                          | 1.80                      | 14.0      | 2.53                   | 2.83  | 2.91 | 2.98 | 3.11 |    |
|                        | 6       | 10.8    | 4.30                       | 13.9              | 46.4                          | 1.83                      | 10.8      | 2.49                   | 2.78  | 2.86 | 2.94 | 3.06 |    |
|                        | 5       | 9.14    | 4.35                       | 11.7              | 39.6                          | 1.84                      | 9.11      | 2.47                   | 2.76  | 2.83 | 2.91 | 3.03 |    |

+ Section not included in BS4848: Part 4

♦ Check availability of section

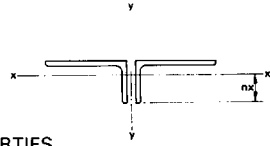
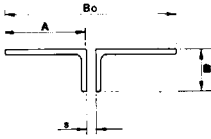
Properties about y-y axis:

$I_{yy} = (\text{Total area}) (r_{yy})^2$

$Z_{yy} = I_{yy} / (0.5Bo)$



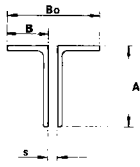
**COMPOUND UNEQUAL ANGLES  
SHORT LEGS BACK TO BACK**



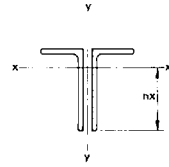
**GROSS DIMENSIONS AND SECTION PROPERTIES**

| Composed Of Two Angles |                         |                | Total Mass Per Metre<br>kg | Distance rx<br>cm    | Total Area<br>cm <sup>2</sup> | Properties About Axis x-x |                      |                        | Radius Of Gyration ryy About Axis y-y in cm |                      |                      |                      |                      |                      |                      |
|------------------------|-------------------------|----------------|----------------------------|----------------------|-------------------------------|---------------------------|----------------------|------------------------|---|----------------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| A<br>mm                | B<br>mm                 | t<br>mm        |                            |                      |                               | lxx<br>cm <sup>4</sup>    | rxx<br>cm            | Zxx<br>cm <sup>3</sup> | Back To Back Spacing, s, in mm              |                      |                      |                      |                      |                      |                      |
|                        |                         |                |                            |                      |                               |                           |                      |                        | 0   | 8                    | 10                   | 12                   | 15                   |                      |                      |
| 200x150                | 18                      | 15             | 12                         | 94.2                 | 11.1                          | 120                       | 2310                 | 4.38                   | 207   | 8.94                 | 9.23                 | 9.30                 | 9.38                 | 9.49                 |                      |
|                        | 15                      | 12             | 15                         | 79.2                 | 11.3                          | 101                       | 1977                 | 4.42                   | 176   | 8.88                 | 9.17                 | 9.24                 | 9.32                 | 9.43                 |                      |
|                        | 12                      | 15             | 12                         | 64.0                 | 11.4                          | 81.9                      | 1625                 | 4.45                   | 143   | 8.83                 | 9.11                 | 9.18                 | 9.25                 | 9.36                 |                      |
| 200x100                | 15                      | 12             | 10                         | 67.4                 | 7.77                          | 86.3                      | 607                  | 2.65                   | 78.0  | 9.62                 | 9.92                 | 10.0                 | 10.1                 | 10.2                 |                      |
|                        | 12                      | 10             | 15                         | 54.6                 | 7.89                          | 69.9                      | 503                  | 2.68                   | 63.8  | 9.55                 | 9.85                 | 9.92                 | 10.0                 | 10.1                 |                      |
|                        | 10                      | 15             | 10                         | 46.0                 | 7.97                          | 58.8                      | 430                  | 2.70                   | 53.9  | 9.50                 | 9.79                 | 9.87                 | 9.95                 | 10.1                 |                      |
| 150x90                 | 15                      | 12             | 10                         | 53.2                 | 6.76                          | 67.9                      | 413                  | 2.47                   | 61.1  | 7.05                 | 7.35                 | 7.42                 | 7.50                 | 7.62                 |                      |
|                        | 12                      | 10             | 15                         | 43.2                 | 6.88                          | 55.1                      | 344                  | 2.50                   | 50.1  | 6.98                 | 7.28                 | 7.35                 | 7.43                 | 7.55                 |                      |
|                        | 10                      | 15             | 10                         | 36.4                 | 6.96                          | 46.4                      | 295                  | 2.52                   | 42.4  | 6.94                 | 7.23                 | 7.31                 | 7.38                 | 7.50                 |                      |
| 150x75                 | 15                      | 12             | 10                         | 49.6                 | 5.69                          | 63.3                      | 240                  | 1.95                   | 42.2  | 7.29                 | 7.60                 | 7.68                 | 7.76                 | 7.88                 |                      |
|                        | 12                      | 10             | 15                         | 40.4                 | 5.80                          | 51.4                      | 201                  | 1.98                   | 34.6  | 7.23                 | 7.53                 | 7.61                 | 7.69                 | 7.80                 |                      |
|                        | 10                      | 15             | 10                         | 34.0                 | 5.88                          | 43.3                      | 173                  | 2.00                   | 29.3  | 7.18                 | 7.48                 | 7.56                 | 7.64                 | 7.75                 |                      |
| 137x102                | 9.5 +<br>7.9 +<br>6.4 + | 15<br>12<br>10 | 10<br>15<br>10             | 34.6<br>19.0<br>23.4 | 7.70<br>7.76<br>7.83          | 43.9<br>36.8<br>30.1      | 395<br>335<br>276    | 3.00<br>3.02<br>3.03   | 51.3<br>43.2<br>35.3                        | 6.07<br>6.03<br>5.99 | 6.35<br>6.31<br>6.27 | 6.42<br>6.39<br>6.35 | 6.50<br>6.46<br>6.42 | 6.61<br>6.57<br>6.53 |                      |
|                        | 125x75                  | 12             | 10                         | 8                    | 35.6<br>30.0<br>24.4          | 5.66<br>5.74<br>5.82      | 45.4<br>38.3<br>31.0 | 192<br>165<br>136      | 2.06<br>2.08<br>2.10                        | 33.9<br>28.8<br>23.4 | 5.85<br>5.81<br>5.76 | 6.15<br>6.10<br>6.05 | 6.23<br>6.18<br>6.13 | 6.31<br>6.26<br>6.20 | 6.42<br>6.37<br>6.32 |
|                        |                         | 8              | 10                         | 8                    | 20.0                          | 5.88                      | 25.5                 | 113                    | 2.11  | 19.2                 | 5.72                 | 6.01                 | 6.08                 | 6.16                 | 6.27                 |
| 100x75                 |                         | 12             | 10                         | 8                    | 30.8<br>26.0<br>21.2          | 5.47<br>5.55<br>5.63      | 39.4<br>33.2<br>27.0 | 181<br>155<br>128      | 2.14<br>2.16<br>2.18                        | 33.0<br>28.0<br>22.8 | 4.50<br>4.46<br>4.42 | 4.80<br>4.76<br>4.71 | 4.88<br>4.83<br>4.78 | 4.96<br>4.91<br>4.86 | 5.07<br>5.03<br>4.98 |
|                        | 100x65                  | 10             | 8                          | 7                    | 24.6<br>19.9<br>17.5          | 4.87<br>4.94<br>4.99      | 31.2<br>25.4<br>22.4 | 102<br>84.7<br>75.4    | 1.81<br>1.83<br>1.84                        | 21.0<br>17.1<br>15.1 | 4.60<br>4.56<br>4.53 | 4.90<br>4.85<br>4.82 | 4.98<br>4.93<br>4.90 | 5.06<br>5.00<br>4.98 | 5.17<br>5.12<br>5.09 |
|                        |                         | 80x60          | 8                          | 7                    | 6                             | 16.7<br>14.7<br>12.7      | 4.44<br>4.48<br>4.52 | 21.2<br>18.7<br>16.2   | 63.0<br>56.1<br>49.0                        | 1.72<br>1.73<br>1.74 | 14.2<br>12.5<br>10.8 | 3.56<br>3.54<br>3.51 | 3.86<br>3.83<br>3.81 | 3.93<br>3.91<br>3.88 | 4.01<br>3.99<br>3.96 |
| 75x50                  |                         |                | 8                          | 6                    | 8                             | 14.8<br>11.3              | 3.71<br>3.79         | 18.9<br>14.4           | 37.1<br>29.3                                | 1.40<br>1.42         | 10.0<br>7.73         | 3.45<br>3.41         | 3.76<br>3.71         | 3.83<br>3.79         | 3.91<br>3.87         |
|                        | 65x50                   |                | 8                          | 6                    | 5                             | 13.5<br>10.3<br>8.70      | 3.63<br>3.70<br>3.74 | 17.2<br>13.2<br>11.1   | 35.7<br>28.1<br>24.1                        | 1.44<br>1.46<br>1.47 | 9.83<br>7.60<br>6.43 | 2.92<br>2.88<br>2.86 | 3.22<br>3.18<br>3.15 | 3.30<br>3.26<br>3.23 | 3.38<br>3.33<br>3.31 |
|                        |                         | 60x30          | 6                          | 5                    | 6                             | 7.98<br>6.74              | 2.28<br>2.32         | 10.2<br>8.61           | 6.11<br>5.27                                | 0.774<br>0.783       | 2.68<br>2.28         | 2.90<br>2.88         | 3.22<br>3.19         | 3.30<br>3.27         | 3.38<br>3.35         |

+ Sections marked thus are not included in BS4848: Part 4  
 Properties about y-y axis:  
 $I_{yy} = (Total\ area)(r_{yy})^2$   
 $Z_{yy} = I_{yy}/(0.5B_0)$



**COMPOUND UNEQUAL ANGLES  
LONG LEGS BACK TO BACK**



**GROSS DIMENSIONS AND SECTION PROPERTIES**

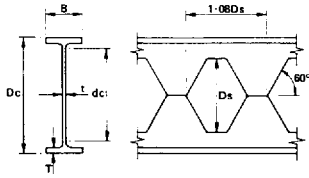
| Composed Of Two Angles |       | Total Mass Per Metre<br>kg | Distance rx<br>cm | Total Area<br>cm <sup>2</sup> | Properties About Axis x-x |          |                        | Radius Of Gyration ryy About Axis y-y in cm |      |      |      |      |
|------------------------|-------|----------------------------|-------------------|-------------------------------|---------------------------|----------|------------------------|---|------|------|------|------|
| A                      | B     |                            |                   |                               | lxx<br>cm <sup>4</sup>    | rx<br>cm | Zxx<br>cm <sup>3</sup> | Back To Back Spacing, s, in mm              |      |      |      |      |
| mm                     | mm    |                            |                   |                               |                           |          |                        | 0   | 8    | 10   | 12   | 15   |
| 200x150                | 18    | 94.2                       | 13.7              | 120                           | 4780                      | 6.30     | 350                    | 5.84  | 6.11 | 6.18 | 6.25 | 6.36 |
|                        | 15    | 79.2                       | 13.8              | 101                           | 4075                      | 6.34     | 296                    | 5.79  | 6.06 | 6.13 | 6.20 | 6.30 |
|                        | 12    | 64.0                       | 13.9              | 81.9                          | 3335                      | 6.38     | 240                    | 5.74  | 6.00 | 6.07 | 6.14 | 6.25 |
| 200x100                | 15    | 67.4                       | 12.8              | 86.3                          | 3545                      | 6.41     | 276                    | 3.46  | 3.73 | 3.81 | 3.88 | 3.99 |
|                        | 12    | 54.6                       | 13.0              | 69.9                          | 2909                      | 6.45     | 224                    | 3.41  | 3.67 | 3.74 | 3.81 | 3.92 |
|                        | 10    | 46.0                       | 13.1              | 58.8                          | 2466                      | 6.48     | 189                    | 3.38  | 3.63 | 3.70 | 3.77 | 3.88 |
| 150x90                 | 15    | 53.2                       | 9.79              | 67.9                          | 1528                      | 4.74     | 156                    | 3.33  | 3.61 | 3.69 | 3.76 | 3.87 |
|                        | 12    | 43.2                       | 9.91              | 55.1                          | 1261                      | 4.78     | 127                    | 3.28  | 3.55 | 3.62 | 3.70 | 3.81 |
|                        | 10    | 36.4                       | 10.0              | 46.4                          | 1073                      | 4.81     | 107                    | 3.24  | 3.51 | 3.58 | 3.65 | 3.76 |
| 150x75                 | 15    | 49.6                       | 9.47              | 63.3                          | 1430                      | 4.75     | 151                    | 2.66  | 2.95 | 3.02 | 3.10 | 3.22 |
|                        | 12    | 40.4                       | 9.59              | 51.4                          | 1181                      | 4.79     | 123                    | 2.60  | 2.88 | 2.96 | 3.03 | 3.15 |
|                        | 10    | 34.0                       | 9.68              | 43.3                          | 1006                      | 4.82     | 104                    | 2.57  | 2.84 | 2.91 | 2.98 | 3.10 |
| 137x102                | 9.5 + | 34.6                       | 9.47              | 43.9                          | 830                       | 4.35     | 87.6                   | 3.91  | 4.17 | 4.24 | 4.31 | 4.42 |
|                        | 7.9 + | 29.0                       | 9.54              | 36.8                          | 702                       | 4.36     | 73.6                   | 3.88  | 4.14 | 4.21 | 4.28 | 4.39 |
|                        | 6.4 + | 23.4                       | 9.61              | 30.1                          | 577                       | 4.38     | 60.1                   | 3.85  | 4.11 | 4.17 | 4.24 | 4.35 |
| 125x75                 | 12    | 35.6                       | 8.19              | 45.4                          | 710                       | 3.95     | 86.8                   | 2.76  | 3.04 | 3.12 | 3.19 | 3.31 |
|                        | 10    | 30.0                       | 8.27              | 38.3                          | 606                       | 3.98     | 73.3                   | 2.72  | 3.00 | 3.07 | 3.15 | 3.26 |
|                        | 8     | 24.4                       | 8.36              | 31.0                          | 497                       | 4.00     | 59.5                   | 2.69  | 2.95 | 3.03 | 3.10 | 3.21 |
| 6.5 +                  | 20.0  | 8.43                       | 25.5              | 411                           | 4.02                      | 48.8     | 2.66                   | 2.92  | 2.99 | 3.06 | 3.17 |      |
| 100x75                 | 12    | 30.8                       | 6.73              | 39.4                          | 378                       | 3.10     | 56.2                   | 2.95  | 3.24 | 3.32 | 3.39 | 3.51 |
|                        | 10    | 26.0                       | 6.81              | 33.2                          | 324                       | 3.12     | 47.6                   | 2.92  | 3.20 | 3.27 | 3.35 | 3.46 |
|                        | 8     | 21.2                       | 6.90              | 27.0                          | 267                       | 3.14     | 38.7                   | 2.88  | 3.15 | 3.23 | 3.30 | 3.42 |
| 100x65                 | 10    | 24.6                       | 6.64              | 31.2                          | 309                       | 3.14     | 46.5                   | 2.44  | 2.72 | 2.80 | 2.88 | 2.99 |
|                        | 8     | 19.9                       | 6.72              | 25.4                          | 254                       | 3.17     | 37.8                   | 2.40  | 2.68 | 2.75 | 2.83 | 2.94 |
|                        | 7     | 17.5                       | 6.77              | 22.4                          | 225                       | 3.18     | 33.3                   | 2.38  | 2.65 | 2.73 | 2.80 | 2.92 |
| 80x60                  | 8     | 16.7                       | 5.45              | 21.2                          | 132                       | 2.49     | 24.1                   | 2.32  | 2.61 | 2.69 | 2.76 | 2.88 |
|                        | 7     | 14.7                       | 5.50              | 18.7                          | 117                       | 2.50     | 21.3                   | 2.30  | 2.59 | 2.66 | 2.74 | 2.86 |
|                        | 6     | 12.7                       | 5.54              | 16.2                          | 102                       | 2.51     | 18.4                   | 2.28  | 2.56 | 2.63 | 2.71 | 2.83 |
| 75x50                  | 8     | 14.8                       | 4.97              | 18.9                          | 105                       | 2.36     | 21.1                   | 1.91  | 2.20 | 2.27 | 2.35 | 2.48 |
|                        | 6     | 11.3                       | 5.06              | 14.4                          | 81.9                      | 2.38     | 16.2                   | 1.87  | 2.15 | 2.23 | 2.31 | 2.43 |
| 65x50                  | 8     | 13.5                       | 4.38              | 17.2                          | 69.8                      | 2.01     | 15.9                   | 1.99  | 2.28 | 2.36 | 2.44 | 2.57 |
|                        | 6     | 10.3                       | 4.46              | 13.2                          | 54.8                      | 2.04     | 12.3                   | 1.95  | 2.24 | 2.32 | 2.40 | 2.52 |
|                        | 5     | 8.70                       | 4.50              | 11.1                          | 46.7                      | 2.05     | 10.4                   | 1.94  | 2.22 | 2.29 | 2.37 | 2.49 |
| 60x30                  | 6     | 7.98                       | 3.80              | 10.2                          | 36.6                      | 1.90     | 9.64                   | 1.06  | 1.37 | 1.45 | 1.54 | 1.67 |
|                        | 5     | 6.74                       | 3.84              | 8.61                          | 31.3                      | 1.91     | 8.16                   | 1.04  | 1.34 | 1.42 | 1.51 | 1.64 |

+ Sections marked thus are not included in BS4848: Part 4

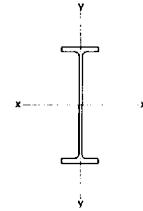
Properties about y-y axis:

$I_{yy} = (Total\ area) (r_{yy})^2$

$Z_{yy} = I_{yy} / (0.5B_0)$



**CASTELLATED UNIVERSAL BEAMS**

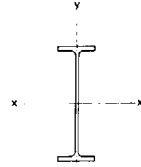


**DIMENSIONS AND PROPERTIES**

| Designation             |                            |                   | Depth Of Section<br>Dc mm | Width Of Section<br>B mm | Thickness |             | Depth Between Fillets<br>dc mm | Pitch 1.08 x Ds<br>mm | Net Second Moment Of Area |                          | Net Radius Of Gyration |             |
|-------------------------|----------------------------|-------------------|---------------------------|--------------------------|-----------|-------------|--------------------------------|-----------------------|---------------------------|--------------------------|------------------------|-------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg |                           |                          | Web t mm  | Flange T mm |                                |                       | Axis x-x cm <sup>4</sup>  | Axis y-y cm <sup>4</sup> | Axis x-x cm            | Axis y-y cm |
| 914x419                 | 1371x419                   | 388               | 1377.5                    | 420.5                    | 21.5      | 36.6        | 1256.1                         | 987.1                 | 1666000                   | 45400                    | 64.8                   | 10.7        |
|                         |                            | 343               | 1368.4                    | 418.5                    | 19.4      | 32.0        | 1256.2                         | 987.1                 | 1452000                   | 39130                    | 64.5                   | 10.6        |
| 914x305                 | 1371x305                   | 289               | 1383.6                    | 307.8                    | 19.6      | 32.0        | 1281.4                         | 987.1                 | 1164000                   | 15580                    | 64.5                   | 7.47        |
|                         |                            | 253               | 1375.5                    | 305.5                    | 17.3      | 27.9        | 1281.5                         | 987.1                 | 1009000                   | 13280                    | 64.3                   | 7.38        |
|                         |                            | 224               | 1367.3                    | 304.1                    | 15.9      | 23.9        | 1281.3                         | 987.1                 | 872600                    | 11220                    | 64.0                   | 7.26        |
|                         |                            | 201               | 1360.0                    | 303.4                    | 15.2      | 20.2        | 1281.4                         | 987.1                 | 757900                    | 9419                     | 63.0                   | 7.09        |
| 838x292                 | 1257x292                   | 226               | 1269.9                    | 293.8                    | 16.1      | 26.8        | 1180.7                         | 905.0                 | 780900                    | 11350                    | 59.4                   | 7.16        |
|                         |                            | 194               | 1259.7                    | 292.4                    | 14.7      | 21.7        | 1180.7                         | 905.0                 | 644500                    | 9055                     | 59.0                   | 6.99        |
|                         |                            | 176               | 1253.9                    | 291.6                    | 14.0      | 18.8        | 1180.7                         | 905.0                 | 569400                    | 7781                     | 58.7                   | 6.86        |
| 762x267                 | 1143x267                   | 197               | 1150.6                    | 268.0                    | 15.6      | 25.4        | 1066.8                         | 823.0                 | 553400                    | 8163                     | 53.8                   | 6.53        |
|                         |                            | 173               | 1143.0                    | 266.7                    | 14.3      | 21.6        | 1066.8                         | 823.0                 | 475000                    | 6840                     | 53.5                   | 6.42        |
|                         |                            | 147               | 1134.9                    | 265.3                    | 12.9      | 17.5        | 1066.9                         | 823.0                 | 392300                    | 5455                     | 53.2                   | 6.27        |
| 686x254                 | 1029x254                   | 170               | 1035.9                    | 255.8                    | 14.5      | 23.7        | 958.1                          | 740.9                 | 393100                    | 6622                     | 48.5                   | 6.30        |
|                         |                            | 152               | 1030.6                    | 254.5                    | 13.2      | 21.0        | 958.2                          | 740.9                 | 348000                    | 5777                     | 48.4                   | 6.23        |
|                         |                            | 140               | 1026.5                    | 253.7                    | 12.4      | 19.0        | 958.1                          | 740.9                 | 315900                    | 5178                     | 48.2                   | 6.17        |
|                         |                            | 125               | 1020.9                    | 253.0                    | 11.7      | 16.2        | 958.1                          | 740.9                 | 274400                    | 4378                     | 47.9                   | 6.06        |
| 610x305                 | 915x305                    | 238               | 938.0                     | 311.5                    | 18.6      | 31.4        | 842.2                          | 658.8                 | 475300                    | 15840                    | 43.8                   | 8.00        |
|                         |                            | 179               | 922.5                     | 307.0                    | 14.1      | 23.6        | 842.3                          | 658.8                 | 349300                    | 11390                    | 43.5                   | 7.85        |
|                         |                            | 149               | 914.6                     | 304.8                    | 11.9      | 19.7        | 842.2                          | 658.8                 | 288800                    | 9303                     | 43.3                   | 7.77        |
| 610x229                 | 915x229                    | 140               | 922.0                     | 230.1                    | 13.1      | 22.1        | 852.4                          | 658.8                 | 257600                    | 4494                     | 43.2                   | 5.70        |
|                         |                            | 125               | 916.9                     | 229.0                    | 11.9      | 19.6        | 852.3                          | 658.8                 | 227900                    | 3928                     | 43.0                   | 5.65        |
|                         |                            | 113               | 912.3                     | 228.2                    | 11.2      | 17.3        | 852.3                          | 658.8                 | 202700                    | 3431                     | 42.9                   | 5.58        |
|                         |                            | 101               | 907.2                     | 227.6                    | 10.6      | 14.8        | 852.2                          | 658.8                 | 176400                    | 2912                     | 42.6                   | 5.48        |
| 533x210                 | 800x210                    | 122               | 811.1                     | 211.9                    | 12.8      | 21.3        | 743.1                          | 575.6                 | 175100                    | 3383                     | 37.9                   | 5.27        |
|                         |                            | 109               | 806.0                     | 210.7                    | 11.6      | 18.8        | 743.0                          | 575.6                 | 154000                    | 2935                     | 37.8                   | 5.22        |
|                         |                            | 101               | 803.2                     | 210.1                    | 10.9      | 17.4        | 743.0                          | 575.6                 | 142400                    | 2693                     | 37.7                   | 5.19        |
|                         |                            | 92                | 799.6                     | 209.3                    | 10.2      | 15.6        | 743.0                          | 575.6                 | 128100                    | 2387                     | 37.6                   | 5.13        |
|                         |                            | 82                | 794.8                     | 208.7                    | 9.6       | 13.2        | 743.0                          | 575.6                 | 110400                    | 2002                     | 37.4                   | 5.03        |
| 457x191                 | 686x191                    | 98                | 695.9                     | 192.8                    | 11.4      | 19.6        | 636.3                          | 493.6                 | 105200                    | 2344                     | 32.6                   | 4.86        |
|                         |                            | 89                | 692.1                     | 192.0                    | 10.6      | 17.7        | 636.3                          | 493.6                 | 94840                     | 2091                     | 32.5                   | 4.82        |
|                         |                            | 82                | 688.7                     | 191.3                    | 9.9       | 16.0        | 636.3                          | 493.6                 | 85710                     | 1869                     | 32.4                   | 4.78        |
|                         |                            | 74                | 685.7                     | 190.5                    | 9.1       | 14.5        | 636.3                          | 493.6                 | 77420                     | 1672                     | 32.3                   | 4.74        |
|                         |                            | 67                | 682.1                     | 189.9                    | 8.5       | 12.7        | 636.3                          | 493.6                 | 68290                     | 1451                     | 32.1                   | 4.69        |
| 457x152                 | 686x152                    | 82                | 693.6                     | 153.5                    | 10.7      | 18.9        | 635.4                          | 493.6                 | 83640                     | 1142                     | 32.3                   | 3.77        |
|                         |                            | 74                | 689.8                     | 152.7                    | 9.9       | 17.0        | 635.4                          | 493.6                 | 75110                     | 1011                     | 32.2                   | 3.73        |
|                         |                            | 67                | 685.7                     | 151.9                    | 9.1       | 15.0        | 635.3                          | 493.6                 | 66340                     | 878                      | 32.1                   | 3.69        |
|                         |                            | 60                | 683.2                     | 152.9                    | 8.0       | 13.3        | 636.2                          | 493.6                 | 59090                     | 794                      | 32.0                   | 3.71        |
|                         |                            | 52                | 678.3                     | 152.4                    | 7.6       | 10.9        | 636.1                          | 493.6                 | 49820                     | 644                      | 31.8                   | 3.62        |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

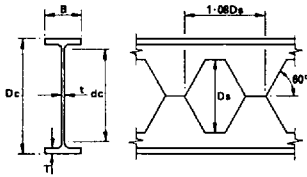
CASTELLATED UNIVERSAL BEAMS



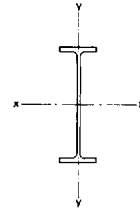
PROPERTIES (Continued)

| Designation             |                            |                   | Net Elastic Modulus      |                          | Elastic Modulus Of Tee     |                         | Net Plastic Modulus      |                          | Net Buckling Parameter | Net Torsional Index | Net Warping Constant | Net Torsional Constant | Net Area           |
|-------------------------|----------------------------|-------------------|--------------------------|--------------------------|----------------------------|-------------------------|--------------------------|--------------------------|------------------------|---------------------|----------------------|------------------------|--------------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Flange x-x cm <sup>3</sup> | Toe x-x cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | u                      | x                   | H dm <sup>6</sup>    | J cm <sup>4</sup>      | An cm <sup>2</sup> |
| 914x419                 | 1371x419                   | 388               | 24180                    | 2159                     | 1376                       | 314                     | 25610                    | 3289                     | 0.975                  | 37.9                | 204                  | 1587                   | 397                |
|                         |                            | 343               | 21230                    | 1870                     | 1251                       | 275                     | 22420                    | 2847                     | 0.974                  | 42.9                | 175                  | 1082                   | 349                |
| 914x305                 | 1371x305                   | 289               | 16820                    | 1013                     | 1079                       | 289                     | 17960                    | 1559                     | 0.972                  | 44.8                | 71.2                 | 816                    | 280                |
|                         |                            | 253               | 14670                    | 869                      | 964                        | 249                     | 15610                    | 1336                     | 0.972                  | 50.9                | 60.3                 | 547                    | 244                |
|                         |                            | 224               | 12760                    | 738                      | 863                        | 223                     | 13570                    | 1135                     | 0.971                  | 58.4                | 50.6                 | 361                    | 213                |
|                         |                            | 201               | 11150                    | 621                      | 773                        | 207                     | 11860                    | 957                      | 0.969                  | 67.0                | 42.3                 | 240                    | 187                |
| 838x292                 | 1257x292                   | 226               | 12300                    | 772                      | 811                        | 204                     | 13080                    | 1184                     | 0.972                  | 49.0                | 43.8                 | 455                    | 221                |
|                         |                            | 194               | 10230                    | 619                      | 704                        | 179                     | 10880                    | 951                      | 0.970                  | 59.0                | 34.7                 | 261                    | 185                |
|                         |                            | 176               | 9082                     | 534                      | 639                        | 166                     | 9655                     | 821                      | 0.969                  | 66.4                | 29.7                 | 183                    | 165                |
| 762x267                 | 1143x267                   | 197               | 9619                     | 609                      | 619                        | 159                     | 10240                    | 935                      | 0.972                  | 46.7                | 25.8                 | 356                    | 191                |
|                         |                            | 173               | 8312                     | 513                      | 553                        | 141                     | 8836                     | 788                      | 0.971                  | 53.9                | 21.5                 | 230                    | 166                |
|                         |                            | 147               | 6914                     | 411                      | 477                        | 123                     | 7344                     | 632                      | 0.970                  | 64.6                | 17.0                 | 133                    | 139                |
| 686x254                 | 1029x254                   | 170               | 7590                     | 518                      | 480                        | 120                     | 8070                     | 793                      | 0.973                  | 44.8                | 17.0                 | 273                    | 167                |
|                         |                            | 152               | 6753                     | 454                      | 438                        | 107                     | 7165                     | 695                      | 0.973                  | 50.1                | 14.7                 | 193                    | 149                |
|                         |                            | 140               | 6156                     | 408                      | 407                        | 98.6                    | 6524                     | 625                      | 0.972                  | 54.8                | 13.1                 | 147                    | 136                |
|                         |                            | 125               | 5375                     | 346                      | 367                        | 90.4                    | 5697                     | 531                      | 0.971                  | 62.8                | 11.0                 | 97.9                   | 119                |
| 610x305                 | 915x305                    | 238               | 10130                    | 1017                     | 548                        | 134                     | 10800                    | 1549                     | 0.973                  | 30.0                | 32.5                 | 724                    | 247                |
|                         |                            | 179               | 7573                     | 742                      | 437                        | 94.6                    | 8003                     | 1128                     | 0.974                  | 39.2                | 23.0                 | 311                    | 185                |
|                         |                            | 149               | 6316                     | 610                      | 380                        | 77.0                    | 6647                     | 927                      | 0.974                  | 46.4                | 18.6                 | 184                    | 154                |
| 610x229                 | 915x229                    | 140               | 5589                     | 391                      | 347                        | 86.1                    | 5941                     | 598                      | 0.973                  | 43.0                | 9.10                 | 193                    | 138                |
|                         |                            | 125               | 4971                     | 343                      | 317                        | 76.4                    | 5273                     | 525                      | 0.973                  | 48.1                | 7.91                 | 137                    | 123                |
|                         |                            | 113               | 4443                     | 301                      | 291                        | 70.2                    | 4709                     | 460                      | 0.972                  | 53.8                | 6.87                 | 97.8                   | 110                |
|                         |                            | 101               | 3890                     | 256                      | 263                        | 64.5                    | 4121                     | 392                      | 0.971                  | 61.5                | 5.80                 | 65.5                   | 97.1               |
| 533x210                 | 800x210                    | 122               | 4317                     | 319                      | 263                        | 66.4                    | 4598                     | 489                      | 0.973                  | 38.9                | 5.28                 | 161                    | 122                |
|                         |                            | 109               | 3821                     | 279                      | 239                        | 58.6                    | 4059                     | 426                      | 0.973                  | 43.7                | 4.55                 | 112                    | 108                |
|                         |                            | 101               | 3545                     | 256                      | 226                        | 54.2                    | 3760                     | 392                      | 0.973                  | 46.9                | 4.16                 | 90.2                   | 100                |
|                         |                            | 92                | 3203                     | 228                      | 209                        | 49.7                    | 3394                     | 349                      | 0.972                  | 51.7                | 3.67                 | 66.8                   | 90.7               |
|                         |                            | 82                | 2777                     | 192                      | 188                        | 45.4                    | 2941                     | 294                      | 0.971                  | 59.5                | 3.06                 | 43.6                   | 79.1               |
| 457x191                 | 686x191                    | 98                | 3024                     | 243                      | 177                        | 43.7                    | 3219                     | 371                      | 0.974                  | 36.4                | 2.68                 | 110                    | 99.2               |
|                         |                            | 89                | 2741                     | 218                      | 166                        | 39.6                    | 2910                     | 333                      | 0.974                  | 39.9                | 2.38                 | 82.2                   | 90.0               |
|                         |                            | 82                | 2489                     | 195                      | 154                        | 36.2                    | 2639                     | 298                      | 0.973                  | 43.8                | 2.11                 | 61.8                   | 81.9               |
|                         |                            | 74                | 2258                     | 176                      | 142                        | 32.7                    | 2389                     | 268                      | 0.973                  | 48.0                | 1.88                 | 46.5                   | 74.3               |
|                         |                            | 67                | 2002                     | 153                      | 130                        | 29.8                    | 2116                     | 233                      | 0.973                  | 54.1                | 1.63                 | 32.5                   | 66.1               |
| 457x152                 | 686x152                    | 82                | 2412                     | 149                      | 146                        | 39.6                    | 2578                     | 229                      | 0.973                  | 38.2                | 1.30                 | 80.2                   | 80.2               |
|                         |                            | 74                | 2178                     | 132                      | 135                        | 35.8                    | 2323                     | 204                      | 0.973                  | 42.1                | 1.14                 | 59.4                   | 72.5               |
|                         |                            | 67                | 1935                     | 116                      | 123                        | 32.0                    | 2060                     | 178                      | 0.972                  | 47.1                | 0.987                | 41.9                   | 64.5               |
|                         |                            | 60                | 1730                     | 104                      | 112                        | 27.9                    | 1836                     | 159                      | 0.973                  | 52.8                | 0.890                | 29.6                   | 57.5               |
|                         |                            | 52                | 1469                     | 84.5                     | 99.2                       | 25.5                    | 1560                     | 130                      | 0.971                  | 62.4                | 0.717                | 18.0                   | 49.3               |

The values of the elastic moduli of the Tee are the elastic modulus at the flange and toe of the Tee formed at the net section. FOR EXPLANATION OF TABLES SEE NOTE 3



**CASTELLATED UNIVERSAL BEAMS**

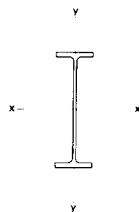


**DIMENSIONS AND PROPERTIES**

| Designation             |                            |                   | Depth Of Section<br>Dc mm | Width Of Section<br>B mm | Thickness   |                | Depth Between Fillets<br>dc mm | Pitch<br>1.08 x Ds<br>mm | Net Second Moment Of Area |                          | Net Radius Of Gyration |             |
|-------------------------|----------------------------|-------------------|---------------------------|--------------------------|-------------|----------------|--------------------------------|--------------------------|---------------------------|--------------------------|------------------------|-------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg |                           |                          | Web<br>t mm | Flange<br>T mm |                                |                          | Axis x-x cm <sup>4</sup>  | Axis y-y cm <sup>4</sup> | Axis x-x cm            | Axis y-y cm |
| 406x178                 | 609x178                    | 74                | 615.8                     | 179.7                    | 9.7         | 16.0           | 563.4                          | 438.5                    | 63150                     | 1549                     | 28.9                   | 4.53        |
|                         |                            | 67                | 612.4                     | 178.8                    | 8.8         | 14.3           | 563.4                          | 438.5                    | 56170                     | 1364                     | 28.8                   | 4.49        |
|                         |                            | 60                | 609.4                     | 177.8                    | 7.8         | 12.8           | 563.4                          | 438.5                    | 49840                     | 1200                     | 28.8                   | 4.46        |
|                         |                            | 54                | 605.6                     | 177.6                    | 7.6         | 10.9           | 563.4                          | 438.5                    | 43350                     | 1019                     | 28.6                   | 4.38        |
| 406x140                 | 609x140                    | 46                | 605.3                     | 142.4                    | 6.9         | 11.2           | 562.5                          | 438.5                    | 36440                     | 540                      | 28.5                   | 3.46        |
|                         |                            | 39                | 600.3                     | 141.8                    | 6.3         | 8.6            | 562.7                          | 438.5                    | 28990                     | 409                      | 28.2                   | 3.35        |
| 356x171                 | 534x171                    | 67                | 542.0                     | 173.2                    | 9.1         | 15.7           | 490.2                          | 384.5                    | 44920                     | 1361                     | 25.5                   | 4.43        |
|                         |                            | 57                | 536.6                     | 172.1                    | 8.0         | 13.0           | 490.2                          | 384.5                    | 37110                     | 1105                     | 25.3                   | 4.37        |
|                         |                            | 51                | 533.6                     | 171.5                    | 7.3         | 11.5           | 490.2                          | 384.5                    | 32810                     | 968                      | 25.2                   | 4.33        |
|                         |                            | 45                | 530.0                     | 171.0                    | 6.9         | 9.7            | 490.2                          | 384.5                    | 28090                     | 809                      | 25.1                   | 4.25        |
| 356x127                 | 534x127                    | 39                | 530.8                     | 126.0                    | 6.5         | 10.7           | 489.0                          | 384.5                    | 23520                     | 357                      | 24.9                   | 3.07        |
|                         |                            | 33                | 526.5                     | 125.4                    | 5.9         | 8.5            | 489.1                          | 384.5                    | 19160                     | 280                      | 24.8                   | 2.99        |
| 305x165                 | 458x165                    | 54                | 463.4                     | 166.8                    | 7.7         | 13.7           | 418.2                          | 329.4                    | 26930                     | 1060                     | 21.8                   | 4.33        |
|                         |                            | 46                | 459.6                     | 165.7                    | 6.7         | 11.8           | 418.2                          | 329.4                    | 22970                     | 895                      | 21.7                   | 4.29        |
|                         |                            | 40                | 456.3                     | 165.1                    | 6.1         | 10.2           | 418.1                          | 329.4                    | 19840                     | 765                      | 21.6                   | 4.25        |
| 305x127                 | 458x127                    | 48                | 462.9                     | 125.2                    | 8.9         | 14.0           | 417.1                          | 329.4                    | 21980                     | 459                      | 21.6                   | 3.12        |
|                         |                            | 42                | 459.1                     | 124.3                    | 8.0         | 12.1           | 417.1                          | 329.4                    | 18940                     | 388                      | 21.5                   | 3.07        |
|                         |                            | 37                | 456.3                     | 123.5                    | 7.2         | 10.7           | 417.1                          | 329.4                    | 16670                     | 337                      | 21.4                   | 3.04        |
| 305x102                 | 458x102                    | 33                | 465.2                     | 102.4                    | 6.6         | 10.8           | 428.4                          | 329.4                    | 14900                     | 194                      | 21.7                   | 2.47        |
|                         |                            | 28                | 461.4                     | 101.9                    | 6.1         | 8.9            | 428.4                          | 329.4                    | 12520                     | 157                      | 21.5                   | 2.41        |
|                         |                            | 25                | 457.3                     | 101.6                    | 5.8         | 6.8            | 428.5                          | 329.4                    | 10100                     | 119                      | 21.3                   | 2.31        |
| 254x146                 | 381x146                    | 43                | 386.6                     | 147.3                    | 7.3         | 12.7           | 346.0                          | 274.3                    | 15110                     | 677                      | 18.2                   | 3.85        |
|                         |                            | 37                | 383.0                     | 146.4                    | 6.4         | 10.9           | 346.0                          | 274.3                    | 12850                     | 570                      | 18.1                   | 3.81        |
|                         |                            | 31                | 378.5                     | 146.1                    | 6.1         | 8.6            | 346.1                          | 274.3                    | 10320                     | 447                      | 17.9                   | 3.73        |
| 254x102                 | 381x102                    | 28                | 387.4                     | 102.1                    | 6.4         | 10.0           | 352.2                          | 274.3                    | 9208                      | 178                      | 18.1                   | 2.51        |
|                         |                            | 25                | 384.0                     | 101.9                    | 6.1         | 8.4            | 352.0                          | 274.3                    | 7887                      | 148                      | 17.9                   | 2.46        |
|                         |                            | 22                | 381.0                     | 101.6                    | 5.8         | 6.8            | 352.2                          | 274.3                    | 6607                      | 119                      | 17.8                   | 2.39        |
| 203x133                 | 305x133                    | 30                | 308.3                     | 133.8                    | 6.3         | 9.6            | 273.9                          | 219.2                    | 6663                      | 384                      | 14.5                   | 3.48        |
|                         |                            | 25                | 304.7                     | 133.4                    | 5.8         | 7.8            | 273.9                          | 219.2                    | 5452                      | 309                      | 14.4                   | 3.43        |
| 203x102                 | 305x102                    | 23                | 304.7                     | 101.6                    | 5.2         | 9.3            | 270.9                          | 219.2                    | 4875                      | 163                      | 14.3                   | 2.62        |
| 178x102                 | 267x102                    | 19                | 266.8                     | 101.6                    | 4.7         | 7.9            | 235.8                          | 192.2                    | 3165                      | 138                      | 12.6                   | 2.63        |
| 152x89                  | 229x89                     | 16                | 228.4                     | 88.9                     | 4.6         | 7.7            | 197.8                          | 164.2                    | 1958                      | 90.3                     | 10.7                   | 2.31        |
| 127x76                  | 191x76                     | 13                | 190.5                     | 76.2                     | 4.2         | 7.6            | 160.1                          | 137.2                    | 1123                      | 56.2                     | 8.92                   | 2.00        |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

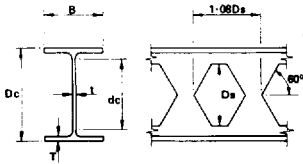
CASTELLATED UNIVERSAL BEAMS



PROPERTIES (Continued)

| Designation             |                            |                   | Net Elastic Modulus      |                          | Elastic Modulus Of Tee     |                         | Net Plastic Modulus      |                          | Net Buckling Parameter | Net Torsional Index | Net Warping Constant | Net Torsional Constant | Net Area                       |
|-------------------------|----------------------------|-------------------|--------------------------|--------------------------|----------------------------|-------------------------|--------------------------|--------------------------|------------------------|---------------------|----------------------|------------------------|--------------------------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Flange x-x cm <sup>3</sup> | Toe x-x cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | u                      | x                   | H dm <sup>6</sup>    | J cm <sup>4</sup>      | A <sub>n</sub> cm <sup>2</sup> |
| 406x178                 | 609x178                    | 74                | 2061                     | 172                      | 122                        | 28.9                    | 2177                     | 263                      | 0.974                  | 38.9                | 1.39                 | 57.5                   | 75.6                           |
|                         |                            | 67                | 1835                     | 153                      | 112                        | 25.6                    | 1942                     | 233                      | 0.974                  | 43.2                | 1.22                 | 41.5                   | 67.7                           |
|                         |                            | 60                | 1636                     | 135                      | 102                        | 22.3                    | 1727                     | 206                      | 0.974                  | 48.0                | 1.07                 | 29.8                   | 60.3                           |
|                         |                            | 54                | 1432                     | 115                      | 93.7                       | 21.0                    | 1511                     | 175                      | 0.972                  | 55.0                | 0.901                | 19.9                   | 53.1                           |
| 406x140                 | 609x140                    | 46                | 1204                     | 75.8                     | 78.5                       | 18.8                    | 1275                     | 116                      | 0.973                  | 54.7                | 0.476                | 17.0                   | 45.0                           |
|                         |                            | 39                | 966                      | 57.7                     | 66.1                       | 16.4                    | 1023                     | 88.7                     | 0.971                  | 68.0                | 0.358                | 8.83                   | 36.4                           |
| 356x171                 | 534x171                    | 67                | 1657                     | 157                      | 92.7                       | 21.4                    | 1759                     | 239                      | 0.974                  | 34.7                | 0.942                | 51.2                   | 69.3                           |
|                         |                            | 57                | 1383                     | 128                      | 81.6                       | 17.9                    | 1462                     | 196                      | 0.974                  | 41.2                | 0.758                | 30.1                   | 58.0                           |
|                         |                            | 51                | 1230                     | 113                      | 74.9                       | 16.0                    | 1297                     | 172                      | 0.974                  | 46.0                | 0.659                | 21.3                   | 51.6                           |
|                         |                            | 45                | 1060                     | 94.6                     | 67.9                       | 14.6                    | 1117                     | 144                      | 0.972                  | 53.2                | 0.548                | 13.7                   | 44.7                           |
| 356x127                 | 534x127                    | 39                | 886                      | 56.7                     | 55.9                       | 13.5                    | 939                      | 87.1                     | 0.974                  | 49.7                | 0.242                | 13.3                   | 37.8                           |
|                         |                            | 33                | 728                      | 44.6                     | 48.1                       | 11.8                    | 771                      | 68.6                     | 0.972                  | 60.1                | 0.188                | 7.43                   | 31.3                           |
| 305x165                 | 458x165                    | 54                | 1162                     | 127                      | 61.6                       | 13.3                    | 1229                     | 193                      | 0.974                  | 33.8                | 0.536                | 32.0                   | 56.5                           |
|                         |                            | 46                | 1000                     | 108                      | 55.0                       | 11.1                    | 1053                     | 164                      | 0.974                  | 38.8                | 0.449                | 20.7                   | 48.6                           |
|                         |                            | 40                | 870                      | 92.7                     | 50.1                       | 9.78                    | 914                      | 141                      | 0.974                  | 44.4                | 0.381                | 13.7                   | 42.3                           |
| 305x127                 | 458x127                    | 48                | 950                      | 73.3                     | 54.2                       | 14.6                    | 1015                     | 113                      | 0.973                  | 33.1                | 0.231                | 27.9                   | 47.3                           |
|                         |                            | 42                | 825                      | 62.4                     | 48.7                       | 12.7                    | 879                      | 96.0                     | 0.973                  | 37.7                | 0.194                | 18.5                   | 41.2                           |
|                         |                            | 37                | 731                      | 54.5                     | 44.2                       | 11.1                    | 776                      | 83.7                     | 0.973                  | 42.2                | 0.167                | 13.0                   | 36.5                           |
| 305x102                 | 458x102                    | 33                | 641                      | 37.8                     | 41.9                       | 11.3                    | 685                      | 58.4                     | 0.971                  | 44.2                | 0.100                | 10.7                   | 31.8                           |
|                         |                            | 28                | 543                      | 30.9                     | 36.8                       | 10.0                    | 580                      | 47.7                     | 0.969                  | 52.1                | 0.0805               | 6.53                   | 27.1                           |
|                         |                            | 25                | 442                      | 23.5                     | 31.0                       | 9.07                    | 473                      | 36.5                     | 0.966                  | 63.8                | 0.0605               | 3.57                   | 22.4                           |
| 254x146                 | 381x146                    | 43                | 782                      | 91.9                     | 39.2                       | 8.76                    | 829                      | 139                      | 0.973                  | 30.2                | 0.237                | 22.4                   | 45.7                           |
|                         |                            | 37                | 671                      | 77.9                     | 35.1                       | 7.35                    | 708                      | 118                      | 0.973                  | 34.9                | 0.197                | 14.3                   | 39.3                           |
|                         |                            | 31                | 545                      | 61.2                     | 31.5                       | 6.56                    | 574                      | 93.0                     | 0.972                  | 42.8                | 0.153                | 7.69                   | 32.2                           |
| 254x102                 | 381x102                    | 28                | 475                      | 34.8                     | 29.4                       | 7.62                    | 507                      | 53.5                     | 0.972                  | 38.7                | 0.0633               | 8.57                   | 28.2                           |
|                         |                            | 25                | 411                      | 29.1                     | 26.5                       | 6.94                    | 438                      | 44.9                     | 0.970                  | 44.6                | 0.0524               | 5.56                   | 24.5                           |
|                         |                            | 22                | 347                      | 23.5                     | 23.4                       | 6.32                    | 370                      | 36.3                     | 0.968                  | 52.4                | 0.0417               | 3.41                   | 20.9                           |
| 203x133                 | 305x133                    | 30                | 432                      | 57.3                     | 22.0                       | 4.79                    | 457                      | 87.0                     | 0.970                  | 31.1                | 0.0856               | 9.36                   | 31.6                           |
|                         |                            | 25                | 358                      | 46.3                     | 19.7                       | 4.14                    | 377                      | 70.4                     | 0.969                  | 37.1                | 0.0681               | 5.39                   | 26.3                           |
| 203x102                 | 305x102                    | 23                | 320                      | 32.0                     | 16.1                       | 3.66                    | 339                      | 48.8                     | 0.975                  | 32.2                | 0.0355               | 6.40                   | 23.7                           |
| 178x102                 | 267x102                    | 19                | 237                      | 27.2                     | 11.8                       | 2.55                    | 251                      | 41.4                     | 0.974                  | 32.5                | 0.0232               | 4.06                   | 20.0                           |
| 152x89                  | 229x89                     | 16                | 171                      | 20.3                     | 7.94                       | 1.83                    | 182                      | 30.9                     | 0.973                  | 28.1                | 0.0110               | 3.36                   | 17.0                           |
| 127x76                  | 191x76                     | 13                | 118                      | 14.7                     | 4.74                       | 1.17                    | 126                      | 22.5                     | 0.974                  | 23.4                | 0.00470              | 2.76                   | 14.1                           |

The values of the elastic moduli of the Tee are the elastic modulus at the flange and toe of the Tee formed at the net section. FOR EXPLANATION OF TABLES SEE NOTE 3



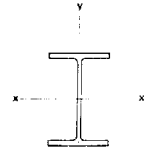
**CASTELLATED UNIVERSAL COLUMNS**

**DIMENSIONS AND PROPERTIES**

| Designation             |                            |                   | Depth Of Section<br>Dc mm | Width Of Section<br>B mm | Thickness   |                | Depth Between Fillets<br>dc mm | Pitch<br>1.08 x Ds<br>mm | Net Second Moment Of Area   |                             | Net Radius Of Gyration |                |
|-------------------------|----------------------------|-------------------|---------------------------|--------------------------|-------------|----------------|--------------------------------|--------------------------|-----------------------------|-----------------------------|------------------------|----------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg |                           |                          | Web<br>t mm | Flange<br>T mm |                                |                          | Axis x-x<br>cm <sup>4</sup> | Axis y-y<br>cm <sup>4</sup> | Axis x-x<br>cm         | Axis y-y<br>cm |
| 356x406                 | 546x406                    | 634               | 665.2                     | 424.1                    | 47.6        | 77.0           | 480.8                          | 411.5                    | 600500                      | 98020                       | 28.9                   | 11.7           |
|                         |                            | 551               | 646.2                     | 418.5                    | 42.0        | 67.5           | 480.8                          | 411.5                    | 503800                      | 82550                       | 28.5                   | 11.5           |
|                         |                            | 467               | 627.1                     | 412.4                    | 35.9        | 58.0           | 480.7                          | 411.5                    | 413300                      | 67960                       | 28.0                   | 11.3           |
|                         |                            | 393               | 609.6                     | 407.0                    | 30.6        | 49.2           | 480.8                          | 411.5                    | 336500                      | 55320                       | 27.6                   | 11.2           |
|                         |                            | 340               | 596.9                     | 403.0                    | 26.5        | 42.9           | 480.7                          | 411.5                    | 284400                      | 46820                       | 27.3                   | 11.1           |
|                         |                            | 287               | 584.2                     | 399.0                    | 22.6        | 36.5           | 480.8                          | 411.5                    | 234800                      | 38660                       | 27.0                   | 10.9           |
|                         |                            | 235               | 571.5                     | 395.0                    | 18.5        | 30.2           | 480.7                          | 411.5                    | 188300                      | 31030                       | 26.7                   | 10.8           |
|                         |                            | COLCORE           | 559x424                   | 477                      | 630.2       | 424.4          | 48.0                           | 53.2                     | 493.4                       | 438.9                       | 408900                 | 67900          |
| 356x368                 | 534x368                    | 202               | 552.7                     | 374.4                    | 16.8        | 27.0           | 468.3                          | 384.5                    | 152100                      | 23630                       | 25.8                   | 10.2           |
|                         |                            | 177               | 546.3                     | 372.1                    | 14.5        | 23.8           | 468.3                          | 384.5                    | 131700                      | 20440                       | 25.7                   | 10.1           |
|                         |                            | 153               | 540.0                     | 370.2                    | 12.6        | 20.7           | 468.2                          | 384.5                    | 112900                      | 17510                       | 25.5                   | 10.1           |
|                         |                            | 129               | 533.6                     | 368.3                    | 10.7        | 17.5           | 468.2                          | 384.5                    | 94100                       | 14570                       | 25.4                   | 9.99           |
| 305x305                 | 458x305                    | 283               | 517.8                     | 321.8                    | 26.9        | 44.1           | 399.2                          | 329.4                    | 172000                      | 24520                       | 23.2                   | 8.76           |
|                         |                            | 240               | 505.1                     | 317.9                    | 23.0        | 37.7           | 399.3                          | 329.4                    | 141900                      | 20200                       | 22.9                   | 8.64           |
|                         |                            | 198               | 492.4                     | 314.1                    | 19.2        | 31.4           | 399.2                          | 329.4                    | 114000                      | 16230                       | 22.6                   | 8.53           |
|                         |                            | 158               | 479.7                     | 310.6                    | 15.7        | 25.0           | 399.3                          | 329.4                    | 87910                       | 12490                       | 22.3                   | 8.40           |
|                         |                            | 137               | 473.0                     | 308.7                    | 13.8        | 21.7           | 399.2                          | 329.4                    | 75010                       | 10640                       | 22.1                   | 8.34           |
|                         |                            | 118               | 467.0                     | 306.8                    | 11.9        | 18.7           | 399.2                          | 329.4                    | 63620                       | 9004                        | 22.0                   | 8.27           |
|                         |                            | 97                | 460.3                     | 304.8                    | 9.9         | 15.4           | 399.1                          | 329.4                    | 51560                       | 7271                        | 21.8                   | 8.20           |
| 254x254                 | 381x254                    | 167               | 416.1                     | 264.5                    | 19.2        | 31.7           | 327.3                          | 274.3                    | 66900                       | 9785                        | 18.9                   | 7.21           |
|                         |                            | 132               | 403.4                     | 261.0                    | 15.6        | 25.3           | 327.4                          | 274.3                    | 51270                       | 7502                        | 18.6                   | 7.10           |
|                         |                            | 107               | 393.7                     | 258.3                    | 13.0        | 20.5           | 327.3                          | 274.3                    | 40310                       | 5891                        | 18.3                   | 7.00           |
|                         |                            | 89                | 387.4                     | 255.9                    | 10.5        | 17.3           | 327.4                          | 274.3                    | 33170                       | 4834                        | 18.2                   | 6.94           |
|                         |                            | 73                | 381.0                     | 254.0                    | 8.6         | 14.2           | 327.2                          | 274.3                    | 26660                       | 3880                        | 18.0                   | 6.88           |
| 203x203                 | 305x203                    | 86                | 323.8                     | 208.8                    | 13.0        | 20.5           | 262.4                          | 219.2                    | 21430                       | 3112                        | 14.9                   | 5.67           |
|                         |                            | 71                | 317.4                     | 206.2                    | 10.3        | 17.3           | 262.4                          | 219.2                    | 17480                       | 2529                        | 14.7                   | 5.61           |
|                         |                            | 60                | 311.1                     | 205.2                    | 9.3         | 14.2           | 262.3                          | 219.2                    | 14130                       | 2046                        | 14.6                   | 5.54           |
|                         |                            | 52                | 307.7                     | 203.9                    | 8.0         | 12.5           | 262.3                          | 219.2                    | 12230                       | 1767                        | 14.5                   | 5.51           |
| 46                      | 304.7                      | 203.2             | 7.3                       | 11.0                     | 262.3       | 219.2          | 10680                          | 1539                     | 14.4                        | 5.47                        |                        |                |
| 152x152                 | 228x152                    | 37                | 237.8                     | 154.4                    | 8.1         | 11.5           | 199.6                          | 164.2                    | 5038                        | 706                         | 11.1                   | 4.14           |
|                         |                            | 30                | 233.5                     | 152.9                    | 6.6         | 9.4            | 199.5                          | 164.2                    | 4018                        | 560                         | 11.0                   | 4.10           |
|                         |                            | 23                | 228.4                     | 152.4                    | 6.1         | 8.8            | 199.6                          | 164.2                    | 2926                        | 401                         | 10.8                   | 4.00           |

FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

CASTELLATED UNIVERSAL COLUMNS

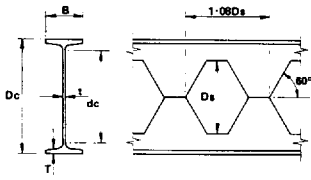


PROPERTIES (Continued)

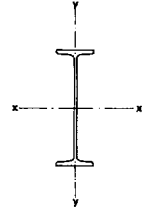
| Designation             |                            |                   | Net Elastic Modulus      |                          | Elastic Modulus Of Tee     |                         | Net Plastic Modulus      |                          | Net Buckling Parameter | Net Torsional Index | Net Warping Constant | Net Torsional Constant | Net Area                       |
|-------------------------|----------------------------|-------------------|--------------------------|--------------------------|----------------------------|-------------------------|--------------------------|--------------------------|------------------------|---------------------|----------------------|------------------------|--------------------------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Flange x-x cm <sup>3</sup> | Toe x-x cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | u                      | x                   | H dm <sup>5</sup>    | J cm <sup>4</sup>      | A <sub>n</sub> cm <sup>2</sup> |
| 356x406                 | 546x406                    | 634               | 18050                    | 4623                     | 707                        | 325                     | 20640                    | 7004                     | 0.946                  | 7.81                | 84.8                 | 13040                  | 717                            |
|                         |                            | 551               | 15580                    | 3945                     | 573                        | 245                     | 17620                    | 5973                     | 0.946                  | 8.72                | 69.1                 | 8762                   | 622                            |
|                         |                            | 467               | 13180                    | 3291                     | 453                        | 177                     | 14700                    | 4978                     | 0.947                  | 9.95                | 54.9                 | 5523                   | 527                            |
|                         |                            | 393               | 11040                    | 2719                     | 359                        | 127                     | 12160                    | 4109                     | 0.947                  | 11.5                | 43.4                 | 3363                   | 442                            |
|                         |                            | 340               | 9528                     | 2324                     | 297                        | 96.5                    | 10400                    | 3510                     | 0.947                  | 13.0                | 35.9                 | 2221                   | 382                            |
|                         |                            | 287               | 8037                     | 1938                     | 244                        | 71.4                    | 8683                     | 2925                     | 0.948                  | 15.1                | 29.0                 | 1367                   | 323                            |
|                         |                            | 235               | 6588                     | 1571                     | 196                        | 50.6                    | 7044                     | 2370                     | 0.948                  | 17.9                | 22.7                 | 773                    | 265                            |
| COLCORE                 | 559x424                    | 477               | 12980                    | 3200                     | 427                        | 178                     | 14390                    | 4864                     | 0.945                  | 10.5                | 56.5                 | 4956                   | 510                            |
| 356x368                 | 534x368                    | 202               | 5502                     | 1262                     | 198                        | 46.9                    | 5875                     | 1905                     | 0.949                  | 19.5                | 16.3                 | 533                    | 228                            |
|                         |                            | 177               | 4822                     | 1099                     | 175                        | 37.9                    | 5118                     | 1657                     | 0.949                  | 21.9                | 14.0                 | 364                    | 200                            |
|                         |                            | 153               | 4180                     | 946                      | 155                        | 30.8                    | 4412                     | 1426                     | 0.950                  | 24.9                | 11.8                 | 240                    | 173                            |
|                         |                            | 129               | 3527                     | 791                      | 136                        | 24.4                    | 3701                     | 1193                     | 0.950                  | 29.2                | 9.70                 | 147                    | 146                            |
| 305x305                 | 458x305                    | 283               | 6643                     | 1524                     | 256                        | 90.6                    | 7380                     | 2309                     | 0.951                  | 10.9                | 13.8                 | 1935                   | 319                            |
|                         |                            | 240               | 5617                     | 1271                     | 210                        | 67.6                    | 6170                     | 1924                     | 0.951                  | 12.5                | 11.0                 | 1208                   | 270                            |
|                         |                            | 198               | 4630                     | 1033                     | 170                        | 48.9                    | 5028                     | 1563                     | 0.951                  | 14.7                | 8.62                 | 699                    | 223                            |
|                         |                            | 158               | 3665                     | 804                      | 137                        | 34.3                    | 3932                     | 1216                     | 0.952                  | 18.1                | 6.46                 | 357                    | 177                            |
|                         |                            | 137               | 3172                     | 690                      | 120                        | 27.8                    | 3381                     | 1042                     | 0.952                  | 20.6                | 5.42                 | 235                    | 153                            |
|                         |                            | 118               | 2725                     | 587                      | 106                        | 22.3                    | 2886                     | 886                      | 0.952                  | 23.6                | 4.52                 | 152                    | 132                            |
|                         |                            | 97                | 2240                     | 477                      | 90.7                       | 17.1                    | 2357                     | 720                      | 0.953                  | 28.2                | 3.60                 | 86.2                   | 108                            |
| 254x254                 | 381x254                    | 167               | 3216                     | 740                      | 115                        | 37.8                    | 3535                     | 1120                     | 0.951                  | 12.2                | 3.61                 | 595                    | 188                            |
|                         |                            | 132               | 2542                     | 575                      | 88.9                       | 25.5                    | 2755                     | 869                      | 0.951                  | 15.0                | 2.68                 | 304                    | 149                            |
|                         |                            | 107               | 2048                     | 456                      | 72.2                       | 18.3                    | 2195                     | 689                      | 0.951                  | 18.1                | 2.05                 | 164                    | 120                            |
|                         |                            | 89                | 1712                     | 378                      | 60.1                       | 13.5                    | 1820                     | 570                      | 0.952                  | 21.2                | 1.66                 | 98.0                   | 100                            |
|                         |                            | 73                | 1399                     | 305                      | 50.4                       | 10.1                    | 1476                     | 461                      | 0.952                  | 25.4                | 1.30                 | 54.8                   | 82.0                           |
| 203x203                 | 305x203                    | 86                | 1324                     | 298                      | 47.4                       | 13.8                    | 1437                     | 451                      | 0.951                  | 14.8                | 0.716                | 130                    | 96.9                           |
|                         |                            | 71                | 1101                     | 245                      | 38.3                       | 9.84                    | 1183                     | 371                      | 0.952                  | 17.3                | 0.569                | 77.3                   | 80.5                           |
|                         |                            | 60                | 908                      | 199                      | 33.2                       | 7.76                    | 968                      | 301                      | 0.951                  | 20.6                | 0.451                | 44.2                   | 66.6                           |
|                         |                            | 52                | 795                      | 173                      | 29.3                       | 6.29                    | 842                      | 262                      | 0.952                  | 23.2                | 0.385                | 30.1                   | 58.2                           |
|                         |                            | 46                | 701                      | 151                      | 26.9                       | 5.40                    | 740                      | 229                      | 0.952                  | 26.1                | 0.332                | 20.9                   | 51.4                           |
| 152x152                 | 228x152                    | 37                | 424                      | 91.4                     | 16.9                       | 4.17                    | 454                      | 138                      | 0.951                  | 19.4                | 0.0904               | 17.9                   | 41.1                           |
|                         |                            | 30                | 344                      | 73.3                     | 14.1                       | 3.08                    | 365                      | 111                      | 0.952                  | 23.3                | 0.0703               | 9.87                   | 33.4                           |
|                         |                            | 23                | 256                      | 52.7                     | 12.3                       | 2.48                    | 270                      | 79.8                     | 0.951                  | 30.5                | 0.0493               | 4.24                   | 25.1                           |

The values of the elastic moduli of the Tee are the elastic modulus at the flange and toe of the Tee formed at the net section.  
FOR EXPLANATION OF TABLES SEE NOTE 3





**CASTELLATED JOISTS**

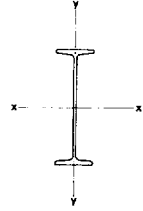


**DIMENSIONS AND PROPERTIES**

| Designation                |                               |                      | Depth Of Section<br>Dc<br>mm | Width Of Section<br>B<br>mm | Thickness      |                   | Depth Between Fillets<br>dc<br>mm | Pitch<br>1.06 x Ds<br>mm | Net Second Moment Of Area   |                             | Net Radius Of Gyration |                |
|----------------------------|-------------------------------|----------------------|------------------------------|-----------------------------|----------------|-------------------|-----------------------------------|--------------------------|-----------------------------|-----------------------------|------------------------|----------------|
| Original Serial Size<br>mm | Castellated Serial Size<br>mm | Mass Per Metre<br>kg |                              |                             | Web<br>t<br>mm | Flange<br>T<br>mm |                                   |                          | Axis x-x<br>cm <sup>4</sup> | Axis y-y<br>cm <sup>4</sup> | Axis x-x<br>cm         | Axis y-y<br>cm |
| 254x203                    | 381x203                       | 81.85                | 381.0                        | 203.2                       | 10.2           | 19.9              | 293.6                             | 274.3                    | 28700                       | 2279                        | 17.7                   | 4.99           |
| 254x114                    | 381x114                       | 37.20                | 381.0                        | 114.3                       | 7.6            | 12.8              | 326.3                             | 274.3                    | 11910                       | 269                         | 17.8                   | 2.67           |
| 203x152                    | 305x152                       | 52.09                | 304.7                        | 152.4                       | 8.9            | 16.5              | 234.7                             | 219.2                    | 11460                       | 815                         | 14.1                   | 3.76           |
| 152x127                    | 228x127                       | 37.20                | 228.4                        | 127.0                       | 10.4           | 13.2              | 170.3                             | 164.2                    | 4354                        | 378                         | 10.5                   | 3.09           |
| 127x114                    | 191x114                       | 29.76                | 190.5                        | 114.3                       | 10.2           | 11.5              | 143.0                             | 137.2                    | 2352                        | 241                         | 8.73                   | 2.80           |
|                            |                               | 26.79                | 190.5                        | 114.3                       | 7.4            | 11.4              | 143.0                             | 137.2                    | 2274                        | 236                         | 8.78                   | 2.83           |
| 127x76                     | 191x76                        | 16.37                | 190.5                        | 76.2                        | 5.6            | 9.6               | 150.0                             | 137.2                    | 1361                        | 60.8                        | 8.81                   | 1.86           |
| 114x114                    | 171x114                       | 26.79                | 171.3                        | 114.3                       | 9.5            | 10.7              | 117.8                             | 123.1                    | 1777                        | 224                         | 7.82                   | 2.77           |
| 102x102                    | 153x102                       | 23.07                | 152.6                        | 101.6                       | 9.5            | 10.3              | 106.2                             | 110.2                    | 1180                        | 154                         | 6.94                   | 2.51           |
| 102x44                     | 153x44                        | 7.44♦                | 152.6                        | 44.5                        | 4.3            | 6.1               | 125.6                             | 110.2                    | 382                         | 7.78                        | 7.04                   | 1.03           |
| 89x89                      | 134x89                        | 19.35                | 133.4                        | 88.9                        | 9.5            | 9.9               | 88.7                              | 96.1                     | 749                         | 101                         | 6.02                   | 2.21           |
| 76x76                      | 114x76                        | 14.67♦               | 114.2                        | 80.0                        | 8.9            | 8.4               | 76.1                              | 82.1                     | 419                         | 60.7                        | 5.16                   | 1.96           |
|                            |                               | 12.65                | 114.2                        | 76.2                        | 5.1            | 8.4               | 76.1                              | 82.1                     | 386                         | 51.7                        | 5.19                   | 1.90           |

♦ Check availability of section  
FOR EXPLANATION OF TABLES SEE NOTES 2 AND 3

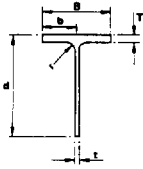
CASTELLATED JOISTS



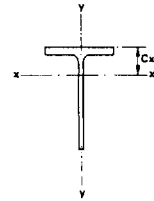
PROPERTIES (Continued)

| Designation             |                            |                   | Net Elastic Modulus      |                          | Elastic Modulus Of Tee     |                         | Net Plastic Modulus      |                          | Net Buckling Parameter u | Net Torsional Index x | Net Warping Constant H dm <sup>6</sup> | Net Torsional Constant J cm <sup>4</sup> | Net Area An cm <sup>2</sup> |
|-------------------------|----------------------------|-------------------|--------------------------|--------------------------|----------------------------|-------------------------|--------------------------|--------------------------|--------------------------|-----------------------|--|--|-----------------------------|
| Original Serial Size mm | Castellated Serial Size mm | Mass Per Metre kg | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | Flange x-x cm <sup>3</sup> | Toe x-x cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> |                          |                       |  |  |                             |
| 254x203                 | 381x203                    | 81.85             | 1506                     | 224                      | 47.6                       | 13.3                    | 1617                     | 367                      | 0.969                    | 16.1                  | 0.743                                  | 147                                      | 91.6                        |
| 254x114                 | 381x114                    | 37.20             | 625                      | 47.0                     | 30.9                       | 8.19                    | 668                      | 77.3                     | 0.975                    | 26.5                  | 0.0911                                 | 23.3                                     | 37.7                        |
| 203x152                 | 305x152                    | 52.09             | 752                      | 107                      | 24.4                       | 7.18                    | 810                      | 174                      | 0.970                    | 15.7                  | 0.169                                  | 62.4                                     | 57.5                        |
| 152x127                 | 228x127                    | 37.20             | 381                      | 59.5                     | 13.3                       | 4.50                    | 414                      | 97.7                     | 0.964                    | 13.8                  | 0.0437                                 | 31.0                                     | 39.6                        |
| 127x114                 | 191x114                    | 29.76             | 247                      | 42.2                     | 8.56                       | 3.00                    | 269                      | 69.2                     | 0.960                    | 13.1                  | 0.0193                                 | 18.5                                     | 30.9                        |
|                         |                            | 26.79             | 239                      | 41.2                     | 7.51                       | 2.41                    | 258                      | 67.3                     | 0.962                    | 13.8                  | 0.0189                                 | 16.0                                     | 29.5                        |
| 127x76                  | 191x76                     | 16.37             | 143                      | 15.9                     | 5.27                       | 1.60                    | 154                      | 25.9                     | 0.974                    | 17.0                  | 0.00497                                | 6.35                                     | 17.5                        |
| 114x114                 | 171x114                    | 26.79             | 207                      | 39.1                     | 7.07                       | 2.59                    | 226                      | 64.5                     | 0.953                    | 11.8                  | 0.0144                                 | 17.2                                     | 29.0                        |
| 102x102                 | 153x102                    | 23.07             | 155                      | 30.2                     | 5.09                       | 1.97                    | 169                      | 49.5                     | 0.953                    | 11.2                  | 0.00778                                | 12.7                                     | 24.5                        |
| 102x44                  | 153x44                     | 7.44              | 47.5                     | 3.50                     | 2.21                       | 0.711                   | 51.2                     | 5.79                     | 0.973                    | 21.2                  | 0.000418                               | 1.12                                     | 7.31                        |
| 89x89                   | 134x89                     | 19.35             | 112                      | 22.7                     | 3.79                       | 1.57                    | 124                      | 37.0                     | 0.951                    | 9.92                  | 0.00385                                | 10.2                                     | 20.6                        |
| 76x76                   | 114x76                     | 14.67             | 73.3                     | 15.2                     | 2.49                       | 1.06                    | 81.0                     | 25.0                     | 0.948                    | 9.76                  | 0.00170                                | 5.94                                     | 15.8                        |
|                         |                            | 12.65             | 67.5                     | 13.6                     | 2.04                       | 0.790                   | 74.1                     | 22.2                     | 0.954                    | 10.8                  | 0.00145                                | 4.43                                     | 14.3                        |

The values of the elastic moduli of the Tee are the elastic modulus at the flange and toe of the Tee formed at the net section.  
 FOR EXPLANATIONS OF TABLES SEE NOTE 3



**STRUCTURAL TEES  
CUT FROM UNIVERSAL BEAMS**

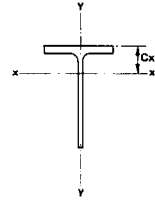


**DIMENSIONS**

| Designation       |                      | Cut From          |                      | Width Of Section<br>B<br>mm | Depth Of Section<br>d<br>mm | Thickness      |                   | Root Radius<br>r<br>mm | Ratios for Local Buckling |      | Dimension Cx<br>cm |
|-------------------|----------------------|-------------------|----------------------|-----------------------------|-----------------------------|----------------|-------------------|------------------------|---------------------------|------|--------------------|
| Serial Size<br>mm | Mass Per Metre<br>kg | Serial Size<br>mm | Mass Per Metre<br>kg |                             |                             | Web<br>t<br>mm | Flange<br>T<br>mm |                        | d/t                       | b/T  |                    |
| 419x457           | 194                  | 914x419           | 388                  | 420.5                       | 460.2                       | 21.5           | 36.6              | 24.1                   | 21.4                      | 5.74 | 10.3               |
|                   | 172                  |                   | 344                  | 418.5                       | 455.7                       | 19.4           | 32.0              | 24.1                   | 23.5                      | 6.54 | 10.2               |
| 305x457           | 145                  | 914x305           | 290                  | 307.8                       | 463.3                       | 19.6           | 32.0              | 19.1                   | 23.6                      | 4.81 | 12.2               |
|                   | 127                  |                   | 254                  | 305.5                       | 459.2                       | 17.3           | 27.9              | 19.1                   | 26.5                      | 5.47 | 12.0               |
|                   | 112                  |                   | 224                  | 304.1                       | 455.2                       | 15.9           | 23.9              | 19.1                   | 28.6                      | 6.36 | 12.1               |
|                   | 101                  |                   | 202                  | 303.4                       | 451.5                       | 15.2           | 20.2              | 19.1                   | 29.7                      | 7.51 | 12.6               |
| 292x419           | 113                  | 838x292           | 226                  | 293.8                       | 425.4                       | 16.1           | 26.8              | 17.8                   | 26.4                      | 5.48 | 10.8               |
|                   | 97                   |                   | 194                  | 292.4                       | 420.4                       | 14.7           | 21.7              | 17.8                   | 28.6                      | 6.74 | 11.1               |
|                   | 88                   |                   | 176                  | 291.6                       | 417.4                       | 14.0           | 18.8              | 17.8                   | 29.8                      | 7.76 | 11.4               |
| 267x381           | 99                   | 762x267           | 198                  | 268.0                       | 384.8                       | 15.6           | 25.4              | 16.5                   | 24.7                      | 5.28 | 9.9                |
|                   | 87                   |                   | 174                  | 266.7                       | 381.0                       | 14.3           | 21.6              | 16.5                   | 26.6                      | 6.17 | 10.0               |
|                   | 74                   |                   | 148                  | 265.3                       | 376.9                       | 12.9           | 17.5              | 16.5                   | 29.2                      | 7.58 | 10.2               |
| 254x343           | 85                   | 686x254           | 170                  | 255.8                       | 346.5                       | 14.5           | 23.7              | 15.2                   | 23.9                      | 5.40 | 8.7                |
|                   | 76                   |                   | 152                  | 254.5                       | 343.8                       | 13.2           | 21.0              | 15.2                   | 26.0                      | 6.06 | 8.6                |
|                   | 70                   |                   | 140                  | 253.7                       | 341.8                       | 12.4           | 19.0              | 15.2                   | 27.6                      | 6.68 | 8.6                |
|                   | 63                   |                   | 126                  | 253.0                       | 339.0                       | 11.7           | 16.2              | 15.2                   | 29.0                      | 7.81 | 8.9                |
| 305x305           | 119                  | 610x305           | 238                  | 311.5                       | 316.5                       | 18.6           | 31.4              | 16.5                   | 17.0                      | 4.96 | 7.1                |
|                   | 90                   |                   | 180                  | 307.0                       | 308.7                       | 14.1           | 23.6              | 16.5                   | 21.9                      | 6.50 | 6.6                |
|                   | 75                   |                   | 150                  | 304.8                       | 304.8                       | 11.9           | 19.7              | 16.5                   | 25.6                      | 7.74 | 6.4                |
| 229x305           | 70                   | 610x229           | 140                  | 230.1                       | 308.5                       | 13.1           | 22.1              | 12.7                   | 23.5                      | 5.21 | 7.6                |
|                   | 63                   |                   | 126                  | 229.0                       | 306.9                       | 11.9           | 19.6              | 12.7                   | 25.7                      | 5.84 | 7.5                |
|                   | 57                   |                   | 114                  | 228.2                       | 303.7                       | 11.2           | 17.3              | 12.7                   | 27.1                      | 6.60 | 7.6                |
|                   | 51                   |                   | 102                  | 227.6                       | 301.1                       | 10.6           | 14.8              | 12.7                   | 28.4                      | 7.69 | 7.8                |
| 210x267           | 61                   | 533x210           | 122                  | 211.9                       | 272.3                       | 12.8           | 21.3              | 12.7                   | 21.3                      | 4.97 | 6.7                |
|                   | 55                   |                   | 110                  | 210.7                       | 269.7                       | 11.6           | 18.8              | 12.7                   | 23.2                      | 5.60 | 6.6                |
|                   | 51                   |                   | 102                  | 210.1                       | 268.4                       | 10.9           | 17.4              | 12.7                   | 24.6                      | 6.04 | 6.6                |
|                   | 46                   |                   | 92                   | 209.3                       | 266.6                       | 10.2           | 15.6              | 12.7                   | 26.1                      | 6.71 | 6.6                |
|                   | 41                   |                   | 82                   | 208.7                       | 264.2                       | 9.6            | 13.2              | 12.7                   | 27.5                      | 7.91 | 6.8                |
| 191x229           | 49                   | 457x191           | 98                   | 192.8                       | 233.7                       | 11.4           | 19.6              | 10.2                   | 20.5                      | 4.92 | 5.5                |
|                   | 45                   |                   | 90                   | 192.0                       | 231.8                       | 10.6           | 17.7              | 10.2                   | 21.9                      | 5.42 | 5.5                |
|                   | 41                   |                   | 82                   | 191.3                       | 230.1                       | 9.9            | 16.0              | 10.2                   | 23.2                      | 5.98 | 5.5                |
|                   | 37                   |                   | 74                   | 190.5                       | 228.6                       | 9.1            | 14.5              | 10.2                   | 25.1                      | 6.67 | 5.4                |
|                   | 34                   |                   | 68                   | 189.9                       | 226.8                       | 8.5            | 12.7              | 10.2                   | 26.7                      | 7.48 | 5.5                |
| 152x229           | 41                   | 457x152           | 82                   | 153.5                       | 232.5                       | 10.7           | 18.9              | 10.2                   | 21.7                      | 4.06 | 6.0                |
|                   | 37                   |                   | 74                   | 152.7                       | 230.6                       | 9.9            | 17.0              | 10.2                   | 23.3                      | 4.49 | 6.0                |
|                   | 34                   |                   | 68                   | 151.9                       | 228.6                       | 9.1            | 15.0              | 10.2                   | 25.1                      | 5.06 | 6.0                |
|                   | 30                   |                   | 60                   | 152.9                       | 227.3                       | 8.0            | 13.3              | 10.2                   | 28.4                      | 5.75 | 5.8                |
|                   | 30                   |                   | 60                   | 152.9                       | 227.3                       | 8.0            | 13.3              | 10.2                   | 28.4                      | 5.75 | 5.8                |
|                   | 26                   |                   | 52                   | 152.4                       | 224.9                       | 7.6            | 10.9              | 10.2                   | 29.6                      | 6.99 | 6.0                |

FOR EXPLANATION OF TABLES SEE NOTE 2

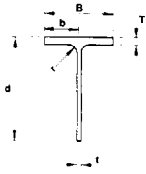
STRUCTURAL TEES  
CUT FROM UNIVERSAL BEAMS



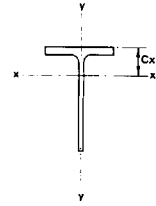
PROPERTIES

| Designation |                   | Second Moment Of Area    |                          | Radius Of Gyration |             | Elastic Modulus        |                     |                          | Plastic Modulus          |                          | Buckling Parameter | Torsional Index | Torsional Constant | Area              |
|-------------|-------------------|--------------------------|--------------------------|--------------------|-------------|------------------------|---------------------|--------------------------|--------------------------|--------------------------|--------------------|-----------------|--------------------|-------------------|
| Serial Size | Mess Per Metre kg | Axis x-x cm <sup>4</sup> | Axis y-y cm <sup>4</sup> | Axis x-x cm        | Axis y-y cm | Axis x-x               |                     | Axis y-y cm <sup>3</sup> | Axis x-x cm <sup>3</sup> | Axis y-y cm <sup>3</sup> | u                  | x               | J cm <sup>4</sup>  | A cm <sup>2</sup> |
|             |                   |                          |                          |                    |             | Flange cm <sup>3</sup> | Toe cm <sup>3</sup> |                          |                          |                          |                    |                 |                    |                   |
| 419x457     | 194               | 44180                    | 22720                    | 13.4               | 9.58        | 4280                   | 1238                | 1081                     | 2190                     | 1671                     | 0.528              | 13.4            | 867                | 247               |
|             | 172               | 38960                    | 19580                    | 13.3               | 9.46        | 3823                   | 1101                | 936                      | 1942                     | 1445                     | 0.534              | 15.1            | 595                | 219               |
| 305x457     | 145               | 37720                    | 7807                     | 14.3               | 6.50        | 3085                   | 1106                | 507                      | 1980                     | 802                      | 0.654              | 16.0            | 464                | 185               |
|             | 127               | 32720                    | 6651                     | 14.2               | 6.42        | 2721                   | 965                 | 435                      | 1728                     | 685                      | 0.655              | 18.1            | 312                | 161               |
|             | 112               | 29080                    | 5618                     | 14.3               | 6.27        | 2395                   | 871                 | 369                      | 1566                     | 582                      | 0.667              | 20.7            | 211                | 143               |
|             | 101               | 26490                    | 4716                     | 14.4               | 6.06        | 2110                   | 813                 | 311                      | 1474                     | 492                      | 0.687              | 23.4            | 146                | 128               |
| 292x419     | 113               | 24620                    | 5680                     | 13.1               | 6.27        | 2276                   | 776                 | 387                      | 1384                     | 606                      | 0.639              | 17.5            | 256                | 144               |
|             | 97                | 21350                    | 4533                     | 13.2               | 6.06        | 1926                   | 690                 | 310                      | 1238                     | 487                      | 0.659              | 20.9            | 152                | 123               |
|             | 88                | 19560                    | 3895                     | 13.2               | 5.90        | 1723                   | 644                 | 267                      | 1164                     | 421                      | 0.675              | 23.3            | 110                | 112               |
| 267x381     | 99                | 17510                    | 4087                     | 11.8               | 5.71        | 1770                   | 613                 | 305                      | 1093                     | 479                      | 0.641              | 16.6            | 202                | 125               |
|             | 87                | 15480                    | 3425                     | 11.9               | 5.58        | 1550                   | 550                 | 257                      | 986                      | 404                      | 0.653              | 18.1            | 133                | 110               |
|             | 74                | 13320                    | 2731                     | 11.9               | 5.39        | 1307                   | 484                 | 206                      | 874                      | 324                      | 0.671              | 22.6            | 79.9               | 94.0              |
| 254x343     | 85                | 12060                    | 3315                     | 10.5               | 5.53        | 1389                   | 464                 | 259                      | 826                      | 406                      | 0.623              | 15.9            | 153                | 108               |
|             | 76                | 10760                    | 2892                     | 10.5               | 5.46        | 1250                   | 418                 | 227                      | 743                      | 355                      | 0.627              | 17.8            | 110                | 97.0              |
|             | 70                | 9918                     | 2592                     | 10.5               | 5.39        | 1149                   | 388                 | 204                      | 692                      | 319                      | 0.633              | 19.4            | 84.1               | 89.2              |
|             | 63                | 8983                     | 2191                     | 10.6               | 5.24        | 1015                   | 359                 | 173                      | 643                      | 271                      | 0.651              | 22.0            | 57.9               | 79.7              |
| 305x305     | 119               | 12300                    | 7926                     | 8.99               | 7.22        | 1731                   | 501                 | 509                      | 895                      | 788                      | 0.483              | 10.6            | 394                | 152               |
|             | 90                | 8934                     | 5699                     | 8.86               | 7.08        | 1344                   | 389                 | 371                      | 651                      | 571                      | 0.482              | 13.8            | 169                | 114               |
|             | 75                | 7372                     | 4654                     | 8.80               | 6.99        | 1145                   | 307                 | 305                      | 538                      | 469                      | 0.483              | 16.3            | 100                | 95.1              |
| 229x305     | 70                | 7740                     | 2250                     | 9.32               | 5.03        | 1017                   | 333                 | 196                      | 592                      | 305                      | 0.613              | 15.3            | 108                | 89.1              |
|             | 63                | 6892                     | 1966                     | 9.30               | 4.97        | 915                    | 299                 | 172                      | 531                      | 268                      | 0.617              | 17.1            | 76.9               | 79.6              |
|             | 57                | 6306                     | 1717                     | 9.34               | 4.88        | 828                    | 277                 | 150                      | 493                      | 235                      | 0.628              | 19.0            | 55.9               | 72.2              |
|             | 51                | 5723                     | 1457                     | 9.40               | 4.75        | 733                    | 257                 | 128                      | 459                      | 200                      | 0.646              | 21.5            | 38.7               | 64.7              |
| 210x267     | 61                | 5196                     | 1694                     | 8.16               | 4.66        | 777                    | 253                 | 160                      | 450                      | 250                      | 0.602              | 13.8            | 89.4               | 78.0              |
|             | 55                | 4603                     | 1469                     | 8.14               | 4.60        | 697                    | 226                 | 139                      | 401                      | 218                      | 0.606              | 15.5            | 63.0               | 69.4              |
|             | 51                | 4278                     | 1348                     | 8.14               | 4.57        | 652                    | 211                 | 128                      | 374                      | 200                      | 0.608              | 16.6            | 50.7               | 64.6              |
|             | 46                | 3916                     | 1195                     | 8.15               | 4.50        | 595                    | 195                 | 114                      | 346                      | 178                      | 0.615              | 18.2            | 38.0               | 58.9              |
|             | 41                | 3531                     | 1002                     | 8.21               | 4.38        | 523                    | 180                 | 96.0                     | 321                      | 150                      | 0.634              | 20.8            | 25.7               | 52.3              |
| 191x229     | 49                | 2974                     | 1174                     | 6.89               | 4.33        | 537                    | 167                 | 122                      | 296                      | 189                      | 0.573              | 12.9            | 60.5               | 62.6              |
|             | 45                | 2709                     | 1046                     | 6.89               | 4.28        | 493                    | 153                 | 108                      | 272                      | 169                      | 0.578              | 14.1            | 45.5               | 57.1              |
|             | 41                | 2480                     | 935                      | 6.89               | 4.23        | 453                    | 141                 | 97.8                     | 250                      | 152                      | 0.584              | 15.5            | 34.5               | 52.3              |
|             | 37                | 2248                     | 837                      | 6.88               | 4.20        | 415                    | 129                 | 87.9                     | 228                      | 136                      | 0.586              | 16.9            | 26.0               | 47.6              |
|             | 34                | 2039                     | 726                      | 6.91               | 4.12        | 373                    | 118                 | 76.5                     | 210                      | 119                      | 0.598              | 19.0            | 18.5               | 42.8              |
| 152x229     | 41                | 2612                     | 572                      | 7.07               | 3.31        | 433                    | 152                 | 74.5                     | 271                      | 118                      | 0.641              | 13.7            | 44.6               | 52.3              |
|             | 37                | 2367                     | 506                      | 7.06               | 3.26        | 395                    | 139                 | 66.3                     | 248                      | 105                      | 0.645              | 15.0            | 33.3               | 47.6              |
|             | 34                | 2122                     | 440                      | 7.05               | 3.21        | 366                    | 126                 | 57.9                     | 225                      | 91.3                     | 0.651              | 16.8            | 23.7               | 42.7              |
|             | 30                | 1865                     | 397                      | 7.01               | 3.24        | 321                    | 110                 | 52.0                     | 197                      | 81.4                     | 0.646              | 18.8            | 16.7               | 37.9              |
|             | 26                | 1672                     | 322                      | 7.08               | 3.11        | 277                    | 102                 | 42.3                     | 183                      | 66.7                     | 0.671              | 22.0            | 10.7               | 33.3              |

Properties have been calculated assuming that there is no loss of material due to splitting.  
 - Indicates that no values of u and x are given as there is no possibility of lateral torsional buckling due to bending about the x-x axis because the second moment of area about y-y axis exceeds the second moment of area about x-x axis.  
 The value of H is virtually zero and has not therefore been given.  
 FOR EXPLANATION OF TABLES SEE NOTE 3



**STRUCTURAL TEES  
CUT FROM UNIVERSAL BEAMS**

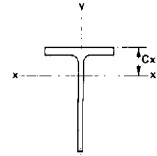


**DIMENSIONS**

| Designation       |                      | Cut From          |                      | Width Of Section<br>B<br>mm | Depth Of Section<br>d<br>mm | Thickness      |                   | Root Radius<br>r<br>mm | Ratios for Local Buckling |      | Dimension<br>Cx<br>cm |
|-------------------|----------------------|-------------------|----------------------|-----------------------------|-----------------------------|----------------|-------------------|------------------------|---------------------------|------|-----------------------|
| Serial Size<br>mm | Mass Per Metre<br>kg | Serial Size<br>mm | Mass Per Metre<br>kg |                             |                             | Web<br>t<br>mm | Flange<br>T<br>mm |                        | d/t                       | b/T  |                       |
| 178x203           | 37                   | 406x178           | 74                   | 179.7                       | 206.4                       | 9.7            | 16.0              | 10.2                   | 21.3                      | 5.62 | 4.8                   |
|                   | 34                   |                   | 68                   | 178.8                       | 204.7                       | 8.8            | 14.3              | 10.2                   | 23.3                      | 6.25 | 4.7                   |
|                   | 30                   |                   | 60                   | 177.8                       | 203.2                       | 7.8            | 12.8              | 10.2                   | 26.1                      | 6.95 | 4.6                   |
|                   | 27                   |                   | 54                   | 177.6                       | 201.3                       | 7.6            | 10.9              | 10.2                   | 26.5                      | 8.15 | 4.8                   |
| 140x203           | 23                   | 406x140           | 46                   | 142.4                       | 201.2                       | 6.9            | 11.2              | 10.2                   | 29.2                      | 6.36 | 5.0                   |
|                   | 20                   |                   | 40                   | 141.8                       | 198.6                       | 6.3            | 8.6               | 10.2                   | 31.5                      | 8.24 | 5.3                   |
| 171x178           | 34                   | 356x171           | 68                   | 173.2                       | 182.0                       | 9.1            | 15.7              | 10.2                   | 20.0                      | 5.52 | 4.0                   |
|                   | 29                   |                   | 58                   | 172.1                       | 179.3                       | 8.0            | 13.0              | 10.2                   | 22.4                      | 6.62 | 4.0                   |
|                   | 26                   |                   | 52                   | 171.5                       | 177.8                       | 7.3            | 11.5              | 10.2                   | 24.4                      | 7.46 | 3.9                   |
|                   | 23                   |                   | 46                   | 171.0                       | 176.0                       | 6.9            | 9.7               | 10.2                   | 25.5                      | 8.81 | 4.0                   |
| 127x178           | 20                   | 356x127           | 40                   | 126.0                       | 176.4                       | 6.5            | 10.7              | 10.2                   | 27.1                      | 5.89 | 4.4                   |
|                   | 17                   |                   | 34                   | 125.4                       | 174.2                       | 5.9            | 8.5               | 10.2                   | 29.5                      | 7.38 | 4.5                   |
| 165x152           | 27                   | 305x165           | 54                   | 166.8                       | 155.4                       | 7.7            | 13.7              | 8.9                    | 20.2                      | 6.09 | 3.2                   |
|                   | 23                   |                   | 46                   | 165.7                       | 153.5                       | 6.7            | 11.8              | 8.9                    | 22.9                      | 7.02 | 3.1                   |
|                   | 20                   |                   | 40                   | 165.1                       | 151.9                       | 6.1            | 10.2              | 8.9                    | 24.9                      | 8.09 | 3.1                   |
| 127x152           | 24                   | 305x127           | 48                   | 125.2                       | 155.2                       | 8.9            | 14.0              | 8.9                    | 17.4                      | 4.47 | 3.9                   |
|                   | 21                   |                   | 42                   | 124.3                       | 153.3                       | 8.0            | 12.1              | 8.9                    | 19.2                      | 5.14 | 3.9                   |
|                   | 19                   |                   | 38                   | 123.5                       | 151.9                       | 7.2            | 10.7              | 8.9                    | 21.1                      | 5.77 | 3.8                   |
| 102x153           | 17                   | 305x102           | 34                   | 102.4                       | 156.3                       | 6.6            | 10.8              | 7.6                    | 23.7                      | 4.74 | 4.1                   |
|                   | 14                   |                   | 28                   | 101.9                       | 154.4                       | 6.1            | 8.9               | 7.6                    | 25.3                      | 5.72 | 4.2                   |
|                   | 13                   |                   | 26                   | 101.6                       | 152.4                       | 5.8            | 6.8               | 7.6                    | 26.3                      | 7.47 | 4.5                   |
| 146x127           | 22                   | 254x146           | 44                   | 147.3                       | 129.8                       | 7.3            | 12.7              | 7.6                    | 17.8                      | 5.80 | 2.7                   |
|                   | 19                   |                   | 38                   | 146.4                       | 128.0                       | 6.4            | 10.9              | 7.6                    | 20.0                      | 6.72 | 2.6                   |
|                   | 16                   |                   | 32                   | 146.1                       | 125.7                       | 6.1            | 8.6               | 7.6                    | 20.6                      | 8.48 | 2.7                   |
| 102x127           | 14                   | 254x102           | 28                   | 102.1                       | 130.2                       | 6.4            | 10.0              | 7.6                    | 20.3                      | 5.11 | 3.3                   |
|                   | 13                   |                   | 26                   | 101.9                       | 128.5                       | 6.1            | 8.4               | 7.6                    | 21.1                      | 6.07 | 3.3                   |
|                   | 11                   |                   | 22                   | 101.6                       | 127.0                       | 5.8            | 6.8               | 7.6                    | 21.9                      | 7.47 | 3.5                   |
| 133x102           | 15                   | 203x133           | 30                   | 133.8                       | 103.4                       | 6.3            | 9.6               | 7.6                    | 16.4                      | 6.97 | 2.1                   |
|                   | 13                   |                   | 26                   | 133.4                       | 101.6                       | 5.8            | 7.8               | 7.6                    | 17.5                      | 8.55 | 2.1                   |
| 102x102           | 12                   | 203x102           | 24                   | 101.6                       | 101.6                       | 5.2            | 9.3               | 7.6                    | 19.5                      | 5.46 | 2.2                   |
| 102x89            | 10                   | 178x102           | 20                   | 101.6                       | 88.9                        | 4.7            | 7.9               | 7.6                    | 18.9                      | 6.43 | 1.8                   |
| 89x76             | 8                    | 152x89            | 16                   | 88.9                        | 76.2                        | 4.6            | 7.7               | 7.6                    | 16.6                      | 5.77 | 1.6                   |
| 76x64             | 7                    | 127x76            | 14                   | 76.2                        | 63.5                        | 4.2            | 7.6               | 7.6                    | 15.1                      | 5.01 | 1.3                   |

FOR EXPLANATION OF TABLES SEE NOTE 2

STRUCTURAL TEES  
CUT FROM UNIVERSAL BEAMS

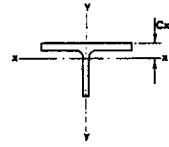
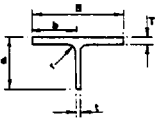


PROPERTIES

| Designation |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 |                 | Plastic Modulus |                 | Buckling Parameter | Torsional Index | Torsional Constant | Area            |
|-------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|--------------------|-----------------|
| Serial Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        |                 | Axis            | Axis x-x        | Axis y-y        | u                  | x               | J                  | A               |
|             |                |                       |                 |                    |          | Flange          | Toe             | Y-Y             |                 |                 |                    |                 |                    |                 |
| mm          | kg             | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> |                    |                 | cm <sup>4</sup>    | cm <sup>2</sup> |
| 178x203     | 37             | 1766                  | 775             | 6.09               | 4.03     | 367             | 112             | 86.3            | 198             | 134             | 0.569              | 13.8            | 31.7               | 47.7            |
|             | 34             | 1575                  | 682             | 6.07               | 3.99     | 333             | 100             | 76.3            | 177             | 118             | 0.561              | 15.2            | 23.0               | 42.8            |
|             | 30             | 1384                  | 600             | 6.03               | 3.97     | 300             | 88.1            | 67.5            | 155             | 104             | 0.559              | 16.9            | 16.5               | 38.1            |
|             | 27             | 1283                  | 510             | 6.12               | 3.86     | 267             | 83.7            | 57.4            | 148             | 89.0            | 0.585              | 19.2            | 11.4               | 34.3            |
| 140x203     | 23             | 1130                  | 270             | 6.19               | 3.03     | 224             | 75.0            | 37.9            | 133             | 59.3            | 0.635              | 19.4            | 9.60               | 29.5            |
|             | 20             | 964                   | 205             | 6.26               | 2.89     | 183             | 66.1            | 28.9            | 119             | 45.4            | 0.665              | 23.8            | 5.24               | 24.6            |
| 171x178     | 34             | 1162                  | 681             | 5.21               | 3.99     | 289             | 81.9            | 78.6            | 145             | 121             | 0.501              | 12.2            | 27.8               | 42.8            |
|             | 29             | 983                   | 553             | 5.22               | 3.91     | 248             | 70.4            | 64.3            | 124             | 99.2            | 0.513              | 14.5            | 16.5               | 36.1            |
|             | 26             | 879                   | 484             | 5.22               | 3.87     | 224             | 63.4            | 56.5            | 112             | 87.0            | 0.519              | 16.1            | 11.8               | 32.3            |
|             | 23             | 795                   | 405             | 5.28               | 3.77     | 197             | 58.6            | 47.3            | 103             | 73.1            | 0.544              | 18.5            | 7.81               | 28.5            |
| 127x178     | 20             | 718                   | 179             | 5.39               | 2.69     | 163             | 54.2            | 28.4            | 96.5            | 44.5            | 0.629              | 17.6            | 7.44               | 24.7            |
|             | 17             | 617                   | 140             | 5.43               | 2.59     | 137             | 47.8            | 22.3            | 85.6            | 35.1            | 0.651              | 21.2            | 4.31               | 20.9            |
| 165x152     | 27             | 633                   | 530             | 4.31               | 3.94     | 199             | 51.2            | 63.6            | 91.0            | 97.6            | 0.380              | 11.9            | 17.1               | 34.1            |
|             | 23             | 539                   | 448             | 4.28               | 3.90     | 175             | 43.9            | 54.1            | 77.4            | 82.8            | 0.383              | 13.6            | 11.1               | 29.4            |
|             | 20             | 477                   | 383             | 4.30               | 3.85     | 156             | 39.3            | 46.4            | 69.0            | 71.0            | 0.402              | 15.5            | 7.42               | 25.8            |
| 127x152     | 24             | 654                   | 230             | 4.64               | 2.75     | 167             | 56.4            | 36.7            | 101             | 57.9            | 0.599              | 11.7            | 15.7               | 30.4            |
|             | 21             | 571                   | 194             | 4.62               | 2.70     | 148             | 49.8            | 31.3            | 88.7            | 49.2            | 0.606              | 13.3            | 10.5               | 26.7            |
|             | 19             | 504                   | 169             | 4.61               | 2.67     | 133             | 44.2            | 27.3            | 78.8            | 42.8            | 0.608              | 14.8            | 7.44               | 23.7            |
| 102x153     | 17             | 487                   | 97.1            | 4.82               | 2.15     | 118             | 42.3            | 19.0            | 75.8            | 30.0            | 0.656              | 15.8            | 6.08               | 20.9            |
|             | 14             | 427                   | 78.8            | 4.84               | 2.08     | 101             | 38.1            | 15.5            | 68.6            | 24.6            | 0.674              | 18.5            | 3.83               | 18.2            |
|             | 13             | 373                   | 59.7            | 4.89               | 1.96     | 83.5            | 34.7            | 11.8            | 63.1            | 18.9            | 0.705              | 22.1            | 2.27               | 15.6            |
| 146x127     | 22             | 348                   | 339             | 3.56               | 3.51     | 131             | 33.7            | 46.0            | 60.3            | 70.6            | 0.239              | 10.6            | 12.0               | 27.5            |
|             | 19             | 297                   | 285             | 3.54               | 3.47     | 115             | 29.0            | 39.0            | 51.5            | 59.7            | 0.262              | 12.2            | 7.71               | 23.7            |
|             | 16             | 263                   | 224             | 3.63               | 3.35     | 97.9            | 26.6            | 30.6            | 46.8            | 47.1            | 0.386              | 14.8            | 4.31               | 20.0            |
| 102x127     | 14             | 281                   | 99.0            | 3.93               | 2.21     | 85.8            | 28.8            | 17.4            | 51.3            | 27.4            | 0.610              | 13.7            | 4.82               | 18.2            |
|             | 13             | 253                   | 74.4            | 3.96               | 2.15     | 75.6            | 26.6            | 14.6            | 47.6            | 23.0            | 0.632              | 15.7            | 3.25               | 16.1            |
|             | 11             | 226                   | 59.7            | 4.00               | 2.06     | 64.9            | 24.5            | 11.7            | 44.3            | 18.7            | 0.660              | 18.1            | 2.11               | 14.1            |
| 133x102     | 15             | 153                   | 192             | 2.84               | 3.18     | 72.9            | 18.5            | 28.7            | 33.1            | 44.0            | -                  | -               | 5.09               | 19.0            |
|             | 13             | 133                   | 155             | 2.87               | 3.10     | 62.8            | 16.5            | 23.2            | 29.2            | 35.6            | -                  | -               | 3.01               | 16.1            |
| 102x102     | 12             | 117                   | 81.4            | 2.84               | 2.37     | 54.3            | 14.6            | 16.0            | 26.1            | 24.7            | 0.453              | 11.3            | 3.43               | 14.5            |
| 102x89      | 10             | 72.4                  | 69.2            | 2.45               | 2.39     | 40.1            | 10.2            | 13.6            | 18.2            | 20.9            | 0.275              | 11.3            | 2.18               | 12.1            |
| 89x76       | 8              | 44.1                  | 45.2            | 2.07               | 2.10     | 28.1            | 7.29            | 10.2            | 13.1            | 15.7            | -                  | -               | 1.80               | 10.2            |
| 76x64       | 7              | 23.3                  | 28.1            | 1.67               | 1.83     | 18.1            | 4.59            | 7.37            | 8.47            | 11.4            | -                  | -               | 1.45               | 8.39            |

Properties have been calculated assuming that there is no loss of material due to splitting.  
 - Indicates that no values of u and x are given as there is no possibility of lateral torsional buckling due to bending about the x-x axis because the second moment of area about y-y axis exceeds the second moment of area about x-x axis.  
 The value of H is virtually zero and has not therefore been given.  
 FOR EXPLANATION OF TABLES SEE NOTE 3

**STRUCTURAL TEES  
CUT FROM UNIVERSAL COLUMNS**

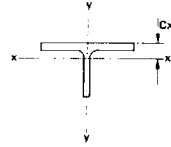


**DIMENSIONS**

| Designation          |                            | Cut From             |                            | Width<br>Of<br>Section<br>B<br>mm | Depth<br>Of<br>Section<br>d<br>mm | Thickness      |                   | Root<br>Radius<br>r<br>mm | Ratios for<br>Local Buckling |      | Dimension<br>Cx<br>cm |
|----------------------|----------------------------|----------------------|----------------------------|-----------------------------------|-----------------------------------|----------------|-------------------|---------------------------|------------------------------|------|-----------------------|
| Serial<br>Size<br>mm | Mass<br>Per<br>Metre<br>kg | Serial<br>Size<br>mm | Mass<br>Per<br>Metre<br>kg |                                   |                                   | Web<br>t<br>mm | Flange<br>T<br>mm |                           | d/t                          | b/T  |                       |
| 406x178              | 317                        | 356x406              | 634                        | 424.1                             | 237.4                             | 47.6           | 77.0              | 15.2                      | 4.99                         | 2.75 | 6.1                   |
|                      | 276                        |                      | 552                        | 418.5                             | 227.8                             | 42.0           | 67.5              | 15.2                      | 5.42                         | 3.10 | 5.6                   |
|                      | 234                        |                      | 468                        | 412.4                             | 218.3                             | 35.9           | 58.0              | 15.2                      | 6.08                         | 3.56 | 5.0                   |
|                      | 197                        |                      | 394                        | 407.0                             | 209.6                             | 30.6           | 49.2              | 15.2                      | 6.85                         | 4.14 | 4.5                   |
|                      | 170                        |                      | 340                        | 403.0                             | 203.2                             | 26.5           | 42.9              | 15.2                      | 7.67                         | 4.70 | 4.2                   |
|                      | 144                        |                      | 288                        | 399.0                             | 196.9                             | 22.6           | 36.5              | 15.2                      | 8.71                         | 5.47 | 3.8                   |
|                      | 118                        |                      | 236                        | 395.0                             | 190.5                             | 18.5           | 30.2              | 15.2                      | 10.3                         | 6.54 | 3.4                   |
| 406x178              | 239                        | COLCORE              | 478                        | 424.4                             | 213.5                             | 48.0           | 53.2              | 15.2                      | 4.45                         | 3.99 | 5.4                   |
| 368x178              | 101                        | 356x368              | 202                        | 374.4                             | 187.3                             | 16.8           | 27.0              | 15.2                      | 11.1                         | 6.93 | 3.3                   |
|                      | 89                         |                      | 178                        | 372.1                             | 184.2                             | 14.5           | 23.8              | 15.2                      | 12.7                         | 7.82 | 3.1                   |
|                      | 77                         |                      | 154                        | 370.2                             | 181.0                             | 12.6           | 20.7              | 15.2                      | 14.4                         | 8.94 | 2.9                   |
|                      | 65                         |                      | 130                        | 368.3                             | 177.8                             | 10.7           | 17.5              | 15.2                      | 16.6                         | 10.5 | 2.7                   |
| 305x152              | 142                        | 305x305              | 294                        | 321.8                             | 182.6                             | 26.9           | 44.1              | 15.2                      | 6.79                         | 3.65 | 4.1                   |
|                      | 120                        |                      | 240                        | 317.9                             | 176.3                             | 23.0           | 37.7              | 15.2                      | 7.67                         | 4.22 | 3.7                   |
|                      | 99                         |                      | 196                        | 314.1                             | 169.9                             | 19.2           | 31.4              | 15.2                      | 8.85                         | 5.00 | 3.4                   |
|                      | 79                         |                      | 158                        | 310.6                             | 163.6                             | 16.7           | 25.0              | 15.2                      | 10.4                         | 6.21 | 3.0                   |
|                      | 69                         |                      | 138                        | 308.7                             | 160.3                             | 13.8           | 21.7              | 15.2                      | 11.6                         | 7.11 | 2.9                   |
|                      | 59                         |                      | 118                        | 306.8                             | 157.2                             | 11.9           | 18.7              | 15.2                      | 13.2                         | 8.20 | 2.7                   |
|                      | 49                         |                      | 98                         | 304.8                             | 153.9                             | 9.9            | 15.4              | 15.2                      | 15.5                         | 9.90 | 2.5                   |
| 254x127              | 84                         | 254x254              | 168                        | 264.5                             | 144.5                             | 19.2           | 31.7              | 12.7                      | 7.53                         | 4.17 | 3.1                   |
|                      | 66                         |                      | 132                        | 261.0                             | 138.2                             | 15.6           | 25.3              | 12.7                      | 8.86                         | 5.16 | 2.7                   |
|                      | 54                         |                      | 108                        | 258.3                             | 133.4                             | 13.0           | 20.5              | 12.7                      | 10.3                         | 6.30 | 2.5                   |
|                      | 45                         |                      | 90                         | 255.9                             | 130.2                             | 10.5           | 17.3              | 12.7                      | 12.4                         | 7.40 | 2.2                   |
|                      | 37                         |                      | 74                         | 254.0                             | 127.0                             | 8.6            | 14.2              | 12.7                      | 14.8                         | 8.94 | 2.1                   |
| 203x102              | 43                         | 203x203              | 86                         | 208.8                             | 111.1                             | 13.0           | 20.5              | 10.2                      | 8.55                         | 5.09 | 2.2                   |
|                      | 36                         |                      | 72                         | 206.2                             | 108.0                             | 10.3           | 17.3              | 10.2                      | 10.5                         | 5.96 | 2.0                   |
|                      | 30                         |                      | 60                         | 205.2                             | 104.8                             | 9.3            | 14.2              | 10.2                      | 11.3                         | 7.23 | 1.9                   |
|                      | 26                         |                      | 52                         | 203.9                             | 103.1                             | 8.0            | 12.5              | 10.2                      | 12.9                         | 8.16 | 1.8                   |
|                      | 23                         |                      | 46                         | 203.2                             | 101.6                             | 7.3            | 11.0              | 10.2                      | 13.9                         | 9.24 | 1.7                   |
| 152x76               | 19                         | 152x152              | 38                         | 154.4                             | 80.9                              | 8.1            | 11.5              | 7.6                       | 9.99                         | 6.71 | 1.5                   |
|                      | 15                         |                      | 30                         | 152.9                             | 78.7                              | 6.6            | 9.4               | 7.6                       | 11.9                         | 8.13 | 1.4                   |
|                      | 12                         |                      | 24                         | 152.4                             | 76.2                              | 6.1            | 6.8               | 7.6                       | 12.5                         | 11.2 | 1.4                   |

FOR EXPLANATION OF TABLES SEE NOTE 2

**STRUCTURAL TEES  
CUT FROM UNIVERSAL COLUMNS**



**PROPERTIES**

| Designation |                | Second Moment Of Area |                 | Radius Of Gyration |          | Elastic Modulus |                 |                 | Plastic Modulus |                 | Torsional Constant | Area            |
|-------------|----------------|-----------------------|-----------------|--------------------|----------|-----------------|-----------------|-----------------|-----------------|-----------------|--------------------|-----------------|
| Serial Size | Mass Per Metre | Axis x-x              | Axis y-y        | Axis x-x           | Axis y-y | Axis x-x        |                 | Axis y-y        | Axis x-x        | Axis y-y        | J                  | A               |
|             |                |                       |                 |                    |          | Flange          | Toe             |                 |                 |                 |                    |                 |
| mm          | kg             | cm <sup>4</sup>       | cm <sup>4</sup> | cm                 | cm       | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>3</sup> | cm <sup>4</sup>    | cm <sup>2</sup> |
| 406x178     | 317            | 11970                 | 49100           | 5.44               | 11.0     | 1962            | 679             | 2315            | 1504            | 3556            | 6810               | 404             |
|             | 276            | 9570                  | 41330           | 5.22               | 10.9     | 1718            | 556             | 1975            | 1219            | 3029            | 4583               | 351             |
|             | 234            | 7431                  | 33970           | 5.00               | 10.7     | 1480            | 442             | 1647            | 957             | 2520            | 2891               | 298             |
|             | 197            | 5786                  | 27680           | 4.81               | 10.5     | 1278            | 352             | 1360            | 748             | 2077            | 1763               | 250             |
|             | 170            | 4685                  | 23430           | 4.66               | 10.4     | 1131            | 290             | 1163            | 608             | 1772            | 1165               | 216             |
|             | 144            | 3752                  | 19340           | 4.53               | 10.3     | 991             | 236             | 969             | 483             | 1475            | 718                | 183             |
|             | 118            | 2881                  | 15520           | 4.38               | 10.2     | 846             | 184             | 786             | 368             | 1193            | 405                | 150             |
| 406x178     | 239            | 8720                  | 34040           | 5.36               | 10.6     | 1623            | 546             | 1604            | 1089            | 2491            | 2797               | 304             |
| 368x178     | 101            | 2503                  | 11820           | 4.40               | 9.57     | 754             | 162             | 631             | 317             | 959             | 279                | 129             |
|             | 89             | 2103                  | 10220           | 4.32               | 9.52     | 678             | 137             | 550             | 264             | 833             | 191                | 113             |
|             | 77             | 1769                  | 8756            | 4.25               | 9.46     | 606             | 117             | 473             | 221             | 717             | 126                | 97.8            |
|             | 65             | 1455                  | 7288            | 4.20               | 9.39     | 532             | 96.7            | 396             | 180             | 599             | 76.8               | 82.6            |
| 305x152     | 142            | 3286                  | 12270           | 4.27               | 8.25     | 800             | 232             | 763             | 488             | 1168            | 1012               | 180             |
|             | 120            | 2609                  | 10110           | 4.13               | 8.14     | 698             | 188             | 636             | 388             | 972             | 632                | 153             |
|             | 99             | 2018                  | 8119            | 4.00               | 8.02     | 598             | 148             | 517             | 299             | 789             | 366                | 126             |
|             | 79             | 1526                  | 6248            | 3.90               | 7.89     | 502             | 115             | 402             | 224             | 613             | 188                | 100             |
|             | 69             | 1288                  | 5324            | 3.85               | 7.82     | 450             | 97.8            | 345             | 188             | 525             | 124                | 87.1            |
|             | 59             | 1071                  | 4503            | 3.78               | 7.76     | 399             | 82.2            | 294             | 155             | 446             | 79.9               | 74.8            |
|             | 48             | 857                   | 3636            | 3.73               | 7.68     | 343             | 66.5            | 239             | 123             | 362             | 45.5               | 61.6            |
| 254x127     | 84             | 1198                  | 4896            | 3.36               | 6.79     | 390             | 105             | 370             | 219             | 566             | 311                | 106             |
|             | 66             | 886                   | 3753            | 3.24               | 6.67     | 326             | 79.8            | 288             | 161             | 438             | 160                | 84.3            |
|             | 54             | 686                   | 2947            | 3.17               | 6.57     | 278             | 63.1            | 228             | 124             | 347             | 86.3               | 68.3            |
|             | 45             | 533                   | 2417            | 3.06               | 6.52     | 238             | 49.5            | 189             | 95.6            | 287             | 51.3               | 56.8            |
|             | 37             | 417                   | 1940            | 3.00               | 6.46     | 203             | 39.2            | 153             | 74.0            | 232             | 28.7               | 46.5            |
| 203x102     | 43             | 381                   | 1557            | 2.63               | 5.32     | 171             | 42.8            | 149             | 86.1            | 228             | 68.6               | 55.0            |
|             | 36             | 289                   | 1265            | 2.52               | 5.28     | 145             | 32.8            | 123             | 65.2            | 187             | 40.4               | 45.5            |
|             | 30             | 242                   | 1023            | 2.52               | 5.19     | 129             | 28.2            | 99.7            | 54.0            | 152             | 23.4               | 38.0            |
|             | 26             | 203                   | 884             | 2.47               | 5.16     | 115             | 23.7            | 86.7            | 45.0            | 132             | 15.9               | 33.2            |
|             | 23             | 179                   | 770             | 2.47               | 5.12     | 105             | 21.2            | 75.7            | 39.5            | 115             | 11.1               | 29.4            |
| 152x76      | 19             | 94.4                  | 353             | 2.00               | 3.87     | 61.1            | 14.4            | 45.7            | 27.5            | 69.8            | 9.60               | 23.6            |
|             | 15             | 73.1                  | 280             | 1.95               | 3.82     | 51.6            | 11.3            | 36.7            | 21.2            | 55.8            | 5.28               | 19.2            |
|             | 12             | 61.1                  | 201             | 2.03               | 3.68     | 42.6            | 9.88            | 26.3            | 17.7            | 40.2            | 2.39               | 14.8            |

Properties have been calculated assuming that there is no loss of material due to splitting. Values of u and x have not been given as there is no possibility of lateral torsional buckling due to bending about the x-x axis, because the second moment of area about y-y axis exceeds the second moment of area about x-x axis. The value of H is virtually zero and has not therefore been given. FOR EXPLANATION OF TABLES SEE NOTE 3



**BS 5950: Part 1: 1990 Section two****Table 5.** Deflection limits other than for pitched roof portal frames

|   |  |
|---|--|
| <i>(a) Deflection on beams due to unfactored imposed load</i>   |  |
| Cantilevers   | Length/180                               |
| Beams carrying plaster or other brittle finish  | Span/360                                 |
| All other beams   | Span/200                                 |
| Purlins and sheeting rails  | See clause 4.12.2                        |
| <i>(b) Horizontal deflection of columns other than portal frames due to unfactored imposed and wind loads</i> |  |
| Tops of columns in single-storey buildings  | Height/300                               |
| In each storey of a building with more than one storey  | Height of storey under consideration/300 |
| <i>(c) Crane gantry girders</i>   |  |
| Vertical deflection due to static wheel loads   | Span/600                                 |
| Horizontal deflection (calculated on the top flange properties alone) due to crane surge                      | Span/500                                 |

NOTE 1. On low-pitched and flat roofs the possibility of ponding needs consideration.

NOTE 2. For limiting deflections in runway beams refer to BS 2853.

**BS 5950: Part 1: 1990: Section three****Table 6.** Design strengths,  $p_y$ , for steel to BS 4360

| BS 4360 Grade | Thickness, less than or equal to | Sections, plates and hollow sections $p_y$ |
|---------------|----------------------------------|--|
| 43            | mm                               | N/mm <sup>2</sup>                          |
|               | 16                               | 275  |
|               | 40                               | 265  |
|               | 63                               | 255  |
|               | 80                               | 245  |
|               | 100                              | 235  |
| 50            | 16                               | 355  |
|               | 40                               | 345  |
|               | 63                               | 335  |
|               | 80                               | 325  |
|               | 100                              | 315  |
| 55            | 16                               | 450  |
|               | 25                               | 430  |
|               | 40                               | 415  |
|               | 63                               | 400  |

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**Table 7.** Limiting width to thickness ratios  
(Elements which exceed these limits are to be taken as class 4, slender cross sections.)

| Type of element   | Type of section            | Class of section  |   |   |
|---|----------------------------|---|---|---|
|   |                            | (1) Plastic   | (2) Compact   | (3) Semi-compact  |
| Outstand element of compression flange                                    | Built-up by welding        | $\frac{b}{T} \leq 7.5\epsilon$  | $\frac{b}{T} \leq 8.5\epsilon$  | $\frac{b}{T} \leq 13\epsilon$   |
|   | Rolled sections            | $\frac{b}{T} \leq 8.5\epsilon$  | $\frac{b}{T} \leq 9.5\epsilon$  | $\frac{b}{T} \leq 15\epsilon$   |
| Internal element of compression flange                                    | Built-up by welding        | $\frac{b}{T} \leq 23\epsilon$   | $\frac{b}{T} \leq 25\epsilon$   | $\frac{b}{T} \leq 28\epsilon$   |
|   | Rolled sections            | $\frac{b}{T} \leq 26\epsilon$   | $\frac{b}{T} \leq 32\epsilon$   | $\frac{b}{T} \leq 39\epsilon$   |
| Web, with neutral axis at mid-depth                                       | All sections               | $\frac{d}{t} \leq 79\epsilon$   | $\frac{d}{t} \leq 98\epsilon$   | $\frac{d}{t} \leq 120\epsilon$  |
| Web, generally  | All sections               | $\frac{d}{t} \leq \frac{79\epsilon}{0.4 + 0.6\alpha}$                   | $\frac{d}{t} \leq \frac{98\epsilon}{\alpha}$                            | See clause 3.5.4  |
| Web, where whole section is subject to compression                        | Built-up by welding        | $\frac{d}{t} \leq 28\epsilon$   | $\frac{d}{t} \leq 28\epsilon$   | $\frac{d}{t} \leq 28\epsilon$   |
|   | Rolled sections            | $\frac{d}{t} \leq 39\epsilon$   | $\frac{d}{t} \leq 39\epsilon$   | $\frac{d}{t} \leq 39\epsilon$   |
| Legs of single angle and double angle members with components separated   | Rolled angle sections      | $\frac{b}{T} \leq 8.5\epsilon$<br>and<br>$\frac{d}{T} \leq 8.5\epsilon$ | $\frac{b}{T} \leq 9.5\epsilon$<br>and<br>$\frac{d}{T} \leq 9.5\epsilon$ | $\frac{b}{T}$ and $\frac{d}{T} \leq 15\epsilon$<br>and<br>$\frac{b+d}{T} \leq 23\epsilon$ |
| Outstand legs of double angle members with angles in contact back-to-back | Rolled angle sections      | $\frac{b}{T} \leq 8.5\epsilon$  | $\frac{b}{T} \leq 9.5\epsilon$  | $\frac{b}{T} \leq 15\epsilon$   |
| Stems of T-sections   | T-section                  | $\frac{d}{t} \leq 8.5\epsilon$  | $\frac{d}{t} \leq 9.5\epsilon$  | $\frac{d}{t} \leq 19\epsilon$   |
| Circular tube subject to moment or axial compression                      | CHS or built-up by welding | $\frac{D}{t} \leq 40\epsilon^2$   | $\frac{D}{t} \leq 57\epsilon^2$   | $\frac{D}{t} \leq 80\epsilon^2$   |

NOTE 1. Dimensions  $b, D, d, T, t$  are as defined in figure 3. of BS 5950: part 1.

$$\alpha = \frac{2y_c}{d}$$

where  $y_c$  is the distance from the plastic neutral axis to the edge of the web connected to the compression flange. But if  $\alpha > 2$  the section should be taken as having compression throughout.

NOTE 2. Check webs for shear buckling in accordance with clause 4.4 when  $d/t > 63\epsilon$ .

NOTE 3.  $\epsilon = \left(\frac{275}{p_y}\right)^{1/2}$

**BS 5950: Part 1: 1990: Section four****Table 11.** Bending strength  $p_b$  (in N/mm<sup>2</sup>) for rolled sections

| $\lambda_{LT}$ | $p_y$ | 245 | 265 | 275 | 325 | 340 | 355 | 415 | 430 | 450 |
|----------------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 30             | 245   | 245 | 265 | 275 | 325 | 340 | 355 | 408 | 421 | 438 |
| 35             | 245   | 245 | 265 | 273 | 316 | 328 | 341 | 390 | 402 | 418 |
| 40             | 238   | 238 | 254 | 262 | 302 | 313 | 325 | 371 | 382 | 397 |
| 45             | 227   | 227 | 242 | 250 | 287 | 298 | 309 | 350 | 361 | 374 |
| 50             | 217   | 217 | 231 | 238 | 272 | 282 | 292 | 329 | 338 | 350 |
| 55             | 206   | 206 | 219 | 226 | 257 | 266 | 274 | 307 | 315 | 325 |
| 60             | 195   | 195 | 207 | 213 | 241 | 249 | 257 | 285 | 292 | 300 |
| 65             | 185   | 185 | 196 | 201 | 225 | 232 | 239 | 263 | 269 | 276 |
| 70             | 174   | 174 | 184 | 188 | 210 | 216 | 222 | 242 | 247 | 253 |
| 75             | 164   | 164 | 172 | 176 | 195 | 200 | 205 | 223 | 226 | 231 |
| 80             | 154   | 154 | 161 | 165 | 181 | 186 | 190 | 204 | 208 | 212 |
| 85             | 144   | 144 | 151 | 154 | 168 | 172 | 175 | 188 | 190 | 194 |
| 90             | 135   | 135 | 141 | 144 | 156 | 159 | 162 | 173 | 175 | 178 |
| 95             | 126   | 126 | 131 | 134 | 144 | 147 | 150 | 159 | 161 | 163 |
| 100            | 118   | 118 | 123 | 125 | 134 | 137 | 139 | 147 | 148 | 150 |
| 105            | 111   | 111 | 115 | 117 | 125 | 127 | 129 | 136 | 137 | 139 |
| 110            | 104   | 104 | 107 | 109 | 116 | 118 | 120 | 126 | 127 | 128 |
| 115            | 97    | 97  | 101 | 102 | 108 | 110 | 111 | 117 | 118 | 119 |
| 120            | 91    | 91  | 94  | 96  | 101 | 103 | 104 | 108 | 109 | 111 |
| 125            | 86    | 86  | 89  | 90  | 95  | 96  | 97  | 101 | 102 | 103 |
| 130            | 81    | 81  | 83  | 84  | 89  | 90  | 91  | 94  | 95  | 96  |
| 135            | 76    | 76  | 78  | 79  | 83  | 84  | 85  | 88  | 89  | 90  |
| 140            | 72    | 72  | 74  | 75  | 78  | 79  | 80  | 83  | 84  | 84  |
| 145            | 68    | 68  | 70  | 71  | 74  | 75  | 75  | 78  | 79  | 79  |
| 150            | 64    | 64  | 66  | 67  | 70  | 70  | 71  | 73  | 74  | 75  |
| 155            | 61    | 61  | 62  | 63  | 66  | 66  | 67  | 69  | 70  | 70  |
| 160            | 58    | 58  | 59  | 60  | 62  | 63  | 63  | 65  | 66  | 66  |
| 165            | 55    | 55  | 56  | 57  | 59  | 60  | 60  | 62  | 62  | 63  |
| 170            | 52    | 52  | 53  | 54  | 56  | 56  | 57  | 59  | 59  | 59  |
| 175            | 50    | 50  | 51  | 51  | 53  | 54  | 54  | 56  | 56  | 56  |
| 180            | 47    | 47  | 48  | 49  | 51  | 51  | 51  | 53  | 53  | 53  |
| 185            | 45    | 45  | 46  | 46  | 48  | 49  | 49  | 50  | 50  | 51  |
| 190            | 43    | 43  | 44  | 44  | 46  | 46  | 47  | 48  | 48  | 48  |
| 195            | 41    | 41  | 42  | 42  | 44  | 44  | 44  | 46  | 46  | 46  |
| 200            | 39    | 39  | 40  | 40  | 42  | 42  | 42  | 43  | 44  | 44  |
| 210            | 36    | 36  | 37  | 37  | 38  | 39  | 39  | 40  | 40  | 40  |
| 220            | 33    | 33  | 34  | 34  | 35  | 35  | 36  | 36  | 37  | 37  |
| 230            | 31    | 31  | 31  | 31  | 32  | 33  | 33  | 33  | 34  | 34  |
| 240            | 29    | 29  | 29  | 29  | 30  | 30  | 30  | 31  | 31  | 31  |
| 250            | 27    | 27  | 27  | 27  | 28  | 28  | 28  | 29  | 29  | 29  |

**Table 12.** Bending strength  $\rho_b$  (in N/mm<sup>2</sup>) for welded sections

| $\lambda_{LT}$ $\rho_y$ | 245 | 265 | 275 | 325 | 340 | 355 | 415 | 430 | 450 |
|-------------------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 30                      | 245 | 265 | 275 | 325 | 340 | 355 | 401 | 412 | 427 |
| 35                      | 245 | 265 | 272 | 307 | 317 | 328 | 368 | 378 | 391 |
| 40                      | 231 | 244 | 250 | 282 | 292 | 301 | 337 | 346 | 358 |
| 45                      | 212 | 224 | 230 | 259 | 268 | 276 | 308 | 316 | 327 |
| 50                      | 196 | 207 | 212 | 238 | 246 | 253 | 282 | 288 | 297 |
| 55                      | 180 | 190 | 195 | 219 | 225 | 232 | 257 | 263 | 275 |
| 60                      | 167 | 176 | 180 | 201 | 207 | 212 | 245 | 253 | 264 |
| 65                      | 154 | 162 | 166 | 188 | 196 | 204 | 235 | 242 | 251 |
| 70                      | 142 | 150 | 155 | 182 | 189 | 196 | 224 | 230 | 238 |
| 75                      | 135 | 145 | 151 | 175 | 182 | 188 | 212 | 218 | 225 |
| 80                      | 131 | 141 | 146 | 168 | 174 | 179 | 201 | 205 | 211 |
| 85                      | 127 | 136 | 140 | 160 | 165 | 171 | 188 | 190 | 194 |
| 90                      | 123 | 131 | 135 | 152 | 157 | 162 | 173 | 175 | 178 |
| 95                      | 118 | 125 | 129 | 144 | 147 | 150 | 159 | 161 | 163 |
| 100                     | 113 | 120 | 123 | 134 | 137 | 139 | 147 | 148 | 150 |
| 105                     | 109 | 115 | 117 | 125 | 127 | 129 | 136 | 137 | 139 |
| 110                     | 104 | 107 | 109 | 116 | 118 | 120 | 126 | 127 | 128 |
| 115                     | 97  | 101 | 102 | 108 | 110 | 111 | 117 | 118 | 119 |
| 120                     | 91  | 94  | 96  | 101 | 103 | 104 | 108 | 109 | 111 |
| 125                     | 86  | 89  | 90  | 95  | 96  | 97  | 101 | 102 | 103 |
| 130                     | 81  | 83  | 84  | 89  | 90  | 91  | 94  | 95  | 96  |
| 135                     | 76  | 78  | 79  | 83  | 84  | 85  | 88  | 89  | 90  |
| 140                     | 72  | 74  | 75  | 78  | 79  | 80  | 83  | 84  | 84  |
| 145                     | 68  | 70  | 71  | 74  | 75  | 75  | 78  | 79  | 79  |
| 150                     | 64  | 66  | 67  | 70  | 70  | 71  | 73  | 74  | 75  |
| 155                     | 61  | 62  | 63  | 66  | 66  | 67  | 69  | 70  | 70  |
| 160                     | 58  | 59  | 60  | 62  | 63  | 63  | 65  | 66  | 66  |
| 165                     | 55  | 56  | 57  | 59  | 60  | 60  | 62  | 62  | 63  |
| 170                     | 52  | 53  | 54  | 56  | 56  | 57  | 59  | 59  | 59  |
| 175                     | 50  | 51  | 51  | 53  | 54  | 54  | 56  | 56  | 56  |
| 180                     | 47  | 48  | 49  | 51  | 51  | 51  | 53  | 53  | 53  |
| 185                     | 45  | 46  | 46  | 48  | 49  | 49  | 50  | 50  | 51  |
| 190                     | 43  | 44  | 44  | 46  | 46  | 47  | 48  | 48  | 48  |
| 195                     | 41  | 42  | 42  | 44  | 44  | 44  | 46  | 46  | 46  |
| 200                     | 39  | 40  | 40  | 42  | 42  | 42  | 43  | 44  | 44  |
| 210                     | 36  | 37  | 37  | 38  | 39  | 39  | 40  | 40  | 40  |
| 220                     | 33  | 34  | 34  | 35  | 35  | 36  | 36  | 37  | 37  |
| 230                     | 31  | 31  | 31  | 32  | 33  | 33  | 33  | 34  | 34  |
| 240                     | 29  | 29  | 29  | 30  | 30  | 30  | 31  | 31  | 31  |
| 250                     | 27  | 27  | 27  | 28  | 28  | 28  | 29  | 29  | 29  |

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**BS 5950: Part 1: 1990: Section four****Table 25.** Strut table selection

| Type of section   | Thickness<br>(see note 1) | Axis of buckling                    |       |
|---|---------------------------|-------------------------------------|-------|
|   |                           | x-x                                 | y-y   |
| Hot-rolled structural hollow section  |                           | 27(a)                               | 27(a) |
| Rolled I-section (or as shown in table 26(a))   |                           | 27(a)                               | 27(b) |
| Rolled H-section (or as shown in table 26(a))   | up to 40 mm               | 27(b)                               | 27(c) |
|   | over 40 mm                | 27(c)                               | 27(d) |
| Welded plate I or H-section (see note 2 and clause 4.7.5)<br>(or as shown in table 26(c)) | up to 40 mm               | 27(b)                               | 27(c) |
|   | over 40 mm                | 27(b)                               | 27(d) |
| Rolled I or H-section with welded flange cover plates (as<br>shown in table 26(b))        | up to 40 mm               | 27(b)                               | 27(a) |
|   | over 40 mm                | 27(c)                               | 27(b) |
| Welded box section (see note 3 and clause 4.7.5)  | up to 40 mm               | 27(b)                               | 27(b) |
|   | over 40 mm                | 27(c)                               | 27(c) |
| Round, square or flat bar   | up to 40 mm               | 27(b)                               | 27(b) |
|   | over 40 mm                | 27(c)                               | 27(c) |
| Rolled angle  |                           | Buckling about<br>any axis<br>27(c) |       |
| Rolled channel or T-section   |                           |                                     |       |
| Two rolled sections laced or battened   |                           |                                     |       |
| Two rolled sections back-to-back  |                           |                                     |       |
| Compound rolled sections  |                           |                                     |       |

NOTE 1. For thicknesses between 40 mm and 50 mm the value of  $p_c$  may be taken as the average of the values for thicknesses up to 40 mm and over 40 mm.

NOTE 2. For welded plate I or H-sections where it can be guaranteed that the edges of the flanges will only be flame-cut, table 27(b) may be used for buckling about the y-y axis for flanges up to 40 mm thick, and table 27(c) for flanges over 40 mm thick.

NOTE 3. 'Welded box section' includes any box section fabricated from plates or rolled sections, provided that all longitudinal welds are near the corners of the section. Box sections with welded longitudinal stiffeners are *not* included in this category.

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**Table 27(a).** Compressive strength  $p_c$  (in N/mm<sup>2</sup>) for struts

| $\lambda$ | $P_y$ | 225 | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 395 | 410 | 415 | 430 | 450 |
|-----------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 15        | 225   | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 394 | 409 | 414 | 429 | 448 |     |
| 20        | 225   | 244 | 254 | 264 | 273 | 303 | 317 | 322 | 332 | 337 | 351 | 390 | 405 | 410 | 424 | 444 |     |
| 25        | 222   | 241 | 251 | 261 | 270 | 299 | 314 | 318 | 328 | 333 | 347 | 386 | 400 | 405 | 419 | 438 |     |
| 30        | 220   | 239 | 248 | 258 | 267 | 296 | 310 | 315 | 324 | 329 | 343 | 381 | 395 | 399 | 414 | 432 |     |
| 35        | 217   | 236 | 245 | 254 | 264 | 292 | 306 | 310 | 320 | 324 | 338 | 375 | 389 | 393 | 407 | 425 |     |
| 40        | 214   | 233 | 242 | 251 | 260 | 287 | 301 | 305 | 315 | 319 | 333 | 368 | 382 | 386 | 399 | 417 |     |
| 42        | 213   | 231 | 240 | 249 | 258 | 285 | 299 | 303 | 312 | 317 | 330 | 365 | 378 | 383 | 396 | 413 |     |
| 44        | 212   | 230 | 239 | 248 | 257 | 283 | 297 | 301 | 310 | 314 | 327 | 362 | 375 | 379 | 392 | 409 |     |
| 46        | 210   | 228 | 237 | 246 | 255 | 281 | 294 | 299 | 307 | 312 | 325 | 359 | 371 | 375 | 388 | 404 |     |
| 48        | 209   | 227 | 236 | 244 | 253 | 279 | 292 | 296 | 305 | 309 | 322 | 355 | 367 | 371 | 383 | 399 |     |
| 50        | 208   | 225 | 234 | 242 | 251 | 277 | 289 | 293 | 302 | 306 | 318 | 351 | 363 | 367 | 379 | 394 |     |
| 52        | 206   | 223 | 232 | 241 | 249 | 274 | 286 | 291 | 299 | 303 | 315 | 346 | 358 | 362 | 373 | 388 |     |
| 54        | 205   | 222 | 230 | 238 | 247 | 271 | 283 | 287 | 295 | 299 | 311 | 342 | 353 | 356 | 367 | 381 |     |
| 56        | 203   | 220 | 228 | 236 | 244 | 268 | 280 | 284 | 292 | 296 | 307 | 336 | 347 | 350 | 361 | 374 |     |
| 58        | 201   | 218 | 226 | 234 | 242 | 265 | 277 | 281 | 288 | 292 | 303 | 331 | 341 | 344 | 354 | 366 |     |
| 60        | 200   | 216 | 224 | 232 | 239 | 262 | 273 | 277 | 284 | 288 | 298 | 325 | 335 | 337 | 347 | 358 |     |
| 62        | 198   | 214 | 221 | 229 | 236 | 259 | 269 | 273 | 280 | 283 | 293 | 318 | 328 | 330 | 339 | 349 |     |
| 64        | 196   | 211 | 219 | 226 | 234 | 255 | 265 | 268 | 275 | 278 | 288 | 311 | 320 | 322 | 331 | 340 |     |
| 66        | 194   | 209 | 216 | 223 | 230 | 251 | 261 | 264 | 270 | 273 | 282 | 304 | 312 | 314 | 322 | 330 |     |
| 68        | 192   | 206 | 213 | 220 | 227 | 247 | 256 | 259 | 265 | 268 | 276 | 296 | 304 | 306 | 313 | 320 |     |
| 70        | 189   | 204 | 210 | 217 | 224 | 242 | 251 | 254 | 259 | 262 | 270 | 288 | 295 | 297 | 303 | 310 |     |
| 72        | 187   | 201 | 207 | 214 | 220 | 237 | 246 | 248 | 253 | 256 | 264 | 280 | 287 | 288 | 294 | 299 |     |
| 74        | 184   | 198 | 204 | 210 | 216 | 233 | 240 | 243 | 247 | 250 | 256 | 272 | 278 | 279 | 284 | 289 |     |
| 76        | 182   | 194 | 200 | 206 | 212 | 227 | 235 | 237 | 241 | 243 | 249 | 264 | 269 | 270 | 275 | 279 |     |
| 78        | 179   | 191 | 197 | 202 | 208 | 222 | 229 | 231 | 235 | 237 | 242 | 255 | 260 | 261 | 265 | 269 |     |
| 80        | 176   | 188 | 193 | 198 | 203 | 217 | 223 | 225 | 229 | 230 | 235 | 247 | 251 | 252 | 256 | 259 |     |
| 82        | 173   | 184 | 189 | 194 | 199 | 211 | 217 | 219 | 222 | 224 | 228 | 239 | 243 | 243 | 247 | 250 |     |
| 84        | 170   | 181 | 185 | 190 | 194 | 206 | 211 | 213 | 216 | 217 | 221 | 231 | 234 | 235 | 238 | 240 |     |
| 86        | 167   | 177 | 181 | 186 | 190 | 200 | 205 | 207 | 209 | 211 | 214 | 223 | 226 | 226 | 229 | 231 |     |
| 88        | 164   | 173 | 177 | 181 | 185 | 195 | 199 | 200 | 203 | 204 | 208 | 215 | 218 | 218 | 221 | 223 |     |
| 90        | 161   | 169 | 173 | 177 | 180 | 189 | 193 | 195 | 197 | 198 | 201 | 208 | 211 | 211 | 213 | 215 |     |
| 92        | 158   | 166 | 169 | 173 | 176 | 184 | 188 | 189 | 191 | 192 | 194 | 201 | 203 | 203 | 206 | 207 |     |
| 94        | 154   | 162 | 165 | 168 | 171 | 179 | 182 | 183 | 185 | 186 | 188 | 194 | 196 | 196 | 198 | 200 |     |
| 96        | 151   | 158 | 161 | 164 | 166 | 173 | 176 | 177 | 179 | 180 | 182 | 187 | 190 | 189 | 191 | 192 |     |
| 98        | 147   | 154 | 157 | 159 | 162 | 168 | 171 | 172 | 173 | 174 | 176 | 181 | 183 | 183 | 185 | 186 |     |
| 100       | 144   | 150 | 153 | 155 | 157 | 163 | 166 | 167 | 168 | 169 | 171 | 175 | 176 | 177 | 178 | 179 |     |
| 102       | 141   | 146 | 149 | 151 | 153 | 158 | 161 | 161 | 163 | 163 | 165 | 169 | 170 | 171 | 172 | 173 |     |
| 104       | 137   | 142 | 145 | 147 | 149 | 154 | 156 | 156 | 158 | 158 | 160 | 163 | 165 | 165 | 166 | 167 |     |
| 106       | 134   | 139 | 141 | 143 | 145 | 149 | 151 | 152 | 153 | 153 | 155 | 158 | 159 | 159 | 160 | 161 |     |
| 108       | 131   | 135 | 137 | 139 | 141 | 145 | 146 | 147 | 148 | 149 | 150 | 153 | 154 | 154 | 155 | 156 |     |





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**Table 27(b).** Compressive strength  $p_c$  (in N/mm<sup>2</sup>) for struts

| $\lambda$ | $p_y$ | 225 | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 395 | 410 | 415 | 430 | 450 |
|-----------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 15        | 225   | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 394 | 409 | 413 | 428 | 447 |     |
| 20        | 224   | 243 | 253 | 263 | 272 | 301 | 315 | 320 | 330 | 334 | 349 | 387 | 401 | 406 | 420 | 439 |     |
| 25        | 220   | 239 | 248 | 258 | 267 | 295 | 309 | 314 | 323 | 328 | 342 | 379 | 393 | 397 | 411 | 430 |     |
| 30        | 216   | 234 | 243 | 253 | 262 | 289 | 303 | 307 | 316 | 321 | 335 | 371 | 384 | 389 | 402 | 420 |     |
| 35        | 211   | 229 | 238 | 247 | 256 | 283 | 296 | 300 | 309 | 313 | 327 | 361 | 374 | 379 | 392 | 409 |     |
| 40        | 207   | 224 | 233 | 241 | 250 | 276 | 288 | 293 | 301 | 305 | 318 | 351 | 364 | 368 | 380 | 396 |     |
| 42        | 205   | 222 | 231 | 239 | 248 | 273 | 285 | 289 | 298 | 302 | 314 | 347 | 359 | 363 | 375 | 391 |     |
| 44        | 203   | 220 | 228 | 237 | 245 | 270 | 282 | 286 | 294 | 298 | 310 | 342 | 354 | 358 | 369 | 385 |     |
| 46        | 201   | 218 | 226 | 234 | 242 | 267 | 279 | 283 | 291 | 294 | 306 | 337 | 349 | 352 | 364 | 379 |     |
| 48        | 199   | 215 | 223 | 231 | 239 | 263 | 275 | 279 | 287 | 291 | 302 | 332 | 343 | 347 | 358 | 372 |     |
| 50        | 197   | 213 | 221 | 229 | 237 | 260 | 271 | 275 | 283 | 286 | 298 | 327 | 337 | 341 | 351 | 365 |     |
| 52        | 195   | 210 | 218 | 226 | 234 | 256 | 267 | 271 | 278 | 282 | 293 | 321 | 331 | 334 | 349 | 358 |     |
| 54        | 192   | 208 | 215 | 223 | 230 | 253 | 263 | 267 | 274 | 278 | 288 | 315 | 325 | 328 | 337 | 350 |     |
| 56        | 190   | 205 | 213 | 220 | 227 | 249 | 259 | 263 | 269 | 273 | 283 | 309 | 318 | 321 | 330 | 342 |     |
| 58        | 188   | 202 | 210 | 217 | 224 | 245 | 255 | 258 | 265 | 268 | 278 | 302 | 311 | 314 | 322 | 333 |     |
| 60        | 185   | 200 | 207 | 214 | 221 | 241 | 250 | 254 | 260 | 263 | 272 | 295 | 304 | 306 | 314 | 325 |     |
| 62        | 183   | 197 | 204 | 210 | 217 | 236 | 246 | 249 | 255 | 258 | 266 | 288 | 296 | 299 | 306 | 316 |     |
| 64        | 180   | 194 | 200 | 207 | 213 | 232 | 241 | 244 | 249 | 252 | 261 | 281 | 289 | 291 | 298 | 307 |     |
| 66        | 178   | 191 | 197 | 203 | 210 | 227 | 236 | 239 | 244 | 247 | 255 | 274 | 281 | 283 | 289 | 298 |     |
| 68        | 175   | 188 | 194 | 200 | 206 | 223 | 231 | 233 | 239 | 241 | 249 | 267 | 273 | 275 | 281 | 288 |     |
| 70        | 172   | 185 | 190 | 196 | 202 | 218 | 226 | 228 | 233 | 235 | 242 | 259 | 265 | 267 | 272 | 279 |     |
| 72        | 169   | 181 | 187 | 193 | 198 | 213 | 220 | 223 | 227 | 230 | 236 | 252 | 257 | 259 | 264 | 270 |     |
| 74        | 167   | 178 | 183 | 189 | 194 | 208 | 215 | 217 | 222 | 224 | 230 | 244 | 249 | 251 | 255 | 261 |     |
| 76        | 164   | 175 | 180 | 185 | 190 | 204 | 210 | 212 | 216 | 218 | 223 | 237 | 241 | 243 | 247 | 252 |     |
| 78        | 161   | 171 | 176 | 181 | 186 | 199 | 205 | 206 | 210 | 212 | 217 | 230 | 234 | 235 | 239 | 244 |     |
| 80        | 158   | 168 | 172 | 177 | 181 | 194 | 199 | 201 | 204 | 206 | 211 | 222 | 226 | 227 | 231 | 235 |     |
| 82        | 155   | 164 | 169 | 173 | 177 | 189 | 194 | 196 | 199 | 200 | 205 | 215 | 219 | 220 | 223 | 227 |     |
| 84        | 152   | 161 | 165 | 169 | 173 | 184 | 189 | 190 | 193 | 195 | 199 | 209 | 212 | 213 | 216 | 219 |     |
| 86        | 149   | 157 | 161 | 165 | 169 | 179 | 183 | 185 | 188 | 189 | 193 | 202 | 205 | 206 | 208 | 212 |     |
| 88        | 146   | 154 | 158 | 161 | 165 | 174 | 178 | 180 | 182 | 183 | 187 | 195 | 198 | 199 | 201 | 204 |     |
| 90        | 143   | 150 | 154 | 157 | 161 | 169 | 173 | 175 | 177 | 178 | 181 | 189 | 192 | 192 | 195 | 197 |     |
| 92        | 139   | 147 | 150 | 153 | 156 | 165 | 168 | 170 | 172 | 173 | 176 | 183 | 185 | 186 | 188 | 191 |     |
| 94        | 136   | 143 | 147 | 150 | 152 | 160 | 164 | 165 | 167 | 168 | 171 | 177 | 179 | 180 | 182 | 184 |     |
| 96        | 133   | 140 | 143 | 146 | 148 | 156 | 159 | 160 | 162 | 163 | 165 | 171 | 173 | 174 | 176 | 178 |     |
| 98        | 130   | 137 | 139 | 142 | 145 | 151 | 154 | 155 | 157 | 158 | 160 | 166 | 168 | 168 | 170 | 172 |     |
| 100       | 127   | 133 | 136 | 138 | 141 | 147 | 150 | 151 | 152 | 153 | 155 | 161 | 162 | 163 | 164 | 166 |     |
| 102       | 124   | 130 | 132 | 135 | 137 | 143 | 146 | 146 | 148 | 149 | 151 | 156 | 157 | 158 | 159 | 161 |     |
| 104       | 122   | 127 | 129 | 131 | 133 | 139 | 141 | 142 | 144 | 144 | 146 | 151 | 152 | 153 | 154 | 156 |     |
| 106       | 119   | 124 | 126 | 128 | 130 | 135 | 137 | 138 | 139 | 140 | 142 | 146 | 148 | 148 | 149 | 151 |     |
| 108       | 116   | 121 | 123 | 125 | 126 | 131 | 133 | 134 | 135 | 136 | 138 | 142 | 143 | 143 | 144 | 146 |     |



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**Table 27(c).** Compressive strength  $p_c$  (in N/mm<sup>2</sup>) for struts

| $\lambda$ | $p_y$ | 225 | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 395 | 410 | 415 | 430 | 450 |
|-----------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 15        | 225   | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 393 | 408 | 413 | 427 | 446 |     |
| 20        | 224   | 242 | 252 | 261 | 271 | 299 | 312 | 317 | 326 | 331 | 345 | 382 | 396 | 401 | 414 | 433 |     |
| 25        | 217   | 235 | 245 | 254 | 263 | 290 | 303 | 308 | 317 | 321 | 335 | 370 | 384 | 388 | 402 | 419 |     |
| 30        | 211   | 228 | 237 | 246 | 255 | 281 | 294 | 298 | 307 | 311 | 324 | 358 | 371 | 375 | 388 | 405 |     |
| 35        | 204   | 221 | 230 | 238 | 247 | 272 | 284 | 288 | 296 | 300 | 313 | 345 | 357 | 361 | 374 | 389 |     |
| 40        | 198   | 214 | 222 | 230 | 238 | 262 | 274 | 278 | 285 | 289 | 301 | 332 | 343 | 347 | 358 | 373 |     |
| 42        | 195   | 211 | 219 | 227 | 235 | 258 | 269 | 273 | 281 | 285 | 296 | 326 | 337 | 340 | 351 | 366 |     |
| 44        | 193   | 208 | 216 | 224 | 231 | 254 | 265 | 269 | 276 | 280 | 291 | 320 | 330 | 334 | 344 | 358 |     |
| 46        | 190   | 205 | 213 | 220 | 228 | 250 | 261 | 264 | 271 | 275 | 286 | 314 | 324 | 327 | 337 | 351 |     |
| 48        | 187   | 202 | 209 | 217 | 224 | 246 | 256 | 260 | 267 | 270 | 280 | 307 | 317 | 321 | 330 | 343 |     |
| 50        | 184   | 199 | 206 | 213 | 220 | 241 | 252 | 255 | 262 | 265 | 275 | 301 | 310 | 314 | 323 | 335 |     |
| 52        | 181   | 196 | 203 | 210 | 217 | 237 | 247 | 250 | 257 | 260 | 270 | 294 | 303 | 306 | 315 | 327 |     |
| 54        | 179   | 193 | 199 | 206 | 213 | 232 | 242 | 245 | 252 | 255 | 264 | 288 | 296 | 299 | 308 | 319 |     |
| 56        | 176   | 189 | 196 | 202 | 209 | 228 | 237 | 240 | 246 | 249 | 258 | 281 | 289 | 292 | 300 | 310 |     |
| 58        | 173   | 186 | 192 | 199 | 205 | 223 | 232 | 235 | 241 | 244 | 252 | 274 | 282 | 284 | 292 | 302 |     |
| 60        | 170   | 183 | 189 | 195 | 201 | 219 | 227 | 230 | 236 | 238 | 247 | 267 | 274 | 277 | 284 | 293 |     |
| 62        | 167   | 179 | 185 | 191 | 197 | 214 | 222 | 225 | 230 | 233 | 241 | 260 | 267 | 269 | 276 | 285 |     |
| 64        | 164   | 176 | 182 | 188 | 193 | 210 | 217 | 220 | 225 | 227 | 235 | 253 | 260 | 262 | 268 | 276 |     |
| 66        | 161   | 173 | 178 | 184 | 189 | 205 | 212 | 215 | 220 | 222 | 229 | 246 | 252 | 254 | 260 | 268 |     |
| 68        | 158   | 169 | 175 | 180 | 185 | 200 | 207 | 210 | 214 | 216 | 223 | 239 | 245 | 247 | 252 | 259 |     |
| 70        | 155   | 166 | 171 | 176 | 181 | 195 | 202 | 204 | 209 | 211 | 217 | 232 | 238 | 239 | 244 | 251 |     |
| 72        | 152   | 163 | 168 | 172 | 177 | 191 | 197 | 199 | 203 | 205 | 211 | 226 | 231 | 232 | 237 | 243 |     |
| 74        | 149   | 159 | 164 | 169 | 173 | 186 | 192 | 194 | 198 | 200 | 205 | 219 | 223 | 225 | 229 | 235 |     |
| 76        | 146   | 156 | 160 | 165 | 169 | 181 | 187 | 189 | 193 | 194 | 200 | 212 | 217 | 218 | 222 | 227 |     |
| 78        | 143   | 152 | 157 | 161 | 165 | 177 | 182 | 184 | 187 | 189 | 194 | 206 | 210 | 211 | 215 | 220 |     |
| 80        | 140   | 149 | 153 | 157 | 161 | 172 | 177 | 179 | 182 | 184 | 188 | 200 | 203 | 205 | 208 | 213 |     |
| 82        | 137   | 146 | 150 | 154 | 157 | 168 | 173 | 174 | 177 | 179 | 183 | 193 | 197 | 198 | 201 | 205 |     |
| 84        | 134   | 142 | 146 | 150 | 154 | 163 | 168 | 169 | 172 | 174 | 178 | 187 | 191 | 192 | 195 | 199 |     |
| 86        | 132   | 139 | 143 | 146 | 150 | 159 | 163 | 165 | 168 | 169 | 173 | 182 | 185 | 186 | 189 | 192 |     |
| 88        | 129   | 136 | 139 | 143 | 146 | 155 | 159 | 160 | 163 | 164 | 168 | 176 | 179 | 180 | 183 | 186 |     |
| 90        | 126   | 133 | 136 | 139 | 142 | 151 | 155 | 156 | 158 | 159 | 163 | 171 | 173 | 174 | 177 | 180 |     |
| 92        | 123   | 130 | 133 | 136 | 139 | 147 | 150 | 152 | 154 | 155 | 158 | 165 | 168 | 169 | 171 | 174 |     |
| 94        | 120   | 127 | 130 | 133 | 135 | 143 | 146 | 147 | 149 | 150 | 153 | 160 | 163 | 163 | 166 | 168 |     |
| 96        | 118   | 124 | 127 | 129 | 132 | 139 | 142 | 143 | 145 | 146 | 149 | 155 | 158 | 158 | 160 | 163 |     |
| 98        | 115   | 121 | 123 | 126 | 129 | 135 | 138 | 139 | 141 | 142 | 145 | 151 | 153 | 154 | 155 | 158 |     |
| 100       | 112   | 118 | 120 | 123 | 125 | 132 | 134 | 135 | 137 | 138 | 140 | 146 | 148 | 149 | 151 | 153 |     |
| 102       | 110   | 115 | 118 | 120 | 122 | 128 | 131 | 132 | 133 | 134 | 136 | 142 | 144 | 144 | 146 | 148 |     |
| 104       | 107   | 112 | 115 | 117 | 119 | 125 | 127 | 128 | 130 | 130 | 133 | 138 | 140 | 140 | 142 | 143 |     |
| 106       | 105   | 110 | 112 | 114 | 116 | 121 | 124 | 125 | 126 | 127 | 129 | 134 | 135 | 136 | 137 | 139 |     |
| 108       | 102   | 107 | 109 | 111 | 113 | 118 | 120 | 121 | 123 | 123 | 125 | 130 | 131 | 132 | 133 | 135 |     |



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**Table 27(d).** Compressive strength  $p_c$  (in N/mm<sup>2</sup>) for struts

| $\lambda$ | $P_y$ | 225 | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 395 | 410 | 415 | 430 | 450 |
|-----------|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 15        | 225   | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 393 | 407 | 411 | 425 | 444 |     |
| 20        | 223   | 241 | 250 | 259 | 269 | 296 | 309 | 314 | 323 | 327 | 341 | 376 | 390 | 394 | 408 | 426 |     |
| 25        | 214   | 231 | 240 | 249 | 257 | 283 | 296 | 301 | 309 | 313 | 326 | 360 | 373 | 377 | 390 | 407 |     |
| 30        | 205   | 222 | 230 | 238 | 247 | 271 | 283 | 287 | 296 | 300 | 312 | 344 | 356 | 360 | 372 | 388 |     |
| 35        | 196   | 212 | 220 | 228 | 236 | 259 | 271 | 274 | 282 | 286 | 297 | 327 | 339 | 342 | 353 | 368 |     |
| 40        | 188   | 203 | 210 | 218 | 225 | 247 | 258 | 261 | 268 | 272 | 283 | 310 | 321 | 324 | 334 | 348 |     |
| 42        | 184   | 199 | 206 | 214 | 221 | 242 | 252 | 256 | 263 | 266 | 277 | 304 | 314 | 317 | 327 | 340 |     |
| 44        | 181   | 195 | 202 | 209 | 216 | 237 | 247 | 251 | 257 | 261 | 271 | 297 | 306 | 309 | 319 | 331 |     |
| 46        | 178   | 192 | 199 | 205 | 212 | 232 | 242 | 245 | 252 | 255 | 265 | 290 | 299 | 302 | 311 | 323 |     |
| 48        | 174   | 188 | 195 | 201 | 208 | 227 | 237 | 240 | 246 | 249 | 259 | 283 | 291 | 294 | 303 | 314 |     |
| 50        | 171   | 184 | 191 | 197 | 204 | 222 | 232 | 235 | 241 | 244 | 253 | 276 | 284 | 287 | 295 | 306 |     |
| 52        | 168   | 181 | 187 | 193 | 199 | 217 | 226 | 229 | 235 | 238 | 246 | 269 | 277 | 279 | 287 | 298 |     |
| 54        | 165   | 177 | 183 | 189 | 195 | 213 | 221 | 224 | 229 | 232 | 240 | 262 | 269 | 272 | 279 | 289 |     |
| 56        | 161   | 173 | 179 | 185 | 191 | 208 | 216 | 219 | 224 | 227 | 234 | 255 | 262 | 264 | 271 | 281 |     |
| 58        | 158   | 170 | 175 | 181 | 187 | 203 | 211 | 213 | 218 | 221 | 229 | 248 | 255 | 257 | 264 | 272 |     |
| 60        | 155   | 166 | 172 | 177 | 183 | 198 | 206 | 208 | 213 | 215 | 223 | 241 | 247 | 250 | 256 | 264 |     |
| 62        | 152   | 163 | 168 | 173 | 178 | 193 | 201 | 203 | 208 | 210 | 217 | 234 | 240 | 242 | 248 | 256 |     |
| 64        | 149   | 159 | 164 | 169 | 174 | 189 | 196 | 198 | 202 | 204 | 211 | 227 | 233 | 235 | 241 | 248 |     |
| 66        | 145   | 156 | 160 | 165 | 170 | 184 | 191 | 193 | 197 | 199 | 205 | 221 | 226 | 228 | 234 | 240 |     |
| 68        | 142   | 152 | 157 | 162 | 166 | 179 | 186 | 188 | 192 | 194 | 200 | 214 | 220 | 221 | 226 | 233 |     |
| 70        | 139   | 149 | 153 | 158 | 162 | 175 | 181 | 183 | 187 | 189 | 194 | 208 | 213 | 215 | 219 | 225 |     |
| 72        | 136   | 145 | 150 | 154 | 158 | 170 | 176 | 178 | 182 | 183 | 189 | 202 | 207 | 208 | 213 | 218 |     |
| 74        | 133   | 142 | 146 | 150 | 155 | 166 | 171 | 173 | 177 | 178 | 183 | 196 | 200 | 202 | 206 | 211 |     |
| 76        | 130   | 139 | 143 | 147 | 151 | 162 | 167 | 169 | 172 | 173 | 178 | 190 | 194 | 195 | 199 | 204 |     |
| 78        | 127   | 136 | 139 | 143 | 147 | 157 | 162 | 164 | 167 | 169 | 173 | 184 | 188 | 189 | 193 | 198 |     |
| 80        | 125   | 132 | 136 | 140 | 143 | 153 | 158 | 160 | 163 | 164 | 168 | 179 | 182 | 184 | 187 | 191 |     |
| 82        | 122   | 129 | 133 | 136 | 140 | 149 | 154 | 155 | 158 | 159 | 163 | 173 | 177 | 178 | 181 | 185 |     |
| 84        | 119   | 126 | 130 | 133 | 136 | 145 | 150 | 151 | 154 | 155 | 159 | 168 | 171 | 172 | 176 | 179 |     |
| 86        | 117   | 123 | 127 | 130 | 133 | 142 | 146 | 147 | 149 | 151 | 154 | 163 | 166 | 167 | 170 | 174 |     |
| 88        | 114   | 120 | 123 | 127 | 130 | 138 | 142 | 143 | 145 | 146 | 150 | 158 | 161 | 162 | 165 | 168 |     |
| 90        | 111   | 118 | 121 | 123 | 126 | 134 | 138 | 139 | 141 | 142 | 146 | 154 | 156 | 157 | 160 | 163 |     |
| 92        | 109   | 115 | 118 | 120 | 123 | 131 | 134 | 135 | 137 | 138 | 142 | 149 | 152 | 152 | 155 | 158 |     |
| 94        | 106   | 112 | 115 | 117 | 120 | 127 | 131 | 132 | 134 | 135 | 138 | 145 | 147 | 148 | 150 | 153 |     |
| 96        | 104   | 109 | 112 | 115 | 117 | 124 | 127 | 128 | 130 | 131 | 134 | 140 | 143 | 143 | 146 | 148 |     |
| 98        | 101   | 107 | 109 | 112 | 114 | 121 | 124 | 125 | 126 | 127 | 130 | 136 | 138 | 139 | 141 | 144 |     |
| 100       | 99    | 104 | 107 | 109 | 111 | 117 | 120 | 121 | 123 | 124 | 126 | 132 | 134 | 135 | 137 | 139 |     |
| 102       | 97    | 102 | 104 | 106 | 108 | 114 | 117 | 118 | 120 | 121 | 123 | 129 | 131 | 131 | 133 | 135 |     |
| 104       | 95    | 99  | 102 | 104 | 106 | 111 | 114 | 115 | 116 | 117 | 120 | 125 | 127 | 127 | 129 | 131 |     |
| 106       | 93    | 97  | 99  | 101 | 103 | 109 | 111 | 112 | 113 | 114 | 116 | 121 | 123 | 124 | 125 | 127 |     |
| 108       | 90    | 95  | 97  | 99  | 101 | 106 | 108 | 109 | 110 | 111 | 113 | 118 | 120 | 120 | 122 | 124 |     |

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**Table 27(d).** (concluded)

| $\lambda$ | $\rho_y$ | 225 | 245 | 255 | 265 | 275 | 305 | 320 | 325 | 335 | 340 | 355 | 395 | 410 | 415 | 430 | 450 |
|-----------|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 110       | 88       | 93  | 95  | 96  | 98  | 103 | 105 | 106 | 108 | 108 | 110 | 115 | 116 | 117 | 118 | 120 |     |
| 112       | 86       | 90  | 92  | 94  | 96  | 101 | 103 | 103 | 105 | 105 | 107 | 112 | 113 | 114 | 115 | 117 |     |
| 114       | 84       | 88  | 90  | 92  | 94  | 98  | 100 | 101 | 102 | 103 | 104 | 109 | 110 | 110 | 112 | 113 |     |
| 116       | 83       | 86  | 88  | 90  | 91  | 96  | 98  | 98  | 99  | 100 | 102 | 106 | 107 | 107 | 109 | 110 |     |
| 118       | 81       | 84  | 86  | 88  | 89  | 93  | 95  | 96  | 97  | 97  | 99  | 103 | 104 | 105 | 106 | 107 |     |
| 120       | 79       | 83  | 84  | 86  | 87  | 91  | 93  | 94  | 94  | 95  | 96  | 100 | 102 | 102 | 103 | 104 |     |
| 122       | 77       | 81  | 82  | 84  | 85  | 89  | 91  | 91  | 92  | 93  | 94  | 97  | 99  | 99  | 100 | 102 |     |
| 124       | 76       | 79  | 81  | 82  | 83  | 87  | 88  | 89  | 90  | 92  | 95  | 96  | 96  | 96  | 97  | 99  |     |
| 126       | 74       | 77  | 79  | 80  | 81  | 84  | 86  | 87  | 88  | 88  | 89  | 93  | 94  | 94  | 95  | 96  |     |
| 128       | 72       | 75  | 77  | 78  | 79  | 83  | 84  | 85  | 85  | 86  | 87  | 90  | 92  | 92  | 93  | 94  |     |
| 130       | 71       | 74  | 75  | 76  | 77  | 81  | 82  | 83  | 83  | 84  | 85  | 88  | 89  | 89  | 90  | 91  |     |
| 135       | 67       | 70  | 71  | 72  | 73  | 76  | 77  | 78  | 79  | 80  | 83  | 84  | 84  | 84  | 85  | 86  |     |
| 140       | 64       | 66  | 67  | 68  | 69  | 72  | 73  | 74  | 74  | 74  | 75  | 78  | 79  | 79  | 80  | 81  |     |
| 145       | 60       | 63  | 64  | 65  | 66  | 68  | 69  | 70  | 70  | 70  | 71  | 73  | 74  | 74  | 75  | 76  |     |
| 150       | 58       | 59  | 61  | 61  | 62  | 64  | 65  | 66  | 66  | 66  | 67  | 69  | 70  | 70  | 71  | 71  |     |
| 155       | 55       | 57  | 58  | 58  | 59  | 61  | 62  | 62  | 63  | 63  | 64  | 65  | 66  | 66  | 67  | 67  |     |
| 160       | 52       | 54  | 55  | 55  | 56  | 58  | 59  | 59  | 59  | 60  | 60  | 62  | 63  | 63  | 63  | 64  |     |
| 165       | 50       | 51  | 52  | 53  | 53  | 55  | 56  | 56  | 56  | 57  | 57  | 59  | 59  | 59  | 60  | 60  |     |
| 170       | 47       | 49  | 50  | 50  | 51  | 52  | 53  | 53  | 54  | 54  | 54  | 56  | 56  | 56  | 57  | 57  |     |
| 175       | 45       | 47  | 47  | 48  | 48  | 50  | 50  | 51  | 51  | 51  | 52  | 53  | 54  | 54  | 54  | 54  |     |
| 180       | 43       | 45  | 45  | 46  | 46  | 47  | 48  | 48  | 48  | 49  | 49  | 50  | 51  | 51  | 51  | 52  |     |
| 185       | 42       | 42  | 43  | 43  | 44  | 45  | 46  | 46  | 46  | 46  | 47  | 48  | 48  | 48  | 49  | 49  |     |
| 190       | 40       | 41  | 41  | 42  | 42  | 43  | 44  | 44  | 44  | 44  | 45  | 46  | 46  | 46  | 47  | 47  |     |
| 195       | 38       | 39  | 40  | 40  | 40  | 41  | 42  | 42  | 42  | 42  | 43  | 44  | 44  | 44  | 44  | 45  |     |
| 200       | 36       | 37  | 38  | 38  | 39  | 40  | 40  | 40  | 40  | 41  | 41  | 42  | 42  | 42  | 42  | 43  |     |
| 210       | 34       | 34  | 35  | 35  | 35  | 36  | 37  | 37  | 37  | 37  | 37  | 38  | 39  | 39  | 39  | 39  |     |
| 220       | 31       | 32  | 32  | 32  | 33  | 33  | 34  | 34  | 34  | 34  | 34  | 35  | 35  | 35  | 36  | 36  |     |
| 230       | 29       | 29  | 30  | 30  | 30  | 31  | 31  | 31  | 31  | 32  | 32  | 32  | 33  | 33  | 33  | 33  |     |
| 240       | 27       | 27  | 28  | 28  | 28  | 29  | 29  | 29  | 29  | 29  | 29  | 30  | 30  | 30  | 30  | 30  |     |
| 250       | 25       | 25  | 26  | 26  | 26  | 27  | 27  | 27  | 27  | 27  | 27  | 28  | 28  | 28  | 28  | 28  |     |
| 260       | 23       | 24  | 24  | 24  | 24  | 25  | 25  | 25  | 25  | 25  | 25  | 26  | 26  | 26  | 26  | 26  |     |
| 270       | 22       | 22  | 23  | 23  | 23  | 23  | 23  | 24  | 24  | 24  | 24  | 24  | 24  | 24  | 24  | 24  |     |
| 280       | 20       | 21  | 21  | 21  | 21  | 22  | 22  | 22  | 22  | 22  | 22  | 23  | 23  | 23  | 23  | 23  |     |
| 290       | 19       | 20  | 20  | 20  | 20  | 20  | 21  | 21  | 21  | 21  | 21  | 21  | 21  | 21  | 21  | 21  |     |
| 300       | 18       | 18  | 19  | 19  | 19  | 19  | 19  | 19  | 19  | 19  | 20  | 20  | 20  | 20  | 20  | 20  |     |
| 310       | 17       | 17  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 18  | 19  | 19  | 19  | 19  | 19  |     |
| 320       | 16       | 16  | 17  | 17  | 17  | 17  | 17  | 17  | 17  | 17  | 17  | 18  | 18  | 18  | 18  | 18  |     |
| 330       | 15       | 15  | 16  | 16  | 16  | 16  | 16  | 16  | 16  | 16  | 16  | 17  | 17  | 17  | 17  | 17  |     |
| 340       | 14       | 15  | 15  | 15  | 15  | 15  | 15  | 15  | 15  | 15  | 15  | 16  | 16  | 16  | 16  | 16  |     |
| 350       | 14       | 14  | 14  | 14  | 14  | 14  | 14  | 14  | 14  | 14  | 15  | 15  | 15  | 15  | 15  | 15  |     |

## Hole sizes – for ordinary bolts and friction grip connections

| Nominal diameter (mm) | Clearance hole diameter <sup>b</sup> (mm) | Oversize hole diameter <sup>a</sup> (mm) | Short slotted holes <sup>a</sup> (mm) |                | Long slotted holes <sup>a</sup> (mm) |                   |
|-----------------------|---|--|---------------------------------------|----------------|--------------------------------------|-------------------|
|                       |   |  | Narrow dimension                      | Slot dimension | Narrow dimension                     | Maximum dimension |
| M12 <sup>a</sup>      | 14  | 17                                       | 14                                    | 18             | 14                                   | 30                |
| M16                   | 18  | 21                                       | 18                                    | 22             | 18                                   | 40                |
| M20                   | 22  | 25                                       | 22                                    | 26             | 22                                   | 50                |
| M22                   | 24  | 27                                       | 24                                    | 28             | 24                                   | 55                |
| M24                   | 26  | 30                                       | 26                                    | 32             | 26                                   | 60                |
| M27                   | 30  | 35                                       | 30                                    | 37             | 30                                   | 67                |
| M30                   | 33  | 38                                       | 33                                    | 40             | 33                                   | 75                |

<sup>a</sup> Hardened washers to be used<sup>b</sup> In cases where there are more than three plies in joint the holes in the inner plies should be one millimetre larger than those in the outer plies

## Bolt strengths

|   | Bolt grade |                   | Steel to BS 4360 |     |     |
|---|------------|-------------------|------------------|-----|-----|
|   | 4.6        | 8.8               | 43               | 50  | 55  |
| Shear strength, $p_s$ (N/mm <sup>2</sup> )      | 160        | 375               |                  |     |     |
| Bearing strength, $p_{bb}$ (N/mm <sup>2</sup> ) | 460        | 1035 <sup>a</sup> | 460              | 550 | 650 |
| Tension strength, $p_t$ (N/mm <sup>2</sup> )    | 195        | 450               |                  |     |     |

<sup>a</sup> The bearing value of the connected part is critical

## Bolt capacities in tension

| Nominal diameter (mm) | Tensile stress area <sup>b</sup> (mm <sup>2</sup> ) | Bolts grade 4.6 @ 195 N/mm <sup>2</sup> (kN) | Bolts grade 8.8 @ 450 N/mm <sup>2</sup> (kN) |
|-----------------------|---|--|--|
| M12                   | 84.3  | 16.43  | 37.93  |
| M16                   | 157   | 30.61  | 70.65  |
| M20                   | 245   | 47.77  | 110.25                                       |
| M22 <sup>a</sup>      | 303   | 59.08  | 136.35                                       |
| M24                   | 353   | 68.83  | 158.85                                       |
| M27 <sup>a</sup>      | 459   | 89.50  | 206.55                                       |
| M30                   | 561   | 109.39                                       | 252.45                                       |

<sup>a</sup> Non-preferred sizes<sup>b</sup> Tensile stress areas are taken from BS 4190 and BS 3692

## Spacing, end and edge distances – minimum values (see Fig. 23.1)

| Nominal diameter of fastener (mm) | Diameter of clearance hole (mm) | Minimum spacing (mm) | Edge distance to rolled, sawn, planed, or machine flame cut edge (mm) | Edge distance to sheared edge or hand flame cut edge and end distance (mm) |
|-----------------------------------|---------------------------------|----------------------|---|--|
| M12                               | 14                              | 30                   | 18  | 20   |
| M16                               | 18                              | 40                   | 23  | 26   |
| M20                               | 22                              | 50                   | 28  | 31   |
| M22 <sup>a</sup>                  | 24                              | 55                   | 30  | 34   |
| M24                               | 26                              | 60                   | 33  | 37   |
| M27 <sup>a</sup>                  | 30                              | 68                   | 38  | 42   |
| M30                               | 33                              | 75                   | 42  | 47   |

<sup>a</sup> Non-preferred size

## Maximum centres of fasteners

| Thickness of element (mm) | Spacing in the direction of stress (mm) | Spacing in any direction in corrosive environments (mm) |
|---------------------------|---|---|
| 5                         | 70                                      | 80  |
| 6                         | 84                                      | 96  |
| 7                         | 98                                      | 112   |
| 8                         | 112                                     | 128   |
| 9                         | 126                                     | 144   |
| 10                        | 140                                     | 160   |
| 11                        | 154                                     | 176   |
| 12                        | 168                                     | 192   |
| 13                        | 182                                     | 200   |
| 14                        | 196                                     | 200   |
| 15                        | 210                                     | 200   |



## Maximum edge distances (1)

| BS 4360<br>grade | Thickness<br>less than or<br>equal to (mm) | $p_y$ (N/mm <sup>2</sup> ) | $\varepsilon = \left(\frac{275}{p_y}\right)^{1/2}$ | $11t\varepsilon^a$ |
|------------------|--|----------------------------|--|--------------------|
| 43<br>A, B & C   | 16   | 275                        | 1.0  | 11t                |
|                  | 40   | 265                        | 1.02   | 11.21t             |
|                  | 63   | 255                        | 1.04   | 11.44t             |
|                  | 80   | 245                        | 1.06   | 11.65t             |
|                  | 100  | 235                        | 1.08   | 11.90t             |
| 50<br>B & C      | 16   | 355                        | 0.88   | 9.68t              |
|                  | 40   | 345                        | 0.89   | 9.79t              |
|                  | 63   | 335                        | 0.91   | 10.0t              |
|                  | 80   | 325                        | 0.92   | 10.12t             |
|                  | 100  | 315                        | 0.93   | 10.28t             |
| 55<br>C          | 16   | 450                        | 0.78   | 8.58t              |
|                  | 25   | 430                        | 0.80   | 8.8t               |
|                  | 40   | 415                        | 0.81   | 8.95t              |
|                  | 63   | 400                        | 0.83   | 9.13t              |


<sup>a</sup> This rule does not apply to fasteners interconnecting the components of back-to-back tension members  
This table is expanded in the next table (Maximum edge distances (2))

## Maximum edge distances (2)

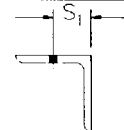
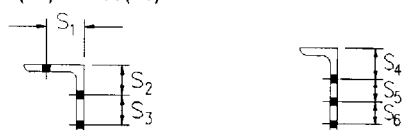
| Thickness of element $t$ (mm) | Corrosive environment<br>$40 \text{ mm} + 4t$<br>(mm) | Steel grade 43<br>A, B & C<br>$\varepsilon = 11t\varepsilon$<br>(mm) | Steel grade 50<br>B & C<br>$\varepsilon = 11t\varepsilon$<br>(mm) | Steel grade 55<br>C<br>$\varepsilon = 11t\varepsilon$<br>(mm) |
|-------------------------------|---|--|---|---|
| 5                             | 60 <sup>a</sup>                                       | 55 <sup>a</sup>  | 48 <sup>a</sup>   | 42 <sup>a</sup>   |
| 6                             | 64 <sup>a</sup>                                       | 66   | 58 <sup>a</sup>   | 51 <sup>a</sup>   |
| 7                             | 68 <sup>a</sup>                                       | 77   | 67 <sup>a</sup>   | 60 <sup>a</sup>   |
| 8                             | 72 <sup>a</sup>                                       | 88   | 77  | 68 <sup>a</sup>   |
| 9                             | 76  | 99   | 87  | 77  |
| 10                            | 80  | 110  | 96  | 85  |
| 11                            | 84  | 121  | 106   | 94  |
| 12                            | 88  | 132  | 116   | 103   |
| 13                            | 92  | 143  | 125   | 111   |
| 14                            | 96  | 154  | 135   | 120   |
| 15                            | 100   | 165  | 145   | 128   |
| 16                            | 104   | 176  | 154   | 137   |
| 20                            | 120   | 224  | 196   | 176   |
| 25                            | 140   | 280  | 245   | 220   |
| 30                            | 160   | 336  | 294   | 267   |
| 35                            | 180   | 392  | 343   | 312   |
| 40                            | 200   | 448  | 392   | 356   |
| 45                            | 220   | 515  | 445   | 411   |
| 50                            | 240   | 572  | 501   | 457   |
| 55                            | 260   | 629  | 551   | 502   |
| 60                            | 280   | 686  | 601   | 548   |
| 65                            | 300   | 757  | 657   |   |
| 70                            | 320   | 816  | 708   |   |
| 75                            | 340   | 874  | 759   |   |

<sup>a</sup> Use the lesser values for the appropriate grade of steel

Back marks in channel flanges

| RSC   | Nominal flange width (mm) | Back mark (mm) | Edge dist. (mm) | Recommended diameter (mm) |
|---|---------------------------|----------------|-----------------|---------------------------|
|  | 102                       | 55             | 47              | 24                        |
|   | 89                        | 55             | 34              | 20                        |
|   | 76                        | 45             | 31              | 20                        |
|   | 64                        | 35             | 29              | 16                        |
|   | 51                        | 30             | 21              | 10                        |
|   | 38                        | 22             | —               | —                         |

Back marks in angles

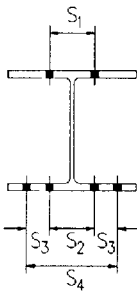
| Nominal leg (mm) | S <sub>1</sub> (mm)   | S <sub>2</sub> (mm) | S <sub>3</sub> (mm)   | S <sub>4</sub> (mm) | S <sub>5</sub> (mm) | S <sub>6</sub> (mm) | Nominal leg (mm) | S <sub>1</sub> (mm) |
|------------------|---|---------------------|---|---------------------|---------------------|---------------------|------------------|---------------------|
| 250              |  | 75(30)              | 75(30)  | 55(20)              | 55(20)              | 55(20)              | 75               | 45(20)              |
| 200              |   |                     |   |                     |                     |                     | 70               | 40(20)              |
| 150              |   |                     |   |                     |                     |                     | 65               | 35(20)              |
| 125              |   |                     |   |                     |                     |                     | 60               | 35(16)              |
| 120              |   |                     |   |                     |                     |                     | 50               | 28(12)              |
| 100              |   |                     |   |                     |                     |                     | 45               | 25                  |
| 90               | 40  | 23                  |  | 20                  |                     |                     |                  |                     |
| 80               | 30  | 15                  |   |                     |                     |                     |                  |                     |

Maximum recommended bolt sizes are given in brackets

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Cross centres through flanges

| Flange width (mm) | Minimum for accessibility (mm) | Maximum for edge dist. (mm) | S <sub>1</sub> (mm) | S <sub>2</sub> (mm) | S <sub>3</sub> (mm) | S <sub>4</sub> (mm) |
|-------------------|--------------------------------|-----------------------------|---------------------|---------------------|---------------------|---------------------|
| <i>Joists</i>     |                                |                             |                     |                     |                     |                     |
| 44                | 27 (5)                         | 30                          | 30                  |                     |                     |                     |
| 64                | 38 (10)                        | 39                          | 40                  |                     |                     |                     |
| 76                | 48 (10)                        | 51                          | 48                  |                     |                     |                     |
| 89                | 54 (12)                        | 59                          | 56                  |                     |                     |                     |
| 102               | 60 (16)                        | 62                          | 60                  |                     |                     |                     |
| 114               | 66 (16)                        | 74                          | 70                  |                     |                     |                     |
| 127               | 72 (20)                        | 77                          | 75                  |                     |                     |                     |
| 152               | 75 (20)                        | 102                         | 90                  |                     |                     |                     |
| 203               | 91 (24)                        | 143                         | 140                 |                     |                     |                     |
| <i>UCs</i>        |                                |                             |                     |                     |                     |                     |
| 152               | 65 (24)                        | 92                          | 90                  |                     |                     |                     |
| 203               | 75 (24)                        | 143                         | 140                 |                     |                     |                     |
| 254               | 87 (24)                        | 194                         | 140                 |                     |                     |                     |
| 305               | 100 (24)                       | 245                         | 140                 | 120 (24)            | 60 (24)             | 240 (24)            |
| 368               | 88 (24)                        | 308                         | 140                 | 140 (24)            | 75 (24)             | 290 (24)            |
| 406               | 120 (24)                       | 346                         | 140                 | 140 (24)            | 75 (24)             | 290 (24)            |
| <i>UBs</i>        |                                |                             |                     |                     |                     |                     |
| 102               | 50 (16)                        | 62                          | 54                  |                     |                     |                     |
| 127               | 62 (20)                        | 77                          | 70                  |                     |                     |                     |
| 133               | 57 (20)                        | 83                          | 70                  |                     |                     |                     |
| 140               | 69 (24)                        | 80                          | 70                  |                     |                     |                     |
| 146               | 64 (24)                        | 86                          | 70                  |                     |                     |                     |
| 152               | 73 (24)                        | 92                          | 90                  |                     |                     |                     |
| 165               | 67 (24)                        | 105                         | 90                  |                     |                     |                     |
| 171               | 72 (24)                        | 111                         | 90                  |                     |                     |                     |
| 178               | 72 (24)                        | 118                         | 90                  |                     |                     |                     |
| 191               | 74 (24)                        | 131                         | 90                  |                     |                     |                     |
| 210               | 80 (24)                        | 150                         | 140                 |                     |                     |                     |
| 229               | 80 (24)                        | 169                         | 140                 |                     |                     |                     |
| 254               | 87 (24)                        | 194                         | 140                 |                     |                     |                     |
| 267               | 91 (24)                        | 207                         | 140                 | 90 (20)             | 50 (20)             | 190 (20)            |
| 292               | 94 (24)                        | 232                         | 140                 | 100 (24)            | 60 (24)             | 220 (24)            |
| 305               | 100 (24)                       | 245                         | 140                 | 120 (24)            | 60 (24)             | 240 (24)            |
| 419               | 112 (24)                       | 359                         | 140                 | 140 (24)            | 75 (24)             | 290 (24)            |



Maximum bolt diameters for dimensions shown are given in brackets



Grade 4.6 bolts – threads excluded from shear plane  
Single shear and bearing – grade 43 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 160 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |      |      |       |   |      | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|-------------------------------|------------------------------------|--|------|------|-------|---|------|-----------------------------|
|                       |                               |                                    | Plate thickness, $t$ (mm)                    |      |      |       |   |      |                             |
|                       |                               |                                    | 5  | 6    | 7    | 8     | 9 | 10   |                             |
| M12                   | 113.1                         | 18.10                              | —  | —    | —    | —     | — | 3.28 |                             |
| M16                   | 201.1                         | 32.18                              | —  | —    | —    | —     | — | 4.37 |                             |
| M20                   | 314.2                         | 50.27                              | 46.0   | —    | —    | —     | — | 5.46 |                             |
| M22 <sup>a</sup>      | 380.1                         | 60.82                              | 50.6   | 60.7 | —    | —     | — | 6.01 |                             |
| M24                   | 452.39                        | 72.38                              | 55.2   | 66.2 | —    | —     | — | 6.56 |                             |
| M27 <sup>a</sup>      | 572.56                        | 91.61                              | 61.1   | 74.5 | 86.9 | —     | — | 7.38 |                             |
| M30                   | 706.86                        | 113.1                              | 69.0   | 82.8 | 96.6 | 110.4 | — | 8.20 |                             |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 4.6 bolts – threads excluded from shear plane  
Double shear and bearing – grade 43 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 2 × 160 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |      |      |       |       |       | $t$ (mm) for $P_s = P_{bb}$ |       |       |       |
|-----------------------|-------------------------------|--|--|------|------|-------|-------|-------|-----------------------------|-------|-------|-------|
|                       |                               |  | Plate thickness, $t$ (mm)                    |      |      |       |       |       |                             |       |       |       |
|                       |                               |  | 5  | 6    | 7    | 8     | 9     | 10    | 11                          | 12    | 15    |       |
| M12                   | 113.1                         | 36.20                                  | 27.6   | 33.1 | —    | —     | —     | —     | —                           | —     | —     | 6.56  |
| M16                   | 201.1                         | 64.36                                  | 36.8   | 44.2 | 51.5 | 58.9  | —     | —     | —                           | —     | —     | 8.74  |
| M20                   | 314.2                         | 100.54                                 | 46.0   | 55.2 | 64.4 | 73.6  | 82.8  | —     | —                           | —     | —     | 10.93 |
| M22 <sup>a</sup>      | 380.1                         | 121.64                                 | 50.6   | 60.7 | 70.8 | 80.9  | 91.1  | 101.2 | 111.3                       | 121.4 | —     | 12.02 |
| M24                   | 452.39                        | 144.76                                 | 55.2   | 66.2 | 77.3 | 88.3  | 99.4  | 110.4 | 121.4                       | 132.5 | —     | 13.11 |
| M27 <sup>a</sup>      | 572.56                        | 183.22                                 | 61.1   | 74.5 | 86.9 | 99.4  | 111.8 | 124.2 | 136.6                       | 149.0 | —     | 14.75 |
| M30                   | 706.86                        | 226.20                                 | 69.0   | 82.8 | 96.6 | 110.4 | 124.2 | 137.9 | 151.8                       | 165.5 | 206.9 | 16.39 |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 8.8 bolts – threads in shear plane  
Single shear and bearing – grade 43 steel

| Nominal diameter (mm) | Tensile area (mm <sup>2</sup> ) | $P_s$ @ 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |      |      |       |       |       |       |       |       |       |       |       |  | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|---------------------------------|------------------------------------|--|------|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|-----------------------------|
|                       |                                 |                                    | Plate thickness, $t$ (mm)                    |      |      |       |       |       |       |       |       |       |       |       |  |                             |
|                       |                                 |                                    | 5  | 6    | 7    | 8     | 9     | 10    | 11    | 12    | 13    | 14    | 15    |       |  |                             |
| M12                   | 84.3                            | 31.6                               | 27.6   | —    | —    | —     | —     | —     | —     | —     | —     | —     | —     | 5.73  |  |                             |
| M16                   | 157                             | 58.9                               | 36.8   | 44.2 | 51.5 | 58.9  | —     | —     | —     | —     | —     | —     | —     | 8.00  |  |                             |
| M20                   | 245                             | 91.9                               | 46.0   | 55.2 | 64.4 | 73.6  | 82.8  | —     | —     | —     | —     | —     | —     | 9.99  |  |                             |
| M22 <sup>a</sup>      | 303                             | 113.6                              | 50.6   | 60.7 | 70.8 | 80.9  | 91.1  | 101.2 | 111.3 | —     | —     | —     | —     | 11.23 |  |                             |
| M24                   | 353                             | 132.4                              | 55.2   | 66.2 | 77.3 | 88.3  | 99.4  | 110.4 | 121.4 | —     | —     | —     | —     | 11.99 |  |                             |
| M27 <sup>a</sup>      | 459                             | 172.1                              | 62.1   | 74.5 | 86.9 | 99.4  | 111.8 | 124.2 | 136.6 | 149.0 | 161.5 | —     | —     | 13.86 |  |                             |
| M30                   | 561                             | 210.4                              | 69.0   | 82.8 | 96.6 | 110.4 | 124.2 | 137.9 | 151.7 | 165.5 | 179.3 | 193.1 | 206.9 | 15.25 |  |                             |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 8.8 bolts – threads in shear plane  
Double shear and bearing – grade 43 steel

| Nominal diameter (mm) | $P_s$ @ 2 × 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |      |      |       |       |       |       |       |       |       |       |       |      | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|--|--|------|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|-----------------------------|
|                       |  | Plate thickness, $t$ (mm)                    |      |      |       |       |       |       |       |       |       |       |       |      |                             |
|                       |  | 5  | 6    | 7    | 8     | 9     | 10    | 12    | 15    | 18    | 20    | 25    | 30    |      |                             |
| M12                   | 63.2                                   | 27.6   | 33.1 | 38.6 | 44.1  | 49.6  | 55.2  | —     | —     | —     | —     | —     | —     | 11.4 |                             |
| M16                   | 117.7                                  | 36.8   | 44.2 | 51.5 | 58.9  | 66.3  | 73.6  | 88.3  | 110.4 | —     | —     | —     | —     | 16.0 |                             |
| M20                   | 183.7                                  | 46.0   | 55.2 | 64.4 | 73.6  | 82.8  | 92.0  | 110.4 | 138.0 | 165.5 | —     | —     | —     | 19.9 |                             |
| M22 <sup>a</sup>      | 227.3                                  | 50.6   | 60.7 | 70.8 | 80.9  | 91.1  | 101.2 | 121.4 | 151.8 | 182.1 | 202.4 | —     | —     | 22.4 |                             |
| M24                   | 264.8                                  | 55.2   | 66.2 | 77.3 | 88.3  | 99.4  | 110.4 | 132.5 | 165.6 | 198.8 | 220.8 | —     | —     | 23.9 |                             |
| M27 <sup>a</sup>      | 344.3                                  | 61.1   | 74.5 | 86.9 | 99.4  | 111.8 | 124.2 | 149.0 | 186.3 | 223.4 | 248.4 | 310.5 | —     | 27.7 |                             |
| M30                   | 420.8                                  | 69.0   | 82.8 | 96.6 | 110.4 | 124.2 | 137.9 | 165.5 | 206.9 | 248.4 | 276.0 | 344.9 | 413.9 | 30.5 |                             |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 8.8 bolts – threads in shear plane  
Single shear and bearing – grade 50 steel

| Nominal diameter (mm) | Tensile area (mm <sup>2</sup> ) | P <sub>s</sub> (a) 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 550 N/mm <sup>2</sup> |      |       |       |       |       |       |       |   |       | t (mm) for P <sub>s</sub> = P <sub>bb</sub> |
|-----------------------|---------------------------------|---|--|------|-------|-------|-------|-------|-------|-------|---|-------|---|
|                       |                                 |   | Plate thickness, t (mm)                      |      |       |       |       |       |       |       |   |       |   |
|                       |                                 |   | 5  | 6    | 7     | 8     | 9     | 10    | 11    | 12    |   |       |   |
| M12                   | 84.3                            | 31.6  | —  | —    | —     | —     | —     | —     | —     | —     | — | 4.79  |   |
| M16                   | 157                             | 58.9  | 44.0   | 52.8 | —     | —     | —     | —     | —     | —     | — | 6.69  |   |
| M20                   | 245                             | 91.9  | 55.0   | 66.0 | 77.0  | 88.0  | —     | —     | —     | —     | — | 8.35  |   |
| M22 <sup>a</sup>      | 303                             | 113.6   | 60.5   | 72.6 | 84.7  | 96.8  | 108.9 | —     | —     | —     | — | 9.39  |   |
| M24                   | 353                             | 132.4   | 66.0   | 79.2 | 92.4  | 105.6 | 118.8 | 132.0 | —     | —     | — | 10.03 |   |
| M27 <sup>a</sup>      | 459                             | 172.1   | 74.3   | 89.1 | 104.0 | 118.8 | 133.7 | 148.5 | 163.4 | —     | — | 11.59 |   |
| M30                   | 561                             | 210.4   | 82.5   | 99.0 | 115.5 | 132.0 | 148.5 | 165.0 | 181.5 | 198.0 | — | 12.75 |   |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads in shear plane  
Double shear and bearing – grade 50 steel

| Nominal diameter (mm) | P <sub>s</sub> (a) 2 x 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 550 N/mm <sup>2</sup> |      |       |       |       |       |       |       |       |       | t (mm) for P <sub>s</sub> = P <sub>bb</sub> |    |      |
|-----------------------|---|--|------|-------|-------|-------|-------|-------|-------|-------|-------|---|----|------|
|                       |   | Plate thickness, t (mm)                      |      |       |       |       |       |       |       |       |       |   |    |      |
|                       |   |  | 5    | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 18    | 20  | 25 |      |
| M12                   | 63.2  | 33.0   | 39.6 | 46.2  | 59.4  | —     | —     | —     | —     | —     | —     | —   | —  | 9.5  |
| M16                   | 117.7   | 44.0   | 52.8 | 61.6  | 79.2  | 88.0  | 105.6 | —     | —     | —     | —     | —   | —  | 13.3 |
| M20                   | 183.7   | 55.0   | 66.0 | 77.0  | 88.0  | 99.0  | 110.0 | 132.0 | 165.0 | —     | —     | —   | —  | 16.7 |
| M22 <sup>a</sup>      | 227.3   | 60.5   | 72.6 | 84.7  | 96.8  | 108.9 | 121.0 | 145.2 | 181.5 | 217.8 | —     | —   | —  | 18.7 |
| M24                   | 264.8   | 66.0   | 79.2 | 92.4  | 105.6 | 118.8 | 132.0 | 158.4 | 198.0 | 237.6 | 264.0 | —   | —  | 20.0 |
| M27 <sup>a</sup>      | 344.3   | 74.3   | 89.1 | 104.0 | 118.8 | 133.7 | 148.5 | 178.2 | 222.8 | 267.3 | 297.0 | —   | —  | 23.1 |
| M30                   | 420.8   | 82.5   | 99.0 | 115.0 | 132.0 | 148.5 | 165.0 | 198.0 | 247.5 | 297.0 | 330.0 | 412.5                                       | —  | 25.5 |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d



Grade 8.8 bolts – threads in shear plane  
Single shear and bearing – grade 55 steel

| Nominal diameter (mm) | Tensile area (mm <sup>2</sup> ) | $P_s$ @ 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 650 N/mm <sup>2</sup> |       |       |       |       |       |   |   |   |   | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|---------------------------------|------------------------------------|--|-------|-------|-------|-------|-------|---|---|---|---|-----------------------------|
|                       |                                 |                                    | Plate thickness, $t$ (mm)                    |       |       |       |       |       |   |   |   |   |                             |
|                       |                                 |                                    | 5  | 6     | 7     | 8     | 9     | 10    |   |   |   |   |                             |
| M12                   | 84.3                            | 31.6                               | —  | —     | —     | —     | —     | —     | — | — | — | — | 4.0                         |
| M16                   | 157                             | 56.9                               | 52.0   | —     | —     | —     | —     | —     | — | — | — | — | 5.6                         |
| M20                   | 245                             | 91.9                               | 65.0   | 78.0  | 91.0  | —     | —     | —     | — | — | — | — | 7.1                         |
| M22 <sup>a</sup>      | 303                             | 113.6                              | 71.5   | 85.8  | 100.1 | —     | —     | —     | — | — | — | — | 7.9                         |
| M24                   | 353                             | 132.4                              | 78.0   | 93.6  | 109.1 | 124.7 | —     | —     | — | — | — | — | 8.5                         |
| M27 <sup>a</sup>      | 459                             | 172.1                              | 87.7   | 105.3 | 122.8 | 140.4 | 157.9 | —     | — | — | — | — | 9.8                         |
| M30                   | 561                             | 210.4                              | 97.5   | 117.0 | 136.5 | 156.0 | 175.5 | 195.0 | — | — | — | — | 10.8                        |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads in shear plane  
Double shear and bearing – grade 55 steel

| Nominal diameter (mm) | $P_s$ @ 2 x 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 650 N/mm <sup>2</sup> |       |       |       |       |       |       |       |       |       | $t$ (mm) for $P_s = P_{bb}$ |   |      |
|-----------------------|--|--|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----------------------------|---|------|
|                       |  | Plate thickness, $t$ (mm)                    |       |       |       |       |       |       |       |       |       |                             |   |      |
|                       |  | 5  | 6     | 7     | 8     | 9     | 10    | 12    | 15    | 18    | 20    |                             |   |      |
| M12                   | 63.2                                   | 39.0   | 46.8  | 54.6  | 62.4  | —     | —     | —     | —     | —     | —     | —                           | — | 8.1  |
| M16                   | 117.7                                  | 52.0   | 62.4  | 72.8  | 83.2  | 93.6  | 104.0 | —     | —     | —     | —     | —                           | — | 11.3 |
| M20                   | 183.7                                  | 65.0   | 78.0  | 91.0  | 103.9 | 116.9 | 129.9 | 155.9 | —     | —     | —     | —                           | — | 14.1 |
| M22 <sup>a</sup>      | 227.3                                  | 71.5   | 85.8  | 100.1 | 114.3 | 128.6 | 142.9 | 171.5 | 214.5 | —     | —     | —                           | — | 15.9 |
| M24                   | 264.8                                  | 78.0   | 93.6  | 109.1 | 124.7 | 140.3 | 155.9 | 187.1 | 234.0 | —     | —     | —                           | — | 16.9 |
| M27 <sup>a</sup>      | 344.3                                  | 87.7   | 105.3 | 122.8 | 140.4 | 157.9 | 175.5 | 210.6 | 263.2 | 315.8 | —     | —                           | — | 19.6 |
| M30                   | 420.8                                  | 97.5   | 117.0 | 136.5 | 156.0 | 175.5 | 195.0 | 234.0 | 292.5 | 315.0 | 390.0 | —                           | — | 21.5 |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads excluded from shear plane  
Single shear and bearing – grade 43 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |      |      |       |       |       |       |       |       |       |   |   |   |   |   | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|-------------------------------|------------------------------------|--|------|------|-------|-------|-------|-------|-------|-------|-------|---|---|---|---|---|-----------------------------|
|                       |                               |                                    | Plate thickness, $t$ (mm)                    |      |      |       |       |       |       |       |       |       |   |   |   |   |   |                             |
|                       |                               |                                    | 5  | 6    | 7    | 8     | 9     | 10    | 12    | 15    | 18    |       |   |   |   |   |   |                             |
| M12                   | 113.1                         | 42.41                              | 27.6   | 33.1 | 38.6 | —     | —     | —     | —     | —     | —     | —     | — | — | — | — | — | 7.68                        |
| M16                   | 201.1                         | 75.41                              | 36.8   | 44.1 | 51.5 | 58.9  | 66.3  | 73.6  | 73.6  | —     | —     | —     | — | — | — | — | — | 10.25                       |
| M20                   | 314.2                         | 117.81                             | 46.0   | 55.2 | 64.4 | 73.6  | 80.9  | 82.8  | 92.0  | 110.4 | —     | —     | — | — | — | — | — | 12.81                       |
| M22 <sup>a</sup>      | 380.1                         | 142.54                             | 50.6   | 60.7 | 70.8 | 80.9  | 88.3  | 91.1  | 101.2 | 121.4 | —     | —     | — | — | — | — | — | 14.08                       |
| M24                   | 452.39                        | 169.64                             | 55.2   | 66.2 | 77.3 | 88.3  | 99.4  | 99.4  | 110.4 | 132.5 | 165.6 | —     | — | — | — | — | — | 15.37                       |
| M27 <sup>a</sup>      | 572.56                        | 214.71                             | 62.1   | 74.5 | 86.9 | 99.4  | 111.8 | 111.8 | 124.2 | 149.0 | 186.3 | —     | — | — | — | — | — | 17.29                       |
| M30                   | 706.86                        | 265.07                             | 69.0   | 82.8 | 96.6 | 110.4 | 124.2 | 124.2 | 137.9 | 165.5 | 206.9 | 248.4 | — | — | — | — | — | 19.21                       |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads excluded from shear plane  
Double shear and bearing – grade 43 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 2 × 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 460 N/mm <sup>2</sup> |       |       |       |       |       |       |       |       |       |     |   |   |   |   | $t$ (mm) for $P_s = P_{bb}$ |
|-----------------------|-------------------------------|--|--|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----|---|---|---|---|-----------------------------|
|                       |                               |  | Plate thickness, $t$ (mm)                    |       |       |       |       |       |       |       |       |       |     |   |   |   |   |                             |
|                       |                               |  | 5  | 10    | 12    | 15    | 18    | 20    | 25    | 30    | 35    | 37    |     |   |   |   |   |                             |
| M12                   | 113.1                         | 84.8                                   | 27.6   | 55.2  | 66.2  | 82.8  | —     | —     | —     | —     | —     | —     | —   | — | — | — | — | 15.36                       |
| M16                   | 201.1                         | 150.8                                  | 36.8   | 73.6  | 88.3  | 110.4 | 132.4 | 147.2 | 147.2 | —     | —     | —     | —   | — | — | — | — | 20.50                       |
| M20                   | 314.2                         | 235.6                                  | 46.0   | 92.0  | 110.4 | 138.0 | 165.6 | 184.0 | 184.0 | 230.0 | —     | —     | —   | — | — | — | — | 25.62                       |
| M22 <sup>a</sup>      | 380.1                         | 285.1                                  | 50.6   | 110.2 | 121.4 | 151.8 | 182.1 | 202.4 | 202.4 | 253.0 | —     | —     | —   | — | — | — | — | 28.16                       |
| M24                   | 452.39                        | 339.2                                  | 55.2   | 110.4 | 132.5 | 165.6 | 198.7 | 220.8 | 220.8 | 276.0 | 331.2 | —     | —   | — | — | — | — | 30.74                       |
| M27 <sup>a</sup>      | 522.56                        | 429.4                                  | 62.1   | 124.2 | 149.0 | 186.3 | 223.4 | 248.4 | 248.4 | 310.5 | 372.6 | —     | —   | — | — | — | — | 34.58                       |
| M30                   | 706.86                        | 530.1                                  | 69.0   | 137.9 | 165.5 | 206.9 | 248.4 | 276.0 | 276.0 | 344.9 | 413.9 | 483.0 | 510 | — | — | — | — | 38.42                       |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads excluded from shear plane  
Single shear and bearing – grade 50 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 550 N/mm <sup>2</sup> |      |       |       |       |       |    |       |   |   |   | $t$ (mm) for $P_s = P_{bb}$ |       |
|-----------------------|-------------------------------|------------------------------------|--|------|-------|-------|-------|-------|----|-------|---|---|---|-----------------------------|-------|
|                       |                               |                                    | Plate thickness, $t$ (mm)                    |      |       |       |       |       |    |       |   |   |   |                             |       |
|                       |                               |                                    | 5  | 6    | 7     | 8     | 9     | 10    | 12 | 15    |   |   |   |                             |       |
| M12                   | 113.1                         | 42.41                              | 33   | 39.6 | —     | —     | —     | —     | —  | —     | — | — | — | —                           | 6.43  |
| M16                   | 201.1                         | 75.41                              | 44.0   | 52.8 | 61.6  | 70.4  | —     | —     | —  | —     | — | — | — | —                           | 8.57  |
| M20                   | 314.2                         | 117.81                             | 55.0   | 66.0 | 77.0  | 88.0  | 99.0  | —     | —  | 110.0 | — | — | — | —                           | 10.71 |
| M22 <sup>a</sup>      | 380.1                         | 142.58                             | 60.5   | 72.6 | 84.7  | 96.8  | 108.9 | 121.0 | —  | —     | — | — | — | —                           | 11.78 |
| M24                   | 452.39                        | 169.64                             | 66.0   | 79.2 | 92.4  | 105.6 | 118.9 | 132.0 | —  | —     | — | — | — | —                           | 12.85 |
| M27 <sup>a</sup>      | 572.56                        | 214.71                             | 74.3   | 89.1 | 104.0 | 118.8 | 133.7 | 148.5 | —  | —     | — | — | — | —                           | 14.46 |
| M30                   | 706.86                        | 265.07                             | 82.5   | 99.0 | 115.5 | 132.0 | 148.5 | 165.0 | —  | —     | — | — | — | —                           | 16.06 |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 8.8 bolts – threads excluded from shear plane  
Double shear and bearing – grade 50 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | $P_s$ @ 2 × 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 550 N/mm <sup>2</sup> |       |       |       |       |       |    |       |   |   |   | $t$ (mm) for $P_s = P_{bb}$ |       |
|-----------------------|-------------------------------|--|--|-------|-------|-------|-------|-------|----|-------|---|---|---|-----------------------------|-------|
|                       |                               |  | Plate thickness, $t$ (mm)                    |       |       |       |       |       |    |       |   |   |   |                             |       |
|                       |                               |  | 5  | 10    | 12    | 15    | 18    | 20    | 25 | 30    |   |   |   |                             |       |
| M12                   | 113.1                         | 84.8                                   | 33.0   | 66.0  | 79.2  | —     | —     | —     | —  | —     | — | — | — | —                           | 12.86 |
| M16                   | 201.1                         | 150.8                                  | 44.0   | 88.0  | 105.6 | 132.0 | —     | —     | —  | —     | — | — | — | —                           | 17.14 |
| M20                   | 314.2                         | 235.6                                  | 55.0   | 110.0 | 132.0 | 165.0 | 198.0 | —     | —  | 220.0 | — | — | — | —                           | 21.42 |
| M22 <sup>a</sup>      | 380.1                         | 285.1                                  | 60.5   | 121.0 | 145.2 | 181.5 | 217.8 | 242.0 | —  | —     | — | — | — | —                           | 23.56 |
| M24                   | 452.39                        | 339.2                                  | 66.0   | 132.0 | 158.4 | 198.0 | 237.6 | 264.0 | —  | —     | — | — | — | —                           | 25.70 |
| M27 <sup>a</sup>      | 522.56                        | 429.4                                  | 74.3   | 148.5 | 178.2 | 222.8 | 267.3 | 297.0 | —  | —     | — | — | — | —                           | 28.92 |
| M30                   | 706.86                        | 530.1                                  | 82.5   | 165.0 | 198.0 | 247.5 | 297.0 | 330.0 | —  | —     | — | — | — | —                           | 32.12 |

<sup>a</sup> Non-preferred size

<sup>b</sup> End distance  $>2d$

Grade 8.8 bolts – threads excluded from shear plane  
Single shear and bearing – grade 55 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | P <sub>s</sub> @ 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 650 N/mm <sup>2</sup> |       |       |       |       |       |       |   |   |   | t (mm) for P <sub>s</sub> = P <sub>bb</sub> |
|-----------------------|-------------------------------|---|--|-------|-------|-------|-------|-------|-------|---|---|---|---|
|                       |                               |   | Plate thickness, t (mm)                      |       |       |       |       |       |       |   |   |   |   |
|                       |                               |   | 5  | 6     | 7     | 8     | 9     | 10    | 12    |   |   |   |   |
| M12                   | 113.1                         | 42.41                                       | 39.0   | —     | —     | —     | —     | —     | —     | — | — | — | 5.44  |
| M16                   | 201.1                         | 75.41                                       | 52.0   | 62.4  | 72.8  | —     | —     | —     | —     | — | — | — | 7.25  |
| M20                   | 314.2                         | 117.81                                      | 65.0   | 78.0  | 91.0  | 103.9 | 116.9 | —     | —     | — | — | — | 9.06  |
| M22 <sup>a</sup>      | 380.1                         | 142.58                                      | 71.5   | 85.8  | 100.1 | 114.3 | 128.6 | —     | —     | — | — | — | 9.97  |
| M24                   | 452.39                        | 169.64                                      | 78.0   | 93.6  | 109.1 | 124.7 | 140.3 | 155.9 | —     | — | — | — | 10.87                                       |
| M27 <sup>a</sup>      | 572.56                        | 214.71                                      | 87.7   | 105.3 | 122.8 | 140.4 | 157.9 | 175.5 | 210.6 | — | — | — | 12.24                                       |
| M30                   | 706.86                        | 265.07                                      | 97.5   | 117.0 | 136.5 | 156.0 | 175.5 | 195.0 | 234.0 | — | — | — | 13.59                                       |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Grade 8.8 bolts – threads excluded from shear plane  
Double shear and bearing – grade 55 steel

| Nominal diameter (mm) | Shank area (mm <sup>2</sup> ) | P <sub>s</sub> @ 2 × 375 N/mm <sup>2</sup> (kN) | Bearing <sup>b</sup> @ 650 N/mm <sup>2</sup> |       |       |       |       |       |       |   |   |   | t (mm) for P <sub>s</sub> = P <sub>bb</sub> |
|-----------------------|-------------------------------|---|--|-------|-------|-------|-------|-------|-------|---|---|---|---|
|                       |                               |   | Plate thickness, t (mm)                      |       |       |       |       |       |       |   |   |   |   |
|                       |                               |   | 5  | 10    | 12    | 15    | 18    | 20    | 25    |   |   |   |   |
| M12                   | 113.1                         | 84.8  | 39.0   | 78.0  | —     | —     | —     | —     | —     | — | — | — | 10.88                                       |
| M16                   | 201.1                         | 150.8   | 52.0   | 104.0 | 124.8 | —     | —     | —     | —     | — | — | — | 14.50                                       |
| M20                   | 314.2                         | 235.6   | 65.0   | 129.9 | 155.9 | 195.0 | 234.0 | —     | —     | — | — | — | 18.12                                       |
| M22 <sup>a</sup>      | 380.1                         | 285.1   | 71.5   | 142.9 | 171.5 | 214.5 | 257.4 | —     | —     | — | — | — | 19.94                                       |
| M24                   | 452.39                        | 339.2   | 78.0   | 155.9 | 187.1 | 234.0 | 280.8 | 312.0 | —     | — | — | — | 21.74                                       |
| M27 <sup>a</sup>      | 572.56                        | 429.4   | 87.7   | 175.5 | 210.6 | 263.2 | 315.9 | 351.0 | 24.48 | — | — | — | 24.48                                       |
| M30                   | 706.86                        | 530.1   | 97.5   | 195.0 | 234.0 | 292.5 | 351.0 | 390.0 | 487.5 | — | — | — | 27.18                                       |

<sup>a</sup> Non-preferred size  
<sup>b</sup> End distance >2d

Bolts to BS 4395: Part 1  
Slip resistance

| Nominal diameter (mm) | Proof load (kN) | $P_{sL}$ (kN) when $\mu = 0.45$ |  |                                |
|-----------------------|-----------------|---------------------------------|--|--------------------------------|
|                       |                 | Clearance holes<br>$K_s = 1.0$  | Short slot holes, etc.<br>$K_s = 0.85$ | Long slot holes<br>$K_s = 0.6$ |
| M12 <sup>a</sup>      | 49.4            | 24.5                            | 20.7                                   | 14.6                           |
| M16                   | 92.1            | 45.5                            | 38.7                                   | 27.3                           |
| M20                   | 144             | 71.2                            | 60.5                                   | 42.7                           |
| M22                   | 177             | 87.6                            | 74.4                                   | 52.5                           |
| M24                   | 207             | 102.4                           | 87.1                                   | 61.4                           |
| M27                   | 234             | 115.8                           | 98.5                                   | 69.5                           |
| M30                   | 286             | 141.5                           | 120.3                                  | 84.9                           |

<sup>a</sup> Non-preferred sizeBolts to BS 4395: Part 2  
Shear connections only – external tension not permitted  
Slip resistance

| Nominal diameter (mm) | Proof load (kN) | Minimum shank tension (kN) | $P_{sL}$ (kN) when $0.45 < \mu < 0.55$ |              |  |              |                                |              |
|-----------------------|-----------------|----------------------------|--|--------------|--|--------------|--------------------------------|--------------|
|                       |                 |                            | Clearance holes<br>$K_s = 1.0$         |              | Short slot holes, etc.<br>$K_s = 0.85$ |              | Long slot holes<br>$K_s = 0.6$ |              |
|                       |                 |                            | $\mu = 0.45$                           | $\mu = 0.55$ | $\mu = 0.45$                           | $\mu = 0.55$ | $\mu = 0.45$                   | $\mu = 0.55$ |
| M16                   | 122.2           | 103.8                      | 51.4                                   | 62.8         | 43.7                                   | 53.4         | 30.8                           | 37.7         |
| M20                   | 190.4           | 161.8                      | 80.1                                   | 97.9         | 68.0                                   | 83.2         | 48.0                           | 58.7         |
| M22                   | 235.5           | 200.1                      | 99.0                                   | 121.1        | 84.2                                   | 102.9        | 59.4                           | 72.6         |
| M24                   | 274.6           | 233.4                      | 115.5                                  | 141.2        | 98.2                                   | 120.0        | 69.3                           | 84.7         |
| M27                   | 356.0           | 302.6                      | 149.7                                  | 183.0        | 127.3                                  | 155.6        | 89.8                           | 109.8        |
| M30                   | 435.0           | 369.7                      | 183.0                                  | 223.6        | 155.5                                  | 190.1        | 109.8                          | 134.2        |

Bolts to BS 4395  
Maximum external tension capacity

| Nominal diameter (mm) | Part 1 (bolts general grade parallel shank) |            |
|-----------------------|---|------------|
|                       | $P_0$ (kN)                                  | $P_t$ (kN) |
| M16                   | 92.1  | 82.8       |
| M20                   | 144   | 129.6      |
| M22                   | 177   | 159.3      |
| M24                   | 207   | 186.3      |
| M27                   | 234   | 210.6      |
| M30                   | 286   | 257.4      |

Bolts to BS 4395  
 Bearing strength  
 Parallel shank fastener  
 Steel to BS 4360

| Nominal diameter (mm) | Plate thickness and steel grade |       |       |                |       |                |
|-----------------------|---------------------------------|-------|-------|----------------|-------|----------------|
|                       | Grade 43 steel                  |       |       | Grade 50       |       | Grade 55       |
|                       | 6 <sup>b</sup>                  | 8     | 10    | 6 <sup>b</sup> | 8     | 6 <sup>b</sup> |
| M12 <sup>a</sup>      | —                               | —     | —     | —              | —     | —              |
| M16                   | 79.2                            | —     | —     | 102.4          | —     | 116.1          |
| M20                   | 99.0                            | 132.0 | —     | 127.8          | —     | 145.1          |
| M22                   | 108.9                           | 145.2 | —     | 140.5          | —     | 159.7          |
| M24                   | 118.8                           | 158.4 | 198.0 | 153.3          | 204.5 | 174.5          |
| M27                   | 133.6                           | 178.2 | 222.8 | 172.5          | 230.0 | 196.0          |
| M30                   | 148.5                           | 198.0 | 247.5 | 191.7          | 255.6 | 217.8          |

These values will only apply in double shear joints in the case of Part 1 fasteners but may need checking against single shear in the case of Part 2 fasteners

<sup>a</sup> Non-preferred size

<sup>b</sup> BS 4604 recommends minimum plate thickness of  $d/2$  or 10 mm thickness whichever is the lesser

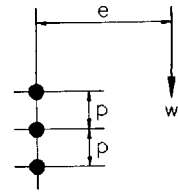
Bolts to BS 4395  
 Long joints

For fasteners where the slip resistance given in the previous tables is assessed using a slip factor of 0.45, the reduction due to long joints does not become effective until  $L_j$  is 1375 mm. When the slip factor is 0.55 the reduction is effective for all joints over 500 mm long.

Parallel shank fasteners  
 (taking  $K_s = 1.0$ ,  $\mu = 0.55$ )

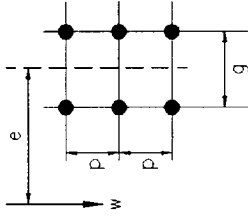
| Nominal diameter (mm) | For joints where $L_j = 500$ mm |                  |                                     |                  |
|-----------------------|---------------------------------|------------------|-------------------------------------|------------------|
|                       | Part 1 bolts general grade      |                  | Part 2 bolts higher grade           |                  |
|                       | $P_0$<br>Proof load (kN)        | $P_{sL}$<br>(kN) | $P_0$<br>Minimum shank tension (kN) | $P_{sL}$<br>(kN) |
| M16                   | 92.1                            | 55.2             | 103.8                               | 62.2             |
| M20                   | 144                             | 86.4             | 161.8                               | 97.0             |
| M22                   | 177                             | 106.2            | 200.1                               | 120.0            |
| M24                   | 207                             | 124.2            | 233.4                               | 140.0            |
| M27                   | 234                             | 140.4            | 302.6                               | 181.5            |
| M30                   | 286                             | 171.6            | 369.7                               | 221.8            |

For joints longer than 500 mm, columns 3 and 5 should be multiplied by the factor  $(5500 - L_j)/5000$



**Bolt groups**  
 One row of fasteners; fasteners in the plane of the force

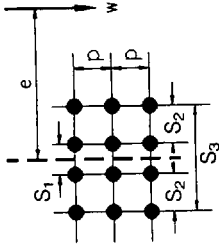
| No. of fasteners<br>in vertical row | Pitch, $p$<br>(mm) | Values of $Z_{xx}$ ( $\text{cm}^3$ ) for<br>diameter of bolt, $D$ (mm) |       |       |       |       |       |       |
|-------------------------------------|--------------------|--|-------|-------|-------|-------|-------|-------|
|                                     |                    | 12   | 16    | 20    | 22    | 24    | 27    | 30    |
| 2                                   | 70                 | 6.0  | 11.4  | 18.0  | 22.5  | 26.6  | 35.1  | 43.8  |
| 3                                   |                    | 11.9   | 22.3  | 35.0  | 43.4  | 50.8  | 66.5  | 81.9  |
| 4                                   |                    | 19.7   | 36.9  | 57.8  | 71.6  | 83.6  | 109.1 | 133.9 |
| 5                                   |                    | 29.6   | 55.2  | 86.3  | 106.9 | 124.7 | 162.5 | 199.2 |
| 6                                   |                    | 41.4   | 77.2  | 120.6 | 149.3 | 174.1 | 226.7 | 277.6 |
| 7                                   |                    | 55.1   | 102.8 | 160.6 | 198.7 | 231.7 | 301.6 | 369.2 |
| 8                                   |                    | 70.9   | 132.1 | 206.3 | 255.3 | 297.6 | 387.3 | 473.8 |
| 9                                   |                    | 88.6   | 165.1 | 257.8 | 318.9 | 371.7 | 483.6 | 591.6 |
| 2                                   |                    | 100  | 8.5   | 16.0  | 25.1  | 31.2  | 36.6  | 48.0  |
| 3                                   | 16.9               |  | 31.6  | 49.5  | 61.3  | 71.6  | 93.4  | 114.6 |
| 4                                   | 28.2               |  | 52.5  | 82.1  | 101.6 | 118.5 | 154.4 | 189.1 |
| 5                                   | 42.2               |  | 78.7  | 122.9 | 152.1 | 177.3 | 230.8 | 282.5 |
| 6                                   | 59.1               |  | 110.1 | 171.9 | 212.7 | 247.9 | 322.6 | 394.6 |
| 7                                   | 78.7               |  | 146.7 | 229.0 | 283.3 | 330.2 | 429.6 | 525.5 |
| 8                                   | 101.2              |  | 188.5 | 294.4 | 364.1 | 424.3 | 552.0 | 675.0 |
| 9                                   | 126.5              |  | 235.6 | 367.9 | 455.0 | 530.2 | 689.7 | 843.3 |



Bolt groups  
Two rows of fasteners; fasteners in the plane of the force

| No. of fasteners<br>in vertical row | Pitch, <i>p</i><br>(mm) | Gauge, <i>g</i><br>(mm) | Values of $Z_{xx}$ (cm <sup>2</sup> ) for<br>diameter of bolt, <i>D</i> (mm) |       |       |       |        |        |        |
|-------------------------------------|-------------------------|-------------------------|--|-------|-------|-------|--------|--------|--------|
|                                     |                         |                         | 12   | 16    | 20    | 22    | 24     | 27     | 30     |
| 2                                   | 70                      | 60                      | 15.7   | 29.5  | 46.5  | 57.9  | 67.9   | 89.2   | 110.3  |
| 3                                   |                         |                         | 27.8   | 52.0  | 81.7  | 101.3 | 118.4  | 154.8  | 190.4  |
| 4                                   |                         |                         | 43.5   | 81.3  | 127.2 | 157.6 | 184.1  | 240.0  | 294.5  |
| 5                                   |                         |                         | 63.1   | 117.8 | 184.2 | 228.0 | 266.1  | 346.7  | 424.8  |
| 6                                   |                         |                         | 86.7   | 161.6 | 252.6 | 312.7 | 364.6  | 474.8  | 581.4  |
| 7                                   |                         |                         | 114.2  | 212.8 | 332.5 | 411.5 | 479.7  | 624.4  | 764.2  |
| 8                                   |                         |                         | 145.6  | 271.4 | 423.9 | 524.4 | 611.3  | 795.6  | 973.4  |
| 9                                   |                         |                         | 181.0  | 337.3 | 526.7 | 651.6 | 759.5  | 988.2  | 1208.8 |
| 2                                   | 100                     | 60                      | 19.8   | 37.1  | 58.2  | 72.2  | 84.6   | 110.6  | 136.3  |
| 3                                   |                         |                         | 36.8   | 68.6  | 107.4 | 133.1 | 155.4  | 202.6  | 248.5  |
| 4                                   |                         |                         | 59.2   | 110.4 | 172.5 | 213.5 | 249.1  | 324.4  | 397.3  |
| 5                                   |                         |                         | 87.2   | 162.6 | 254.0 | 314.3 | 366.4  | 476.9  | 583.7  |
| 6                                   |                         |                         | 120.9  | 225.3 | 351.8 | 435.3 | 507.4  | 660.2  | 807.7  |
| 7                                   |                         |                         | 160.2  | 298.5 | 466.0 | 576.5 | 671.9  | 874.2  | 1069.1 |
| 8                                   |                         |                         | 205.1  | 382.2 | 596.6 | 738.0 | 860.1  | 1118.8 | 1368.1 |
| 9                                   |                         |                         | 255.7  | 476.3 | 743.5 | 919.7 | 1071.8 | 1394.0 | 1704.5 |

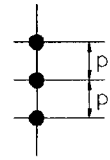




**Bolt groups**  
**Four rows of fasteners; fasteners in the plane of the force**

| No. of fasteners<br>in vertical row | Pitch, <i>p</i><br>(mm) | <i>S</i> <sub>1</sub><br>(mm) | <i>S</i> <sub>2</sub><br>(mm) | <i>S</i> <sub>3</sub><br>(mm) | Values of <i>Z</i> <sub>xx</sub> (cm <sup>2</sup> ) for<br>diameter of bolt, <i>D</i> (mm) |        |        |        |        |  |
|-------------------------------------|-------------------------|-------------------------------|-------------------------------|-------------------------------|--|--------|--------|--------|--------|--|
|                                     |                         |                               |                               |                               | 20   | 22     | 24     | 27     | 30     |  |
| 2                                   | 70                      | 120                           | 60                            | 240                           | 161.3  | 199.8  | 233.1  | 303.7  | 372.2  |  |
| 3                                   |                         |                               |                               |                               | 261.0  | 323.0  | 376.8  | 490.8  | 601.3  |  |
| 4                                   |                         |                               |                               |                               | 373.4  | 462.2  | 539.0  | 701.9  | 859.4  |  |
| 5                                   |                         |                               |                               |                               | 501.3  | 620.4  | 723.4  | 941.6  | 1152.6 |  |
| 6                                   |                         |                               |                               |                               | 647.2  | 800.8  | 933.6  | 1215.1 | 1486.9 |  |
| 7                                   |                         |                               |                               |                               | 813.0  | 1005.9 | 1172.5 | 1525.7 | 1866.6 |  |
| 8                                   |                         |                               |                               |                               | 999.8  | 1236.9 | 1441.7 | 1875.7 | 2294.4 |  |
| 9                                   |                         |                               |                               |                               | 1208.2   | 1494.7 | 1742.0 | 2266.3 | 2771.8 |  |
| 2                                   | 70                      | 120                           | 85                            | 290                           | 178.7  | 221.2  | 258.0  | 336.1  | 411.6  |  |
| 3                                   |                         |                               |                               |                               | 285.6  | 353.5  | 412.3  | 536.8  | 657.3  |  |
| 4                                   |                         |                               |                               |                               | 405.1  | 501.3  | 584.6  | 761.0  | 931.5  |  |
| 5                                   |                         |                               |                               |                               | 539.1  | 667.1  | 777.8  | 1012.3 | 1238.8 |  |
| 6                                   |                         |                               |                               |                               | 690.0  | 853.7  | 995.2  | 1295.1 | 1584.5 |  |
| 7                                   |                         |                               |                               |                               | 859.6  | 1063.5 | 1239.6 | 1612.9 | 1973.0 |  |
| 8                                   |                         |                               |                               |                               | 1049.3   | 1298.1 | 1512.9 | 1968.3 | 2407.5 |  |
| 9                                   |                         |                               |                               |                               | 1259.9   | 1558.6 | 1816.5 | 2363.1 | 2890.0 |  |
| 2                                   | 70                      | 140                           | 50                            | 240                           | 171.5  | 212.4  | 247.8  | 322.8  | 395.5  |  |
| 3                                   |                         |                               |                               |                               | 274.7  | 340.0  | 396.7  | 516.6  | 632.8  |  |
| 4                                   |                         |                               |                               |                               | 389.4  | 481.9  | 562.0  | 731.8  | 896.0  |  |
| 5                                   |                         |                               |                               |                               | 518.6  | 641.7  | 748.2  | 974.0  | 1192.1 |  |
| 6                                   |                         |                               |                               |                               | 665.2  | 823.1  | 959.6  | 1248.8 | 1528.1 |  |
| 7                                   |                         |                               |                               |                               | 831.4  | 1028.7 | 1199.1 | 1560.3 | 1908.8 |  |
| 8                                   |                         |                               |                               |                               | 1018.4   | 1260.0 | 1468.6 | 1910.7 | 2337.2 |  |
| 9                                   |                         |                               |                               |                               | 1227.1   | 1518.0 | 1769.1 | 2301.5 | 2814.8 |  |

|   |     |     |    |     |       |        |        |        |        |        |        |
|---|-----|-----|----|-----|-------|--------|--------|--------|--------|--------|--------|
| 2 | 70  | 140 | 75 | 290 | 64.3  | 119.8  | 187.3  | 231.8  | 270.3  | 352.1  | 431.1  |
| 3 |     |     |    |     | 102.1 | 190.4  | 297.5  | 368.2  | 429.4  | 559.1  | 684.5  |
| 4 |     |     |    |     | 144.0 | 268.4  | 419.4  | 518.9  | 605.1  | 787.7  | 964.1  |
| 5 |     |     |    |     | 190.6 | 355.3  | 554.9  | 686.7  | 800.5  | 1041.9 | 1275.0 |
| 6 |     |     |    |     | 242.8 | 452.5  | 706.8  | 874.5  | 1019.4 | 1326.6 | 1623.0 |
| 7 |     |     |    |     | 301.4 | 561.6  | 877.0  | 1085.1 | 1264.8 | 1645.6 | 2013.0 |
| 8 |     |     |    |     | 366.8 | 683.4  | 1067.2 | 1320.2 | 1538.7 | 2001.8 | 2448.5 |
| 9 |     |     |    |     | 439.4 | 818.6  | 1278.1 | 1581.1 | 1842.7 | 2397.1 | 2931.6 |
| 2 | 100 | 120 | 60 | 240 | 59.8  | 111.5  | 174.4  | 215.8  | 251.8  | 328.0  | 401.9  |
| 3 |     |     |    |     | 101.6 | 189.5  | 296.1  | 366.4  | 427.4  | 556.4  | 681.3  |
| 4 |     |     |    |     | 151.1 | 281.7  | 440.1  | 544.5  | 634.9  | 826.3  | 1011.3 |
| 5 |     |     |    |     | 209.8 | 391.0  | 610.6  | 755.5  | 880.6  | 1145.9 | 1401.9 |
| 6 |     |     |    |     | 278.6 | 519.2  | 810.6  | 1002.9 | 1168.8 | 1520.7 | 1860.0 |
| 7 |     |     |    |     | 358.1 | 667.2  | 1041.7 | 1288.6 | 1501.7 | 1953.5 | 2389.0 |
| 8 |     |     |    |     | 448.6 | 835.6  | 1304.5 | 1613.6 | 1880.4 | 2445.9 | 2990.8 |
| 9 |     |     |    |     | 550.0 | 1024.6 | 1599.4 | 1978.4 | 2305.4 | 2998.5 | 3666.1 |
| 2 | 100 | 120 | 85 | 290 | 65.2  | 121.6  | 190.1  | 235.3  | 274.4  | 357.3  | 437.6  |
| 3 |     |     |    |     | 109.1 | 203.4  | 317.9  | 393.3  | 458.7  | 597.0  | 730.8  |
| 4 |     |     |    |     | 160.6 | 299.3  | 467.4  | 578.3  | 674.2  | 877.4  | 1073.6 |
| 5 |     |     |    |     | 220.7 | 411.2  | 642.2  | 794.5  | 926.1  | 1205.0 | 1474.0 |
| 6 |     |     |    |     | 290.5 | 541.3  | 845.2  | 1045.6 | 1218.6 | 1585.4 | 1939.0 |
| 7 |     |     |    |     | 370.7 | 690.7  | 1078.3 | 1333.9 | 1554.5 | 2022.1 | 2472.8 |
| 8 |     |     |    |     | 461.7 | 860.0  | 1342.6 | 1660.7 | 1935.3 | 2517.2 | 3077.9 |
| 9 |     |     |    |     | 563.5 | 1049.7 | 1638.6 | 2026.8 | 2361.7 | 3071.7 | 3755.7 |
| 2 | 100 | 140 | 50 | 240 | 63.2  | 117.8  | 184.2  | 228.0  | 265.9  | 346.4  | 424.3  |
| 3 |     |     |    |     | 105.8 | 197.3  | 308.3  | 381.6  | 445.0  | 579.4  | 709.3  |
| 4 |     |     |    |     | 155.7 | 290.2  | 453.3  | 560.9  | 654.0  | 851.2  | 1041.6 |
| 5 |     |     |    |     | 214.5 | 399.7  | 624.3  | 772.3  | 900.3  | 1171.5 | 1433.1 |
| 6 |     |     |    |     | 283.4 | 528.0  | 824.4  | 1019.9 | 1188.7 | 1546.5 | 1891.5 |
| 7 |     |     |    |     | 362.9 | 676.1  | 1055.5 | 1305.7 | 1521.6 | 1979.4 | 2420.6 |
| 8 |     |     |    |     | 453.3 | 844.5  | 1318.3 | 1630.7 | 1900.2 | 2471.7 | 3022.3 |
| 9 |     |     |    |     | 554.8 | 1033.4 | 1613.2 | 1995.4 | 2325.1 | 3024.2 | 3697.6 |
| 2 | 100 | 140 | 75 | 290 | 68.1  | 127.0  | 198.4  | 245.6  | 286.4  | 372.9  | 456.6  |
| 3 |     |     |    |     | 112.9 | 210.4  | 328.7  | 406.8  | 474.3  | 617.4  | 755.6  |
| 4 |     |     |    |     | 164.8 | 307.1  | 479.6  | 593.5  | 691.8  | 900.3  | 1101.6 |
| 5 |     |     |    |     | 225.1 | 419.5  | 655.1  | 810.5  | 944.7  | 1229.1 | 1503.6 |
| 6 |     |     |    |     | 295.1 | 549.8  | 858.4  | 1062.0 | 1237.7 | 1610.2 | 1969.3 |
| 7 |     |     |    |     | 375.4 | 699.3  | 1091.7 | 1350.5 | 1573.8 | 2047.2 | 2503.5 |
| 8 |     |     |    |     | 466.3 | 868.7  | 1356.0 | 1677.4 | 1954.6 | 2542.4 | 3108.7 |
| 9 |     |     |    |     | 568.2 | 1058.3 | 1652.0 | 2043.4 | 2381.1 | 3097.0 | 3786.5 |



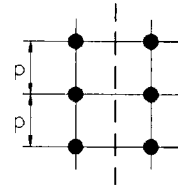
**Bolt groups**

One row of fasteners; fasteners not in the plane of the force

| No. of fasteners in vertical row | Pitch, $p$ (mm) | Values of $Z_{xx}$ (cm <sup>3</sup> ) for diameter of bolt, $D$ (mm) |       |       |       |        |        |        |
|----------------------------------|-----------------|--|-------|-------|-------|--------|--------|--------|
|                                  |                 | 12   | 16    | 20    | 22    | 24     | 27     | 30     |
| 2                                | 70              | 13.3   | 24.8  | 38.8  | 48.0  | 55.9   | 72.8   | 89.1   |
| 3                                |                 | 25.5   | 47.5  | 74.2  | 91.8  | 107.0  | 139.2  | 170.3  |
| 4                                |                 | 41.7   | 77.6  | 121.2 | 149.9 | 174.6  | 227.2  | 277.8  |
| 5                                |                 | 61.8   | 115.0 | 179.5 | 222.1 | 258.8  | 336.5  | 411.4  |
| 6                                |                 | 85.8   | 159.8 | 249.4 | 308.4 | 359.4  | 467.3  | 571.3  |
| 7                                |                 | 113.7  | 211.8 | 330.6 | 408.9 | 476.4  | 619.6  | 757.3  |
| 8                                |                 | 145.6  | 271.2 | 423.3 | 523.5 | 610.0  | 793.2  | 969.6  |
| 9                                |                 | 181.5  | 338.0 | 527.4 | 652.3 | 760.0  | 988.3  | 1208.0 |
| 2                                |                 | 100  | 15.4  | 28.7  | 44.8  | 55.4   | 64.6   | 84.1   |
| 3                                | 31.4            |  | 58.5  | 91.3  | 112.9 | 131.6  | 171.2  | 209.3  |
| 4                                | 53.0            |  | 98.8  | 154.2 | 190.7 | 222.2  | 288.9  | 353.2  |
| 5                                | 80.3            |  | 149.5 | 233.4 | 288.6 | 336.3  | 437.3  | 534.6  |
| 6                                | 113.2           |  | 210.8 | 328.9 | 406.8 | 474.0  | 616.3  | 753.4  |
| 7                                | 151.6           |  | 282.4 | 440.8 | 545.2 | 635.1  | 825.9  | 1009.5 |
| 8                                | 195.8           |  | 364.6 | 569.0 | 703.7 | 819.9  | 1066.1 | 1303.1 |
| 9                                | 245.5           |  | 457.2 | 713.5 | 882.5 | 1028.1 | 1336.9 | 1634.1 |

Centre of rotation is assumed 60 mm below the bottom bolt

The tabulated values are conservative when the centre of rotation is located more than 60 mm below the bottom bolt. The tabulated values are unconservative when the centre of rotation is located less than 60 mm below the bottom line.



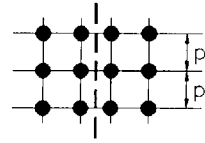
**Bolt groups**

Two rows of fasteners; fasteners not in the plane of the force

| No. of fasteners in vertical row | Pitch, $p$ (mm) | Values of $Z_{xx}$ (cm <sup>3</sup> ) for diameter of bolt, $D$ (mm) |       |        |        |        |        |        |
|----------------------------------|-----------------|--|-------|--------|--------|--------|--------|--------|
|                                  |                 | 12   | 16    | 20     | 22     | 24     | 27     | 30     |
| 2                                | 70              | 26.6   | 49.6  | 77.5   | 95.9   | 111.8  | 145.6  | 178.2  |
| 3                                |                 | 51.0   | 95.1  | 148.5  | 183.7  | 214.1  | 278.5  | 340.6  |
| 4                                |                 | 83.3   | 155.2 | 242.3  | 299.7  | 349.3  | 454.3  | 555.5  |
| 5                                |                 | 123.5  | 230.1 | 359.1  | 444.1  | 517.5  | 673.1  | 822.9  |
| 6                                |                 | 171.5  | 319.5 | 498.7  | 616.8  | 718.7  | 934.7  | 1142.6 |
| 7                                |                 | 227.5  | 423.7 | 661.2  | 817.8  | 952.8  | 1239.1 | 1514.7 |
| 8                                |                 | 291.2  | 542.5 | 846.6  | 1047.1 | 1219.9 | 1586.4 | 1939.2 |
| 9                                |                 | 362.9  | 675.9 | 1054.8 | 1304.6 | 1520.0 | 1976.5 | 2416.0 |
| 2                                |                 | 100  | 30.8  | 57.4   | 89.6   | 110.9  | 129.3  | 168.2  |
| 3                                | 62.8            |  | 117.0 | 182.6  | 225.9  | 263.2  | 342.4  | 418.6  |
| 4                                | 106.1           |  | 197.5 | 308.3  | 381.4  | 444.4  | 577.9  | 706.5  |
| 5                                | 160.6           |  | 299.1 | 466.7  | 577.3  | 672.6  | 874.7  | 1069.2 |
| 6                                | 226.3           |  | 421.5 | 657.8  | 813.6  | 947.9  | 1232.6 | 1506.7 |
| 7                                | 303.3           |  | 564.9 | 881.6  | 1090.3 | 1270.3 | 1651.8 | 2019.1 |
| 8                                | 391.5           |  | 729.2 | 1138.0 | 1407.4 | 1639.7 | 2132.2 | 2606.2 |
| 9                                | 491.0           |  | 914.5 | 1427.1 | 1765.0 | 2056.3 | 2673.8 | 3268.2 |

Centre of rotation is assumed 60 mm below the bottom bolts

The tabulated values are conservative when the centre of rotation is located more than 60 mm below the bottom bolts. The tabulated values are unconservative when the centre of rotation is located less than 60 mm below the bottom bolts.

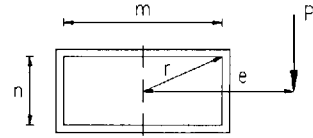


Bolt groups  
Four rows of fasteners; fasteners not in the plane of the force

| No. of fasteners<br>in vertical row | Pitch, $p$<br>(mm) | Values of $Z_{xx}$ ( $\text{cm}^3$ ) for<br>diameter of bolt, $D$ (mm) |        |        |        |        |        |        |
|-------------------------------------|--------------------|--|--------|--------|--------|--------|--------|--------|
|                                     |                    | 12   | 16     | 20     | 22     | 24     | 27     | 30     |
| 2                                   | 70                 | 53.2   | 99.2   | 155.0  | 191.8  | 223.7  | 291.1  | 356.3  |
| 3                                   |                    | 102.1  | 190.2  | 296.9  | 367.3  | 428.1  | 557.0  | 681.2  |
| 4                                   |                    | 166.7  | 310.5  | 484.7  | 599.5  | 698.6  | 908.7  | 1111.1 |
| 5                                   |                    | 247.0  | 460.1  | 718.2  | 888.3  | 1035.0 | 1346.1 | 1645.7 |
| 6                                   |                    | 343.1  | 639.1  | 997.4  | 1233.7 | 1437.4 | 1869.3 | 2285.2 |
| 7                                   |                    | 454.9  | 847.3  | 1322.4 | 1635.6 | 1905.7 | 2478.2 | 3029.4 |
| 8                                   |                    | 582.5  | 1084.9 | 1693.2 | 2094.1 | 2439.9 | 3172.8 | 3878.3 |
| 9                                   |                    | 725.8  | 1351.8 | 2109.7 | 2609.2 | 3039.9 | 3953.1 | 4832.0 |
| 2                                   |                    | 100  | 61.6   | 114.8  | 179.2  | 221.8  | 258.5  | 336.4  |
| 3                                   | 125.6              |  | 234.0  | 365.2  | 451.8  | 526.5  | 684.8  | 837.3  |
| 4                                   | 212.1              |  | 395.1  | 616.7  | 762.7  | 888.7  | 1155.8 | 1413.0 |
| 5                                   | 321.1              |  | 598.1  | 933.5  | 1154.5 | 1345.2 | 1749.3 | 2138.4 |
| 6                                   | 452.6              |  | 843.0  | 1315.6 | 1627.2 | 1895.8 | 2465.3 | 3013.5 |
| 7                                   | 606.6              |  | 1129.8 | 1763.1 | 2180.6 | 2540.6 | 3303.7 | 4038.2 |
| 8                                   | 783.1              |  | 1458.4 | 2276.0 | 2814.9 | 3279.5 | 4264.5 | 5212.5 |
| 9                                   | 982.0              |  | 1828.9 | 2854.2 | 3529.9 | 4112.6 | 5347.7 | 6536.4 |

Centre of rotation is assumed 60 mm below the bottom bolts

The tabulated values are conservative when the centre of rotation is located more than 60 mm below the bottom bolts. The tabulated values are unconservative when the centre of rotation is located less than 60 mm below the bottom bolts.

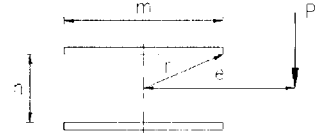


Weld groups  
Welds in the plane of the force

Values of  $Z_p$  (cm<sup>3</sup>) for 1 mm throat thickness

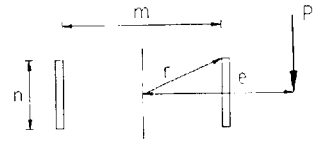
| Values of $n$<br>(mm) | Values of $m$ (mm) |       |       |       |       |       |       |       |       |       |       |
|-----------------------|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                       | 50                 | 75    | 100   | 125   | 150   | 175   | 200   | 225   | 250   | 275   | 300   |
| 50                    | 4.7                | 7.2   | 10.1  | 13.3  | 16.9  | 20.9  | 25.3  | 30.1  | 35.3  | 40.9  | 47.0  |
| 75                    | 7.2                | 10.6  | 14.3  | 18.3  | 22.6  | 27.4  | 32.5  | 37.9  | 43.8  | 50.1  | 56.8  |
| 100                   | 10.1               | 14.3  | 18.9  | 23.7  | 28.9  | 34.4  | 40.2  | 46.5  | 53.1  | 60.1  | 67.5  |
| 125                   | 13.3               | 18.3  | 23.7  | 29.5  | 35.5  | 41.8  | 48.5  | 55.5  | 62.9  | 70.6  | 78.7  |
| 150                   | 16.9               | 22.6  | 28.9  | 35.5  | 42.4  | 49.6  | 57.2  | 65.0  | 73.2  | 81.7  | 90.6  |
| 175                   | 20.9               | 27.4  | 34.4  | 41.8  | 49.6  | 57.7  | 66.1  | 74.8  | 83.9  | 93.2  | 102.9 |
| 200                   | 25.3               | 32.5  | 40.2  | 48.5  | 57.2  | 66.1  | 75.4  | 85.0  | 94.9  | 105.1 | 115.6 |
| 225                   | 30.1               | 37.9  | 46.5  | 55.5  | 65.0  | 74.8  | 85.0  | 95.5  | 106.2 | 117.3 | 128.6 |
| 250                   | 35.3               | 43.8  | 53.1  | 62.9  | 73.2  | 83.9  | 94.9  | 106.2 | 117.9 | 129.8 | 142.0 |
| 275                   | 40.9               | 50.1  | 60.1  | 70.6  | 81.7  | 93.2  | 105.1 | 117.3 | 129.8 | 142.6 | 155.7 |
| 300                   | 47.0               | 56.8  | 67.5  | 78.7  | 90.6  | 102.9 | 115.6 | 128.6 | 142.0 | 155.7 | 169.7 |
| 325                   | 53.5               | 64.0  | 75.3  | 87.2  | 99.8  | 112.9 | 126.4 | 140.3 | 154.5 | 169.1 | 184.0 |
| 350                   | 60.3               | 71.5  | 83.4  | 96.1  | 109.4 | 123.3 | 137.6 | 152.3 | 167.4 | 182.8 | 198.6 |
| 375                   | 67.6               | 79.4  | 92.0  | 105.4 | 119.4 | 134.0 | 149.1 | 164.6 | 180.6 | 196.9 | 213.5 |
| 400                   | 75.4               | 87.8  | 101.1 | 115.1 | 129.8 | 145.1 | 161.0 | 177.3 | 194.1 | 211.2 | 228.7 |
| 425                   | 83.5               | 96.5  | 110.5 | 125.2 | 140.6 | 156.7 | 173.3 | 190.4 | 207.9 | 225.9 | 244.2 |
| 450                   | 92.0               | 105.7 | 120.3 | 135.7 | 151.8 | 168.5 | 185.9 | 203.8 | 222.1 | 240.9 | 260.0 |
| 475                   | 101.0              | 115.3 | 130.5 | 146.6 | 163.4 | 180.8 | 198.9 | 217.5 | 236.6 | 256.2 | 276.2 |
| 500                   | 110.4              | 125.3 | 141.2 | 157.9 | 175.4 | 193.5 | 212.3 | 231.7 | 251.6 | 271.9 | 292.7 |
| 525                   | 120.2              | 135.8 | 152.3 | 169.6 | 187.8 | 206.6 | 226.1 | 246.2 | 266.8 | 288.0 | 309.5 |
| 550                   | 130.4              | 146.6 | 163.8 | 181.8 | 200.6 | 220.1 | 240.3 | 261.1 | 282.5 | 304.4 | 326.8 |
| 575                   | 141.0              | 157.9 | 175.7 | 194.3 | 213.8 | 234.0 | 254.9 | 276.4 | 298.5 | 321.2 | 344.3 |
| 600                   | 152.0              | 169.5 | 188.0 | 207.3 | 227.4 | 248.3 | 269.8 | 292.1 | 314.9 | 338.3 | 362.2 |

Weld groups  
Welds in the plane of the force



Values of  $Z_p$  (cm<sup>3</sup>) for 1 mm throat thickness

| Values of $n$<br>(mm) | Values of $m$ (mm) |      |      |      |      |       |       |       |       |       |       |
|-----------------------|--------------------|------|------|------|------|-------|-------|-------|-------|-------|-------|
|                       | 50                 | 75   | 100  | 125  | 150  | 175   | 200   | 225   | 250   | 275   | 300   |
| 50                    | 2.4                | 3.6  | 5.2  | 7.2  | 9.5  | 12.2  | 15.4  | 18.9  | 22.9  | 27.3  | 32.1  |
| 75                    | 3.6                | 5.3  | 7.2  | 9.3  | 11.7 | 14.6  | 17.8  | 21.3  | 25.3  | 29.7  | 34.6  |
| 100                   | 4.8                | 7.1  | 9.4  | 11.9 | 14.6 | 17.5  | 20.9  | 24.6  | 28.6  | 33.1  | 37.9  |
| 125                   | 6.1                | 9.0  | 11.8 | 14.7 | 17.8 | 21.0  | 24.6  | 28.4  | 32.6  | 37.2  | 42.1  |
| 150                   | 7.4                | 10.9 | 14.3 | 17.7 | 21.2 | 24.8  | 28.7  | 32.8  | 37.2  | 41.9  | 47.0  |
| 175                   | 8.6                | 12.8 | 16.8 | 20.8 | 24.8 | 28.9  | 33.1  | 37.5  | 42.2  | 47.1  | 52.4  |
| 200                   | 9.9                | 14.7 | 19.4 | 24.0 | 28.5 | 33.1  | 37.7  | 42.5  | 47.5  | 52.7  | 58.2  |
| 225                   | 11.2               | 16.6 | 21.9 | 27.1 | 32.2 | 37.3  | 42.5  | 47.7  | 53.1  | 58.7  | 64.5  |
| 250                   | 12.4               | 18.5 | 24.5 | 30.3 | 36.0 | 41.7  | 47.4  | 53.1  | 58.9  | 64.9  | 71.1  |
| 275                   | 13.7               | 20.4 | 27.0 | 33.4 | 39.8 | 46.1  | 52.3  | 58.6  | 64.9  | 71.3  | 77.9  |
| 300                   | 14.9               | 22.3 | 29.5 | 36.6 | 43.6 | 50.5  | 57.3  | 64.1  | 71.0  | 77.8  | 84.9  |
| 325                   | 16.2               | 24.2 | 32.0 | 39.8 | 47.4 | 54.9  | 62.3  | 69.7  | 77.1  | 84.5  | 92.0  |
| 350                   | 17.4               | 26.1 | 34.6 | 43.0 | 51.2 | 59.3  | 67.4  | 75.4  | 83.3  | 91.3  | 99.2  |
| 375                   | 18.7               | 27.9 | 37.1 | 46.1 | 55.0 | 63.8  | 72.5  | 81.0  | 89.6  | 98.1  | 106.6 |
| 400                   | 19.9               | 29.8 | 39.6 | 49.3 | 58.8 | 68.2  | 77.5  | 86.7  | 95.8  | 104.9 | 114.0 |
| 425                   | 21.2               | 31.7 | 42.1 | 52.4 | 62.6 | 72.7  | 82.6  | 92.4  | 102.1 | 111.8 | 121.5 |
| 450                   | 22.5               | 33.6 | 44.7 | 55.6 | 66.4 | 77.1  | 87.7  | 98.1  | 108.5 | 118.7 | 129.0 |
| 475                   | 23.7               | 35.5 | 47.2 | 58.7 | 70.2 | 81.5  | 92.7  | 103.8 | 114.8 | 125.7 | 136.5 |
| 500                   | 25.0               | 37.4 | 49.7 | 61.9 | 74.0 | 86.0  | 97.8  | 109.5 | 121.1 | 132.6 | 144.1 |
| 525                   | 26.2               | 39.2 | 52.2 | 65.0 | 77.8 | 90.4  | 102.9 | 115.2 | 127.5 | 139.6 | 151.6 |
| 550                   | 27.5               | 41.1 | 54.7 | 68.2 | 81.6 | 94.8  | 107.9 | 120.9 | 133.8 | 146.6 | 159.2 |
| 575                   | 28.7               | 43.0 | 57.2 | 71.3 | 85.4 | 99.2  | 113.0 | 126.6 | 140.1 | 153.5 | 166.8 |
| 600                   | 30.0               | 44.9 | 59.7 | 74.5 | 89.1 | 103.7 | 118.1 | 132.3 | 146.5 | 160.5 | 174.4 |



Weld groups  
Welds in the plane of the force

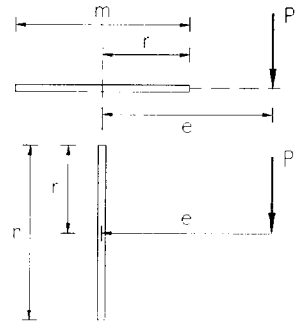
Values of  $Z_p$  (cm<sup>3</sup>) for 1 mm throat thickness

| Values of $n$<br>(mm) | Values of $m$ (mm) |       |       |       |       |       |       |       |       |       |       |
|-----------------------|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
|                       | 50                 | 75    | 100   | 125   | 150   | 175   | 200   | 225   | 250   | 275   | 300   |
| 50                    | 2.4                | 3.6   | 4.8   | 6.1   | 7.4   | 8.6   | 9.9   | 11.2  | 12.4  | 13.7  | 14.9  |
| 75                    | 3.6                | 5.3   | 7.1   | 9.0   | 10.9  | 12.8  | 14.7  | 16.6  | 18.5  | 20.4  | 22.3  |
| 100                   | 5.2                | 7.2   | 9.4   | 11.8  | 14.3  | 16.8  | 19.4  | 21.9  | 24.5  | 27.0  | 29.5  |
| 125                   | 7.2                | 9.3   | 11.9  | 14.7  | 17.7  | 20.8  | 24.0  | 27.1  | 30.3  | 33.4  | 36.6  |
| 150                   | 9.5                | 11.7  | 14.6  | 17.8  | 21.2  | 24.8  | 28.5  | 32.2  | 36.0  | 39.8  | 43.6  |
| 175                   | 12.2               | 14.6  | 17.5  | 21.0  | 24.8  | 28.9  | 33.1  | 37.3  | 41.7  | 46.1  | 50.5  |
| 200                   | 15.4               | 17.8  | 20.9  | 24.6  | 28.7  | 33.1  | 37.7  | 42.5  | 47.4  | 52.3  | 57.3  |
| 225                   | 18.9               | 21.3  | 24.6  | 28.4  | 32.8  | 37.5  | 42.5  | 47.7  | 53.1  | 58.6  | 64.1  |
| 250                   | 22.9               | 25.3  | 28.6  | 32.6  | 37.2  | 42.2  | 47.5  | 53.1  | 58.9  | 64.9  | 71.0  |
| 275                   | 27.3               | 29.7  | 33.1  | 37.2  | 41.9  | 47.1  | 52.7  | 58.7  | 64.9  | 71.3  | 77.8  |
| 300                   | 32.1               | 34.6  | 37.9  | 42.1  | 47.0  | 52.4  | 58.2  | 64.5  | 71.1  | 77.9  | 84.9  |
| 325                   | 37.3               | 39.8  | 43.2  | 47.4  | 52.4  | 58.0  | 64.1  | 70.6  | 77.4  | 84.6  | 92.0  |
| 350                   | 42.9               | 45.4  | 48.9  | 53.2  | 58.2  | 63.9  | 70.2  | 76.9  | 84.1  | 91.6  | 99.3  |
| 375                   | 48.9               | 51.5  | 55.0  | 59.3  | 64.4  | 70.2  | 76.7  | 83.6  | 91.0  | 98.8  | 106.9 |
| 400                   | 55.4               | 57.9  | 61.4  | 65.8  | 71.0  | 76.9  | 83.5  | 90.6  | 98.2  | 106.3 | 114.7 |
| 425                   | 62.3               | 64.8  | 68.3  | 72.8  | 78.0  | 84.0  | 90.7  | 98.0  | 105.8 | 114.0 | 122.7 |
| 450                   | 69.6               | 72.1  | 75.7  | 80.1  | 85.4  | 91.5  | 98.2  | 105.7 | 113.6 | 122.1 | 131.0 |
| 475                   | 77.3               | 79.8  | 83.4  | 87.8  | 93.2  | 99.3  | 106.2 | 113.7 | 121.9 | 130.5 | 139.7 |
| 500                   | 85.4               | 88.0  | 91.5  | 96.0  | 101.4 | 107.6 | 114.5 | 122.2 | 130.4 | 139.3 | 148.6 |
| 525                   | 94.0               | 96.5  | 100.1 | 104.6 | 110.0 | 116.2 | 123.2 | 131.0 | 139.4 | 148.4 | 157.9 |
| 550                   | 102.9              | 105.5 | 109.0 | 113.6 | 119.0 | 125.3 | 132.4 | 140.2 | 148.7 | 157.8 | 167.5 |
| 575                   | 112.3              | 114.9 | 118.4 | 123.0 | 128.4 | 134.7 | 141.9 | 149.8 | 158.4 | 167.6 | 177.5 |
| 600                   | 122.1              | 124.7 | 128.2 | 132.8 | 138.2 | 144.6 | 151.8 | 159.8 | 168.5 | 177.8 | 187.8 |

Weld groups  
Welds in the plane of the force

Values of  $Z_p$  (cm<sup>3</sup>) for 1 mm of throat thickness

| $m$ or $n$ (mm) | $Z_p$ (cm <sup>3</sup> ) |
|-----------------|--------------------------|
| 50              | 0.4                      |
| 75              | 0.9                      |
| 100             | 1.7                      |
| 125             | 2.6                      |
| 150             | 3.8                      |
| 175             | 5.1                      |
| 200             | 6.7                      |
| 225             | 8.4                      |
| 250             | 10.4                     |
| 275             | 12.6                     |
| 300             | 15.0                     |
| 325             | 17.6                     |
| 350             | 20.4                     |
| 375             | 23.4                     |
| 400             | 26.7                     |
| 425             | 30.1                     |
| 450             | 33.8                     |
| 475             | 37.6                     |
| 500             | 41.7                     |
| 525             | 45.9                     |
| 550             | 50.4                     |
| 575             | 55.1                     |
| 600             | 60.0                     |





**Capacities of fillet welds**

(1) Angle between fusion faces 60° to 90° using BS 639 electrodes grade E43, with BS 4360 steel of grade 40, 43, WR50 or 50 (or BS EN 10 025 equivalent) or electrodes grade E51 with grade 40 or 43 steel

| Leg length, S<br>(mm) | Throat thickness $a = 0.7S$<br>(mm) | Capacity @ 215 N/mm <sup>2</sup><br>(kN/mm) |
|-----------------------|-------------------------------------|---|
| 3                     | 2.1                                 | 0.451                                       |
| 4                     | 2.8                                 | 0.602                                       |
| 5                     | 3.5                                 | 0.752                                       |
| 6                     | 4.2                                 | 0.903                                       |
| 8                     | 5.6                                 | 1.204                                       |
| 10                    | 7.0                                 | 1.505                                       |
| 12                    | 8.4                                 | 1.806                                       |
| 15                    | 10.5                                | 2.257                                       |
| 18                    | 12.6                                | 2.719                                       |
| 20                    | 14.0                                | 3.01  |
| 22                    | 15.4                                | 3.311                                       |
| 25                    | 17.5                                | 3.762                                       |

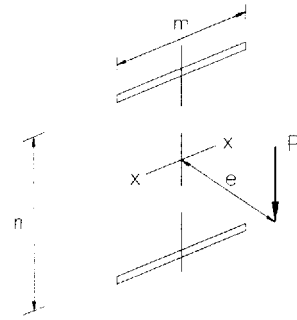
(2) Angle between fusion faces 60° to 90° using BS 639 electrodes grade E51, with BS 4360 steel of grade WR50, 50 or 55 (or BS EN 10 025 equivalent)

| Leg length, S<br>(mm) | Throat thickness $a = 0.7S$<br>(mm) | Capacity @ 255 N/mm <sup>2</sup><br>(kN/mm) |
|-----------------------|-------------------------------------|---|
| 3                     | 2.1                                 | 0.535                                       |
| 4                     | 2.8                                 | 0.714                                       |
| 5                     | 3.5                                 | 0.892                                       |
| 6                     | 4.2                                 | 1.071                                       |
| 8                     | 5.6                                 | 1.428                                       |
| 10                    | 7.0                                 | 1.785                                       |
| 12                    | 8.4                                 | 2.142                                       |
| 15                    | 10.5                                | 2.677                                       |
| 18                    | 12.6                                | 3.213                                       |
| 20                    | 14.0                                | 3.570                                       |
| 22                    | 15.4                                | 3.927                                       |
| 25                    | 17.5                                | 4.462                                       |

(3) Angle between fusion faces 60° to 90° using BS 639 electrodes grade E51<sup>a</sup>, with BS 4360 steel of grade 55 (or BS EN 10 025 equivalent)

| Leg length, S<br>(mm) | Throat thickness $a = 0.7S$<br>(mm) | Capacity @ 275 N/mm <sup>2</sup><br>(kN/mm) <sup>a</sup> |
|-----------------------|-------------------------------------|--|
| 3                     | 2.1                                 | 0.577  |
| 4                     | 2.8                                 | 0.77   |
| 5                     | 3.5                                 | 0.962  |
| 6                     | 4.2                                 | 1.155  |
| 8                     | 5.6                                 | 1.540  |
| 10                    | 7.0                                 | 1.925  |
| 12                    | 8.4                                 | 2.310  |
| 15                    | 10.5                                | 2.887  |
| 18                    | 12.6                                | 3.465  |
| 20                    | 14.0                                | 3.850  |
| 22                    | 15.4                                | 4.230  |
| 25                    | 17.5                                | 4.812  |

<sup>a</sup> Only applies to electrodes having a minimum tensile strength of 550 N/mm<sup>2</sup> and a minimum yield strength of 450 N/mm<sup>2</sup>



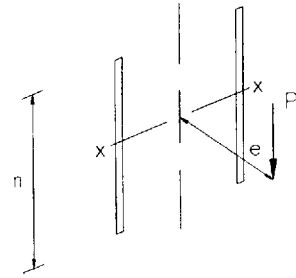
Weld groups  
Welds not in the plane of the force

Values of  $Z_{xx}$  (cm<sup>3</sup>) for 1 mm throat thickness

| Values of $n$<br>(mm) | Values of $m$ (mm) |      |      |      |      |       |       |       |       |       |       |
|-----------------------|--------------------|------|------|------|------|-------|-------|-------|-------|-------|-------|
|                       | 50                 | 75   | 100  | 125  | 150  | 175   | 200   | 225   | 250   | 275   | 300   |
| 50                    | 2.5                | 3.8  | 5.0  | 6.3  | 7.5  | 8.8   | 10.0  | 11.3  | 12.5  | 13.8  | 15.0  |
| 75                    | 3.8                | 5.6  | 7.5  | 9.4  | 11.3 | 13.1  | 15.0  | 16.9  | 18.8  | 20.6  | 22.5  |
| 100                   | 5.0                | 7.5  | 10.0 | 12.5 | 15.0 | 17.5  | 20.0  | 22.5  | 25.0  | 27.5  | 30.0  |
| 125                   | 6.3                | 9.4  | 12.5 | 15.6 | 18.8 | 21.9  | 25.0  | 28.1  | 31.3  | 34.4  | 37.5  |
| 150                   | 7.5                | 11.3 | 15.0 | 18.8 | 22.5 | 26.3  | 30.0  | 33.8  | 37.5  | 41.3  | 45.0  |
| 175                   | 8.8                | 13.1 | 17.5 | 21.9 | 26.3 | 30.6  | 35.0  | 39.4  | 43.8  | 48.1  | 52.5  |
| 200                   | 10.0               | 15.0 | 20.0 | 25.0 | 30.0 | 35.0  | 40.0  | 45.0  | 50.0  | 55.0  | 60.0  |
| 225                   | 11.3               | 16.9 | 22.5 | 28.1 | 33.8 | 39.4  | 45.0  | 50.6  | 56.3  | 61.9  | 67.5  |
| 250                   | 12.5               | 18.8 | 25.0 | 31.3 | 37.5 | 43.8  | 50.0  | 56.3  | 62.5  | 68.8  | 75.0  |
| 275                   | 13.8               | 20.6 | 27.5 | 34.4 | 41.3 | 48.1  | 55.0  | 61.9  | 68.8  | 75.6  | 82.5  |
| 300                   | 15.0               | 22.5 | 30.0 | 37.5 | 45.0 | 52.5  | 60.0  | 67.5  | 75.0  | 82.5  | 90.0  |
| 325                   | 16.3               | 24.4 | 32.5 | 40.6 | 48.8 | 56.9  | 65.0  | 73.1  | 81.3  | 89.4  | 97.5  |
| 350                   | 17.5               | 26.3 | 35.0 | 43.8 | 52.5 | 61.3  | 70.0  | 78.8  | 87.5  | 96.3  | 105.0 |
| 375                   | 18.8               | 28.1 | 37.5 | 46.9 | 56.3 | 65.6  | 75.0  | 84.4  | 93.8  | 103.1 | 112.5 |
| 400                   | 20.0               | 30.0 | 40.0 | 50.0 | 60.0 | 70.0  | 80.0  | 90.0  | 100.0 | 110.0 | 120.0 |
| 425                   | 21.3               | 31.9 | 42.5 | 53.1 | 63.8 | 74.4  | 85.0  | 95.6  | 106.3 | 116.9 | 127.5 |
| 450                   | 22.5               | 33.8 | 45.0 | 56.3 | 67.5 | 78.8  | 90.0  | 101.3 | 112.5 | 123.8 | 135.0 |
| 475                   | 23.8               | 35.6 | 47.5 | 59.4 | 71.3 | 83.1  | 95.0  | 106.9 | 118.8 | 130.6 | 142.5 |
| 500                   | 25.0               | 37.5 | 50.0 | 62.5 | 75.0 | 87.5  | 100.0 | 112.5 | 125.0 | 137.5 | 150.0 |
| 525                   | 26.3               | 39.4 | 52.5 | 65.6 | 78.8 | 91.9  | 105.0 | 118.1 | 131.3 | 144.4 | 157.5 |
| 550                   | 27.5               | 41.3 | 55.0 | 68.8 | 82.5 | 96.3  | 110.0 | 123.8 | 137.5 | 151.3 | 165.0 |
| 575                   | 28.8               | 43.1 | 57.5 | 71.9 | 86.3 | 100.6 | 115.0 | 129.4 | 143.8 | 158.1 | 172.5 |
| 600                   | 30.0               | 45.0 | 60.0 | 75.0 | 90.0 | 105.0 | 120.0 | 135.0 | 150.0 | 165.0 | 180.0 |

Weld groups  
 Welds not in the plane of the force

| Values of $Z_{xx}$ (cm <sup>3</sup> ) for 1 mm throat thickness |                             |
|---|-----------------------------|
| $n$ (mm)  | $Z_{xx}$ (cm <sup>3</sup> ) |
| 50  | 0.8                         |
| 75  | 1.9                         |
| 100   | 3.3                         |
| 125   | 5.2                         |
| 150   | 7.5                         |
| 175   | 10.2                        |
| 200   | 13.3                        |
| 225   | 16.9                        |
| 250   | 20.8                        |
| 275   | 25.2                        |
| 300   | 30.0                        |
| 325   | 35.2                        |
| 350   | 40.8                        |
| 375   | 46.9                        |
| 400   | 53.3                        |
| 425   | 60.2                        |
| 450   | 67.5                        |
| 475   | 75.2                        |
| 500   | 83.3                        |
| 525   | 91.9                        |
| 550   | 100.8                       |
| 575   | 110.2                       |
| 600   | 120.0                       |



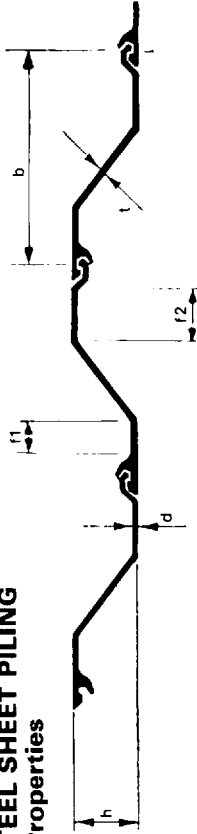


Weld groups  
Welds in the plane of the force

Values of  $Z_p$  (cm<sup>3</sup>) for 1 mm throat thickness

| Values of $n$<br>(mm) | Values of $m$ (mm) |       |       |       |       |       |       |       |       |       |       |  |
|-----------------------|--------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|
|                       | 50                 | 75    | 100   | 125   | 150   | 175   | 200   | 225   | 250   | 275   | 300   |  |
| 50                    | 2.8                | 4.3   | 6.2   | 8.5   | 11.2  | 14.3  | 17.9  | 21.9  | 26.2  | 31.0  | 36.2  |  |
| 75                    | 4.3                | 6.2   | 8.4   | 11.0  | 13.9  | 17.3  | 21.1  | 25.2  | 29.8  | 34.8  | 40.3  |  |
| 100                   | 6.2                | 8.5   | 11.0  | 13.9  | 17.1  | 20.7  | 24.7  | 29.2  | 34.0  | 39.2  | 44.9  |  |
| 125                   | 8.3                | 11.0  | 14.0  | 17.2  | 20.7  | 24.6  | 28.9  | 33.6  | 38.7  | 44.1  | 50.0  |  |
| 150                   | 10.6               | 13.9  | 17.3  | 20.9  | 24.8  | 29.0  | 33.5  | 38.5  | 43.8  | 49.6  | 55.7  |  |
| 175                   | 13.2               | 17.0  | 20.8  | 24.9  | 29.1  | 33.7  | 38.6  | 43.8  | 49.4  | 55.4  | 61.8  |  |
| 200                   | 16.0               | 20.3  | 24.7  | 29.1  | 33.8  | 38.8  | 44.0  | 49.6  | 55.5  | 61.8  | 68.4  |  |
| 225                   | 19.0               | 23.9  | 28.8  | 33.7  | 38.8  | 44.2  | 49.8  | 55.7  | 61.9  | 68.5  | 75.5  |  |
| 250                   | 22.2               | 27.7  | 33.1  | 38.5  | 44.1  | 49.9  | 55.9  | 62.2  | 68.8  | 75.7  | 82.9  |  |
| 275                   | 25.6               | 31.7  | 37.7  | 43.6  | 49.7  | 55.9  | 62.3  | 69.0  | 75.9  | 83.2  | 90.8  |  |
| 300                   | 29.2               | 35.9  | 42.5  | 49.0  | 55.5  | 62.2  | 69.0  | 76.1  | 83.4  | 91.1  | 99.0  |  |
| 325                   | 33.1               | 40.4  | 47.5  | 54.5  | 61.6  | 68.7  | 76.0  | 83.5  | 91.3  | 99.3  | 107.6 |  |
| 350                   | 37.1               | 45.0  | 52.7  | 60.3  | 67.9  | 75.5  | 83.3  | 91.3  | 99.4  | 107.8 | 116.5 |  |
| 375                   | 41.4               | 49.9  | 58.2  | 66.3  | 74.5  | 82.6  | 90.9  | 99.3  | 107.8 | 116.7 | 125.7 |  |
| 400                   | 45.9               | 55.0  | 63.8  | 72.6  | 81.2  | 89.9  | 98.7  | 107.5 | 116.6 | 125.8 | 135.3 |  |
| 425                   | 50.6               | 60.3  | 69.7  | 79.0  | 88.3  | 97.5  | 106.7 | 116.1 | 125.6 | 135.3 | 145.1 |  |
| 450                   | 55.4               | 65.8  | 75.8  | 85.7  | 95.5  | 105.3 | 115.0 | 124.9 | 134.8 | 145.0 | 155.3 |  |
| 475                   | 60.6               | 71.5  | 82.2  | 92.6  | 103.0 | 113.3 | 123.6 | 133.9 | 144.4 | 155.0 | 165.7 |  |
| 500                   | 65.9               | 77.4  | 88.7  | 99.8  | 110.7 | 121.5 | 132.4 | 143.2 | 154.2 | 165.2 | 176.5 |  |
| 525                   | 71.4               | 83.6  | 95.4  | 107.1 | 118.6 | 130.0 | 141.4 | 152.8 | 164.2 | 175.8 | 187.5 |  |
| 550                   | 77.1               | 89.9  | 102.4 | 114.6 | 126.7 | 138.7 | 150.6 | 162.5 | 174.5 | 186.5 | 198.7 |  |
| 575                   | 83.0               | 96.5  | 109.6 | 122.4 | 135.1 | 147.6 | 160.1 | 172.6 | 185.0 | 197.6 | 210.2 |  |
| 600                   | 89.2               | 103.2 | 116.9 | 130.4 | 143.7 | 156.8 | 169.8 | 182.8 | 195.8 | 208.9 | 222.0 |  |

**FRODINGHAM STEEL SHEET PILING**  
Dimensions and Properties

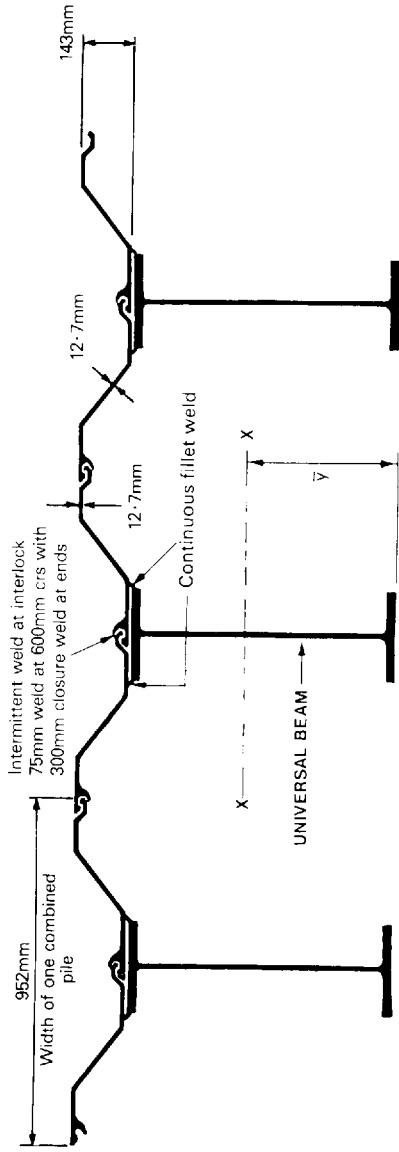


| Section | b<br>mm<br>(nom) | h<br>mm<br>(nom) | d<br>mm | t<br>mm<br>(nom) | f1<br>mm<br>(nom) | f2<br>mm<br>(nom) | Sectional<br>Area<br>sq. cm. | Mass                      |                             | Moment<br>of<br>Inertia<br>cm <sup>4</sup><br>per<br>metre | Section<br>Modulus<br>cm <sup>3</sup><br>per<br>metre | Section |
|---------|------------------|------------------|---------|------------------|-------------------|-------------------|------------------------------|---------------------------|-----------------------------|--|---|---------|
|         |                  |                  |         |                  |                   |                   |                              | kg per<br>linear<br>metre | kg per<br>sq. m.<br>of wall |  |   |         |
| 1BXN    | 476              | 143              | 12.7    | 12.7             | 78                | 123               | 166.5                        | 62.1                      | 130.4                       | 4919   | 688   | 1BXN    |
| 1N      | 483              | 170              | 9.0     | 9.0              | 105               | 137               | 126.0                        | 47.8                      | 99.1                        | 6048   | 713   | 1N      |
| 2N      | 483              | 235              | 9.7     | 8.4              | 97                | 149               | 143.0                        | 54.2                      | 112.3                       | 13513  | 1150  | 2N      |
| 3N      | 483              | 283              | 11.7    | 8.9              | 89                | 145               | 175.0                        | 66.2                      | 137.1                       | 23885  | 1688  | 3N      |
| 3NA     | 483              | 305              | 9.7     | 9.5              | 96                | 146               | 165.0                        | 62.6                      | 129.8                       | 25687  | 1690  | 3NA     |
| 4N      | 483              | 330              | 14.0    | 10.4             | 77                | 127               | 218.0                        | 82.4                      | 170.8                       | 39831  | 2414  | 4N      |
| 5       | 425              | 311              | 17.0    | 11.9             | 89                | 118               | 302.0                        | 100.8                     | 236.9                       | 49262  | 3168  | 5       |

**SPECIAL SECTIONS**

Sections may be "rolled up" (thickened) or "rolled down" (thinned) by special arrangement to increase or decrease the thickness of both webs and flanges by a maximum of 0.8mm.

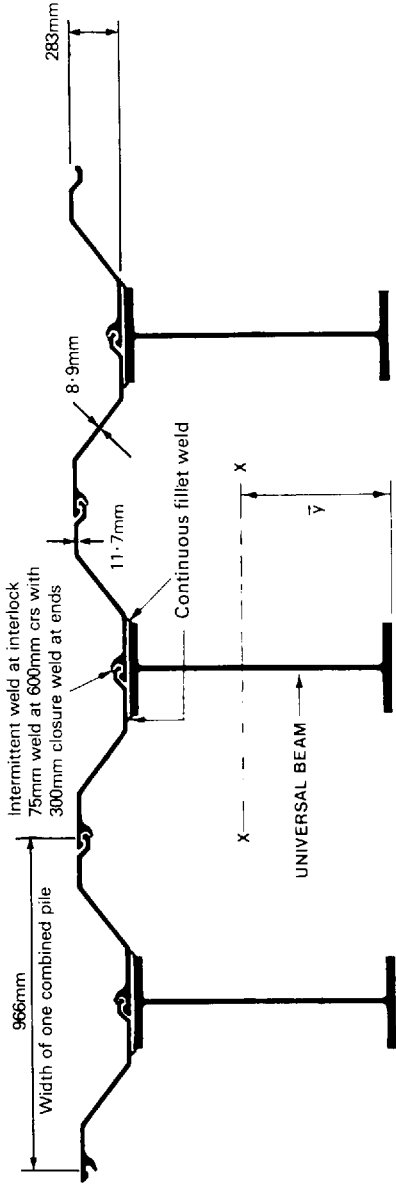
### High Modulus Piles with Frodingham 1BXN Wings – Dimensions and Properties



| Universal Beam |           | Crs. of u.b. s mm (nom) | Mass |                   | Area of Section cm <sup>2</sup> | y cm | Moment of Inertia xx    |                              | Section Modulus xx      |                              | Rad of gyration xx cm |
|----------------|-----------|-------------------------|------|-------------------|---------------------------------|------|-------------------------|------------------------------|-------------------------|------------------------------|-----------------------|
| serial size mm | mass kg/m |                         | kg/m | kg/m <sup>3</sup> |                                 |      | cm <sup>4</sup> /m wall | cm <sup>4</sup> /single pile | cm <sup>3</sup> /m wall | cm <sup>3</sup> /single pile |                       |
| 533 x 210      | 101       | 952                     | 225  | 237               | 287                             | 45.6 | 156841                  | 148361                       | 3420                    | 3256                         | 22.7                  |
| 610 x 229      | 113       | 952                     | 237  | 249               | 302                             | 50.0 | 208203                  | 198209                       | 4164                    | 3964                         | 25.6                  |
| *610 x 305     | 149       | 952                     | 270  | 284               | 344                             | 47.4 | 263788                  | 251126                       | 5564                    | 5297                         | 27.0                  |
| 686 x 254      | 152       | 952                     | 276  | 290               | 352                             | 53.1 | 320324                  | 304949                       | 6036                    | 5746                         | 29.4                  |
| 762 x 267      | 173       | 952                     | 297  | 312               | 378                             | 57.0 | 418126                  | 398056                       | 7331                    | 6979                         | 32.4                  |
| 762 x 267      | 197       | 952                     | 321  | 337               | 409                             | 56.2 | 468674                  | 446178                       | 8346                    | 7945                         | 33.0                  |
| *838 x 292     | 194       | 952                     | 316  | 332               | 403                             | 61.1 | 542137                  | 516115                       | 8869                    | 8443                         | 35.8                  |
| *914 x 305     | 224       | 952                     | 344  | 362               | 438                             | 64.0 | 693250                  | 659974                       | 10836                   | 10316                        | 38.8                  |
| *914 x 305     | 253       | 952                     | 372  | 391               | 474                             | 63.0 | 772405                  | 735330                       | 12261                   | 11672                        | 39.4                  |
| *914 x 305     | 289       | 952                     | 407  | 428               | 519                             | 61.9 | 860627                  | 819317                       | 13902                   | 13235                        | 39.7                  |
| *914 x 419     | 388       | 952                     | 469  | 492               | 597                             | 56.4 | 1048950                 | 998800                       | 18599                   | 17706                        | 41.0                  |

\* Denotes beam section with top flange reduced to 280mm to facilitate fabrication.  
 Note: Centre line of common interlock on sheet pile does not coincide with centre line of Universal Beam.

**High Modulus Piles with Frodingham 3N Wings – Dimensions and Properties**

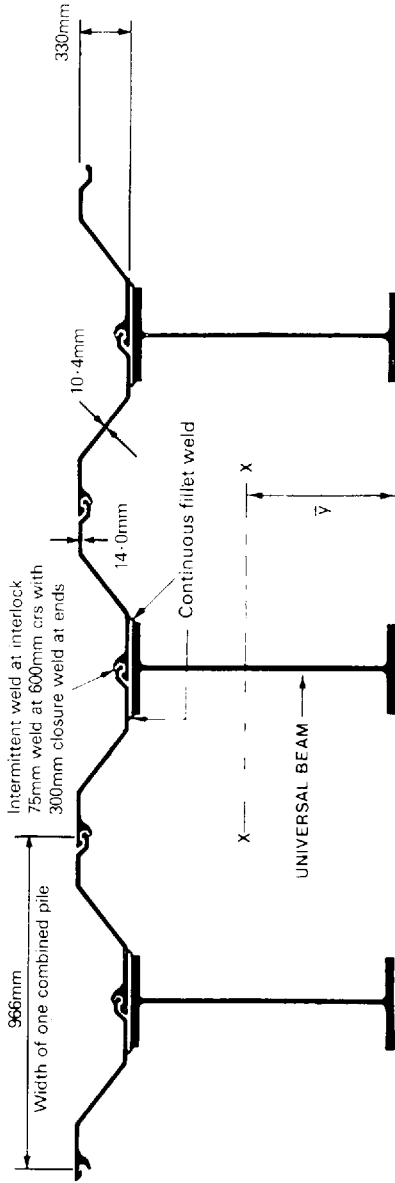


| Universal Beam |           | Crs of u.b.'s mm (nom) | Mass |                   | Area of section cm <sup>2</sup> | y cm | Moment of Inertia <sub>xx</sub> |                              | Section Modulus <sub>xx</sub> |                              | Rad of gyration <sub>xx</sub> cm |
|----------------|-----------|------------------------|------|-------------------|---------------------------------|------|---------------------------------|------------------------------|-------------------------------|------------------------------|----------------------------------|
| serial size mm | mass kg/m |                        | kg/m | kg/m <sup>2</sup> |                                 |      | cm <sup>4</sup> /m wall         | cm <sup>4</sup> /single pile | cm <sup>3</sup> /m wall       | cm <sup>3</sup> /single pile |                                  |
| 533 x 210      | 101       | 966                    | 234  | 242               | 298                             | 50.1 | 215095                          | 207782                       | 4297                          | 4151                         | 26.4                             |
| 610 x 229      | 113       | 966                    | 246  | 254               | 314                             | 54.4 | 274184                          | 264862                       | 5044                          | 4872                         | 29.1                             |
| 610 x 305      | 149       | 966                    | 282  | 292               | 359                             | 51.5 | 337405                          | 325933                       | 6554                          | 6331                         | 30.1                             |
| 686 x 254      | 152       | 966                    | 285  | 295               | 363                             | 57.0 | 399583                          | 385997                       | 7012                          | 6774                         | 32.6                             |
| 762 x 267      | 173       | 966                    | 306  | 316               | 389                             | 60.8 | 506669                          | 489442                       | 8337                          | 8054                         | 35.4                             |
| 762 x 267      | 197       | 966                    | 330  | 341               | 420                             | 59.7 | 561731                          | 542632                       | 9414                          | 9094                         | 36.0                             |
| 838 x 292      | 194       | 966                    | 327  | 338               | 416                             | 64.8 | 641188                          | 619388                       | 9887                          | 9551                         | 38.6                             |
| 914 x 305      | 224       | 966                    | 356  | 369               | 454                             | 67.7 | 803113                          | 775807                       | 11858                         | 11454                        | 41.3                             |
| 914 x 305      | 253       | 966                    | 386  | 399               | 492                             | 66.6 | 889309                          | 859072                       | 13357                         | 12902                        | 41.8                             |
| 914 x 305      | 289       | 966                    | 422  | 437               | 538                             | 65.3 | 984122                          | 950662                       | 15060                         | 14548                        | 42.1                             |
| *914 x 419     | 388       | 966                    | 486  | 506               | 623                             | 60.9 | 1202899                         | 1162000                      | 19761                         | 19090                        | 41.2                             |

\*Denotes beam section with one flange reduced to 310mm to facilitate fabrication.

Note: Centre line of common interlock on sheet pile does not coincide with centre line of Universal Beam.

**High Modulus Piles with Frodingham 4N Wings – Dimensions and Properties**



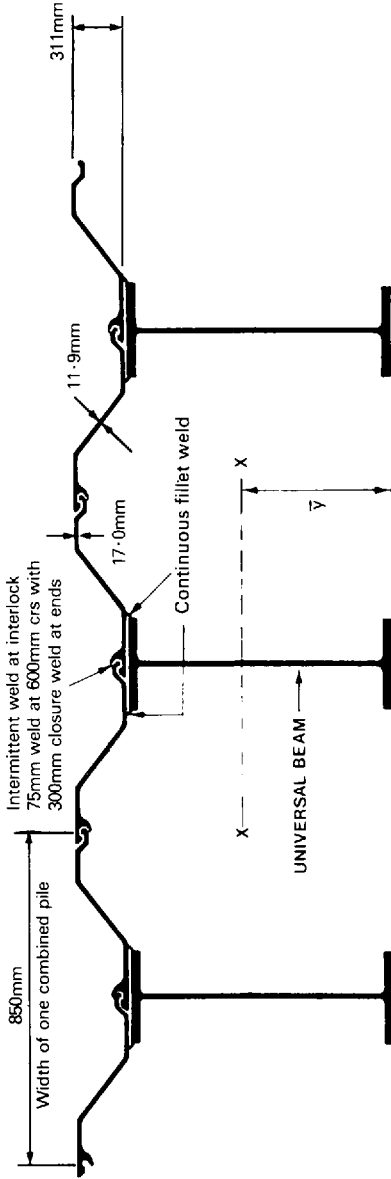
| Universal Beam |           | Crs of u.b.'s<br>mm<br>(nom) | Mass |                   | Area of section<br>cm <sup>2</sup> | Y<br>cm | Moment of Inertia<br>xx |                              | Section Modulus<br>xx   |                              | Rad of gyration<br>xx<br>cm |
|----------------|-----------|------------------------------|------|-------------------|------------------------------------|---------|-------------------------|------------------------------|-------------------------|------------------------------|-----------------------------|
| serial size mm | mass kg/m |                              | kg/m | kg/m <sup>2</sup> |                                    |         | cm <sup>4</sup> /m wall | cm <sup>4</sup> /single pile | cm <sup>3</sup> /m wall | cm <sup>3</sup> /single pile |                             |
| 533 × 210      | 101       | 966                          | 267  | 276               | 340                                | 53.68   | 259478                  | 250555                       | 4832                    | 4668                         | 27.2                        |
| 610 × 229      | 113       | 966                          | 278  | 288               | 355                                | 58.15   | 325149                  | 314094                       | 5591                    | 5401                         | 29.8                        |
| 610 × 305      | 149       | 966                          | 314  | 326               | 401                                | 55.17   | 397108                  | 383606                       | 7198                    | 6953                         | 30.9                        |
| 686 × 254      | 152       | 966                          | 317  | 329               | 404                                | 60.87   | 465848                  | 450009                       | 7653                    | 7393                         | 33.4                        |
| 762 × 267      | 173       | 966                          | 338  | 350               | 431                                | 64.77   | 584576                  | 564700                       | 9026                    | 8719                         | 36.2                        |
| 762 × 267      | 197       | 966                          | 362  | 375               | 461                                | 63.57   | 646288                  | 624314                       | 10167                   | 9821                         | 36.8                        |
| 838 × 292      | 194       | 966                          | 359  | 372               | 458                                | 68.96   | 732365                  | 707465                       | 10621                   | 10259                        | 39.3                        |
| 914 × 305      | 224       | 966                          | 389  | 403               | 496                                | 71.84   | 911226                  | 880244                       | 12683                   | 12253                        | 42.1                        |
| 914 × 305      | 253       | 966                          | 419  | 433               | 533                                | 70.56   | 1005797                 | 971600                       | 14254                   | 13770                        | 42.7                        |
| 914 × 305      | 289       | 966                          | 455  | 471               | 579                                | 69.16   | 1109824                 | 1072090                      | 16047                   | 15502                        | 43.0                        |
| *914 × 419     | 388       | 966                          | 522  | 540               | 665                                | 63.13   | 1353126                 | 1307120                      | 21435                   | 20706                        | 44.3                        |

\* Denotes beam section with one flange reduced to 310mm to facilitate fabrication.

Note: Centre line of common interlock on sheet pile does not coincide with centre line of Universal Beam.



**High Modulus Piles with Frodingham 5 Wings – Dimensions and Properties**

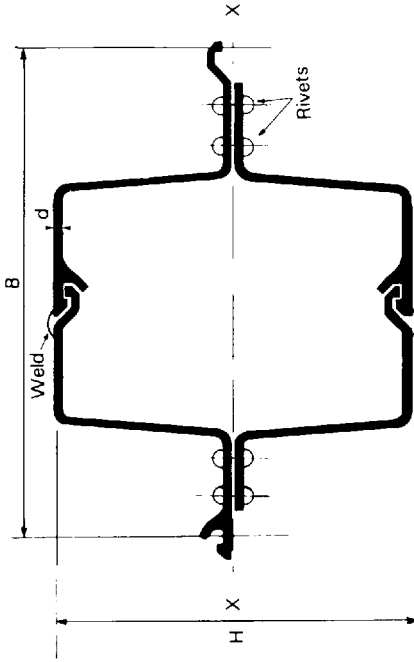


| Universal Beam |           | Crs of u.b.'s (nom) | Mass |                   | Area of section cm <sup>2</sup> | y cm  | Moment of Inertia xx    |                              | Section Modulus xx      |                              | Rad of gyration xx cm |
|----------------|-----------|---------------------|------|-------------------|---------------------------------|-------|-------------------------|------------------------------|-------------------------|------------------------------|-----------------------|
| serial size mm | mass kg/m |                     | kg/m | kg/m <sup>2</sup> |                                 |       | cm <sup>4</sup> /m wall | cm <sup>4</sup> /single pile | cm <sup>3</sup> /m wall | cm <sup>3</sup> /single pile |                       |
| 533 x 210      | 101       | 850                 | 303  | 357               | 387                             | 55.04 | 303751                  | 258188                       | 5518                    | 4691                         | 25.8                  |
| 610 x 229      | 113       | 850                 | 315  | 371               | 402                             | 59.77 | 381691                  | 324437                       | 6386                    | 5428                         | 28.4                  |
| 610 x 305      | 149       | 850                 | 351  | 413               | 447                             | 56.95 | 468496                  | 398222                       | 8226                    | 6992                         | 29.8                  |
| 686 x 254      | 152       | 850                 | 354  | 417               | 451                             | 62.86 | 550374                  | 467818                       | 8756                    | 7442                         | 32.2                  |
| 762 x 267      | 173       | 850                 | 375  | 441               | 478                             | 66.99 | 692787                  | 588869                       | 10342                   | 8790                         | 35.1                  |
| 762 x 267      | 197       | 850                 | 399  | 469               | 508                             | 65.84 | 767719                  | 652561                       | 11661                   | 9911                         | 35.8                  |
| 838 x 292      | 194       | 850                 | 396  | 466               | 504                             | 71.40 | 869912                  | 739425                       | 12183                   | 10356                        | 38.3                  |
| 914 x 305      | 224       | 850                 | 426  | 501               | 543                             | 74.47 | 1085066                 | 922306                       | 14571                   | 12385                        | 41.2                  |
| 914 x 305      | 253       | 850                 | 456  | 536               | 580                             | 73.19 | 1199518                 | 1019590                      | 16389                   | 13931                        | 41.9                  |
| 914 x 305      | 289       | 850                 | 491  | 578               | 626                             | 71.76 | 1325682                 | 1126830                      | 18474                   | 15703                        | 42.4                  |
| *914 x 419     | 388       | 850                 | 559  | 657               | 712                             | 65.77 | 1623634                 | 1380089                      | 24687                   | 20984                        | 44.0                  |

\* Denotes beam section with one flange reduced to 310mm to facilitate fabrication.

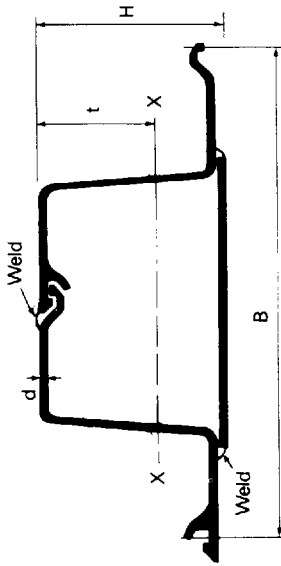
Note: Centre line of common interlock on sheet pile does not coincide with centre line of Universal Beam.

**Frodingham Double Box Piles—Dimensions and Properties**



| Section | B<br>mm<br>(nominal) | H<br>mm<br>(nominal) | d<br>mm | Mass<br>per metre<br>kg | Section Area cm <sup>2</sup> |               | Min. Rad.<br>of Gyr'n<br>cm | Approx.<br>Perimeter<br>mm | Moment<br>of Inertia<br>cm <sup>4</sup> |       | Section<br>Modulus<br>cm <sup>3</sup> |       |
|---------|----------------------|----------------------|---------|-------------------------|------------------------------|---------------|-----------------------------|----------------------------|---|-------|---------------------------------------|-------|
|         |                      |                      |         |                         | Steel<br>only                | Whole<br>Pile |                             |                            | X - X                                   | X - X | X - X                                 | X - X |
| 1BXN    | 953                  | 286                  | 12.7    | 231.3                   | 290                          | 1496          | 9.00                        | 2450                       | 25515                                   | 1785  | X - X                                 | 1785  |
| 1N      | 965                  | 340                  | 9.0     | 179.5                   | 225                          | 1717          | 10.95                       | 2520                       | 29279                                   | 1722  | X - X                                 | 1722  |
| 2N      | 965                  | 470                  | 9.7     | 201.8                   | 255                          | 2384          | 15.24                       | 2790                       | 64305                                   | 2735  | X - X                                 | 2735  |
| 3N      | 965                  | 565                  | 11.7    | 246.3                   | 310                          | 2856          | 18.34                       | 2970                       | 113415                                  | 4015  | X - X                                 | 4015  |
| 3NA     | 966                  | 610                  | 9.7     | 235.4                   | 298                          | 3035          | 19.69                       | 3100                       | 123861                                  | 4064  | X - X                                 | 4064  |
| 4N      | 965                  | 660                  | 14.0    | 305.1                   | 384                          | 3350          | 21.34                       | 3200                       | 191660                                  | 5805  | X - X                                 | 5805  |
| 5       | 850                  | 622                  | 17.0    | 367.8                   | 464                          | 2853          | 20.12                       | 3230                       | 208430                                  | 6700  | X - X                                 | 6700  |

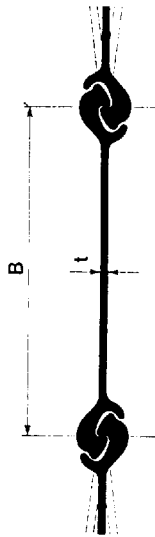
**Frodingham Plated Box Piles—Dimensions and Properties**



| Section | B<br>mm<br>(nom.) | H<br>mm<br>(nom.) | t<br>mm | d<br>mm | *Plate<br>Size<br>mm | Mass<br>per<br>metre<br>kg | Section Area cm <sup>2</sup> |               | Min. Rad.<br>of Gyr'n<br>cm | Approx<br>Perimeter<br>mm | Moment<br>of Inertia<br>cm <sup>4</sup> |      | Section<br>Modulus<br>cm <sup>3</sup> |     |
|---------|-------------------|-------------------|---------|---------|----------------------|----------------------------|------------------------------|---------------|-----------------------------|---------------------------|---|------|---------------------------------------|-----|
|         |                   |                   |         |         |                      |                            | Steel<br>Only                | Whole<br>Pile |                             |                           | X-X                                     | X-X  | X-X                                   | X-X |
| 1BXN    | 953               | 158               | 103     | 12.7    | 711 x 15.0           | 208.0                      | 265                          | 864           | 5.74                        | 2210                      | 8705                                    | 845  |                                       |     |
| 1N      | 965               | 180               | 117     | 9.0     | 686 x 10.0           | 149.4                      | 191                          | 935           | 7.04                        | 2240                      | 9407                                    | 804  |                                       |     |
| 2N      | 965               | 247.5             | 164     | 9.7     | 660 x 12.5           | 173.3                      | 221                          | 1290          | 9.75                        | 2390                      | 20970                                   | 1279 |                                       |     |
| 3N      | 965               | 298               | 196     | 11.7    | 660 x 15.0           | 210.2                      | 268                          | 1555          | 11.73                       | 2470                      | 36840                                   | 1880 |                                       |     |
| 3NA     | 965               | 317.5             | 206     | 9.7     | 660 x 12.5           | 190.1                      | 242                          | 1613          | 12.60                       | 2550                      | 38528                                   | 1870 |                                       |     |
| 4N      | 965               | 345               | 220     | 14.0    | 660 x 15.0           | 242.8                      | 310                          | 1819          | 13.77                       | 2600                      | 58564                                   | 2662 |                                       |     |
| 5       | 850               | 331               | 204     | 17.0    | 533 x 20.0           | 285.4                      | 364                          | 1561          | 13.13                       | 2510                      | 62650                                   | 3071 |                                       |     |

\*Standard plate thickness have been used.

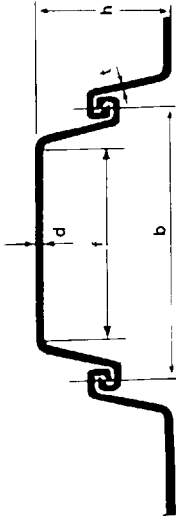
**Frodingham Straight Web Sections—Dimensions and Properties**



Section modulus of a single pile = 91.5 cm<sup>3</sup>

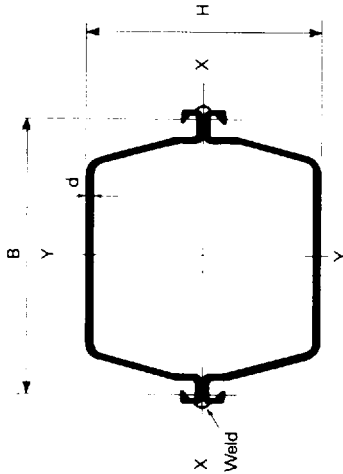
| Section | B<br>mm<br>(nominal) | t<br>mm | MASS                              |                                   | Standard<br>Junctions<br>per lin. metre | Minimum Ultimate Strength of<br>Interlock tonnes per metre |                |
|---------|----------------------|---------|-----------------------------------|-----------------------------------|---|--|----------------|
|         |                      |         | Per lineal<br>metre of Pile<br>kg | Per square<br>metre of<br>Wall kg |   | Grade 43A<br>Steel   | ASTM –<br>A328 |
| SW-1    | 413                  | 9.5     | 55.3                              | 134.0                             | 83.6kg/m                                | 285  | 299            |
| SW-1A   | 413                  | 12.7    | 63.8                              | 154.5                             | 96.3kg/m                                | 285  | 299            |
|         |                      |         |                                   |                                   |   | Grade 50A<br>Steel   | 384<br>384     |

**LARSEN STEEL SHEET PILING**  
**Dimensions and Properties**



| Section | b<br>mm<br>(nominal) | h<br>mm<br>(nominal) | d<br>mm | t<br>mm<br>(nominal) | f<br>Flat of Pan<br>mm | Sectional<br>Area<br>cm <sup>2</sup><br>per metre<br>of wall | Mass                      |                                   | Combined<br>Moment<br>of Inertia<br>cm <sup>4</sup><br>per metre | Section<br>Modulus<br>cm <sup>3</sup><br>per metre |
|---------|----------------------|----------------------|---------|----------------------|------------------------|--|---------------------------|-----------------------------------|--|--|
|         |                      |                      |         |                      |                        |  | kg per<br>linear<br>metre | kg per<br>sq.<br>metre<br>of wall |  |  |
| 6W      | 525                  | 212                  | 7.8     | 6.4                  | 331                    | 108  | 44.7                      | 85.1                              | 6459   | 610  |
| 9W      | 525                  | 260                  | 8.9     | 6.4                  | 343                    | 124  | 51.0                      | 97.1                              | 11726  | 902  |
| 12W     | 525                  | 306                  | 9.0     | 8.5                  | 343                    | 147  | 60.4                      | 115.1                             | 18345  | 1199   |
| 16W     | 525                  | 348                  | 10.5    | 8.6                  | 341                    | 166  | 68.3                      | 130.1                             | 27857  | 1601   |
| 20W     | 525                  | 400                  | 11.3    | 9.2                  | 333                    | 188  | 77.3                      | 147.2                             | 40180  | 2009   |
| 25W     | 525                  | 454                  | 12.1    | 10.5                 | 317                    | 213  | 87.9                      | 167.4                             | 56727  | 2499   |
| 32W     | 525                  | 454                  | 17.0    | 10.5                 | 317                    | 252  | 103.6                     | 197.4                             | 73003  | 3216   |
| 3       | 400                  | 248                  | 14.1    | 8.5                  | 253                    | 198  | 62.2                      | 155.5                             | 16980  | 1360   |
| 4A      | 400                  | 381                  | 15.7    | 9.6                  | 219                    | 236  | 74.0                      | 185.1                             | 44916  | 2360   |
| 6       | 420                  | 440                  | 22.0    | 14.0                 | 248                    | 370  | 122.0                     | 290.5                             | 92452  | 4200   |
| 6       | 420                  | 440                  | 25.4    | 14.0                 | 251                    | 397  | 131.0                     | 311.8                             | 102861   | 4675   |
| 6       | 420                  | 440                  | 28.6    | 14.0                 | 251                    | 421  | 138.7                     | 330.2                             | 111450   | 5066   |

**Larsen Box Piles—Dimensions and Properties**



| Section     | B<br>mm<br>nom. | H<br>mm<br>nom. | d<br>mm | Mass<br>per<br>metre<br>kg | Section Area<br>cm <sup>2</sup> |               | Least<br>Rad. of<br>Gyr.<br>cm | Approx.<br>Perim.<br>mm | Moment of Inertia<br>cm <sup>4</sup> |              | Section Modulus<br>cm <sup>3</sup> |              |
|-------------|-----------------|-----------------|---------|----------------------------|---------------------------------|---------------|--------------------------------|-------------------------|--------------------------------------|--------------|------------------------------------|--------------|
|             |                 |                 |         |                            | Steel<br>only                   | Whole<br>Pile |                                |                         | About<br>X-X                         | About<br>Y-Y | About<br>X-X                       | About<br>Y-Y |
| 6W          | 525             | 252             | 7.8     | 89.4                       | 113.8                           | 1122          | 9.33                           | 1652                    | 10028                                | 39280        | 796                                | 1400         |
| 9W          | 525             | 300             | 8.9     | 102.0                      | 129.9                           | 1344          | 11.43                          | 1748                    | 16976                                | 43812        | 1132                               | 1562         |
| 12W         | 525             | 349             | 9.0     | 120.8                      | 153.9                           | 1589          | 13.00                          | 1872                    | 25992                                | 55442        | 1490                               | 1970         |
| 16W         | 525             | 391             | 10.5    | 136.6                      | 174.0                           | 1776          | 14.80                          | 1952                    | 38126                                | 60920        | 1950                               | 2164         |
| 20W         | 525             | 447             | 11.3    | 154.6                      | 196.9                           | 2005          | 16.63                          | 2084                    | 54474                                | 70120        | 2438                               | 2482         |
| 25W         | 525             | 502             | 12.1    | 175.8                      | 223.9                           | 2221          | 18.33                          | 2164                    | 75240                                | 80082        | 2998                               | 2830         |
| 32W         | 525             | 502             | 17.0    | 207.3                      | 264.1                           | 2224          | 18.02                          | 2168                    | 96584                                | 85806        | 3848                               | 3032         |
| 3           | 400             | 296             | 14.1    | 124.4                      | 158.6                           | 1020          | 11.22                          | 1596                    | 19954                                | 30559        | 1348                               | 1399         |
| 4A          | 400             | 428             | 15.7    | 148.0                      | 188.7                           | 1413          | 13.82                          | 1772                    | 47055                                | 36039        | 2199                               | 1649         |
| 6 (122kg)   | 420             | 502             | 22.0    | 244.0                      | 310.6                           | 1794          | 14.77                          | 2080                    | 106780                               | 67756        | 4237                               | 2920         |
| 6 (131kg)   | 420             | 502             | 25.4    | 262.0                      | 333.6                           | 1794          | 14.47                          | 2080                    | 118588                               | 69859        | 4725                               | 3011         |
| 6 (138.7kg) | 420             | 502             | 28.6    | 277.4                      | 353.2                           | 1794          | 14.27                          | 2080                    | 128448                               | 71392        | 5117                               | 3077         |

The piling information on pp 1194-1203 is extracted from *Piling Handbook* 6th Edn, published by British Steel General Steels, 1988.

1204 *Floor plates*

Ultimate load capacity (kN/m<sup>2</sup>) for floor plates simply supported on two edges stressed to 275 N/mm<sup>2</sup>

| Thickness on plain mm | Span (mm) |       |       |       |       |       |       |       |
|-----------------------|-----------|-------|-------|-------|-------|-------|-------|-------|
|                       | 600       | 800   | 1000  | 1200  | 1400  | 1600  | 1800  | 2000  |
| 4.5                   | 20.48     | 11.62 | 7.45  | 5.17  | 3.80  | 2.95  | 2.28  | 1.87  |
| 6.0                   | 36.77     | 20.68 | 13.28 | 9.20  | 6.73  | 5.20  | 4.07  | 3.30  |
| 8.0                   | 65.40     | 36.87 | 23.48 | 16.38 | 11.97 | 9.23  | 7.23  | 5.93  |
| 10.0                  | 102.03    | 57.42 | 36.67 | 25.55 | 18.70 | 14.45 | 11.30 | 9.25  |
| 12.5                  | 159.70    | 89.85 | 57.40 | 39.98 | 29.27 | 22.62 | 17.68 | 14.50 |

*Stiffeners should be used for spans in excess of 1100 mm to avoid excessive deflections.*

Ultimate load capacity (kN/m<sup>2</sup>) for floor plates simply supported on all four edges stressed to 275 N/mm<sup>2</sup> (Values obtained using Pounder's formula allowing corners to lift)

| Thickness on plain mm | Breadth B mm | Length (mm) |      |      |      |       |       |       |       |
|-----------------------|--------------|-------------|------|------|------|-------|-------|-------|-------|
|                       |              | 600         | 800  | 1000 | 1200 | 1400  | 1600  | 1800  | 2000  |
| 4.5                   | 600          | 34.9        | 25.5 | 22.7 | 21.7 | 21.2  | 21.0  | 20.8  | 20.8  |
|                       | 800          |             | 19.6 | 15.1 | 13.4 | 12.6  | 12.2  | 12.0  | 11.8  |
|                       | 1000         |             |      | 12.6 | 10.0 | 8.8   | 8.3   | 7.9   | 7.7   |
|                       | 1200         |             |      |      | 8.7  | 7.1   | 6.3   | 5.9   | 5.6   |
|                       | 1400         |             |      |      |      | 6.4   | 5.3   | 4.8   | 4.4   |
|                       | 1600         |             |      |      |      |       | 4.9   | 4.1   | 3.7   |
|                       | 1800         |             |      |      |      |       |       | 3.8   | 3.3   |
| 6.0                   | 600          | 62.1        | 45.3 | 40.4 | 38.5 | 37.7  | 37.3  | 37.0  | 36.9  |
|                       | 800          |             | 34.9 | 26.8 | 23.7 | 22.3  | 21.7  | 21.3  | 21.1  |
|                       | 1000         |             |      | 22.4 | 17.8 | 15.8  | 14.8  | 14.2  | 13.9  |
|                       | 1200         |             |      |      | 15.5 | 12.7  | 11.3  | 10.6  | 10.1  |
|                       | 1400         |             |      |      |      | 11.4  | 9.5   | 8.5   | 7.9   |
|                       | 1600         |             |      |      |      |       | 8.7   | 7.4   | 6.7   |
|                       | 1800         |             |      |      |      |       |       | 6.9   | 5.9   |
| 8.0                   | 600          | 110         | 80.6 | 71.1 | 68.4 | 67.0  | 66.2  | 65.8  | 65.6  |
|                       | 800          |             | 62.1 | 47.7 | 42.2 | 39.7  | 38.5  | 37.8  | 37.4  |
|                       | 1000         |             |      | 39.7 | 31.7 | 28.1  | 26.2  | 25.2  | 24.6  |
|                       | 1200         |             |      |      | 27.6 | 22.6  | 20.1  | 18.8  | 17.9  |
|                       | 1400         |             |      |      |      | 20.3  | 17.0  | 15.2  | 14.1  |
|                       | 1600         |             |      |      |      |       | 15.5  | 13.3  | 11.9  |
|                       | 1800         |             |      |      |      |       |       | 12.3  | 10.6  |
| 10.0                  | 600          | 172*        | 126* | 112* | 107* | 105*  | 103*  | 103*  | 103*  |
|                       | 800          |             | 97.0 | 74.5 | 65.9 | 62.1  | 60.1  | 59.1  | 58.5  |
|                       | 1000         |             |      | 62.1 | 49.5 | 43.9  | 41.0  | 39.4  | 38.5  |
|                       | 1200         |             |      |      | 43.1 | 35.4  | 31.5  | 29.3  | 28.0  |
|                       | 1400         |             |      |      |      | 31.7  | 26.6  | 23.8  | 22.1  |
|                       | 1600         |             |      |      |      |       | 24.3  | 20.7  | 18.6  |
|                       | 1800         |             |      |      |      |       |       | 19.2  | 16.6  |
| 12.5                  | 600          | 269*        | 197* | 175* | 167* | 163*  | 162*  | 161*  | 160*  |
|                       | 800          |             | 152  | 116* | 103* | 97.0* | 94.0* | 92.3* | 91.4* |
|                       | 1000         |             |      | 97.0 | 77.4 | 68.5  | 64.1  | 61.6  | 60.1  |
|                       | 1200         |             |      |      | 67.4 | 55.3  | 49.2  | 45.8  | 43.8  |
|                       | 1400         |             |      |      |      | 49.5  | 41.5  | 37.1  | 34.5  |
|                       | 1600         |             |      |      |      |       | 37.9  | 32.4  | 29.1  |
|                       | 1800         |             |      |      |      |       |       | 29.9  | 25.9  |

Ultimate load capacity (kN/m<sup>2</sup>) for floor plates fixed on all four edges stressed to 275 N/mm<sup>2</sup>

| Thickness on plain mm | Breadth B mm | Length (mm) |       |       |       |       |       |       |       |
|-----------------------|--------------|-------------|-------|-------|-------|-------|-------|-------|-------|
|                       |              | 600         | 800   | 1000  | 1200  | 1400  | 1600  | 1800  | 2000  |
| 4.5                   | 600          | 47.7*       | 36.8* | 33.5* | 32.2* | 31.6* | 31.4* | 31.2* | 31.1* |
|                       | 800          |             | 26.8  | 21.5* | 19.5* | 18.6* | 18.1* | 17.9* | 17.7* |
|                       | 1000         |             |       | 17.2* | 14.2* | 12.9* | 12.2* | 11.8* | 11.6* |
|                       | 1200         |             |       |       | 11.9  | 10.1  | 9.1   | 8.6   | 8.3   |
|                       | 1400         |             |       |       |       | 8.7   | 7.5   | 6.9   | 6.5   |
|                       | 1600         |             |       |       |       |       | 6.7   | 5.8   | 5.3   |
|                       | 1800         |             |       |       |       |       |       | 5.3   | 4.7   |
| 6.0                   | 600          | 84.8*       | 65.4* | 59.5* | 57.3* | 56.2* | 55.7* | 55.5* | 55.3* |
|                       | 800          |             | 47.7* | 38.3* | 34.7* | 33.1* | 32.2* | 31.7* | 31.5* |
|                       | 1000         |             |       | 30.5* | 25.3* | 22.9* | 21.7* | 21.0* | 20.6* |
|                       | 1200         |             |       |       | 21.2* | 18.0* | 16.3* | 15.4* | 14.9* |
|                       | 1400         |             |       |       |       | 15.6* | 13.4* | 12.3* | 11.6  |
|                       | 1600         |             |       |       |       |       | 11.9  | 10.4  | 9.5   |
|                       | 1800         |             |       |       |       |       |       | 9.4   | 8.3   |
| 8.0                   | 600          | 151*        | 116*  | 106*  | 102*  | 100*  | 99.1* | 98.6* | 98.3* |
|                       | 800          |             | 68.1* | 61.7* | 58.8* | 57.3* | 56.4* | 55.9* |       |
|                       | 1000         |             |       | 54.3* | 44.9* | 40.7* | 38.6* | 37.4* | 36.7* |
|                       | 1200         |             |       |       | 37.7* | 31.9* | 29.0* | 27.4* | 26.5* |
|                       | 1400         |             |       |       |       | 27.7* | 23.9* | 21.8* | 20.6* |
|                       | 1600         |             |       |       |       |       | 21.2* | 18.6* | 17.0* |
|                       | 1800         |             |       |       |       |       |       | 16.9* | 14.8* |
| 10.0                  | 600          | 236*        | 182*  | 165*  | 159*  | 156*  | 155*  | 154*  | 154*  |
|                       | 800          |             | 132*  | 106*  | 96.4* | 91.8* | 89.5* | 88.2* | 87.4* |
|                       | 1000         |             |       | 84.8* | 70.2* | 63.7* | 60.3* | 58.4* | 57.3* |
|                       | 1200         |             |       |       | 58.9* | 49.9* | 45.4* | 42.9* | 41.3* |
|                       | 1400         |             |       |       |       | 43.3* | 37.3* | 34.1* | 32.2* |
|                       | 1600         |             |       |       |       |       | 33.1* | 29.0* | 26.6* |
|                       | 1800         |             |       |       |       |       |       | 26.2* | 23.2* |
| 12.5                  | 600          | 368*        | 284*  | 258*  | 249*  | 244*  | 242*  | 241*  | 240*  |
|                       | 800          |             | 207*  | 166*  | 151*  | 144*  | 140*  | 138*  | 137*  |
|                       | 1000         |             |       | 132*  | 110*  | 99.5* | 94.2* | 91.2* | 89.5* |
|                       | 1200         |             |       |       | 92.0* | 77.9* | 70.9* | 67.0* | 64.6* |
|                       | 1400         |             |       |       |       | 67.6* | 58.3* | 53.3* | 50.3* |
|                       | 1600         |             |       |       |       |       | 51.8* | 45.3* | 41.6* |
|                       | 1800         |             |       |       |       |       |       | 40.9* | 36.2* |

**Note on tables:**

Values without an asterisk cause deflection greater than B/100 at serviceability, assuming that the only dead load present is due to self-weight.



# STEELWORK IN FIRE

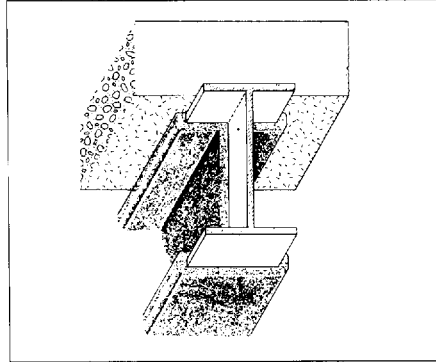
## INFORMATION SHEET

**MO1**

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below.

### SPRAYED PROTECTION

**UP TO 4 HRS**



#### METHOD

Fire protective insulation can be applied by spraying to any type of steel member. Most products can achieve up to 4 hour rating.

#### PRINCIPLE

Insulation reduces the heating rate of a steel member so that its limiting temperature is not exceeded during the required fire resistance period. The protection material thickness necessary depends on the section factor ( $H_p/A$ ) of the member and the fire rating required.

#### ADVANTAGES

- a) Low cost
- b) Rapid application
- c) Easy to cover complex details
- d) Often applied to non-primed steelwork
- e) Some products may be suitable for external use

#### LIMITATIONS (check with manufacturer)

- a) Appearance may be inadequate for visible members
- b) Overspray may need masking or shielding
- c) Primer, if used, must be compatible

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FOR MORE DETAILED INFORMATION SEE:-  
"Fire protection of Structural Steel in Building"  
published jointly by:  
ASFPCM - (0252 336318) and  
The Steel Construction Institute - (0344 23345)

Sheet Code  
ISF/M01  
January 1991

## **PROTECTION THICKNESS**

Thickness recommendations given in "Fire Protection of Structural Steel in Building" have normally been derived from fire tests on orthodox H or I rolled sections. For other sections the recommended thickness for a given section factor and fire rating should be modified as follows:

### **CASTELLATED SECTIONS**

The thickness of fire protection material on a castellated section should be 20% greater than that required for the section from which it was cut.

### **HOLLOW SECTIONS**

For spray applied fire protection materials the recommended thickness ( $t$ ) should be increased as follows

For section factor ( $H_p/A$ ) less than 250  
modified thickness =  $t [1 + (H_p/A)/1000]$

For section factor ( $H_p/A$ ) 250 or over  
modified thickness =  $1.25 \times t$

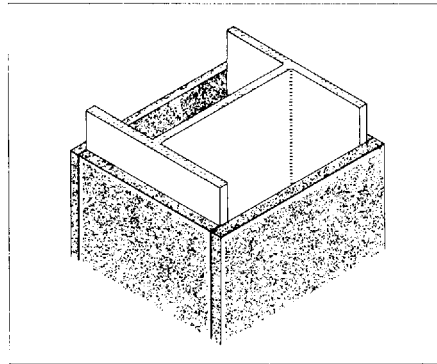
# STEELWORK IN FIRE INFORMATION SHEET

MO2

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below.

## BOARD PROTECTION

**UP TO 4 HRS**



### METHOD

Fire protective insulation can be applied by fixing boards to any type of steel member. Most products can achieve up to 4 hour rating. Fixing methods vary.

### PRINCIPLE

Insulation reduces the heating rate of a steel member so that its limiting temperature is not exceeded during the required fire resistance period. The protection board thickness necessary depends on the section factor of the member ( $H_p/A$ ) and the fire rating required.

### ADVANTAGES

- a) Boxed appearance suitable for visible members
- b) Clean dry fixing
- c) Factory manufactured, guaranteed thickness
- d) Often applied to non-primed steelwork
- e) Some products may be suitable for external use

### LIMITATIONS (check with manufacturer)

- a) Require fitting around complex details
- b) May be more expensive and slower to fix than sprays

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FOR MORE DETAILED INFORMATION SEE:-  
"Fire protection of Structural Steel in Building"  
published jointly by:  
ASFPCM - (0252 336318) and  
The Steel Construction Institute - (0344 23345)

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ISF/M02  
January 1991

## **PROTECTION THICKNESS**

Thickness recommendations given in "Fire Protection of Structural Steel in Building" have normally been derived from fire tests on orthodox H or I rolled sections. For other sections the recommended thickness for a given section factor and fire rating should be modified as follows:

## **CASTELLATED SECTIONS**

The thickness of fire protection material on a castellated section should be 20% greater than that required for the section from which it was cut.

# STEELWORK IN FIRE

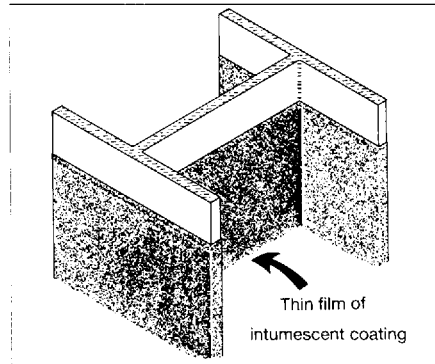
## INFORMATION SHEET

**M03**

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below

### INTUMESCENT COATINGS

**UP TO 2 HRS**



#### METHOD

Most intumescent coatings can be applied by spray, brush or roller and can achieve up to 1 hour fire resistance on fully exposed steel members. Some thick film products can achieve up to 2 hours fire resistance on some section sizes.

#### PRINCIPLE

Insulation is created by swelling of the coating at elevated temperatures to generate a foam like char. This reduces the heating rate so that the limiting temperature of the steel member is not exceeded during the required fire resistance period. The coating thickness necessary depends on the section factor ( $H_p/A$ ) and the fire rating required.

#### ADVANTAGES

- a) Decorative finish
- b) Rapid application
- c) Easy to cover complex details
- d) Easy post protection fixings to steelwork eg service hangers

#### LIMITATIONS (check with manufacturer)

- a) May be suitable for dry internal environments only
- b) May be more expensive than sprayed insulation
- c) May require blast cleaned surface and compatible primer

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FOR MORE DETAILED INFORMATION SEE:-  
"Fire Protection of Structural Steel in Building"  
published jointly by:  
ASFCM - (0252 336318) and  
The Steel Construction Institute - Tel: 0344 23345

Sheet Code  
ISF/M03  
January 1991

## **PROTECTION THICKNESS**

Thickness recommendations given in "Fire Protection of Structural Steel in Building" have normally been derived from fire tests on orthodox H or I rolled sections. For other sections the recommended thickness for a given section factor and fire rating should be modified as follows:

### **CASTELLATED SECTIONS**

The thickness of fire protection material on a castellated section should be 20% greater than that required for the section from which it was cut.

### **HOLLOW SECTIONS**

For intumescent materials applied to hollow sections the manufacturers should have carried out separate tests and appraisal.

# STEELWORK IN FIRE

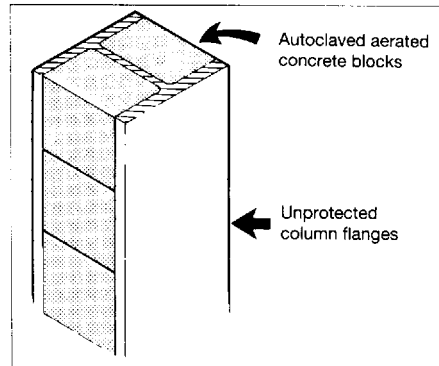
## INFORMATION SHEET

MO4

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below

### BLOCK - FILLED COLUMNS

**30 MINUTES**



#### METHOD

Unprotected universal sections with section factors up to  $69m^{-1}$  (see overleaf) can attain 30 minutes fire resistance by fitting autoclaved aerated concrete blocks between the flanges tied to the web at approximately 1m intervals.

#### PRINCIPLE

Partial exposure of steel members affects fire resistance in two ways-

Firstly the reduction of exposed surface area reduces the rate of heating by radiation and thus increases the time to reach failure temperature.

Secondly, if fire exposure creates both hot and cold regions in the cross section, plastic yielding occurs in the hot region and load is transferred to the stronger cooler region. Thus a non-uniformly heated section has a higher fire resistance than one heated evenly.

#### ADVANTAGES

- a) Reduced cost - compared with total encasement with insulation
- b) More slender finished columns occupy less floor space
- c) Good durability - high resistance to impact and abrasion damage

#### LIMITATIONS

With unprotected steel the method is limited to 30 minute fire rating.

When higher ratings are required exposed steel must be treated with the full insulation or intumescent coating thickness recommended for the higher rating.

This method should not be used when the blockwork also forms a separating wall. In this case the column will be heated on one side only and thermal bowing may cause the wall to crack or collapse. In such cases the flange(s) should be protected. Alternatively, if the limit of wall deformation is known, the bowing can be calculated to ensure no integrity failure.

FOR MORE DETAILED INFORMATION SEE:-  
BRE Digest 317, Building Research Advisory Service,  
Fire Research Station, Borehamwood,  
Herts WD6 2BL  
Telephone 081 953 6177

Sheet Code  
ISF/M04  
January 1991

**METHODS OF ACHIEVING 30 MINUTES FIRE RESISTANCE**

| COLUMN SECTIONS - AXIALLY LOADED <sup>(1)</sup> FREE STANDING |   |  |
|---|---|--|
| SERIAL SIZE<br>mm   | MASS/METRE<br>kg  | PROTECTION METHOD<br>RECOMMENDED   |
| 305 x 406   | 393 and over  | No fire protection required  |
| 356 x 406<br>305 x 305<br>254 x 254<br>203 x 203<br>203 x 203 | 340 and under<br>All weights<br>All weights<br>52 and over<br>46 <sup>(2)</sup> | Block filling with autoclaved<br>aerated concrete blocks                   |
| 152 x 203   | All weights   | Apply fire protection<br>material as per manufacturers'<br>recommendations |

| BEAM SECTIONS ACTING AS PORTAL FRAME STANCHIONS <sup>(1)</sup>   |   |  |
|--|---|--|
| 914 x 419<br>914 x 305<br>*610 x 305   | All weights<br>289<br>238   | No fire protection required  |
| *914 x 305<br>838 x 292<br>762 x 267<br>686 x 254<br>*610 x 305<br>610 x 229<br>533 x 210<br>457 x 191<br>457 x 152<br>406 x 178<br>356 x 171<br>305 x 165<br>305 x 127<br>254 x 146 | 253 and under<br>All weights<br>All weights<br>All weights<br>179 and under<br>All weights<br>All weights<br>All weights<br>60 and over<br>60 and over<br>57 and over<br>54<br>48<br>43 | Block filling with autoclaved<br>aerated concrete blocks                   |
| Other beam sizes   |   | Apply fire protection<br>material as per manufacturers'<br>recommendations |

Notes:

- 1) This table applies to sections designed to BS 5950:Part 1:1990 provided the load factor ( $\gamma_f$ ) does not exceed 1.5
- 2) To achieve 30 min fire resistance, a 203 x 203 x 46 kg/m column with blocked in webs should be loaded only up to 80% of the maximum allowable per BS 449: Part 2: 1969 or BS 5950: Part 1: 1990
- \*3) The table revises BRE Digest 317 (1986) in accordance with BS 5950: Part 8: 1990



# STEELWORK IN FIRE

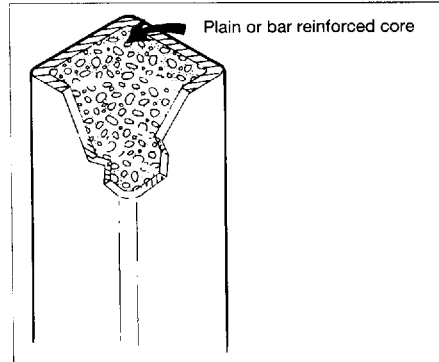
## INFORMATION SHEET

**M05**

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below

### CONCRETE FILLED HOLLOW COLUMNS

**UP TO 2 HRS**



#### METHOD

Unprotected square or rectangular hollow sections can attain up to 120 minutes fire resistance by filling with plain, fibre reinforced or bar reinforced concrete.

#### PRINCIPLE

Heat flows through the steel wall into the concrete core which being a poor conductor heats up slowly.

As the temperature increases the steel yield strength reduces and the load is progressively transferred into the concrete core.

The steel acts as a restraint to the concrete preventing spalling and hence the rate of degradation of the concrete.

#### ADVANTAGES

- a) Steel acts as a permanent shuttering
- b) More slender finished columns occupy less floor space
- c) Good durability - high resistance to impact and abrasion damage

#### LIMITATIONS

- a) A minimum column size of 140mm x 140mm or 100mm x 200mm is required for plain or fibre reinforced sections.
- b) A minimum column size of 200mm x 200mm. or 150mm x 250mm is required for bar reinforced sections.
- c) CHS columns are not included due to insufficient data at present.

FOR MORE DETAILED INFORMATION SEE:-  
BS 5950 Part 8  
Concrete filled column design manual TD 296 from  
British Steel General Steels Welded Tubes (0536 402121)

Sheet Code  
ISF/M05  
January 1991

## CONCRETE FILLED RECTANGULAR HOLLOW SECTIONS

The fire resistance of externally unprotected concrete filled hollow sections is dependent on three main variables.

- The concrete strength selected
- The ratio of axial load and moment
- The addition of fibre or bar reinforcement

## CONCRETE STRENGTH

The core capacity and hence its fire resistance is directly related to the concrete strength selected.

## AXIAL LOAD AND MOMENT

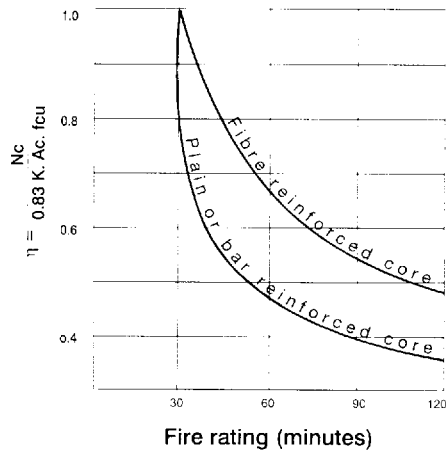
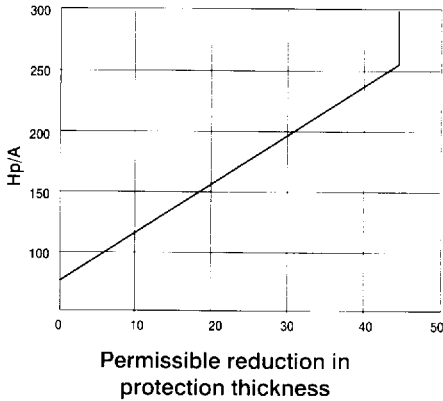
Plain concrete does not perform well in tension and when subject to axial load and moment it is necessary to produce a resultant compressive stress in the core.

## REINFORCEMENT

Fibre reinforcement will enhance the core axial capacity yet retain the advantage of filling into a section without obstructions. Bar reinforcement will enhance the moment capacity.

## COMBINED PROTECTION

As an alternative the concrete filled section can be designed for full factored loads and provided with external fire protection. The thickness of the external fire protection is assessed as for an unfilled section, and, due to the effect of the core, the thickness can be reduced.



# STEELWORK IN FIRE

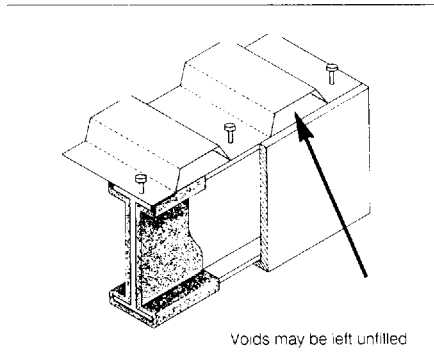
## INFORMATION SHEET

**M06**

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below.

### COMPOSITE SLABS WITH PROFILED METAL DECK WITH UNFILLED VOIDS

**UP TO 2 HRS**



#### METHOD

In composite construction using profiled metal deck floors it is unnecessary to fill the deck voids above the top flange for any fire resistance period using dovetail deck, or up to 90 minutes using trapezoidal deck

#### PRINCIPLE

In a composite beam/slab member the neutral axis in bending lies in, or close to, the beam top flange. Thus the top flange makes little significant contribution to the structural behaviour of the total composite system and its temperature can be allowed to increase with little detriment to performance in fire.

#### ADVANTAGES

- a) Saving in time on site
- b) Saving in cost for filling voids
- c) It is unnecessary to build up the full thickness of protection on toes of upper flange
- d) Void filling is unnecessary when using dovetail deck

#### LIMITATIONS

Voids must be filled where:-

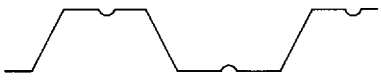
- a) Trapezoidal deck is used for fire ratings over 90 minutes
- b) Trapezoidal deck is used in non-composite construction
- c) Any type of deck crosses a fire separating wall


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FOR MORE DETAILED INFORMATION SEE:-  
Technical Report 087  
"Fire resistance of composite beams"  
The Steel Construction Institute  
(0344 23345)

Sheet Code  
ISF/M06  
January 1991

## COMPOSITE BEAMS - UNFILLED VOIDS

| TRAPEZOIDAL DECK  |                         |   |   |            |
|---|-------------------------|---|---|------------|
|  |                         |   |   |            |
| Construction  | Fire Protection On Beam | Fire Resistance (minutes)   |   |            |
|   |                         | Up to 60  | 90  | Over 90    |
| Composite Beams   | BOARD or SPRAY          | No increase in thickness*   | Increase thickness by 10% (or use thickness* appropriate to beam $H_p/A + 15\%$ whichever is less)  | Fill voids |
|   | INTUMESCENT             | Increase thickness* by 20% (or use thickness* appropriate to beam $H_p/A + 30\%$ whichever is less) | Increase thickness* by 30% (or use thickness* appropriate to beam $H_p/A + 50\%$ whichever is less) | Fill voids |
| Non-Composite Beams   | All types               | Fill Voids  |   |            |

| DOVETAIL DECK   |                         |   |
|---|-------------------------|---|
|  |                         |   |
| Construction  | Fire Protection On Beam | Fire Resistance (minutes)                                   |
| Composite or Non-composite Beams  | All types               | Voids may be left unfilled for all fire resistance periods. |

\* Thickness is the board, spray or intumescent thickness given for 30, 60 or 90 minutes rating in "Fire Protection for Structural Steel in Buildings" published by ASFCM (0252 336318) and The Steel Construction Institute (0344 23345)

# STEELWORK IN FIRE

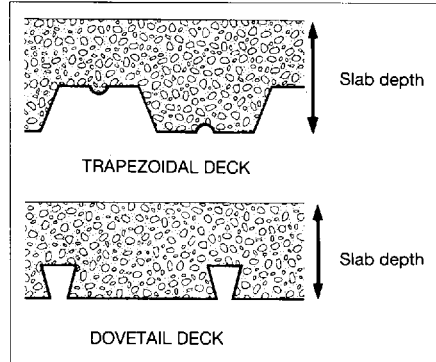
## INFORMATION SHEET

MO7

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below.

### COMPOSITE SLABS WITH PROFILED METAL DECK

UP TO 2 HRS



#### METHOD

Fire resistance of composite slabs up to 90 mins can be achieved using normal A142 mesh reinforcement. This can be increased to 120 mins if heavier mesh is used and the slab depth increased (see overleaf).

Other cases outside the limits overleaf can be evaluated by the "Fire Engineering Method" (See below)

#### PRINCIPLE

Mesh reinforcement, which is not designed to act structurally under normal conditions, makes a significant contribution to structural continuity in fire.

#### ADVANTAGES

- a) Standard mesh, without additional reinforcing bars, may be used.
- b) No fire protection is required on the deck soffit.


#### LIMITATIONS

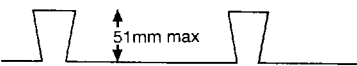
- a) Applies only to slabs designed to BS5950 Part 4
- b) Mesh overlaps should exceed 50 times bar diameters
- c) Mesh bar ductility should exceed 12% elongation in tension (to BS 4449)
- d) Mesh should lie between 20 & 45mm from slab upper surface
- e) Imposed load should not exceed 6.7 kN/m<sup>2</sup> (including finishes)

FOR MORE DETAILED INFORMATION SEE:-  
 SCI Publication 059  
 "Fire resistance of composite floors with steel decking."  
 The Steel Construction Institute - (0344 23345) and  
 CIRIA Special publication 42 CIRIA (071 222 8891)

Sheet Code  
 ISF/M07  
 January 1991

## FIRE RESISTANT COMPOSITE SLABS

| TRAPEZOIDAL DECK |                 |                    |                    |                    |   |
|------------------|-----------------|--------------------|--------------------|--------------------|---|
|                  |                 |                    |                    |                    |  |
| Maximum Span (m) | Fire Rating (h) | Minimum Dimensions |                    |                    | Mesh Size   |
|                  |                 | Sheet thickness    | Slab depth (mm)    |                    |   |
|                  |                 |                    | NWC <sup>(2)</sup> | LWC <sup>(3)</sup> |   |
| 2.7              | 1               | 0.8                | 130                | 120                | A142  |
| 3.0              | 1               | 0.9                | 130                | 120                | A142  |
|                  | 1½              | 0.9                | 140                | 130                | A142  |
|                  | 2               | 0.9                | 155                | 140                | A193  |
| 3.6              | 1               | 1.0                | 130                | 120                | A193  |
|                  | 1½              | 1.2                | 140                | 130                | A193  |
|                  | 2               | 1.2                | 155                | 140                | A252  |

| DOVETAIL DECK    |                 |                    |                    |                    |   |
|------------------|-----------------|--------------------|--------------------|--------------------|---|
|                  |                 |                    |                    |                    |  |
| Maximum Span (m) | Fire Rating (h) | Minimum Dimensions |                    |                    | Mesh Size   |
|                  |                 | Sheet thickness    | Slab depth (mm)    |                    |   |
|                  |                 |                    | NWC <sup>(2)</sup> | LWC <sup>(3)</sup> |   |
| 2.5              | 1               | 0.8                | 100                | 100                | A142  |
| 3.0              | 1½              | 0.8                | 110                | 105                | A142  |
|                  | 1               | 0.9                | 120                | 110                | A142  |
|                  | 1½              | 0.9                | 130                | 120                | A142  |
| 3.6              | 2               | 0.9                | 140                | 130                | A193  |
|                  | 1               | 1.0                | 125                | 120                | A193  |
|                  | 1½              | 1.2                | 135                | 125                | A193  |
|                  | 2               | 1.2                | 145                | 130                | A252  |

1) Imposed load not exceeding 5kN/m<sup>2</sup> (+ 1.7kN/m<sup>2</sup> ceiling and services)

2) NWC = Normal weight concrete

3) LWC = Light weight concrete

NOTE: Minimum slab depths given in BS 5950 part 8 are to satisfy the insulation criterion only. Figures given in the table above incorporate a strength criterion also and thus may exceed the minimum depth given in the code.

# STEELWORK IN FIRE

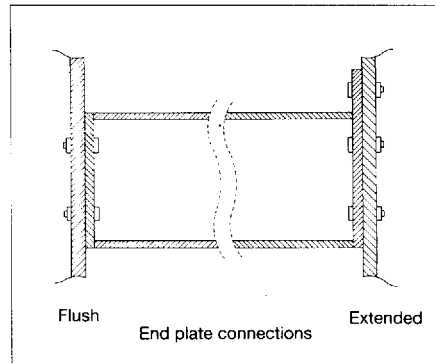
## INFORMATION SHEET

M08

This series of information sheets is intended to illustrate methods of achieving fire resistance in steel structures. It should not be used for design without consulting detailed design guidance referenced below.

### BEAM - COLUMN CONNECTIONS

**30 MINUTES**



#### METHOD

Most beams can achieve 30 minutes fire resistance without additional protection by mobilising the moment capacity of the connections to reduce the effective load ratio of the beam at the fire limit state (see overleaf).

#### PRINCIPLE

It is known that so - called "simple" connections can resist moments but this is usually ignored in design. At the fire limit state large rotations are permitted and moments may be transferred to adjacent members. Reduction of moment in the beam increases the limiting temperature and thus the fire resistance of the beam.

#### ADVANTAGES

- a) Elimination of fire protection for 30 minutes rating of most beams.
- b) Reduction of fire protection thickness for higher ratings.

#### LIMITATIONS

- a) Applies only to end plate connections designed to be "simple" in normal design
- b) Does not apply to continuous frames (eg portal frames)
- c) Bolt sizes are M16, 20 or 24 in grades 4.6 or 8.8
- d) Applies only to internal beams with span variation less than 25%
- e) Special considerations are required for edge columns or for beam-beam connections which do not align through the web

FOR MORE DETAILED INFORMATION SEE:-  
 SCI Technical Report 086  
 "Enhancement of fire resistance by beam  
 column connections" published by  
 The Steel Construction Institute (0344 23345)

Sheet Code  
 ISF/M08  
 January 1991

## INCREASE IN LIMITING TEMPERATURE

Connections provide an increase in limiting temperature over that of a simply supported beam. The limiting temperature of the simply supported beam is a function of the load ratio. The increase in limiting temperatures due to the connection has been determined conservatively as;

For flush end plates  $T^{\circ}\text{C} = 135 \text{ Mc/Mp}$

For extended end plates  $T^{\circ}\text{C} = 160 \text{ Mc/Mp}$

Valid over a range of  $0.15 < \text{Mc/Mp} < 0.7$

Where  $\text{Mc}$  = "cold" moment capacity of the connection (obtained by calculation)  
 $\text{Mp}$  = "cold" moment capacity of the beam

### MAXIMUM SECTION FACTORS FOR 30 MINUTES FIRE RESISTANCE OF INTERNAL NON - COMPOSITE BEAMS.

| CONNECTION TYPE                                 | APPLIED LOAD RATIO OF SIMPLE BEAM | EFFECTIVE LOAD RATIO | LIMITING TEMPERATURE OF BEAM (°C) | MAXIMUM SECTION FACTOR (m <sup>-1</sup> ) OF BEAM |
|---|-----------------------------------|----------------------|-----------------------------------|---|
| Extended end plates<br>Moment capacity > 0.6 Mp | 0.40                              | 0.20                 | 780                               | 230   |
|   | 0.45                              | 0.23                 | 770                               | 210   |
|   | 0.50                              | 0.25                 | 755                               | 180   |
|   | 0.55                              | 0.28                 | 735                               | 120   |
| Flush end plates<br>Moments capacity > 0.3 Mp   | 0.35                              | 0.24                 | 765                               | 200   |
|   | 0.40                              | 0.27                 | 745                               | 150   |
|   | 0.45                              | 0.30                 | 725                               | 110   |
|   | 0.50                              | 0.34                 | 710                               | 105   |
|   | 0.55                              | 0.37                 | 695                               | 95  |

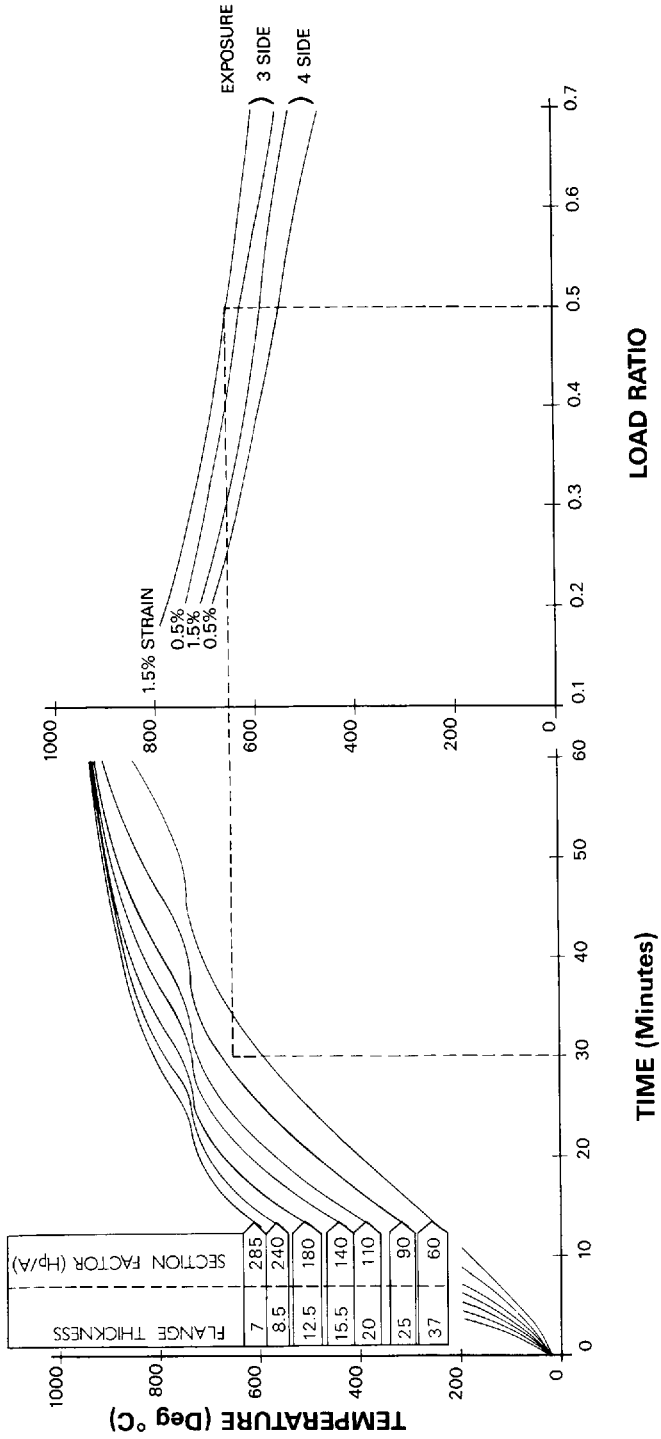
Notes:

- 1) Beam supporting concrete slabs
- 2) Internal beam connected to internal column by connections of the above type
- 3) Load ratio takes into account reduced load factors at limit state
- 4) Capacity of bolt group in shear is taken as 50% of their design capacity when determining their normal loadcarrying capacity





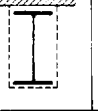
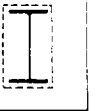
**LIMITING TEMPERATURE - BEAMS**

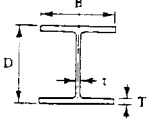

**DESIGN TEMPERATURE**







Limiting temperatures for design of protected and unprotected members

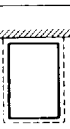
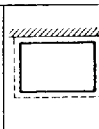
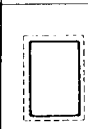
| Case No. | Members in compression   | Load ratio |     |     |     |     |     |
|----------|--|------------|-----|-----|-----|-----|-----|
|          |  | 0.7        | 0.6 | 0.5 | 0.4 | 0.3 | 0.2 |
|          | Uniform heating on all faces; braced members in simple construction:           |            |     |     |     |     |     |
| (1)      | Slenderness ratio $\leq 70$  | 510        | 540 | 580 | 615 | 655 | 710 |
| (2)      | Slenderness ratio $\leq 180$   | 460        | 510 | 545 | 590 | 635 | 635 |
|          | <b>Members in bending</b>  |            |     |     |     |     |     |
|          | Supporting concrete or composite deck floors:                                  |            |     |     |     |     |     |
| (3)      | Unprotected members, or protected members complying with clause 2.3 (a) or (b) | 590        | 620 | 650 | 680 | 725 | 780 |
| (4)      | Other protected members  | 540        | 585 | 625 | 655 | 700 | 745 |
|          | Not supporting concrete floors:  |            |     |     |     |     |     |
| (5)      | Unprotected members, or protected members complying with Clause 2.3 (a) or (b) | 520        | 555 | 585 | 620 | 660 | 745 |
| (6)      | Other protected members  | 460        | 510 | 545 | 590 | 635 | 690 |
|          | <b>Members in tension</b>  |            |     |     |     |     |     |
| (7)      | All cases  | 460        | 510 | 545 | 590 | 635 | 690 |

| Universal beams |                    |                    |           |          |                        | Section factor $H_p/A$  |   |   |  |          |
|-----------------|--------------------|--------------------|-----------|----------|------------------------|---|---|---|--|----------|
|                 |                    |                    |           |          |                        | Profile   |   | Box   |  |          |
|                 |                    |                    |           |          |                        | 3 sides   | 4 sides   | 3 sides   | 4 sides  |          |
| Designation     | Depth of section D | Width of section B | Thickness |          | Area of section $cm^2$ |  |  |  |  |          |
| Serial size     | Mass per metre     | Web t              | Flange T  | $m^{-1}$ |                        |   |   |   |  | $m^{-1}$ |
| mm              | kg                 | mm                 | mm        | mm       | mm                     | $m^{-1}$  | $m^{-1}$  | $m^{-1}$  | $m^{-1}$   |          |
| 914x419         | 388                | 920.5              | 420.5     | 21.5     | 36.6                   | 494.4   | 60  | 70  | 45   | 55       |
|                 | 343                | 911.4              | 418.5     | 19.4     | 32.0                   | 437.4   | 70  | 80  | 50   | 60       |
| 914x305         | 289                | 926.6              | 307.8     | 19.6     | 32.0                   | 368.8   | 75  | 80  | 60   | 65       |
|                 | 253                | 918.5              | 305.5     | 17.3     | 27.9                   | 322.8   | 85  | 95  | 65   | 75       |
|                 | 224                | 910.3              | 304.1     | 15.9     | 23.9                   | 285.2   | 95  | 105   | 75   | 85       |
|                 | 201                | 903                | 303.4     | 15.2     | 20.2                   | 256.4   | 105   | 115   | 80   | 95       |
| 838x292         | 226                | 850.9              | 293.8     | 16.1     | 26.8                   | 288.7   | 85  | 95  | 70   | 80       |
|                 | 194                | 840.7              | 292.4     | 14.7     | 21.7                   | 247.1   | 100   | 115   | 90   | 90       |
|                 | 176                | 834.9              | 291.6     | 14       | 18.8                   | 224.1   | 110   | 125   | 90   | 100      |
| 762x267         | 197                | 769.6              | 268       | 15.6     | 25.4                   | 250.7   | 90  | 100   | 70   | 85       |
|                 | 173                | 762                | 266.7     | 14.3     | 21.6                   | 220.4   | 105   | 115   | 80   | 95       |
|                 | 147                | 753.9              | 265.3     | 12.9     | 17.5                   | 188.0   | 120   | 135   | 95   | 110      |
| 686x254         | 170                | 692.9              | 255.8     | 14.5     | 23.7                   | 216.5   | 95  | 110   | 75   | 90       |
|                 | 152                | 687.6              | 254.5     | 13.2     | 21.0                   | 193.8   | 110   | 120   | 85   | 95       |
|                 | 140                | 683.5              | 253.7     | 12.4     | 19.0                   | 178.6   | 115   | 130   | 90   | 105      |
|                 | 125                | 677.9              | 253       | 11.7     | 16.2                   | 159.6   | 130   | 145   | 100  | 115      |
| 610x305         | 238                | 633                | 311.5     | 18.6     | 31.4                   | 303.7   | 70  | 80  | 50   | 60       |
|                 | 179                | 617.5              | 307       | 14.1     | 23.6                   | 227.9   | 90  | 105   | 70   | 80       |
|                 | 149                | 609.6              | 304.8     | 11.9     | 19.7                   | 190.1   | 110   | 125   | 80   | 95       |
| 610x229         | 140                | 617                | 230.1     | 13.1     | 22.1                   | 178.3   | 105   | 120   | 80   | 95       |
|                 | 125                | 611.9              | 229       | 11.9     | 19.6                   | 159.5   | 115   | 130   | 90   | 105      |
|                 | 113                | 607.3              | 228.2     | 11.2     | 17.3                   | 144.4   | 130   | 145   | 100  | 115      |
|                 | 101                | 602.2              | 227.6     | 10.6     | 14.8                   | 129.1   | 145   | 160   | 110  | 130      |
| 533x210         | 122                | 544.6              | 211.9     | 12.8     | 21.3                   | 155.7   | 110   | 120   | 85   | 95       |
|                 | 109                | 539.5              | 210.7     | 11.6     | 18.8                   | 138.5   | 120   | 135   | 95   | 110      |
|                 | 101                | 536.7              | 210.1     | 10.9     | 17.4                   | 129.7   | 130   | 145   | 100  | 115      |
|                 | 92                 | 533.1              | 209.3     | 10.2     | 15.6                   | 117.7   | 140   | 160   | 110  | 125      |
|                 | 82                 | 528.3              | 208.7     | 9.6      | 13.2                   | 104.4   | 155   | 175   | 120  | 140      |
| 457x191         | 98                 | 467.4              | 192.8     | 11.4     | 19.6                   | 125.2   | 120   | 135   | 90   | 105      |
|                 | 89                 | 463.6              | 192       | 10.6     | 17.7                   | 113.9   | 130   | 145   | 100  | 115      |
|                 | 82                 | 460.2              | 191.3     | 9.9      | 16.0                   | 104.5   | 140   | 160   | 105  | 125      |
|                 | 74                 | 457.2              | 190.5     | 9.1      | 14.5                   | 94.98   | 155   | 175   | 115  | 135      |
|                 | 67                 | 453.6              | 189.9     | 8.5      | 12.7                   | 85.44   | 170   | 190   | 130  | 150      |
| 457x152         | 82                 | 465.1              | 153.5     | 10.7     | 18.9                   | 104.4   | 130   | 145   | 105  | 120      |
|                 | 74                 | 461.3              | 152.7     | 9.9      | 17.0                   | 94.99   | 140   | 155   | 115  | 130      |
|                 | 67                 | 457.2              | 151.9     | 9.1      | 15.0                   | 85.41   | 155   | 175   | 125  | 145      |
|                 | 60                 | 454.7              | 152.9     | 8.0      | 13.3                   | 75.93   | 175   | 195   | 140  | 160      |
|                 | 52                 | 449.8              | 152.4     | 7.6      | 10.9                   | 66.49   | 200   | 220   | 160  | 180      |
| 406x178         | 74                 | 412.8              | 179.7     | 9.7      | 16.0                   | 94.95   | 140   | 160   | 105  | 125      |
|                 | 67                 | 409.4              | 178.8     | 8.8      | 14.3                   | 85.49   | 155   | 175   | 115  | 140      |
|                 | 60                 | 406.4              | 177.8     | 7.8      | 12.8                   | 76.01   | 175   | 195   | 130  | 155      |
|                 | 54                 | 402.6              | 177.6     | 7.6      | 10.9                   | 68.42   | 190   | 215   | 145  | 170      |
| 406x140         | 46                 | 402.3              | 142.4     | 6.9      | 11.2                   | 58.96   | 205   | 230   | 160  | 185      |
|                 | 39                 | 397.3              | 141.8     | 6.3      | 8.6                    | 49.40   | 240   | 270   | 190  | 220      |
| 356x171         | 67                 | 364                | 173.2     | 9.1      | 15.7                   | 85.42   | 140   | 160   | 105  | 125      |
|                 | 57                 | 358.6              | 172.1     | 8        | 13.0                   | 72.18   | 165   | 190   | 125  | 145      |
|                 | 51                 | 355.6              | 171.5     | 7.3      | 11.5                   | 64.58   | 185   | 210   | 135  | 160      |
|                 | 45                 | 352                | 171       | 6.9      | 9.7                    | 56.96   | 210   | 240   | 155  | 185      |
| 356x127         | 39                 | 352.8              | 126       | 6.5      | 10.7                   | 49.40   | 215   | 240   | 170  | 195      |
|                 | 33                 | 348.5              | 125.4     | 5.9      | 8.5                    | 41.83   | 250   | 280   | 195  | 225      |
| 305x165         | 54                 | 310.9              | 166.8     | 7.7      | 13.7                   | 68.38   | 160   | 185   | 115  | 140      |
|                 | 46                 | 307.1              | 165.7     | 6.7      | 11.8                   | 58.90   | 185   | 210   | 130  | 160      |
|                 | 40                 | 303.8              | 165.1     | 6.1      | 10.2                   | 51.50   | 210   | 240   | 150  | 180      |
| 305x127         | 48                 | 310.4              | 125.2     | 9.9      | 14.0                   | 60.83   | 160   | 180   | 125  | 145      |
|                 | 42                 | 306.6              | 124.3     | 8        | 12.1                   | 53.18   | 180   | 205   | 140  | 160      |
|                 | 37                 | 303.8              | 123.5     | 7.2      | 10.7                   | 47.47   | 200   | 225   | 155  | 180      |
| 305x102         | 33                 | 312.7              | 102.4     | 6.6      | 10.8                   | 41.77   | 215   | 240   | 175  | 200      |
|                 | 28                 | 308.9              | 101.9     | 6.1      | 8.9                    | 36.30   | 245   | 275   | 200  | 225      |
|                 | 25                 | 304.8              | 101.6     | 5.8      | 6.8                    | 31.39   | 285   | 315   | 225  | 260      |
| 254x146         | 43                 | 259.6              | 147.3     | 7.3      | 12.7                   | 55.10   | 170   | 195   | 120  | 150      |
|                 | 37                 | 256                | 146.4     | 6.4      | 10.9                   | 47.45   | 195   | 225   | 140  | 170      |
|                 | 31                 | 251.5              | 146.1     | 6.1      | 8.6                    | 40.00   | 230   | 265   | 160  | 200      |
| 254x102         | 28                 | 260.4              | 102.1     | 6.4      | 10.0                   | 36.19   | 220   | 250   | 170  | 200      |
|                 | 25                 | 257                | 101.9     | 6.1      | 8.4                    | 32.17   | 245   | 280   | 190  | 225      |
|                 | 22                 | 254                | 101.6     | 5.8      | 6.8                    | 28.42   | 275   | 315   | 215  | 250      |
| 203x133         | 30                 | 206.8              | 133.8     | 6.3      | 9.6                    | 38.00   | 210   | 245   | 145  | 180      |
|                 | 25                 | 203.2              | 133.4     | 5.8      | 7.8                    | 32.31   | 240   | 285   | 165  | 210      |
| 203x102         | 23                 | 203.2              | 101.6     | 5.2      | 9.3                    | 29  | 235   | 270   | 175  | 210      |
| 178x102         | 19                 | 177.8              | 101.6     | 4.7      | 7.9                    | 24.2  | 265   | 305   | 190  | 230      |
| 152x89          | 16                 | 152.4              | 88.9      | 4.6      | 7.7                    | 20.5  | 270   | 310   | 190  | 235      |
| 127x76          | 13                 | 127                | 76.2      | 4.2      | 7.6                    | 16.8  | 275   | 320   | 195  | 240      |

| Universal columns   |                    |                    |           |          |                 |                 | Section factor $H_p/A$   |                 |                 |                 |
|---|--------------------|--------------------|-----------|----------|-----------------|-----------------|--|-----------------|-----------------|-----------------|
|   |                    |                    |           |          |                 |                 | Profile  |                 | Box             |                 |
|   |                    |                    |           |          |                 |                 | 3 sides  | 4 sides         | 3 sides         | 4 sides         |
|  |                    |                    |           |          |                 |                 |  |                 |                 |                 |
| Designation   | Depth of section D | Width of section B | Thickness |          | Area of section | Profile 3 sides | Profile 4 sides  | Box 3 sides     | Box 4 sides     |                 |
| Serial size   | mm                 | mm                 | Web t     | Flange T |                 |                 |  |                 |                 | mm <sup>2</sup> |
| mm  | kg                 | mm                 | mm        | mm       | mm              | mm <sup>2</sup> | m <sup>-1</sup>  | m <sup>-1</sup> | m <sup>-1</sup> | m <sup>-1</sup> |
| 356 x 406   | 634                | 474.7              | 424.1     | 47.6     | 77.0            | 808.1           | 25   | 30              | 15              | 20              |
|   | 551                | 455.7              | 418.5     | 42.0     | 67.5            | 701.8           | 30   | 35              | 20              | 25              |
|   | 467                | 436.6              | 412.4     | 35.9     | 58.0            | 595.5           | 35   | 40              | 20              | 30              |
|   | 393                | 419.1              | 407.0     | 30.6     | 49.2            | 500.9           | 40   | 45              | 25              | 35              |
|   | 340                | 406.4              | 403.0     | 26.5     | 42.9            | 432.7           | 45   | 55              | 30              | 35              |
|   | 287                | 393.7              | 399.0     | 22.6     | 36.5            | 366.0           | 50   | 65              | 30              | 45              |
|   | 235                | 381.0              | 395.0     | 18.5     | 30.2            | 299.8           | 65   | 75              | 40              | 50              |
| 356 x 368   | 202                | 374.7              | 374.4     | 16.8     | 27.0            | 257.9           | 70   | 85              | 45              | 60              |
|   | 177                | 368.3              | 372.1     | 14.5     | 23.8            | 225.7           | 80   | 95              | 50              | 65              |
|   | 153                | 362.0              | 370.2     | 12.6     | 20.7            | 195.2           | 90   | 110             | 55              | 75              |
|   | 129                | 355.6              | 368.3     | 10.7     | 17.5            | 164.9           | 105  | 130             | 65              | 90              |
| 305 x 305   | 283                | 365.3              | 321.8     | 26.9     | 44.1            | 360.4           | 45   | 55              | 30              | 40              |
|   | 240                | 352.6              | 317.9     | 23.0     | 37.7            | 305.6           | 50   | 60              | 35              | 45              |
|   | 198                | 339.9              | 314.1     | 19.2     | 31.4            | 252.3           | 60   | 75              | 40              | 50              |
|   | 158                | 327.2              | 310.6     | 15.7     | 25.0            | 201.2           | 75   | 90              | 50              | 65              |
|   | 137                | 320.5              | 308.7     | 13.8     | 21.7            | 174.6           | 85   | 105             | 55              | 75              |
|   | 118                | 314.5              | 306.8     | 11.9     | 18.7            | 149.8           | 100  | 120             | 60              | 80              |
|   | 97                 | 307.8              | 304.8     | 9.9      | 15.4            | 123.3           | 120  | 145             | 75              | 100             |
| 254 x 254   | 167                | 289.1              | 264.5     | 19.2     | 31.7            | 212.4           | 60   | 75              | 40              | 50              |
|   | 132                | 276.4              | 261.0     | 15.6     | 25.3            | 167.7           | 75   | 90              | 50              | 65              |
|   | 107                | 266.7              | 258.3     | 13.0     | 20.5            | 136.6           | 90   | 110             | 60              | 75              |
|   | 89                 | 260.4              | 255.9     | 10.5     | 17.3            | 114.0           | 110  | 130             | 70              | 90              |
|   | 73                 | 254.0              | 254.0     | 8.6      | 14.2            | 92.9            | 130  | 160             | 80              | 110             |
| 203 x 203   | 86                 | 222.3              | 208.8     | 13.0     | 20.5            | 110.1           | 95   | 110             | 60              | 80              |
|   | 71                 | 215.9              | 206.2     | 10.3     | 17.3            | 91.1            | 110  | 135             | 70              | 95              |
|   | 60                 | 209.6              | 205.2     | 9.3      | 14.2            | 75.8            | 130  | 160             | 80              | 110             |
|   | 52                 | 206.2              | 203.9     | 8.0      | 12.5            | 66.4            | 150  | 180             | 95              | 125             |
|   | 46                 | 203.2              | 203.2     | 7.3      | 11.0            | 58.8            | 165  | 200             | 105             | 140             |
| 152 x 152   | 37                 | 161.8              | 154.4     | 8.1      | 11.5            | 47.4            | 160  | 190             | 100             | 135             |
|   | 30                 | 157.5              | 152.9     | 6.6      | 9.4             | 38.2            | 195  | 235             | 120             | 160             |
|   | 23                 | 152.4              | 152.4     | 6.1      | 6.8             | 29.8            | 245  | 300             | 155             | 205             |

| Circular hollow sections |             |                |                 | Section factor $H_p/A$  |   |
|--------------------------|-------------|----------------|-----------------|---|---|
|                          |             |                |                 | Profile or Box  |   |
| Designation              |             | Mass per metre | Area of section |  |  |
| Outside diameter D       | Thickness t |                |                 |   |   |
| mm                       | mm          | kg             | cm <sup>2</sup> | m <sup>-1</sup>   |   |
| 21.3                     | 3.2         | 1.43           | 1.82            | 370   |   |
| 26.9                     | 3.2         | 1.87           | 2.38            | 355   |   |
| 33.7                     | 2.6         | 1.99           | 2.54            | 415   |   |
|                          | 3.2         | 2.41           | 3.07            | 345   |   |
| 42.4                     | 4.0         | 2.93           | 3.73            | 285   |   |
|                          | 2.6         | 2.55           | 3.25            | 410   |   |
| 48.3                     | 3.2         | 3.09           | 3.94            | 340   |   |
|                          | 4.0         | 3.79           | 4.83            | 275   |   |
| 60.3                     | 3.2         | 3.56           | 4.53            | 335   |   |
|                          | 4.0         | 4.37           | 5.57            | 270   |   |
| 76.1                     | 5.0         | 5.34           | 6.80            | 225   |   |
|                          | 3.2         | 4.51           | 5.74            | 330   |   |
| 88.9                     | 4.0         | 5.55           | 7.07            | 270   |   |
|                          | 5.0         | 6.82           | 8.69            | 220   |   |
| 114.3                    | 3.2         | 5.75           | 7.33            | 325   |   |
|                          | 4.0         | 7.11           | 9.06            | 265   |   |
| 139.7                    | 5.0         | 8.77           | 11.2            | 215   |   |
|                          | 3.2         | 6.76           | 8.62            | 325   |   |
| 168.3                    | 4.0         | 8.38           | 10.70           | 260   |   |
|                          | 5.0         | 10.3           | 13.2            | 210   |   |
| 193.7                    | 3.6         | 9.83           | 12.5            | 285   |   |
|                          | 5.0         | 13.5           | 17.2            | 210   |   |
| 219.1                    | 6.3         | 16.8           | 21.4            | 170   |   |
|                          | 5.0         | 16.6           | 21.2            | 205   |   |
| 244.5                    | 6.3         | 20.7           | 26.4            | 165   |   |
|                          | 8.0         | 26.0           | 33.1            | 135   |   |
| 273.0                    | 10.0        | 32.0           | 40.7            | 110   |   |
|                          | 5.0         | 20.1           | 25.7            | 205   |   |
| 323.9                    | 6.3         | 25.2           | 37.1            | 165   |   |
|                          | 8.0         | 31.6           | 40.3            | 130   |   |
| 355.6                    | 10.0        | 39.0           | 49.7            | 105   |   |
|                          | 5.0         | 23.3           | 29.6            | 205   |   |
| 406.4                    | 6.3         | 29.1           | 37.1            | 165   |   |
|                          | 8.0         | 36.6           | 46.7            | 130   |   |
| 457.0                    | 10.0        | 45.3           | 57.7            | 105   |   |
|                          | 12.5        | 55.9           | 71.2            | 85  |   |
| 508.0                    | 16.0        | 70.1           | 89.3            | 70  |   |
|                          | 5.0         | 26.4           | 33.6            | 205   |   |
| 580.0                    | 6.3         | 33.1           | 42.1            | 165   |   |
|                          | 8.0         | 41.6           | 53.1            | 130   |   |
| 660.0                    | 10.0        | 51.6           | 65.7            | 105   |   |
|                          | 12.5        | 63.7           | 81.1            | 85  |   |
| 744.0                    | 16.0        | 80.1           | 102             | 65  |   |
|                          | 20.0        | 98.2           | 125             | 55  |   |

|                    |             |                |                 | Section factor $H_p/A$  |  |
|--------------------|-------------|----------------|-----------------|---|--|
|                    |             |                |                 | Profile or Box  |  |
| Designation        |             | Mass per metre | Area of section |  |  |
| Outside diameter D | Thickness t |                |                 |   |  |
| mm                 | mm          | kg             | cm <sup>2</sup> | m <sup>-1</sup>   |  |
| 244.5              | 6.3         | 37.0           | 47.1            | 165   |  |
|                    | 8.0         | 46.7           | 59.4            | 130   |  |
|                    | 10.0        | 57.8           | 73.7            | 105   |  |
|                    | 12.5        | 71.5           | 91.1            | 85  |  |
|                    | 16.0        | 90.2           | 115             | 65  |  |
| 273.0              | 20.0        | 111            | 141             | 55  |  |
|                    | 6.3         | 41.4           | 52.8            | 160   |  |
|                    | 8.0         | 52.3           | 66.6            | 130   |  |
|                    | 10.0        | 64.9           | 82.6            | 105   |  |
|                    | 12.5        | 80.3           | 102             | 85  |  |
| 323.9              | 16.0        | 101            | 129             | 65  |  |
|                    | 20.0        | 125            | 159             | 55  |  |
|                    | 25.0        | 153            | 195             | 45  |  |
|                    | 6.3         | 49.3           | 62.9            | 160   |  |
|                    | 8.0         | 62.3           | 79.4            | 130   |  |
| 355.6              | 10.0        | 77.4           | 98.6            | 105   |  |
|                    | 12.5        | 96.0           | 122             | 85  |  |
|                    | 16.0        | 121            | 155             | 65  |  |
|                    | 20.0        | 150            | 191             | 55  |  |
|                    | 25.0        | 184            | 235             | 45  |  |
| 406.4              | 8.0         | 68.6           | 87.4            | 130   |  |
|                    | 10.0        | 85.2           | 109             | 100   |  |
|                    | 12.5        | 106            | 135             | 85  |  |
|                    | 16.0        | 134            | 171             | 65  |  |
|                    | 20.0        | 166            | 211             | 55  |  |
| 457.0              | 25.0        | 204            | 260             | 45  |  |
|                    | 10.0        | 97.8           | 125             | 100   |  |
|                    | 12.5        | 121            | 155             | 80  |  |
|                    | 16.0        | 154            | 196             | 65  |  |
|                    | 20.0        | 191            | 243             | 55  |  |
| 508.0              | 25.0        | 235            | 300             | 45  |  |
|                    | 32.0        | 295            | 376             | 35  |  |
|                    | 10.0        | 110            | 140             | 105   |  |
|                    | 12.5        | 137            | 175             | 80  |  |
|                    | 16.0        | 174            | 222             | 65  |  |
| 580.0              | 20.0        | 216            | 275             | 50  |  |
|                    | 25.0        | 266            | 339             | 40  |  |
|                    | 32.0        | 335            | 427             | 35  |  |
|                    | 40.0        | 411            | 524             | 25  |  |
|                    | 10.0        | 123            | 156             | 100   |  |
| 660.0              | 12.5        | 153            | 195             | 80  |  |
|                    | 16.0        | 194            | 247             | 65  |  |

| Rectangular hollow sections |             |                |                 | Section factor $H_p/A$  |   |   |
|-----------------------------|-------------|----------------|-----------------|---|---|---|
|                             |             |                |                 | 3 sides   |   | 4 sides   |
| Designation                 |             | Mass per metre | Area of section |  |  |  |
| Size D x B                  | Thickness t |                |                 |   |   |   |
| mm                          | mm          | kg             | cm <sup>2</sup> | m <sup>-1</sup>   | m <sup>-1</sup>   | m <sup>-1</sup>   |
| 50x25                       | 2.5         | 2.72           | 3.47            | 360   | 290   | 430   |
|                             | 3.0         | 3.22           | 4.10            | 305   | 245   | 365   |
|                             | 3.2         | 3.41           | 4.34            | 290   | 230   | 345   |
| 50x30                       | 2.5         | 2.92           | 3.72            | 350   | 295   | 430   |
|                             | 3.0         | 3.45           | 4.40            | 295   | 250   | 365   |
|                             | 3.2         | 3.66           | 4.66            | 280   | 235   | 345   |
|                             | 4.0         | 4.46           | 5.68            | 230   | 195   | 280   |
|                             | 5.0         | 5.40           | 6.88            | 190   | 160   | 235   |
| 60x40                       | 2.5         | 3.71           | 4.72            | 340   | 295   | 425   |
|                             | 3.0         | 4.39           | 5.60            | 285   | 250   | 365   |
|                             | 3.2         | 4.66           | 5.94            | 270   | 235   | 335   |
|                             | 4.0         | 5.72           | 7.28            | 220   | 190   | 275   |
|                             | 5.0         | 6.97           | 8.88            | 180   | 160   | 225   |
|                             | 6.3         | 8.49           | 10.8            | 150   | 130   | 185   |
| 80x40                       | 3.0         | 5.34           | 6.80            | 295   | 235   | 355   |
|                             | 3.2         | 5.67           | 7.22            | 275   | 220   | 330   |
|                             | 4.0         | 6.97           | 8.88            | 225   | 180   | 270   |
|                             | 5.0         | 8.54           | 10.9            | 185   | 145   | 220   |
|                             | 6.3         | 10.5           | 13.3            | 150   | 120   | 180   |
|                             | 8.0         | 12.8           | 16.3            | 125   | 100   | 145   |
| 90x50                       | 3.0         | 6.28           | 8.00            | 290   | 240   | 350   |
|                             | 3.6         | 7.46           | 9.50            | 240   | 200   | 295   |
|                             | 5.0         | 10.1           | 12.9            | 180   | 145   | 215   |
|                             | 6.3         | 12.5           | 15.9            | 145   | 120   | 175   |
|                             | 8.0         | 15.3           | 19.5            | 120   | 95  | 145   |
| 100x50                      | 3.0         | 6.75           | 8.60            | 290   | 235   | 350   |
|                             | 3.2         | 7.18           | 9.14            | 275   | 220   | 330   |
|                             | 4.0         | 8.86           | 11.3            | 220   | 175   | 265   |
|                             | 5.0         | 10.9           | 13.9            | 180   | 145   | 215   |
|                             | 6.3         | 13.4           | 17.1            | 145   | 115   | 175   |
|                             | 8.0         | 16.6           | 21.1            | 120   | 95  | 140   |
| 100x60                      | 3.0         | 7.22           | 9.20            | 285   | 240   | 350   |
|                             | 3.6         | 8.59           | 10.9            | 240   | 200   | 295   |
|                             | 5.0         | 11.7           | 14.9            | 175   | 150   | 215   |
|                             | 6.3         | 14.4           | 18.4            | 140   | 120   | 175   |
|                             | 8.0         | 17.8           | 22.7            | 115   | 95  | 140   |
|                             | 10.0        | 22.2           | 28.4            | 90  | 75  | 110   |
| 120x60                      | 3.6         | 9.72           | 12.4            | 240   | 195   | 290   |
|                             | 5.0         | 13.3           | 16.9            | 180   | 140   | 215   |
|                             | 6.3         | 16.4           | 20.9            | 145   | 115   | 170   |
|                             | 8.0         | 20.4           | 25.9            | 115   | 95  | 140   |
|                             | 10.0        | 25.9           | 32.9            | 90  | 75  | 110   |
| 120x80                      | 5.0         | 14.8           | 18.9            | 170   | 150   | 210   |
|                             | 6.3         | 18.4           | 23.4            | 135   | 120   | 170   |
|                             | 8.0         | 22.9           | 29.1            | 110   | 95  | 135   |
|                             | 10.0        | 27.9           | 35.5            | 90  | 75  | 115   |
| 150x100                     | 5.0         | 18.7           | 23.9            | 165   | 145   | 210   |
|                             | 6.3         | 23.8           | 29.7            | 135   | 120   | 170   |
|                             | 8.0         | 29.1           | 37.1            | 110   | 95  | 135   |
|                             | 10.0        | 35.7           | 45.5            | 90  | 75  | 110   |
|                             | 12.5        | 43.6           | 55.5            | 70  | 65  | 90  |
| 160x80                      | 5.0         | 18.0           | 22.9            | 175   | 140   | 210   |
|                             | 6.3         | 22.3           | 28.5            | 140   | 110   | 170   |
|                             | 8.0         | 27.9           | 35.5            | 115   | 90  | 135   |
|                             | 10.0        | 34.2           | 43.5            | 90  | 75  | 110   |
|                             | 12.5        | 41.6           | 53.0            | 75  | 60  | 90  |
|                             | 15.0        | 50.0           | 63.0            | 60  | 50  | 75  |
| 200x100                     | 5.0         | 22.7           | 28.9            | 175   | 140   | 210   |
|                             | 6.3         | 28.3           | 36.0            | 140   | 110   | 165   |
|                             | 8.0         | 35.4           | 45.1            | 110   | 90  | 135   |
|                             | 10.0        | 43.6           | 55.5            | 90  | 70  | 110   |
|                             | 12.5        | 53.4           | 68.0            | 75  | 60  | 90  |
|                             | 16.0        | 66.4           | 84.5            | 60  | 45  | 70  |
|                             | 20.0        | 82.0           | 104.0           | 50  | 35  | 55  |
| 250x150                     | 6.3         | 38.2           | 48.6            | 135   | 115   | 165   |
|                             | 8.0         | 48.0           | 61.1            | 105   | 90  | 130   |
|                             | 10.0        | 59.3           | 75.5            | 85  | 75  | 105   |
|                             | 12.5        | 73.0           | 93.0            | 70  | 60  | 85  |
|                             | 16.0        | 91.5           | 117             | 55  | 45  | 70  |
|                             | 20.0        | 113.0          | 144.0           | 45  | 35  | 55  |
| 300x200                     | 6.3         | 48.1           | 61.2            | 130   | 115   | 165   |
|                             | 8.0         | 60.5           | 77.1            | 105   | 90  | 130   |
|                             | 10.0        | 75.0           | 95.5            | 85  | 75  | 105   |
|                             | 12.5        | 92.6           | 118             | 70  | 60  | 85  |
|                             | 16.0        | 117            | 149             | 55  | 45  | 65  |
| 400x200                     | 10.0        | 90.7           | 116             | 85  | 70  | 105   |
|                             | 12.5        | 112            | 143             | 70  | 55  | 85  |
|                             | 16.0        | 142            | 181             | 55  | 45  | 65  |
| 450x250                     | 10.0        | 106            | 136             | 85  | 70  | 105   |
|                             | 12.5        | 132            | 168             | 70  | 55  | 85  |
|                             | 16.0        | 167            | 213             | 55  | 45  | 65  |

| Designation |             | Mass per metre | Area of section | Section factor $H_p/A$ |                 |
|-------------|-------------|----------------|-----------------|------------------------|-----------------|
|             |             |                |                 | 3 sides                | 4 sides         |
| Size D × D  | Thickness t | kg             | cm <sup>2</sup> | m <sup>-1</sup>        | m <sup>-1</sup> |
| 20×20       | 2.0         | 1.12           | 1.42            | 425                    | 565             |
|             | 2.5         | 1.35           | 1.72            | 350                    | 465             |
| 25×25       | 2.0         | 1.43           | 1.82            | 410                    | 550             |
|             | 2.5         | 1.74           | 2.22            | 340                    | 450             |
|             | 3.0         | 2.04           | 2.60            | 290                    | 385             |
|             | 3.2         | 2.15           | 2.74            | 275                    | 365             |
| 30×30       | 2.5         | 2.14           | 2.72            | 330                    | 440             |
|             | 3.0         | 2.51           | 3.20            | 280                    | 375             |
|             | 3.2         | 2.65           | 3.38            | 265                    | 355             |
| 40×40       | 2.5         | 2.92           | 3.72            | 325                    | 430             |
|             | 3.0         | 3.45           | 4.40            | 275                    | 365             |
|             | 3.2         | 3.66           | 4.66            | 260                    | 345             |
|             | 4.0         | 4.46           | 5.68            | 210                    | 280             |
| 50×50       | 5.0         | 5.40           | 6.88            | 175                    | 235             |
|             | 2.5         | 3.71           | 4.72            | 320                    | 425             |
| 60×60       | 3.0         | 4.39           | 5.60            | 270                    | 355             |
|             | 3.2         | 4.66           | 5.94            | 255                    | 335             |
|             | 4.0         | 5.72           | 7.28            | 205                    | 275             |
|             | 5.0         | 6.97           | 8.88            | 170                    | 225             |
| 70×70       | 6.3         | 8.49           | 10.8            | 140                    | 185             |
|             | 3.0         | 5.34           | 6.80            | 265                    | 355             |
|             | 3.2         | 5.67           | 7.22            | 250                    | 330             |
|             | 4.0         | 6.97           | 8.88            | 205                    | 270             |
|             | 5.0         | 8.54           | 10.9            | 165                    | 220             |
|             | 6.3         | 10.5           | 13.3            | 135                    | 180             |
| 80×80       | 8.0         | 12.8           | 16.3            | 110                    | 145             |
|             | 3.0         | 6.28           | 8.00            | 260                    | 350             |
|             | 3.6         | 7.46           | 9.50            | 220                    | 295             |
|             | 5.0         | 10.1           | 12.9            | 165                    | 215             |
| 90×90       | 6.3         | 12.5           | 15.9            | 130                    | 175             |
|             | 8.0         | 15.3           | 19.5            | 110                    | 145             |
|             | 3.0         | 7.22           | 9.20            | 260                    | 350             |
|             | 3.6         | 8.59           | 10.9            | 220                    | 295             |
|             | 5.0         | 11.7           | 14.9            | 160                    | 215             |
|             | 6.3         | 14.4           | 18.4            | 130                    | 175             |
| 100×100     | 8.0         | 17.8           | 22.7            | 105                    | 140             |
|             | 3.6         | 9.72           | 12.4            | 220                    | 290             |
|             | 5.0         | 13.3           | 16.9            | 160                    | 215             |
|             | 6.3         | 16.4           | 20.9            | 130                    | 170             |
| 120×120     | 8.0         | 20.4           | 25.9            | 105                    | 140             |
|             | 4.0         | 12.0           | 15.3            | 195                    | 260             |
|             | 5.0         | 14.8           | 18.9            | 160                    | 210             |
|             | 6.3         | 18.4           | 23.4            | 130                    | 170             |
|             | 8.0         | 22.9           | 29.1            | 105                    | 135             |
| 10.0        | 27.9        | 35.5           | 85              | 115                    |                 |

| Designation |             | Mass per metre | Area of section | Section factor $H_p/A$ |                 |
|-------------|-------------|----------------|-----------------|------------------------|-----------------|
|             |             |                |                 | 3 sides                | 4 sides         |
| Size D × D  | Thickness t | kg             | cm <sup>2</sup> | m <sup>-1</sup>        | m <sup>-1</sup> |
| 120×120     | 5.0         | 18.0           | 22.9            | 155                    | 210             |
|             | 6.3         | 22.3           | 28.5            | 125                    | 170             |
|             | 8.0         | 27.9           | 35.5            | 100                    | 135             |
|             | 10.0        | 34.2           | 43.5            | 85                     | 110             |
|             | 12.5        | 41.6           | 53.0            | 70                     | 90              |
| 140×140     | 5.0         | 21.1           | 26.9            | 155                    | 210             |
|             | 6.3         | 26.3           | 33.5            | 125                    | 165             |
|             | 8.0         | 32.9           | 41.9            | 100                    | 135             |
| 150×150     | 10.0        | 40.4           | 51.5            | 80                     | 110             |
|             | 12.5        | 49.5           | 63.0            | 65                     | 90              |
|             | 5.0         | 22.7           | 28.9            | 155                    | 210             |
| 180×180     | 6.3         | 28.3           | 36.0            | 125                    | 165             |
|             | 8.0         | 35.4           | 45.1            | 100                    | 135             |
|             | 10.0        | 43.6           | 55.5            | 80                     | 110             |
|             | 12.5        | 53.4           | 68.0            | 65                     | 90              |
|             | 16.0        | 66.4           | 84.5            | 55                     | 70              |
| 200×200     | 6.3         | 34.2           | 43.6            | 125                    | 165             |
|             | 8.0         | 43.0           | 54.7            | 100                    | 130             |
|             | 10.0        | 53.0           | 67.5            | 80                     | 105             |
|             | 12.5        | 65.2           | 83.0            | 65                     | 85              |
| 250×250     | 16.0        | 81.4           | 104             | 50                     | 70              |
|             | 6.3         | 38.2           | 48.6            | 125                    | 165             |
|             | 8.0         | 48.0           | 61.1            | 100                    | 130             |
|             | 10.0        | 59.3           | 75.5            | 80                     | 105             |
|             | 12.5        | 73.0           | 93.0            | 65                     | 85              |
| 300×300     | 16.0        | 91.5           | 117             | 50                     | 70              |
|             | 6.3         | 48.1           | 61.2            | 125                    | 165             |
|             | 8.0         | 60.5           | 77.1            | 95                     | 130             |
|             | 10.0        | 75.0           | 95.5            | 80                     | 105             |
|             | 12.5        | 92.6           | 118             | 65                     | 85              |
| 350×350     | 16.0        | 117            | 149             | 50                     | 65              |
|             | 10.0        | 90.7           | 116             | 80                     | 105             |
|             | 12.5        | 112            | 143             | 65                     | 85              |
| 400×400     | 16.0        | 142            | 181             | 50                     | 65              |
|             | 10.0        | 106            | 136             | 75                     | 105             |
|             | 12.5        | 132            | 168             | 65                     | 85              |
| 450×450     | 16.0        | 167            | 213             | 50                     | 65              |
|             | 10.0        | 122            | 156             | 75                     | 105             |
|             | 12.5        | 152            | 193             | 60                     | 85              |
| 16.0        | 192         | 245            | 50              | 65                     |                 |

Minimum thickness of a typical spray protection to an I-section

| $H_p/A$<br>up to | Dry thickness (mm) to provide fire resistance of |        |                      |         |         |         |
|------------------|--|--------|----------------------|---------|---------|---------|
|                  | $\frac{1}{2}$ hour                               | 1 hour | $1\frac{1}{2}$ hours | 2 hours | 3 hours | 4 hours |
| 30               | 10   | 10     | 10                   | 10      | 15      | 25      |
| 50               | 10   | 10     | 10                   | 14      | 21      | 29      |
| 70               | 10   | 10     | 12                   | 17      | 27      | 36      |
| 90               | 10   | 10     | 14                   | 20      | 31      | 42      |
| 110              | 10   | 10     | 16                   | 22      | 34      | 47      |
| 130              | 10   | 10     | 17                   | 24      | 37      | 51      |
| 150              | 10   | 11     | 18                   | 25      | 40      | 54      |
| 170              | 10   | 12     | 19                   | 27      | 42      | 57      |
| 190              | 10   | 12     | 20                   | 28      | 44      | 59      |
| 210              | 10   | 13     | 21                   | 29      | 45      |         |
| 230              | 10   | 13     | 21                   | 30      | 47      |         |
| 250              | 10   | 14     | 22                   | 31      | 48      |         |
| 270              | 10   | 14     | 23                   | 31      | 49      |         |
| 290              | 10   | 14     | 23                   | 32      | 50      |         |
| 310              | 10   | 14     | 23                   | 33      | 51      |         |

Linear interpolation is permissible between values of  $H_p/A$



**Basic data on corrosion**

| <b>INTERIOR ENVIRONMENTS</b>                                |                       |   |
|---|-----------------------|---|
| <b>environment</b>  | <b>corrosion risk</b> | <b>examples*</b>  |
| Normal  | Negligible            | Offices<br>Shops<br>Industrial Production/Assembly<br>Warehousing<br>Hospital wards<br>Schools<br>Hotels                        |
| Occasional<br>Condensation                                  | Low                   | Unheated Buildings<br>Vehicle Depots<br>Sports Halls  |
| Frequent<br>Condensation                                    | Significant           | Food Processing Plants/Kitchens<br>Laundries<br>Breweries<br>Dairies  |
| Frequent<br>Condensation<br>with<br>Corrosive<br>Atmosphere | High                  | Chemical Processing Plant<br>Dye Works<br>Swimming Pools<br>Paper Manufacture<br>Boat Yards over seawater<br>Foundries/Smelters |

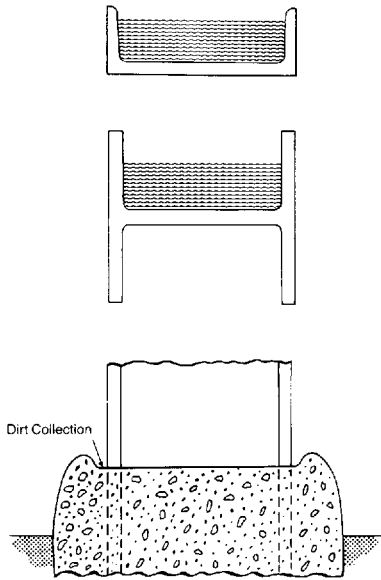
\* Buildings may contain areas where different conditions apply, e.g. hospitals will contain kitchen and laundry areas

| <b>EXTERIOR ENVIRONMENTS</b> |  |                             |
|------------------------------|--|-----------------------------|
| <b>Environment</b>           | <b>Description</b>   | <b>Steel Corrosion Risk</b> |
| Normal inland                | Most rural and urban areas with low sulphur dioxide, acid, alkali and salt pollution.<br>(Some apparently non-industrial areas may be polluted from distant sources according to prevailing wind and topography) | Low                         |
| Polluted inland              | Areas of high airborne sulphur dioxide, or other pollution from industrial or domestic sources.  | Significant                 |
| Normal coastal               | As normal inland with high airborne salt levels.<br>(This salt contaminated zone may extend to a maximum of 3 km from the coast)   | High                        |
| Polluted coastal             | As polluted inland with high airborne salt levels.<br>(This salt contaminated zone may extend to a maximum of 3 km from the coast)   | Very high                   |
|                              | Aggressive industrial environments such as steelwork adjacent to acid plants, salt storage depots, electroplating shops, chemical works etc. Buried or immersed steelwork<br>Sea water splash zones.             | Variable                    |

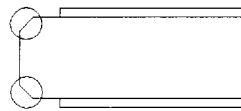
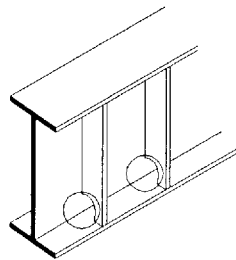
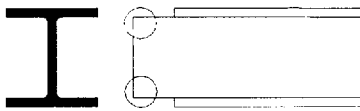
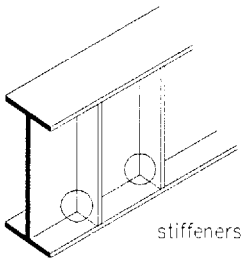
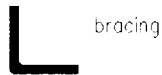
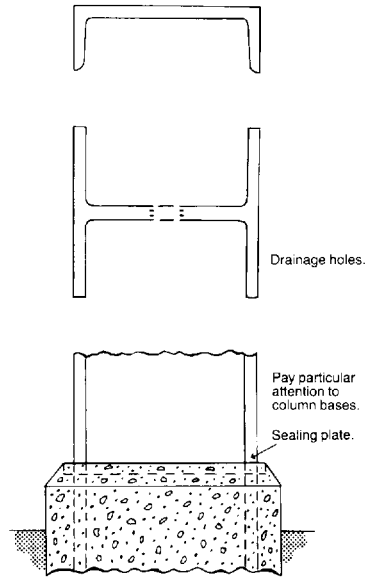
## DETAILING TO MINIMISE CORROSION

Details should be designed to shed water and avoid collection of dirt whenever possible.

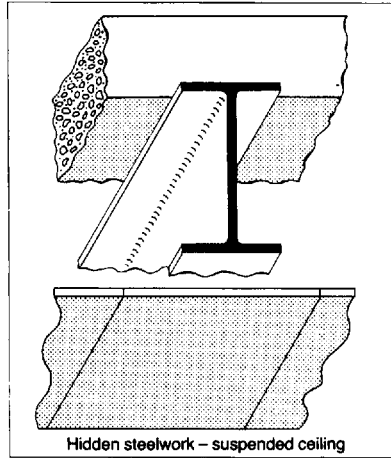
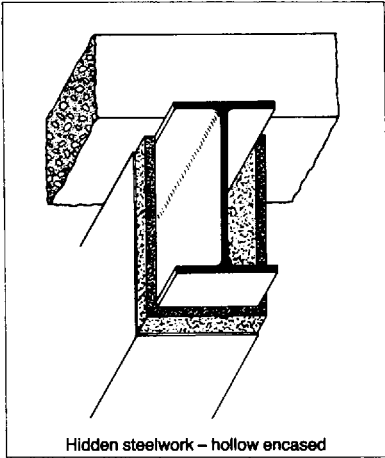
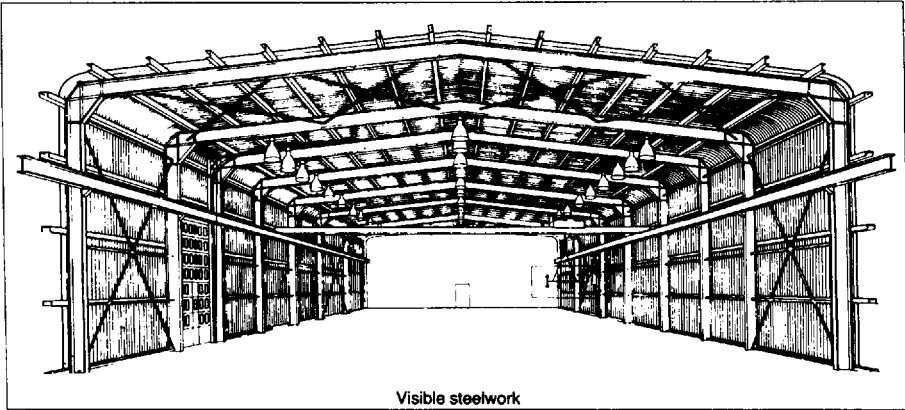
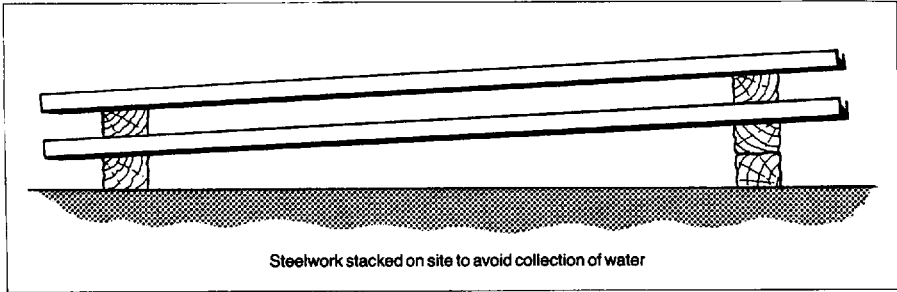
More prone to corrosion

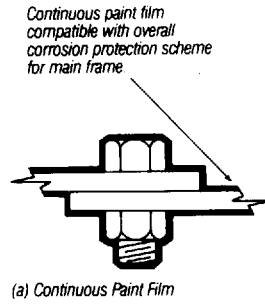
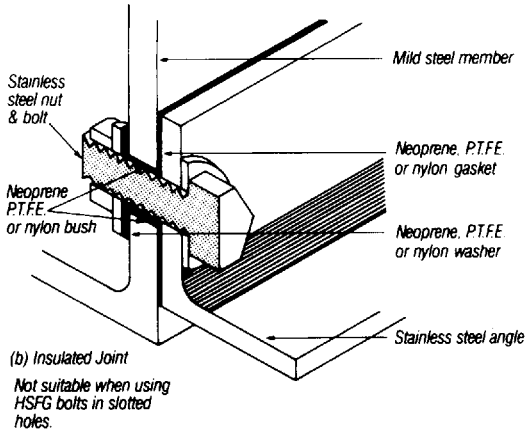


Improved



### Methods of preventing bi-metallic corrosion.





The above basic data on corrosion are extracted from *Corrosion Protection Guides for Steelwork* in: (i) Building Interiors (issue 3), (ii) Exterior Environments (issue 2) and (iii) Building Refurbishment, published by British Steel General Steels.

SECOND MOMENTS OF AREA  
INCHES<sup>4</sup> UNITS TO CENTIMETRES<sup>4</sup> UNITS

| in. <sup>4</sup> | 0                | -1               | -2               | -3               | -4               | -5               | -6               | -7               | -8               | -9               |
|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
|                  | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> | cm. <sup>4</sup> |
| 1                | 41-62314256      | 45-785           | 49-948           | 54-110           | 58-272           | 62-435           | 66-597           | 70-759           | 74-922           | 79-084           |
| 2                | 83-24628         | 87-409           | 91-571           | 95-733           | 99-895           | 104-058          | 108-220          | 112-382          | 116-545          | 120-707          |
| 3                | 124-86942        | 129-032          | 133-194          | 137-356          | 141-519          | 145-681          | 149-843          | 154-006          | 158-168          | 162-330          |
| 4                | 166-49257        | 170-655          | 174-817          | 178-979          | 183-142          | 187-304          | 191-466          | 195-629          | 199-791          | 203-953          |
| 5                | 208-11571        | 212-278          | 216-440          | 220-603          | 224-765          | 228-927          | 233-089          | 237-252          | 241-414          | 245-576          |
| 6                | 249-73886        | 253-901          | 258-063          | 262-226          | 266-388          | 270-550          | 274-713          | 278-875          | 283-037          | 287-200          |
| 7                | 291-36200        | 295-524          | 299-687          | 303-849          | 308-011          | 312-173          | 316-336          | 320-498          | 324-660          | 328-823          |
| 8                | 332-98514        | 337-147          | 341-310          | 345-472          | 349-634          | 353-797          | 357-959          | 362-121          | 366-284          | 370-446          |
| 9                | 374-60829        | 378-771          | 382-933          | 387-095          | 391-257          | 395-420          | 399-582          | 403-744          | 407-907          | 412-069          |
| 10               | 416-23143        |                  |                  |                  |                  |                  |                  |                  |                  |                  |

CENTIMETRES<sup>4</sup> UNITS TO INCHES<sup>4</sup> UNITS

| cm. <sup>4</sup> | 0                | -1               | -2               | -3               | -4               | -5               | -6               | -7               | -8               | -9               |
|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
|                  | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> | in. <sup>4</sup> |
| 1                | 0-02402510       | 0-02643          | 0-02883          | 0-03123          | 0-03363          | 0-03604          | 0-03844          | 0-04084          | 0-04324          | 0-04565          |
| 2                | 0-04805019       | 0-05045          | 0-05285          | 0-05526          | 0-05766          | 0-06006          | 0-06246          | 0-06487          | 0-06727          | 0-06967          |
| 3                | 0-07207529       | 0-07448          | 0-07688          | 0-07928          | 0-08168          | 0-08409          | 0-08649          | 0-08889          | 0-09129          | 0-09370          |
| 4                | 0-09610038       | 0-09850          | 0-10091          | 0-10331          | 0-10571          | 0-10811          | 0-11052          | 0-11292          | 0-11532          | 0-11772          |
| 5                | 0-12012548       | 0-12253          | 0-12493          | 0-12733          | 0-12974          | 0-13214          | 0-13454          | 0-13694          | 0-13935          | 0-14175          |
| 6                | 0-14415058       | 0-14655          | 0-14895          | 0-15136          | 0-15376          | 0-15616          | 0-15856          | 0-16097          | 0-16337          | 0-16577          |
| 7                | 0-16817567       | 0-17058          | 0-17298          | 0-17538          | 0-17779          | 0-18019          | 0-18259          | 0-18499          | 0-18740          | 0-18980          |
| 8                | 0-19220077       | 0-19460          | 0-19701          | 0-19941          | 0-20181          | 0-20421          | 0-20662          | 0-20902          | 0-21142          | 0-21382          |
| 9                | 0-21622586       | 0-21863          | 0-22103          | 0-22343          | 0-22584          | 0-22824          | 0-23064          | 0-23304          | 0-23545          | 0-23785          |
| 10               | 0-24025096       |                  |                  |                  |                  |                  |                  |                  |                  |                  |

MODULI OF SECTION

INCHES<sup>3</sup> UNITS TO CENTIMETRES<sup>3</sup> UNITS

| in. <sup>3</sup> | 0                | -1               | -2               | -3               | -4               | -5               | -6               | -7               | -8               | -9               |
|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
|                  | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> | cm. <sup>3</sup> |
| 1                | 16-387064        | 18-026           | 19-664           | 21-303           | 22-942           | 24-580           | 26-219           | 27-858           | 29-497           | 31-135           |
| 2                | 32-77413         | 34-413           | 36-051           | 37-690           | 39-329           | 40-967           | 42-606           | 44-245           | 45-884           | 47-522           |
| 3                | 49-16119         | 50-800           | 52-438           | 54-077           | 55-716           | 57-355           | 58-993           | 60-632           | 62-271           | 63-909           |
| 4                | 65-54826         | 67-187           | 68-826           | 70-464           | 72-103           | 73-742           | 75-380           | 77-019           | 78-658           | 80-297           |
| 5                | 81-93532         | 83-574           | 85-213           | 86-851           | 88-490           | 90-129           | 91-767           | 93-406           | 95-045           | 96-684           |
| 6                | 98-32238         | 99-961           | 101-600          | 103-238          | 104-877          | 106-516          | 108-154          | 109-793          | 111-432          | 113-071          |
| 7                | 114-70945        | 116-348          | 117-987          | 119-625          | 121-264          | 122-903          | 124-542          | 126-180          | 127-819          | 129-458          |
| 8                | 131-09651        | 132-735          | 134-374          | 136-012          | 137-651          | 139-290          | 140-929          | 142-567          | 144-206          | 145-845          |
| 9                | 147-48358        | 149-122          | 150-761          | 152-400          | 154-038          | 155-677          | 157-316          | 158-954          | 160-593          | 162-232          |
| 10               | 163-87064        |                  |                  |                  |                  |                  |                  |                  |                  |                  |

CENTIMETRES<sup>3</sup> UNITS TO INCHES<sup>3</sup> UNITS

| cm. <sup>3</sup> | 0                | -1               | -2               | -3               | -4               | -5               | -6               | -7               | -8               | -9               |
|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
|                  | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> | in. <sup>3</sup> |
| 1                | 0-061024         | 0-06713          | 0-07323          | 0-07933          | 0-08543          | 0-09154          | 0-09764          | 0-10374          | 0-10984          | 0-11594          |
| 2                | 0-122047         | 0-12815          | 0-13425          | 0-14035          | 0-14646          | 0-15256          | 0-15866          | 0-16476          | 0-17087          | 0-17697          |
| 3                | 0-183071         | 0-18917          | 0-19527          | 0-20138          | 0-20748          | 0-21358          | 0-21968          | 0-22579          | 0-23189          | 0-23799          |
| 4                | 0-244095         | 0-25020          | 0-25630          | 0-26240          | 0-26850          | 0-27461          | 0-28071          | 0-28681          | 0-29291          | 0-29902          |
| 5                | 0-305119         | 0-31122          | 0-31732          | 0-32342          | 0-32953          | 0-33563          | 0-34173          | 0-34783          | 0-35394          | 0-36004          |
| 6                | 0-366142         | 0-37224          | 0-37835          | 0-38445          | 0-39055          | 0-39665          | 0-40276          | 0-40886          | 0-41496          | 0-42106          |
| 7                | 0-427166         | 0-43327          | 0-43937          | 0-44547          | 0-45158          | 0-45768          | 0-46378          | 0-46988          | 0-47599          | 0-48209          |
| 8                | 0-488190         | 0-49429          | 0-50040          | 0-50650          | 0-51260          | 0-51870          | 0-52480          | 0-53091          | 0-53701          | 0-54311          |
| 9                | 0-549213         | 0-55532          | 0-56142          | 0-56752          | 0-57362          | 0-57973          | 0-58583          | 0-59193          | 0-59803          | 0-60414          |
| 10               | 0-610237         |                  |                  |                  |                  |                  |                  |                  |                  |                  |

Based on 1 inch = 25.4 millimetres

Extract from B.S. 350 : 1944

## WEIGHTS PER UNIT LENGTH

### POUNDS PER FOOT TO KILOGRAMS PER METRE

Based on 1 inch = 25.4 millimetres ; 1 pound = 0.45359243 kilograms

| Pounds<br>per ft. | 0       | 1       | 2       | 3       | 4       | 5       | 6       | 7       | 8       | 9       |
|-------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| —                 | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  | kg./m.  |
| —                 | —       | 1.4882  | 2.9763  | 4.4645  | 5.9527  | 7.4408  | 8.9290  | 10.417  | 11.905  | 13.393  |
| 10                | 14.882  | 16.370  | 17.858  | 19.346  | 20.834  | 22.322  | 23.811  | 25.299  | 26.787  | 28.275  |
| 20                | 29.763  | 31.251  | 32.740  | 34.228  | 35.716  | 37.204  | 38.692  | 40.180  | 41.669  | 43.157  |
| 30                | 44.645  | 46.133  | 47.621  | 49.109  | 50.598  | 52.086  | 53.574  | 55.062  | 56.550  | 58.038  |
| 40                | 59.527  | 61.015  | 62.503  | 63.991  | 65.479  | 66.967  | 68.456  | 69.944  | 71.432  | 72.920  |
| 50                | 74.408  | 75.896  | 77.385  | 78.873  | 80.361  | 81.849  | 83.337  | 84.825  | 86.314  | 87.802  |
| 60                | 89.290  | 90.778  | 92.266  | 93.754  | 95.242  | 96.731  | 98.219  | 99.707  | 101.195 | 102.683 |
| 70                | 104.171 | 105.660 | 107.148 | 108.636 | 110.124 | 111.612 | 113.100 | 114.589 | 116.077 | 117.565 |
| 80                | 119.053 | 120.541 | 122.029 | 123.518 | 125.006 | 126.494 | 127.982 | 129.470 | 130.958 | 132.447 |
| 90                | 133.935 | 135.423 | 136.911 | 138.399 | 139.887 | 141.376 | 142.864 | 144.352 | 145.840 | 147.328 |
| 100               | 148.816 |         |         |         |         |         |         |         |         |         |

### KILOGRAMS PER METRE TO POUNDS PER FOOT

Based on 1 inch = 25.4 millimetres ; 1 pound = 0.45359243 kilograms

| Kg.<br>per m. | 0       | 1       | 2       | 3       | 4       | 5       | 6       | 7       | 8       | 9        |
|---------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|
| —             | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft. | lb./ft.  |
| —             | —       | 0.67197 | 1.3439  | 2.0159  | 2.6879  | 3.3598  | 4.0318  | 4.7038  | 5.3758  | 6.0477   |
| 10            | 6.7197  | 7.3917  | 8.0636  | 8.7356  | 9.4076  | 10.0795 | 10.7515 | 11.4235 | 12.0954 | 12.7674  |
| 20            | 13.4394 | 14.1113 | 14.7833 | 15.4553 | 16.1273 | 16.7992 | 17.4712 | 18.1432 | 18.8151 | 19.4871  |
| 30            | 20.1591 | 20.8310 | 21.5030 | 22.1750 | 22.8469 | 23.5189 | 24.1909 | 24.8629 | 25.5348 | 26.2068  |
| 40            | 26.8788 | 27.5507 | 28.2227 | 28.8947 | 29.5666 | 30.2386 | 30.9106 | 31.5825 | 32.2545 | 32.9265  |
| 50            | 33.5984 | 34.2704 | 34.9424 | 35.6144 | 36.2863 | 36.9583 | 37.6303 | 38.3022 | 38.9742 | 39.6462  |
| 60            | 40.3181 | 40.9901 | 41.6621 | 42.3340 | 43.0060 | 43.6780 | 44.3500 | 45.0219 | 45.6939 | 46.3659  |
| 70            | 47.0378 | 47.7098 | 48.3818 | 49.0537 | 49.7257 | 50.3976 | 51.0696 | 51.7415 | 52.4135 | 53.0855  |
| 80            | 53.7575 | 54.4295 | 55.1015 | 55.7734 | 56.4454 | 57.1174 | 57.7893 | 58.4613 | 59.1333 | 59.8053  |
| 90            | 60.4772 | 61.1492 | 61.8212 | 62.4931 | 63.1651 | 63.8371 | 64.5090 | 65.1810 | 65.8530 | 66.5250  |
| 100           | 67.1969 | 67.8689 | 68.5409 | 69.2128 | 69.8848 | 70.5568 | 71.2287 | 71.9007 | 72.5727 | 73.2447  |
| 110           | 73.9166 | 74.5886 | 75.2606 | 75.9325 | 76.6045 | 77.2765 | 77.9484 | 78.6204 | 79.2924 | 79.9644  |
| 120           | 80.6363 | 81.3083 | 81.9803 | 82.6522 | 83.3242 | 83.9962 | 84.6681 | 85.3401 | 86.0121 | 86.6841  |
| 130           | 87.3560 | 88.0280 | 88.7000 | 89.3719 | 90.0439 | 90.7159 | 91.3878 | 92.0598 | 92.7318 | 93.4038  |
| 140           | 94.0757 | 94.7477 | 95.4197 | 96.0916 | 96.7636 | 97.4356 | 98.1075 | 98.7795 | 99.4515 | 100.1235 |

Extract from B.S. 350: 1944

**WEIGHTS**  
**POUNDS TO KILOGRAMS**

Based on 1 pound = 0.45359243 kilograms

| <b>Lb.</b> | <b>0</b>   | <b>1</b>   | <b>2</b>   | <b>3</b>   | <b>4</b>   | <b>5</b>   | <b>6</b>   | <b>7</b>   | <b>8</b>   | <b>9</b>   |
|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|            | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> | <b>kg.</b> |
| —          | —          | 0.45359    | 0.90718    | 1.36078    | 1.81437    | 2.26796    | 2.72155    | 3.17515    | 3.62874    | 4.08233    |
| 10         | 4.53592    | 4.98952    | 5.4431     | 5.8967     | 6.3503     | 6.8039     | 7.2575     | 7.7111     | 8.1647     | 8.6183     |
| 20         | 9.0718     | 9.5254     | 9.9790     | 10.4326    | 10.8862    | 11.3398    | 11.7934    | 12.2470    | 12.7006    | 13.1542    |
| 30         | 13.6078    | 14.0614    | 14.5150    | 14.9686    | 15.4221    | 15.8757    | 16.3293    | 16.7829    | 17.2365    | 17.6901    |
| 40         | 18.1437    | 18.5973    | 19.0509    | 19.5045    | 19.9581    | 20.4117    | 20.8653    | 21.3188    | 21.7724    | 22.2260    |
| 50         | 22.6796    | 23.1332    | 23.5868    | 24.0404    | 24.4940    | 24.9476    | 25.4012    | 25.8548    | 26.3084    | 26.7620    |
| 60         | 27.2155    | 27.6691    | 28.1227    | 28.5763    | 29.0299    | 29.4835    | 29.9371    | 30.3907    | 30.8443    | 31.2979    |
| 70         | 31.7515    | 32.2051    | 32.6587    | 33.1122    | 33.5658    | 34.0194    | 34.4730    | 34.9266    | 35.3802    | 35.8338    |
| 80         | 36.2874    | 36.7410    | 37.1946    | 37.6482    | 38.1018    | 38.5554    | 39.0089    | 39.4625    | 39.9161    | 40.3697    |
| 90         | 40.8233    | 41.2769    | 41.7305    | 42.1841    | 42.6377    | 43.0913    | 43.5449    | 43.9985    | 44.4521    | 44.9057    |
| 100        | 45.3592    | 45.8128    | 46.2664    | 46.7200    | 47.1736    | 47.6272    | 48.0808    | 48.5344    | 48.9880    | 49.4416    |
| 10         | 49.8952    | 50.349     | 50.802     | 51.256     | 51.710     | 52.163     | 52.617     | 53.070     | 53.524     | 53.977     |
| 20         | 54.431     | 54.885     | 55.338     | 55.792     | 56.245     | 56.699     | 57.153     | 57.606     | 58.060     | 58.513     |
| 30         | 58.967     | 59.421     | 59.874     | 60.328     | 60.781     | 61.235     | 61.689     | 62.142     | 62.596     | 63.049     |
| 40         | 63.503     | 63.957     | 64.410     | 64.864     | 65.317     | 65.771     | 66.224     | 66.678     | 67.132     | 67.585     |
| 50         | 68.039     | 68.492     | 68.946     | 69.400     | 69.853     | 70.307     | 70.760     | 71.214     | 71.668     | 72.121     |
| 60         | 72.575     | 73.028     | 73.482     | 73.936     | 74.389     | 74.843     | 75.296     | 75.750     | 76.204     | 76.657     |
| 70         | 77.111     | 77.564     | 78.018     | 78.471     | 78.925     | 79.379     | 79.832     | 80.286     | 80.739     | 81.193     |
| 80         | 81.647     | 82.100     | 82.554     | 83.007     | 83.461     | 83.915     | 84.368     | 84.822     | 85.275     | 85.729     |
| 90         | 86.183     | 86.636     | 87.090     | 87.543     | 87.997     | 88.451     | 88.904     | 89.358     | 89.811     | 90.265     |
| 200        | 90.718     | 91.172     | 91.626     | 92.079     | 92.533     | 92.986     | 93.440     | 93.894     | 94.347     | 94.801     |
| 10         | 95.254     | 95.708     | 96.162     | 96.615     | 97.069     | 97.522     | 97.976     | 98.430     | 98.883     | 99.337     |
| 20         | 99.790     | 100.244    | 100.698    | 101.151    | 101.605    | 102.058    | 102.512    | 102.965    | 103.419    | 103.873    |
| 30         | 104.326    | 104.780    | 105.233    | 105.687    | 106.141    | 106.594    | 107.048    | 107.501    | 107.955    | 108.409    |
| 40         | 108.862    | 109.316    | 109.769    | 110.223    | 110.677    | 111.130    | 111.584    | 112.037    | 112.491    | 112.945    |
| 50         | 113.398    | 113.852    | 114.305    | 114.759    | 115.212    | 115.666    | 116.120    | 116.573    | 117.027    | 117.480    |
| 60         | 117.934    | 118.388    | 118.841    | 119.295    | 119.748    | 120.202    | 120.656    | 121.109    | 121.563    | 122.016    |
| 70         | 122.470    | 122.924    | 123.377    | 123.831    | 124.284    | 124.738    | 125.192    | 125.645    | 126.099    | 126.552    |
| 80         | 127.006    | 127.459    | 127.913    | 128.367    | 128.820    | 129.274    | 129.727    | 130.181    | 130.635    | 131.088    |
| 90         | 131.542    | 131.995    | 132.449    | 132.903    | 133.356    | 133.810    | 134.263    | 134.717    | 135.171    | 135.624    |
| 300        | 136.078    | 136.531    | 136.985    | 137.439    | 137.892    | 138.346    | 138.799    | 139.253    | 139.706    | 140.160    |
| 10         | 140.614    | 141.067    | 141.521    | 141.974    | 142.428    | 142.882    | 143.335    | 143.789    | 144.242    | 144.696    |
| 20         | 145.150    | 145.603    | 146.057    | 146.510    | 146.964    | 147.418    | 147.871    | 148.325    | 148.778    | 149.232    |
| 30         | 149.686    | 150.139    | 150.593    | 151.046    | 151.500    | 151.953    | 152.407    | 152.861    | 153.314    | 153.768    |
| 40         | 154.221    | 154.675    | 155.129    | 155.582    | 156.036    | 156.489    | 156.943    | 157.397    | 157.850    | 158.304    |
| 50         | 158.757    | 159.211    | 159.665    | 160.118    | 160.572    | 161.025    | 161.479    | 161.932    | 162.386    | 162.840    |
| 60         | 163.293    | 163.747    | 164.200    | 164.654    | 165.108    | 165.561    | 166.015    | 166.468    | 166.922    | 167.376    |
| 70         | 167.829    | 168.283    | 168.736    | 169.190    | 169.644    | 170.097    | 170.551    | 171.004    | 171.458    | 171.912    |
| 80         | 172.365    | 172.819    | 173.272    | 173.726    | 174.179    | 174.633    | 175.087    | 175.540    | 175.994    | 176.447    |
| 90         | 176.901    | 177.355    | 177.808    | 178.262    | 178.715    | 179.169    | 179.623    | 180.076    | 180.530    | 180.983    |
| 400        | 181.437    | 181.891    | 182.344    | 182.798    | 183.251    | 183.705    | 184.159    | 184.612    | 185.066    | 185.519    |
| 10         | 185.973    | 186.426    | 186.880    | 187.334    | 187.787    | 188.241    | 188.694    | 189.148    | 189.602    | 190.055    |
| 20         | 190.509    | 190.962    | 191.416    | 191.870    | 192.323    | 192.777    | 193.230    | 193.684    | 194.138    | 194.591    |
| 30         | 195.045    | 195.498    | 195.952    | 196.406    | 196.859    | 197.313    | 197.766    | 198.220    | 198.673    | 199.127    |
| 40         | 199.581    | 200.034    | 200.488    | 200.941    | 201.395    | 201.849    | 202.302    | 202.756    | 203.209    | 203.663    |
| 50         | 204.117    | 204.570    | 205.024    | 205.477    | 205.931    | 206.385    | 206.838    | 207.292    | 207.745    | 208.199    |
| 60         | 208.653    | 209.106    | 209.560    | 210.013    | 210.467    | 210.920    | 211.374    | 211.828    | 212.281    | 212.735    |
| 70         | 213.188    | 213.642    | 214.096    | 214.549    | 215.003    | 215.456    | 215.910    | 216.364    | 216.817    | 217.271    |
| 80         | 217.724    | 218.178    | 218.632    | 219.085    | 219.539    | 219.992    | 220.446    | 220.900    | 221.353    | 221.807    |
| 90         | 222.260    | 222.714    | 223.167    | 223.621    | 224.075    | 224.528    | 224.982    | 225.435    | 225.889    | 226.343    |





Extract from B.S. 350 : 1944

**FEET AND INCHES TO METRES**

Based on 1 inch = 25·4 millimetres

Uncontracted values

| Feet | Inches  |         |         |         |         |         | Differences<br>for<br>sixteenths<br>of an inch |
|------|---------|---------|---------|---------|---------|---------|--|
|      | 0       | 1       | 2       | 3       | 4       | 5       |  |
|      | m.      | m.      | m.      | m.      | m.      | m.      | m.   |
| 0    | —       | 0·0254  | 0·0508  | 0·0762  | 0·1016  | 0·1270  |  |
| 1    | 0·3048  | 0·3302  | 0·3556  | 0·3810  | 0·4064  | 0·4318  | 1 0·0016                                       |
| 2    | 0·6096  | 0·6350  | 0·6604  | 0·6858  | 0·7112  | 0·7366  |  |
| 3    | 0·9144  | 0·9398  | 0·9652  | 0·9906  | 1·0160  | 1·0414  |  |
| 4    | 1·2192  | 1·2446  | 1·2700  | 1·2954  | 1·3208  | 1·3462  |  |
| 5    | 1·5240  | 1·5494  | 1·5748  | 1·6002  | 1·6256  | 1·6510  | 2 0·0032                                       |
| 6    | 1·8288  | 1·8542  | 1·8796  | 1·9050  | 1·9304  | 1·9558  |  |
| 7    | 2·1336  | 2·1590  | 2·1844  | 2·2098  | 2·2352  | 2·2606  |  |
| 8    | 2·4384  | 2·4638  | 2·4892  | 2·5146  | 2·5400  | 2·5654  | 3 0·0048                                       |
| 9    | 2·7432  | 2·7686  | 2·7940  | 2·8194  | 2·8448  | 2·8702  |  |
| 10   | 3·0480  | 3·0734  | 3·0988  | 3·1242  | 3·1496  | 3·1750  |  |
| 11   | 3·3528  | 3·3782  | 3·4036  | 3·4290  | 3·4544  | 3·4798  | 4 0·0064                                       |
| 12   | 3·6576  | 3·6830  | 3·7084  | 3·7338  | 3·7592  | 3·7846  |  |
| 13   | 3·9624  | 3·9878  | 4·0132  | 4·0386  | 4·0640  | 4·0894  |  |
| 14   | 4·2672  | 4·2926  | 4·3180  | 4·3434  | 4·3688  | 4·3942  | 5 0·0079                                       |
| 15   | 4·5720  | 4·5974  | 4·6228  | 4·6482  | 4·6736  | 4·6990  |  |
| 16   | 4·8768  | 4·9022  | 4·9276  | 4·9530  | 4·9784  | 5·0038  |  |
| 17   | 5·1816  | 5·2070  | 5·2324  | 5·2578  | 5·2832  | 5·3086  | 6 0·0095                                       |
| 18   | 5·4864  | 5·5118  | 5·5372  | 5·5626  | 5·5880  | 5·6134  |  |
| 19   | 5·7912  | 5·8166  | 5·8420  | 5·8674  | 5·8928  | 5·9182  |  |
| 20   | 6·0960  | 6·1214  | 6·1468  | 6·1722  | 6·1976  | 6·2230  | 7 0·0111                                       |
| 21   | 6·4008  | 6·4262  | 6·4516  | 6·4770  | 6·5024  | 6·5278  |  |
| 22   | 6·7056  | 6·7310  | 6·7564  | 6·7818  | 6·8072  | 6·8326  |  |
| 23   | 7·0104  | 7·0358  | 7·0612  | 7·0866  | 7·1120  | 7·1374  | 8 0·0127                                       |
| 24   | 7·3152  | 7·3406  | 7·3660  | 7·3914  | 7·4168  | 7·4422  |  |
| 25   | 7·6200  | 7·6454  | 7·6708  | 7·6962  | 7·7216  | 7·7470  |  |
| 26   | 7·9248  | 7·9502  | 7·9756  | 8·0010  | 8·0264  | 8·0518  | 9 0·0143                                       |
| 27   | 8·2296  | 8·2550  | 8·2804  | 8·3058  | 8·3312  | 8·3566  |  |
| 28   | 8·5344  | 8·5598  | 8·5852  | 8·6106  | 8·6360  | 8·6614  |  |
| 29   | 8·8392  | 8·8646  | 8·8900  | 8·9154  | 8·9408  | 8·9662  | 10 0·0159                                      |
| 30   | 9·1440  | 9·1694  | 9·1948  | 9·2202  | 9·2456  | 9·2710  |  |
| 31   | 9·4488  | 9·4742  | 9·4996  | 9·5250  | 9·5504  | 9·5758  |  |
| 32   | 9·7536  | 9·7790  | 9·8044  | 9·8298  | 9·8552  | 9·8806  | 11 0·0175                                      |
| 33   | 10·0584 | 10·0838 | 10·1092 | 10·1346 | 10·1600 | 10·1854 |  |
| 34   | 10·3632 | 10·3886 | 10·4140 | 10·4394 | 10·4648 | 10·4902 |  |
| 35   | 10·6680 | 10·6934 | 10·7188 | 10·7442 | 10·7696 | 10·7950 | 12 0·0190                                      |
| 36   | 10·9728 | 10·9982 | 11·0236 | 11·0490 | 11·0744 | 11·0998 |  |
| 37   | 11·2776 | 11·3030 | 11·3284 | 11·3538 | 11·3792 | 11·4046 |  |
| 38   | 11·5824 | 11·6078 | 11·6332 | 11·6586 | 11·6840 | 11·7094 | 13 0·0206                                      |
| 39   | 11·8872 | 11·9126 | 11·9380 | 11·9634 | 11·9888 | 12·0142 |  |
| 40   | 12·1920 | 12·2174 | 12·2428 | 12·2682 | 12·2936 | 12·3190 |  |
| 41   | 12·4968 | 12·5222 | 12·5476 | 12·5730 | 12·5984 | 12·6238 | 14 0·0222                                      |
| 42   | 12·8016 | 12·8270 | 12·8524 | 12·8778 | 12·9032 | 12·9286 |  |
| 43   | 13·1064 | 13·1318 | 13·1572 | 13·1826 | 13·2080 | 13·2334 |  |
| 44   | 13·4112 | 13·4366 | 13·4620 | 13·4874 | 13·5128 | 13·5382 | 15 0·0238                                      |
| 45   | 13·7160 | 13·7414 | 13·7668 | 13·7922 | 13·8176 | 13·8430 |  |
| 46   | 14·0208 | 14·0462 | 14·0716 | 14·0970 | 14·1224 | 14·1478 |  |
| 47   | 14·3256 | 14·3510 | 14·3764 | 14·4018 | 14·4272 | 14·4526 |  |
| 48   | 14·6304 | 14·6558 | 14·6812 | 14·7066 | 14·7320 | 14·7574 |  |
| 49   | 14·9352 | 14·9606 | 14·9860 | 15·0114 | 15·0368 | 15·0622 |  |

Extract from B.S. 350 : 1944

**FEET AND INCHES TO METRES**

Based on 1 inch = 25·4 millimetres

Uncontracted values

| Feet | Inches    |           |           |           |           |           | Differences for sixteenths of an inch |        |
|------|-----------|-----------|-----------|-----------|-----------|-----------|---------------------------------------|--------|
|      | 6         | 7         | 8         | 9         | 10        | 11        | m.                                    |        |
| 0    | m. 0·1524 | m. 0·1778 | m. 0·2032 | m. 0·2286 | m. 0·2540 | m. 0·2794 |                                       |        |
| 1    | 0·4572    | 0·4826    | 0·5080    | 0·5334    | 0·5588    | 0·5842    |                                       |        |
| 2    | 0·7620    | 0·7874    | 0·8128    | 0·8382    | 0·8636    | 0·8890    | 1                                     | 0·0016 |
| 3    | 1·0668    | 1·0922    | 1·1176    | 1·1430    | 1·1684    | 1·1938    |                                       |        |
| 4    | 1·3716    | 1·3970    | 1·4224    | 1·4478    | 1·4732    | 1·4986    |                                       |        |
| 5    | 1·6764    | 1·7018    | 1·7272    | 1·7526    | 1·7780    | 1·8034    | 2                                     | 0·0032 |
| 6    | 1·9812    | 2·0066    | 2·0320    | 2·0574    | 2·0828    | 2·1082    |                                       |        |
| 7    | 2·2860    | 2·3114    | 2·3368    | 2·3622    | 2·3876    | 2·4130    |                                       |        |
| 8    | 2·5908    | 2·6162    | 2·6416    | 2·6670    | 2·6924    | 2·7178    | 3                                     | 0·0048 |
| 9    | 2·8956    | 2·9210    | 2·9464    | 2·9718    | 2·9972    | 3·0226    |                                       |        |
| 10   | 3·2004    | 3·2258    | 3·2512    | 3·2766    | 3·3020    | 3·3274    |                                       |        |
| 11   | 3·5052    | 3·5306    | 3·5560    | 3·5814    | 3·6068    | 3·6322    | 4                                     | 0·0064 |
| 12   | 3·8100    | 3·8354    | 3·8608    | 3·8862    | 3·9116    | 3·9370    |                                       |        |
| 13   | 4·1148    | 4·1402    | 4·1656    | 4·1910    | 4·2164    | 4·2418    |                                       |        |
| 14   | 4·4196    | 4·4450    | 4·4704    | 4·4958    | 4·5212    | 4·5466    | 5                                     | 0·0079 |
| 15   | 4·7244    | 4·7498    | 4·7752    | 4·8006    | 4·8260    | 4·8514    |                                       |        |
| 16   | 5·0292    | 5·0546    | 5·0800    | 5·1054    | 5·1308    | 5·1562    |                                       |        |
| 17   | 5·3340    | 5·3594    | 5·3848    | 5·4102    | 5·4356    | 5·4610    | 6                                     | 0·0095 |
| 18   | 5·6388    | 5·6642    | 5·6896    | 5·7150    | 5·7404    | 5·7658    |                                       |        |
| 19   | 5·9436    | 5·9690    | 5·9944    | 6·0198    | 6·0452    | 6·0706    |                                       |        |
| 20   | 6·2484    | 6·2738    | 6·2992    | 6·3246    | 6·3500    | 6·3754    | 7                                     | 0·0111 |
| 21   | 6·5532    | 6·5786    | 6·6040    | 6·6294    | 6·6548    | 6·6802    |                                       |        |
| 22   | 6·8580    | 6·8834    | 6·9088    | 6·9342    | 6·9596    | 6·9850    |                                       |        |
| 23   | 7·1628    | 7·1882    | 7·2136    | 7·2390    | 7·2644    | 7·2898    | 8                                     | 0·0127 |
| 24   | 7·4676    | 7·4930    | 7·5184    | 7·5438    | 7·5692    | 7·5946    |                                       |        |
| 25   | 7·7724    | 7·7978    | 7·8232    | 7·8486    | 7·8740    | 7·8994    |                                       |        |
| 26   | 8·0772    | 8·1026    | 8·1280    | 8·1534    | 8·1788    | 8·2042    | 9                                     | 0·0143 |
| 27   | 8·3820    | 8·4074    | 8·4328    | 8·4582    | 8·4836    | 8·5090    |                                       |        |
| 28   | 8·6868    | 8·7122    | 8·7376    | 8·7630    | 8·7884    | 8·8138    |                                       |        |
| 29   | 8·9916    | 9·0170    | 9·0424    | 9·0678    | 9·0932    | 9·1186    | 10                                    | 0·0159 |
| 30   | 9·2964    | 9·3218    | 9·3472    | 9·3726    | 9·3980    | 9·4234    |                                       |        |
| 31   | 9·6012    | 9·6266    | 9·6520    | 9·6774    | 9·7028    | 9·7282    |                                       |        |
| 32   | 9·9060    | 9·9314    | 9·9568    | 9·9822    | 10·0076   | 10·0330   | 11                                    | 0·0175 |
| 33   | 10·2108   | 10·2362   | 10·2616   | 10·2870   | 10·3124   | 10·3378   |                                       |        |
| 34   | 10·5156   | 10·5410   | 10·5664   | 10·5918   | 10·6172   | 10·6426   |                                       |        |
| 35   | 10·8204   | 10·8458   | 10·8712   | 10·8966   | 10·9220   | 10·9474   | 12                                    | 0·0190 |
| 36   | 11·1252   | 11·1506   | 11·1760   | 11·2014   | 11·2268   | 11·2522   |                                       |        |
| 37   | 11·4300   | 11·4554   | 11·4808   | 11·5062   | 11·5316   | 11·5570   |                                       |        |
| 38   | 11·7348   | 11·7602   | 11·7856   | 11·8110   | 11·8364   | 11·8618   | 13                                    | 0·0206 |
| 39   | 12·0396   | 12·0650   | 12·0904   | 12·1158   | 12·1412   | 12·1666   |                                       |        |
| 40   | 12·3444   | 12·3698   | 12·3952   | 12·4206   | 12·4460   | 12·4714   |                                       |        |
| 41   | 12·6492   | 12·6746   | 12·7000   | 12·7254   | 12·7508   | 12·7762   | 14                                    | 0·0222 |
| 42   | 12·9540   | 12·9794   | 13·0048   | 13·0302   | 13·0556   | 13·0810   |                                       |        |
| 43   | 13·2588   | 13·2842   | 13·3096   | 13·3350   | 13·3604   | 13·3858   |                                       |        |
| 44   | 13·5636   | 13·5890   | 13·6144   | 13·6398   | 13·6652   | 13·6906   | 15                                    | 0·0238 |
| 45   | 13·8684   | 13·8938   | 13·9192   | 13·9446   | 13·9700   | 13·9954   |                                       |        |
| 46   | 14·1732   | 14·1986   | 14·2240   | 14·2494   | 14·2748   | 14·3002   |                                       |        |
| 47   | 14·4780   | 14·5034   | 14·5288   | 14·5542   | 14·5796   | 14·6050   |                                       |        |
| 48   | 14·7828   | 14·8082   | 14·8336   | 14·8590   | 14·8844   | 14·9098   |                                       |        |
| 49   | 15·0876   | 15·1130   | 15·1384   | 15·1638   | 15·1892   | 15·2146   |                                       |        |

Extract from B.S. 350: 1944

**FEET AND INCHES TO METRES**

Based on 1 inch = 25.4 millimetres

Uncontracted values

| Feet | Inches  |         |         |         |         |         | Differences for sixteenths of an inch |
|------|---------|---------|---------|---------|---------|---------|---------------------------------------|
|      | 0       | 1       | 2       | 3       | 4       | 5       |                                       |
|      | m.      | m.      | m.      | m.      | m.      | m.      | m.                                    |
| 50   | 15.2400 | 15.2654 | 15.2908 | 15.3162 | 15.3416 | 15.3670 |                                       |
| 51   | 15.5448 | 15.5702 | 15.5956 | 15.6210 | 15.6464 | 15.6718 |                                       |
| 52   | 15.8496 | 15.8750 | 15.9004 | 15.9258 | 15.9512 | 15.9766 | 1 0.0016                              |
| 53   | 16.1544 | 16.1798 | 16.2052 | 16.2306 | 16.2560 | 16.2814 |                                       |
| 54   | 16.4592 | 16.4846 | 16.5100 | 16.5354 | 16.5608 | 16.5862 |                                       |
| 55   | 16.7640 | 16.7894 | 16.8148 | 16.8402 | 16.8656 | 16.8910 | 2 0.0032                              |
| 56   | 17.0688 | 17.0942 | 17.1196 | 17.1450 | 17.1704 | 17.1958 |                                       |
| 57   | 17.3736 | 17.3990 | 17.4244 | 17.4498 | 17.4752 | 17.5006 |                                       |
| 58   | 17.6784 | 17.7038 | 17.7292 | 17.7546 | 17.7800 | 17.8054 | 3 0.0048                              |
| 59   | 17.9832 | 18.0086 | 18.0340 | 18.0594 | 18.0848 | 18.1102 |                                       |
| 60   | 18.2880 | 18.3134 | 18.3388 | 18.3642 | 18.3896 | 18.4150 |                                       |
| 61   | 18.5928 | 18.6182 | 18.6436 | 18.6690 | 18.6944 | 18.7198 | 4 0.0064                              |
| 62   | 18.8976 | 18.9230 | 18.9484 | 18.9738 | 18.9992 | 19.0246 |                                       |
| 63   | 19.2024 | 19.2278 | 19.2532 | 19.2786 | 19.3040 | 19.3294 | 5 0.0079                              |
| 64   | 19.5072 | 19.5326 | 19.5580 | 19.5834 | 19.6088 | 19.6342 |                                       |
| 65   | 19.8120 | 19.8374 | 19.8628 | 19.8882 | 19.9136 | 19.9390 |                                       |
| 66   | 20.1168 | 20.1422 | 20.1676 | 20.1930 | 20.2184 | 20.2438 | 6 0.0095                              |
| 67   | 20.4216 | 20.4470 | 20.4724 | 20.4978 | 20.5232 | 20.5486 |                                       |
| 68   | 20.7264 | 20.7518 | 20.7772 | 20.8026 | 20.8280 | 20.8534 |                                       |
| 69   | 21.0312 | 21.0566 | 21.0820 | 21.1074 | 21.1328 | 21.1582 | 7 0.0111                              |
| 70   | 21.3360 | 21.3614 | 21.3868 | 21.4122 | 21.4376 | 21.4630 |                                       |
| 71   | 21.6408 | 21.6662 | 21.6916 | 21.7170 | 21.7424 | 21.7678 |                                       |
| 72   | 21.9456 | 21.9710 | 21.9964 | 22.0218 | 22.0472 | 22.0726 | 8 0.0127                              |
| 73   | 22.2504 | 22.2758 | 22.3012 | 22.3266 | 22.3520 | 22.3774 |                                       |
| 74   | 22.5552 | 22.5806 | 22.6060 | 22.6314 | 22.6568 | 22.6822 |                                       |
| 75   | 22.8600 | 22.8854 | 22.9108 | 22.9362 | 22.9616 | 22.9870 | 9 0.0143                              |
| 76   | 23.1648 | 23.1902 | 23.2156 | 23.2410 | 23.2664 | 23.2918 |                                       |
| 77   | 23.4696 | 23.4950 | 23.5204 | 23.5458 | 23.5712 | 23.5966 |                                       |
| 78   | 23.7744 | 23.7998 | 23.8252 | 23.8506 | 23.8760 | 23.9014 | 10 0.0159                             |
| 79   | 24.0792 | 24.1046 | 24.1300 | 24.1554 | 24.1808 | 24.2062 |                                       |
| 80   | 24.3840 | 24.4094 | 24.4348 | 24.4602 | 24.4856 | 24.5110 |                                       |
| 81   | 24.6888 | 24.7142 | 24.7396 | 24.7650 | 24.7904 | 24.8158 | 11 0.0175                             |
| 82   | 24.9936 | 25.0190 | 25.0444 | 25.0698 | 25.0952 | 25.1206 |                                       |
| 83   | 25.2984 | 25.3238 | 25.3492 | 25.3746 | 25.4000 | 25.4254 |                                       |
| 84   | 25.6032 | 25.6286 | 25.6540 | 25.6794 | 25.7048 | 25.7302 | 12 0.0190                             |
| 85   | 25.9080 | 25.9334 | 25.9588 | 25.9842 | 26.0096 | 26.0350 |                                       |
| 86   | 26.2128 | 26.2382 | 26.2636 | 26.2890 | 26.3144 | 26.3398 |                                       |
| 87   | 26.5176 | 26.5430 | 26.5684 | 26.5938 | 26.6192 | 26.6446 | 13 0.0206                             |
| 88   | 26.8224 | 26.8478 | 26.8732 | 26.8986 | 26.9240 | 26.9494 |                                       |
| 89   | 27.1272 | 27.1526 | 27.1780 | 27.2034 | 27.2288 | 27.2542 |                                       |
| 90   | 27.4320 | 27.4574 | 27.4828 | 27.5082 | 27.5336 | 27.5590 | 14 0.0222                             |
| 91   | 27.7368 | 27.7622 | 27.7876 | 27.8130 | 27.8384 | 27.8638 |                                       |
| 92   | 28.0416 | 28.0670 | 28.0924 | 28.1178 | 28.1432 | 28.1686 |                                       |
| 93   | 28.3464 | 28.3718 | 28.3972 | 28.4226 | 28.4480 | 28.4734 | 15 0.0238                             |
| 94   | 28.6512 | 28.6766 | 28.7020 | 28.7274 | 28.7528 | 28.7782 |                                       |
| 95   | 28.9560 | 28.9814 | 29.0068 | 29.0322 | 29.0576 | 29.0830 |                                       |
| 96   | 29.2608 | 29.2862 | 29.3116 | 29.3370 | 29.3624 | 29.3878 |                                       |
| 97   | 29.5656 | 29.5910 | 29.6164 | 29.6418 | 29.6672 | 29.6926 |                                       |
| 98   | 29.8704 | 29.8958 | 29.9212 | 29.9466 | 29.9720 | 29.9974 |                                       |
| 99   | 30.1752 | 30.2006 | 30.2260 | 30.2514 | 30.2768 | 30.3022 |                                       |
| 100  | 30.4800 |         |         |         |         |         |                                       |

Extract from B.S. 350 : 1944

**FEET AND INCHES TO METRES**

Based on 1 inch = 25.4 millimetres

Uncontracted values

| Feet | Inches  |         |         |         |         |         | Differences for sixteenths of an inch |        |
|------|---------|---------|---------|---------|---------|---------|---------------------------------------|--------|
|      | 6       | 7       | 8       | 9       | 10      | 11      |                                       |        |
|      | m.      | m.      | m.      | m.      | m.      | m.      |                                       | m.     |
| 50   | 15.3924 | 15.4178 | 15.4432 | 15.4686 | 15.4940 | 15.5194 |                                       |        |
| 51   | 15.6972 | 15.7226 | 15.7480 | 15.7734 | 15.7988 | 15.8242 |                                       |        |
| 52   | 16.0020 | 16.0274 | 16.0528 | 16.0782 | 16.1036 | 16.1290 | 1                                     | 0.0016 |
| 53   | 16.3068 | 16.3322 | 16.3576 | 16.3830 | 16.4084 | 16.4338 |                                       |        |
| 54   | 16.6116 | 16.6370 | 16.6624 | 16.6878 | 16.7132 | 16.7386 |                                       |        |
| 55   | 16.9164 | 16.9418 | 16.9672 | 16.9926 | 17.0180 | 17.0434 | 2                                     | 0.0032 |
| 56   | 17.2212 | 17.2466 | 17.2720 | 17.2974 | 17.3228 | 17.3482 |                                       |        |
| 57   | 17.5260 | 17.5514 | 17.5768 | 17.6022 | 17.6276 | 17.6530 |                                       |        |
| 58   | 17.8304 | 17.8561 | 17.8816 | 17.9070 | 17.9324 | 17.9578 | 3                                     | 0.0048 |
| 59   | 18.1356 | 18.1610 | 18.1864 | 18.2118 | 18.2372 | 18.2626 |                                       |        |
| 60   | 18.4404 | 18.4658 | 18.4912 | 18.5166 | 18.5420 | 18.5674 |                                       |        |
| 61   | 18.7452 | 18.7706 | 18.7960 | 18.8214 | 18.8468 | 18.8722 | 4                                     | 0.0064 |
| 62   | 19.0500 | 19.0754 | 19.1008 | 19.1262 | 19.1516 | 19.1770 |                                       |        |
| 63   | 19.3548 | 19.3802 | 19.4056 | 19.4310 | 19.4564 | 19.4818 |                                       |        |
| 64   | 19.6596 | 19.6850 | 19.7104 | 19.7358 | 19.7612 | 19.7866 | 5                                     | 0.0079 |
| 65   | 19.9644 | 19.9898 | 20.0152 | 20.0406 | 20.0660 | 20.0914 |                                       |        |
| 66   | 20.2692 | 20.2946 | 20.3200 | 20.3454 | 20.3708 | 20.3962 |                                       |        |
| 67   | 20.5740 | 20.5994 | 20.6248 | 20.6502 | 20.6756 | 20.7010 | 6                                     | 0.0095 |
| 68   | 20.8788 | 20.9042 | 20.9296 | 20.9550 | 20.9804 | 21.0058 |                                       |        |
| 69   | 21.1836 | 21.2090 | 21.2344 | 21.2598 | 21.2852 | 21.3106 |                                       |        |
| 70   | 21.4884 | 21.5138 | 21.5392 | 21.5646 | 21.5900 | 21.6154 | 7                                     | 0.0111 |
| 71   | 21.7932 | 21.8186 | 21.8440 | 21.8694 | 21.8948 | 21.9202 |                                       |        |
| 72   | 22.0980 | 22.1234 | 22.1488 | 22.1742 | 22.1996 | 22.2250 |                                       |        |
| 73   | 22.4028 | 22.4282 | 22.4536 | 22.4790 | 22.5044 | 22.5298 | 8                                     | 0.0127 |
| 74   | 22.7076 | 22.7330 | 22.7584 | 22.7838 | 22.8092 | 22.8346 |                                       |        |
| 75   | 23.0124 | 23.0378 | 23.0632 | 23.0886 | 23.1140 | 23.1394 |                                       |        |
| 76   | 23.3172 | 23.3426 | 23.3680 | 23.3934 | 23.4188 | 23.4442 | 9                                     | 0.0143 |
| 77   | 23.6220 | 23.6474 | 23.6728 | 23.6982 | 23.7236 | 23.7490 |                                       |        |
| 78   | 23.9268 | 23.9522 | 23.9776 | 24.0030 | 24.0284 | 24.0538 |                                       |        |
| 79   | 24.2316 | 24.2570 | 24.2824 | 24.3078 | 24.3332 | 24.3586 | 10                                    | 0.0159 |
| 80   | 24.5364 | 24.5618 | 24.5872 | 24.6126 | 24.6380 | 24.6634 |                                       |        |
| 81   | 24.8412 | 24.8666 | 24.8920 | 24.9174 | 24.9428 | 24.9682 |                                       |        |
| 82   | 25.1460 | 25.1714 | 25.1968 | 25.2222 | 25.2476 | 25.2730 | 11                                    | 0.0175 |
| 83   | 25.4508 | 25.4762 | 25.5016 | 25.5270 | 25.5524 | 25.5778 |                                       |        |
| 84   | 25.7556 | 25.7810 | 25.8064 | 25.8318 | 25.8572 | 25.8826 |                                       |        |
| 85   | 26.0604 | 26.0858 | 26.1112 | 26.1366 | 26.1620 | 26.1874 | 12                                    | 0.0190 |
| 86   | 26.3652 | 26.3906 | 26.4160 | 26.4414 | 26.4668 | 26.4922 |                                       |        |
| 87   | 26.6700 | 26.6954 | 26.7208 | 26.7462 | 26.7716 | 26.7970 |                                       |        |
| 88   | 26.9748 | 27.0002 | 27.0256 | 27.0510 | 27.0764 | 27.1018 | 13                                    | 0.0206 |
| 89   | 27.2796 | 27.3050 | 27.3304 | 27.3558 | 27.3812 | 27.4066 |                                       |        |
| 90   | 27.5844 | 27.6098 | 27.6352 | 27.6606 | 27.6860 | 27.7114 |                                       |        |
| 91   | 27.8892 | 27.9146 | 27.9400 | 27.9654 | 27.9908 | 28.0162 | 14                                    | 0.0222 |
| 92   | 28.1940 | 28.2194 | 28.2448 | 28.2702 | 28.2956 | 28.3210 |                                       |        |
| 93   | 28.4988 | 28.5242 | 28.5496 | 28.5750 | 28.6004 | 28.6258 |                                       |        |
| 94   | 28.8036 | 28.8290 | 28.8544 | 28.8798 | 28.9052 | 28.9306 | 15                                    | 0.0238 |
| 95   | 29.1084 | 29.1338 | 29.1592 | 29.1846 | 29.2100 | 29.2354 |                                       |        |
| 96   | 29.4132 | 29.4386 | 29.4640 | 29.4894 | 29.5148 | 29.5402 |                                       |        |
| 97   | 29.7180 | 29.7434 | 29.7688 | 29.7942 | 29.8196 | 29.8450 |                                       |        |
| 98   | 30.0228 | 30.0482 | 30.0736 | 30.0990 | 30.1244 | 30.1498 |                                       |        |
| 99   | 30.3276 | 30.3530 | 30.3784 | 30.4038 | 30.4292 | 30.4546 |                                       |        |

Extract from B.S. 350 : 1944

**SQUARE FEET TO SQUARE METRES**

Based on 1 inch = 25.4 millimetres

| Sq. ft. | 0               | 1               | 2               | 3               | 4               | 5               | 6               | 7               | 8               | 9               |
|---------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| —       | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> | m. <sup>2</sup> |
| —       | —               | 0.09290         | 0.18581         | 0.27871         | 0.37161         | 0.46452         | 0.55742         | 0.65032         | 0.74322         | 0.83613         |
| 10      | 0.92903         | 1.02193         | 1.11484         | 1.20774         | 1.30064         | 1.39355         | 1.48645         | 1.57935         | 1.67225         | 1.76516         |
| 20      | 1.85806         | 1.95096         | 2.04387         | 2.13677         | 2.22967         | 2.32258         | 2.41548         | 2.50838         | 2.60129         | 2.69419         |
| 30      | 2.78709         | 2.87999         | 2.97290         | 3.06580         | 3.15870         | 3.25161         | 3.34451         | 3.43741         | 3.53032         | 3.62322         |
| 40      | 3.71612         | 3.80902         | 3.90193         | 3.99483         | 4.08773         | 4.18064         | 4.27354         | 4.36644         | 4.45935         | 4.55225         |
| 50      | 4.64515         | 4.73806         | 4.83096         | 4.92386         | 5.01676         | 5.10967         | 5.20257         | 5.29547         | 5.38838         | 5.48128         |
| 60      | 5.5742          | 5.6671          | 5.7600          | 5.8529          | 5.9458          | 6.0387          | 6.1316          | 6.2245          | 6.3174          | 6.4103          |
| 70      | 6.5032          | 6.5961          | 6.6890          | 6.7819          | 6.8748          | 6.9677          | 7.0606          | 7.1535          | 7.2464          | 7.3393          |
| 80      | 7.4322          | 7.5251          | 7.6180          | 7.7110          | 7.8039          | 7.8968          | 7.9897          | 8.0826          | 8.1755          | 8.2684          |
| 90      | 8.3613          | 8.4542          | 8.5471          | 8.6400          | 8.7329          | 8.8258          | 8.9187          | 9.0116          | 9.1045          | 9.1974          |
| 100     | 9.2903          | 9.3832          | 9.4761          | 9.5690          | 9.6619          | 9.7548          | 9.8477          | 9.9406          | 10.0335         | 10.1264         |
| 10      | 10.2193         | 10.3122         | 10.4051         | 10.4980         | 10.5909         | 10.6838         | 10.7768         | 10.8697         | 10.9626         | 11.0555         |
| 20      | 11.1484         | 11.2413         | 11.3342         | 11.4271         | 11.5200         | 11.6129         | 11.7058         | 11.7987         | 11.8916         | 11.9845         |
| 30      | 12.0774         | 12.1703         | 12.2632         | 12.3561         | 12.4490         | 12.5419         | 12.6348         | 12.7277         | 12.8206         | 12.9135         |
| 40      | 13.0064         | 13.0993         | 13.1922         | 13.2851         | 13.3780         | 13.4709         | 13.5638         | 13.6567         | 13.7496         | 13.8426         |
| 50      | 13.9355         | 14.0284         | 14.1213         | 14.2142         | 14.3071         | 14.4000         | 14.4929         | 14.5858         | 14.6787         | 14.7716         |
| 60      | 14.8645         | 14.9574         | 15.0503         | 15.1432         | 15.2361         | 15.3290         | 15.4219         | 15.5148         | 15.6077         | 15.7006         |
| 70      | 15.7935         | 15.8864         | 15.9793         | 16.0722         | 16.1651         | 16.2580         | 16.3509         | 16.4438         | 16.5367         | 16.6296         |
| 80      | 16.7225         | 16.8155         | 16.9084         | 17.0013         | 17.0942         | 17.1871         | 17.2800         | 17.3729         | 17.4658         | 17.5587         |
| 90      | 17.6516         | 17.7445         | 17.8374         | 17.9303         | 18.0232         | 18.1161         | 18.2090         | 18.3019         | 18.3948         | 18.4877         |
| 200     | 18.5806         | 18.6735         | 18.7664         | 18.8593         | 18.9522         | 19.0451         | 19.1380         | 19.2309         | 19.3238         | 19.4167         |
| 10      | 19.5096         | 19.6025         | 19.6954         | 19.7883         | 19.8813         | 19.9742         | 20.0671         | 20.1600         | 20.2529         | 20.3458         |
| 20      | 20.4387         | 20.5316         | 20.6245         | 20.7174         | 20.8103         | 20.9032         | 20.9961         | 21.0890         | 21.1819         | 21.2748         |
| 30      | 21.3677         | 21.4606         | 21.5535         | 21.6464         | 21.7393         | 21.8322         | 21.9251         | 22.0180         | 22.1109         | 22.2038         |
| 40      | 22.2967         | 22.3896         | 22.4825         | 22.5754         | 22.6683         | 22.7612         | 22.8541         | 22.9471         | 23.0400         | 23.1329         |
| 50      | 23.2258         | 23.3187         | 23.4116         | 23.5045         | 23.5974         | 23.6903         | 23.7832         | 23.8761         | 23.9690         | 24.0619         |
| 60      | 24.1548         | 24.2477         | 24.3406         | 24.4335         | 24.5264         | 24.6193         | 24.7122         | 24.8051         | 24.8980         | 24.9909         |
| 70      | 25.0838         | 25.1767         | 25.2696         | 25.3625         | 25.4554         | 25.5483         | 25.6412         | 25.7341         | 25.8270         | 25.9199         |
| 80      | 26.0129         | 26.1058         | 26.1987         | 26.2916         | 26.3845         | 26.4774         | 26.5703         | 26.6632         | 26.7561         | 26.8490         |
| 90      | 26.9419         | 27.0348         | 27.1277         | 27.2206         | 27.3135         | 27.4064         | 27.4993         | 27.5922         | 27.6851         | 27.7780         |
| 300     | 27.8709         | 27.9638         | 28.0567         | 28.1496         | 28.2425         | 28.3354         | 28.4283         | 28.5212         | 28.6141         | 28.7070         |
| 10      | 28.7999         | 28.8928         | 28.9857         | 29.0787         | 29.1716         | 29.2645         | 29.3574         | 29.4503         | 29.5432         | 29.6361         |
| 20      | 29.7290         | 29.8219         | 29.9148         | 30.0077         | 30.1006         | 30.1935         | 30.2864         | 30.3793         | 30.4722         | 30.5651         |
| 30      | 30.6580         | 30.7509         | 30.8438         | 30.9367         | 31.0296         | 31.1225         | 31.2154         | 31.3083         | 31.4012         | 31.4941         |
| 40      | 31.5870         | 31.6799         | 31.7728         | 31.8657         | 31.9586         | 32.0515         | 32.1444         | 32.2373         | 32.3302         | 32.4231         |
| 50      | 32.5161         | 32.6090         | 32.7019         | 32.7948         | 32.8877         | 32.9806         | 33.0735         | 33.1664         | 33.2593         | 33.3522         |
| 60      | 33.4451         | 33.5380         | 33.6309         | 33.7238         | 33.8167         | 33.9096         | 34.0025         | 34.0954         | 34.1883         | 34.2812         |
| 70      | 34.3741         | 34.4670         | 34.5599         | 34.6528         | 34.7457         | 34.8386         | 34.9315         | 35.0244         | 35.1173         | 35.2103         |
| 80      | 35.3032         | 35.3961         | 35.4890         | 35.5819         | 35.6748         | 35.7677         | 35.8606         | 35.9535         | 36.0464         | 36.1393         |
| 90      | 36.2322         | 36.3251         | 36.4180         | 36.5109         | 36.6038         | 36.6967         | 36.7896         | 36.8825         | 36.9754         | 37.0683         |
| 400     | 37.1612         | 37.2541         | 37.3470         | 37.4399         | 37.5328         | 37.6257         | 37.7186         | 37.8115         | 37.9044         | 37.9973         |
| 10      | 38.0902         | 38.1831         | 38.2761         | 38.3690         | 38.4619         | 38.5548         | 38.6477         | 38.7406         | 38.8335         | 38.9264         |
| 20      | 39.0193         | 39.1122         | 39.2051         | 39.2980         | 39.3909         | 39.4838         | 39.5767         | 39.6696         | 39.7625         | 39.8554         |
| 30      | 39.9483         | 40.0412         | 40.1341         | 40.2270         | 40.3199         | 40.4128         | 40.5057         | 40.5986         | 40.6915         | 40.7844         |
| 40      | 40.8773         | 40.9702         | 41.0631         | 41.1560         | 41.2489         | 41.3418         | 41.4347         | 41.5276         | 41.6205         | 41.7134         |
| 50      | 41.8064         | 41.8993         | 41.9922         | 42.0851         | 42.1780         | 42.2709         | 42.3638         | 42.4567         | 42.5496         | 42.6425         |
| 60      | 42.7354         | 42.8283         | 42.9212         | 43.0141         | 43.1070         | 43.1999         | 43.2928         | 43.3857         | 43.4786         | 43.5715         |
| 70      | 43.6644         | 43.7573         | 43.8502         | 43.9431         | 44.0360         | 44.1289         | 44.2218         | 44.3147         | 44.4076         | 44.5005         |
| 80      | 44.5935         | 44.6864         | 44.7793         | 44.8722         | 44.9651         | 45.0580         | 45.1509         | 45.2438         | 45.3367         | 45.4296         |
| 90      | 45.5225         | 45.6154         | 45.7083         | 45.8012         | 45.8941         | 45.9870         | 46.0799         | 46.1728         | 46.2657         | 46.3586         |



Pressure, Stress: UK tons-force per square inch to meganewtons per square metre (newtons per square millimetre)  
 Basis: 1 UK ton = 2240 lb; 1 lbf = 0.453 592 37 kgf; 1 kgf = 9.806 65 N; 1 in = 0.0254 m.

| UK tonf/in <sup>2</sup> | 0                            | 0.1     | 0.2     | 0.3     | 0.4     | 0.5     | 0.6     | 0.7     | 0.8     | 0.9     |  |
|-------------------------|------------------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--|
|                         | meganewtons per square metre |         |         |         |         |         |         |         |         |         |  |
| 0                       | 0.00000                      | 1.54443 | 3.08885 | 4.63328 | 6.17770 | 7.72213 | 9.26655 | 10.8110 | 12.3554 | 13.8998 |  |
| 1                       | 15.4443                      | 16.9887 | 18.5331 | 20.0775 | 21.6220 | 23.1664 | 24.7108 | 26.2552 | 27.7997 | 29.3441 |  |
| 2                       | 30.8885                      | 32.4329 | 33.9774 | 35.5218 | 37.0662 | 38.6106 | 40.1551 | 41.6995 | 43.2439 | 44.7883 |  |
| 3                       | 46.3328                      | 47.8772 | 49.4216 | 50.9660 | 52.5105 | 54.0549 | 55.5993 | 57.1437 | 58.6882 | 60.2326 |  |
| 4                       | 61.7770                      | 63.3215 | 64.8659 | 66.4103 | 67.9547 | 69.4992 | 71.0436 | 72.5880 | 74.1324 | 75.6769 |  |
| 5                       | 77.2213                      | 78.7657 | 80.3101 | 81.8546 | 83.3990 | 84.9434 | 86.4878 | 88.0323 | 89.5767 | 91.1211 |  |
| 6                       | 92.6655                      | 94.2100 | 95.7544 | 97.2988 | 98.8432 | 100.388 | 101.932 | 103.477 | 105.021 | 106.565 |  |
| 7                       | 108.110                      | 109.654 | 111.199 | 112.743 | 114.287 | 115.832 | 117.376 | 118.921 | 120.465 | 122.010 |  |
| 8                       | 123.554                      | 125.098 | 126.643 | 128.187 | 129.732 | 131.276 | 132.821 | 134.365 | 135.909 | 137.454 |  |
| 9                       | 138.998                      | 140.543 | 142.087 | 143.632 | 145.176 | 146.720 | 148.265 | 149.809 | 151.354 | 152.898 |  |
| 10                      | 154.443                      | 155.987 | 157.531 | 159.076 | 160.620 | 162.165 | 163.709 | 165.254 | 166.798 | 168.342 |  |
| 11                      | 169.887                      | 171.431 | 172.976 | 174.520 | 176.065 | 177.609 | 179.153 | 180.698 | 182.242 | 183.787 |  |
| 12                      | 185.331                      | 186.876 | 188.420 | 189.964 | 191.509 | 193.053 | 194.598 | 196.142 | 197.686 | 199.231 |  |
| 13                      | 200.775                      | 202.320 | 203.864 | 205.409 | 206.953 | 208.497 | 210.042 | 211.586 | 213.131 | 214.675 |  |
| 14                      | 216.220                      | 217.764 | 219.308 | 220.853 | 222.397 | 223.942 | 225.486 | 227.031 | 228.575 | 230.119 |  |
| 15                      | 231.664                      | 233.208 | 234.753 | 236.297 | 237.842 | 239.386 | 240.930 | 242.475 | 244.019 | 245.564 |  |
| 16                      | 247.108                      | 248.653 | 250.197 | 251.741 | 253.286 | 254.830 | 256.375 | 257.919 | 259.464 | 261.008 |  |
| 17                      | 262.552                      | 264.097 | 265.641 | 267.186 | 268.730 | 270.274 | 271.819 | 273.363 | 274.908 | 276.452 |  |
| 18                      | 277.997                      | 279.541 | 281.085 | 282.630 | 284.174 | 285.719 | 287.263 | 288.808 | 290.352 | 291.896 |  |
| 19                      | 293.441                      | 294.985 | 296.530 | 298.074 | 299.619 | 301.163 | 302.707 | 304.252 | 305.796 | 307.341 |  |
| 20                      | 308.885                      | 310.430 | 311.974 | 313.518 | 315.063 | 316.607 | 318.152 | 319.696 | 321.241 | 322.785 |  |
| 21                      | 324.329                      | 325.874 | 327.418 | 328.963 | 330.507 | 332.052 | 333.596 | 335.140 | 336.685 | 338.229 |  |
| 22                      | 339.774                      | 341.318 | 342.862 | 344.407 | 345.951 | 347.496 | 349.040 | 350.585 | 352.129 | 353.673 |  |
| 23                      | 355.218                      | 356.762 | 358.307 | 359.851 | 361.396 | 362.940 | 364.484 | 366.029 | 367.573 | 369.118 |  |
| 24                      | 370.662                      | 372.207 | 373.751 | 375.295 | 376.840 | 378.384 | 379.929 | 381.473 | 383.018 | 384.562 |  |

Supplement No. 1 (1967) to  
 B.S. 350 : Part 2 : 1962

Pressure, Stress: UK tons-force per square inch to meganewtons per square metre  
 Basis: 1 UK ton = 2240 lb; 1 lbf = 0.453 592 37 kgf; 1 kgf = 9.806 65 N; 1 in = 0.0254 m.

| UK<br>tonf/in <sup>2</sup>   | 0       | 0.1     | 0.2     | 0.3     | 0.4     | 0.5     | 0.6     | 0.7     | 0.8     | 0.9     |
|------------------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| meganewtons per square metre |         |         |         |         |         |         |         |         |         |         |
| 25                           | 386.106 | 387.651 | 389.195 | 390.740 | 392.284 | 393.829 | 395.373 | 396.917 | 398.462 | 400.006 |
| 26                           | 401.551 | 403.095 | 404.640 | 406.184 | 407.728 | 409.273 | 410.817 | 412.362 | 413.906 | 415.450 |
| 27                           | 416.995 | 418.539 | 420.084 | 421.628 | 423.173 | 424.717 | 426.261 | 427.806 | 429.350 | 430.895 |
| 28                           | 432.439 | 433.984 | 435.528 | 437.072 | 438.617 | 440.161 | 441.706 | 443.250 | 444.795 | 446.339 |
| 29                           | 447.883 | 449.428 | 450.972 | 452.517 | 454.061 | 455.606 | 457.150 | 458.694 | 460.239 | 461.783 |
| 30                           | 463.328 | 464.872 | 466.417 | 467.961 | 469.505 | 471.050 | 472.594 | 474.139 | 475.683 | 477.228 |
| 31                           | 478.772 | 480.316 | 481.861 | 483.405 | 484.950 | 486.494 | 488.039 | 489.583 | 491.127 | 492.672 |
| 32                           | 494.216 | 495.761 | 497.305 | 498.849 | 500.394 | 501.938 | 503.483 | 505.027 | 506.572 | 508.116 |
| 33                           | 509.660 | 511.205 | 512.749 | 514.294 | 515.838 | 517.383 | 518.927 | 520.471 | 522.016 | 523.560 |
| 34                           | 525.105 | 526.649 | 528.194 | 529.738 | 531.282 | 532.827 | 534.371 | 535.916 | 537.460 | 539.005 |
| 35                           | 540.549 | 542.093 | 543.638 | 545.182 | 546.727 | 548.271 | 549.816 | 551.360 | 552.904 | 554.449 |
| 36                           | 555.993 | 557.538 | 559.082 | 560.627 | 562.171 | 563.715 | 565.260 | 566.804 | 568.349 | 569.893 |
| 37                           | 571.437 | 572.982 | 574.526 | 576.071 | 577.615 | 579.160 | 580.704 | 582.248 | 583.793 | 585.337 |
| 38                           | 586.882 | 588.426 | 589.971 | 591.515 | 593.059 | 594.604 | 596.148 | 597.693 | 599.237 | 600.782 |
| 39                           | 602.326 | 603.870 | 605.415 | 606.959 | 608.504 | 610.048 | 611.593 | 613.137 | 614.681 | 616.226 |
| 40                           | 617.770 | 619.315 | 620.859 | 622.404 | 623.948 | 625.492 | 627.037 | 628.581 | 630.126 | 631.670 |
| 41                           | 633.215 | 634.759 | 636.303 | 637.848 | 639.392 | 640.937 | 642.481 | 644.025 | 645.570 | 647.114 |
| 42                           | 648.659 | 650.203 | 651.748 | 653.292 | 654.836 | 656.381 | 657.925 | 659.470 | 661.014 | 662.559 |
| 43                           | 664.103 | 665.647 | 667.192 | 668.736 | 670.281 | 671.825 | 673.370 | 674.914 | 676.458 | 678.003 |
| 44                           | 679.547 | 681.092 | 682.636 | 684.181 | 685.725 | 687.269 | 688.814 | 690.358 | 691.903 | 693.447 |
| 45                           | 694.992 | 696.536 | 698.080 | 699.625 | 701.169 | 702.714 | 704.258 | 705.803 | 707.347 | 708.891 |
| 46                           | 710.436 | 711.980 | 713.525 | 715.069 | 716.613 | 718.158 | 719.702 | 721.247 | 722.791 | 724.336 |
| 47                           | 725.880 | 727.424 | 728.969 | 730.513 | 732.058 | 733.602 | 735.147 | 736.691 | 738.235 | 739.780 |
| 48                           | 741.324 | 742.869 | 744.413 | 745.958 | 747.502 | 749.046 | 750.591 | 752.135 | 753.680 | 755.224 |
| 49                           | 756.769 | 758.313 | 759.857 | 761.402 | 762.946 | 764.491 | 766.035 | 767.580 | 769.124 | 770.668 |



## Pressure, stress:

UK tons-force per square inch to meganewtons per square metre

| UK<br>tonf/in <sup>2</sup> | 0                            | 0.1     | 0.2     | 0.3     | 0.4     | 0.5     | 0.6     | 0.7     | 0.8     | 0.9     |
|----------------------------|------------------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
|                            | meganewtons per square metre |         |         |         |         |         |         |         |         |         |
| 50                         | 772.213                      | 773.757 | 775.302 | 776.846 | 778.391 | 779.935 | 781.479 | 783.024 | 784.568 | 786.113 |
| 51                         | 787.657                      | 789.201 | 790.746 | 792.290 | 793.835 | 795.379 | 796.924 | 798.468 | 800.012 | 801.557 |
| 52                         | 803.101                      | 804.646 | 806.190 | 807.735 | 809.279 | 810.823 | 812.368 | 813.912 | 815.457 | 817.001 |
| 53                         | 818.546                      | 820.090 | 821.634 | 823.179 | 824.723 | 826.268 | 827.812 | 829.357 | 830.901 | 832.445 |
| 54                         | 833.990                      | 835.534 | 837.079 | 838.623 | 840.168 | 841.712 | 843.256 | 844.801 | 846.345 | 847.890 |
| 55                         | 849.434                      | 850.979 | 852.523 | 854.067 | 855.612 | 857.156 | 858.701 | 860.245 | 861.790 | 863.334 |
| 56                         | 864.878                      | 866.423 | 867.967 | 869.512 | 871.056 | 872.600 | 874.145 | 875.689 | 877.234 | 878.778 |
| 57                         | 880.323                      | 881.867 | 883.411 | 884.956 | 886.500 | 888.045 | 889.589 | 891.134 | 892.678 | 894.222 |
| 58                         | 895.767                      | 897.311 | 898.856 | 900.400 | 901.945 | 903.489 | 905.033 | 906.578 | 908.122 | 909.667 |
| 59                         | 911.211                      | 912.756 | 914.300 | 915.844 | 917.389 | 918.933 | 920.478 | 922.022 | 923.567 | 925.111 |
| 60                         | 926.655                      | 928.200 | 929.744 | 931.289 | 932.833 | 934.378 | 935.922 | 937.466 | 939.011 | 940.555 |
| 61                         | 942.100                      | 943.644 | 945.188 | 946.733 | 948.277 | 949.822 | 951.366 | 952.911 | 954.455 | 955.999 |
| 62                         | 957.544                      | 959.088 | 960.633 | 962.177 | 963.722 | 965.266 | 966.810 | 968.355 | 969.899 | 971.444 |
| 63                         | 972.988                      | 974.533 | 976.077 | 977.621 | 979.166 | 980.710 | 982.255 | 983.799 | 985.344 | 986.888 |
| 64                         | 988.432                      | 989.977 | 991.521 | 993.066 | 994.610 | 996.155 | 997.699 | 999.243 | 1000.79 | 1002.33 |
| 65                         | 1003.88                      | 1005.42 | 1006.97 | 1008.51 | 1010.05 | 1011.60 | 1013.14 | 1014.69 | 1016.23 | 1017.78 |
| 66                         | 1019.32                      | 1020.87 | 1022.41 | 1023.95 | 1025.50 | 1027.04 | 1028.59 | 1030.13 | 1031.68 | 1033.22 |
| 67                         | 1034.77                      | 1036.31 | 1037.85 | 1039.40 | 1040.94 | 1042.49 | 1044.03 | 1045.58 | 1047.12 | 1048.67 |
| 68                         | 1050.21                      | 1051.75 | 1053.30 | 1054.84 | 1056.39 | 1057.93 | 1059.48 | 1061.02 | 1062.56 | 1064.11 |
| 69                         | 1065.65                      | 1067.20 | 1068.74 | 1070.29 | 1071.83 | 1073.38 | 1074.92 | 1076.46 | 1078.01 | 1079.55 |
| 70                         | 1081.10                      | 1082.64 | 1084.19 | 1085.73 | 1087.28 | 1088.82 | 1090.36 | 1091.91 | 1093.45 | 1095.00 |
| 71                         | 1096.54                      | 1098.09 | 1099.63 | 1101.18 | 1102.72 | 1104.26 | 1105.81 | 1107.35 | 1108.90 | 1110.44 |
| 72                         | 1111.99                      | 1113.53 | 1115.08 | 1116.62 | 1118.16 | 1119.71 | 1121.25 | 1122.80 | 1124.34 | 1125.89 |
| 73                         | 1127.43                      | 1128.98 | 1130.52 | 1132.06 | 1133.61 | 1135.15 | 1136.70 | 1138.24 | 1139.79 | 1141.33 |
| 74                         | 1142.87                      | 1144.42 | 1145.96 | 1147.51 | 1149.05 | 1150.60 | 1152.14 | 1153.69 | 1155.23 | 1156.77 |



## **British Standards covering the design and construction of steelwork**

A basic list of British Standards covering the design and construction of steelwork is given.

*Note* Dates in parentheses indicate that the British Standard has been reviewed at that date.

### **Bolts**

- BS 3692 1967 Specification for ISO metric precision hexagon bolts, screws and nuts. Metric units.
- BS 4190 1967 Specification for ISO metric black hexagon bolts, screws and nuts. Metric units.
- BS 4395 Specification for high strength friction grip bolts and associated nuts and washers for structural engineering. Metric series.
  - Part 1: 1969 General grade
  - Part 2: 1969 Higher grade bolts and nuts and general grade washers
- BS 4604 Specification for the use of high strength friction grip bolts in structural steelwork. Metric series.
  - Part 1: 1970 General grade
  - Part 2: 1970 Higher grade (parallel shank)

### **Corrosion**

- BS 1501 Steels for pressure purposes: plates, sheet and strip
  - Part 3: 1990 Specification for corrosion and heat-resisting steels
- BS 5493 1977 Code of practice for protective coating of iron and steel structures against corrosion
- BS 7079 Preparation of steel substrates before application of paints and related products
  - Part 0: 1990 Introduction
  - Part A1: 1989 Specification for rust grades and preparation grades of uncoated steel substrates after overall removal of previous coatings
  - Part A1: Supplement 1: 1989 Representative photographic examples of the change of appearance when blast-cleaned with different abrasives

## **Design**

- BS 449 Specification for the use of structural steel in building  
Part 2: 1969 Metric units
- BS 2573 Rules for the design of cranes  
Part 1: 1983 Specification for classification, stress calculations and design criteria for structures
- BS 2853 1957 Specification for the design and testing of steel overhead runway beams
- BS 5400 Steel, concrete and composite bridges  
Part 1: 1988 General statement  
Part 3: 1982 Code of practice for design of steel bridges  
Part 4: 1990 Code of practice for design of concrete bridges  
Part 5: 1979 Code of practice for design of composite bridges  
Part 6: 1980 Specification for materials and workmanship: steel  
Part 9: Section 9.1: 1983 Code of practice for design of bridge bearings  
Part 9: Section 9.2: 1983 Specification for materials, manufacture and installation of bridge bearings  
Part 10: 1980 Code of practice for fatigue
- BS 5502 Code of practice for the design of buildings and structures for agriculture  
Part 1: Section 1.1: 1986 Materials  
Part 22: 1987 Code of practice for design, construction and loading
- BS 5950 Structural use of steelwork in building  
Part 1: 1990 Code of practice for design in simple and continuous construction: hot rolled sections  
Part 2: 1985 Specification for materials fabrication and erection: hot rolled sections  
Part 3: Section 3.1: 1990 Code of practice for design of simple and continuous composite beams  
Part 4: 1982 Code of practice for design of floors with profiled steel sheeting  
Part 5: 1987 Code of practice for design of cold formed sections  
Part 6: Code of practice for design of light gauge sheeting, decking and cladding (in preparation)  
Part 7: Specification for materials and workmanship: cold formed sections and sheeting

## **Erection**

- BS 5531 1988 Code of practice for safety in erecting structural frames

## **Fire**

- BS 476 Fire tests on building materials and structures  
Part 20: 1987 Methods for determination of the fire resistance of elements of construction (general principles)  
Part 21: 1987 Methods for determination of the fire resistance of load-bearing elements of construction
- BS 5950 Structural use of steelwork in building  
Part 8: 1990 Code of practice for fire resistant design

## **Loading**

- BS 648 1964: Schedule of weights of building materials
- BS 5400 Steel, concrete and composite bridges  
Part 2: 1978 Specification for loads
- BS 6399 Loading for buildings  
Part 1: 1984 Code of practice for dead and imposed loads  
Part 2: Code of practice for wind loading (to be published and will replace CP3: Chapter V: Part 2)  
Part 3: 1988 Code of practice for imposed roof loads
- CP3 Code of basic data for the design of buildings  
Chapter V: Part 2: 1972 Wind loads

## **Steel**

- BS 4 Structural steel sections  
Part 1: 1980 Specification for hot rolled sections
- BS 970 Part 1: 1991 General inspection and testing procedures and specific requirements for carbon, carbon-manganese, alloy and stainless steels
- BS 1449 Steel plate, sheet and strip  
Part 1: 1983 Specification for carbon and carbon-manganese plate, sheet and strip  
Part 2: 1983 Specification for stainless and heat-resisting steel plate, sheet and strip
- BS 2989 1982 Specification for continuously hot-dip zinc coated and iron-zinc alloy coated steel: wide strip, sheet/plate and slit wide strip

- BS 2994 1976 (1987) Specification for cold rolled steel sections
- BS 4360 1990 Specification for weldable structural steels
- BS 4848 Specification for hot-rolled structural steel sections
  - Part 2: 1975 Hollow sections
  - Part 4: 1972 (1986) Equal and unequal angles
  - Part 5: 1980 Bulb flats
- BS 6363 1983 Specification for welded cold formed steel structural hollow sections
- BS 7191 1989 Specification for weldable structural steels for fixed offshore structures
- BS EN 10 025 1990 Specification for hot rolled products of non-alloy structural steels and their technical delivery conditions

## **Welding**

- BS 499 Welding terms and symbols
  - Part 1: 1983 Glossary for welding, brazing and thermal cutting
  - Part 2: 1980 (1989) Specification for symbols for welding
  - Part 2C: 1980 Welding symbols
- BS 639 1986 Specification for covered carbon and carbon manganese steel electrodes for manual metal-arc welding
- BS 4165 1984 Specification for electrode wires and fluxes for the submerged arc welding of carbon steel and medium-tensile steel
- BS 4870 Specification for approval testing of welding procedures
  - Part 1: 1981 Fusion welding of steel
- BS 4871 Specification for approval testing of welders working to approved welding procedures
  - Part 1: 1982 Fusion welding of steel
- BS 4872 Specification for approval testing of welders when welding procedure approval is not required
  - Part 1: 1982 Fusion welding of steel
- BS 5135 1984 Specification for arc welding of carbon and carbon manganese steels
- BS 7084 1989 Specification for carbon and carbon manganese steel tubular cored welding electrodes

**Weld testing**

- BS 2600 Radiographic examination of fusion welded butt joints in steel  
Part 1: 1983 Methods for steel 2 mm up to and including 50 mm thick  
Part 2: 1973 Methods for steel over 50 mm thick up to and including 200 mm thick
- BS 2910 1986 Methods for radiographic examination of fusion welded circumferential butt joints in steel pipes
- BS 3923 Methods for ultrasonic examination of welds  
Part 1: 1986 Methods for manual examination of fusion welds in ferritic steels
- BS 5289 1976 (1983) Code of practice. Visual inspection of fusion welded joints.

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